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# Validation Study of the Multi-Fidelity Toolkit in SPARC

Compressible fluid dynamics at multiple physics fidelities

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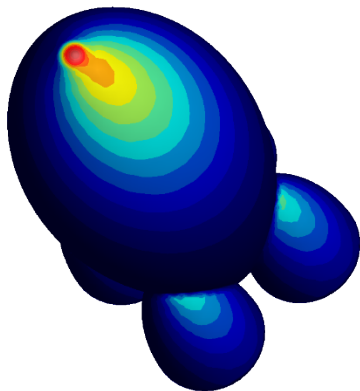


# The Multi-Fidelity Toolkit (MFTK) is implemented in SPARC, developed by Sandia National Laboratories, to solve compressible fluid dynamics

- Developed as efficient aerodynamic table generator for hypersonic vehicle analysis
- Has three levels of physics fidelity
  - High: Reynolds-Averaged Navier—Stokes (RANS)
  - Medium: Euler + Momentum/Energy Integral Technique (Euler+MEIT)
  - Low: modified Newtonian aero + flat-plate boundary layer model (MNA+FPBL)

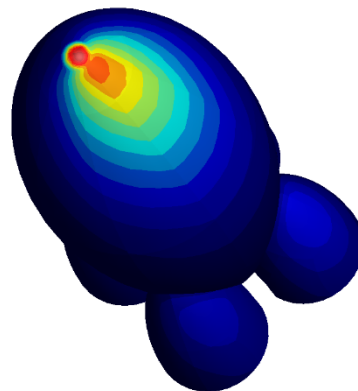
Rocket ship example at angle of attack of  $16^\circ$ , yaw of  $8^\circ$ , Mach 15, altitude 20 km

Pressure (Pa): 100000 400000 700000 1E+06 1.3E+06



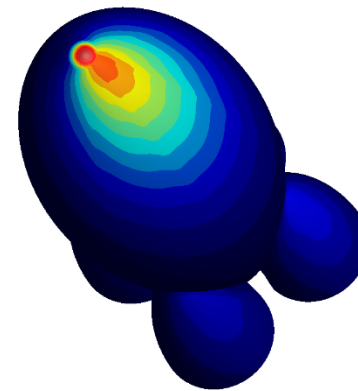
Modified Newtonian Aero  
Runtime ~10 seconds, 1 core

Pressure (Pa): 100000 400000 700000 1E+06 1.3E+06



Euler  
Runtime ~10 minutes, 8 cores

Pressure (Pa): 100000 400000 700000 1E+06 1.3E+06



RANS  
Runtime ~100 minutes, 288 cores





# Model validation is the process of determining the predictive accuracy of physics codes

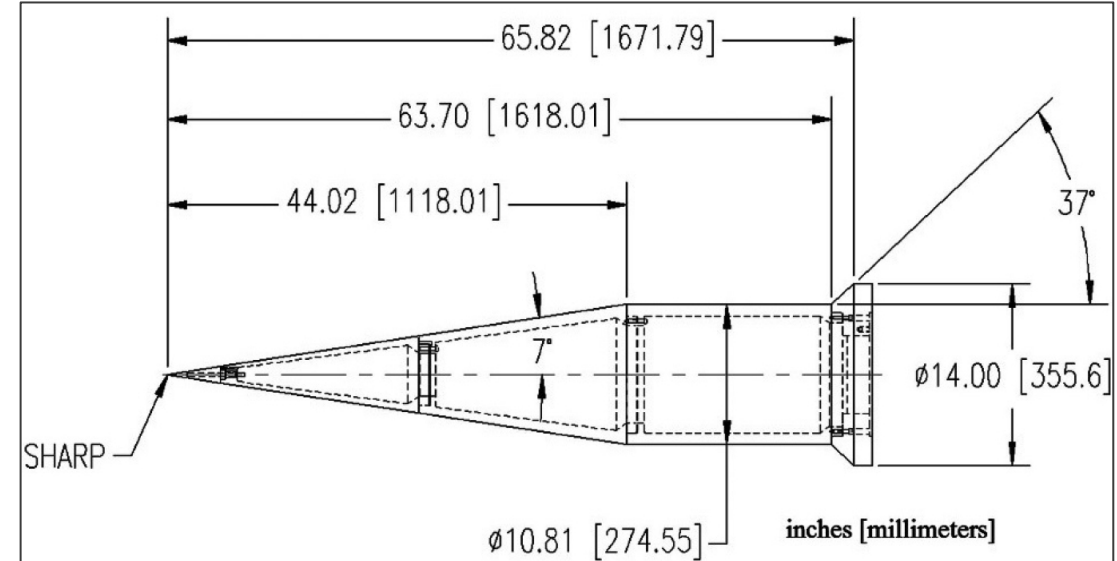
- Validation: “The process of determining the degree to which a model is an accurate representation of the real world from the perspective of the intended uses of the model”
- Validation Error
  - $E = S - D$
  - $S$  is a simulation result
  - $D$  is experimental data
- Validation Uncertainty
  - $u_{\text{val}} = \sqrt{u_{\text{num}}^2 + u_{\text{input}}^2 + u_D^2}$
  - $u_{\text{num}}$  is numerical uncertainty
  - $u_{\text{input}}$  is input uncertainty propagated through model
  - $u_D$  is the experimental data uncertainty





# HIFiRE-1 wind tunnel tests provide high quality, hypersonic validation data on a complex vehicle

- Geometry has
  - Laminar cone
  - Turbulent cone
  - Cylinder
  - Flare
- High quality and spatial resolution pressure and heat flux measurements
- This study used Run 30
  - $M = 7.19$
  - $\alpha = 0^\circ$
- Validation studies of other runs with angles of attack and different Reynolds numbers are planned



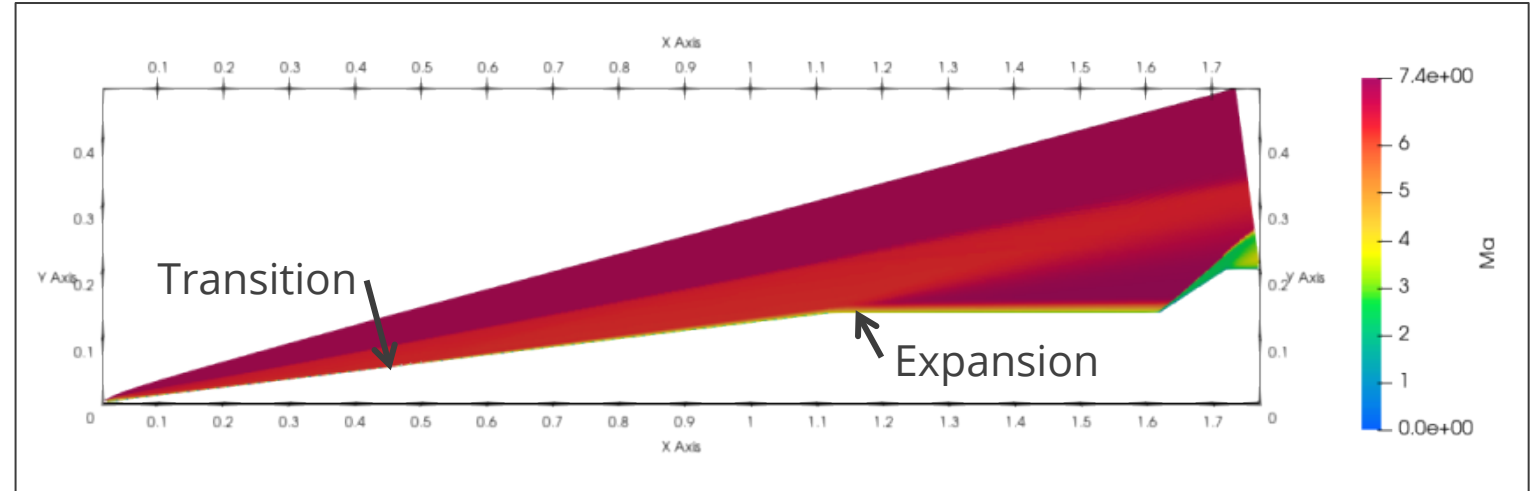
The HIFiRE-1 wind tunnel test geometry that shows the forecone on the left, the cylindrical section in the center, and the flare on the right; from Wadhams 2008. The text states that the final nosetip was changed from sharp to a radius of 2.5 mm and the flare angle was changed from 37° to 33°.



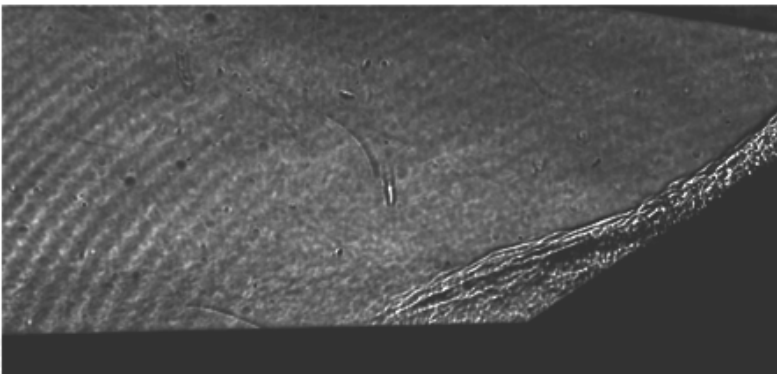
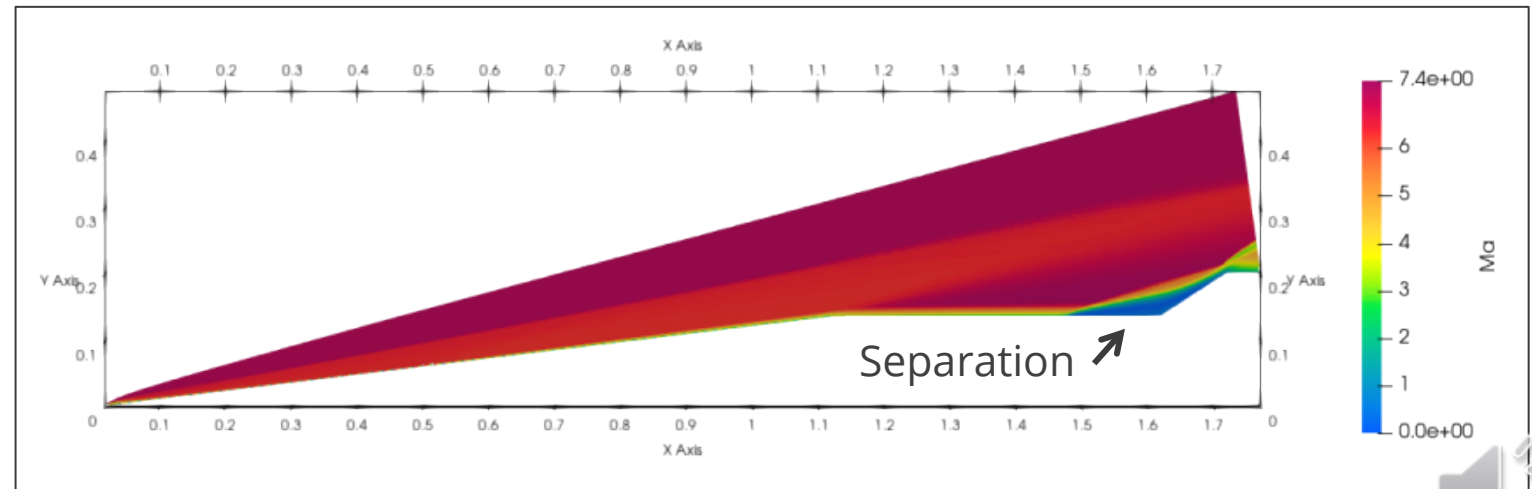
# The flow includes a separation region near the cylinder-flare intersection that is a challenge

RANS Spalart—Allmaras (SA)

- Like the findings of HIFiRE-1 modelers (see MacLean 2008)
  - The SA prediction has negligible separation at the cylinder-flare intersection
  - The SST prediction has sizeable separation (larger than experiment)



RANS Shear Stress Transport (SST)



Measured separation from Schlieren imaging, from MacLean 2008

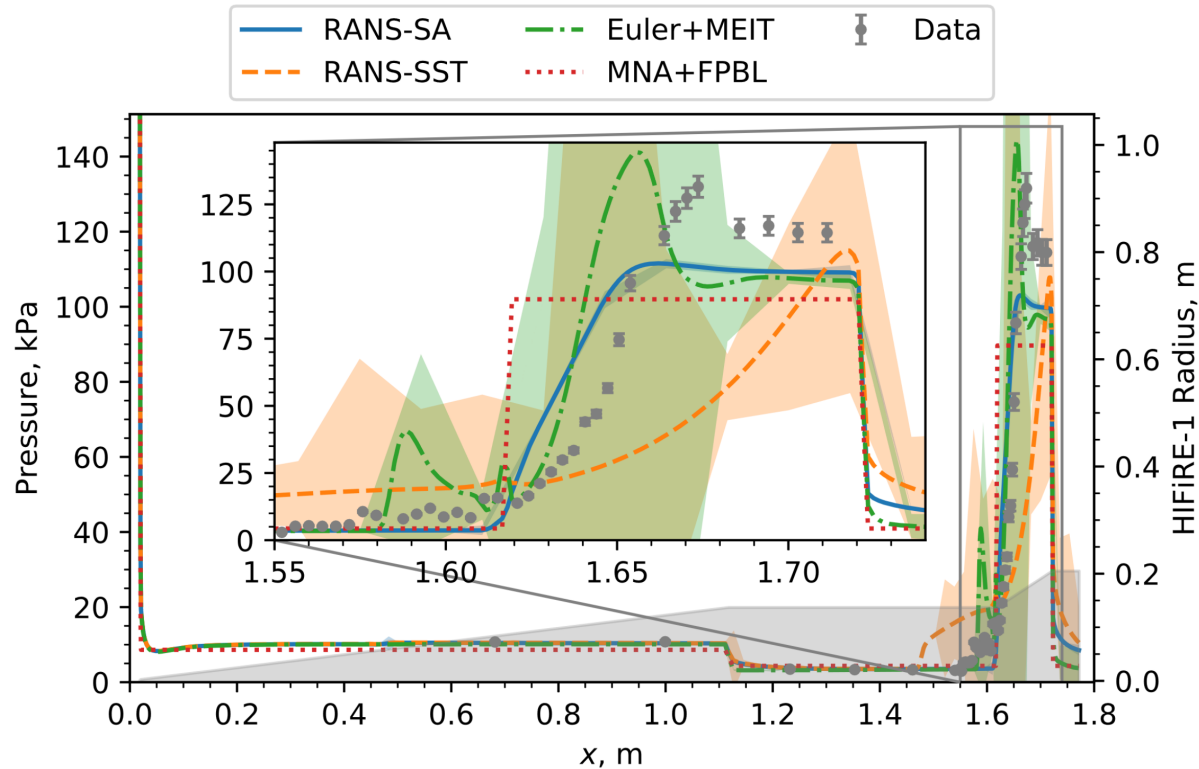




# Surface pressure validation comparisons along axis

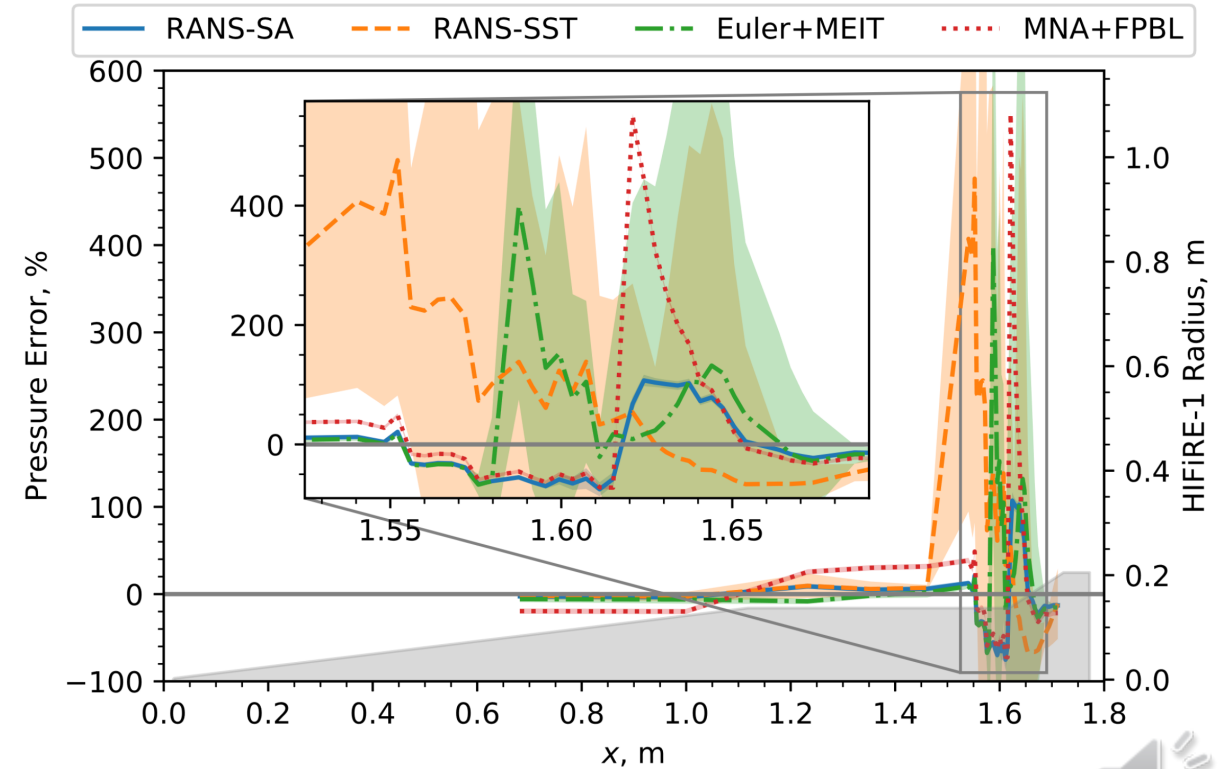
## Nominal Results

- Four model predictions with numerical uncertainty
  - Uncertainty from grid convergence study, see Krueger MFTK verification 2022 SciTech paper
- Experimental data points with uncertainty



## Error Results ( $E = S - D$ )

- Error is relative to measurements
- Each model has its own error curve
- Validation uncertainty  $u_{val}$  shown on error plots
  - $u_{input}$  not calculated in this work



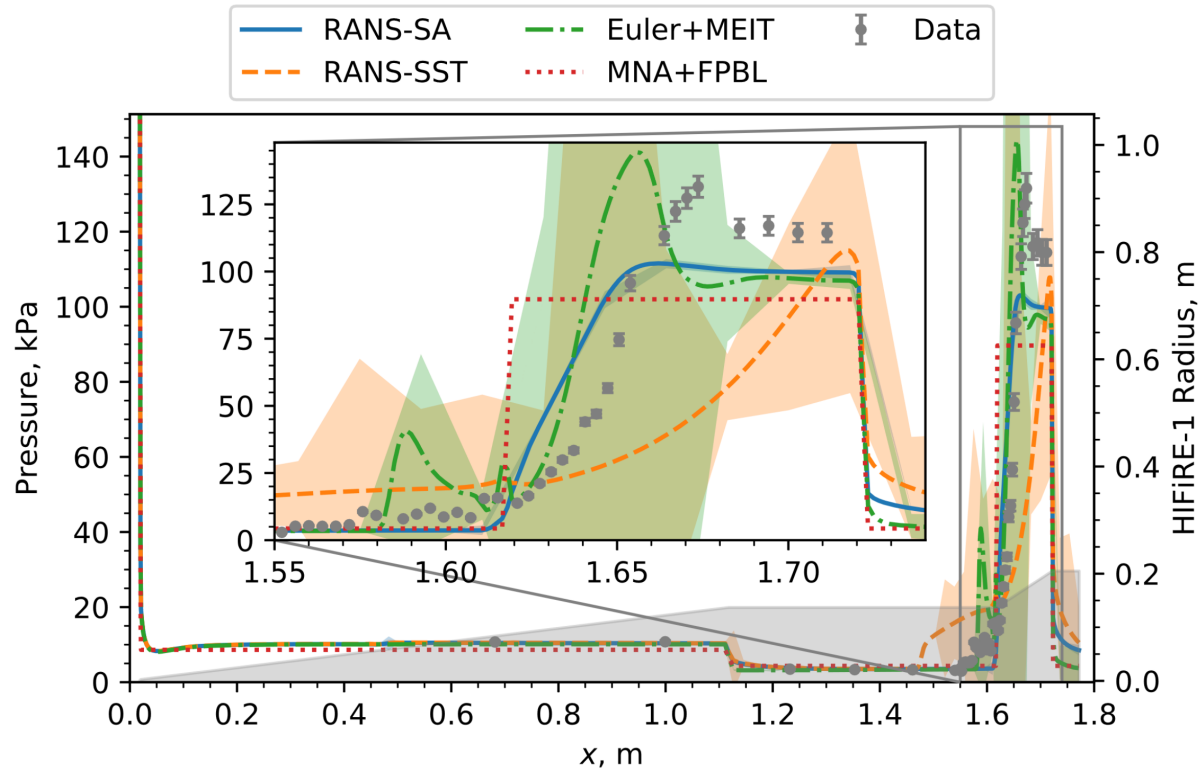
- HIFiRE-1 geometry is shaded gray



# Surface pressure validation comparisons along axis

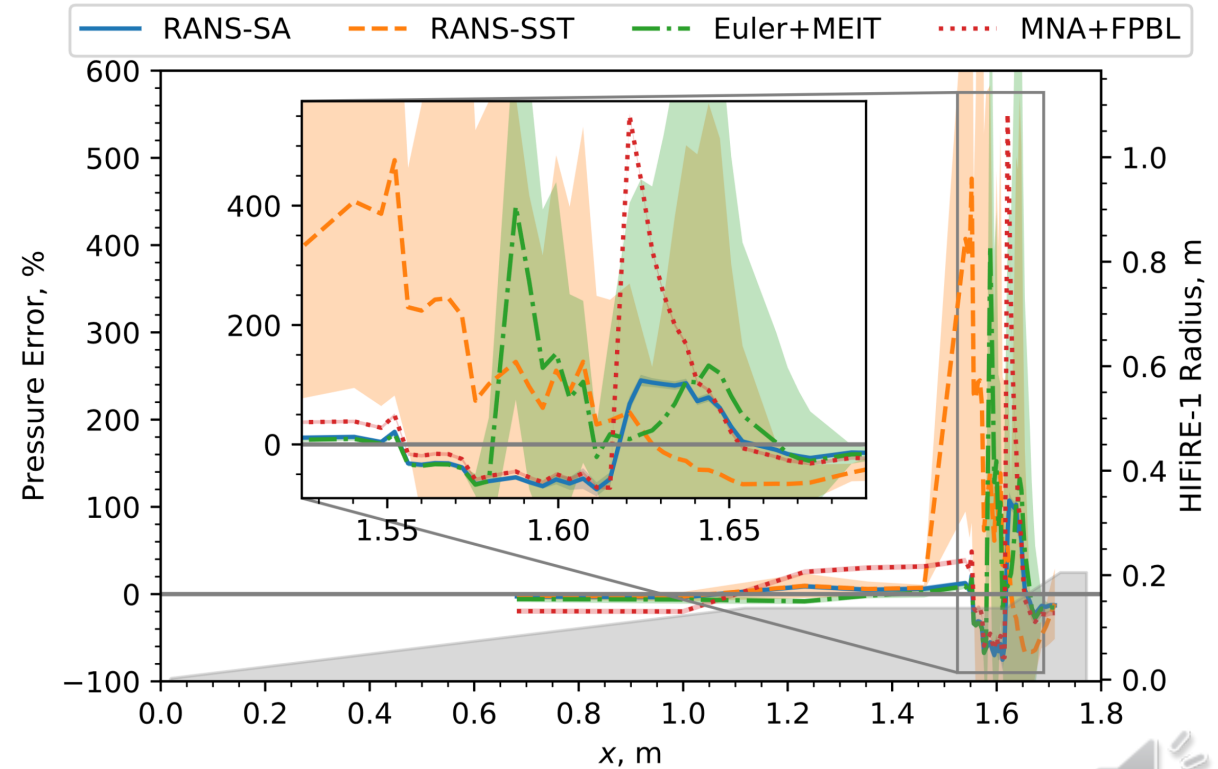
## Nominal Results

- Agreement is very good in cone and cylinder sections
  - More challenging near separation
- RANS-SA and Euler+MEIT capture separation behavior best



## Error Results

- Validation uncertainty is large for RANS-SST and Euler+MEIT
  - Driven by numerical uncertainty
- Error in cone and cylinder upstream of separation below 40%

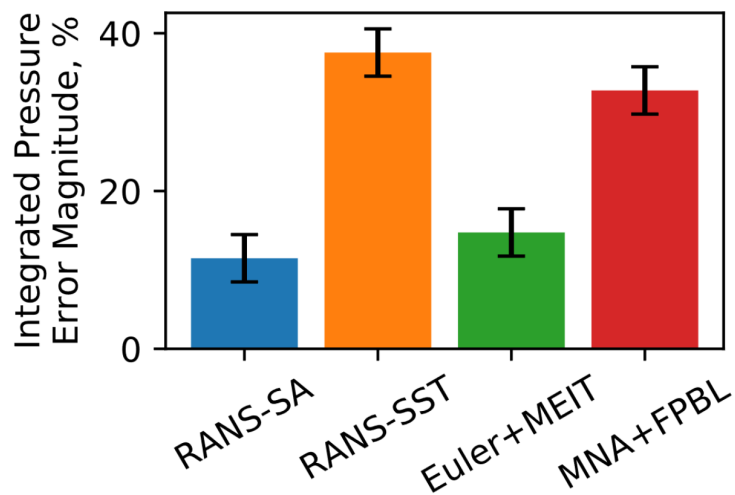




# Surface pressure validation error integrated over space

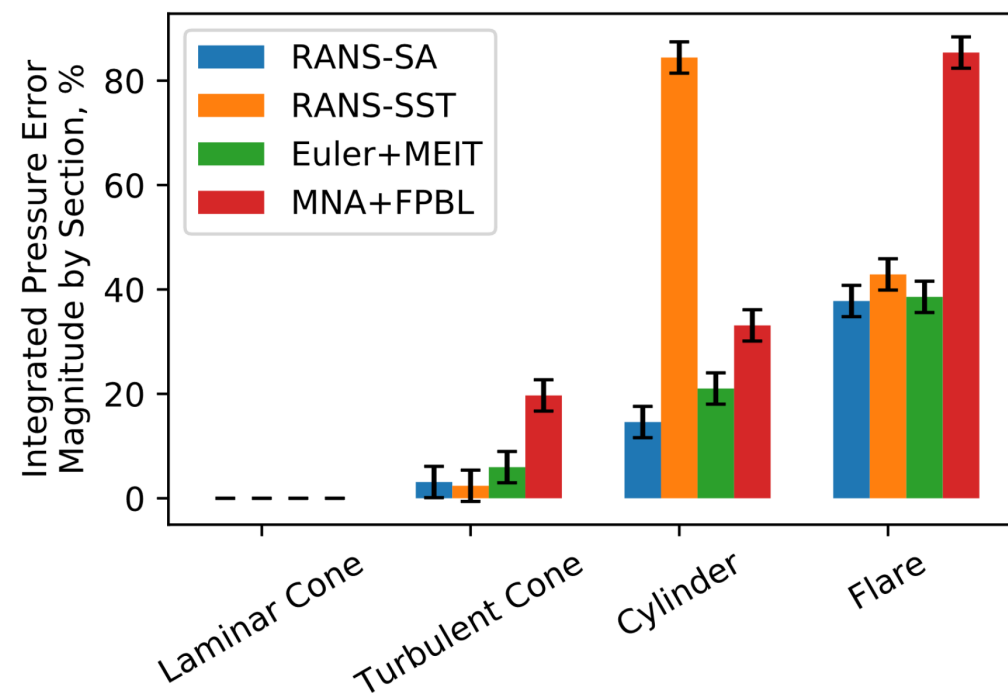
The validation error magnitude  $|E|$  is normalized by experimental data and integrated over all space

- RANS-SA is most accurate, followed by Euler+MEIT
- RANS-SST predicts much larger separation region than measured
- Uncertainty bands (error bars) showing only experimental uncertainty (3%)



The validation error magnitude  $|E|$  is normalized by experimental data and integrated within each section

- No pressure data for laminar cone section
- The three higher-fidelity models are much more accurate in the turbulent cone and flare sections
- The RANS-SST error is quite large in the cylindrical section



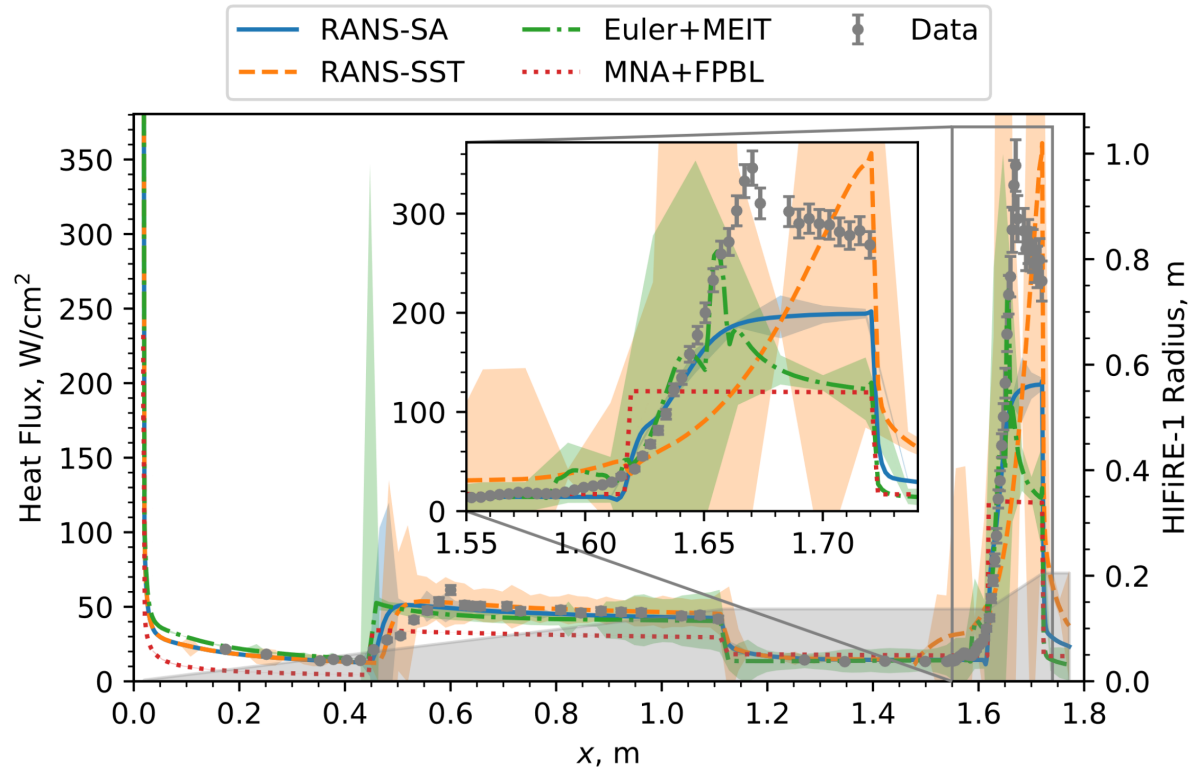




# Surface heat flux validation comparisons along axis

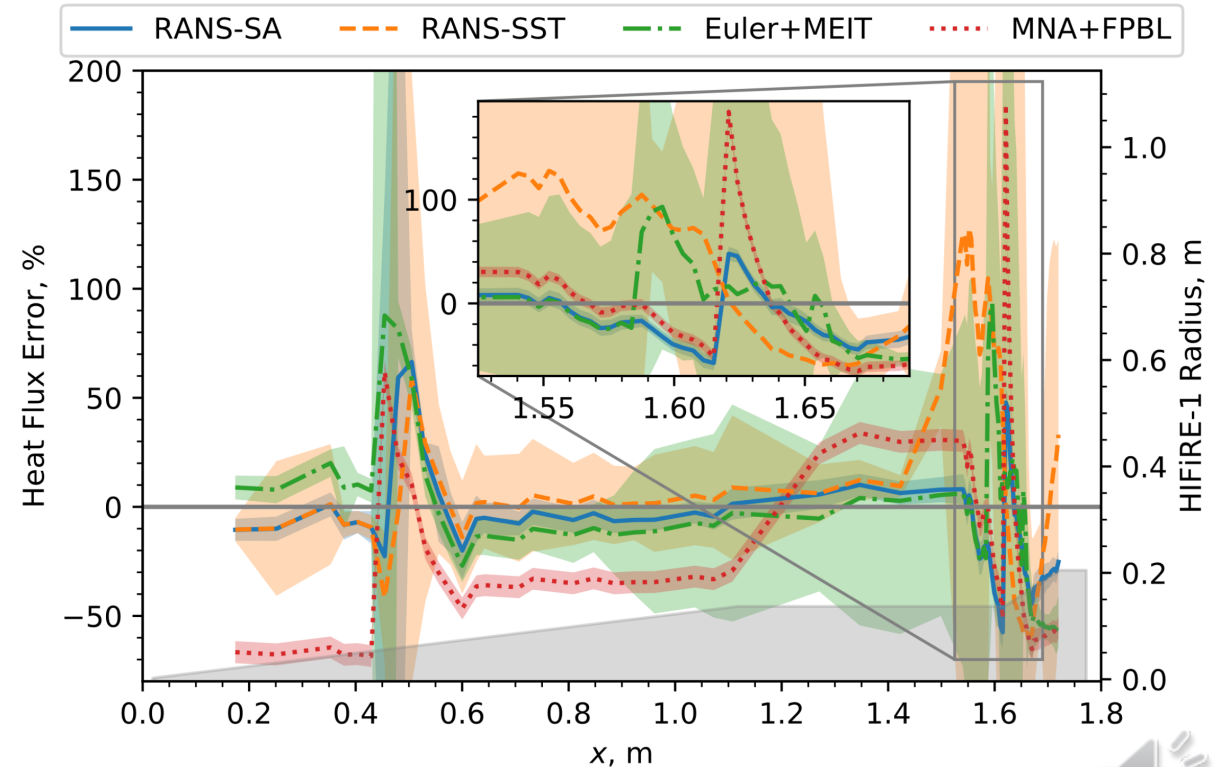
## Nominal Results

- Agreement is very good in cone and cylinder sections
  - more challenging near separation and transition ( $x \approx 0.45$  m)
- RANS-SA and Euler+MEIT capture separation behavior best



## Error Results

- Validation uncertainty is large for RANS-SST and Euler+MEIT
  - Driven by numerical uncertainty
- Higher-fidelity models predict best upstream of separation

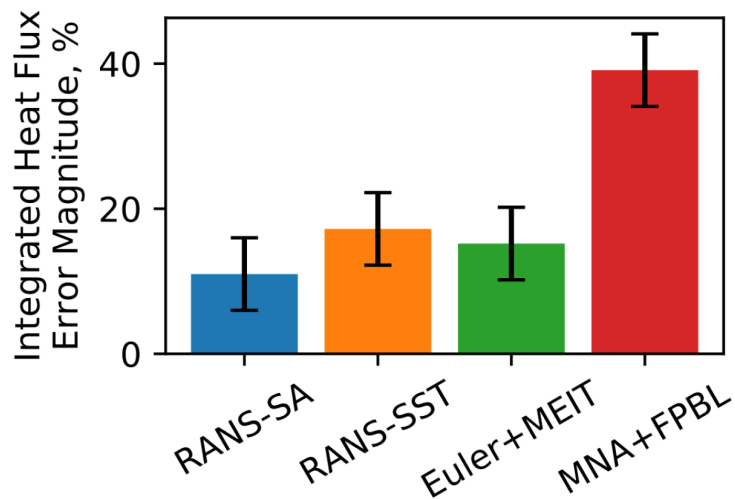




# Surface heat flux validation error integrated over space

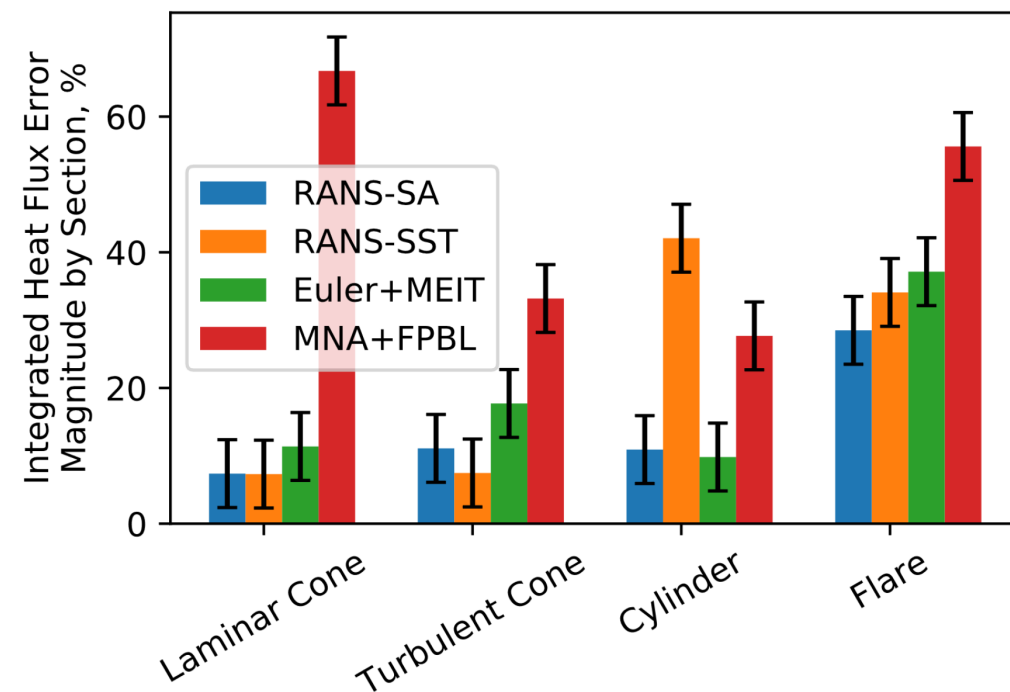
The validation error magnitude  $|E|$  is normalized by experimental data and integrated over all space

- RANS-SA is most accurate, followed by Euler+MEIT (same as for pressure)
- RANS-SST predicts much larger separation region than measured
- Uncertainty bands (error bars) showing only experimental uncertainty (5%)



The validation error magnitude  $|E|$  is normalized by experimental data and integrated within each section

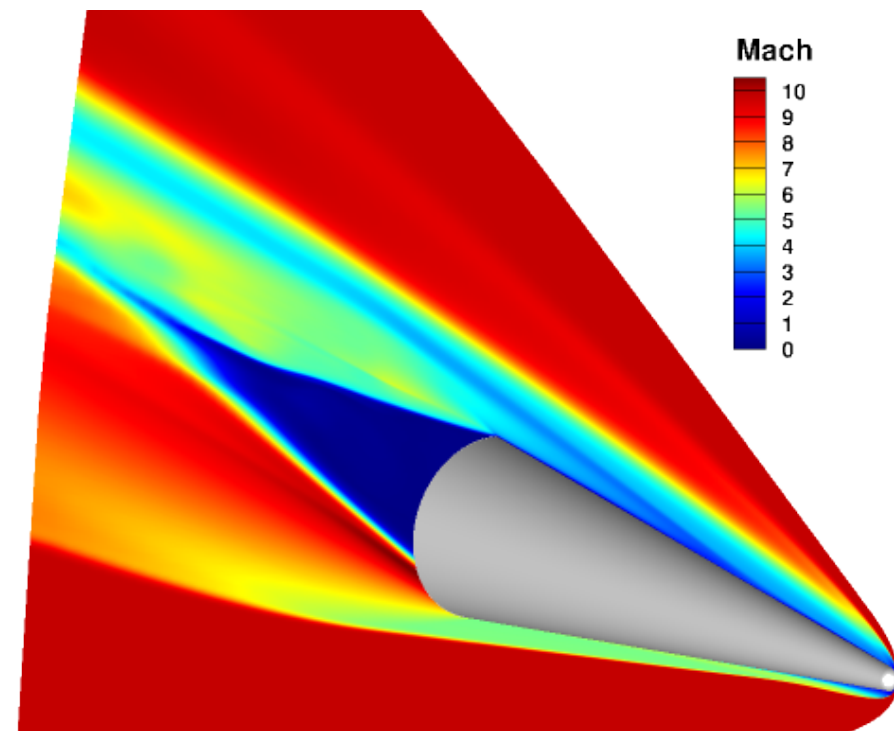
- RANS-SST is most accurate on the cone
- The three higher-fidelity models are much more accurate in the cone and flare sections
- The RANS-SST error is large in the cylindrical section





## Conclusions

- This is the first known validation study for different physics-fidelity models in SPARC (MFTK)
- HIFiRE-1 wind tunnel test data were used for validation
- The RANS models are most accurate for cones
- Most models struggled in the separated region
  - RANS-SA model is most accurate overall
- Lack of grid convergence for RANS-SST and Euler+MEIT should be investigated
- Though not quantified, the reduced fidelity models have sizeable speedup
  - ~100x for Euler+MEIT over RANS
  - ~100x for MNA+FPBL over Euler+MEIT



"Hypersonic Research at Sandia National Labs",  
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