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# Detecting False Data Injection Attacks in Battery Stacks Using Physics-Based Modeling and Cumulative Sum Algorithm

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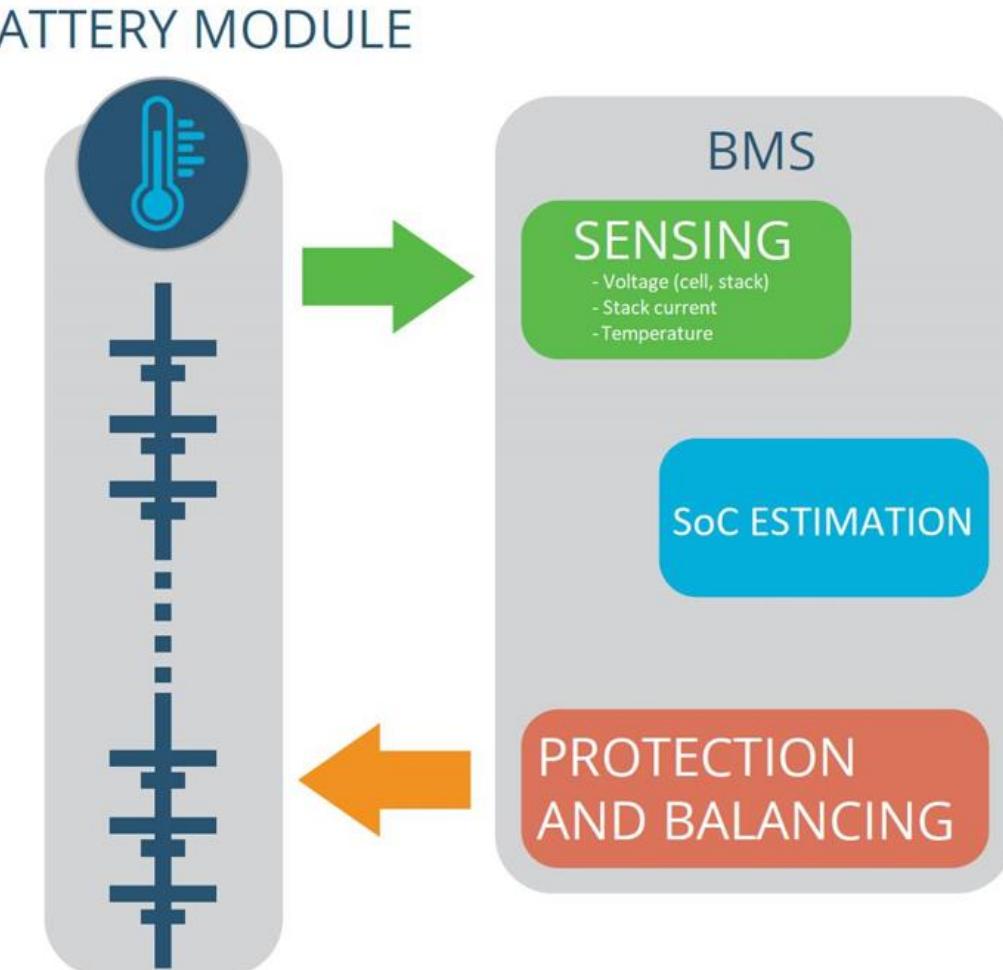
# Introduction and Problem Formulation



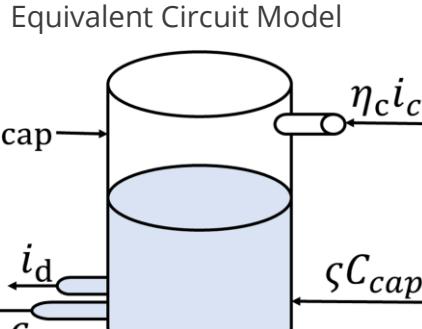
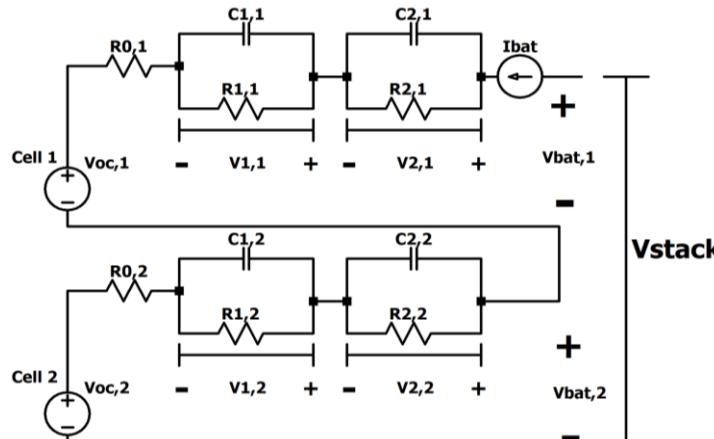
- False Data Injection Attacks (FDIAs) can inject false measurements on sensors, monitor sensor readings, or deny service,
  - Typically evade traditional bad data detectors
  - Can cause equipment malfunction

Contributions of this work:

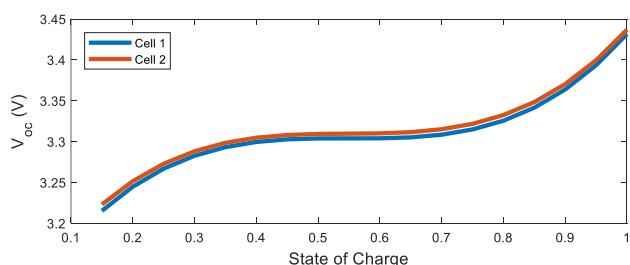
- Accurate SoC estimation for a stack of batteries
  - Current literature focuses on modeling batteries as single cells or modeling stacks of batteries using the "big cell" approximation [1] - [6]
- Quick detection of small magnitude FDIAs in SoC estimation for a stack of batteries using a physical models, an Extended Kalman Filter (EKF), and a statistics-based Cumulative Sum (CUSUM) Algorithm
- Monitoring battery stacks will allow the EKF to compute estimations in the event of some sensor failures – adding robustness to the estimation



# SoC Estimation for Battery Stacks



Battery Charge Reservoir Model



Average Open Circuit Voltage of Cells, as done in [7]

## Governing Equations:

$$x[k+1] = f(x[k], u[k], w[k])$$

$$y[k] = g(x[k], u[k], v[k])$$

where  $w[k] \sim \mathcal{N}(0, Q)$  and  $v[k] \sim \mathcal{N}(0, R)$

$$i_{bat}[k] = i_c[k] + i_d[k]$$

$$\varsigma_1[k+1] = e^{-\eta_{s1}\Delta t} \varsigma_1[k] + \frac{\eta_{c1}\Delta t}{C_{cap_1}} i_c[k] + \frac{\Delta t}{C_{cap_1}} i_d[k]$$

$$\varsigma_2[k+1] = e^{-\eta_{s2}\Delta t} \varsigma_2[k] + \frac{\eta_{c2}\Delta t}{C_{cap_2}} i_c[k] + \frac{\Delta t}{C_{cap_2}} i_d[k]$$

$$v_{1,1}[k+1] = e^{-\frac{\Delta t}{R_{1,1}C_{1,1}}} v_{1,1}[k] + \frac{\Delta t}{C_{1,1}} i_c[k] + \frac{\Delta t}{C_{1,1}} i_d[k]$$

$$v_{2,1}[k+1] = e^{-\frac{\Delta t}{R_{2,1}C_{2,1}}} v_{2,1}[k] + \frac{\Delta t}{C_{2,1}} i_c[k] + \frac{\Delta t}{C_{2,1}} i_d[k]$$

$$v_{1,2}[k+1] = e^{-\frac{\Delta t}{R_{1,2}C_{1,2}}} v_{1,2}[k] + \frac{\Delta t}{C_{1,2}} i_c[k] + \frac{\Delta t}{C_{1,2}} i_d[k]$$

$$v_{2,2}[k+1] = e^{-\frac{\Delta t}{R_{2,2}C_{2,2}}} v_{2,2}[k] + \frac{\Delta t}{C_{2,2}} i_c[k] + \frac{\Delta t}{C_{2,2}} i_d[k]$$

$$v_{bat_1}[k] = v_{oc1}(\varsigma_1[k]) + v_{1,1}[k] + v_{2,1}[k] + R_{0,1}(i_c[k] + i_d[k])$$

$$v_{bat_2}[k] = v_{oc2}(\varsigma_2[k]) + v_{1,2}[k] + v_{2,2}[k] + R_{0,2}(i_c[k] + i_d[k])$$

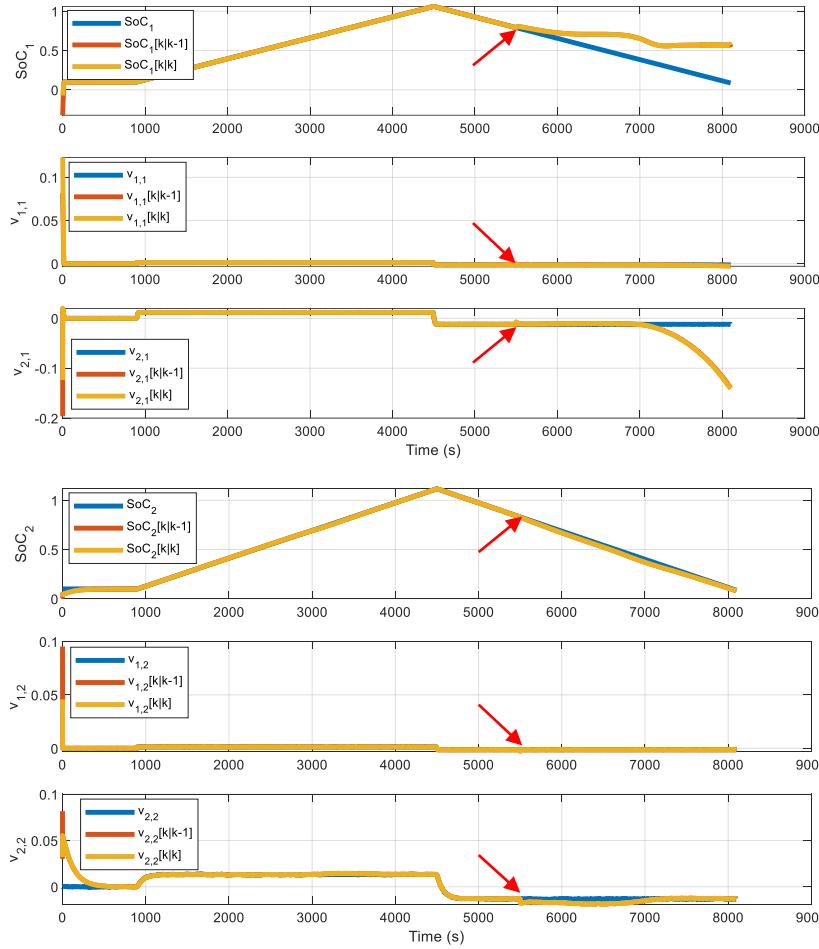
$$v_{stack}[k] = v_{bat_1}[k] + v_{bat_2}[k]$$

$k, \Delta t$	Current time step, sampling time	Kalman Filter Variables	
$u$	System input		
$y, \hat{y}$	Model output, predicted output		
$x, \hat{x}$	State, predicted state		
$w$	Process noise		
$v$	Measurement noise		
$\varsigma_1$	Battery SoC for Cell 1	System State Variables	
$v_{1,1}$	RC voltage drop 1 for cell 1		
$v_{2,1}$	RC voltage drop 2 for cell 1		
$\varsigma_2$	Battery SoC for Cell 2		
$v_{1,2}$	RC voltage drop 1 for cell 2	System Inputs	
$v_{2,2}$	RC voltage drop 2 for cell 2		
$i_d$	Discharge current		
$i_c$	Charge current		
$v_{bat_1}$	Battery voltage for cell 1	System Outputs	
$v_{bat_2}$	Battery voltage for cell 2		
$v_{stack}$	Battery stack voltage		
$i_{bat}$	Battery current		

## Extended Kalman Filter:

- Required to estimate the SoC of the battery stack using the nonlinear relationship between open circuit voltages and SoC
- The a priori measurement residuals derived from the EKF are used in the CUSUM algorithm to detect FDIs

# Detection of FDIA in Battery Stacks



Attack of 10 mV added to the  $v_{bat_1}$  measurement at  $t = 5500$ , for visualization purposes. Estimated states for Cell 1 (top) and Cell 2 (bottom)

## Cumulative Sum Algorithm:

- Performed using a priori residual data with mean ( $\mu = 0$ ):

$$z[k|k-1] = y[k] - \hat{y}[k|k-1]$$

- Population Standard Deviation:

$$\sigma_z = \frac{A_3 \bar{s}}{3}$$

- Upper / Lower Control Limit:

$$UCL = h\sigma_z, LCL = -h\sigma_z$$

- High and Low CUSUM:

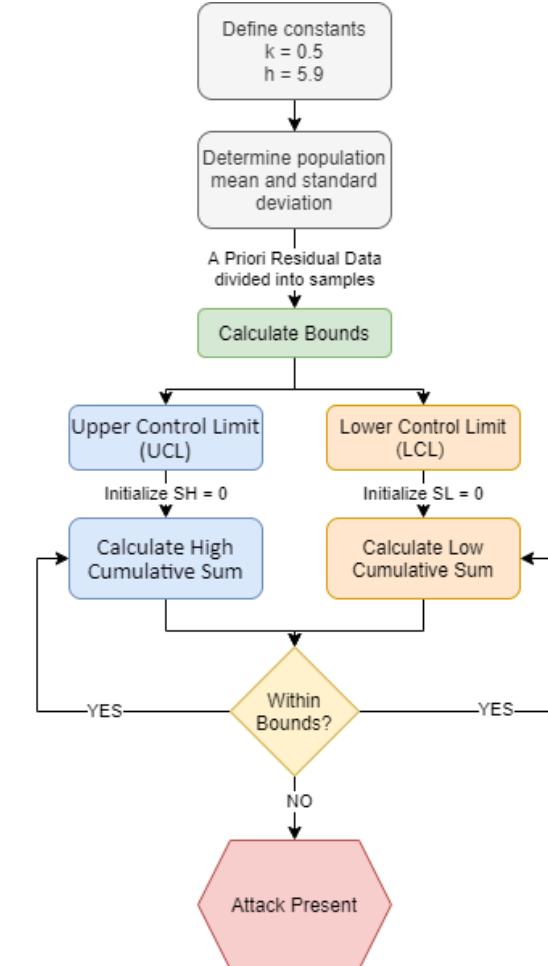
$$SH_i = \max(0, \bar{z}_i - \mu - k\sigma_z + SH_{i-1})$$

$$SL_i = \min(0, \bar{z}_i - \mu + k\sigma_z + SL_{i-1})$$

- Determine presence of attack:

$$SH_i > UCL \text{ or } SL_i < LCL \rightarrow \text{attack present}$$

$$SH_i \leq UCL \text{ and } SL_i \geq LCL \rightarrow \text{no attack}$$

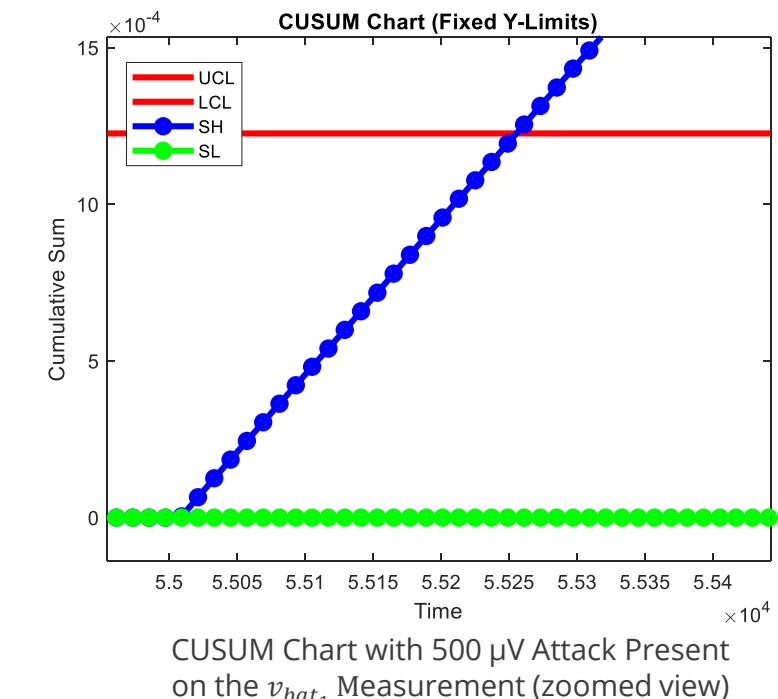
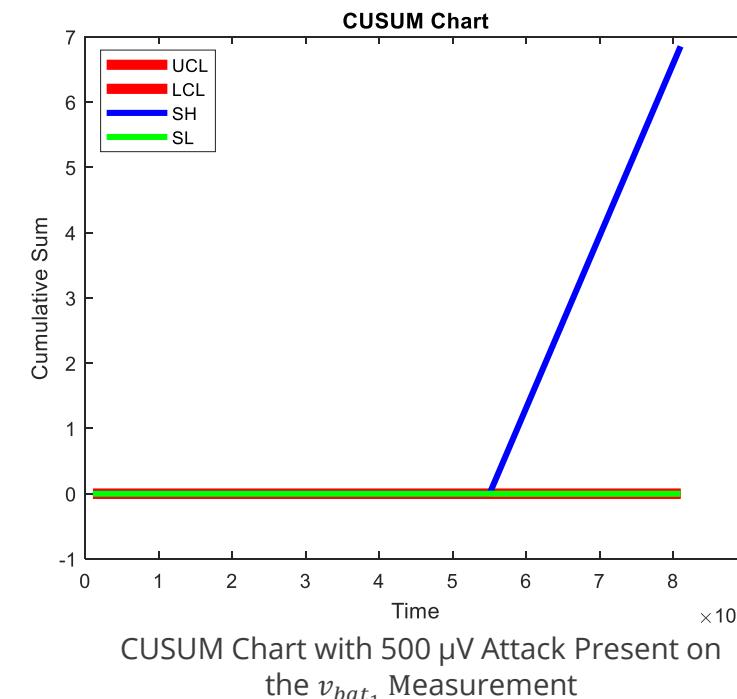
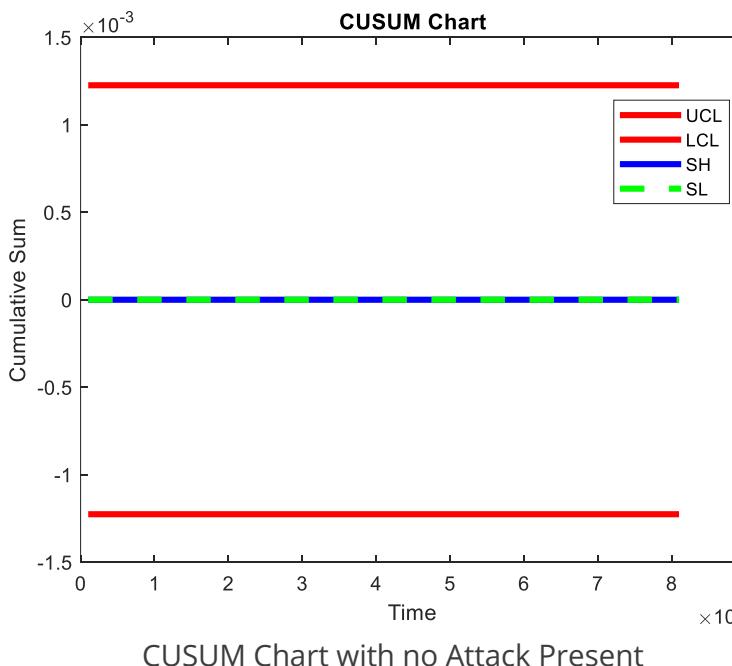


CUSUM Algorithm Flowchart

# Results and Conclusions



- The method described can be used to quickly detect FDIA in BESS state estimation
  - This CUSUM Algorithm could detect attacks as low as  $500 \mu\text{V}$  added to  $v_{bat_1}$  measurement
  - The algorithm resulted in zero false alarms
- Performing estimation with a stack of batteries, rather than a single cell, adds redundancy to the measurements allowing the system to remain observable when all but one sensor failed
  - Created a more robust estimation algorithm





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## Project Deliverables and Publications

- V. Obrien, R. D. Trevizan and V. Rao, "Detecting False Data Injection Attacks to Battery State Estimation Using Cumulative Sum Algorithm," *53<sup>rd</sup> North American Power Symposium (NAPS)*, Nov. 2021 pp 1-6, *Accepted for publication*.
- V. Obrien, R. D. Trevizan, and V. Rao, " Detection of false data injection attacks targeting state of charge estimation of battery energy storage systems," *2021 Advanced Energy Conference*, Jun 2021. *Winner of best graduate student poster award*.

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