



A data-driven roadmap towards Pareto optimal hydrogen storage alloys

PRESENTED BY

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Experiments

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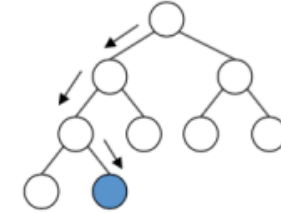
Rachel Hurst (NREL)
Nick Wunder (NREL)
Max Gallant (NREL)

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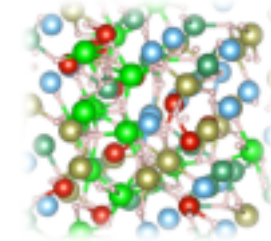


**Approach:**

Using data-driven/machine learning techniques for materials discovery

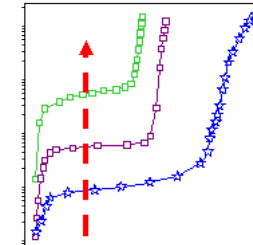
**Application:**

Discovering more efficient materials-based hydrogen storage

**Results:**

Success stories in data-driven discovery of hydrogen storage materials

- New technical capabilities/physical insights
- Towards Pareto optimal materials

**Future Work:**

Overcoming current limitations in ML-driven discovery for hydrogen storage materials



$$v = \text{avg}(v_1^{t0}, v_2^{t0})$$



$$v_1^{t1} = (v_1^{t0} \oplus v_2^{t0} \oplus e_{12}) \cdot W + b$$





Approach:

Why use data-driven/machine learning techniques for materials discovery?



Data science/ML models in materials/chemical sciences can be applied to problems of “all shapes and sizes”



Angstroms

...

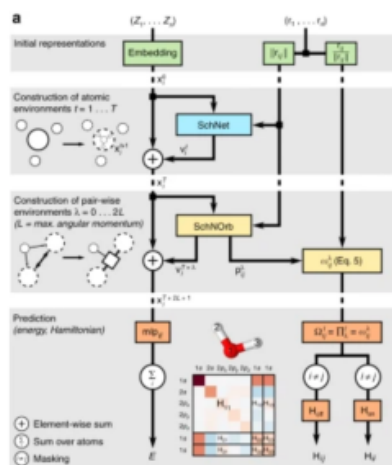
to

...

Acres

Small molecule property predictions¹

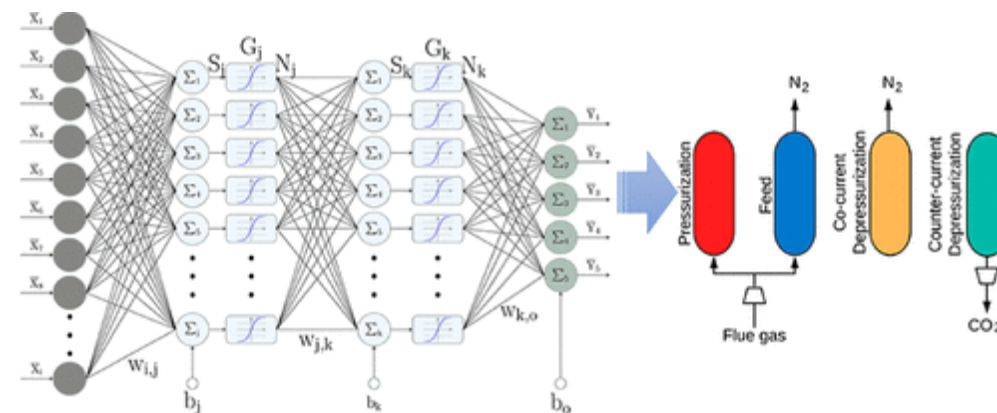
Inputs
(Z, r)



Outputs
(E)

Chemical plant performance prediction²

Inputs
(PSA unit parameters)



Outputs
(CO₂ purity of PSA units)

ML models are not: a magic box that solve all our problems, will always require “truth” data from experiments or first principles calculations (often difficult in materials science)

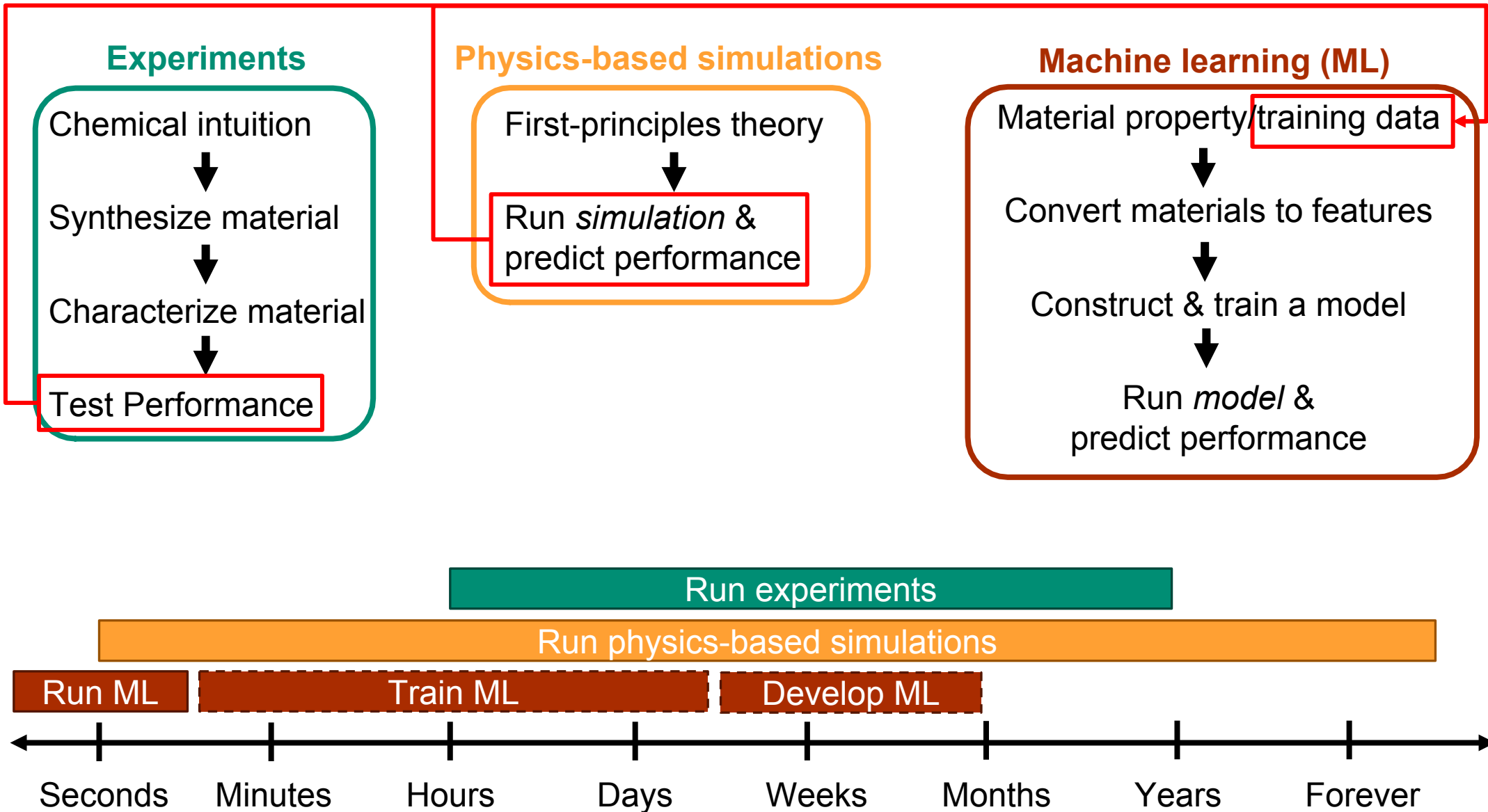
ML models are: *surrogates that execute many orders of magnitude faster than an experiment or first principles calculation to make task X tractable (high-throughput screening, optimization, active search, etc.)*

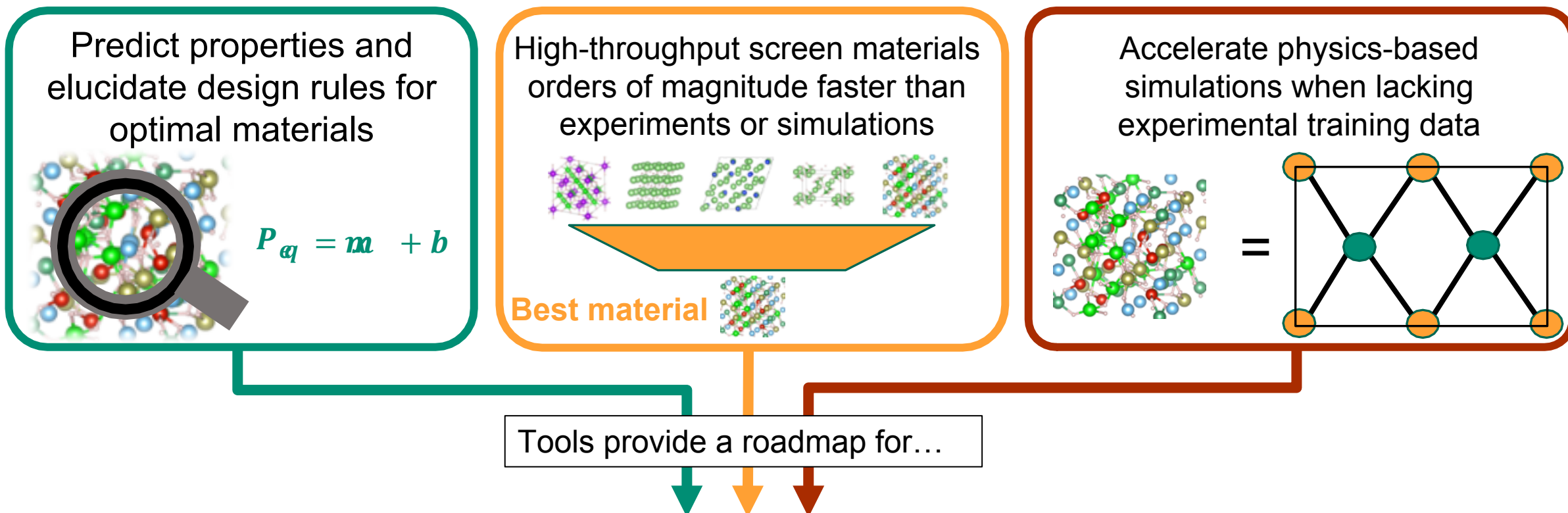


[1] Schutt, et al. *Nat. Comm.* 10, 2019

[2] Leperi, et al. *I&EC*. 58 (39), 2019

Three main approaches to materials discovery





H₂ storage: Data-driven discovery of Pareto optimal hydrogen storage alloys

H₂ generation: Data-driven discovery of water-splitting materials (STCH, liquid metals, etc.)





Application:

Discovering more efficient materials-based hydrogen storage



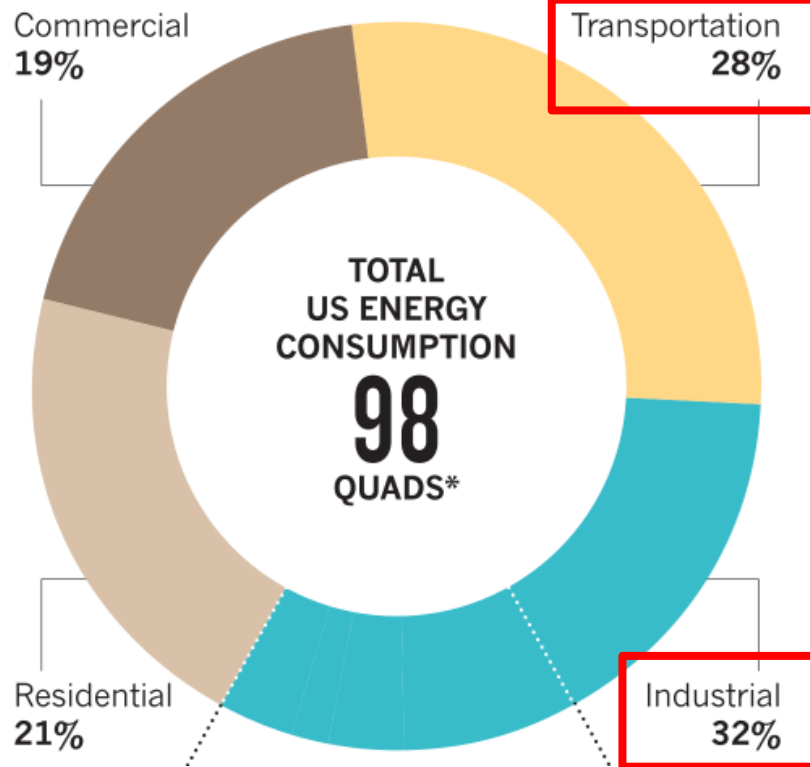


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Discovering improved H₂ storage and generation techniques will facilitate progress towards a hydrogen economy

H₂ to play a critical role in...

Heavy duty (planes, trains, ships)



High T applications

Personal transportation
(Toyota/Hyundai)



Air Travel
(Airbus)



Home energy storage
(Lavo)



Utility-scale generation
(Shell)



First Energy Earthshot Aims to Slash the Cost of Clean Hydrogen by 80% to \$1 per Kilogram in One Decade

"Clean hydrogen is a game changer" -- Secretary Granholm



Are there undiscovered materials that could improve upon conventional H₂ storage and generation technologies?



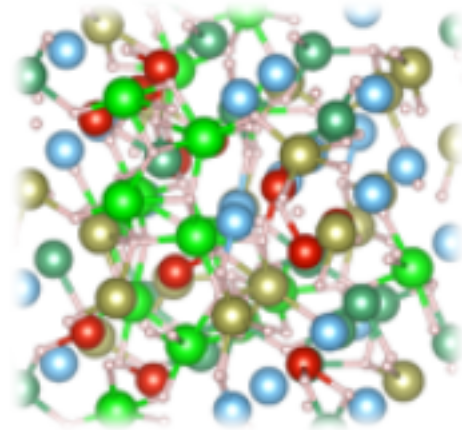
H₂ Storage objectives:

- High H₂ gravimetric and/or volumetric density
- Fast, reversible release near ambient T
- Practical/cost-effective
- Reduced infrastructure cost



“Conventional”
(Compressed gas)

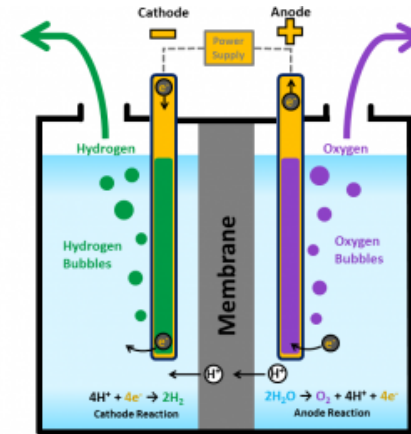
vs.



Material X ??

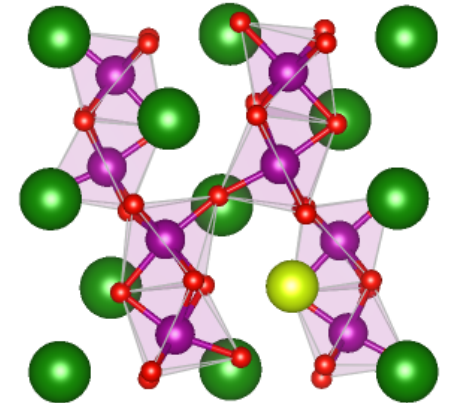
H₂ Generation objectives:

- Water-splitting using only renewable energy
- Practical/cost-effective



“Conventional”
1.2 V in theory
1.8 V in practice

vs.



Material Y ??

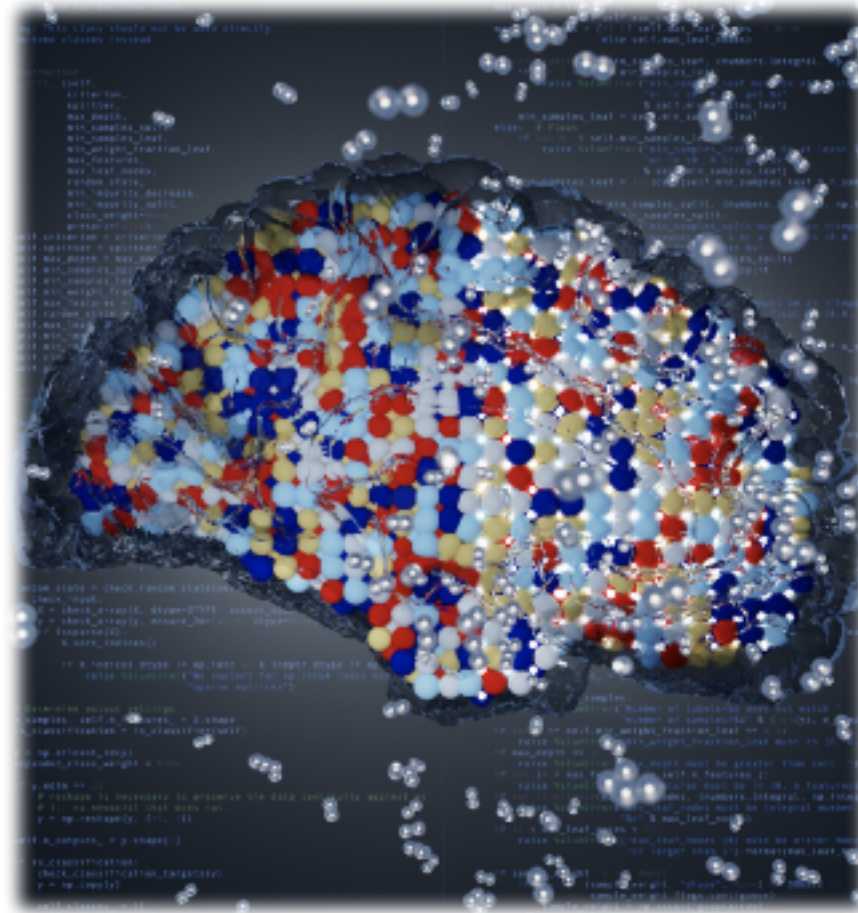


Results: A data-driven roadmap towards Pareto optimal hydrogen storage alloys

- **Milestone #1** : Explainable ML models predict metal hydride thermodynamics
- **Milestone #2** : ML enables discovery of destabilized high entropy alloy (HEA) hydrides
- **Milestone #3** : ML screening & identification of *Pareto optimal* HEA hydrides



Milestone #1: Explainable ML models predict metal hydride thermodynamics



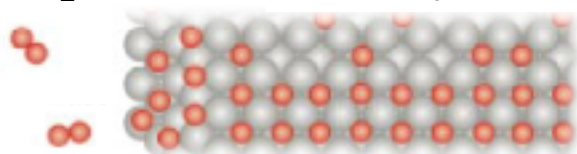
Milestone #1: Explainable ML models predict metal hydride thermodynamics



(1) $\ln(P_{eq}^o/P_o)$ target property

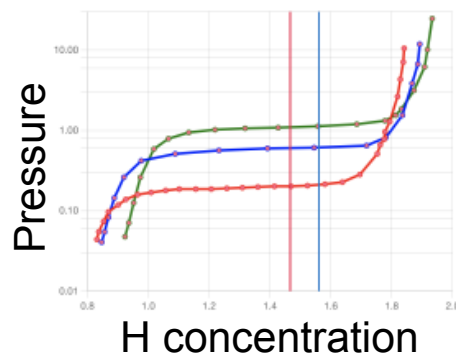
H₂

Metal Hydride



$$\ln(P_{eq}^o/P_o) = -\frac{\Delta H}{R(25^\circ C)} + \frac{\Delta S}{R}$$

Extracted from isotherms & van't Hoff



$\Delta H, \Delta S$ are tabulated in HydPARK.csv

- Missing data, errors, etc.
- **Only 15% of 2500 entries usable**

(2) Constructing a compositional ML model¹

- Features derived from substituent elemental properties:
 $f_i \equiv$ fraction of element i , $p_i \equiv$ elemental property of i
- Simple operations map composition to scalar feature:
 $\bar{p} = \sum_i f_i p_i$, $\hat{p} = \sum_i f_i |p_i - \bar{p}|$, $\ddot{p} = \max(p_i) - \min(p_i)$, etc...
- Any composition mapped to same dimensional feature vector:
 $\mathbf{x}_{\text{Magpie}} = \{\bar{v}_{pa}, \bar{r}_{cov}, \bar{\chi}, \dots\} \in \mathbb{R}^{145}$
- **Necessary if exact structure unknown** (e.g. TiFe_{0.92}Nb_{0.08})
- Gradient boosting trees (ensemble of m trees):
 $y = F_m(\mathbf{x}) + h_m(\mathbf{x})$
 $h_m(\mathbf{x})$, a new estimator, corrects the previous model, $F_m(\mathbf{x})$
 i.e. is fit to minimize residual error, $y - F_m(\mathbf{x})$
- **Expressive, interpretable model if sufficient data**

[1] Ward, et al. *npj Comp. Mater.* 2016

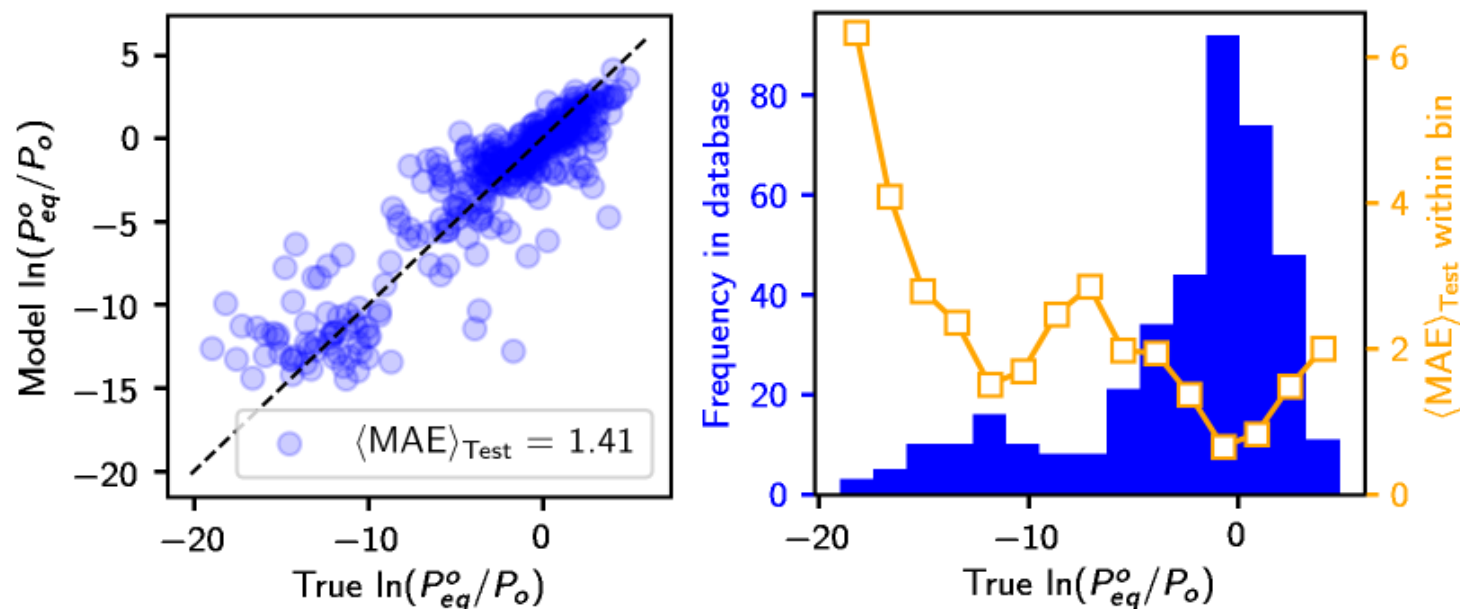
Witman, Ling, Grant, Walker, Agarwal, Stavila, Allendorf. *J. Phys. Chem. Lett.*, 11 (1), 2020



Milestone #1: Explainable ML models predict metal hydride thermodynamics



Thermodynamics (equilibrium plateau pressure) model validation

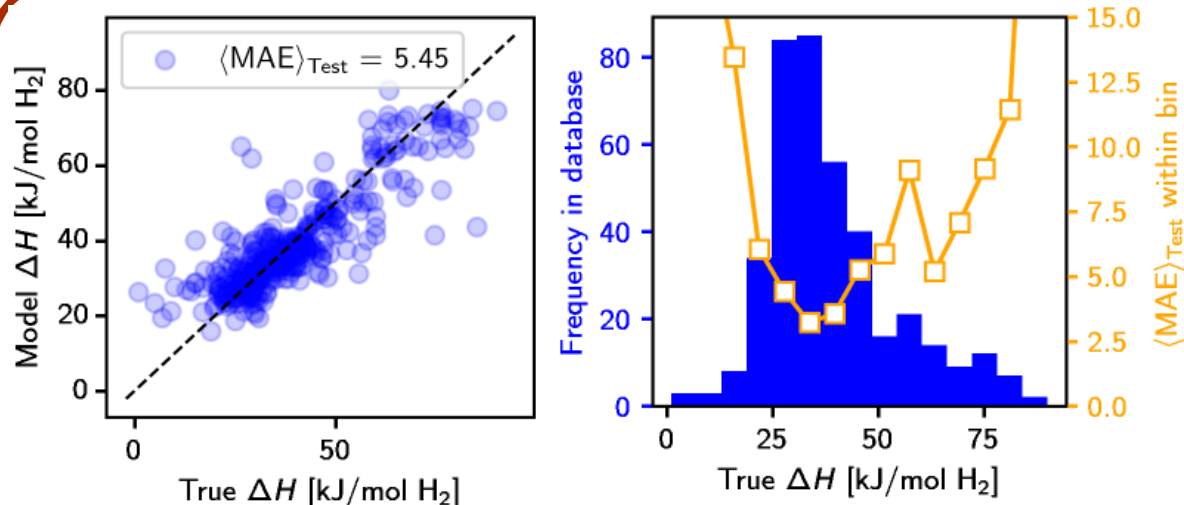


*ML model can predict $\hat{y} \equiv \ln(P_{eq}^o/P_o)$ with cross-validation test $\langle \text{MAE} \rangle = 1.4$



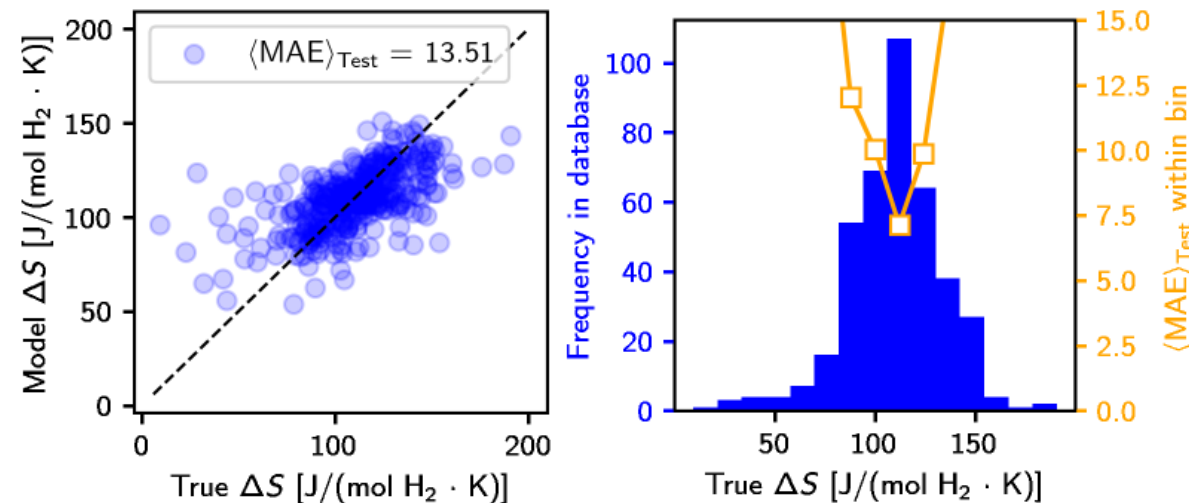


(3) Thermodynamics (individual ΔH and ΔS) model validation



Can predict $\hat{y} \equiv \Delta H$ with cross-validation test
 $\langle MAE \rangle = 5.5$ kJ/mol H_2

Can predict $\hat{y} \equiv \Delta S$ with cross-validation test
 $\langle MAE \rangle = 14$ J/(mol K)

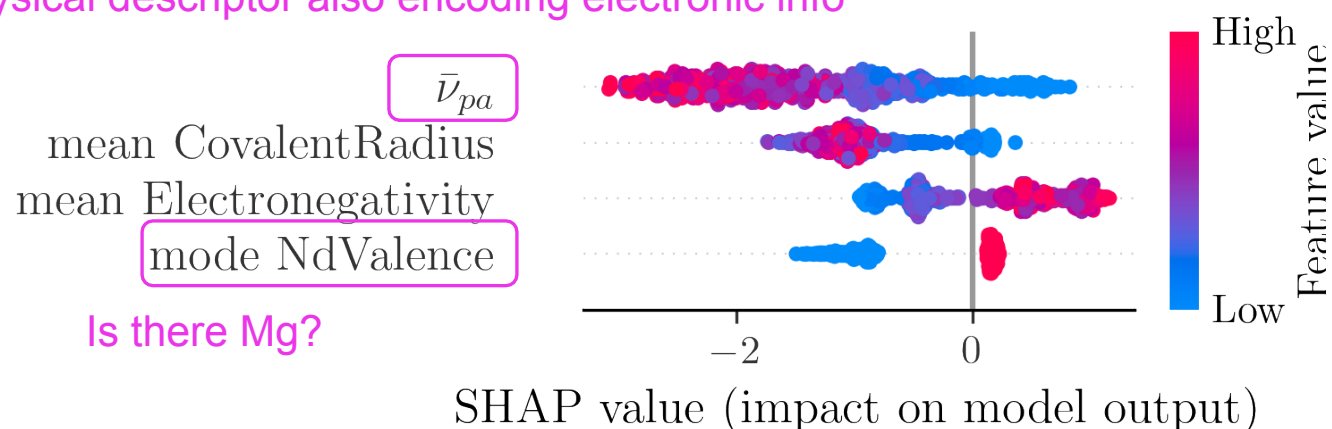




Model interpretability with SHapely Additive Predictions (SHAP)¹

How does a model's output depend on the value of a given feature?

“Elemental solid ground state volume/atom”:
A physical descriptor also encoding electronic info



*Linear correlation with \bar{v}_{pa} :

$$\ln \left(\frac{P_{eq}^o}{P_o} \right) \approx -m \bar{v}_{pa} + b$$

[1] Lundberg, et al. *NIPS*, 2017.

Witman, Ling, Grant, Walker, Agarwal, Stavila, Allendorf. *J. Phys. Chem. Lett.*, 11 (1), 2020

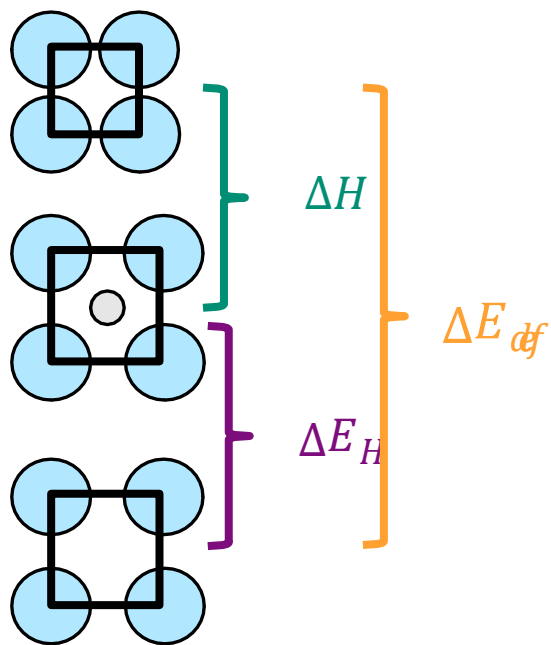


Milestone #1: Explainable ML models predict metal hydride thermodynamics

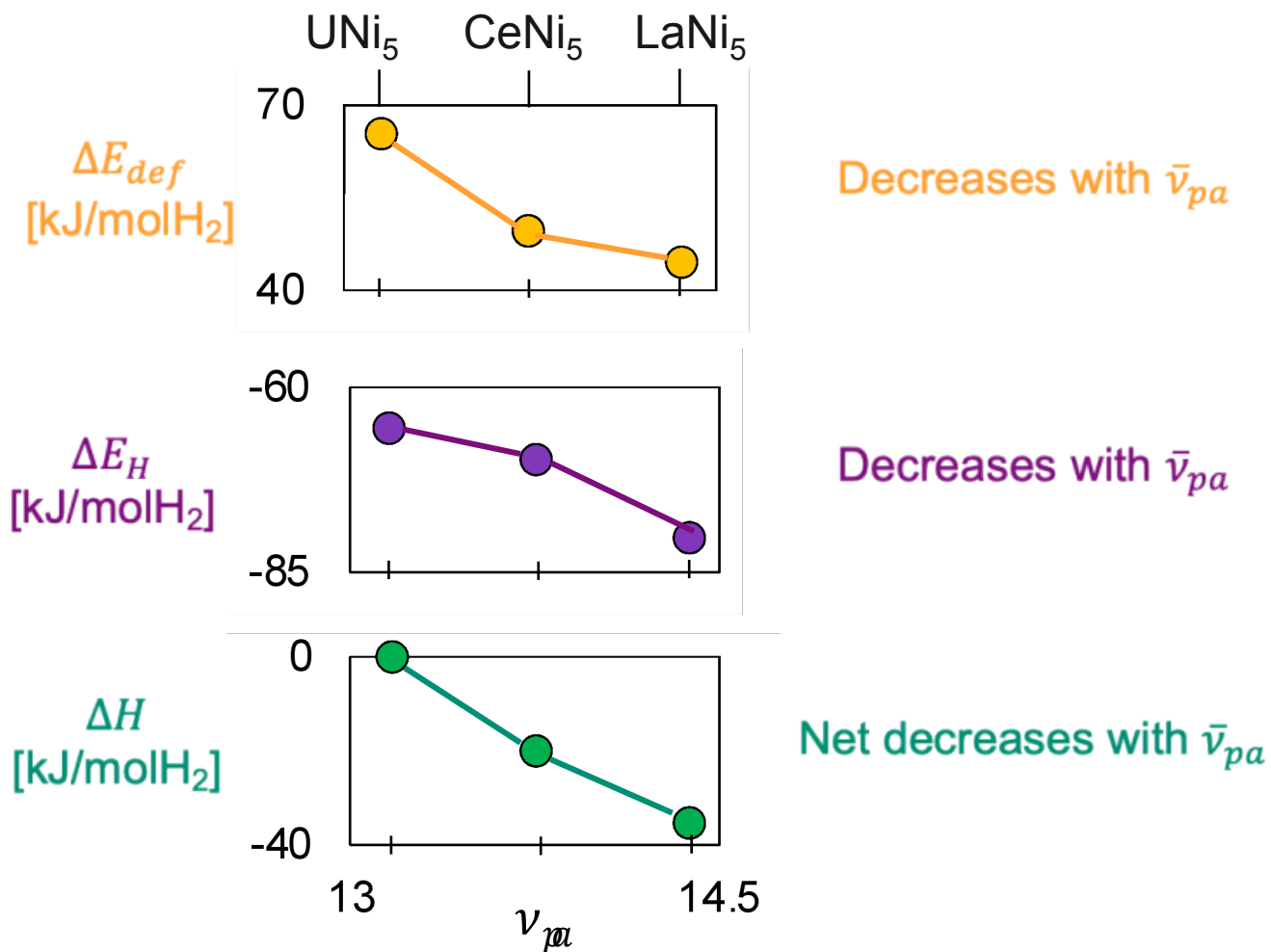


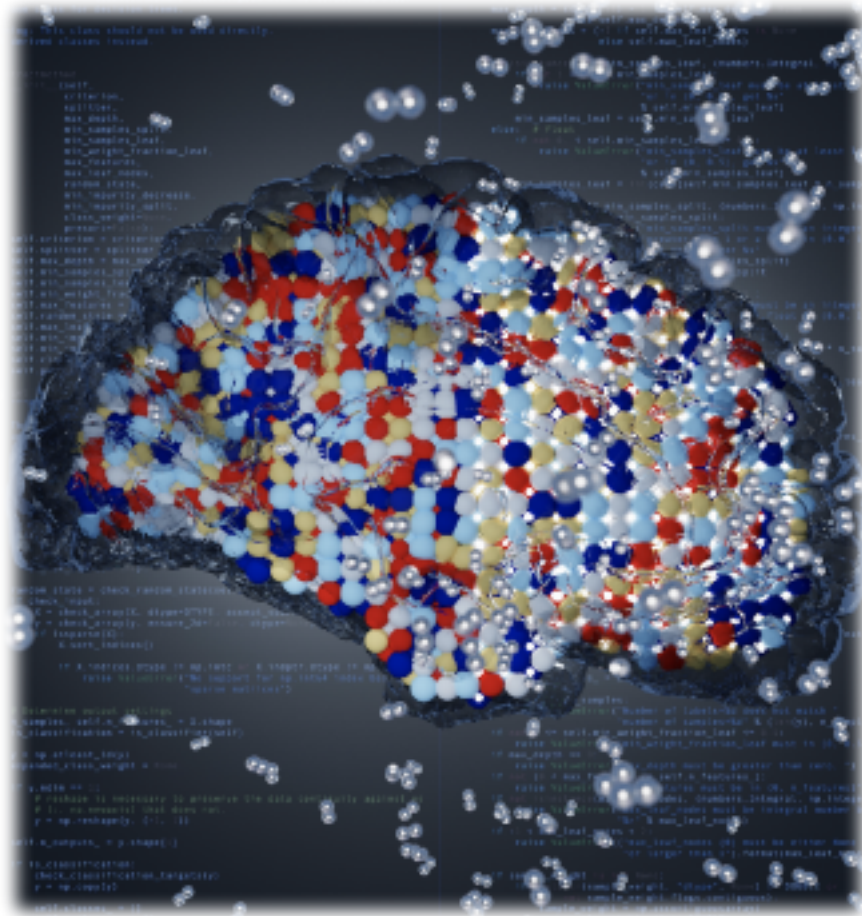
A DFT case study on correlation of hydride thermodynamics with $\bar{\nu}_{pa}$

Probe the reaction:
 $AB_5 + 3.5H_2 \rightarrow AB_5H_7$



Lattice deformation penalty
 H stabilization energy
 Hydride enthalpy



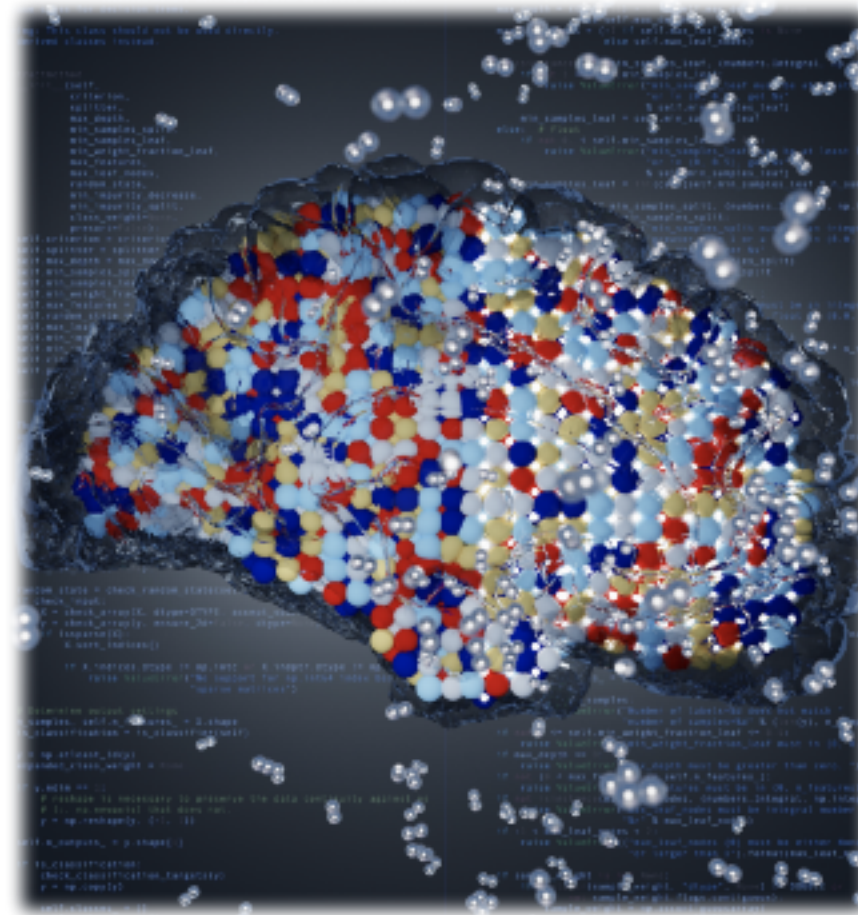


Conclusions:

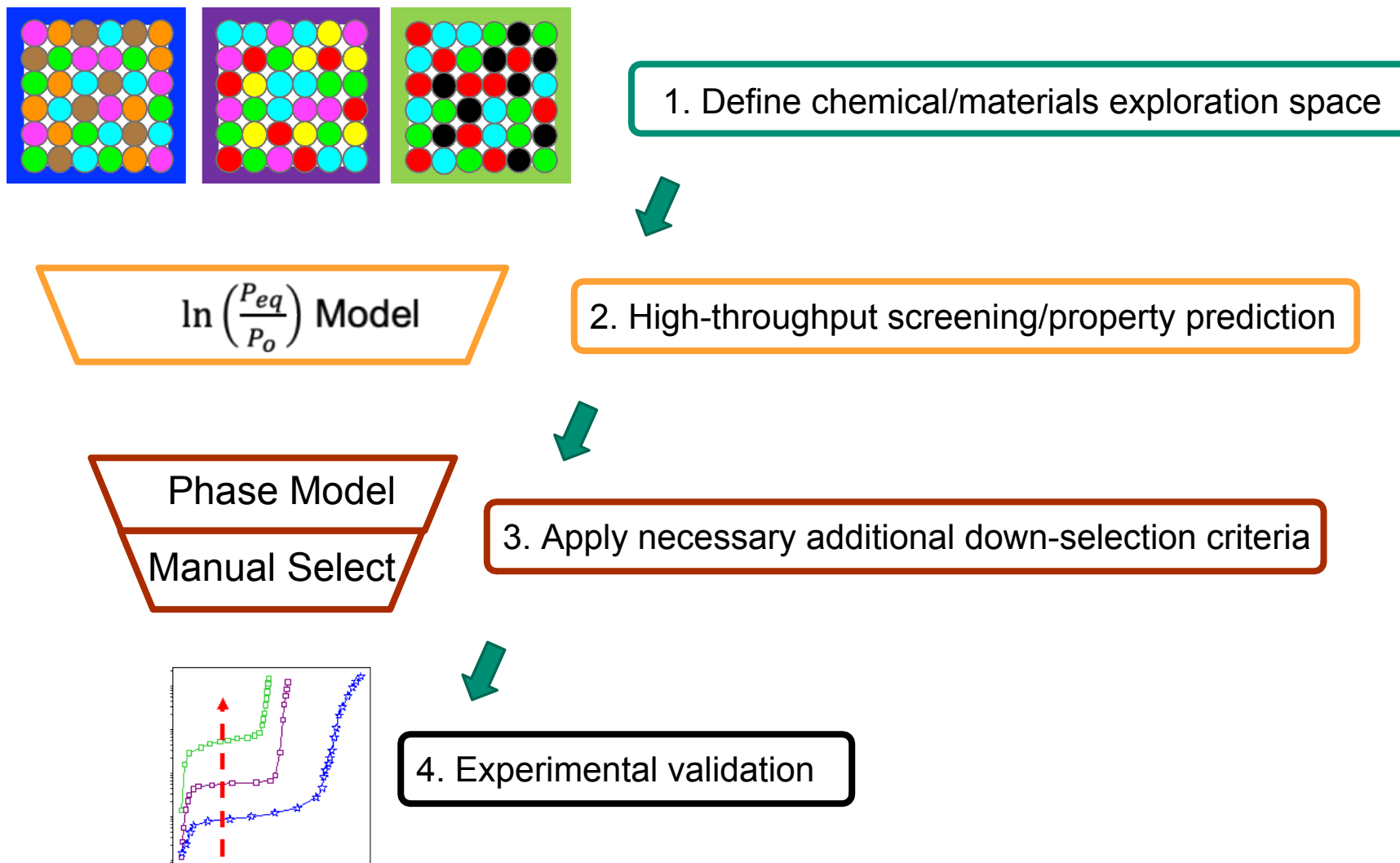
- Compositional ML models can predict metal hydride thermodynamics
- Interpretability of ML models reveals design rules of increasing complexity
- DFT can validate ML-established design rules for specific hydride classes with limited throughput



Milestone #2: ML enables discovery of destabilized high entropy alloy (HEA) hydrides



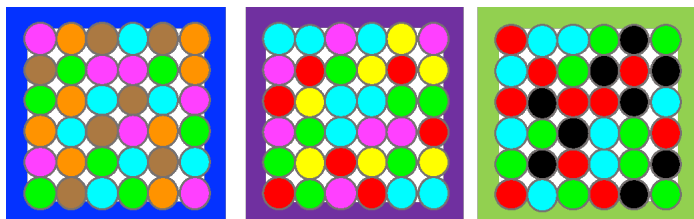
Milestone #2: ML enables discovery of destabilized high entropy alloy (HEA) hydrides



Milestone #2: ML-based discovery of destabilized high entropy alloy (HEA) hydrides



(1) HEA overview:



- > 4 elements, ~ equimolar
- Defined lattice type
- Solid solution character necessitates a compositional ML model

(2) Enumerating refractory HEA space

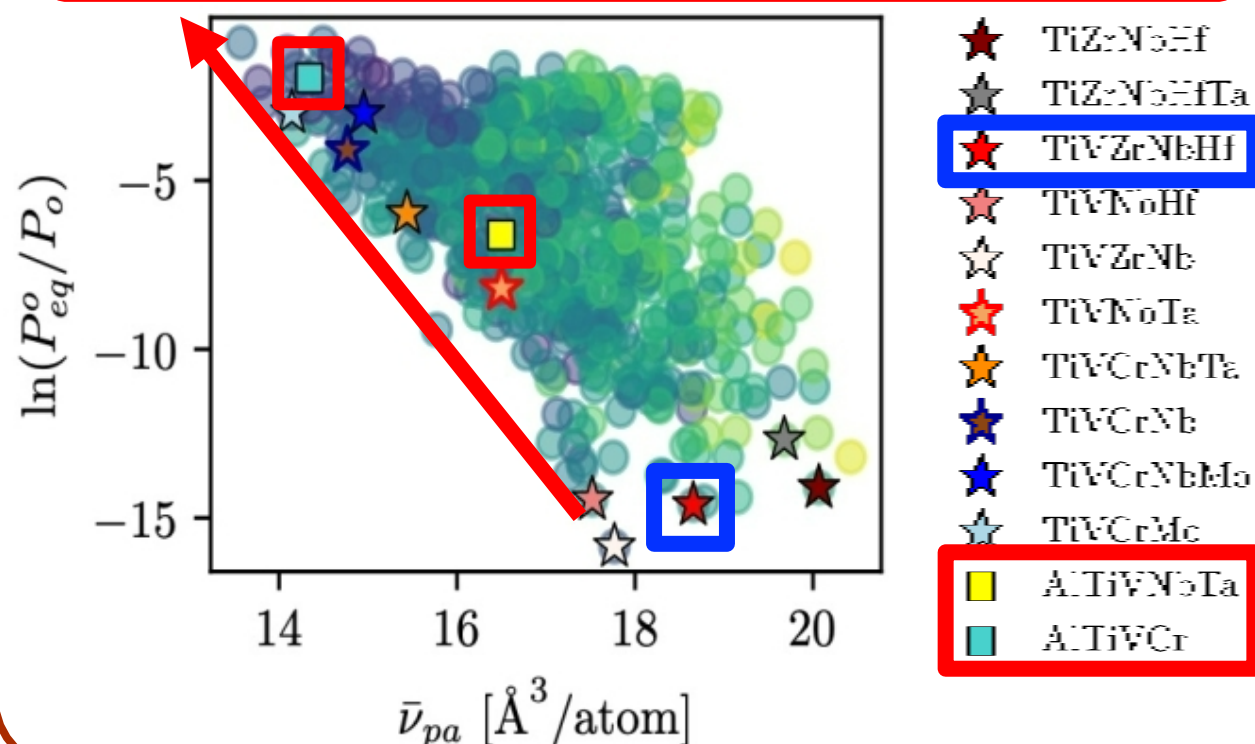
$$E = \{\text{Al, Ti, V, Cr, Zr, Nb, Mo, Pd, Hf, Ta}\}$$

$$\binom{E}{4} + \binom{E}{5} + \binom{E}{6} \rightarrow 672 \text{ compositions}$$

Far too many for experiments...

(3) Screening refractory HEA space

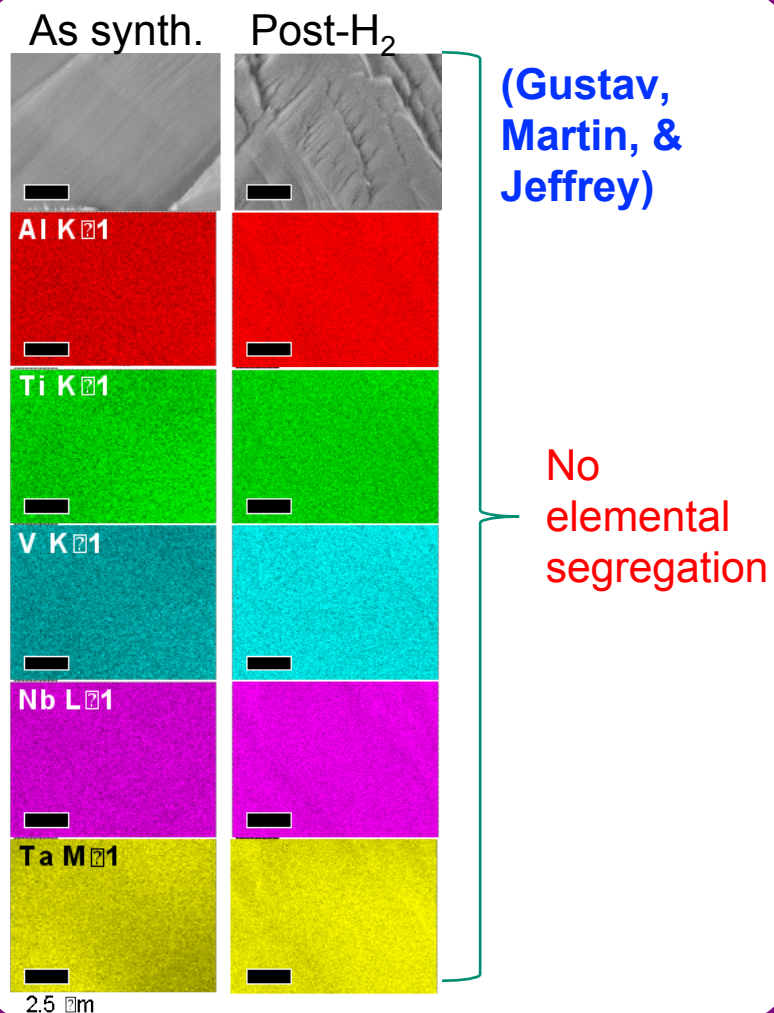
Destabilized hydrides experimentally confirmed!



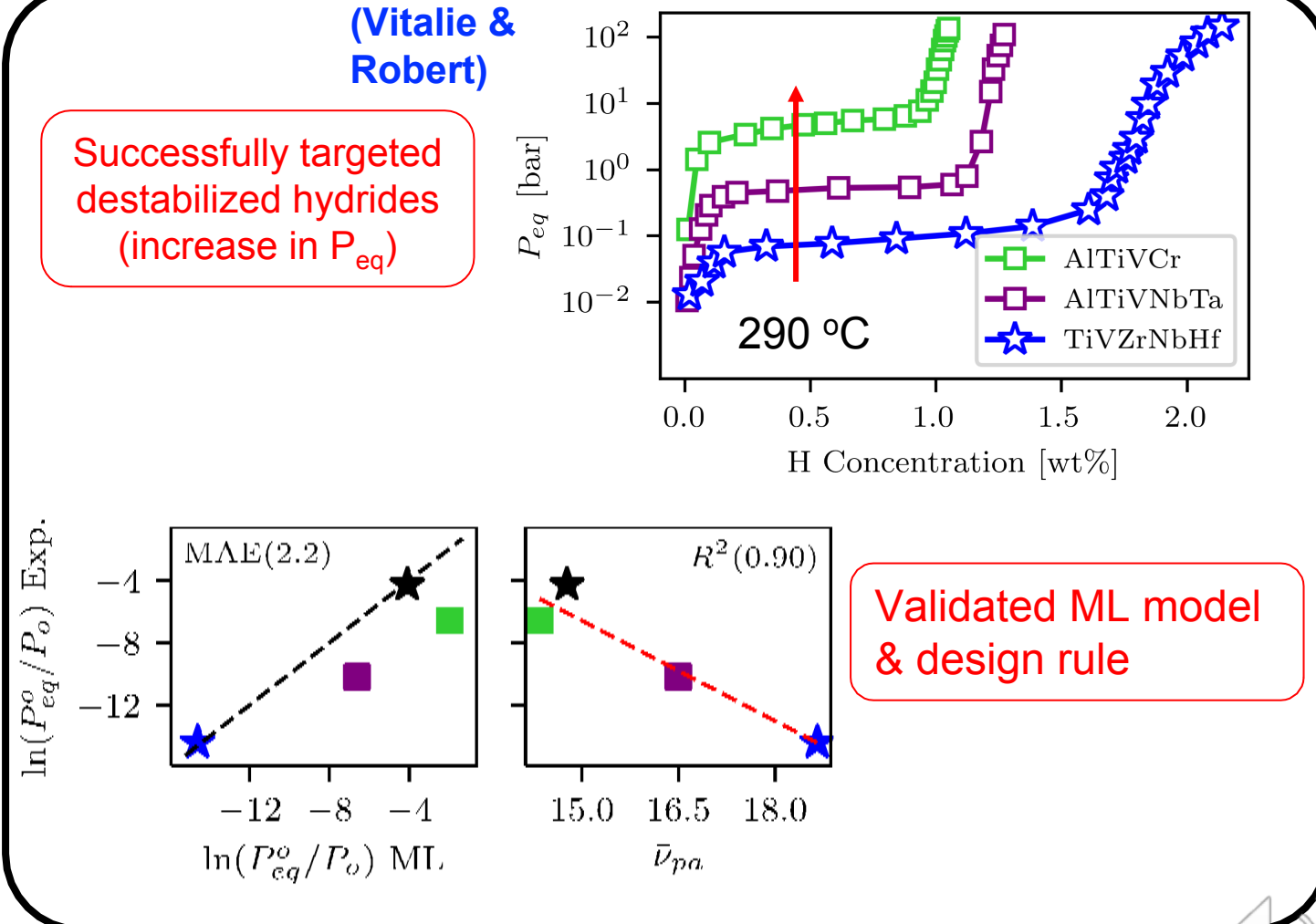
Milestone #2: ML enables discovery of destabilized high entropy alloy (HEA) hydrides



(1) AlTiVNbTa & AlTiVCr synthesis



(2) ML model & design rule confirmed by PCT experiments





Investigating thermodynamic trends with Density Functional Theory

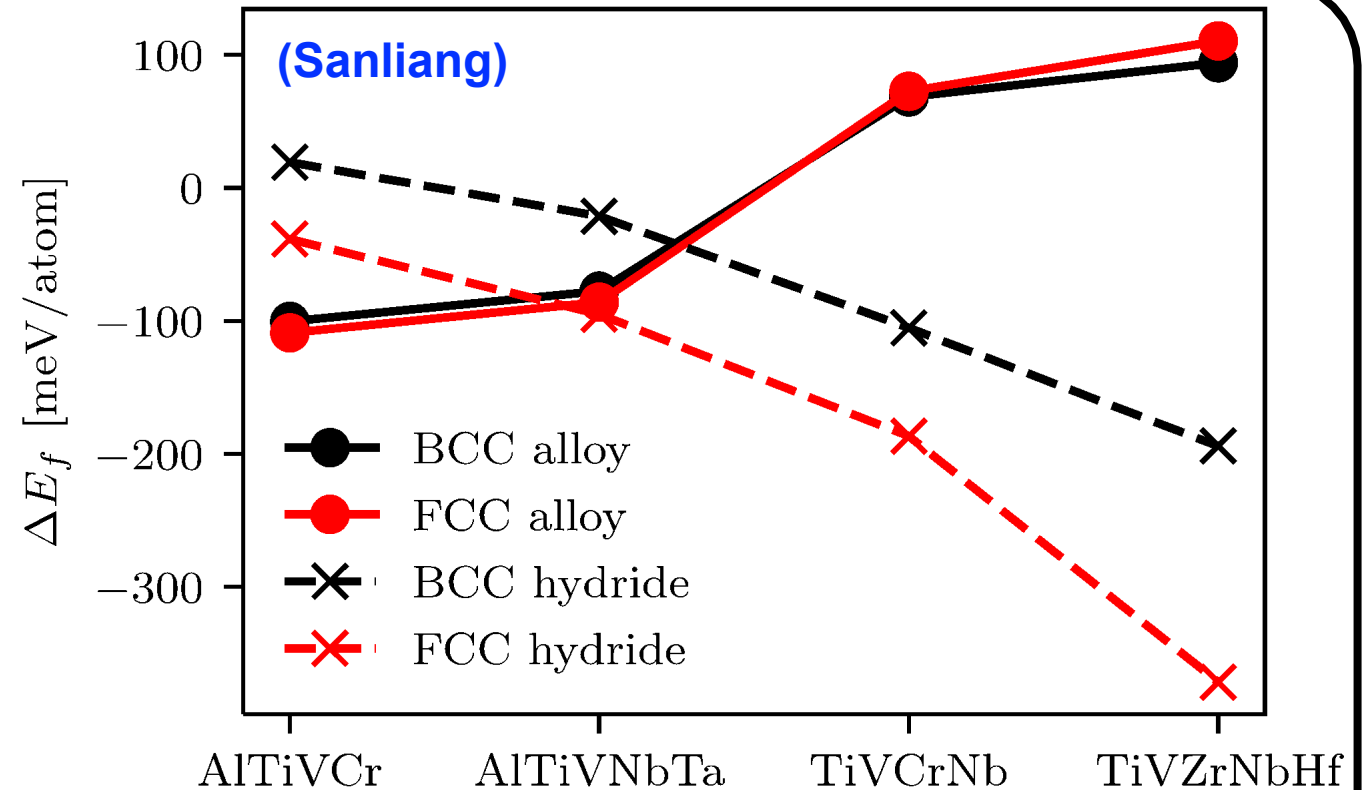
Compute 0K formation enthalpy of alloy and hydride for single HEA config.:

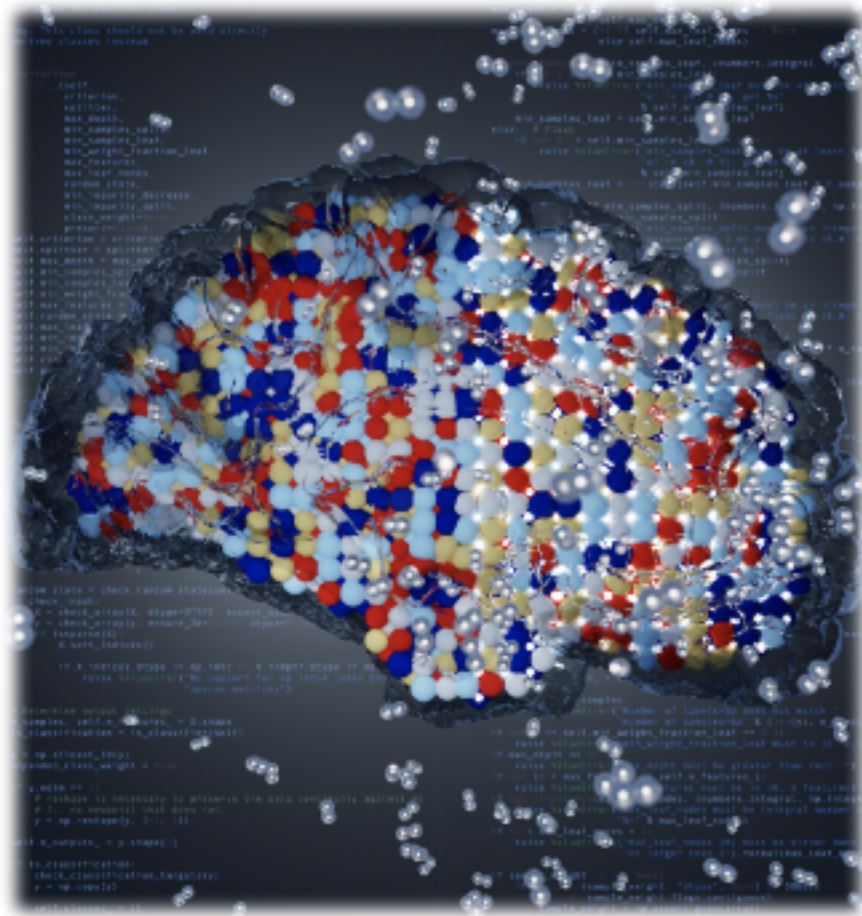
$$\Delta E_{f,\text{alloy}} = \frac{1}{N} (E_{\text{alloy}} - \sum_{i \in \{\text{alloy}\}} E_i)$$

$$\Delta E_{f,\text{hydride}} = \frac{1}{N} \left(E_{\text{hydride}} - \left(\frac{N}{2} \right) E_{\text{H}_2} - \sum_{i \in \{\text{alloy}\}} E_i \right)$$

Analysis Reveals:

- Enthalpic driving force for BCC alloy → FCC transition @ high H/M ratios
- The general correlation of less stable lattice = more stable hydride (similar to \bar{v}_{pa} design rule)



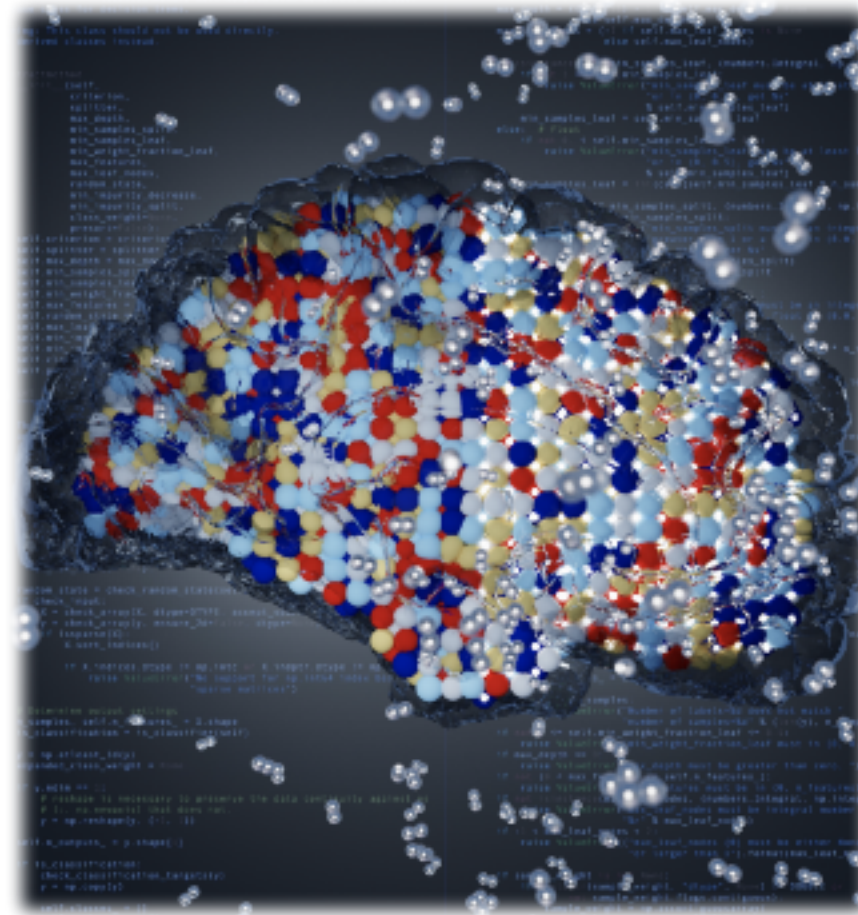


Conclusions:

- Introduced a powerful ML capability for high-throughput screening
- ML-directed and experimentally validated synthesis of HEA hydrides
- DFT-enabled insights into thermodynamic trends



Milestone #3: ML screening & identification of *Pareto* optimal HEA hydrides



Milestone #3: ML screening & identification of Pareto optimal HEA hydrides

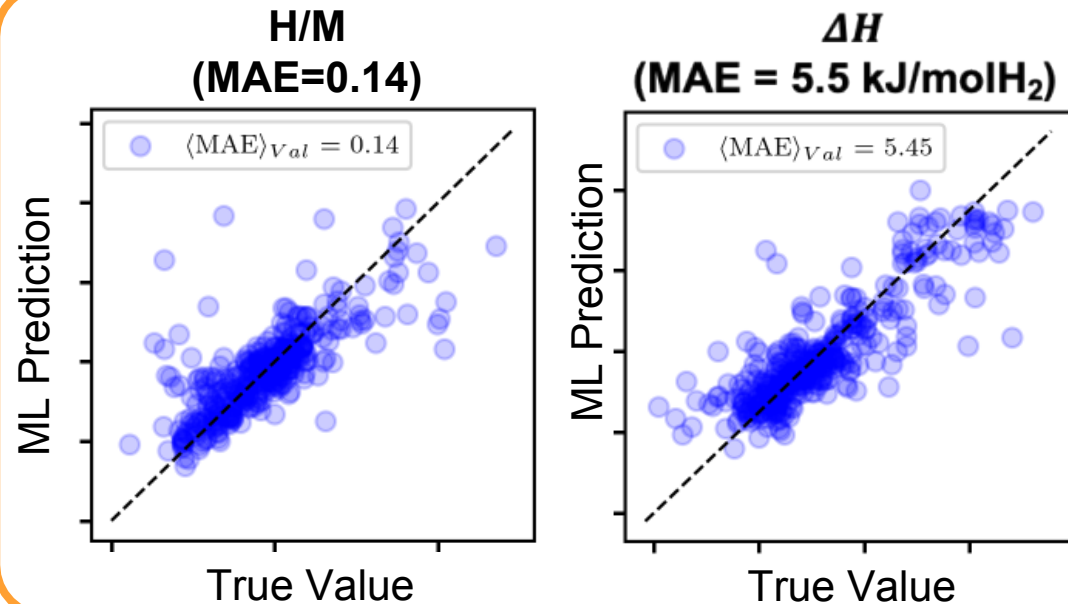


(1) Screening an expansive HEA space

$E = \{\text{Mg, Al, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Zr, Nb, Mo, Pd, Hf, Ta}\}$

$$\binom{E}{4} + \binom{E}{5} + \binom{E}{6} \rightarrow 20,944 \text{ compositions}$$

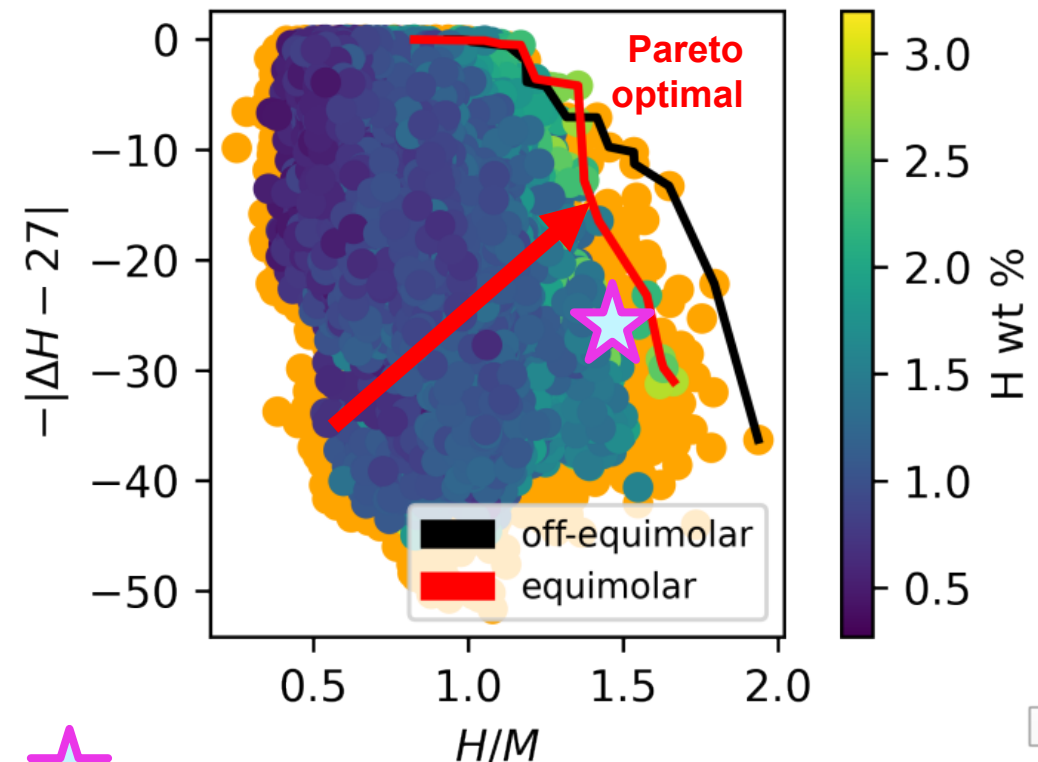
(2) Multiple ML property predictions



(3) Identification of ~100 Pareto optimal materials for stationary storage

Objectives / Quantity to maximize:

- Optimal thermodynamics $\rightarrow -|\Delta H - 27|$
- High volumetric capacity $\rightarrow \text{H/M}$
- High gravimetric capacity $\rightarrow \text{Hwt\%}$
- Raw material cost $\rightarrow -\text{cost}$



★ = Experimental validation (Claudia & Anis)

Milestone #3: ML screening & identification of Pareto optimal HEA hydrides

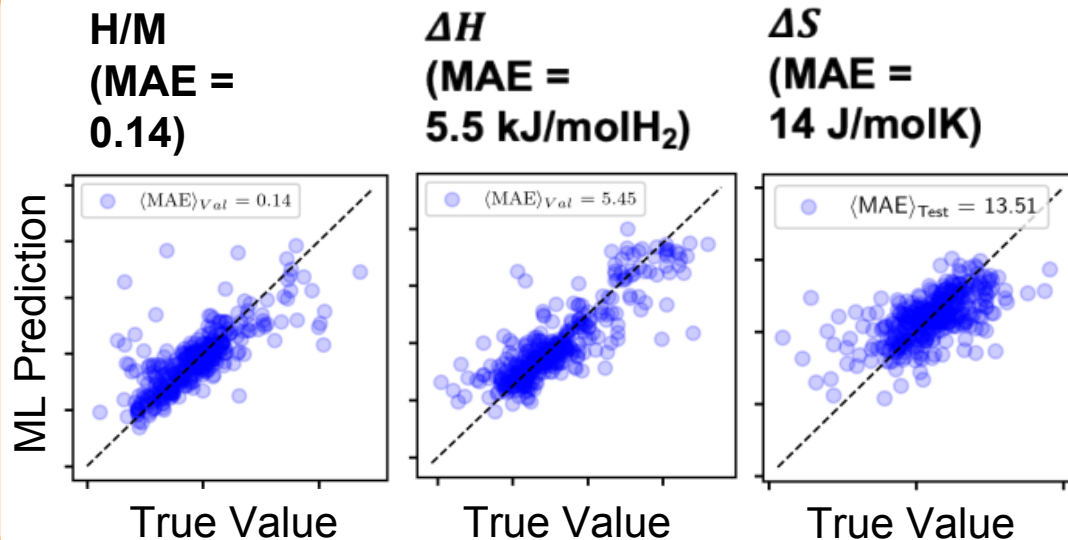


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(2) Multiple ML property predictions

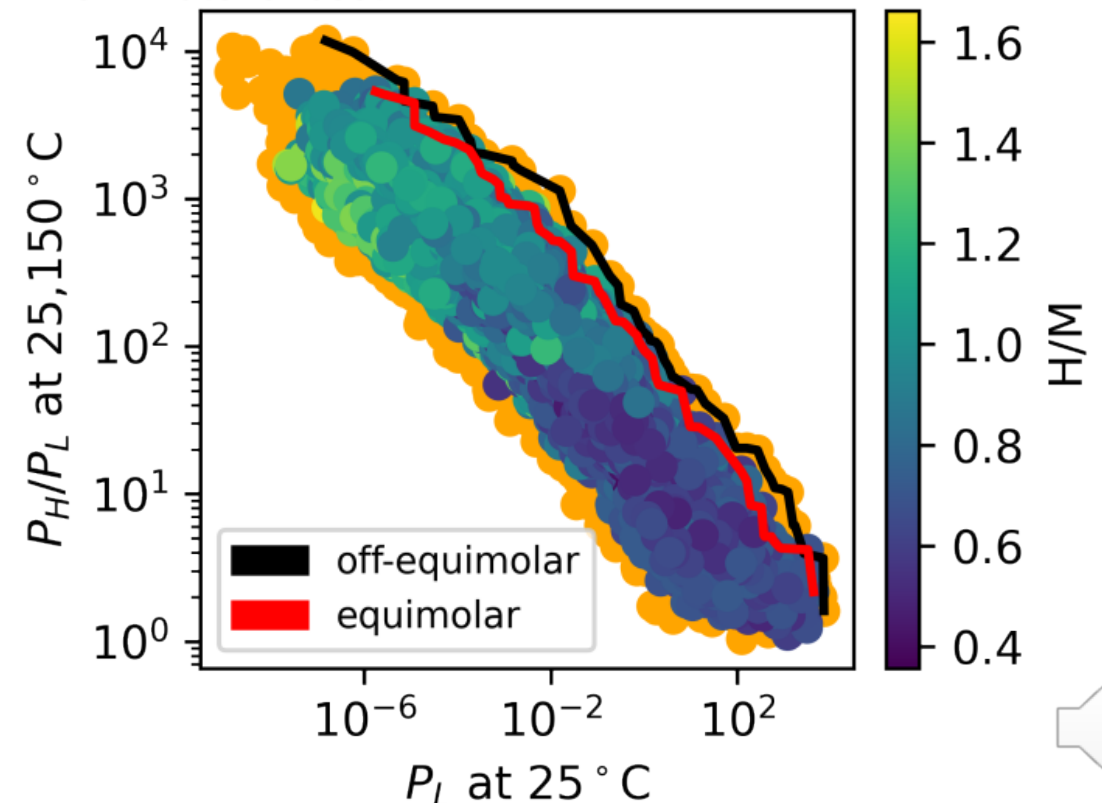


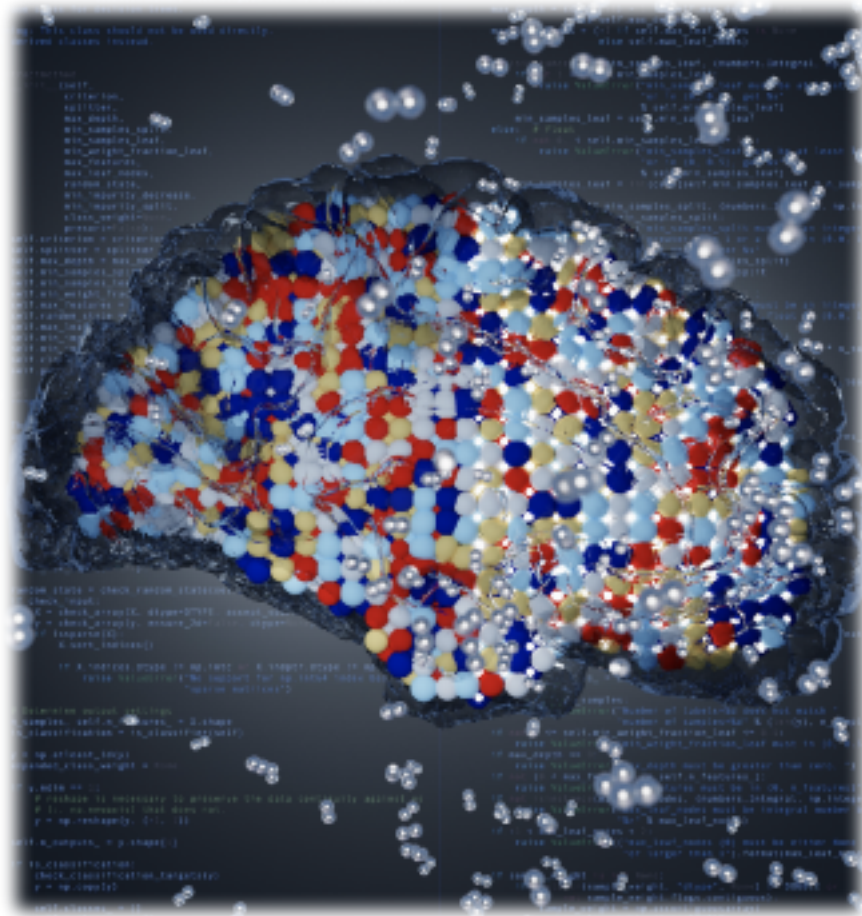
In preparation

(3) Identification of ~100 Pareto optimal materials for hydrogen compressors

Objectives / Quantity to maximize:

- $P_{eq} @ T_L = 25 \text{ C}$ → P_L
- Compression ratio @ $T_H = 150 \text{ C}$ → P_H/P_L
- High volumetric capacity → H/M
- Raw material cost → -cost





Conclusions:

- Given a set of ML models for various hydride properties, Pareto frontiers can be determined
- Random off-equimolar perturbations substantially advance the Pareto frontier, indicating potential for future improvement
- We have highlighted (with experimental validation pending) Pareto optimal compressor and stationary storage materials





Future Work:

Overcoming barriers to ML-driven hydride discovery
(e.g. how to deal with limited data)



More/Better Experimental Data: Promoting standardization, reproducibility, and community-based “high-throughput” data acquisition

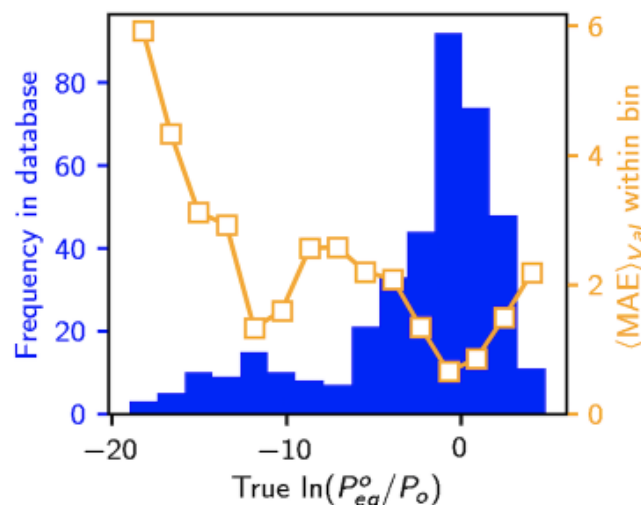
Challenge: Accuracy and accessibility of HydPARK data

Lack of updatability: data stored in “offline” CSV file

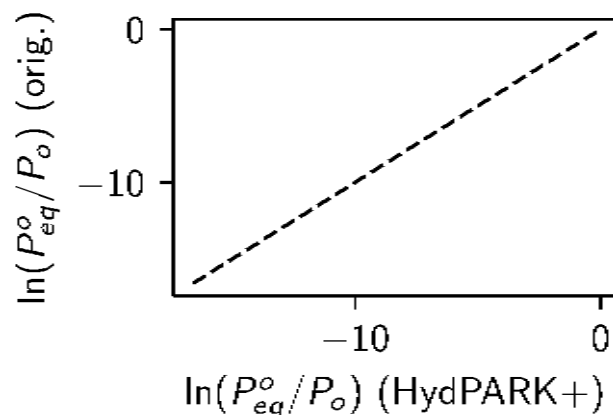
Lack of completeness: **15%** of HydPARK entries are usable

Lack of consistency: different values for identical materials

Very non-uniform distribution of target



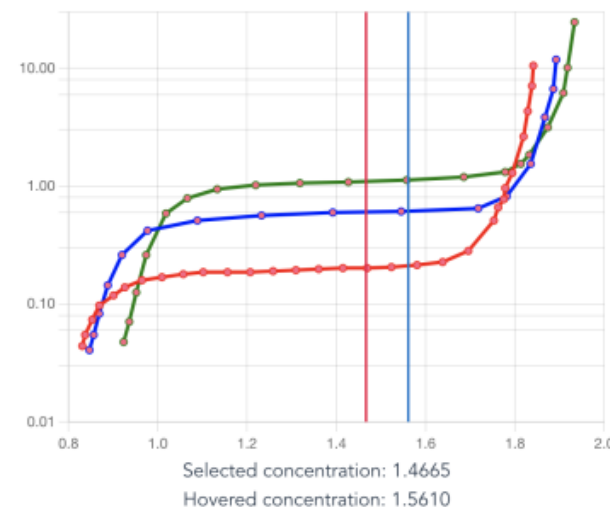
Addition of new data systematically shifts predictions



Solution: NREL DataHub app and backend for standardized PCT upload and storage

File Name	Temperature (from metadata)	CSV Parse Result
des1_348K.csv	348	Success
des2_373K.csv	373	Success
des3_388K.csv	388	Success

Save these CSVs to DataHub



Much faster data acquisition than can be achieved by one group alone

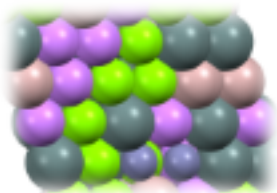
More/Better Computational Data: If experimental measurements and physics-based simulation are too expensive, accelerate the latter with ML

Challenge: Need an accurate, many-element potential energy surface (PES) for simulations (MD or MC)

PES choices: Force Field ,



Not necessarily transferable/generalizable



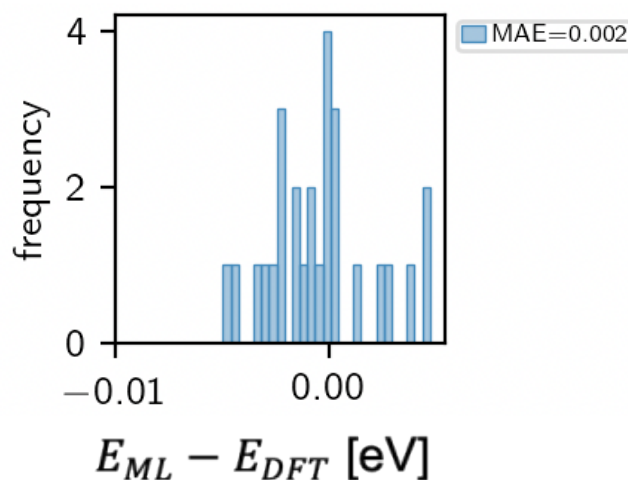
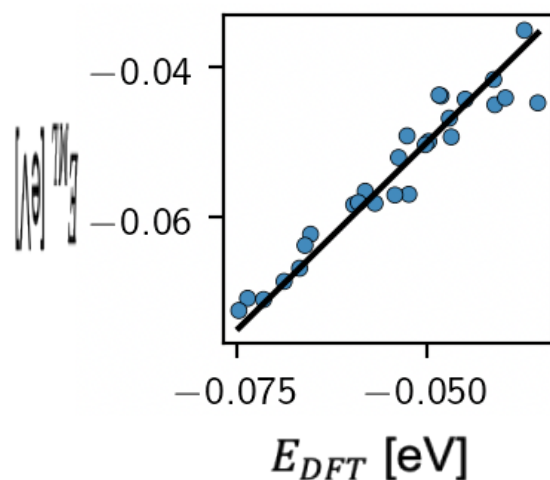
ML PES,



DFT



Too expensive for extensive sampling in complex systems



Solution: Direct atomistic simulation & screening of metal hydride thermodynamics?





Thank you for your attention.

Questions?

Contact: mwitman@sandia.gov

