

23 between 48–57% of the total strength up to 600 °C, the primary influence on the high temperature strength
24 of superalloy 718. The strength factors for γ'' and δ precipitates were found to trend inversely with tensile
25 test temperature and may be attributable to the differences in precipitate coherency. A post-build heat
26 treatment is recommended to maintain high strength at elevated temperatures. A quantitative
27 microstructure-property relationship, dependent on precipitate size, density, and morphology, was derived
28 and can estimate the yield strength across a wide temperature range applicable to the operational regimes
29 for superalloy 718.

30 Key words: Alloy 718, heat treatment, precipitation, tensile properties, laser powder bed fusion

31 **1. Introduction**

32 Ni-based superalloys are a primary candidate alloy class for high-temperature applications in the
33 petrochemical, aerospace, and nuclear power industries because of their intrinsic resistance to creep, their
34 adequate corrosion resistance, and the ability to tailor the microstructure for high strength [1,2]. These
35 high-strength Ni-based alloys gain their strength primarily through solid solution strengthening and/or
36 secondary precipitating phases in the lattice [3], such as the intermetallic phases δ , γ' , or γ'' . The poor
37 machinability and extensive work hardening of Ni-based superalloys makes additive manufacturing (AM)
38 an attractive option to produce geometrically complex components. Powder bed fusion – laser beam (PBF-
39 LB) is an AM process used to build parts through sequential application of thin layers (20–100 μm) of metal
40 feedstock powder melted by a scanning laser, resulting in rapid solidification and thermal cycling, and has
41 been used to produce parts from a Ni-based superalloy, 718 [4–6].

42 Despite the continual improvement in processing parameters, the microstructures of AM materials
43 typically contain a high density of pores and other nonequilibrium features that encourage the use of post-
44 fabrication heat treatments [5]. Like alloy 718, many nickel superalloys have compositions that allow for
45 the formation of many different precipitating phases, all of which may result from PBF-LB. Several of these
46 appear to be beneficial for the alloy at high temperatures (γ' and γ''), whereas alternative phases (δ and
47 Laves) are detrimental [7,8]. Post-build heat treatments typically include direct aging, solution annealing,
48 hot isostatic pressing (HIP), or a combination [9–13] in an attempt to produce a high strength component

49 [14]. The literature of post-build heat treatments show varying degrees of success [6,15,16] to achieve a
50 yield strength in the range of 800 - 1300 MPa at room temperature but with visible δ and Laves particles
51 [17]. In many cases, an additional step of a high temperature homogenization at 1100 °C or greater was
52 needed to result in high strength [18,19] and does not always eliminate the Laves phase [20–22] or porosity
53 [23]. For a comprehensive review, the reader is referred to a recent article [24] on laser bed fusion of Ni-
54 based superalloys highlighting many of the processing parameter studies, heat treatments, and properties
55 from which this study was pursued, and the challenges with unpredictable heat treatments for precipitation
56 hardening. Although high strength can be recovered at room temperature, very few studies demonstrate
57 success over the wide operating temperature regime from room temperature to 650 °C for superalloy 718.
58 There is still a need to determine a post-processing heat treatment of additively manufactured superalloy
59 718 that results in high strength at the elevated temperatures expected during service and eliminates
60 detrimental phases.

61 Furthermore, as the strength of the 3D-printed component depends on the nanoscale particles that
62 develop during the repetitive heating and cooling cycles associated with AM, there is a significant need to
63 understand how each precipitate that can be formed from AM contributes to the overall strength of the
64 alloy. The objectives of this study are 1) to demonstrate the combination of a two-step post-build high
65 temperature normalization and aging heat treatments on the microstructure and mechanical properties of
66 alloy 718, and 2) use the post-heat treatment properties to determine the strength contribution of nanoscale
67 precipitating phases to the overall mechanical properties of Superalloy 718 through a combination of
68 electron microscopy and uniaxial tensile straining. The results of this study will be used to recommend a
69 post-build heat treatment and provide a physically informed equation connecting the microstructure and
70 yield strength across elevated temperatures for modeling and simulation. Superalloy 718 was characterized
71 in the as-built condition, and with multiple heat treatments, to form δ precipitates, as well as γ' and γ''
72 precipitates at multiple length scales using scanning electron microscopy (SEM) and transmission electron
73 microscopy (TEM) to correlate the microstructure to the bulk properties. Uniaxial tensile tests were
74 performed under conditions ranging from room temperature to 600 °C on subsize specimens to determine

75 the common engineering properties of yield strength, elastic modulus, ultimate tensile strength, uniform
76 elongation, and total elongation. An Orowan dispersed barrier hardening model was used to assess the
77 contributions of microstructural features to the yield strength as a function of tensile test temperatures, and
78 from the calculated trends, to elucidate the role of precipitate coherency on tensile strength. The
79 microstructure-property relationship derived from this work can be used to estimate the yield strength of
80 wrought and AM superalloy 718 components across a wide temperature range applicable to the operational
81 regimes for nickel superalloys.

82 **2. Methodology**

83 2.1 Composition, Fabrication and Heat Treatments

84 The additively manufactured superalloy 718, designated AM718, used in this investigation was
85 printed in one build cycle by using PBF-LB on the Concept X-Line 2000R at the Manufacturing
86 Demonstration Facility (MDF) at Oak Ridge National Laboratory (ORNL, build ID: 20200206XL) using a
87 powder with the composition listed in Table 1 with process parameters of a laser power of 370 W, spot size
88 of 300 μm , scanning speed of 500 mm/s, and hatch spacing of 0.16 mm with 67° rotation between layers. The
89 plate was sectioned into four pieces: three for subsequent heat treatments, and one for the as-built (ASB)
90 microstructure. Three heat treatments, summarized in Table 2 and shown schematically in Figure 1 with the
91 time-temperature-transformation (TTT) diagram for superalloy 718, were designed to reduce the complexity
92 of the AM microstructure and to allow for comparative analysis of the microstructure and mechanical
93 properties. Based on the work performed by Poole et al. [25] to identify the δ and Laves phase solvus
94 temperatures, a two-step homogenization treatment of 1,174 °C for 2 h followed by 1,204 °C for 6 h was
95 chosen to remove all secondary phases, including the detrimental Laves phase that typically forms during AM
96 and competes with δ , γ' , and γ'' precipitates for Nb [14]. Annealing further at 1,093 °C for 1 h with no
97 additional heat treatments provides a reference case solution-annealed alloy 718 with minimal precipitation,
98 designated as AM718-HM. The extensive knowledge of the precipitation in alloy 718 [26–30] led to the
99 adoption of a standard heat treatment to produce δ precipitates that consists of solution annealing at 945 °C
100 followed by aging at 718 °C and then 621 °C for 8 hours at each step, shortened to 945 °C/718 °C/621 °C

101 [30–32], and designated as AM718-HT1. A higher temperature heat treatment of 1,093 °C/718 °C/621 °C
 102 was chosen to form a large density of small γ' and γ'' precipitates based on the work performed in [8,30,31],
 103 designated as AM718-HT2. A traditional wrought alloy 718, designated W718 heat Z1653 was prepared
 104 according to ASTM specifications [33], was used as a control, and was compared with the AM specimens.
 105 However, as demonstrated further in the article, the same heat treatment for AM718-HT2 and W718 resulted
 106 in distinct microstructures and mechanical properties. and the reader is referred to the Appendix for more
 107 details. After heat treatment, specimens were fabricated into the form of SS-J2 subsize tensile specimens [34],
 108 displayed in Figure 2, for uniaxial tensile tests with a gauge 5 mm long, 0.5 mm thick, and 1.2 mm wide using
 109 electrical discharge machining (EDM). The SS-J2 geometry was chosen to minimize the amount of material
 110 needed for testing, provide adequate tensile property measurements [35], and allow for future studies in which
 111 subsize specimens will be used. Each specimen was individually engraved via a laser with a unique ID for
 112 tracking from the original build plate to the tensile specimen. Previously obtained results for room temperature
 113 properties and preliminary characterization were reported by Taller et al. [36], from which this manuscript
 114 builds.

115

116 **Table 1. Composition of superalloy 718 powder used for PBF-LB in wt % provided by the vendor for Lot 119 and a**
 117 **commercially purchased wrought superalloy 718 for comparison as measured with x-ray fluorescence.**

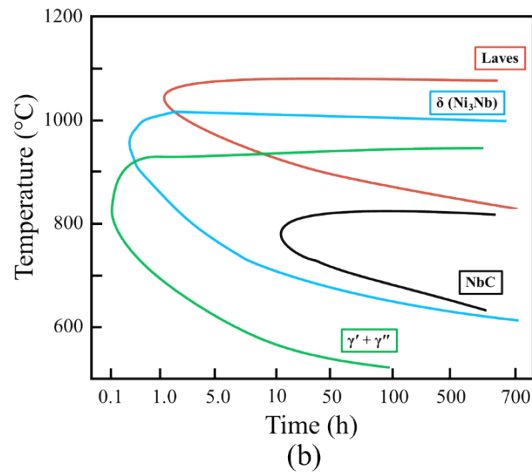
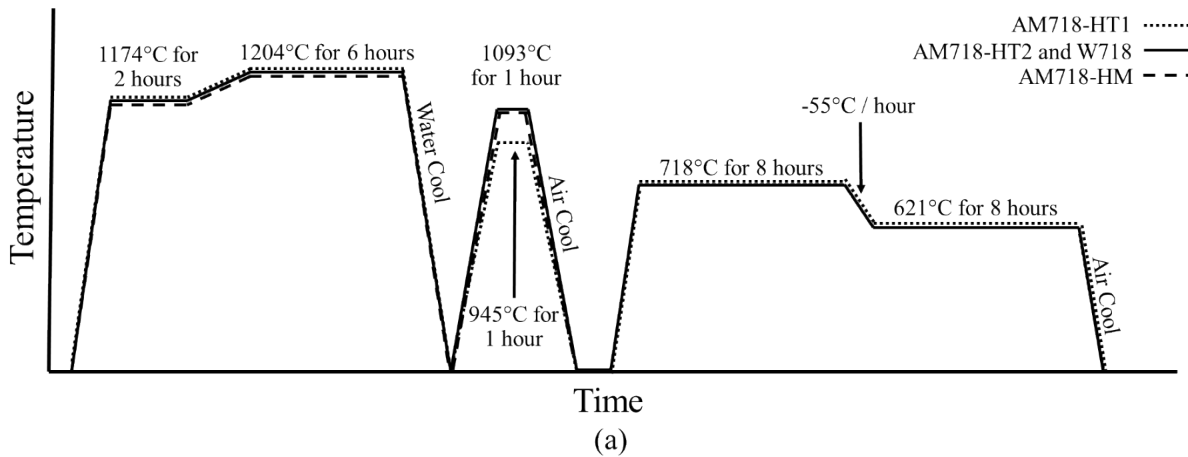
Designation	Ni	Fe	Cr	Nb	Mo	Ti	Al	Si	C	N	O	Co	B	Mn	P	S
AM718-Lot 119	Bal.	18.22	18.99	5.15	3.0	0.93	0.50	0.04	0.04	0.012	0.016	0.1	0.001	0.02	0.006	0.001
W718-Z1653	Bal.	18.77	17.56	5.18	2.89	0.94	0.49	0.08	0.02	-	-	0.05	0.004	0.03	0.008	<0.00 03
ASTM-B670 Reference [37]	50.0 – 55.0	Bal.	17.0 – 21.0	4.75 – 5.50	2.8 – 3.3	0.65 – 1.15	0.2 – 0.8	0.35 max	0.08 max	- -	- -	1.0 max	0.006 max	0.35 max	0.015 max	0.015 max

118

119 **Table 2. Heat treatments for AM718 and W718 to produce increasingly simpler microstructures for characterization and**
 120 **mechanical property measurement.** The cooling between steps was performed using either water cooling (WC) or air cooling
 121 (AC).

Designation	Homogenization (°C/h)	Cooling	Solution anneal (°C/h)	Cooling	Aging #1 (°C/h)	Cooling rate to reach aging #2 (°C/h)	Aging #2 (°C/h)	Cooling rate to room temp.
W718-Z1653	1174/2+1204/6	WC	1093/1	AC	718/8	55	621/8	AC
AM718-HT1	1174/2+1204/6	WC	945/1	AC	718/8	55	621/8	AC
AM718-HT2	1174/2+1204/6	WC	1093/1	AC	718/8	55	621/8	AC
AM718-HM	1174/2+1204/6	WC	1093/1	AC	N/A	N/A	N/A	N/A

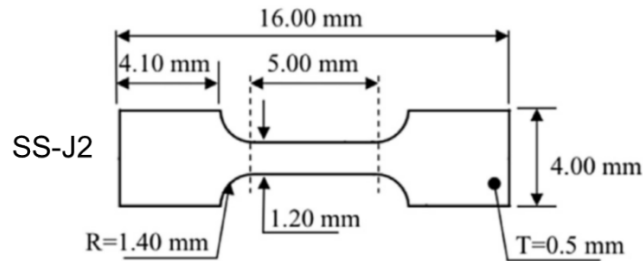
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123

124 **Figure 1. The (a) time-temperature diagram for the heat treatments in this study with (b) a TTT diagram for alloy 718**
125 **derived from [8,38,39].**

126



127

128 **Figure 2. Schematic of the subsize tensile specimens with appropriate dimensions.**

129

130 2.2 Microscopy

131 Prior to characterization, standard metallographic grinding using successively finer grits of SiC
132 paper and polishing using diamond solutions with successively decreasing particle sizes of 6 μm , 3 μm , and
133 0.25 μm were performed until a mirror-like surface was achieved with $\sim 0.02 \mu\text{m}$ silica particles. Surface
134 characterization was performed on a Tescan MIRA3 GHM scanning electron microscope (SEM) using 20
135 keV electrons. Electron backscatter diffraction (EBSD) Kikuchi band patterns were collected on an Oxford
136 Instruments Symmetry EBSD detector with AZtec software using a step size of 1 μm . At each point, the
137 AZtec software indexes the Kikuchi band structure and determines the Euler angles of the lattice. The open
138 source MTEX toolbox [40] was used to generate orientation maps and inverse pole figures and to determine
139 grain sizes from the Euler angles exported from AZtec for grains consisting of more than 5 pixels. The
140 equivalent grain diameter was calculated by taking the area of the grain determined by the orientation map
141 and assuming a circular area through Eq. (1):

$$142 \quad d_{eq} = 2\sqrt{\frac{A}{\pi}}. \quad (1)$$

143 TEM lamellae were prepared on an FEI VersaTM NanolabTM 650 or an FEI QuantaTM NanolabTM
144 focused ion beam (FIB) system by using standardized lift-out procedures. Each lamella was made with a

145 thick window frame to minimize foil bending and twisting during sample thinning below a thickness of
146 ~300 nm. Low-energy Ga ion beams at 2 and 5 keV were used to thin the ~150 nm thick lamella to a final
147 thickness of around 80–100 nm, which effectively eliminated the TEM-visible FIB damage induced at high-
148 beam energy. For each condition, two lamellae were extracted from different grains comprising of at least
149 $25 \mu\text{m}^2$ of electron transparent area to assess uniformity.

150 The nanoscale microstructure for each heat treatment of AM718 and W718 was characterized by
151 using the FEI Talos F200X scanning transmission electron microscope (STEM) instrument equipped with
152 high counting rate electron dispersive spectroscopy (EDS). Before imaging and EDS spectra collection, the
153 lamella was tilted to a low-order zone axis such as the (001), and the collection angles were optimized.
154 Each STEM image set consisting of Bright Field (BF), Dark Field (DF), and High Angle Annular Dark
155 Field (HAADF) images was collected with a region of interest size of $2,048 \times 2,048$ pixels with a resolution
156 of ~0.7 nm/pixel. Additional images were collected as needed at a higher resolution of 0.16 nm/pixel to
157 confirm the precipitate structure and composition. EDS-based spectrum images for precipitate measurement
158 were taken over a broad area by using a region-of-interest size of $1,024 \times 1,024$ pixels with a resolution of
159 ~1.3 nm/pixel, a probe full-width half-maximum of ~1.5 nm, and a beam current of around 3 nA. Each scan
160 had a duration of 1 h, with more than 35,000 counts/s and dead times from 1–6%. The qualitative x-ray
161 counts were converted to quantified weight percentages by using the Cliff-Lorimer [41] method for
162 calculation at each pixel.

163 Each corresponding collection of STEM images and EDS spectrum images was characterized for
164 nanoscale features. Precipitates were identified by using the composition expected for each phase [38] and
165 overlaying the corresponding EDS maps for the elements of interest in the phase. Phase identification was
166 assisted using a trained dynamic segmentation convolutional neural network [42]. Each feature was
167 annotated by the neural network and designated as belonging to a class. These annotations were used to
168 produce an image in which the type of feature present at any given pixel was labeled by a class number.
169 Each feature class was individually filtered out of the image and analyzed by using the particle analysis
170 function in FIJI [43] to obtain parameters for the area, perimeter, minimum width, maximum width, and

171 circularity for each feature present. When features were found to overlap in the two-dimensional image, the
172 features were separated manually and confirmed using hand counting procedures. An equivalent diameter
173 for each feature to use with the dispersed barrier hardening model was calculated using Eq. (2). The mean
174 and standard error of the mean for the equivalent diameter were calculated for each identified feature of the
175 microstructure.

176
$$d_{eq} = \sqrt{major\ axis \times minor\ axis}. \quad (2)$$

177
178 **2.3 Uniaxial Tensile Testing**

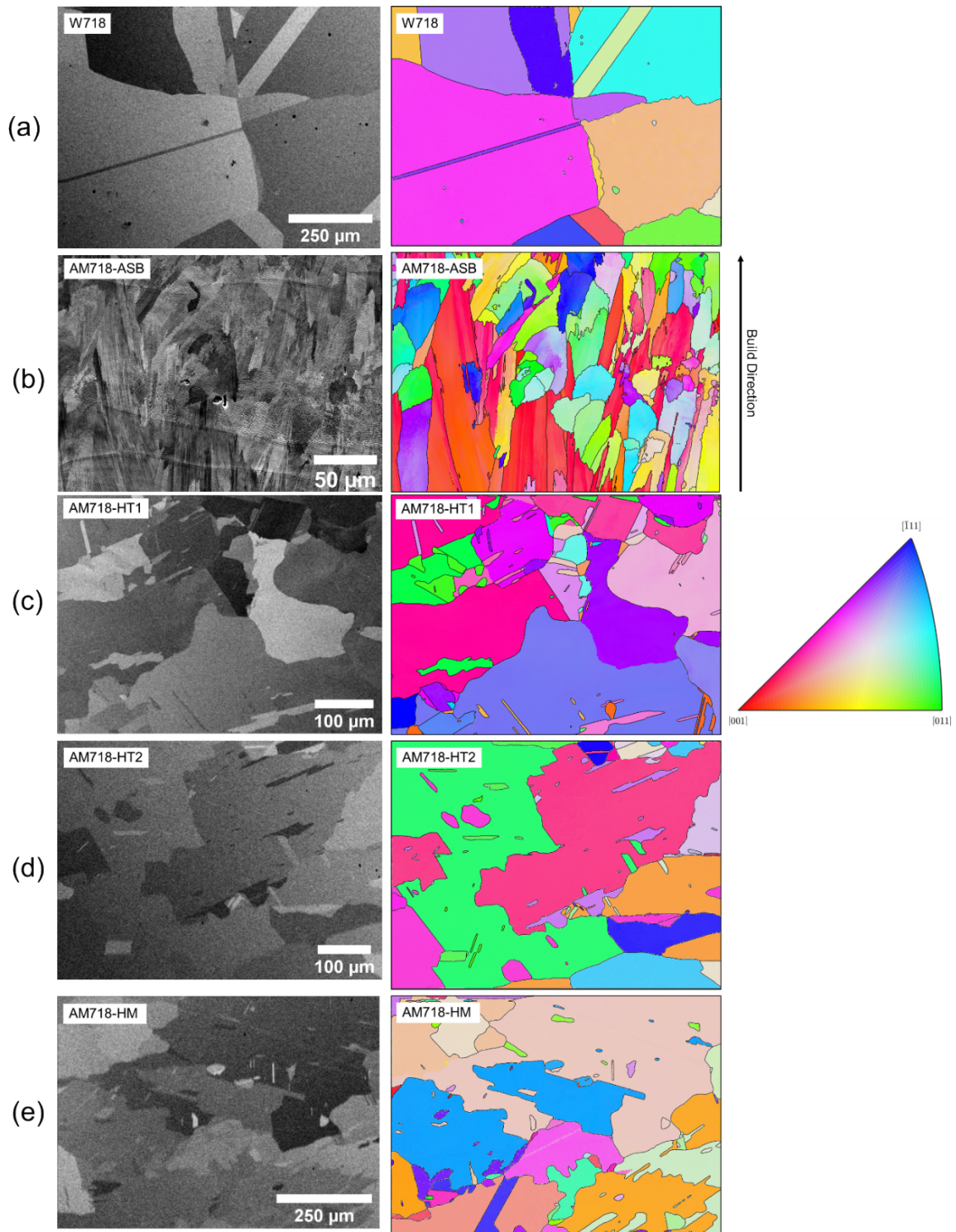
179 Subsize SS-J2 specimens were tested for common engineering properties by using uniaxial tensile
180 straining. Five specimens of each heat treatment of the AM718 and W718 were strained at room
181 temperature, 300 °C, 450 °C, or 600 °C. Tensile straining was conducted according to ASTM E8/E8M for
182 room temperature and ASTM E21-20 for elevated temperatures on an MTS Systems uniaxial test frame.
183 The straining was maintained at a crosshead displacement of 0.15 mm/min for a strain rate of $5 \times 10^{-4} \text{ s}^{-1}$ to
184 avoid complications typical at high strain rates [44]. Specimens were strained to failure at the test
185 temperature.

186 **3. Results**

187 **3.1 Grain size determination**

188 Representative foreshatter SEM images and corresponding colored EBSD orientation maps are
189 shown in Figure 3. The wrought alloy 718 displayed the expected microstructure consisting of large grains
190 with an average equivalent grain diameter of $106 \pm 21.8 \mu\text{m}$ gathered from three areas containing 229 grains
191 and with interior annealing twins. For AM718, the as-built microstructure consisted of elongated grains that
192 showed a preferred orientation along the build direction, resulting in an average equivalent grain diameter
193 of $8.3 \pm 0.22 \mu\text{m}$ from 10 areas containing 3732 grains. The grain size distributions normalized by the total
194 number of grains observed for the AM718 in the as-built and heat-treated conditions are shown in Figure
195 4. With the application of the homogenization heat treatment and subsequent solution anneal, incomplete

196 recrystallization occurred, leading to a mixture of large and small grains in the heat-treated AM conditions
197 and average equivalent grain diameters of $24.6 \pm 2.5 \mu\text{m}$ gathered from three areas containing 342 grains
198 for AM718-HT1, $29.4 \pm 2.8 \mu\text{m}$ gathered from three areas containing 315 grains for AM718-HT2, and
199 $37.9 \pm 2.6 \mu\text{m}$ gathered from three areas containing 442 grains for AM718-HM. However, the skewness
200 of the distributions may make the median a more relevant parameter which results in median equivalent
201 diameters of 3.1, 9.9, 12.5, and $18.8 \mu\text{m}$ for AM718-ASB, AM718-HT1, AM718-HT2, and AM718-HM,
202 respectively, and $62.7 \mu\text{m}$ for W718. With each heat treatment, the tail of the grain size distributions
203 extended to larger sizes, but the subsequent aging steps did not significantly increase the grain size further.

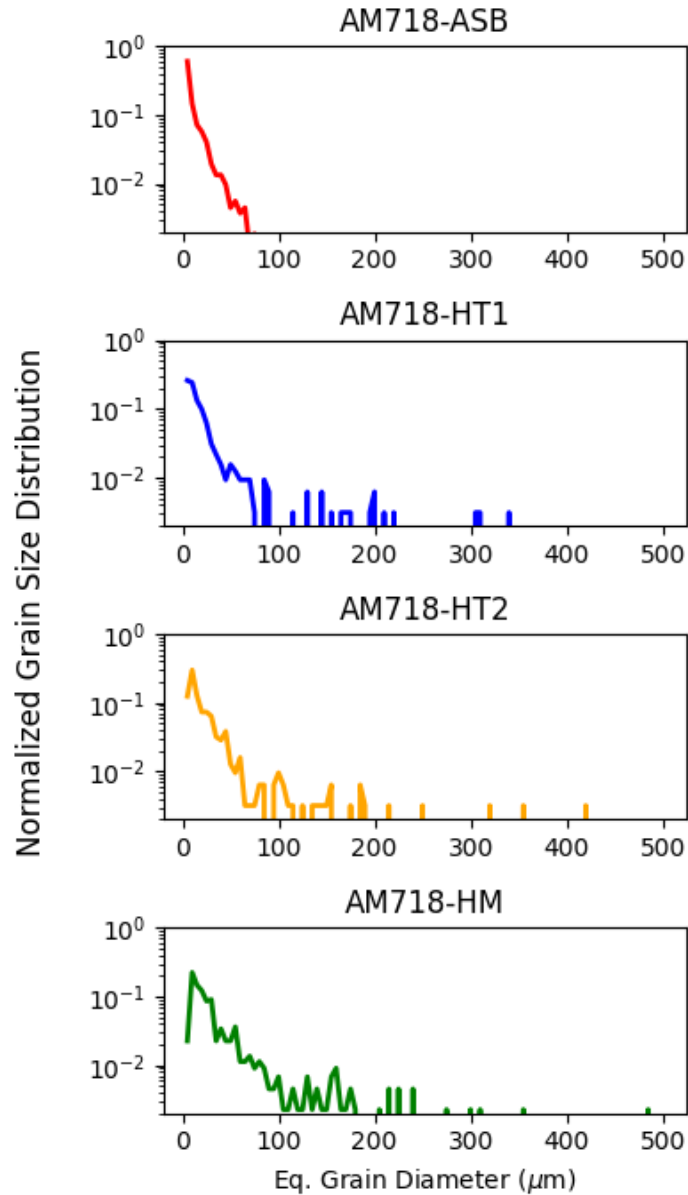


204

205 **Figure 3. Representative foreshcatter electron images and corresponding EBSD orientation maps for (a) W718, (b) AM718-**

206 **ASB, (c) AM718-HT1, (d) AM718-HT2, and (e) AM718-HM.**

207



208

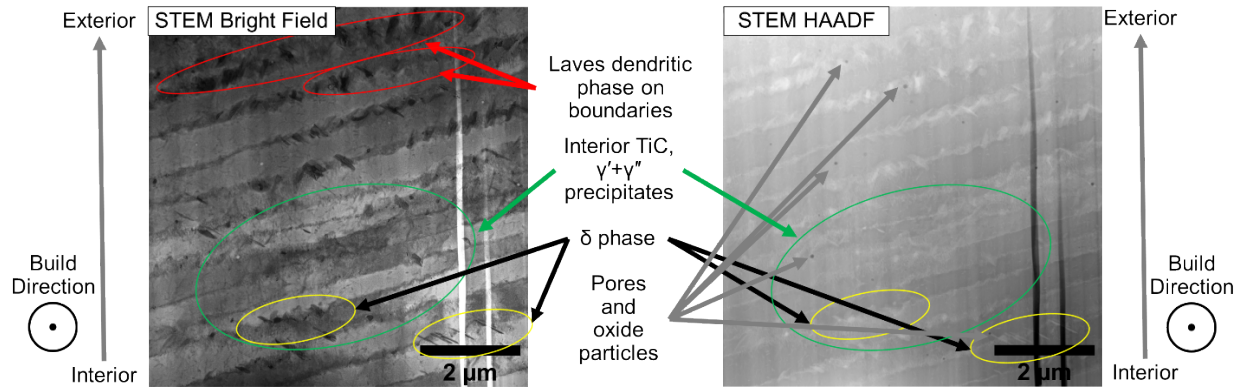
209 **Figure 4. Grain size distributions for AM718 normalized by the total number of grains captured within the EBSD map**
 210 **areas.**

211

212 3.2 Precipitate Characterization Using STEM

213 The first characterization performed was on the ASB superalloy 718. An overview of the
 214 microstructure at the micron scale is shown in Figure 5, in which the print direction is out of the page. The
 215 grain structure consisted of fine lath-like boundaries decorated with Nb-rich precipitates. Toward the part

216 exterior, the Laves phase formed as a dendrite, and the δ phase formed on boundaries nearer to the part's
217 interior. For volumes of the part consistently above the δ solvus line at 1,010 °C [45,46], Laves phase
218 formation is preferred as a metastable phase from solidification at high cooling rates, whereas the δ phase
219 forms latter in the fabrication process, likely from the longer time at elevated temperatures, to form the
220 stable phase. At a higher magnification, a high density of γ'' precipitates was observed in the vicinity of
221 larger δ phase particles (Figure 6), which is consistent with previous observations from AM-fabricated
222 superalloy 718 [47] and as-cast wrought alloy 718 [46]. The time-temperature-precipitation diagram
223 suggests that at higher temperatures such as those present during AM, the formation of interdendritic γ''
224 was favored over γ'' interior to the grain [47]. Interspersed throughout the grain interiors was a mixture of
225 fine γ' and γ'' precipitates of a very high density (Figure 7) with the frequency size distributions in Figure
226 8. Two nonoverlapping areas were examined for precipitate formation closer to the part interior to attempt
227 to capture representative microstructures and determine the local heterogeneity in the microstructure. A
228 quantitative summary of the observed microstructure is included in Table 3, including the number of
229 precipitates observed, the percentage that each precipitate phase contributes to the total precipitation, the
230 mean equivalent diameter, the standard error of the mean equivalent diameter, and the number density for
231 each phase. Between the two areas examined, the size and density of γ'' , Laves, and oxide precipitates were
232 found to be nearly identical. However, both γ' and δ showed a large variation in density ($\sim 2\times$) between
233 ASB-1 and ASB-2, with no carbides being observed in ASB-2. Although mechanical properties could be
234 obtained for comparison with this microstructure, it is unlikely to yield correlative results because of the
235 high level of complexity and heterogeneity found in the ASB superalloy 718. Therefore, ASB superalloy
236 718 was excluded from the mechanical testing campaign and is not included in subsequent sections.



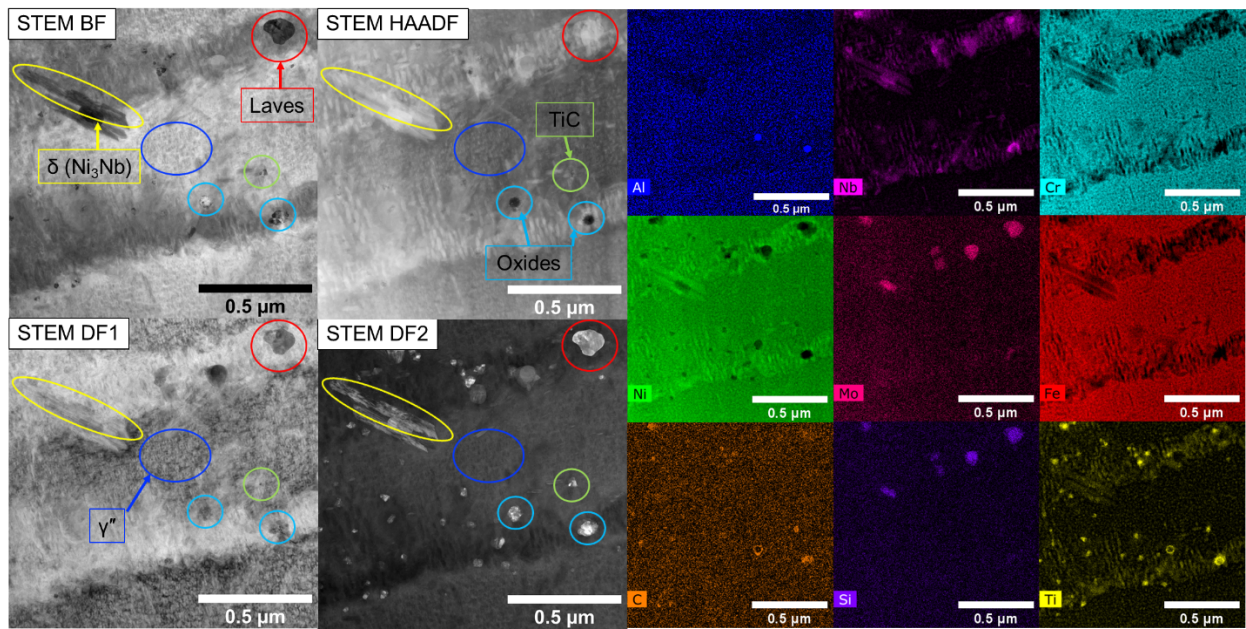
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Figure 5. STEM images of ASB AM Superalloy 718 showing dendritic Laves phase, large δ precipitates, TiC, pores, oxide particles, and γ' and γ'' precipitates as a function of distance from the part surface. Note the build direction vector is directed out of the page towards the viewer.



241

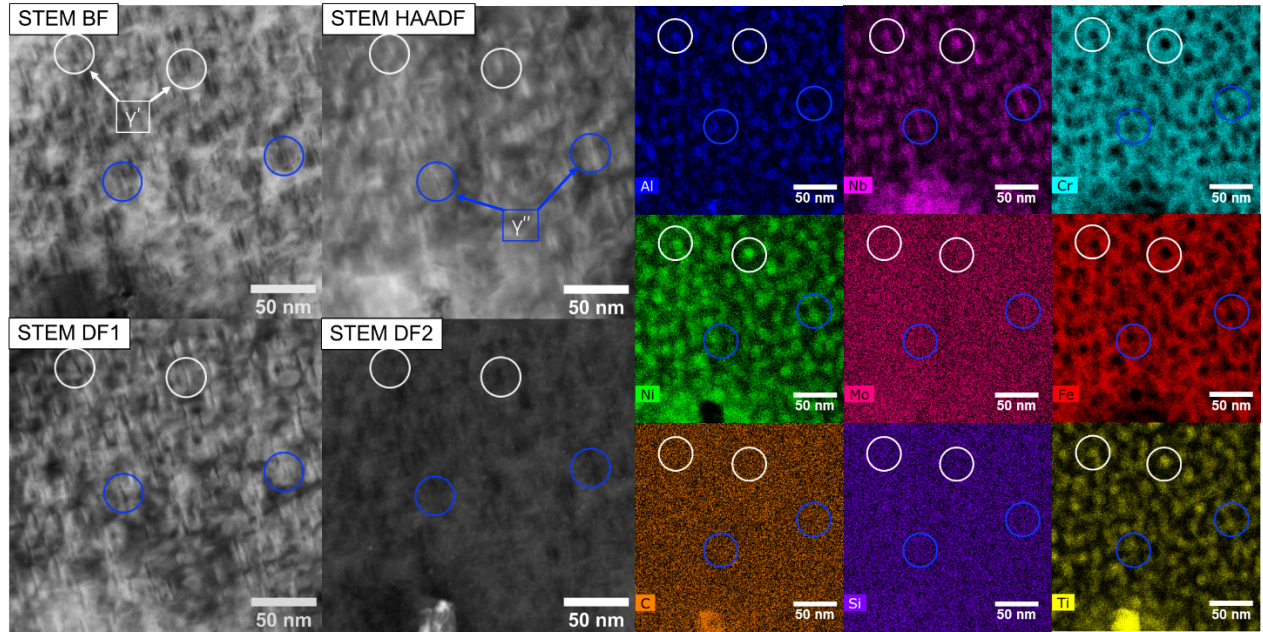
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Figure 6. STEM images of ASB AM Superalloy 718 with corresponding EDS maps for precipitate-forming elements showing large δ precipitates circled in yellow (Ni_3Nb), Laves particles circled in red (Nb-Mo-Si rich), TiC, and γ'' precipitates circled in blue (Ni_3Nb), and oxide particles circled in light blue. For interpretation of the references to color in this figure, the reader is referred to the web version of this article.



246

247 **Figure 7. Higher magnification STEM images of ASB AM Superalloy 718 with corresponding EDS maps for precipitate**
 248 **forming elements showing γ' ($\text{Ni}_3[\text{Ti},\text{Al}]$) circled in white and γ'' (Ni_3Nb) precipitates circled in blue. For interpretation of**
 249 **the references to color in this figure, the reader is referred to the web version of this article.**

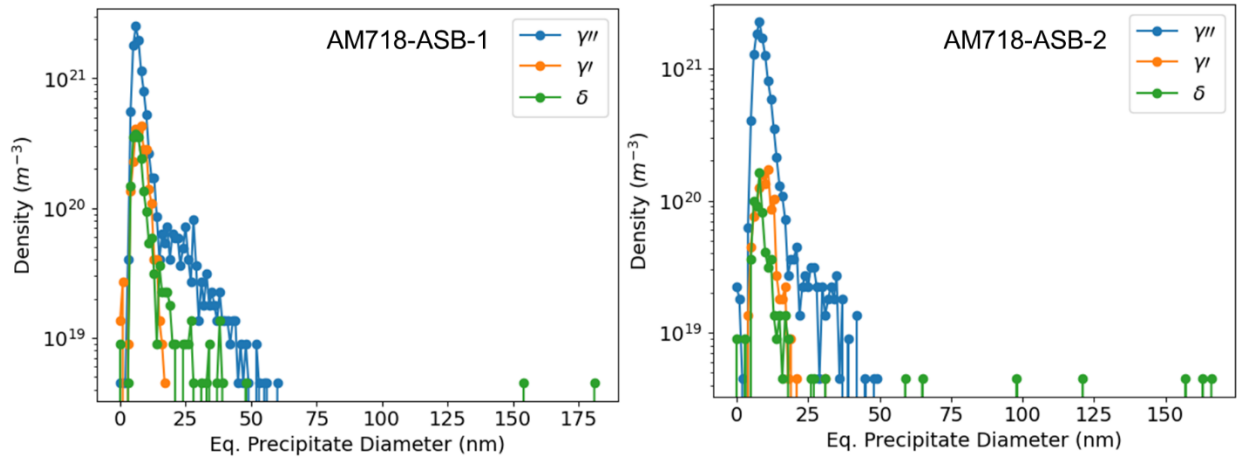
250

251 **Table 3. Summary of characterization results for precipitate phases observed in ASB AM718.** The error in number densities
 252 is the minimum of error from counting statistics [48] or from the TEM foil thickness measurement. *N.O.* indicates that the feature
 253 was not observed.

Alloy designation	Feature	Number of features observed	Percent of total precipitation (%)	Mean eq. diameter (nm)	Standard error of mean (nm)	Number density (m^{-3})
AM718-ASB-1	γ'	571	16.08	8.34	0.11	$2.68 \pm 0.3 \times 10^{21}$
	γ''	2,484	69.94	9.47	0.14	$1.17 \pm 0.1 \times 10^{22}$
	δ	467	13.15	9.89	0.55	$2.19 \pm 0.2 \times 10^{21}$
	Laves	7	0.20	77.25	9.9	$3.29 \pm 0.6 \times 10^{19}$
	Carbides	15	0.42	27.52	2.7	$7.04 \pm 0.9 \times 10^{19}$
	Pores	10	-	12.49	1.3	$4.70 \pm 0.8 \times 10^{19}$
	Oxide	7	0.20	25.65	6.2	$3.29 \pm 0.8 \times 10^{19}$
AM718-ASB-2	γ'	247	8.27	10.59	0.21	$1.16 \pm 0.2 \times 10^{21}$
	γ''	2,570	86.01	10.05	0.09	$1.21 \pm 0.1 \times 10^{22}$
	δ	156	5.22	14.34	1.9	$7.33 \pm 0.9 \times 10^{20}$
	Laves	9	0.30	51.56	14.9	$4.23 \pm 0.4 \times 10^{19}$

Carbides	N.O.	-	-	-	-
Pores	26	-	9.24	0.44	$1.27 \pm 0.3 \times 10^{20}$
Oxide	7	0.20	14.3	6.7	$2.82 \pm 0.6 \times 10^{19}$

254



255

256 **Figure 8. Precipitate size distributions for γ' , γ'' , and δ phases in ASB AM Superalloy 718.**

257

258 The microstructure found in the heat-treated specimens was not as complex as the ASB AM718.

259 Representative STEM HAADF images for the wrought alloy 718 and the three heat treatments of AM718

260 are shown in Figure 9. The wrought alloy contained the expected microstructure that consists of a high

261 density of fine γ' and γ'' precipitates, consistent with the ASTM-prescribed microstructure for precipitate-

262 hardened superalloys [33]. Following the homogenization treatment to produce AM718-HM, the

263 microstructure consisted of a low density of remaining oxide and carbide particles and dissolved all Laves,

264 δ , γ' , or γ'' phases present in the ASB AM718. After aging, the AM718-HT1 and AM718-HT2 treatments

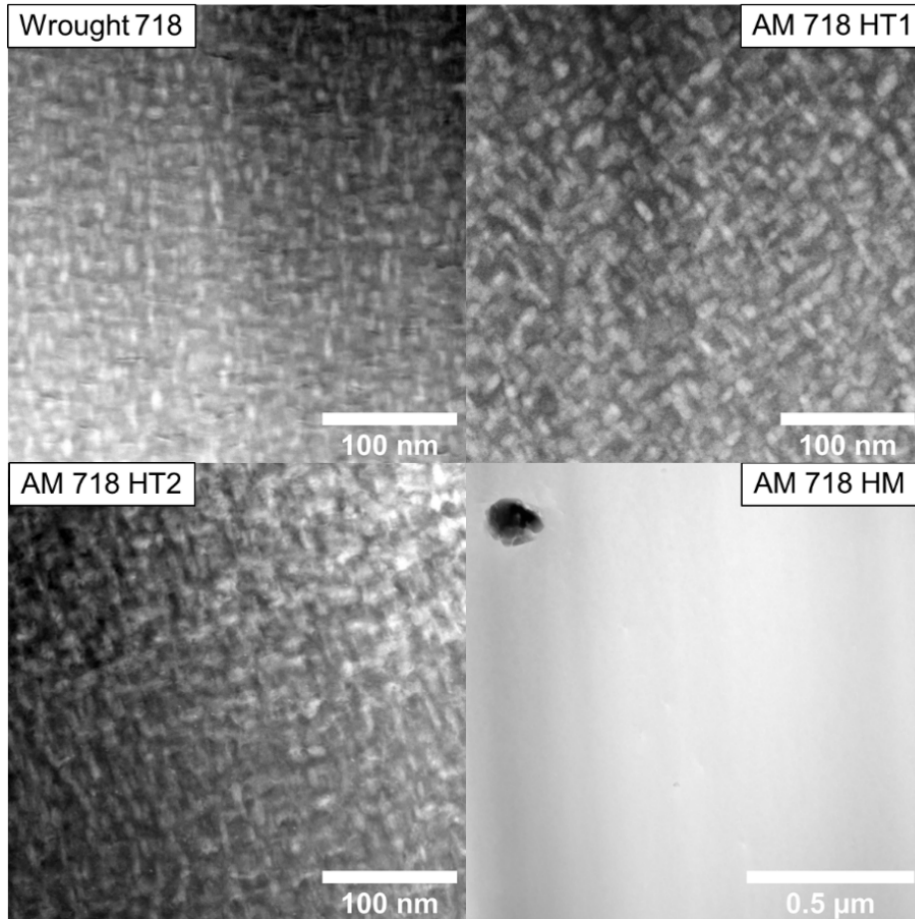
265 appeared qualitatively similar and contained a high density of fine γ' , γ'' , and δ precipitates, with AM718-

266 HT2 having greater precipitate densities overall. However, AM718-HT1 contained a higher fraction of δ

267 phase, as expected from the heat treatment. The quantitative analysis of γ' , γ'' , and δ particles is provided

268 in Table 4, and the size distribution of γ' , γ'' , and δ precipitates from each heat treatment is shown in Figure

269 10.



270

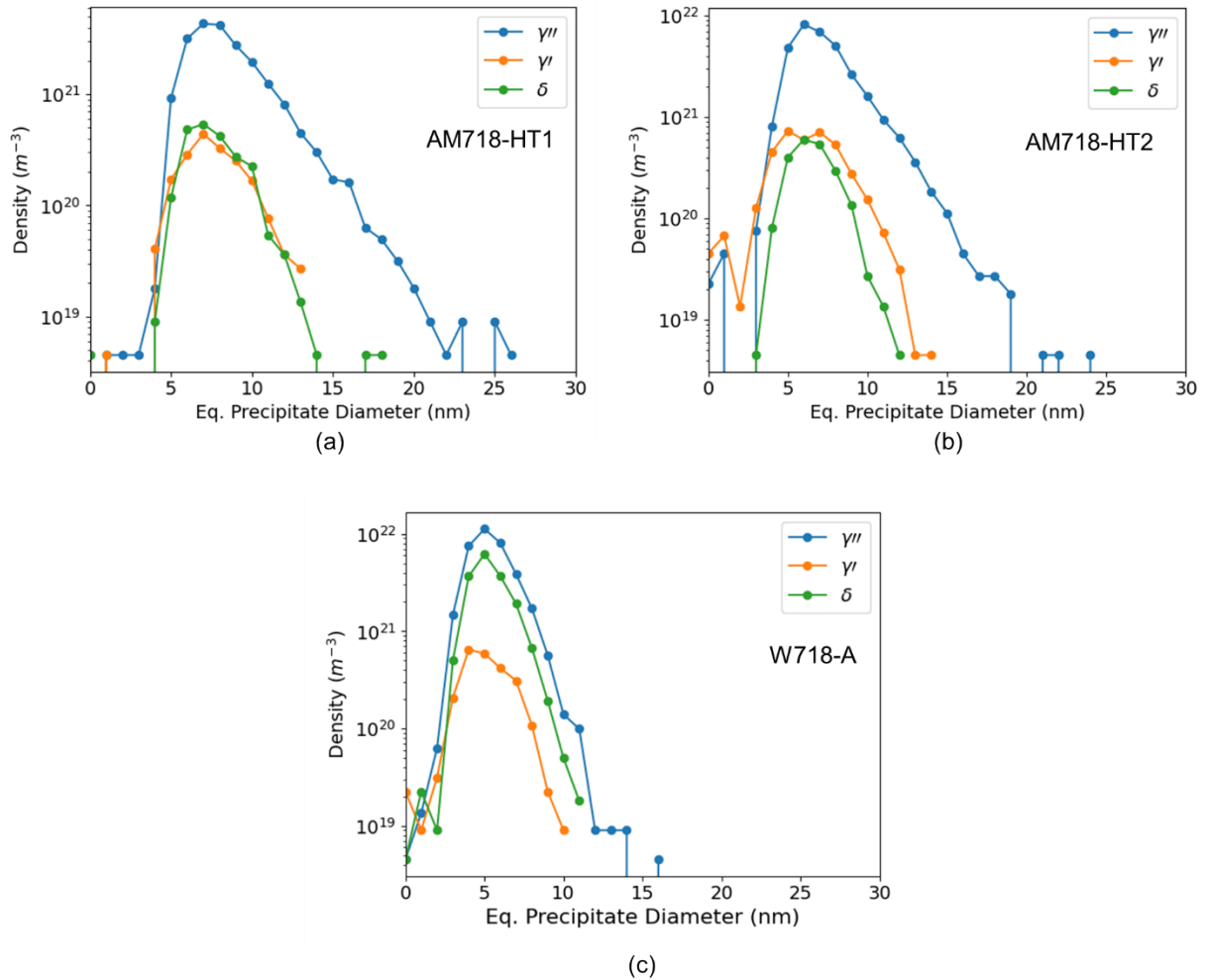
271 **Figure 9. STEM HAADF images of wrought alloy 718, AM718-HT1, AM718-HT2, and AM718-HM showing the mixture**
272 **of γ' , γ'' , and δ as bright features and oxides as dark features.**

273

274 **Table 4. Summary of characterization results for precipitate phases observed in heat-treated AM718 and W718.** The error
 275 in number densities is the minimum of error from counting statistics [48] or from the TEM foil thickness measurement. *N.O.*
 276 indicates that the feature was not observed. *N/A* indicates there was not enough of the feature to calculate this value.

Alloy designation	Feature	Number of features observed	Percent of total precipitation (%)	Mean eq. diameter (nm)	Standard error of mean (nm)	Number density (m ⁻³)
AM718-HT1	γ'	407	7.39	8.16	0.09	$1.91 \pm 0.2 \times 10^{21}$
	γ''	4,615	83.74	8.93	0.04	$2.17 \pm 0.2 \times 10^{22}$
	δ	487	8.84	8.17	0.08	$2.29 \pm 0.2 \times 10^{21}$
	Laves	N.O.	-	-	-	-
	Carbides	2	0.04	35.2	14.4	$9.39 \pm 1.2 \times 10^{18}$
	Pores	N.O.	-	-	-	-
	Oxide	N.O.	-	-	-	-
AM718-HT2	γ'	846	9.93	6.80	0.073	$3.97 \pm 0.4 \times 10^{21}$
	γ''	7,208	84.59	7.72	0.024	$3.39 \pm 0.3 \times 10^{22}$
	δ	466	5.47	7.06	0.062	$2.19 \pm 0.2 \times 10^{21}$
	Laves	N.O.	-	-	-	-
	Carbides	1	0.01	63.59	N/A	$4.70 \pm 2.4 \times 10^{18}$
	Pores	N.O.	-	-	-	-
	Oxide	N.O.	-	-	-	-
AM718-HM-1	γ'	N.O.	-	-	-	-
	γ''	N.O.	-	-	-	-
	δ	N.O.	-	-	-	-
	Laves	N.O.	-	-	-	-
	Carbides	3	75.00	45.79	13.7	$1.41 \pm 0.5 \times 10^{19}$
	Pores	N.O.	-	-	-	-
	Oxide	1	25.00	135.89	N/A	$4.70 \pm 2.4 \times 10^{18}$
AM718-HM-2	γ'	N.O.	-	-	-	-
	γ''	N.O.	-	-	-	-
	δ	N.O.	-	-	-	-
	Laves	N.O.	-	-	-	-
	Carbides	4	66.67	81.83	49.5	$1.88 \pm 0.6 \times 10^{19}$
	Pores	1	-	11.10	N/A	$4.70 \pm 2.4 \times 10^{18}$
	Oxide	2	33.33	47.33	40.9	$9.39 \pm 1.8 \times 10^{18}$
W718-Z1653	γ'	528	4.38	5.6	0.065	$2.38 \pm 0.25 \times 10^{21}$
	γ''	7735	64.28	5.9	0.015	$3.48 \pm 0.38 \times 10^{22}$
	δ	3770	31.33	5.9	0.019	$1.69 \pm 1.8 \times 10^{22}$
	Laves	N.O.	-	-	-	-
	Carbides	N.O.	-	-	-	-
	Pores	N.O.	-	-	-	-
	Oxide	N.O.	-	-	-	-

277



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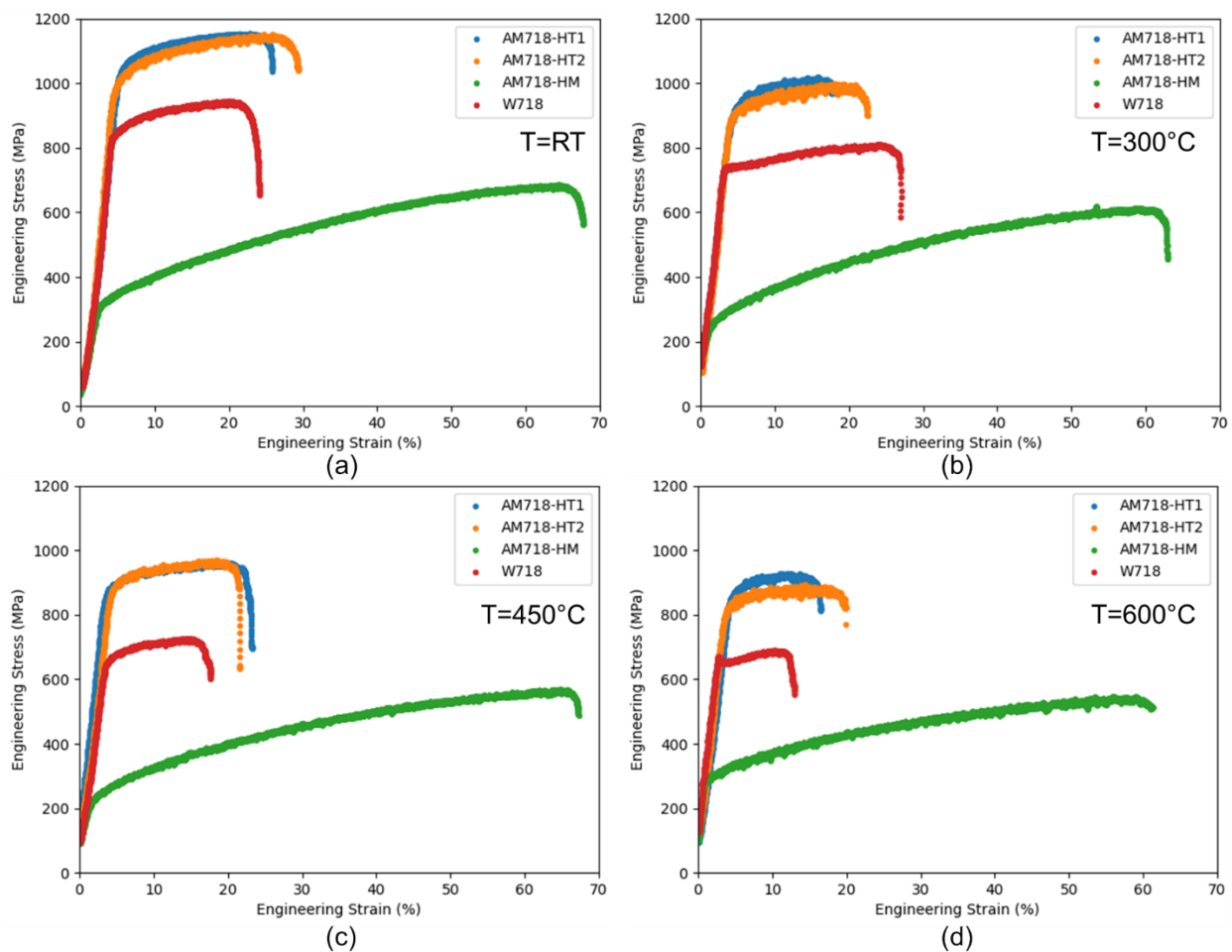
279 **Figure 10. Precipitate size distributions for γ' , γ'' , and δ phases in (a,b) heat-treated AM alloy 718 and (c) W718.**

280

281 3.3 Tensile test results up to 600 °C

282 Representative engineering stress-strain curves for each heat treatment of AM718 and the reference
 283 wrought alloy 718, labeled as W718, strained at each test temperature, are shown in Figure 11, and the
 284 stress-strain curves for each strained specimen are provided in the supplementary materials. Engineering
 285 stress-strain curves for each strained specimen from each condition are displayed in the appendix as Figure
 286 A.14 through Figure A.17 for transparency. These curves were used to calculate the common engineering
 287 properties of elastic modulus, 0.2% offset yield strength, uniform elongation, ultimate tensile stress, total
 288 elongation, and fracture strength. These properties are included in Table 5. Although acoustic methods are

289 preferred for determining the elastic modulus, the elastic modulus here was calculated by fitting a line to
290 the elastic portion of each tensile curve, minimizing the least squares error, and extracting the slope of the
291 line through a simple Hooke's Law approximation.

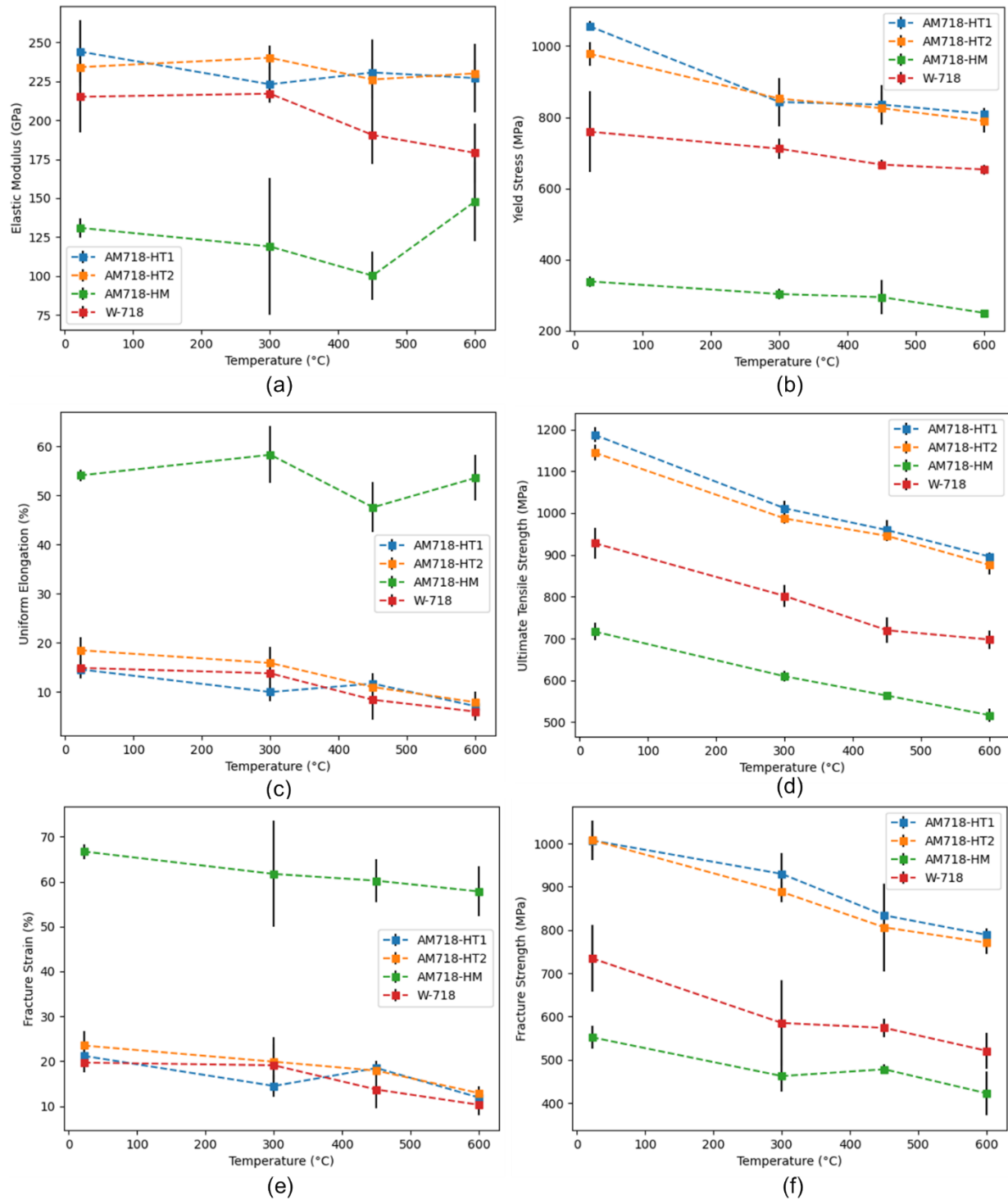


292
293 **Figure 11. Representative engineering stress-strain curves for heat-treated AM alloy 718 and wrought alloy 718 at (a) room**
294 **temperature, (b) 300 °C, (c) 450 °C, and (d) 600 °C.**

295 **Table 5. Engineering properties derived from room temperature tensile tests of wrought alloy 718 and heat-treated AM**
 296 **alloy 718.** Values reported are the averages of all tested specimens and their associated standard deviations.

Designation	Test temp. (°C)	Elastic modulus (GPa)	0.2% offset yield (MPa)	Uniform elongation (%)	Ultimate tensile strength (MPa)	Total Elongation (%)	Fracture Strength (MPa)
AM718-HT1	22	244 ± 19.9	1056 ± 13.6	14.6 ± 1.9	1,187 ± 17.7	26.1 ± 1.7	1007 ± 45.0
	300	223 ± 11.5	843 ± 68.0	9.99 ± 1.9	1,011 ± 17.9	19.6 ± 2.1	930 ± 48.3
	450	230.6 ± 21.3	836 ± 53.5	11.7 ± 2.2	959 ± 23.1	23.2 ± 0.8	834 ± 118
	600	227 ± 22.1	810 ± 17.0	7.1 ± 1.2	896 ± 9.22	16.3 ± 1.2	789 ± 15.1
AM718-HT2	22	234 ± 11.8	978 ± 33.2	18.5 ± 2.7	1,144 ± 18.6	28.6 ± 3.3	1008 ± 24.3
	300	240 ± 7.6	852 ± 22.7	15.9 ± 3.3	987 ± 12.7	24.6 ± 3.4	888 ± 22.9
	450	226.1 ± 11.9	825 ± 45.5	11.0 ± 1.9	945 ± 12.9	22.3 ± 1.5	806 ± 102
	600	230 ± 8.2	789 ± 33.0	7.9 ± 2.2	876 ± 23.4	17.1 ± 1.5	770 ± 26.1
AM718-HM	22	131 ± 6.1	338 ± 14.8	54.1 ± 1.2	717 ± 20.3	67.5 ± 1.5	552 ± 26.1
	300	119 ± 44	303 ± 14.7	58.3 ± 5.8	610 ± 12.4	63.8 ± 4.4	463 ± 36.8
	450	100.3 ± 15.4	294 ± 48.0	47.6 ± 5.1	563 ± 9.22	66.7 ± 3.7	478 ± 10.8
	600	148 ± 27	250 ± 9.39	53.6 ± 4.6	517 ± 16.4	62.5 ± 3.5	423 ± 51.4
W718-Z1653	22	215 ± 23.0	759 ± 114	14.9 ± 1.8	928 ± 37.2	24.4 ± 1.3	734 ± 77.7
	300	217 ± 3.5	711 ± 28.6	13.8 ± 4.8	802 ± 25.3	22.6 ± 6.0	585 ± 97.8
	450	190.5 ± 18.5	666 ± 14.0	8.4 ± 4.1	719 ± 30.8	17.5 ± 3.8	574 ± 21.9
	600	179 ± 18.8	653 ± 13.5	6.0 ± 1.9	697 ± 21.8	14.3 ± 2.3	521 ± 40.7

297



298

299 **Figure 12. Engineering properties for heat-treated AM718 and W718 as a function of testing temperature: (a) elastic**
 300 **modulus, (b) yield stress, (c) uniform elongation, (d) ultimate tensile strength, (e) total elongation, and (f) fracture strength.**

301

4. Discussion

4.1 Comparison of Wrought and AM 718

The wrought superalloy 718 displayed the expected behavior for a precipitate-hardened alloy consisting of a large yield stress and a high ultimate tensile stress. However, both the yield and ultimate tensile stress were 15–20% lower than expected for the ASTM heat treatment [1,8], and both had an increased uniform elongation and fracture strain compared with results presented in the literature [8,46,49]. The increased fracture strain is consistent with the expectation of subsize specimens and may result from the decrease in scale factor [35]. A fraction of the metastable γ'' transformed into intragranular δ -phase precipitates as predicted by the time-temperature-transformation diagram [45], and over-aging as discussed in Appendix A.2. Although δ precipitates share the composition of Ni_3Nb with γ'' , the lattice-precipitate interface is incoherent for the δ -phase, thus reducing its contribution to strength [8]. The high density of δ precipitates (Table 4) in the wrought superalloy 718 likely reduced the strength of the alloy compared to the expected ASTM-designated strength.

Prior to heat treatments, there was a clear preferred grain orientation in the as-built condition relative to the build direction. This likely would result in anisotropic properties. However, the first step of the heat treatment was a high temperature solution anneal meant to remove all previous precipitation. This resulted in significant grain growth, as expected for annealing above 982 °C [50], and a transition from lath-like elongated grains to more equiaxed grains, as expected for the recrystallization regime from 900 to 1066 °C [50]. Likely as a result, the yield strength and ultimate tensile strength of AM718-HT1 and AM718-HT2 (Table 2) increased relative to W718 and were well within ASTM specifications of superalloy 718. The AM718-HT2 condition displayed a larger uniform elongation after yield compared with the AM718-HT1 condition. Comparison of the microstructures of these two conditions as presented in Table 4, both exhibited a high density of γ'' precipitates on the order of 10^{22} m^{-3} , with AM718-HT-2 having a larger density. However, AM718-HT1 had a higher fraction of the δ -phase, which likely contributed to the

326 decrease in uniform elongation. The agreement in the uniform elongation between AM718-HT-1 and W718
327 lends support to the detrimental effects of δ -phase precipitates observed in W718.

328 When the precipitates were removed through homogenization and solution annealing (AM718-
329 HM), the yield stress and ultimate tensile strength decreased with a significantly greater uniform elongation
330 and fracture strain, which is consistent with solution-annealed alloy 718 [51]. However, the elastic modulus
331 was significantly lower than the 190–220 GPa range expected for polycrystalline pure Ni [52], stemming
332 from the decrease in yield stress. In the literature, a decreased elastic modulus was found when annealing
333 at high temperatures for 1 h to achieve values of 165–172 GPa [53–58]. Increasing the annealing
334 temperature reduced the elastic modulus linearly and correlated with an increase in the grain size [55].
335 Compared with these previous works, the homogenization treatment in this work was performed for a much
336 longer time and at higher temperatures. In this work, the recrystallized, homogenized AM718-HM still had
337 a reduced grain size compared to that of the wrought alloy, but without precipitates, making the implied
338 relationship between grain size and elasticity unclear. Additionally, at 600 °C, the elastic modulus appeared
339 to increase for AM718-HM. While precipitation is not expected based on the TTT diagram (Figure 1b),
340 solute clustering is likely occurring. Many precipitating phases proceed along a mechanism consisting of
341 clustering of the constituent elements and accumulation of solutes until a critical concentration then
342 transition to a distinct phase [59–61]. Therefore, the elastic modulus increase may stem from dislocation
343 pinning on solute clusters that have not transitioned into γ' or γ'' precipitates. These clusters were not visible
344 in the STEM EDS datasets and thus may reside below the resolution of the technique estimated at
345 approximately 2 nm for the parameters presented in the Methodology. An approach is needed to
346 deconvolute the contributions of grain size, precipitates, and other features contributing to the yield
347 strength.

348 4.2 Microstructure-Property Relationships

349 There is an inherent link between a material's microstructure and macroscopic mechanical
350 properties. In the broadest sense, the yield strength of a material is the sum of the inherent strength from
351 the crystal lattice, $\sigma_{Y,0}$, with additional strength from the effects of defects and secondary phases, σ_D ,
352 interpreted through a classical Orowan dislocation bowing process [62]. The inherent strengthening shown
353 in Eq. (2) stems from (1) the solid solution strength from substitutional elements in the face-centered
354 cubic (FCC) Ni lattice, σ_{SS} ; (2) the grain boundaries through the Hall-Petch relationship, $\frac{k_y}{\sqrt{d}}$, where k_y is a
355 constant, and d is the grain diameter; and (3) the dislocation friction stress, also known as the Peierls-
356 Nabarro stress, τ_{P-N} [63]. The impact of defects and precipitates is generally described by a dispersed
357 barrier hardening model, as shown in Eq. (3): $\alpha_i M \mu b \sqrt{N_i d_i}$, where α represents the strength of the barrier,
358 M is the Taylor factor, μ is the shear modulus, b is the Burgers vector, N is the density of the precipitates,
359 and d is their size described as an equivalent diameter:

$$360 \quad \sigma_Y = \sigma_{SS} + \tau_{P-N} + \frac{k_y}{\sqrt{d}} + \sum_i^{\delta, \gamma', \gamma'', MX, oxide} \alpha_i M \mu b \sqrt{N_i d_i}. \quad (3)$$

361 A linear superposition was utilized because the contributions from each component are not
362 expected to be similar in strength. Because W718 and each heat treatment of AM718 all exhibited similar
363 microstructure features, all yield stress measurements were made into a linear system of equations to solve
364 for the contributions of each component of the microstructure to the strength. Because of the low density
365 of carbides and oxides, these features were assumed to contribute a negligible amount of strength compared
366 to the other factors and were excluded from the analysis. The solid solution strengthening and the
367 dislocation friction stress were grouped together and assumed to act together linearly. The median grain
368 diameter was used instead of the average to reduce the influence of outliers. Rather than assume an average
369 density and diameter, the precipitate size distributions shown in Figure 10 were integrated to be included
370 in the dispersed barrier calculations. M is 3.06 [64], whereas the Burgers vector was assumed to be equal
371 to the lattice parameter for FCC nickel. This results in a linear system of equations with 5 unknown variables
372 ($\sigma_{SS} + \tau_{P-N}$, k_y , $\alpha_{\gamma'}$, $\alpha_{\gamma''}$ and α_{δ}) for each of the 16 yield stress measurements given in Table 5. Assuming

373 that the inherent strengthening and grain boundary contributions are the same for each measurement of the
 374 same heat treatment, the system reduces the system to 16 equations with 28 unknowns—an
 375 underdetermined system. In many similar analyses, the barrier strength is assumed to be independent of
 376 temperature for each feature, which would reduce the system to 16 equations with 7 unknowns and would
 377 become overdetermined. An overdetermined system almost always yields inconsistent solutions when
 378 constructed with randomly determined starting points for each variable. Although an underdetermined
 379 system cannot be solved for a unique solution, the Moore-Penrose pseudoinverse of the linear coefficient
 380 matrix of the unknowns can be used to construct a linear solution that minimizes the least-squares
 381 approximation. The coefficients found from this solution are displayed in Table 6. An alternative approach
 382 using theoretical strength factors from Tan and Busby [65] is presented in the Appendix for reference and
 383 suggests similar values for α as this discussion.

384 **Table 6. Coefficients determined to correlate microstructure to yield strength with linear least squares error.**

Temperature (°C)	T/T _m	Solid solution + friction stress modifier, C ₁ (×1 MPa)	Hall-Petch coefficient, k _y (MPa×m ^{1/2})	α for γ'' (unitless)	α for δ (unitless)
22	0.17	0 (see text)	1,716,711	0.129	0.129
300	0.33	236.24	484,541	0.131	0.057
450	0.42	134.46	882,908	0.118	0.078
600	0.50	56.35	1,000,045	0.112	0.111

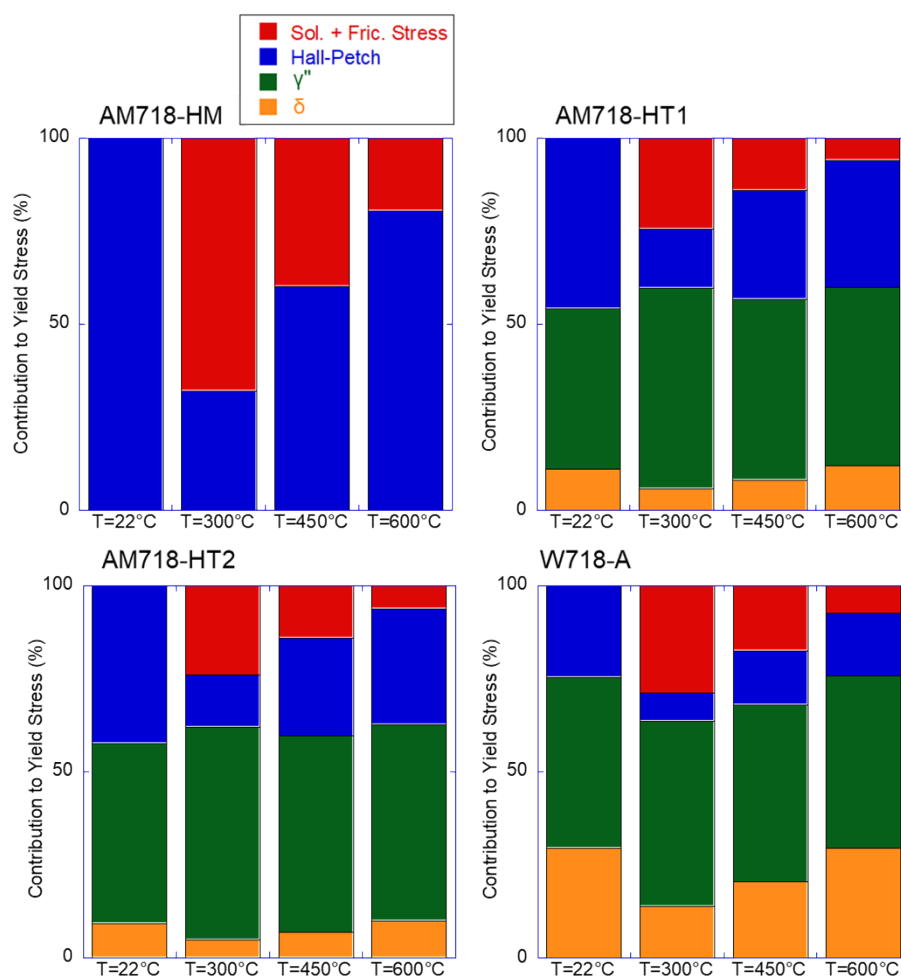
385

386 Lucas [66] summarizes the reported α values of different types of defects and categorizes them into
 387 three groups: (1) weak barriers such as small bubbles/loops and dislocations with $\alpha < 0.25$, (2) intermediate
 388 barriers such as Frank loops and small precipitates with $0.33 < \alpha < 0.45$, and (3) strong barriers such as
 389 voids and large precipitates with $\alpha \sim 1$ obstacles. According to this interpretation, the precipitates examined
 390 are all weak barriers with a variable strength coefficient based on temperature. All materials exhibit several
 391 major temperature regimes separated by the onset of migration of point defects. In pure nickel, vacancy
 392 defects are immobile below about 77–100 °C, whereas small interstitial clusters and interstitial-solute
 393 clusters may migrate [67]. Thus, the tensile tests at room temperature can be considered as testing the
 394 resistance of each class of microstructural features to primarily stress-driven interstitial dislocation motion.
 395 The results in Table 6 suggest that the main contributions to yield strength at room temperature are grain

396 boundaries, γ'' , and δ precipitates, with the γ'' and δ exhibiting the same obstacle strength. However, when
397 the tensile temperature is increased above the onset of vacancy mobility, the strength coefficient for γ''
398 precipitates remain about the same as at room temperature but decreases for δ phase. Because 300 °C is
399 still a relatively low temperature and is unlikely to have a significant thermal concentration of vacancies,
400 this reduction in the strength of δ can be attributed to the increase in interstitial motion between room
401 temperature and 300 °C. With increasing temperature up to 600 °C and corresponding increase in thermal
402 contributions to interstitial motion and vacancy concentration, the strengthening coefficient for γ''
403 decreases, and δ increases until these precipitate phases become equal strength. Both phases are the same
404 chemical composition of Ni_3Nb , but the disk-shaped γ'' precipitates are coherent with the nickel lattice on
405 $\{100\}$ planes, maintaining the c-axis perpendicular to the disks, whereas the δ phase is semi-coherent [49],
406 possibly driving the differences in the observed strengthening factors when thermal motion is considered.
407 Coherent precipitates produce larger long-range strain fields compared to semi-coherent precipitates, and
408 thus they also increase the combined mechanical and thermal work required to overcome a barrier. If the
409 required work is sufficiently small, then thermal vibrations of the lattice may assist dislocations to pass
410 through a weak strain field and overcome the precipitate [68]. Atomistic simulations of point defect and
411 dislocation interactions with these precipitates would provide strong additional insight into the role of
412 precipitate coherency on strength at high temperatures.

413 With these coefficients, the relative contribution of each term to the total yield strength can be
414 estimated and is displayed as a percentage in Figure 13. Based on this analysis, several trends are visible,
415 and general processes can be proposed. At room temperature, the grain boundaries appear to be responsible
416 for most of the strength from the lattice (AM718-HM), whereas the precipitates contribute more than half
417 of the yield strength (AM718-HT1, AM718-HT2, and W718). However, this result is counterintuitive
418 because some contribution from solutes in the lattice would be expected. Assuming primarily stress-driven
419 dislocation motion, these results suggest that the stresses necessary to eject dislocations from grain
420 boundaries are significantly higher than those necessary to overcome small interstitial solutes or solutes in
421 solution. Therefore, motion around solutes is comparatively trivial and results in an apparent lack of

422 strengthening from these features. As temperature increases to 300 °C, interstitials have more thermal
 423 motion, and solutes in the matrix provide pinning sites and increase the relative contribution to the yield
 424 strength. However, as temperature increases even further, it becomes easier to bypass the solutes, and the
 425 grain boundaries once again become a relatively stronger barrier to overcome. The main assumption in the
 426 Hall-Petch slope (k_y) is that it is proportional to the work required to eject dislocations from grain
 427 boundaries [69], and thus the trends in Table 6 and Figure 13 suggest a strong reliance on interstitial motion,
 428 similar to the discussion surrounding δ phase precipitates in the preceding paragraph. At all temperatures,
 429 the relative contribution to the yield strength from γ'' remained consistent between 48–57% of the total
 430 strength, indicating the utility of this phase to the high-temperature strength of superalloy 718. One
 431 drawback from this analysis is that the contributions of other microstructural features such as carbides,
 432 oxides, and γ' precipitates could not be assessed because of their lower density and apparent strength.



433

434 **Figure 13. Fractional contribution to the yield strength from solid solution strengthening and friction strength, grain**
435 **boundaries through the Hall-Petch relationship, γ'' precipitates, and δ precipitates for each heat treatment of superalloy**
436 **718 examined in this work.**

437

438 While many researchers investigated the relationships between post-build heat treatments,
439 mechanical response, and microstructure of superalloy 718, the results tend to focus more on the room
440 temperature properties and semi-empirical relationships. However, superalloy 718 is used in many
441 applications up to its high creep-rupture strength, which limits its use at high temperatures near 650 - 700
442 °C. This is believed to stem from the coarsening of the γ'' precipitates [8] expected from the TTT diagram
443 (Figure 1b). Because of the wide temperature range in the derivation and relative simplicity of the dispersed
444 barrier model produced in this work, it can easily integrate into modeling and simulation workflows to
445 estimate the yield strength of AM superalloy 718 components after fabrication. Such projects, for example
446 the ExaAM initiative [70], are expected to transform AM through high performance computing (exascale)
447 simulation of the complex interplay between the physical phenomena (e.g., heat transfer, melting,
448 solidification, fluid flow) involved in the additive process to simulate the microstructure and resulting
449 properties. Because the precipitation in superalloy 718 is strongly sensitive to the thermal history, having a
450 microstructure-strength relationship dependent on the precipitate size, precipitate density, and morphology
451 will significantly improve the quality of efforts to simulate the properties of traditional and AM
452 components.

453 **5. Conclusions**

454 Microstructure characterization and baseline mechanical testing were performed on additively
455 manufactured superalloy 718 produced via PBF-LB. The key findings and conclusions derived from this
456 work are summarized as follows.

457 The microstructure of as-built superalloy 718 contained many of the phases predicted from the
458 isothermal phase diagram with strong variation, depending on the location in the part at nano- to micro-
459 scales. The formation of Laves and on-boundary δ phase suggests that the mechanical properties would

460 result in poor performance of the as-built component, whereas the lath-like structure suggests that the
461 mechanical properties would strongly depend on orientation. Purely based on the as-built microstructure,
462 superalloy 718 is not recommended for structural use without post-build heat treatments using these
463 processing parameters.

464 Three heat treatments consisting of two step homogenization, solution treatment, and aging were
465 employed to control the precipitate morphology in additively manufactured superalloy 718 after fabrication.
466 The yield strength and ultimate tensile strength of the heat treated additively manufactured superalloy 718
467 increased relative to the wrought 718 and were well within ASTM specifications for superalloy 718. Both
468 HT-1 and HT-2 treatments resulted in a high density of γ'' precipitates on the order of 10^{22} m^{-3} , with AM718-
469 HT-2 having a larger density and a lower fraction of intragranular δ -phase. Interpreting the yield strength
470 through an Orowan dislocation mechanism determined that all precipitates analyzed in this work proved to
471 be weak barriers to dislocation motion, but they provided strength to the alloy through their consistent high
472 density. At temperatures ranging from 22 to 600 °C, the relative contribution to the yield strength from γ''
473 remained consistent between 48–57% of the total strength, indicating the utility of this phase to the high-
474 temperature strength of superalloy 718. The strength factors for γ'' and δ precipitates were found to trend
475 inversely with tensile test temperature and may be attributable to the differences in precipitate coherency.
476 From the homogenized condition, it is suggested that the contributions in strength from solutes and grain
477 boundaries are strongly temperature dependent. Based on the results of this study, a high-temperature
478 homogenization followed by a traditional ASTM aging, designated *HT-2* in this work, is recommended to
479 recover the properties and microstructure from additively manufactured superalloy 718 necessary for high-
480 temperature strength. Because of the wide temperature range in the derivation and relative simplicity of the
481 dispersed barrier model produced in this work, it can easily be integrated into modeling and simulation
482 workflows to estimate the yield strength of traditional and AM components.

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494

495 **7. CRediT statement**

496 Stephen Taller – Conceptualization, Methodology, Software, Formal analysis, Investigation,
497 Visualization, Writing - Original Draft, Project administration

498 Ty Austin – Software, Formal analysis, Investigation, Writing - Review and Editing

499

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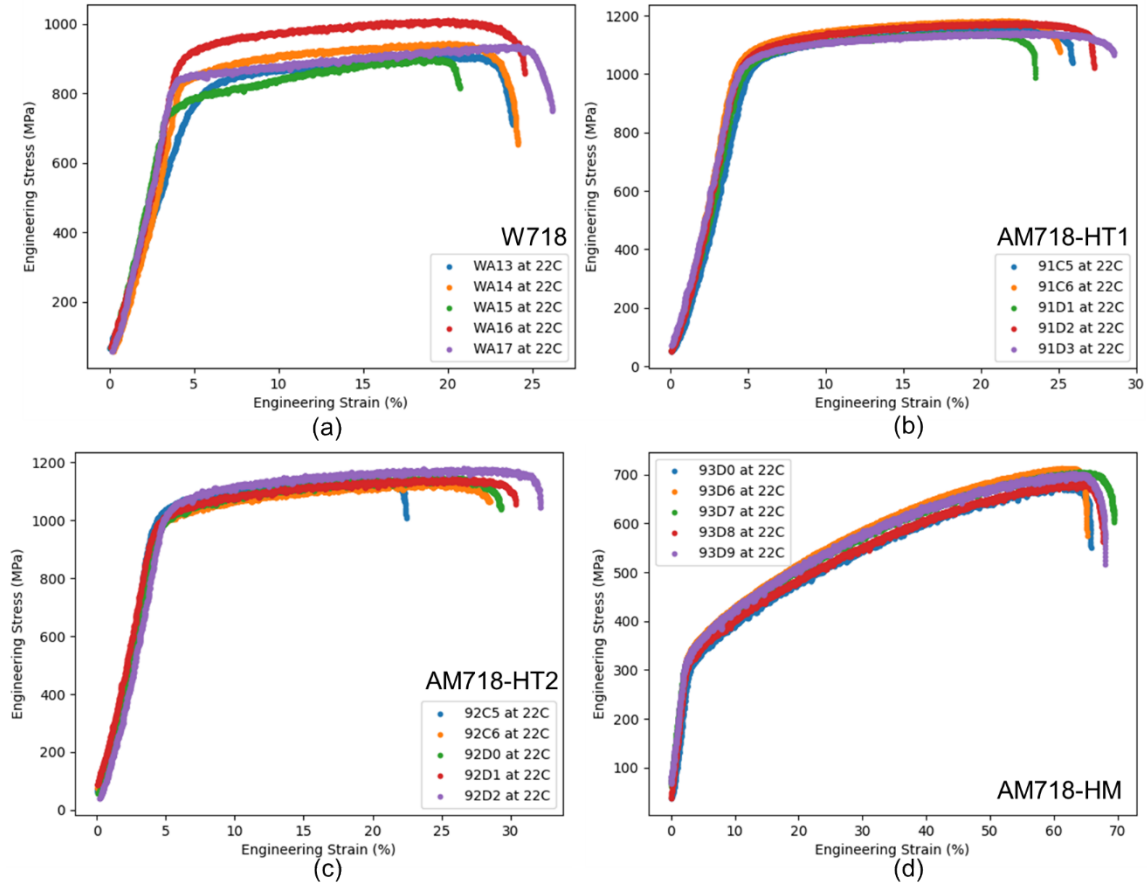
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710

Appendix

711 A.1 Engineering Stress-Strain Curves for All Specimens in this Study

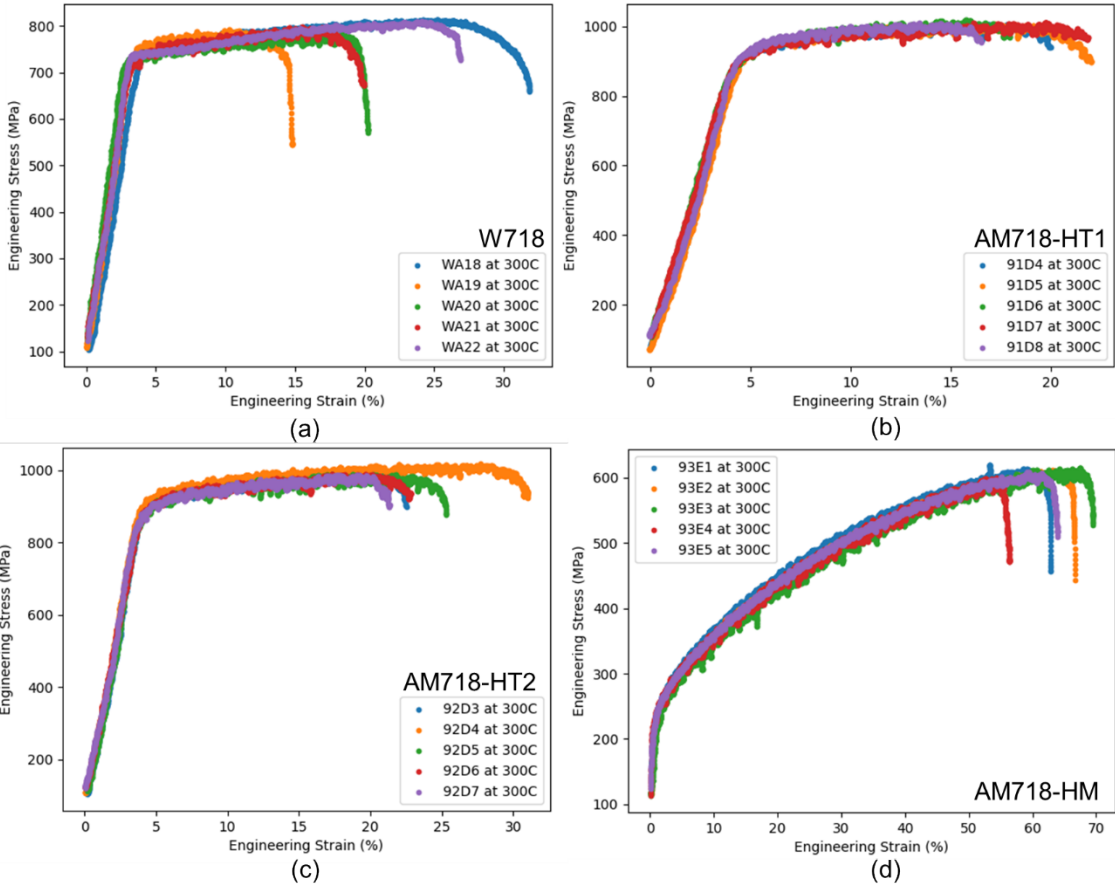
712 While averages and representative values capture the overall behavior of the material, transparency
713 requires that all necessary information be included. Therefore, the stress-strain curves for each tensile test
714 are provided here in Figures Figure A.14 – Figure A.17.



715

716 **Figure A.14. Individual engineering stress-strain curves for wrought superalloy 718 (a) and heat-treated AM superalloy**
717 **718 (b–d) at room temperature.**

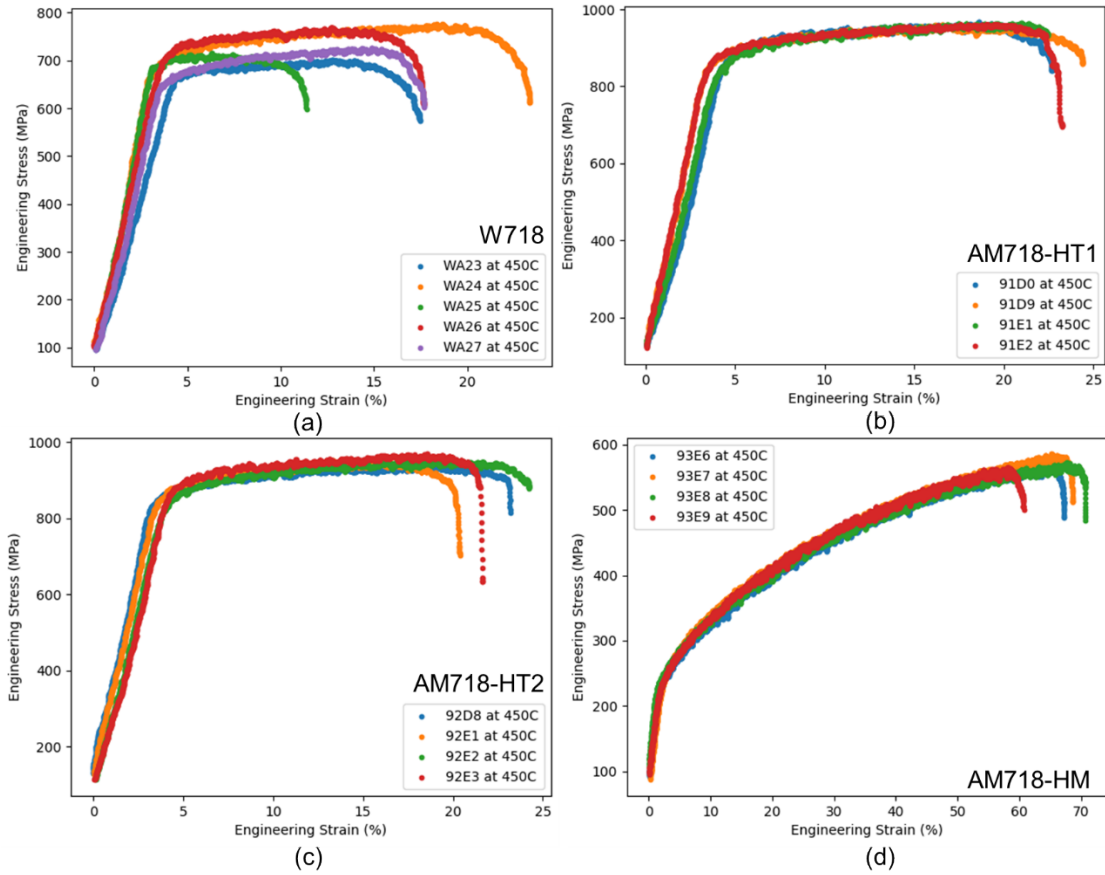
718



719

720 **Figure A.15. Individual engineering stress-strain curves for wrought superalloy 718 (a) and heat-treated AM superalloy**
 721 **718 (b–d) at 300 °C.**

722



723

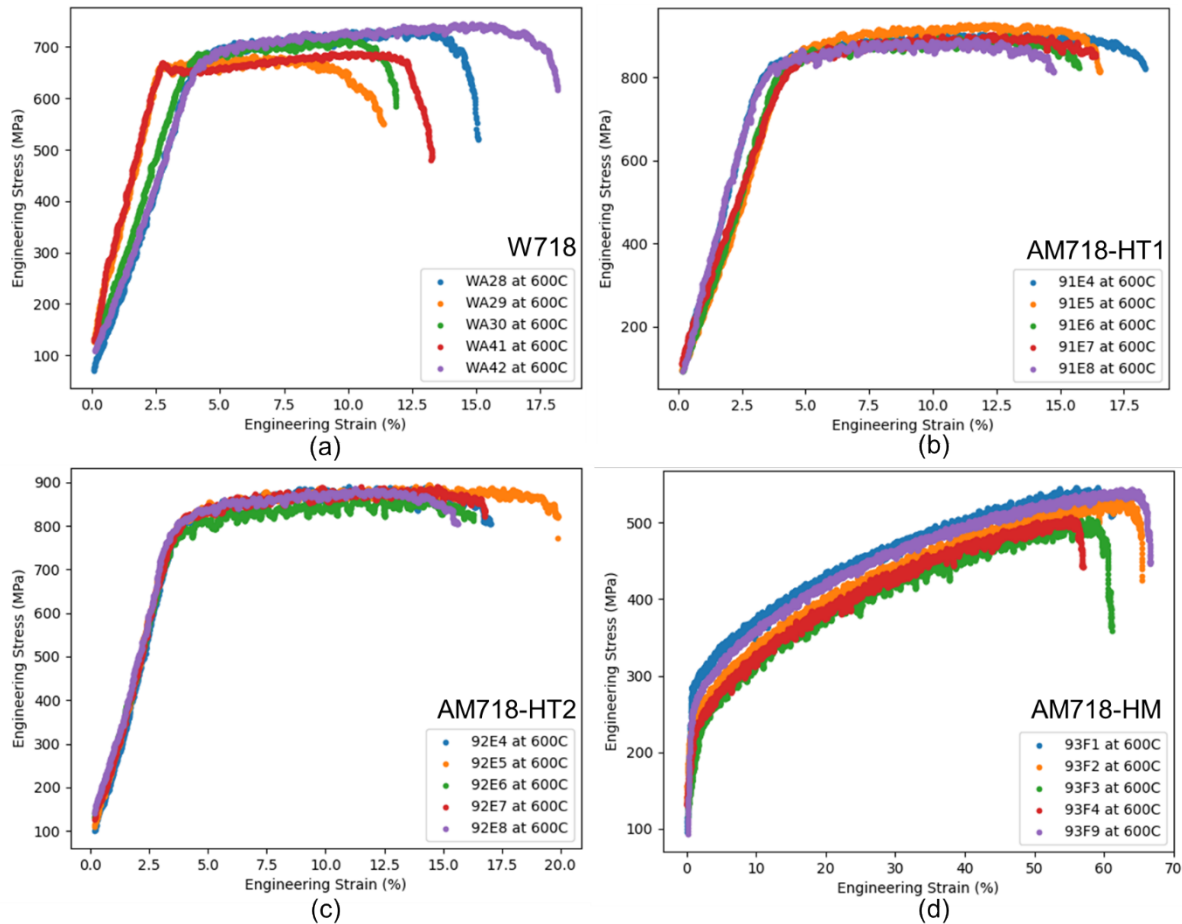
724

Figure A.16. Individual engineering stress-strain curves for wrought superalloy 718 (a) and heat-treated AM superalloy

725

718 (b–d) at 450 °C.

726



727

728 **Figure A.17. Individual engineering stress-strain curves for wrought superalloy 718 (a) and heat-treated AM superalloy**
 729 **718 (b–d) at 600 °C.**

730 **A.2 On the Differences in Microstructure in W718 and AM-HT2 for the Same Heat Treatments**

731 In an ideal scenario, putting two samples of the same material in the same furnace for heat treatment
 732 and subjecting them to the same temperature history would result in the same microstructure and properties.
 733 In this study, both AM718-HT2 and W718 went through the same heat treatment history, but they resulted
 734 in different microstructures and properties. The AM718 block was homogenized and aged in the form of a
 735 block with dimensions of $15 \times 30 \times 60$ mm for its length, width, and height respectively. The W718 was
 736 heat treated as a cylinder with a diameter of 25.4 mm and a height of 22 mm. The furnace used was an
 737 open-air furnace, so the method of heat transfer to the samples was natural convection. Thus, the Biot

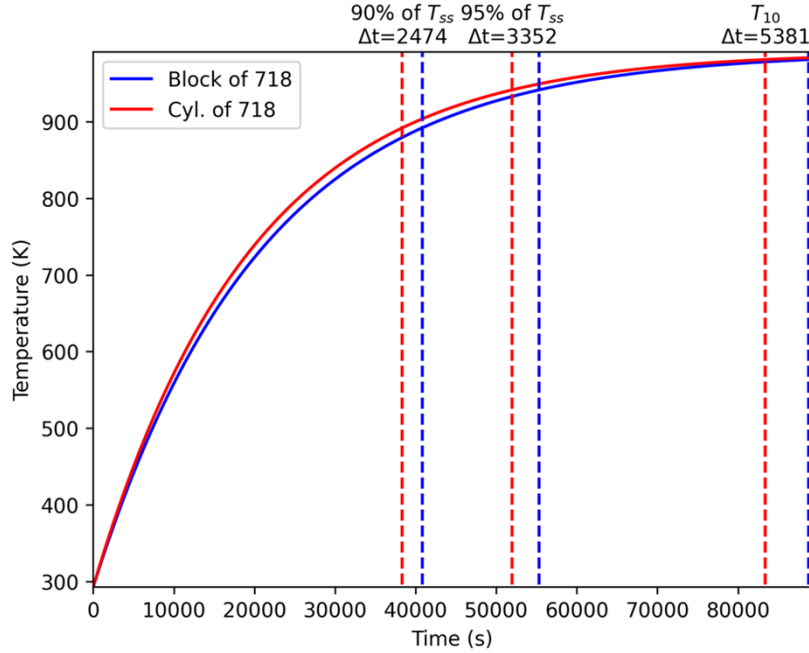
738 number can be used as an indication of the thermal resistance inside of each body and at the surface of each
739 body:

$$740 \quad Bi = \frac{\bar{h}(V)}{k(A)}, \quad (A.4)$$

741 where \bar{h} is the average convective heat transfer coefficient for air, k is the thermal conductivity of alloy
742 718, V is the volume of the component, and A is the surface area available for heat transfer. Using the
743 properties of 718 from Agazhanov et al. [71] and the dimensions noted above, the Biot number for each
744 block is 0.0071, and for the W718 cylinder, the Biot number is 0.0067. The absolute values of both are
745 small (<0.1), implying that heat conduction inside 718 is much faster than heating from the environment,
746 so there are negligible temperature gradients inside each piece. Because of this low Biot number, the
747 transient temperature of each piece can be estimated using the lumped capacitance model of heat transfer,
748 as shown in Eq. A.5:

$$749 \quad \frac{T(t) - T_{\infty}}{T_i - T_{\infty}} = e^{-t \frac{A\bar{h}}{\rho c V}}, \quad (A.5)$$

750 where $T(t)$ is the temperature of the metal at time t , T_{∞} is the temperature of the heat reservoir, T_i is the
751 initial temperature of the piece, and c is the specific heat capacity. The time-dependent temperature of each
752 piece is shown in Figure A.18 and is solved with time- and temperature-dependent material properties
753 updating every 1 second based on the average temperature of the previous three timesteps. From this
754 estimation, the cylinder heats up quicker than the block, resulting in a difference in the time at which each
755 piece reaches the same temperature. During heat treatment, the aging time was started when a thermocouple
756 on the surface of the AM718 block read within 10 °C of the target temperature, which is designated as T_{10}
757 in Figure A.18. When the AM718 block reaches T_{10} , the cylinder of W718 has already been at the aging
758 temperature for about 1.5 hours. Based on the T-T-T diagram [45], for an aging temperature of 718 °C,
759 W718 would be closer to the boundary at which delta phase forms. Thus, while the same heat treatments
760 and aging were used on AM718 and W718, the sample geometry in the furnace led to an over-aging of the
761 W718 and significant formation of intragranular delta phase precipitates.



762

763 **Figure A.18. Transient temperature build-up in superalloy 718 blocks and cylinder through the lumped capacitance**
 764 **method.**

765 **A.3 On the Use of Theoretical Strength Factors**

766 In the work presented in the main manuscript, no assumptions were made in the strength
 767 coefficients. Traditionally, the strengthening coefficients, α , are usually adjusted to obtain a best fit when
 768 compared with experimental data. This approach limits any predictability of the model and neglects any
 769 contributions of precipitate shape or size. The effects of the precipitate shape and size on the strength factor
 770 were considered by Tan and Busby [65] in a paper which presented forms for α for spherical, rod-shaped,
 771 and thin plate precipitates. In this study, the γ' precipitates were observed as spherical features, whereas the
 772 γ'' and intragranular δ precipitates were found as thin disk or plate precipitates. Thus, the relevant
 773 strengthening coefficients from Tan and Busby are as follows:

774 Spherical $\alpha_{SP} = \frac{0.135}{(1-\nu)^{1/2}(1-0.816d\sqrt{ND})} \ln\left(\frac{0.816d}{r_0}\right)$. (A.6)

775 Thin-plate $\alpha_{PP} = \frac{0.271A}{(1-\nu)^{1/2}\sqrt{ND}(16-\pi tA)} \ln\left(\frac{0.637D}{r_0}\right)$, with $A = \sqrt{16\pi ND} + 4ND^2 - \pi^2 NDt$, (A.7)

776 where N is the number density of the precipitating phase, d is the average diameter of spherical precipitates,
777 D is the large diameter of thin plate precipitates, t is the thickness of the thin plate precipitate, ν is Poisson's
778 ratio (~ 0.3), and r_0 is the dislocation core radius ($r_0 \sim \mathbf{b}$ to $4\mathbf{b}$ [72]). A value of $r_0 = 4\mathbf{b}$ was chosen for
779 estimating the dislocation core radius, whereas all other values were calculated from the characterized
780 microstructures. Lucas [66] summarizes the reported values of different types of defects and categorizes
781 them into three groups: (1) weak barriers such as small bubbles/loops and dislocations with $\alpha < 0.25$,
782 (2) intermediate barriers such as Frank loops and small precipitates with $0.33 < \alpha < 0.45$, and (3) strong
783 barriers such as voids and large precipitates with $\alpha \sim 1$ obstacles. The estimations of α for γ' , γ'' , and δ
784 precipitates are included in Table A.7, along with their contributions to the yield strength calculated using
785 Eq. (3) and the microstructure presented in Table 4. This approach resulted in strength coefficients
786 suggesting that each phase is still in the weak-to-intermediate barrier range. However, with these strength
787 coefficients, the summation of contributions from each phase exceeds the measured yield stresses at each
788 tensile test temperature, suggesting that these strength coefficients overestimate the strength of the barriers.
789 Considering the precipitate-dislocation interaction, before the dislocation core becomes pinned on the
790 precipitate, the precipitate and dislocation will first interact through the strain fields around them. Although
791 the size of the strain field is not directly known, the works of Kohnert and Capolungo suggest that the strain
792 field around a dislocation can be as large as $10\mathbf{b}$ [73,74]. If this strain field ($r_0 \sim 10\mathbf{b}$) is used instead of the
793 dislocation core radius, then the strengthening coefficients decrease, and the precipitates become barrier
794 strengths similar to those determined through solving the linear least squares problem as done in the main
795 manuscript shown in Table 6.

796 **Table A.7. Coefficients determined through a theoretical approach to correlate microstructure to yield strength with**
797 **estimated contributions from γ' , γ'' , and δ phase precipitates.**

Property	Tensile test temperature (°C)	W718	AM718-HT1	AM718-HT2
$\alpha_{\gamma'}$ (unitless), $r_0 \sim 4\mathbf{b}$	N.A.	0.193	0.257	0.228
$\alpha_{\gamma''}$ (unitless), $r_0 \sim 4\mathbf{b}$	N.A.	0.250	0.328	0.306

α_{δ} (unitless), $r_0 \sim 4\mathbf{b}$	N.A.	0.237	0.288	0.256
σ_{yield} (MPa)	22	873 ± 131	1214 ± 15.6	1125 ± 38.2
$\Delta\sigma_{\gamma'}$ (MPa)	22	148.75	238.76	291.96
$\Delta\sigma_{\gamma''}$ (MPa)	22	780.92	1314.68	1317.68
$\Delta\sigma_{\delta}$ (MPa)	22	478.61	293.75	208.87
σ_{yield} (MPa)	300	818 ± 32.9	969 ± 78.2	980 ± 26.1
$\Delta\sigma_{\gamma'}$ (MPa)	300	137.44	220.61	269.78
$\Delta\sigma_{\gamma''}$ (MPa)	300	721.58	1214.79	1217.56
$\Delta\sigma_{\delta}$ (MPa)	300	442.25	271.43	193.00
σ_{yield} (MPa)	450	766 ± 16.1	961 ± 61.5	949 ± 52.3
$\Delta\sigma_{\gamma'}$ (MPa)	450	131.34	210.83	257.81
$\Delta\sigma_{\gamma''}$ (MPa)	450	689.57	1160.89	1163.54
$\Delta\sigma_{\delta}$ (MPa)	450	422.62	259.39	184.43
σ_{yield} (MPa)	600	751 ± 15.5	931 ± 19.6	907 ± 38.0
$\Delta\sigma_{\gamma'}$ (MPa)	600	125.24	201.04	245.84
$\Delta\sigma_{\gamma''}$ (MPa)	600	657.55	1106.99	1109.51
$\Delta\sigma_{\delta}$ (MPa)	600	403.00	247.34	175.87
$\alpha_{\gamma'}$ (unitless), $r_0 \sim 10\mathbf{b}$	N.A.	0.042	0.105	0.075
$\alpha_{\gamma''}$ (unitless), $r_0 \sim 10\mathbf{b}$	N.A.	0.102	0.173	0.149
α_{δ} (unitless), $r_0 \sim 10\mathbf{b}$	N.A.	0.094	0.149	0.119