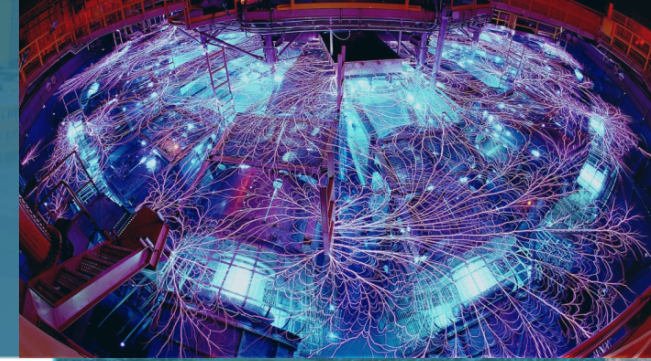




# Bayesian Methods in Inertial Confinement Fusion Research: Embracing uncertainty and Learning More from our Data



Patrick F. Knapp

63<sup>rd</sup> Annual Meeting of the APS Division of Plasma Physics

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# Thanks to my many colleagues and contributors



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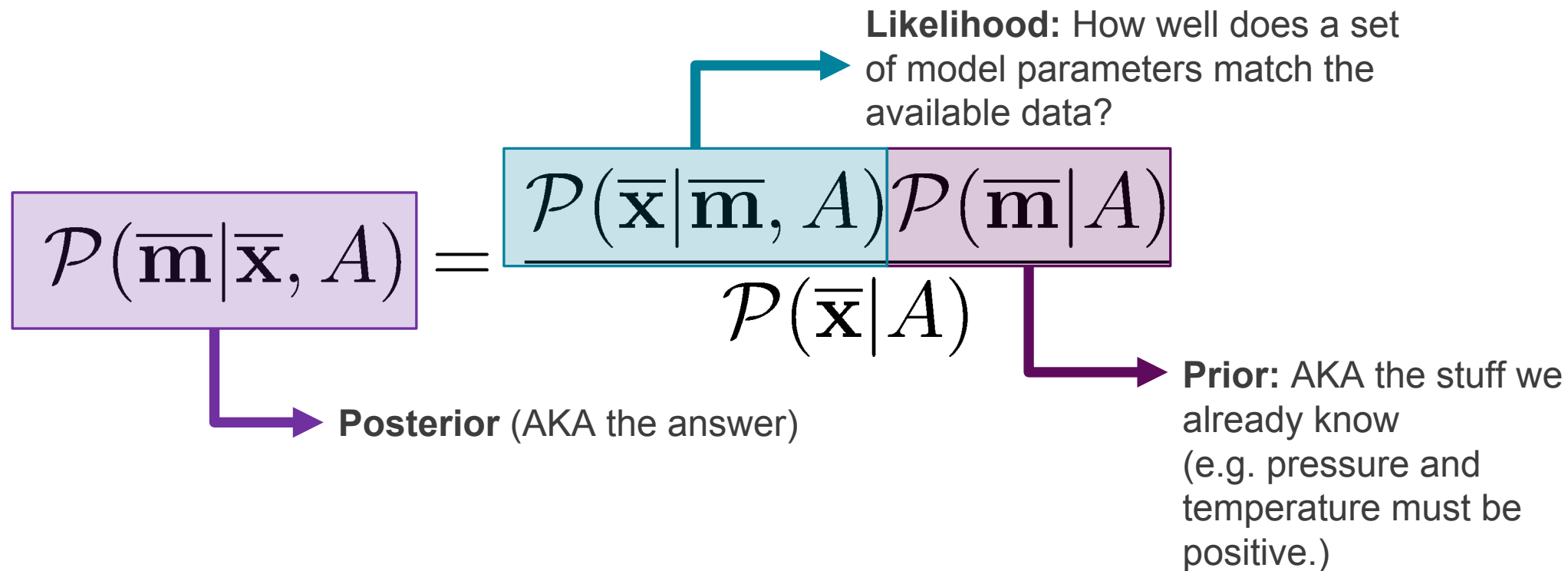
<sup>5</sup>Department of Physics and Astronomy, University of Rochester, Rochester, NY

<sup>6</sup>Nuclear Engineering & Radiological Sciences Department, University of Michigan, Ann Arbor, MI

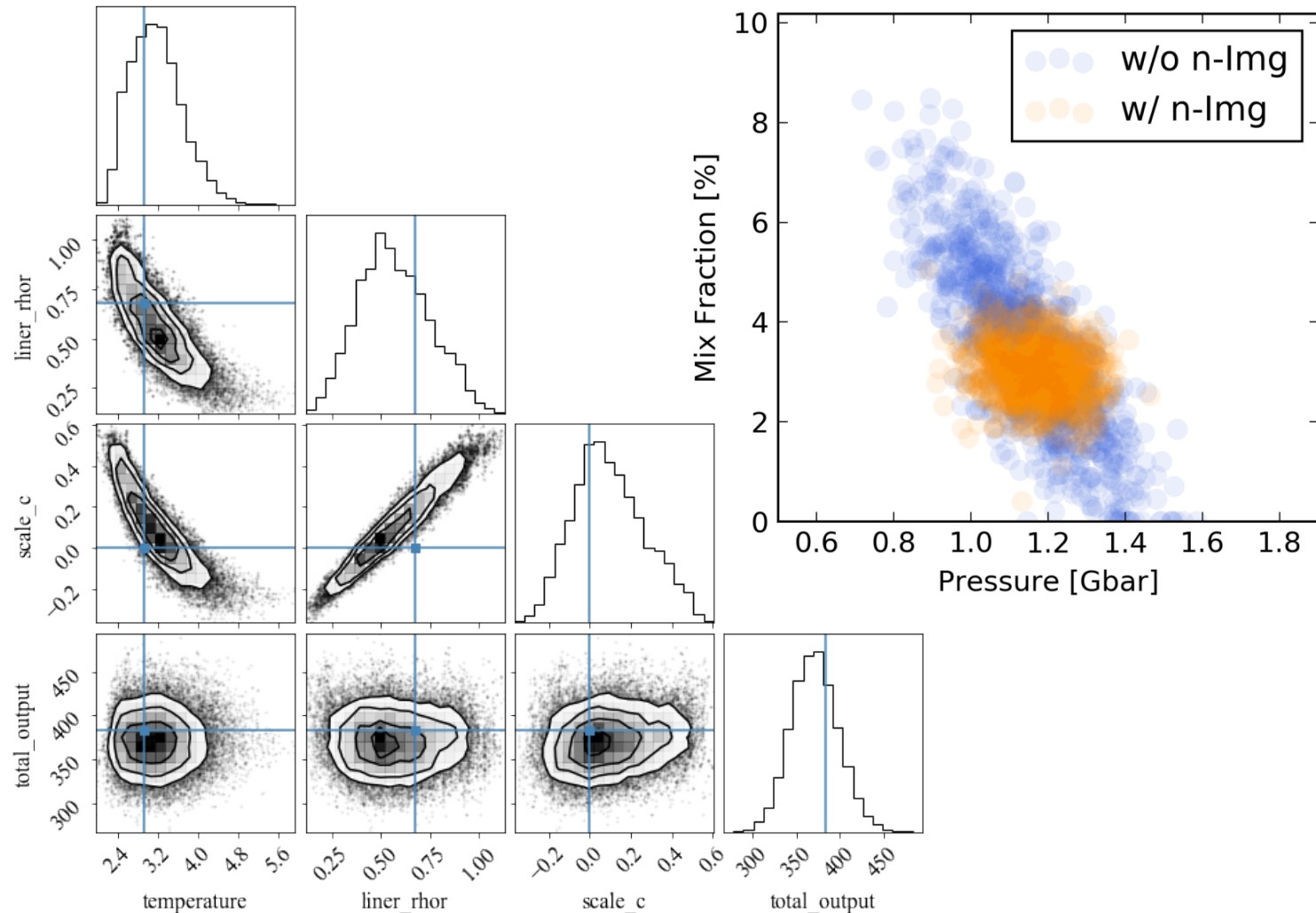
Bayes' theorem provides us with a way to extract information from data with rigorously quantified uncertainties



$$\mathcal{P}(\overline{\mathbf{m}}|\overline{\mathbf{x}}, A)\mathcal{P}(\overline{\mathbf{x}}|A) = \mathcal{P}(\overline{\mathbf{x}}|\overline{\mathbf{m}}, A)\mathcal{P}(\overline{\mathbf{m}}|A)$$



# The posterior distribution is much more than a point estimate of the parameters of interest



The full distribution provides estimates of the mean/median of various model parameters

Credible intervals

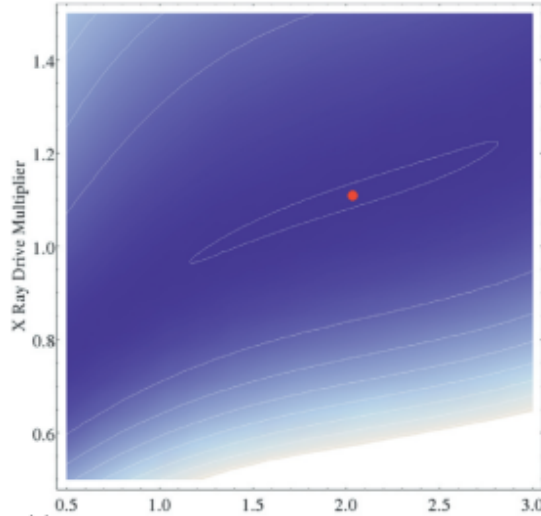
Correlations between parameters

Assess the information content contained in the posterior to

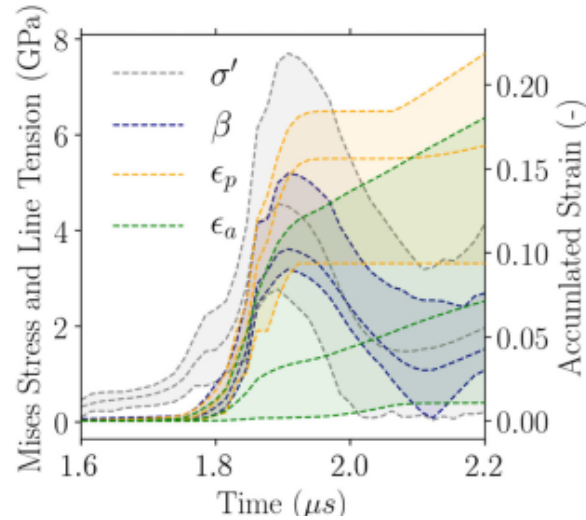
- Evaluate addition of new information
- Determine sensitivity to noise, calibration, model uncertainty, etc.

There are a wide variety of efforts in HED and ICF to exploit the power of Bayesian methods to better understand our data and models

### Model Calibration



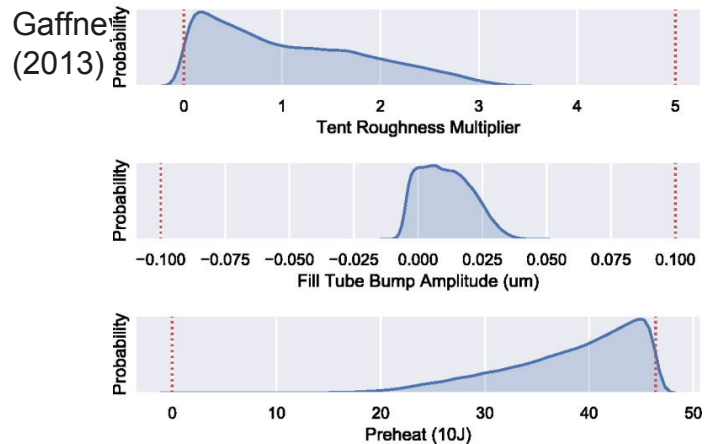
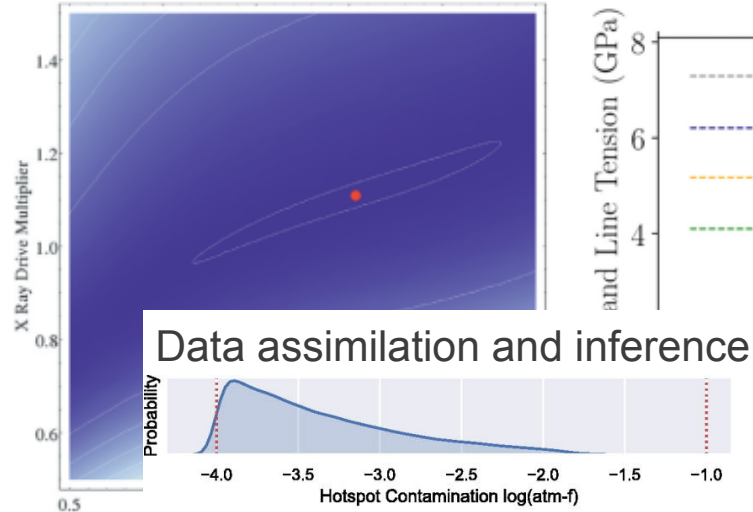
Gaffney et al. Nucl. Fusion 53 (2013)



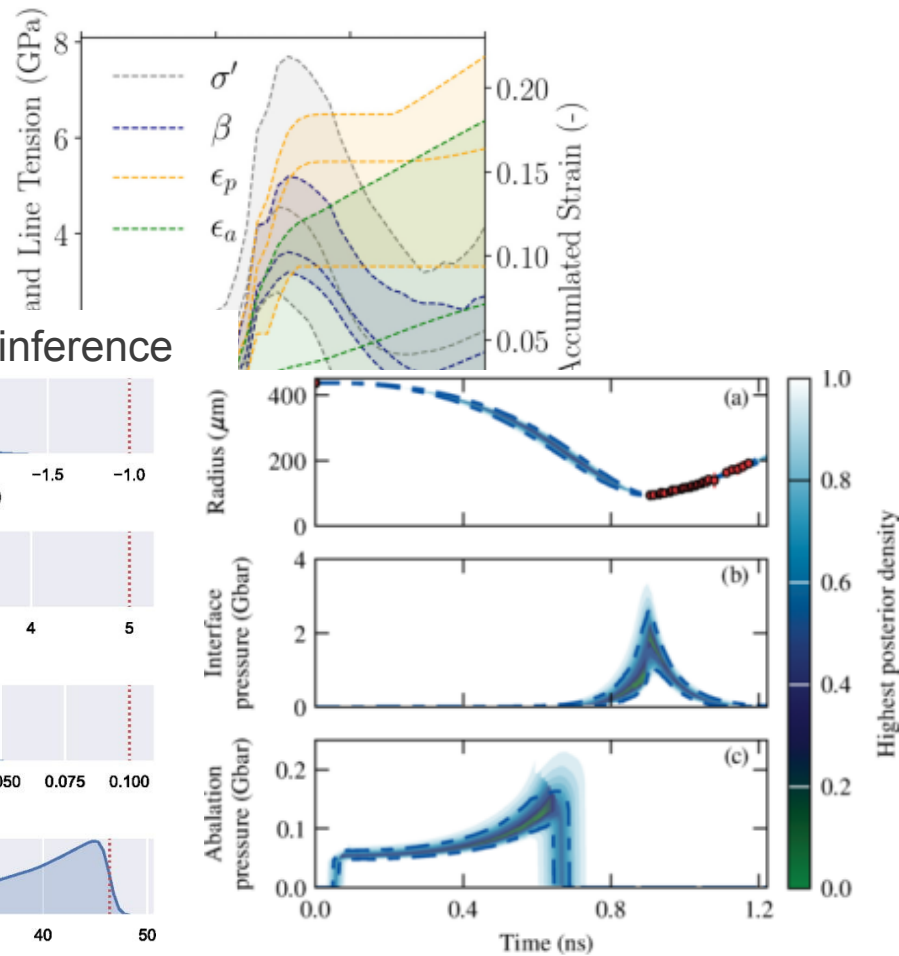
S. Ali et al. J. Appl. Phys. 130, 055901 (2021)

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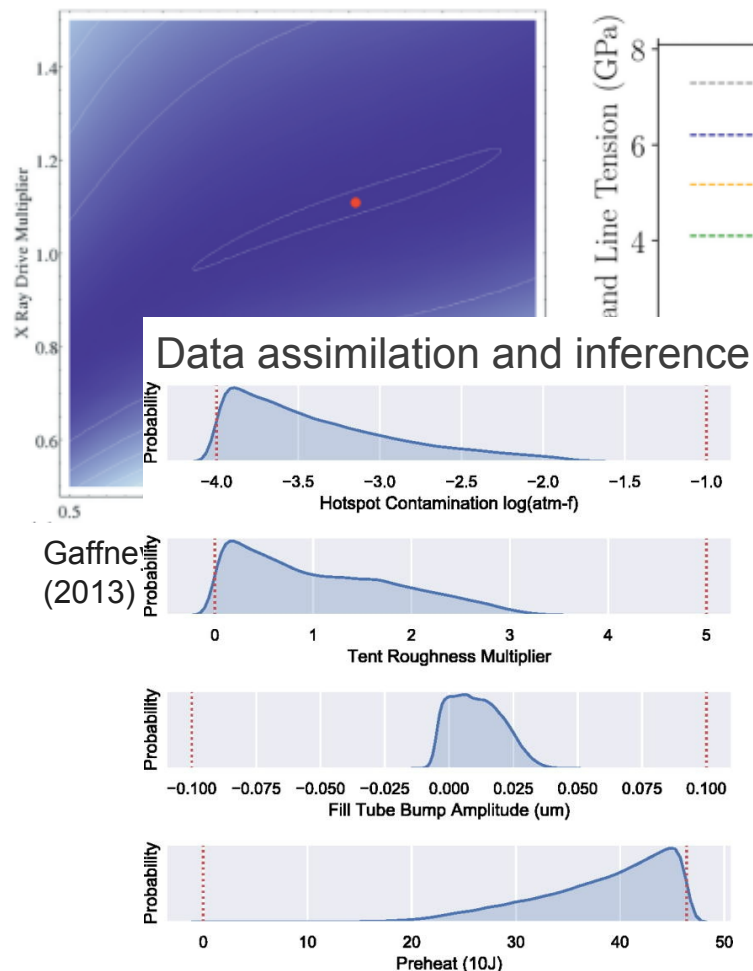
Gaffney et al., *Physics of Plasmas* **26**, 082704 (2019)



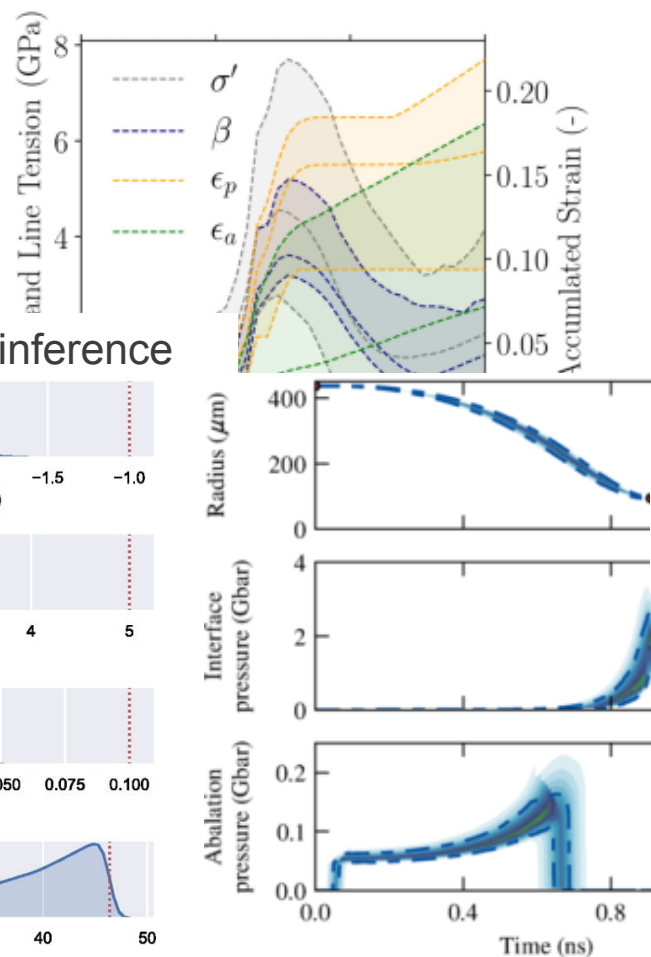
JJ Ruby et al., *Phy. Rev. Letters* **125**, 215001 (2020)

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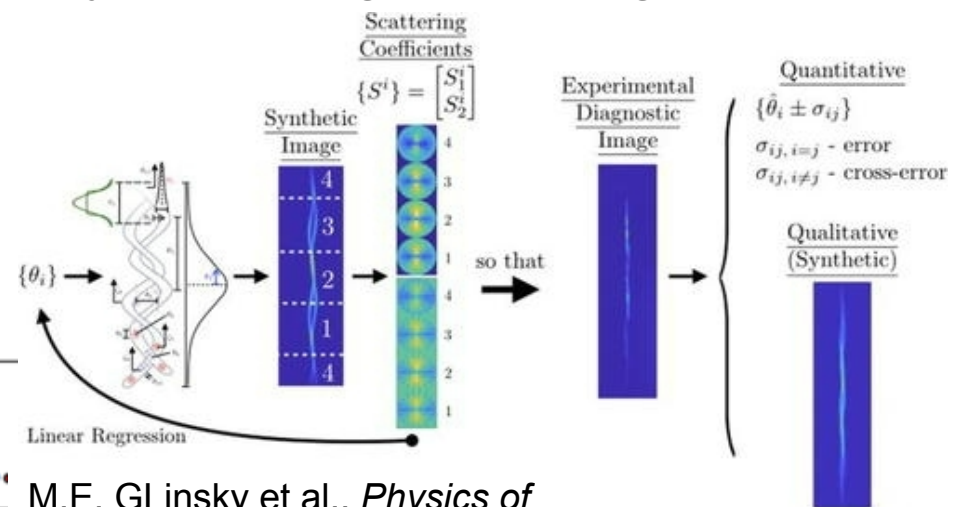


Gaffney et al., *Physics of Plasmas* **26**, 082704 (2019)

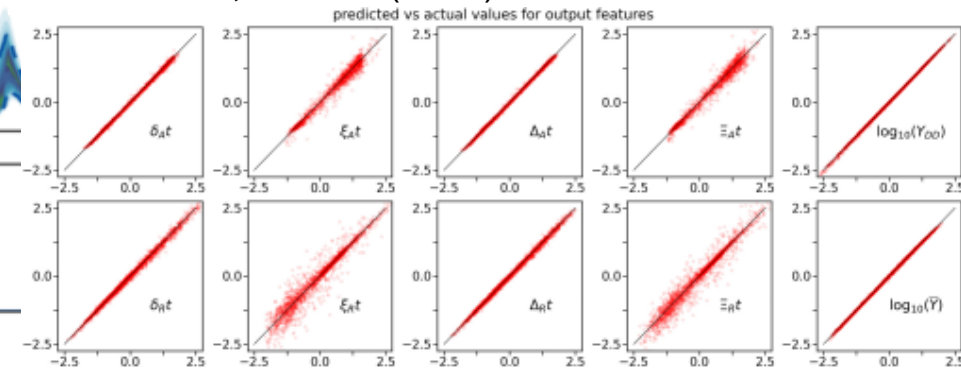


JJ Ruby et al., *Phy. Rev. Lett.* **125**, 215001 (2020)

## Bayesian Surrogate Modeling



M.E. GLinsky et al., *Physics of Plasmas* **27**, 112703 (2020)

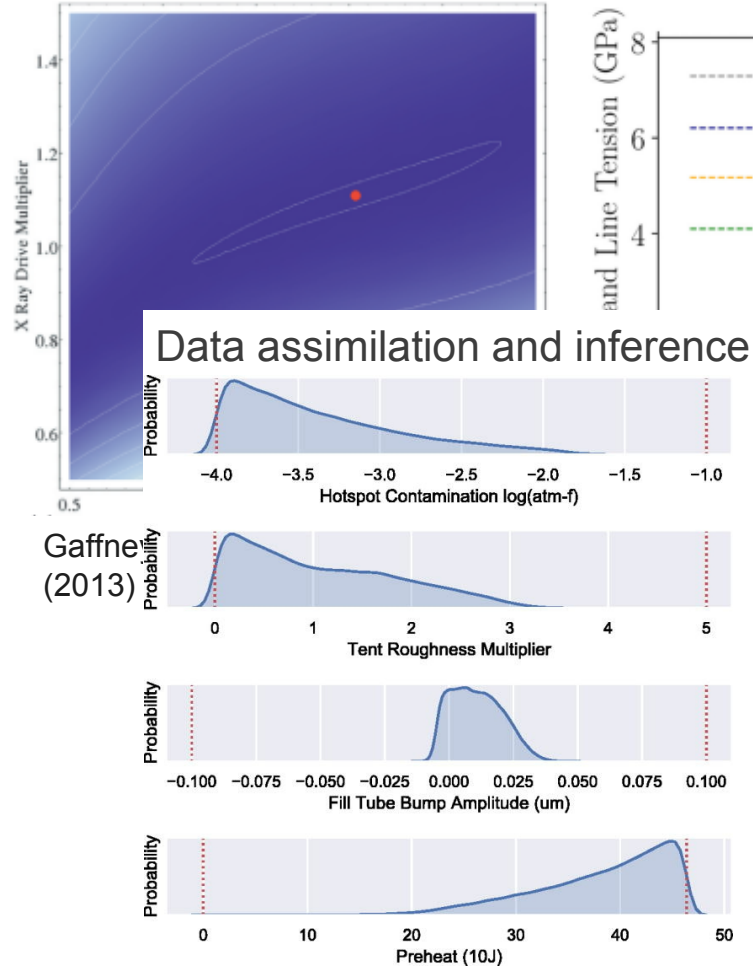


W.E. Lewis et al., *Physics of Plasmas* **28**, 092701 (2021)

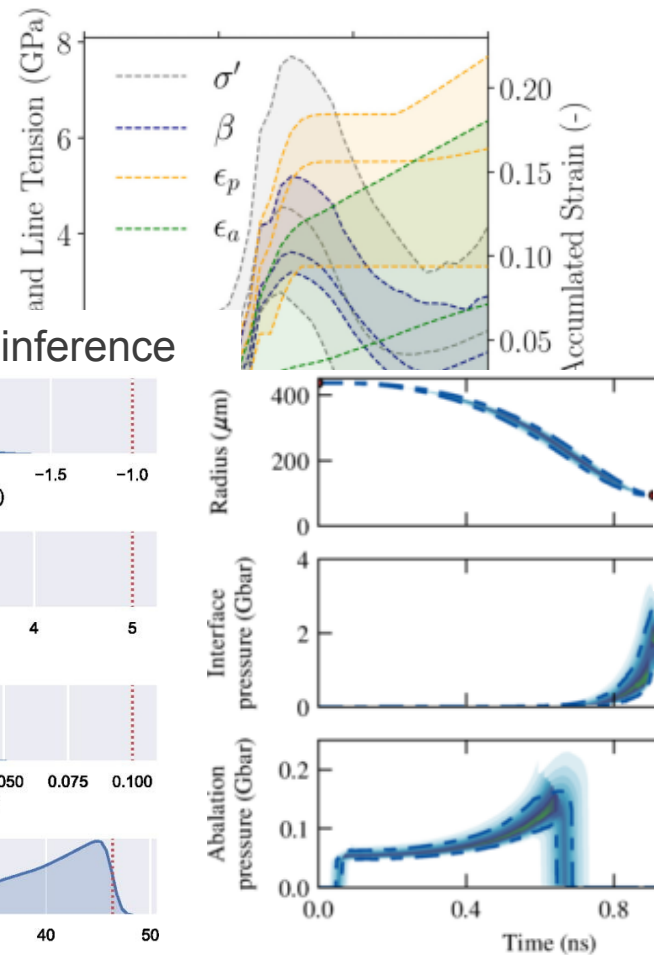
...And many more!

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## Model Calibration

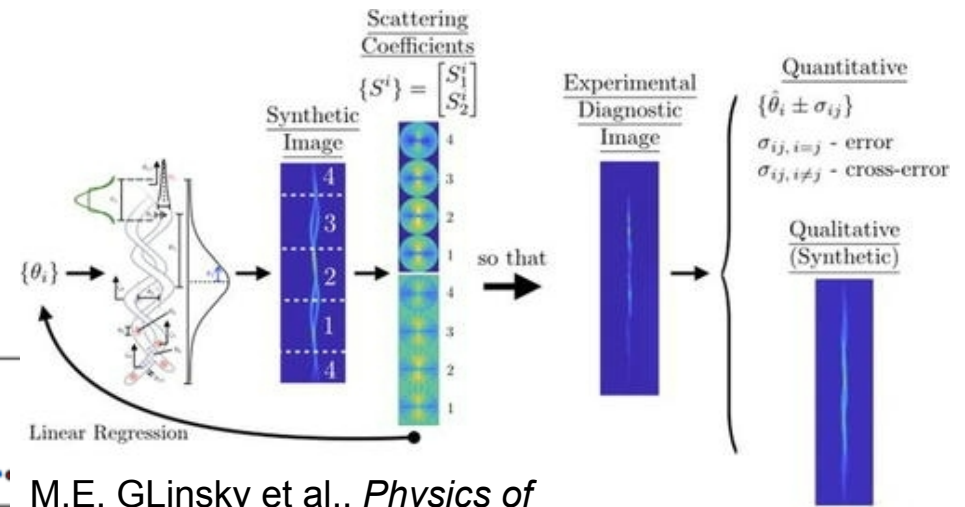


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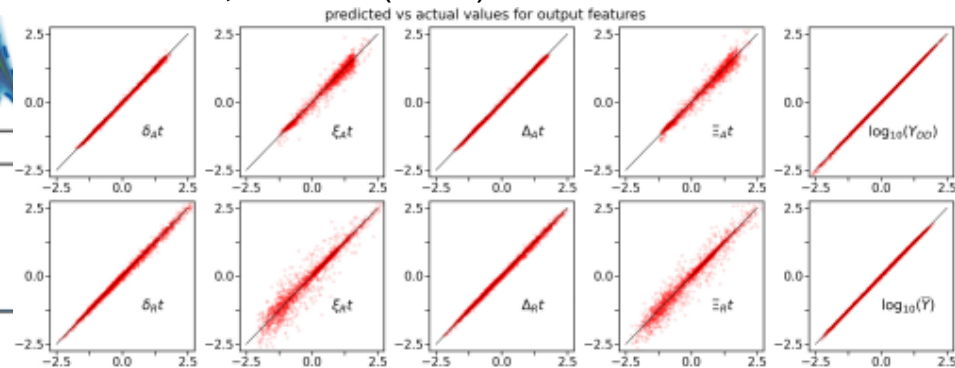


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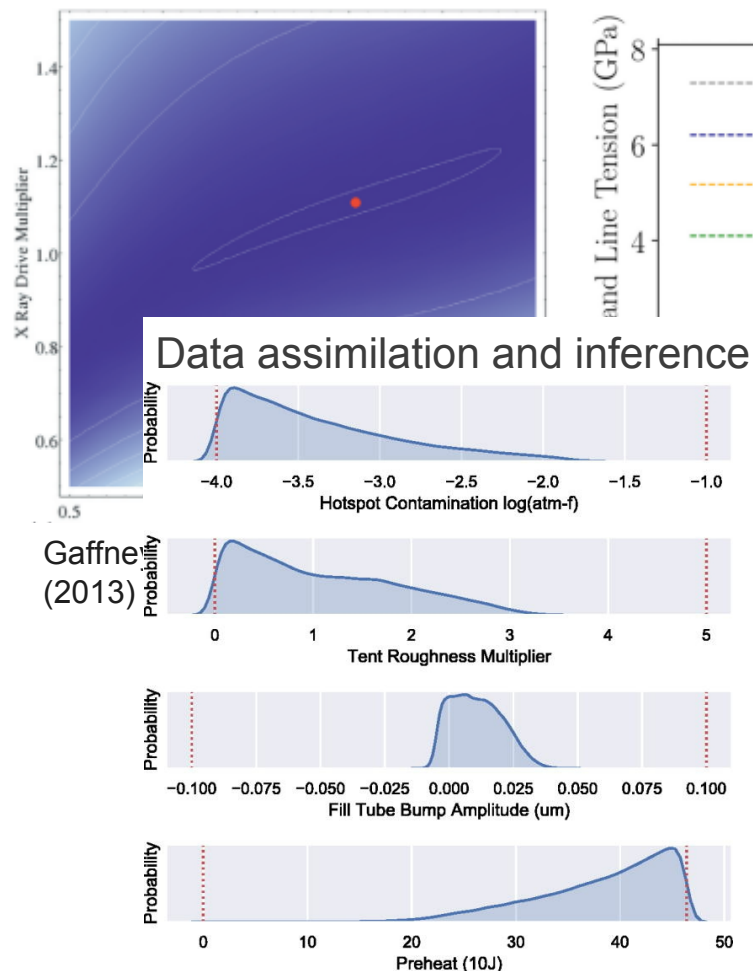
M.E. GLinsky et al., *Physics of Plasmas* **27**, 112703 (2020)



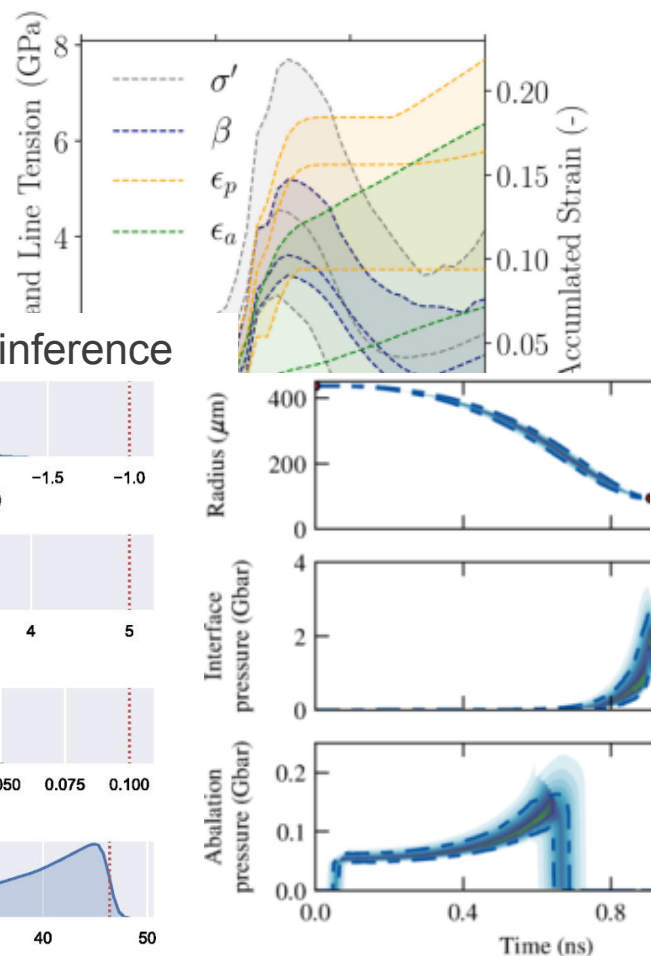
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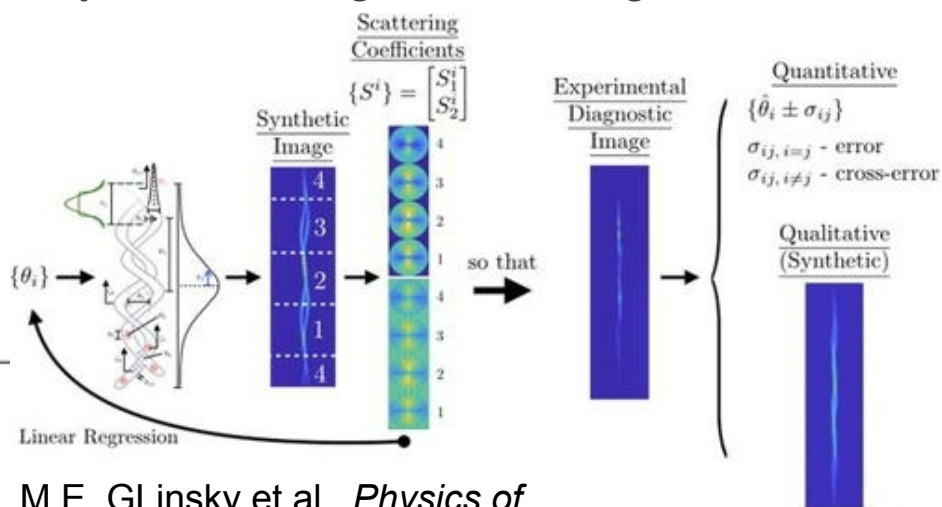


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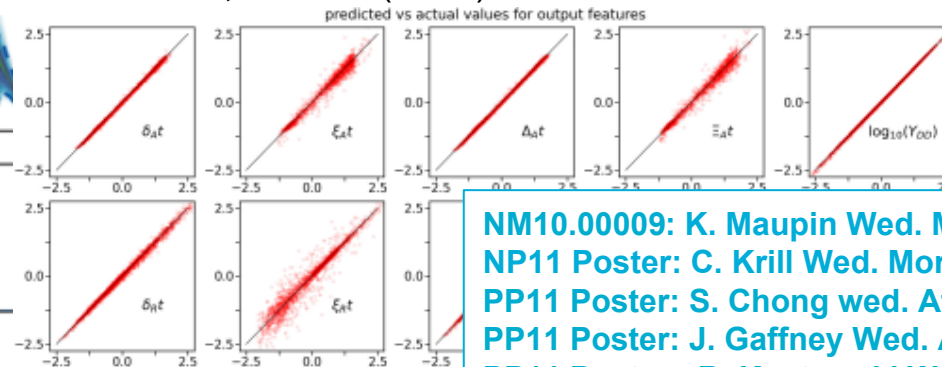


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M.E. GLinsky et al., *Physics of Plasmas* **27**, 112703 (2020)



W.E. Lewis et al., *Physics of Plasmas* **28**, 092701 (2021)

NM10.00009: K. Maupin Wed. Morning  
NP11 Poster: C. Krill Wed. Morning  
PP11 Poster: S. Chong wed. Afternoon  
PP11 Poster: J. Gaffney Wed. Afternoon  
PP11 Poster: B. Kustowski Wed. Afternoon  
TO07.00007: J. Gaffney Thurs. Morning  
TO07.00009: J.L. Peterson Thurs. Morning  
...And many more

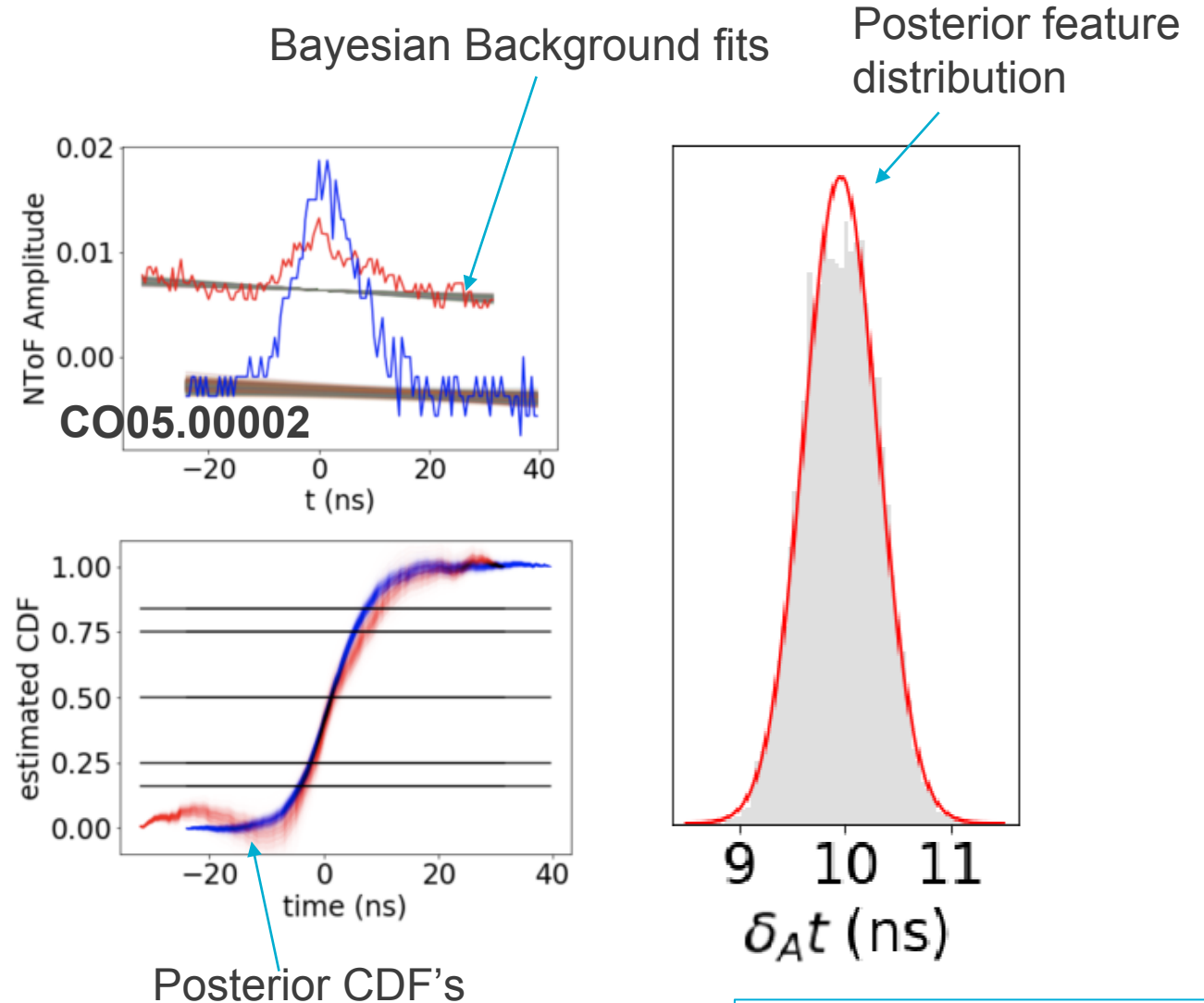
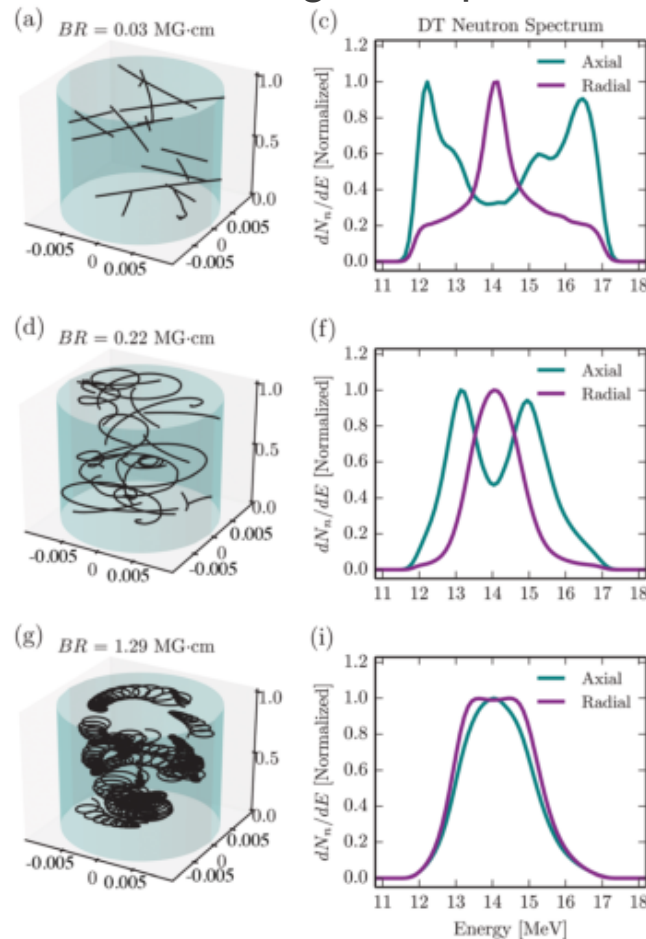
Bayesian methods can be applied to a variety of tasks in the physical sciences to greatly improve how well we use the available information



- **Automated feature extraction**
  - reduce raw data to useful quantities with quantified uncertainties
- **Data Assimilation**
  - Combine experimental data from disparate sources for a self-consistent description of the processes under study
  - Mathematically rigorous uncertainties propagated from all sources (model, experiment, surrogate, etc.)
- **Experiment design and optimization**
  - Utilize the full posterior to guide the design of instruments and experiments to maximize information gain

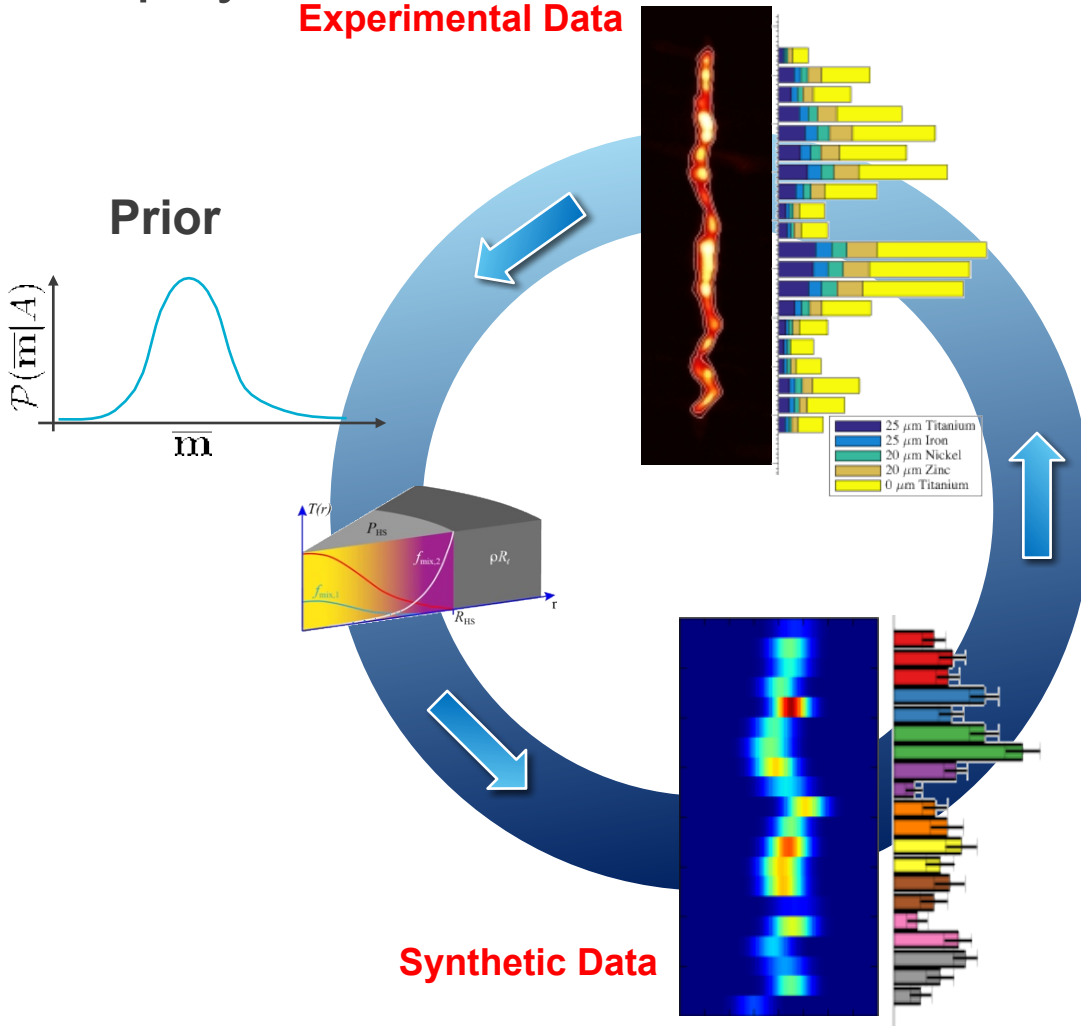
# Bayesian fits to experimental data provide a means to extract features with rigorous uncertainties

In this application the width and asymmetry of the neutron time of flight signal is sensitive to magnetization in MagLIF experiments



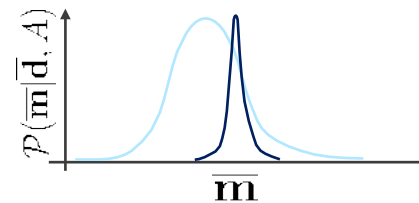
# Bayesian data assimilation provides a means to self-consistently integrate multiple sources of diagnostic information through a physical model

Experimental Data

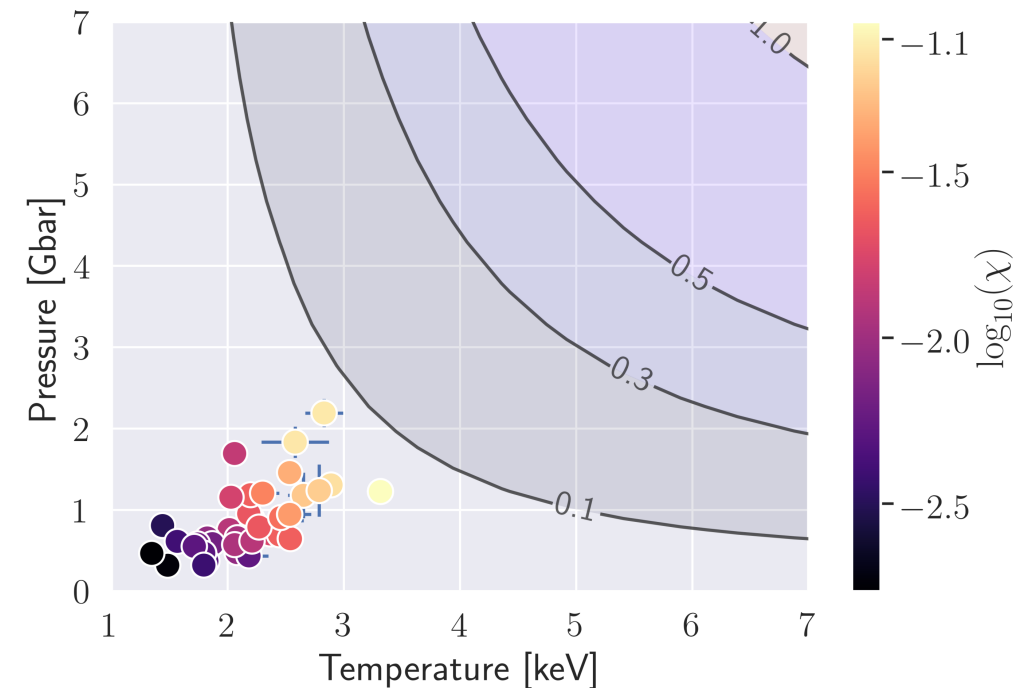


Synthetic Data

Posterior



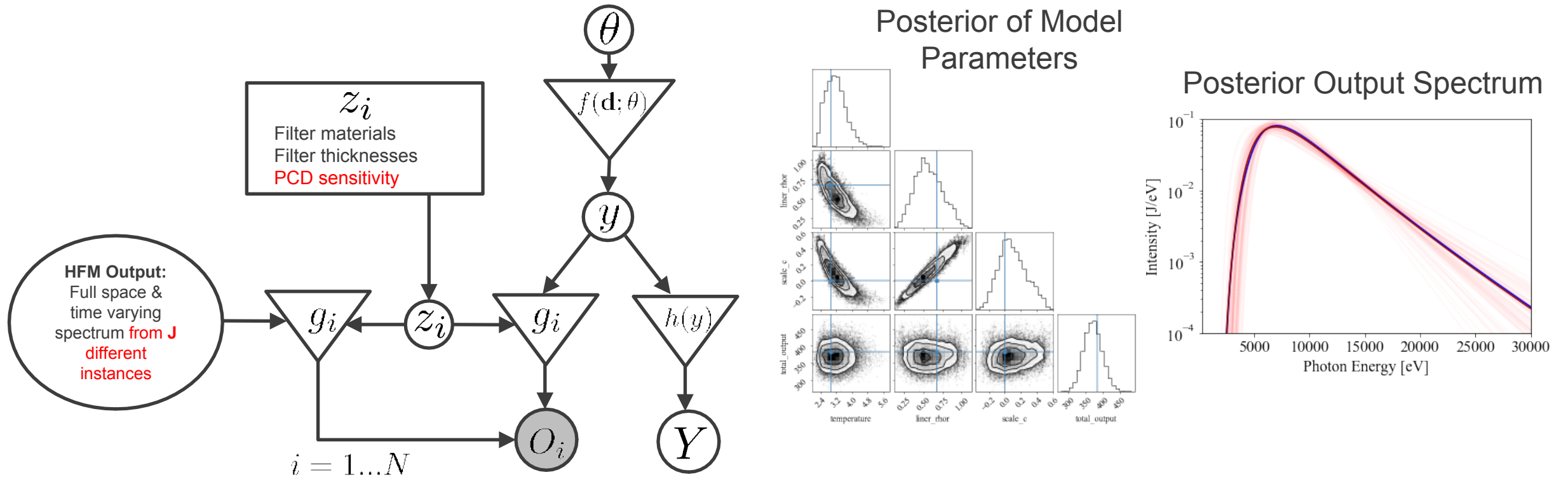
## Bayesian Performance Metrics



# A well constructed posterior provides us with rigorous metrics we can use to find optimal experiment designs



We want to use synthetic data to find the best set of radiation detectors and filters to optimally constrain the source spectrum over a range of possible outcomes



Bayesian Optimization

$$\mathcal{M} = \log(MSE) + \lambda \left( \frac{1}{N_{\text{PCD}}} \sum_{n=1}^{N_{\text{PCD}}} \exp \left( \frac{2V_{\text{peak},n}}{V_{\text{bias}}} \right) - 1 \right)$$

# These examples provide a model for an end-to-end fully Bayesian design, analysis, and integration loop



This Bayesian inference network graphically depicts how we infer important quantities from experimental data

