

# Rotation-vibration non-equilibrium measurement using pure rotational fs/ps CARS coherence beating

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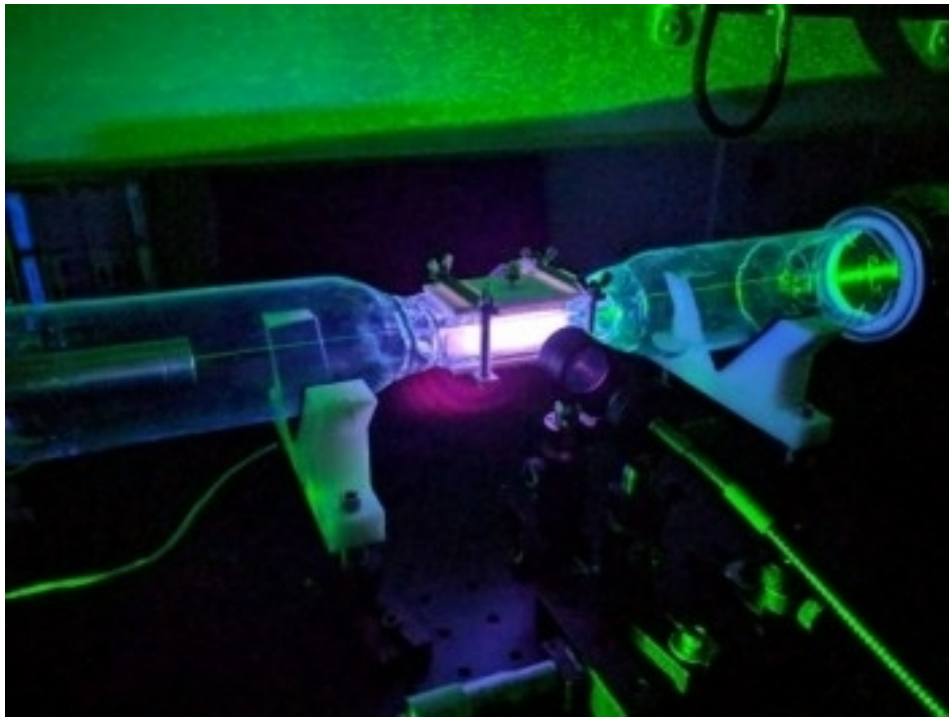
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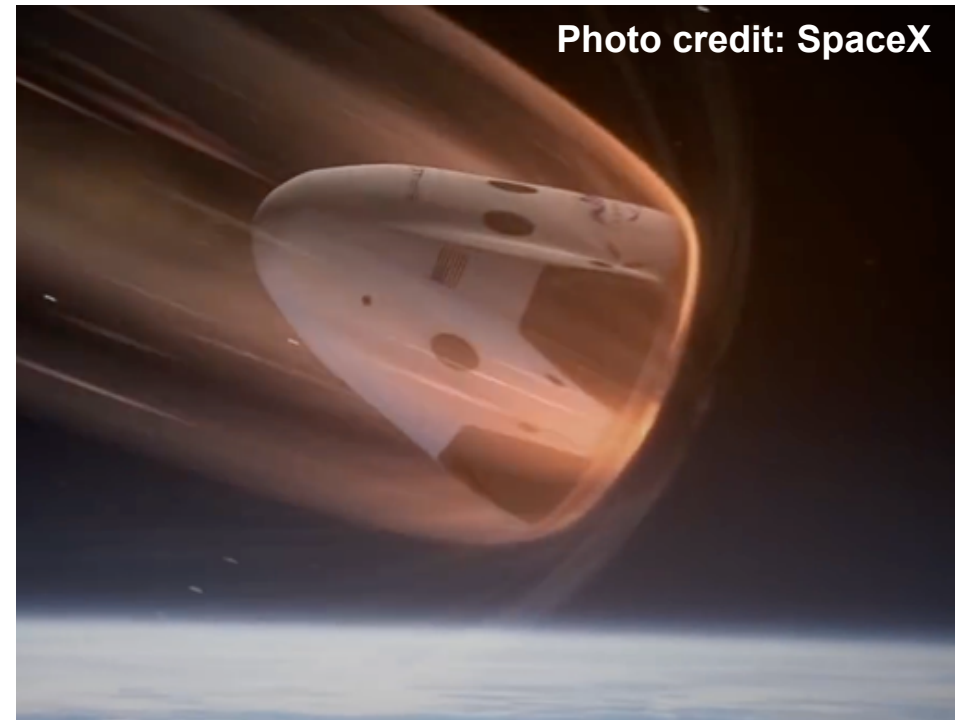
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# Rotation-vibration non-equilibrium is important for plasmas and hypersonics

$$T_{rot} \neq T_{vib}$$

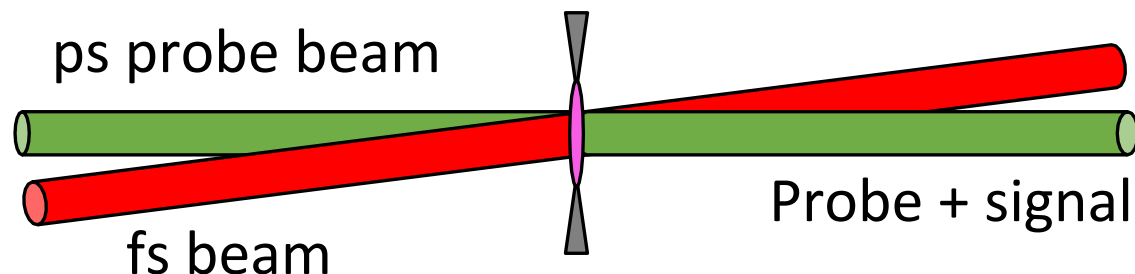


Chemical reactivity and thermalization

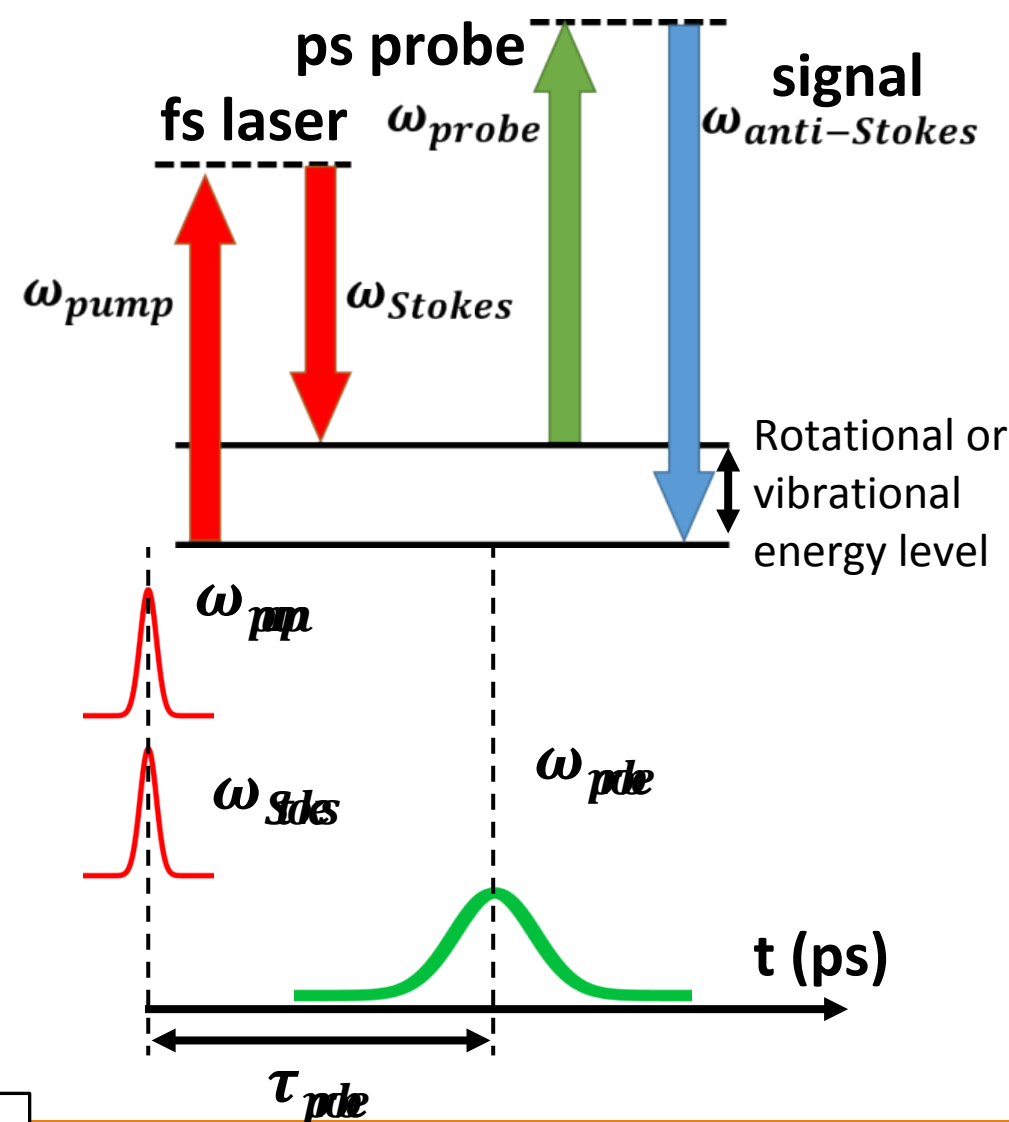


Hypersonic vehicle thermal loading and aerodynamics

# What is hybrid fs/ps CARS?



- Use broadband femtosecond pulse for simultaneous acquisition of many Raman transitions and picosecond probe for spectral resolution [1-2]
- Several advantages:
  - $I_{CARS} \propto I_{fs}^2 * I_{ps} \rightarrow$  1-D or 2-D imaging of temperature and species concentrations within  $50 \mu\text{m}$  of surface [3-5]
  - No need to scan Stokes frequency and only needs 2 beams



# We can use pure rotational fs/ps CARS for simultaneous $T_{\text{rot}}$ and $T_{\text{vib}}$ measurements

Rotational energy level  $F(v, J)$

$$F(v, J) = B_v(J(J + 1)) - D_v(J^2(J + 1)^2)$$

$$B_v = B_e - \alpha \left( v + \frac{1}{2} \right) + \gamma_e \left( v + \frac{1}{2} \right)^2$$

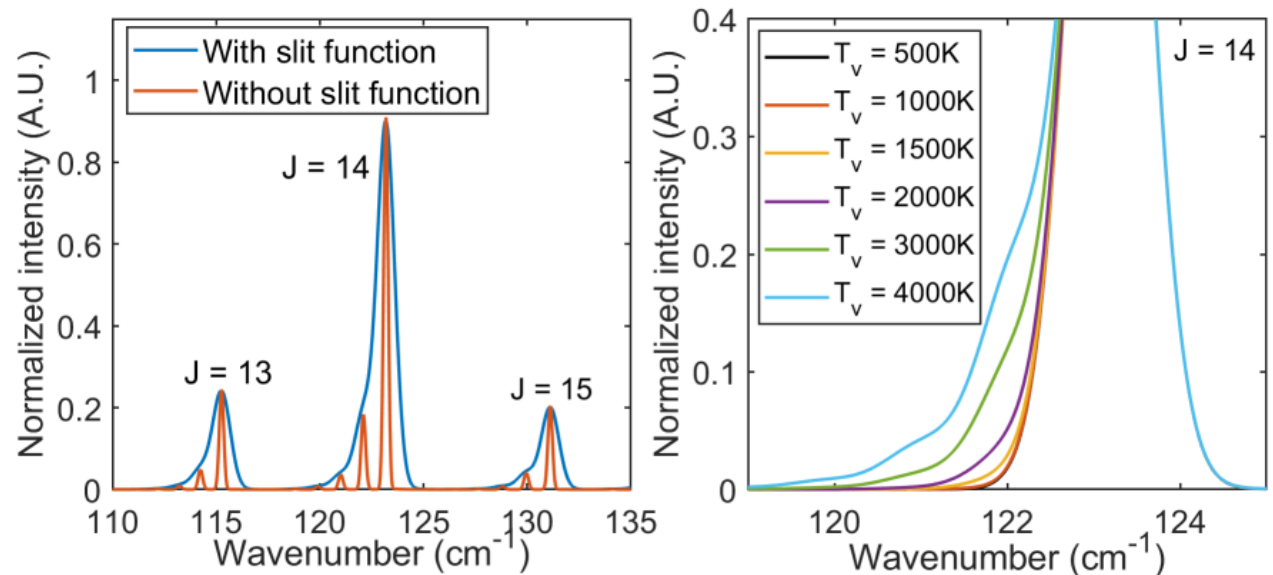
$v$  = vibrational quantum number

$J$  = rotational quantum number

$B_v$  = rotational constant

$\alpha$  = rotation-vibration coupling constant

$D_v$  = centrifugal constant



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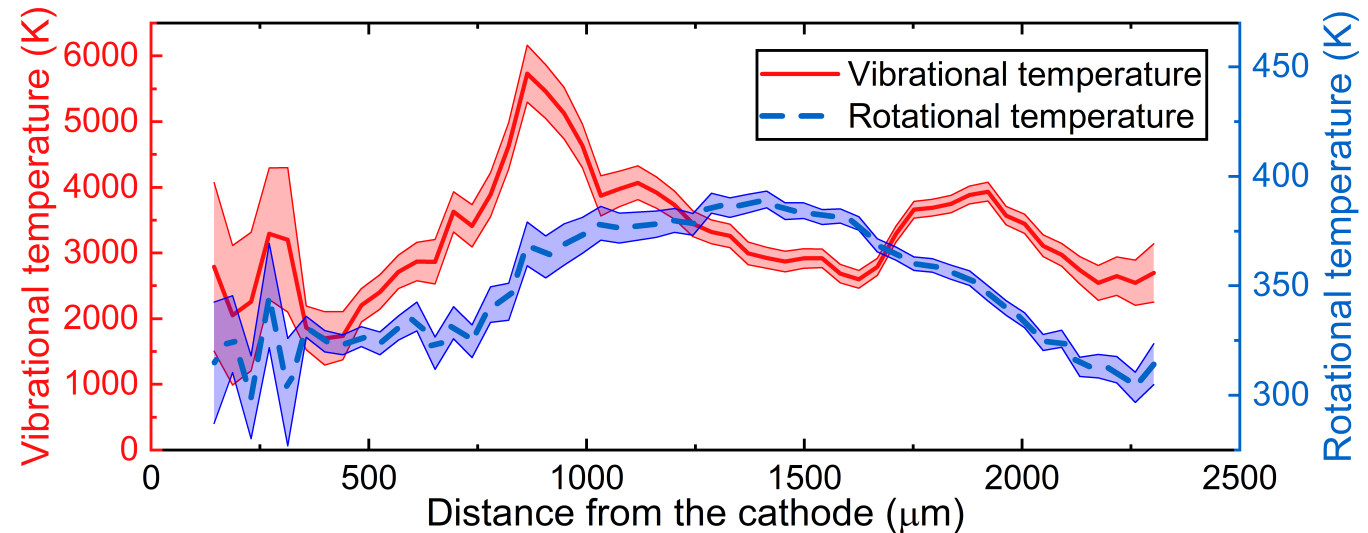
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**Demonstrated 1-D imaging of rotation-vibration non-equilibrium**

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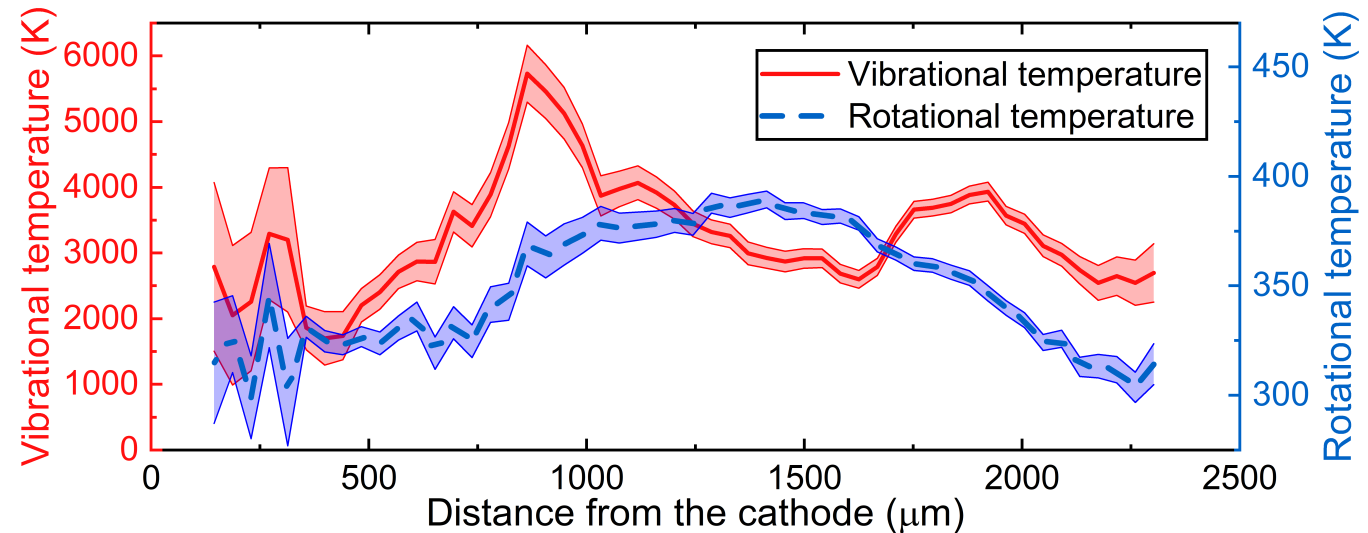
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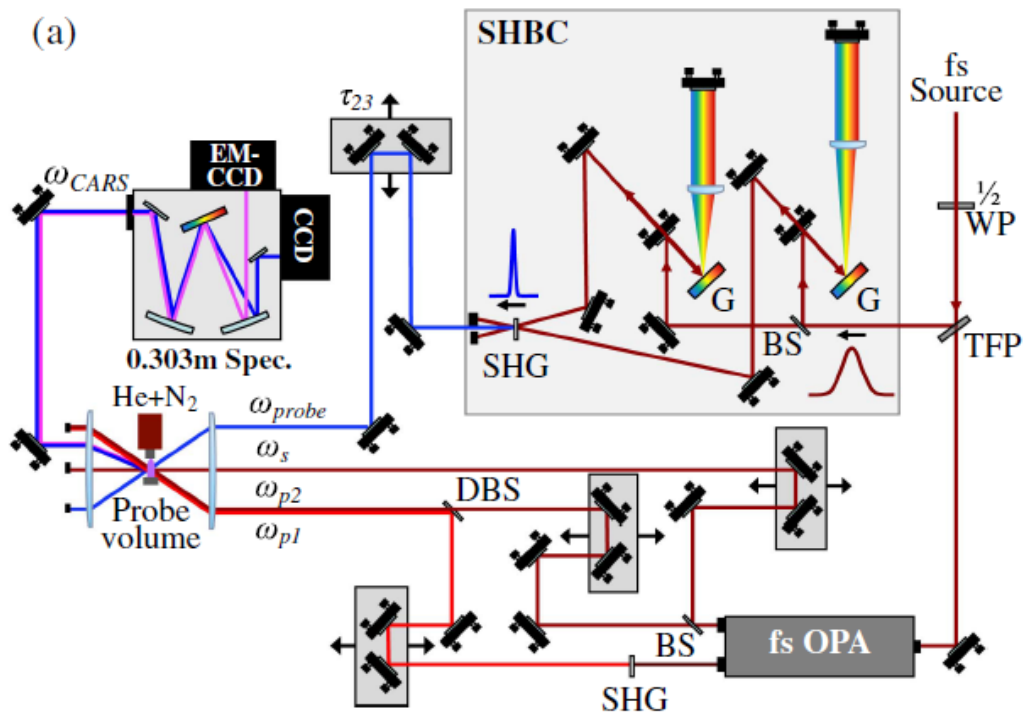
$D_v$  = centrifugal constant



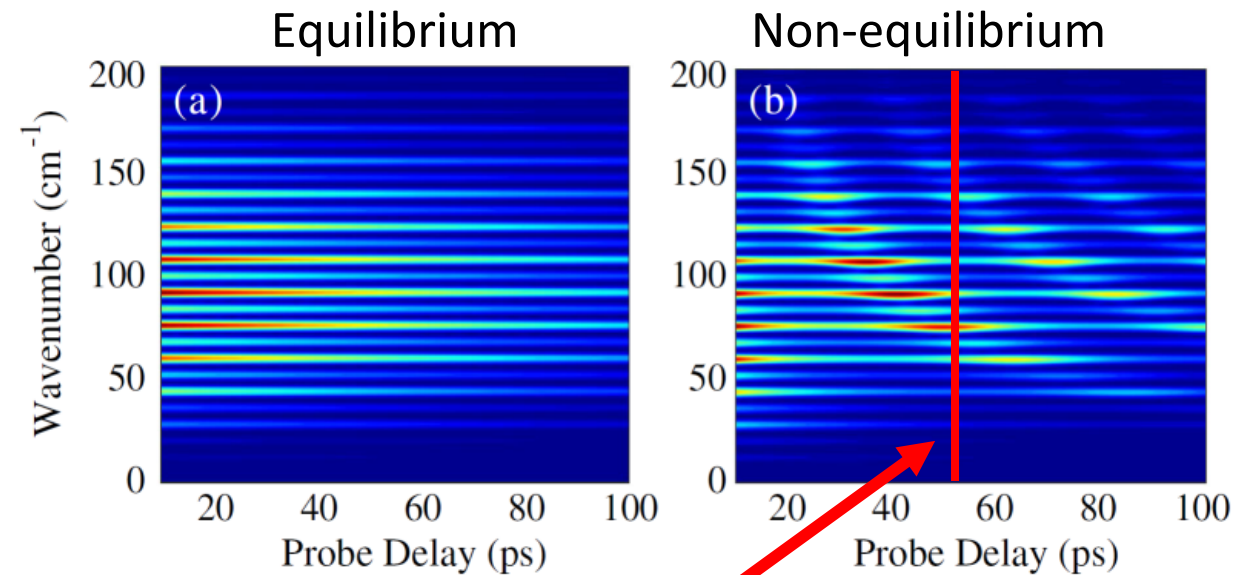
**Needs a spectrally narrow laser  
(< 0.5 cm<sup>-1</sup>)**

# Is there a simpler method?

Dual pump fs/ps CARS is sensitive uses one fs laser but needs **4 beams**

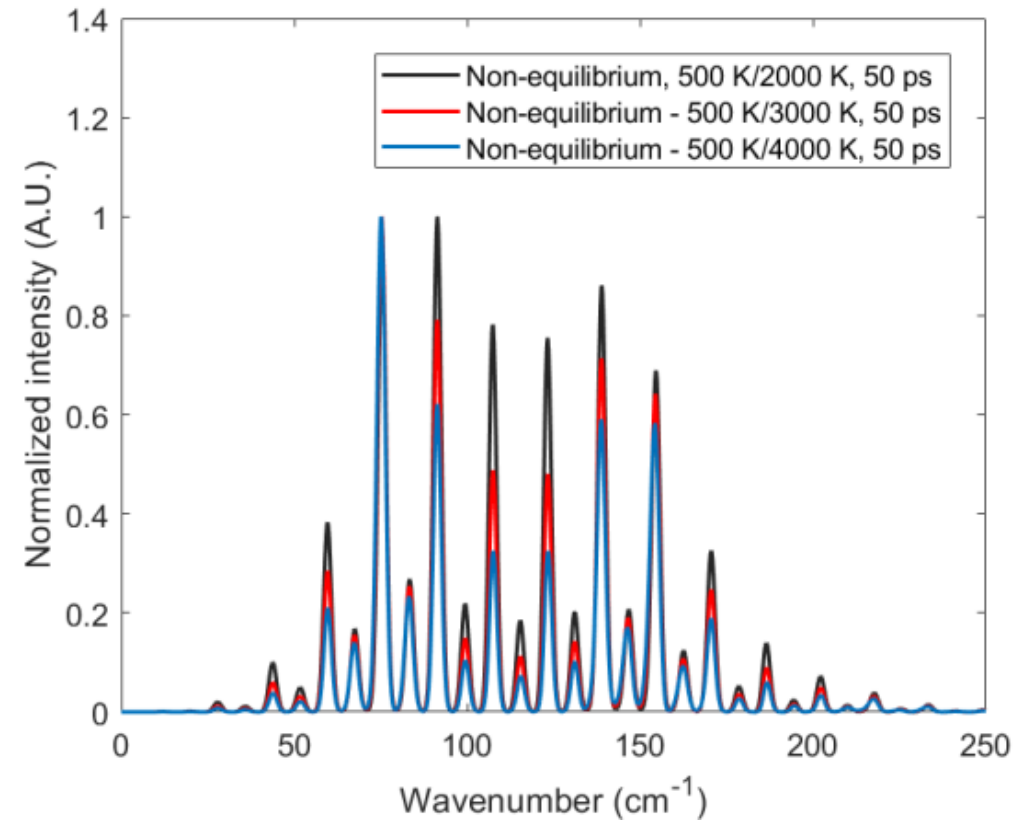
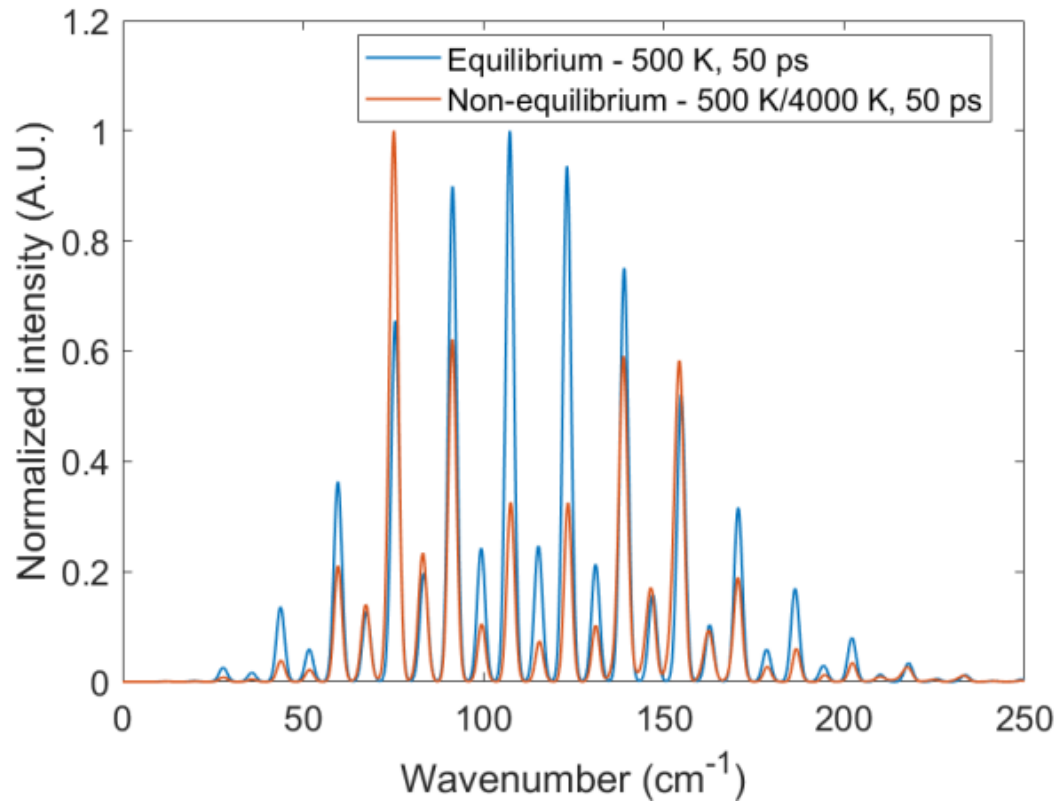


Dedic, C.E. et al., *Optica*, (2017)



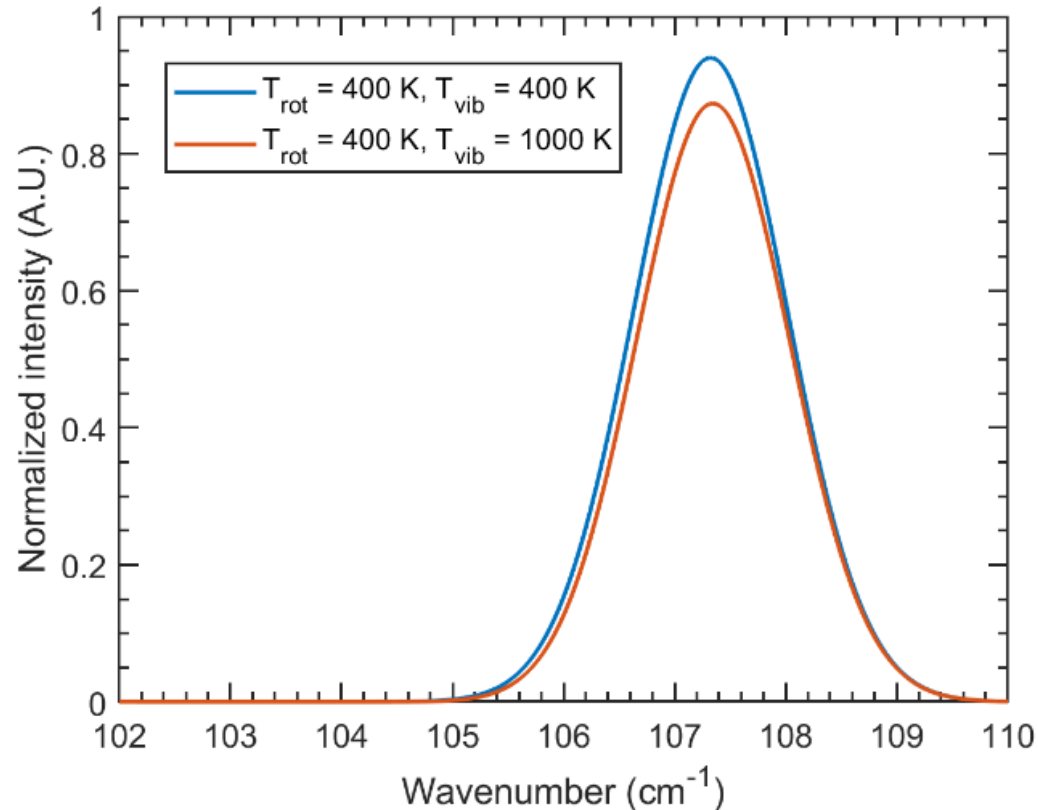
If we know probe delay and beating pattern, can we extract  $T_{vib}$  and  $T_{rot}$  ?

# We can use coherence beating for simultaneous $T_{\text{rot}}$ and $T_{\text{vib}}$ measurements

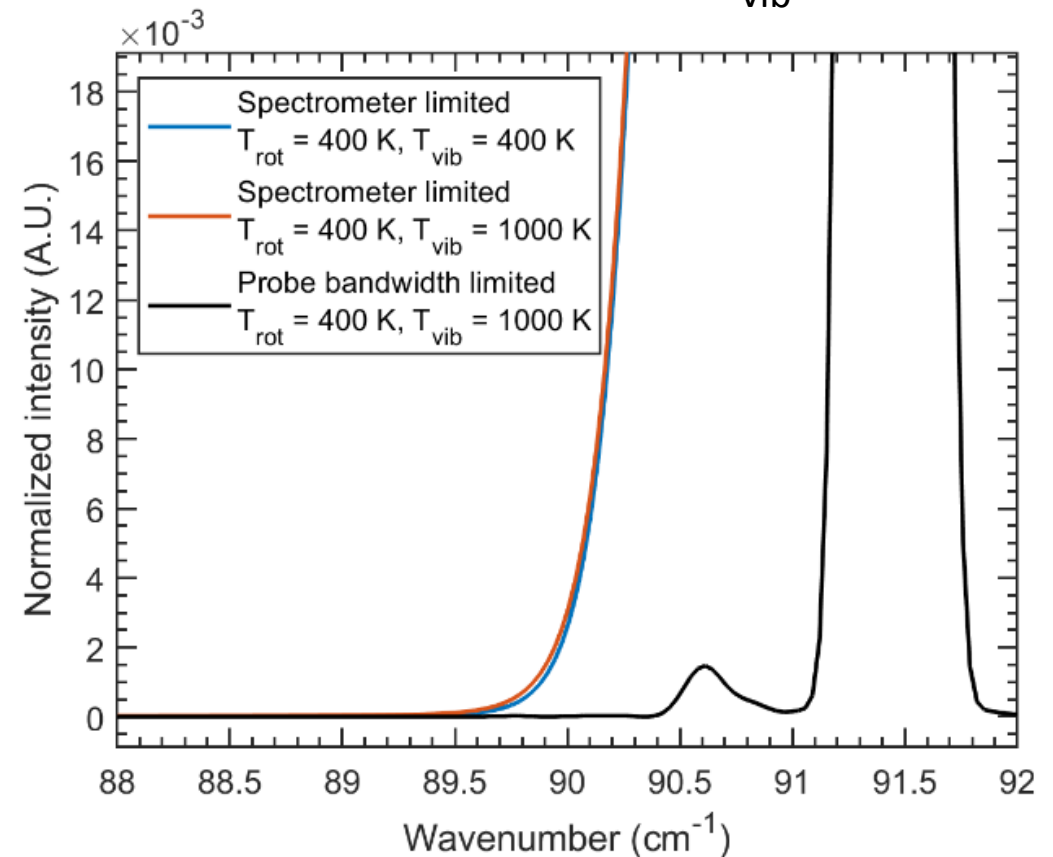


# How does the sensitivity compare to frequency domain detection?

Sensitive to  $T_{\text{vib}} = 1000$  K

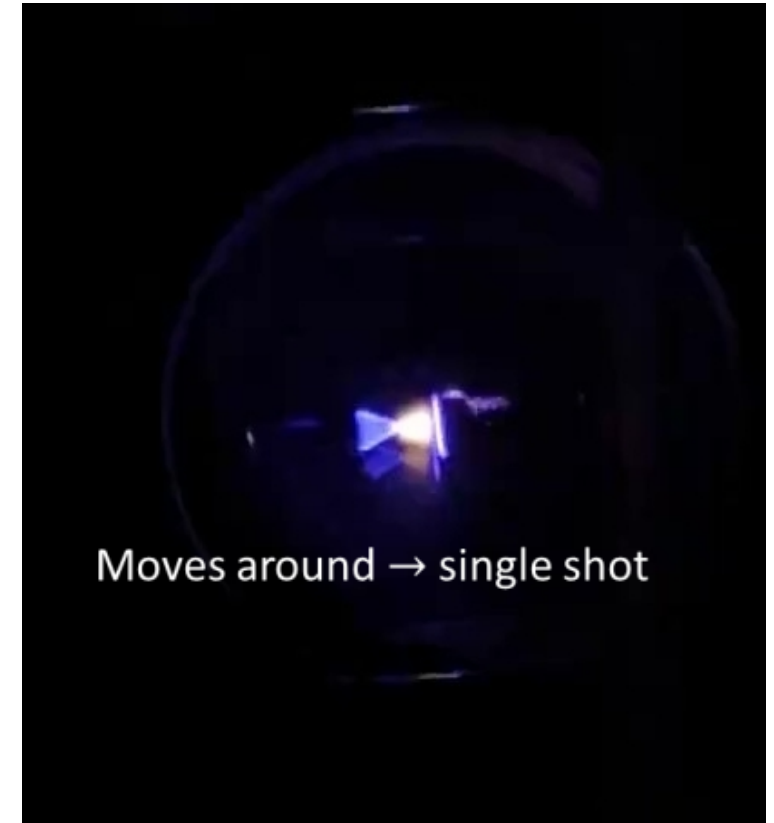
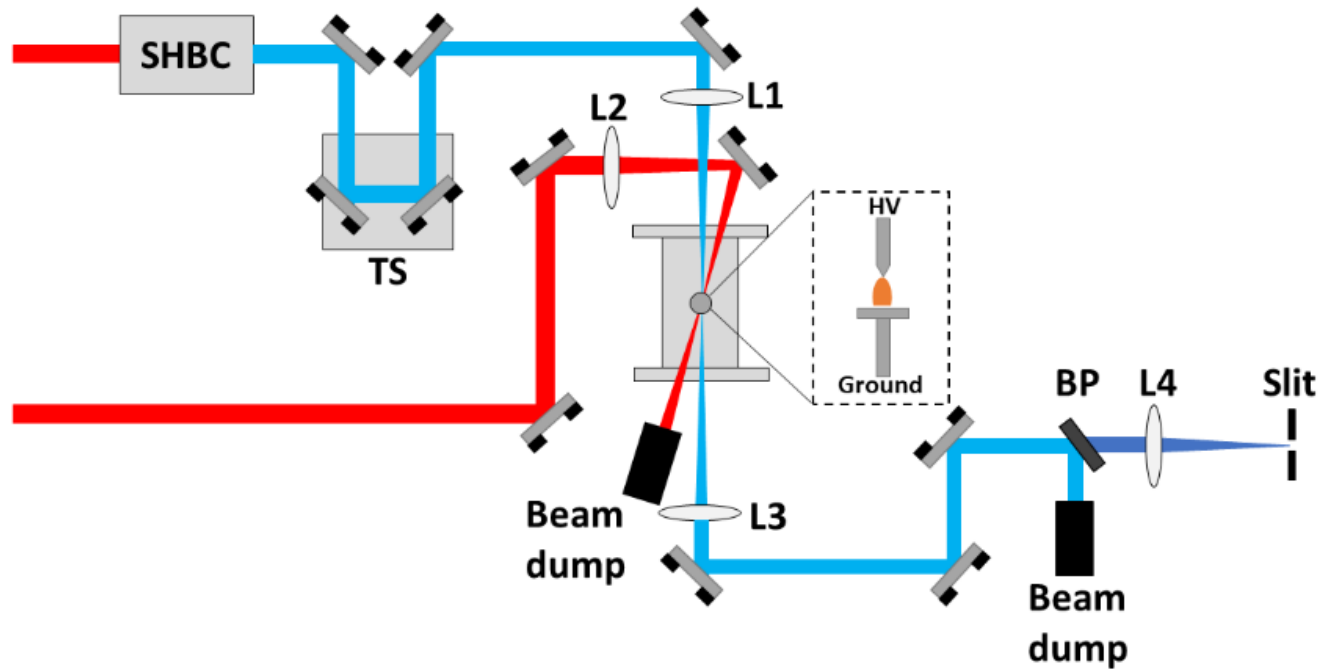


High spectrometer resolution needed for measurement of  $T_{\text{vib}} = 1000$  K



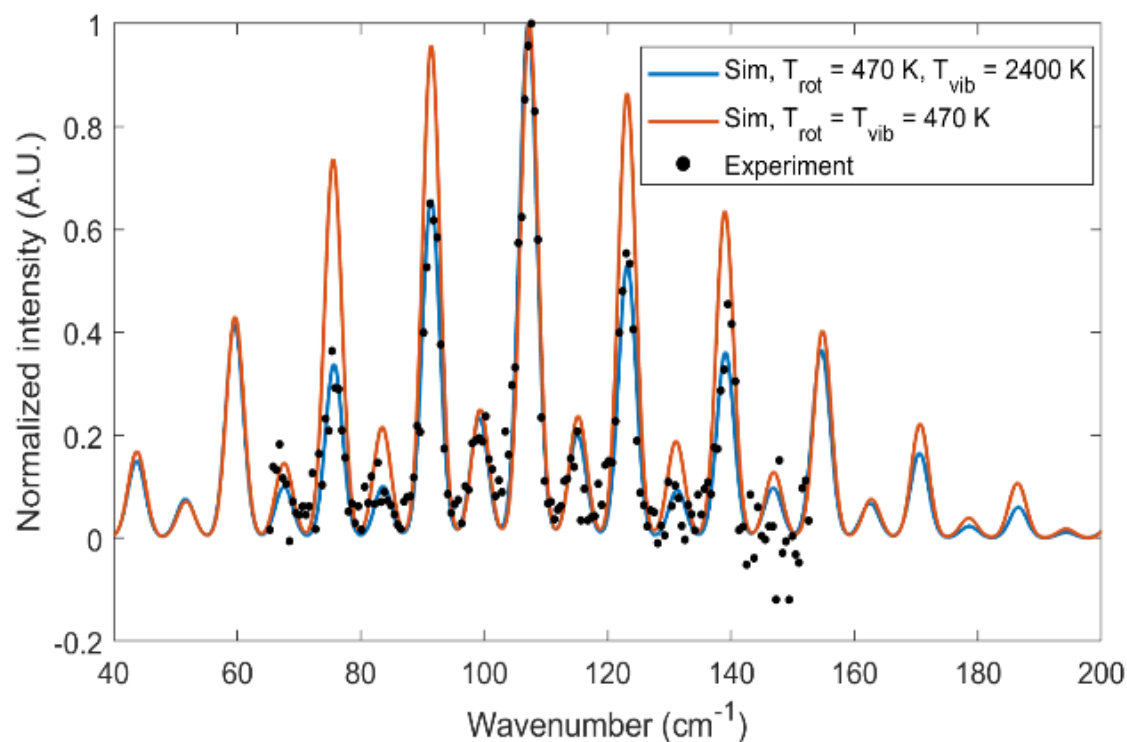
# Experimental setup for model validation

75 Torr pure N<sub>2</sub>, 2 kV DC, 100 kΩ resistor in series,  $I \sim 15$  mA

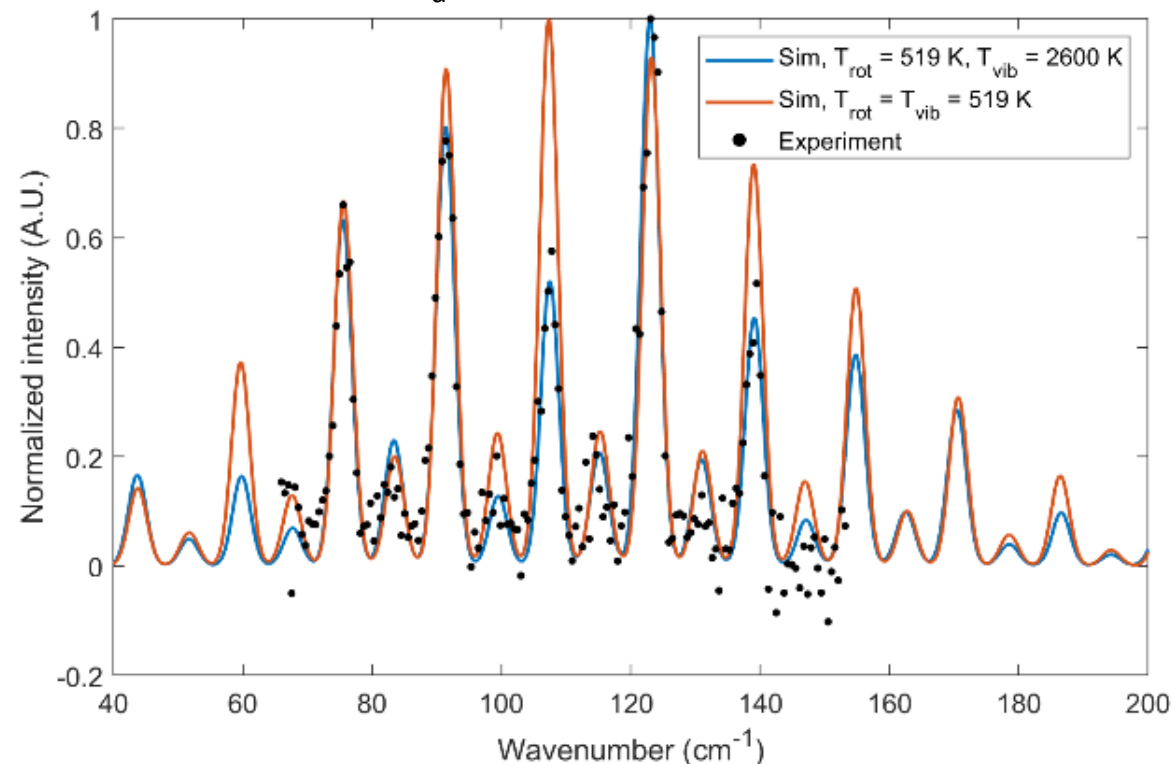


# Simulated spectra fit well with the measurements

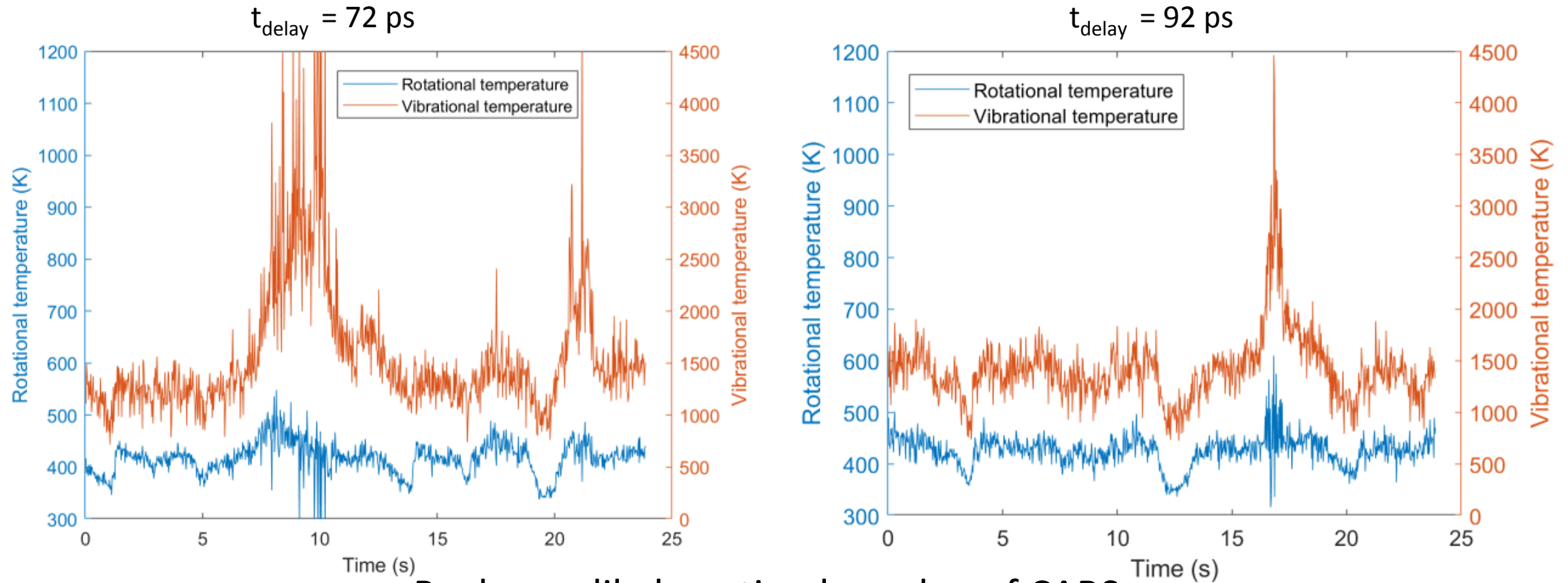
$T_d = 72$  ps



$T_d = 92$  ps



# Time traces at two probe delays show consistent temperatures and dynamics



Peaks are likely optimal overlap of CARS  
 probe volume and positive column of plasma

# Conclusions

- Developed new diagnostic for simultaneous  $T_{\text{rot}}$  and  $T_{\text{vib}}$  measurement using pure rotational fs/ps CARS coherence beating
- Can be more sensitive than detection in frequency-domain
- Demonstrated this technique with a  $\text{N}_2$  DC discharge and successfully fit and extracted non-equilibrium  $T_{\text{rot}}$  and  $T_{\text{vib}}$
- Enables high speed 1-D and 2-D CARS measurements of rotation-vibration non-equilibrium in plasmas and hypersonic flows

# Acknowledgements

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## Questions?