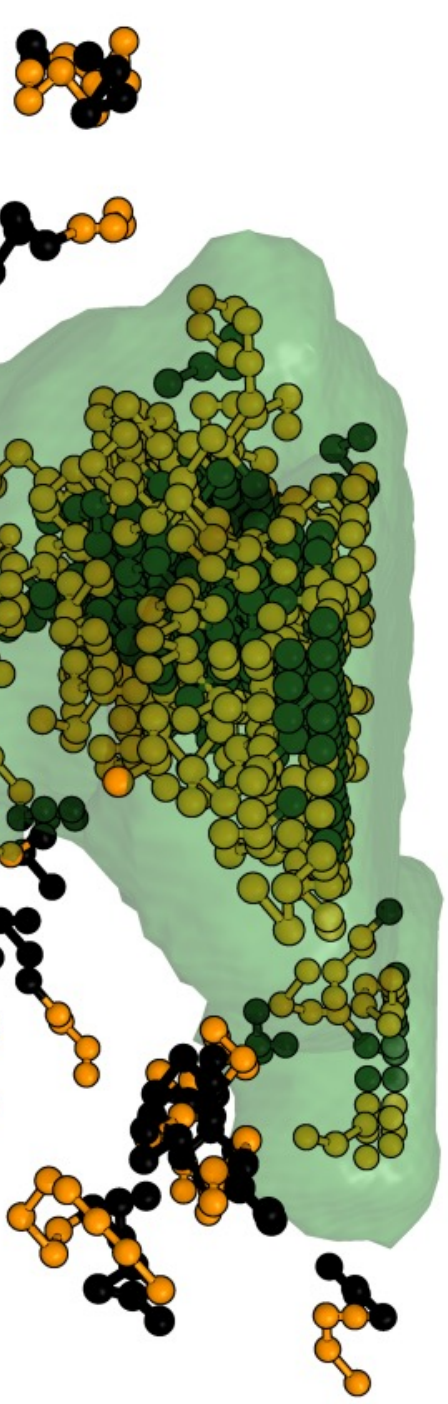


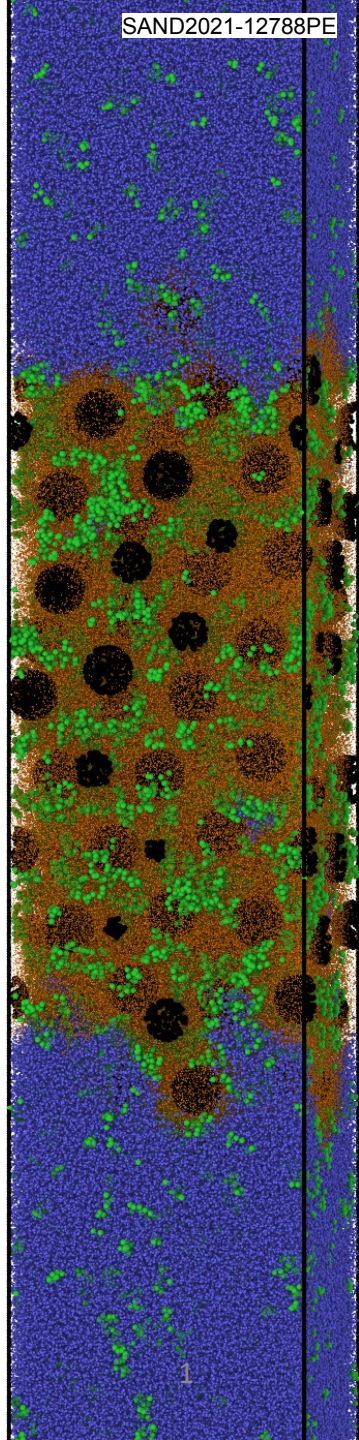


Molecular Simulation of Soft Matter Self-Assembly and Phase Behavior

Andrew Santos, PhD

TSM Branch Seminar

October, 13th 2021

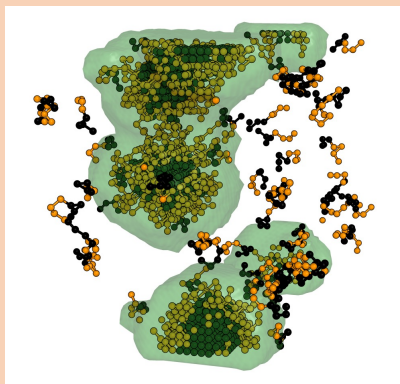


Materials

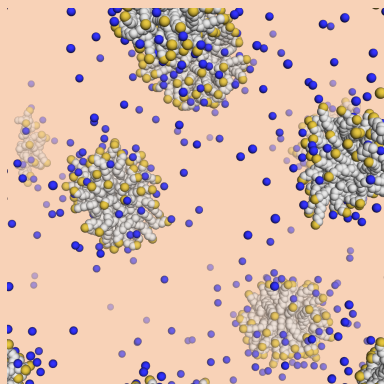
2

Surfactants

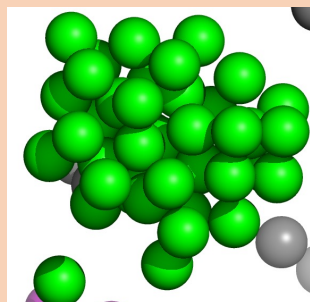
nonionic



ionic

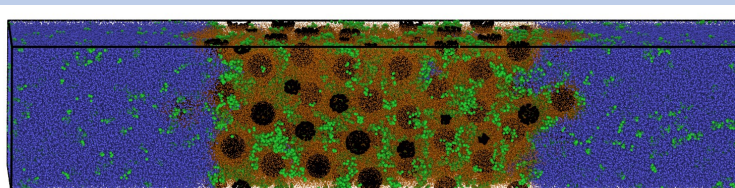


SALR Colloids

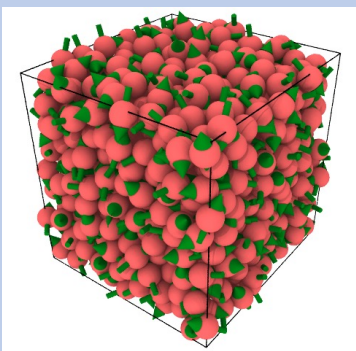


Nanocomposites

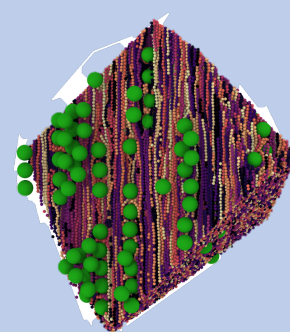
Grafted-NP



Magnetic

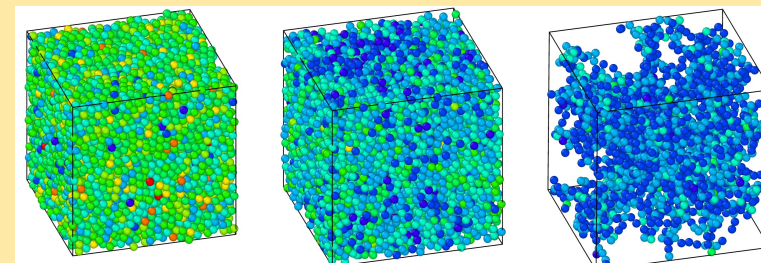


Bare NPs

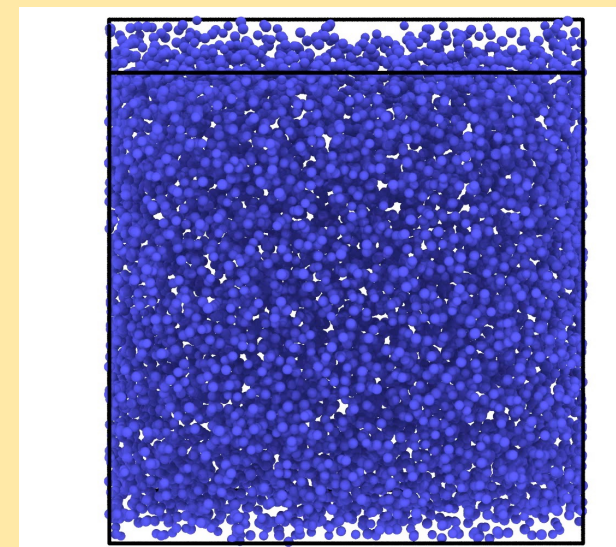


Granular

Packings



Flow



Methods

3

Surfactants

Molecular Dynamics (MD)

- NVT ensembles
- Gromacs, Hoomd, LAMMPS

Monte Carlo (MC)

- μVT , NVT ensembles
- Cassandra, Legacy code (Fortran)

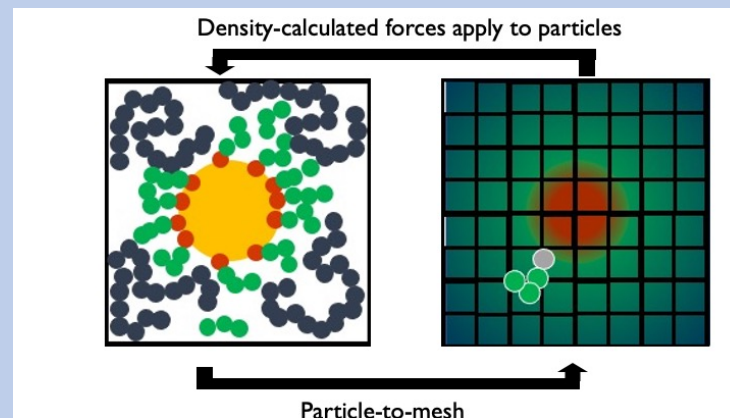
Law-of-mass-action modelling

Nanocomposites

Molecular dynamics

Theoretically-informed Langevin dynamics (TILD)

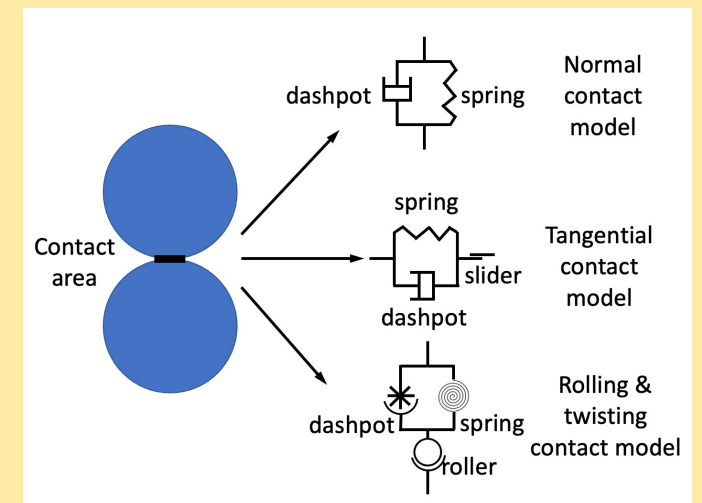
- MD evolves simulation of particles
- Force on particle is calculated from a field-based interaction
- Fast for dense systems
- Thermal fluctuations
- Implemented into LAMMPS



Granular

Discrete element modeling (DEM)

- Forces calculated at contact
- Requires memory of interaction
- Dissipative, out-of-equilibrium
- LAMMPS

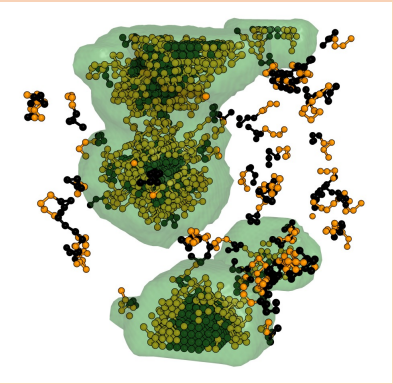


Materials

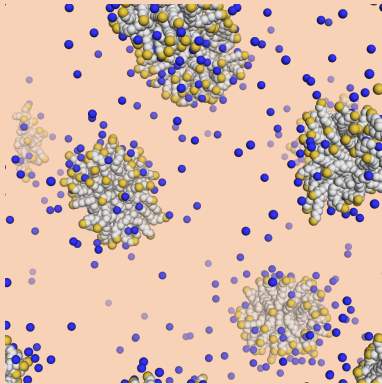
4

Surfactants

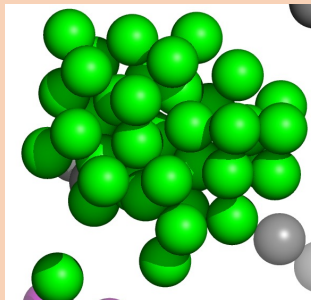
nonionic



ionic

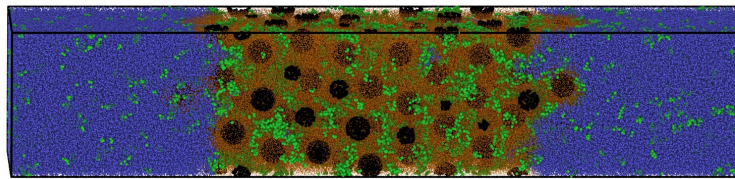


Colloids

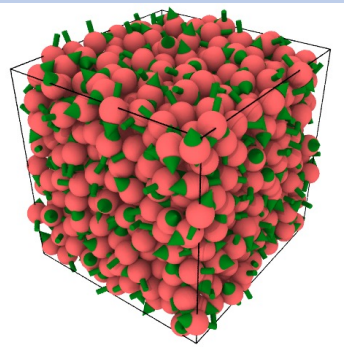


Nanocomposites

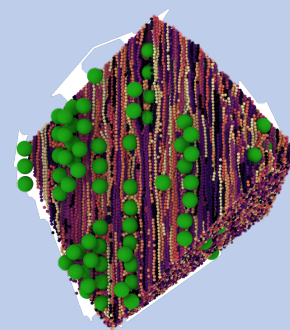
Grafted-NP



Magnetic

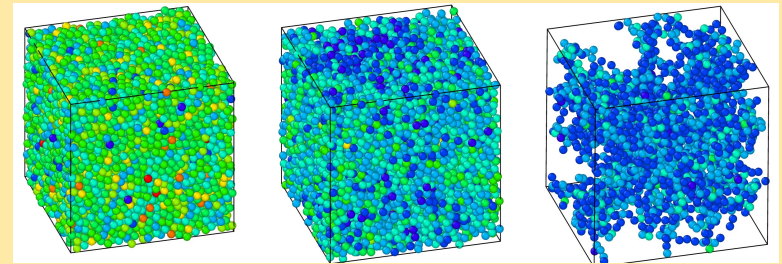


Bare NPs

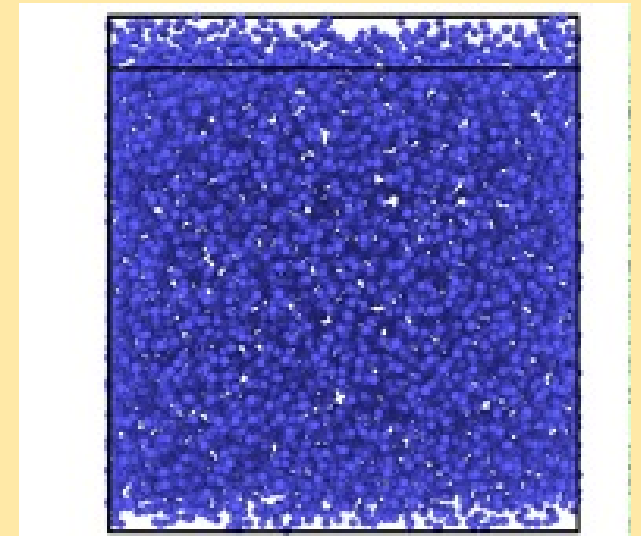


Granular

Packings

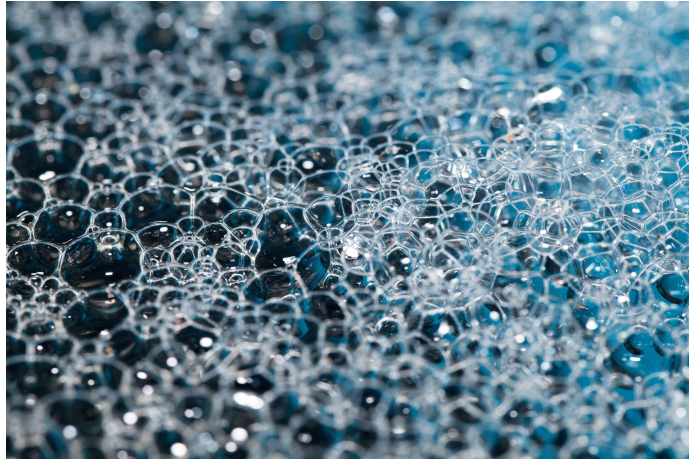


Flow

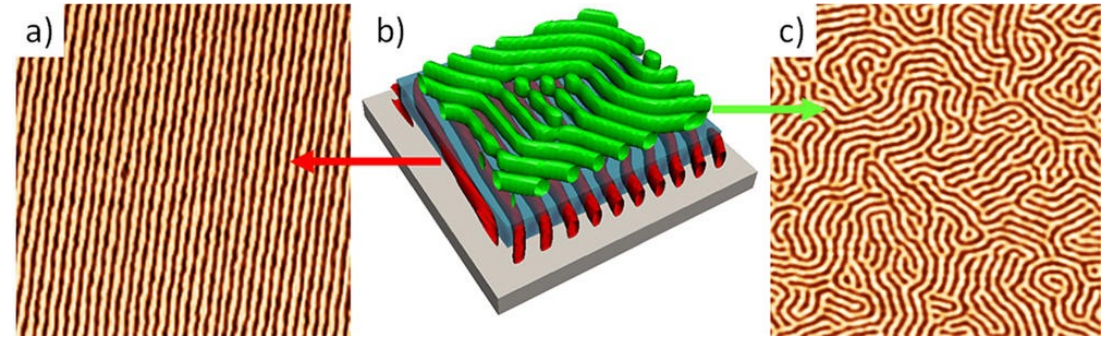


Amphiphile self-assembly for complex materials

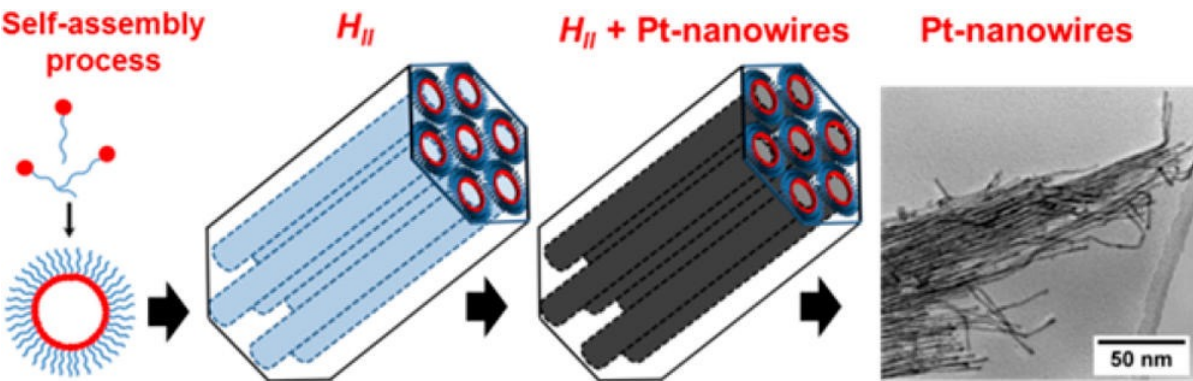
Detergency



Thin films



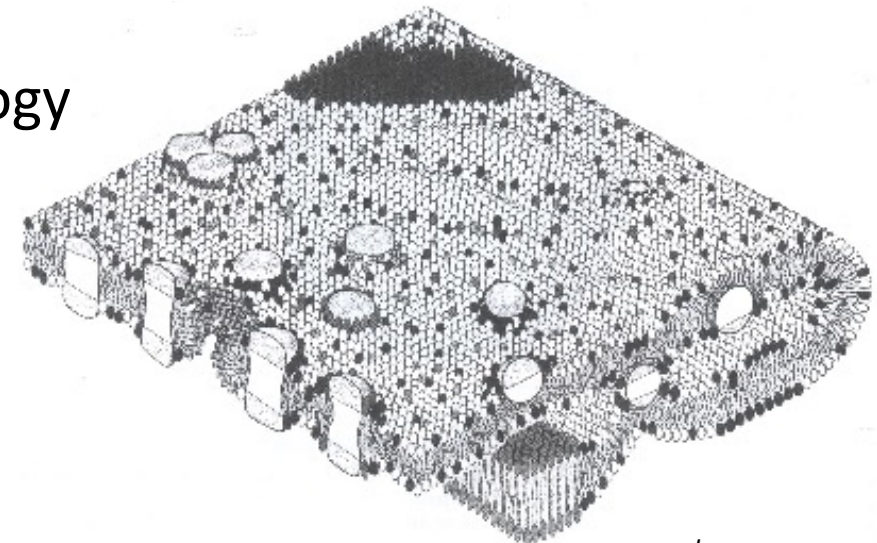
Register et al., *Macromolecules*, 7588–7596, 2016



Nanotechnology

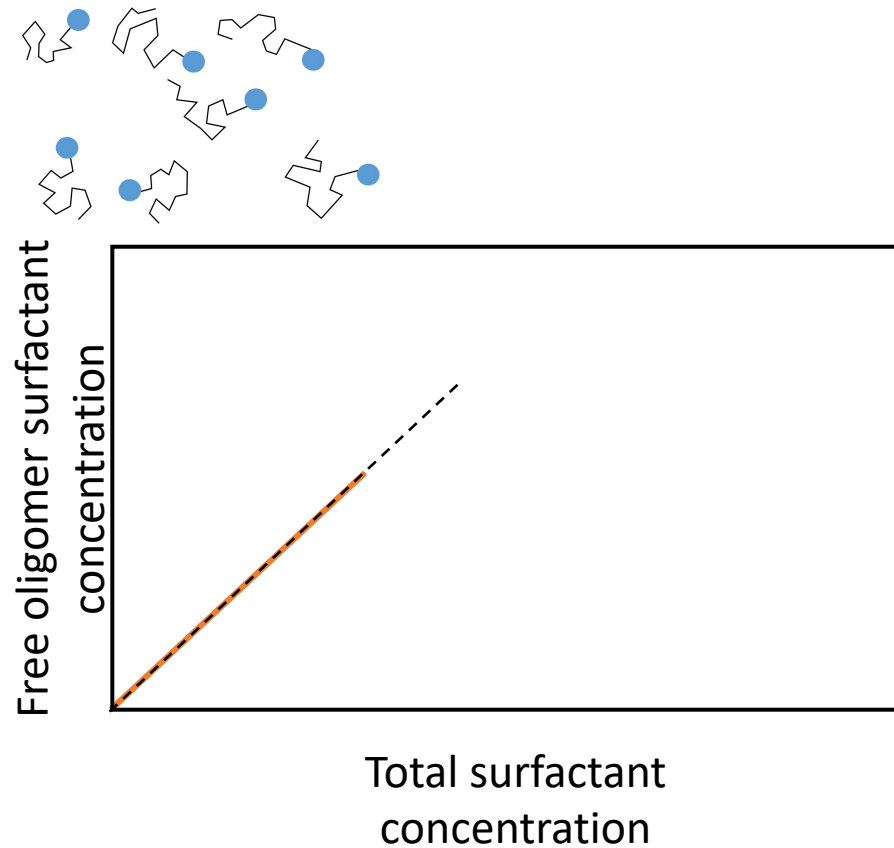
Squires et al., *Langmuir*, 6991–6996, 2018

Biology



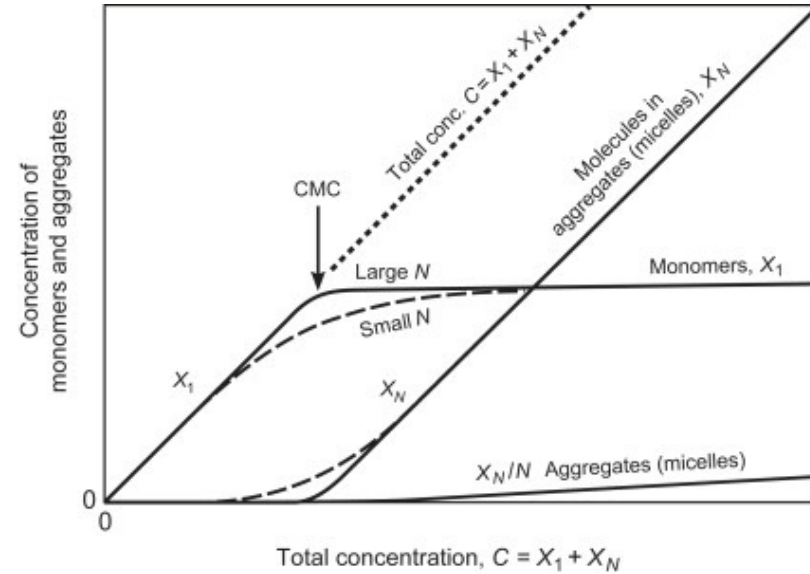
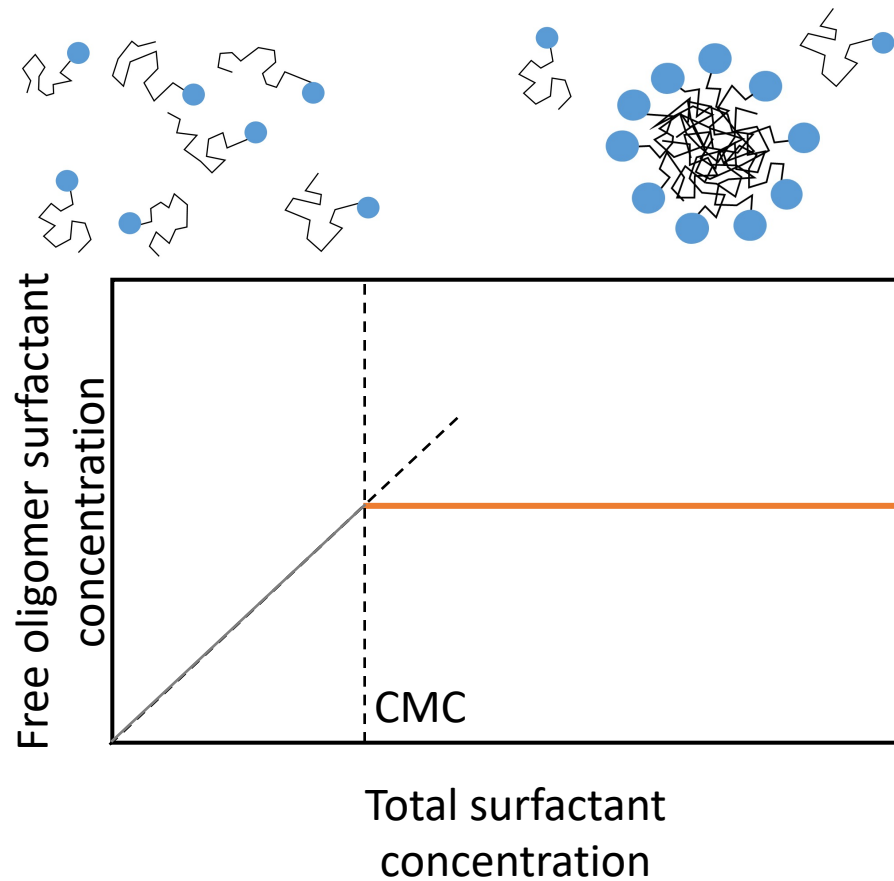
Israelachvili, *Intermolecular and Surface Forces 3rd ed.*, 2011

Surfactant micellization



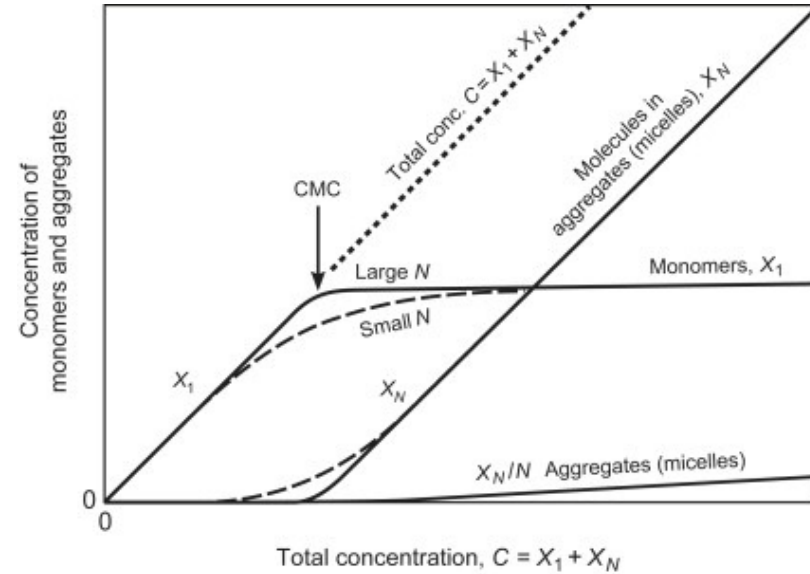
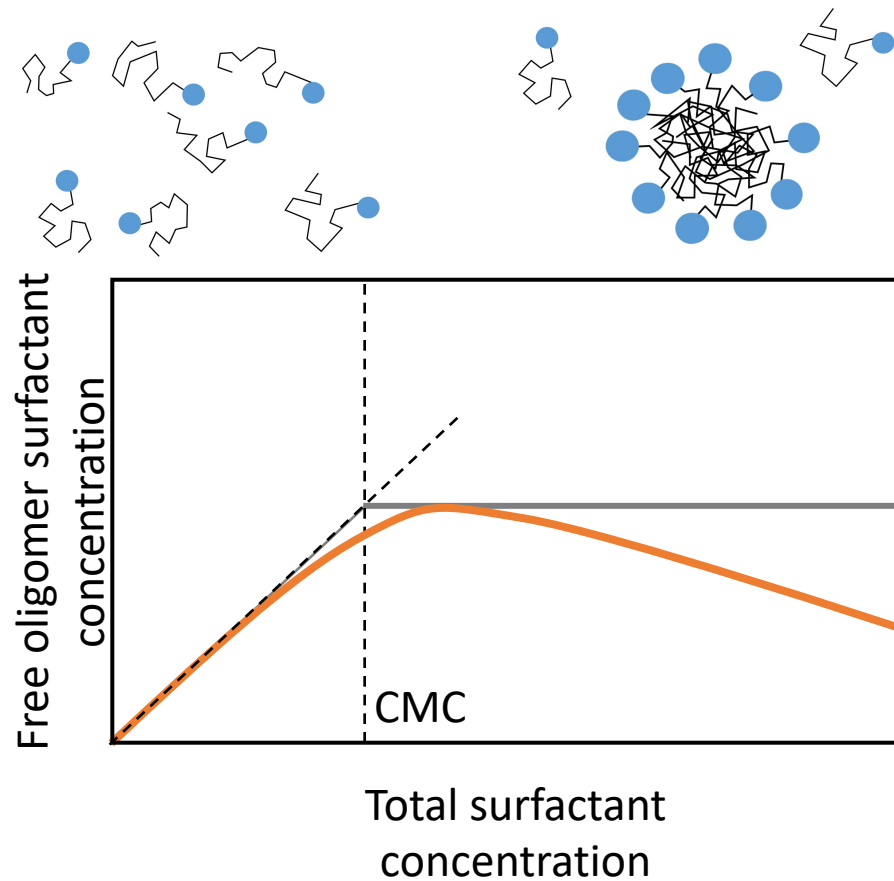
Surfactant micellization

7



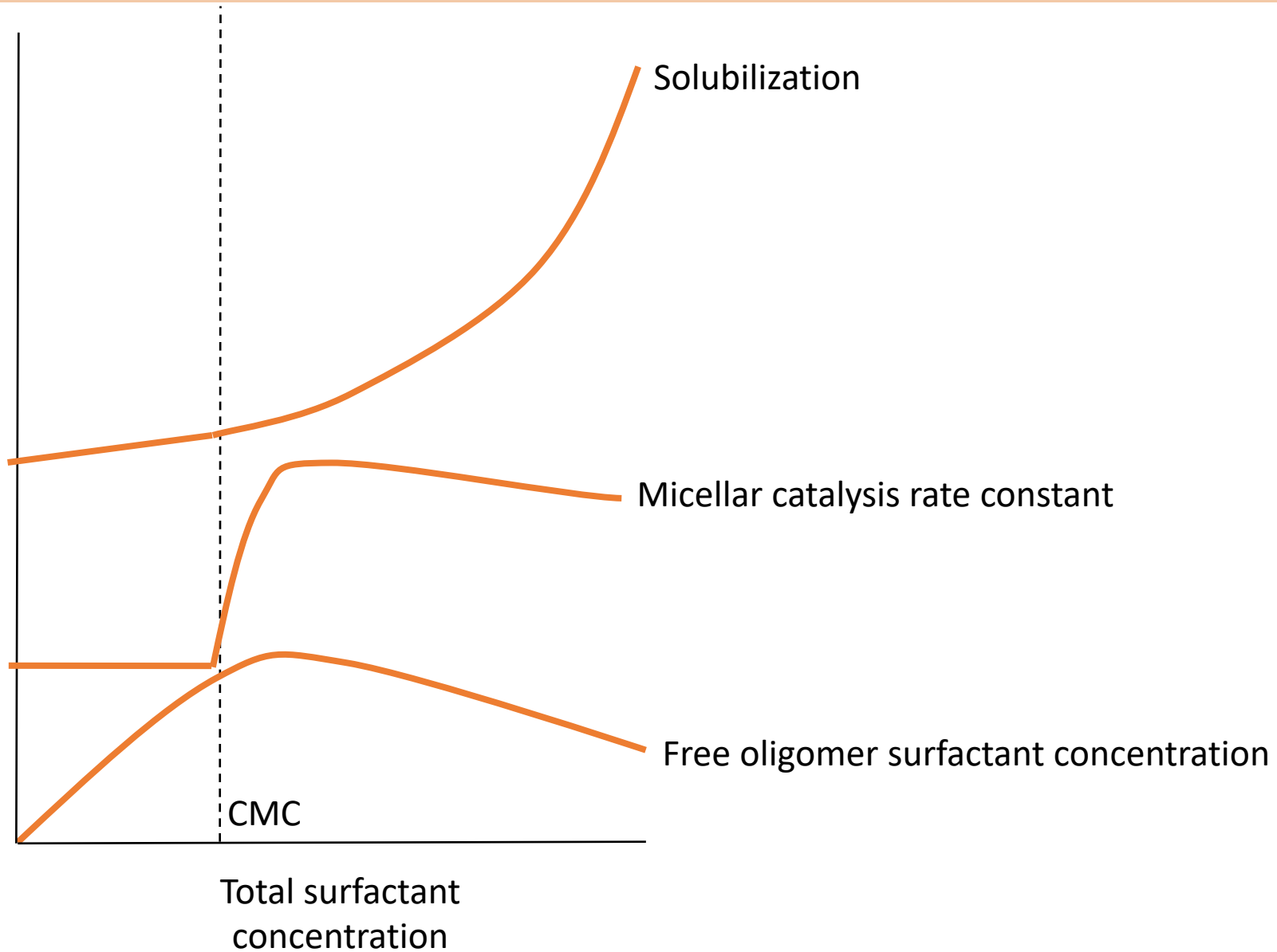
Israelachvili, *Intermolecular and Surface Forces*
3rd ed., 2011

Surfactant micellization

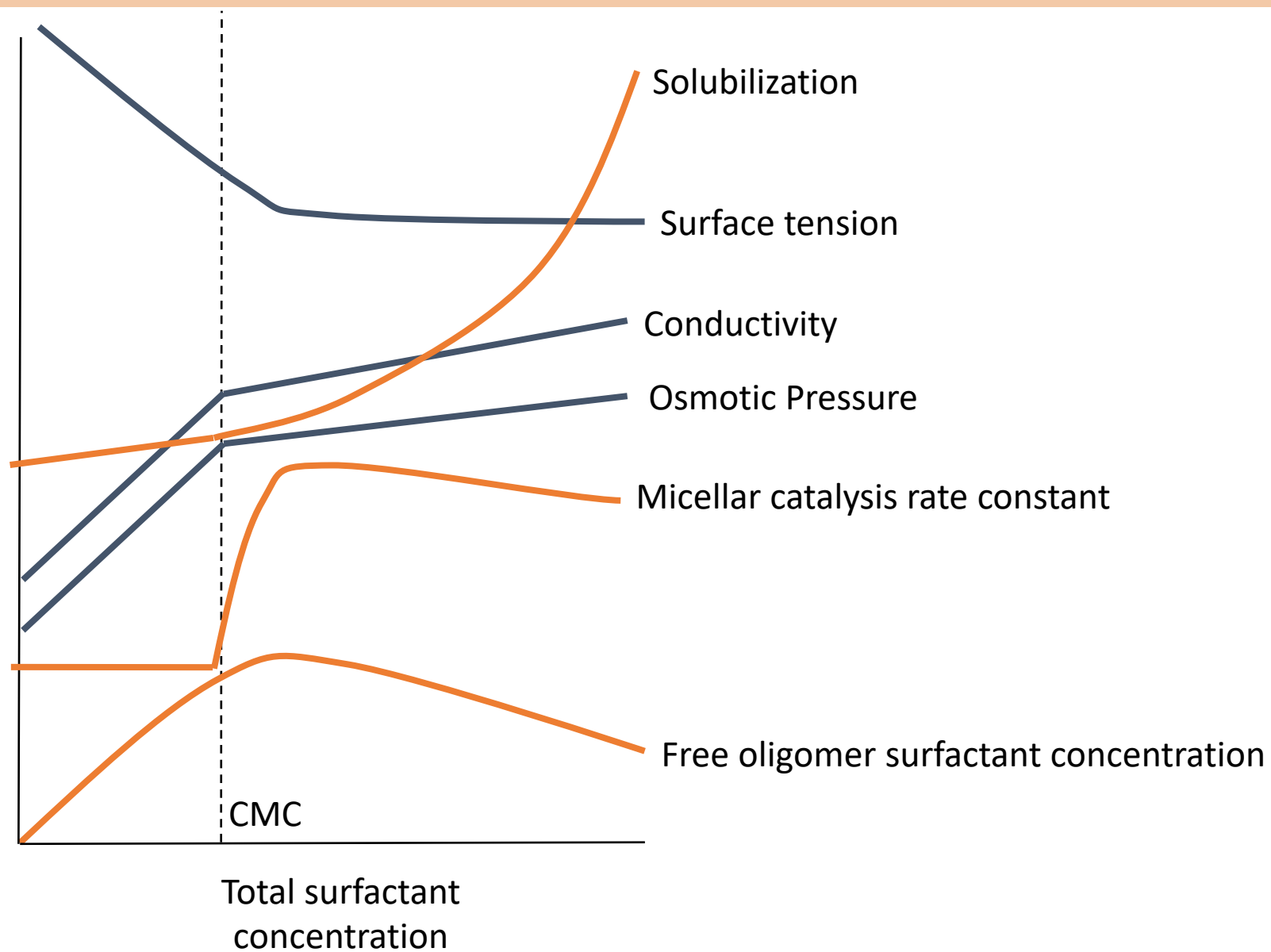


Israelachvili, *Intermolecular and Surface Forces*
3rd ed., 2011

Surfactant micellization



Surfactant micellization



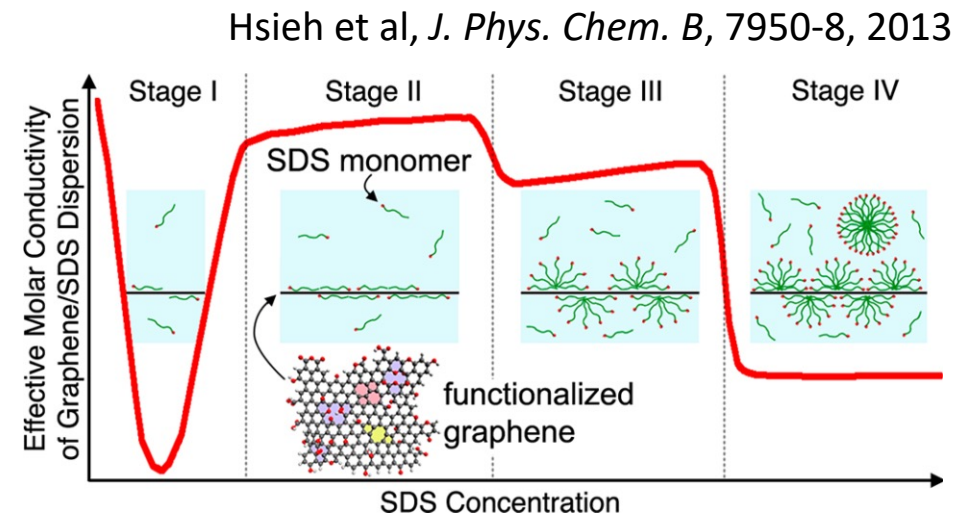
Importance of free surfactant effects



Tear-free
shampoo

Johnsonsbaby.com, Cetaphil.com, loreal.com

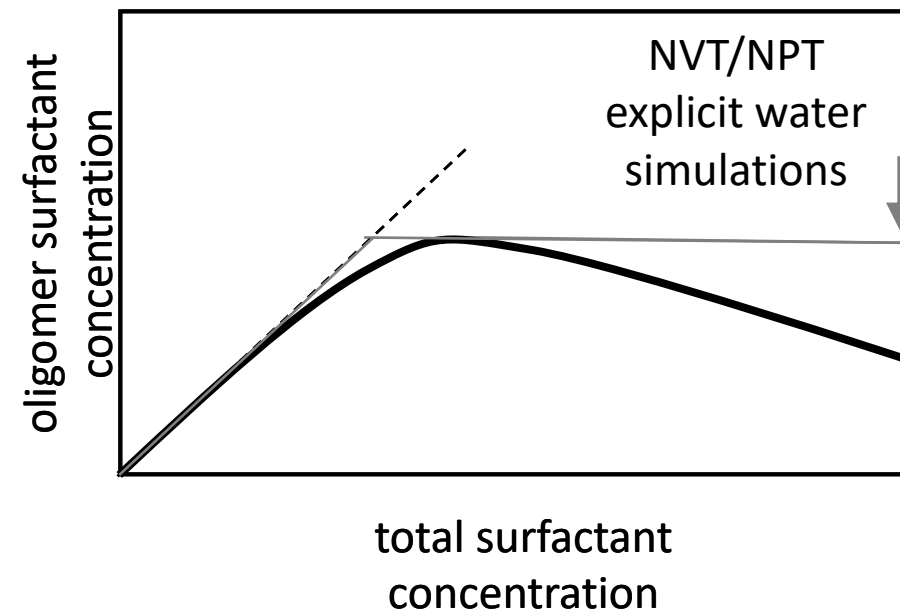
Nanoparticle
dispersion



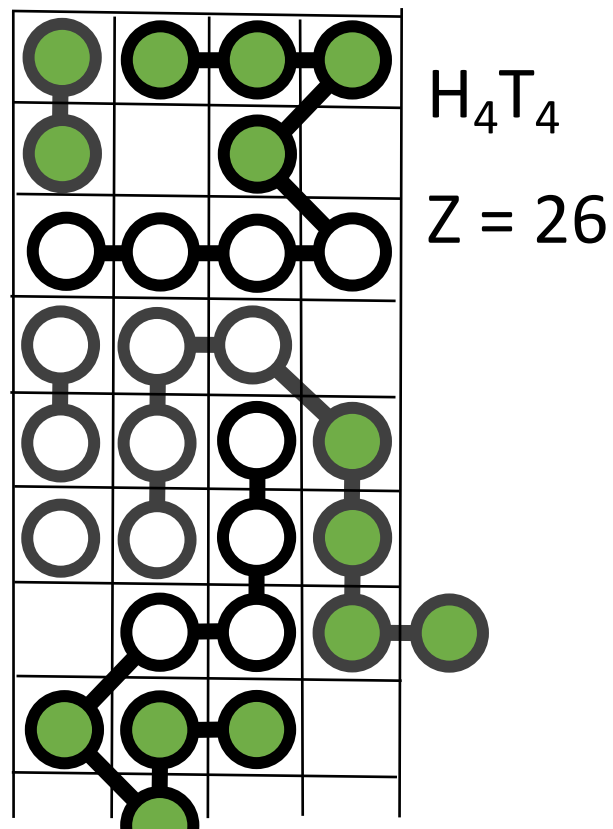
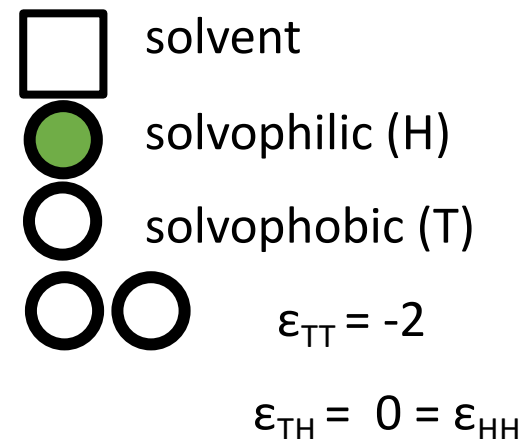
Experimental Measurement

Property	Technique
$\alpha, \Delta G^\circ$	Specific conductivity
$\langle M \rangle$	Nuclear magnetic resonance
$\alpha, \langle M \rangle$	Fluorescence quenching
$\langle M \rangle$	Light Scattering

Critical micelle
Simulation
measurement



Monte Carlo Simulation Methods

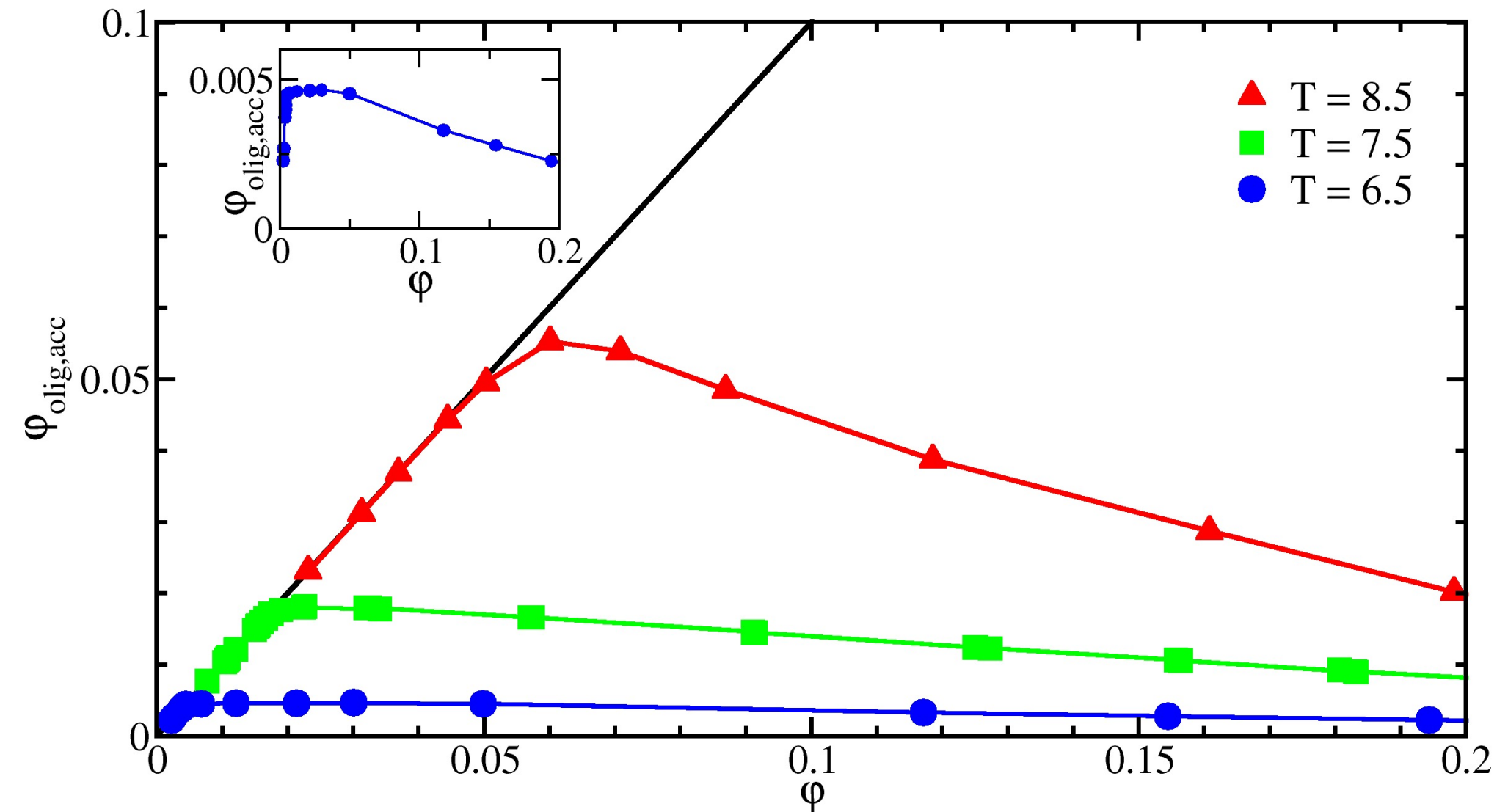


Monte Carlo

- Grand-canonical (μVT) and canonical (NVT) ensembles
- Histogram reweighting

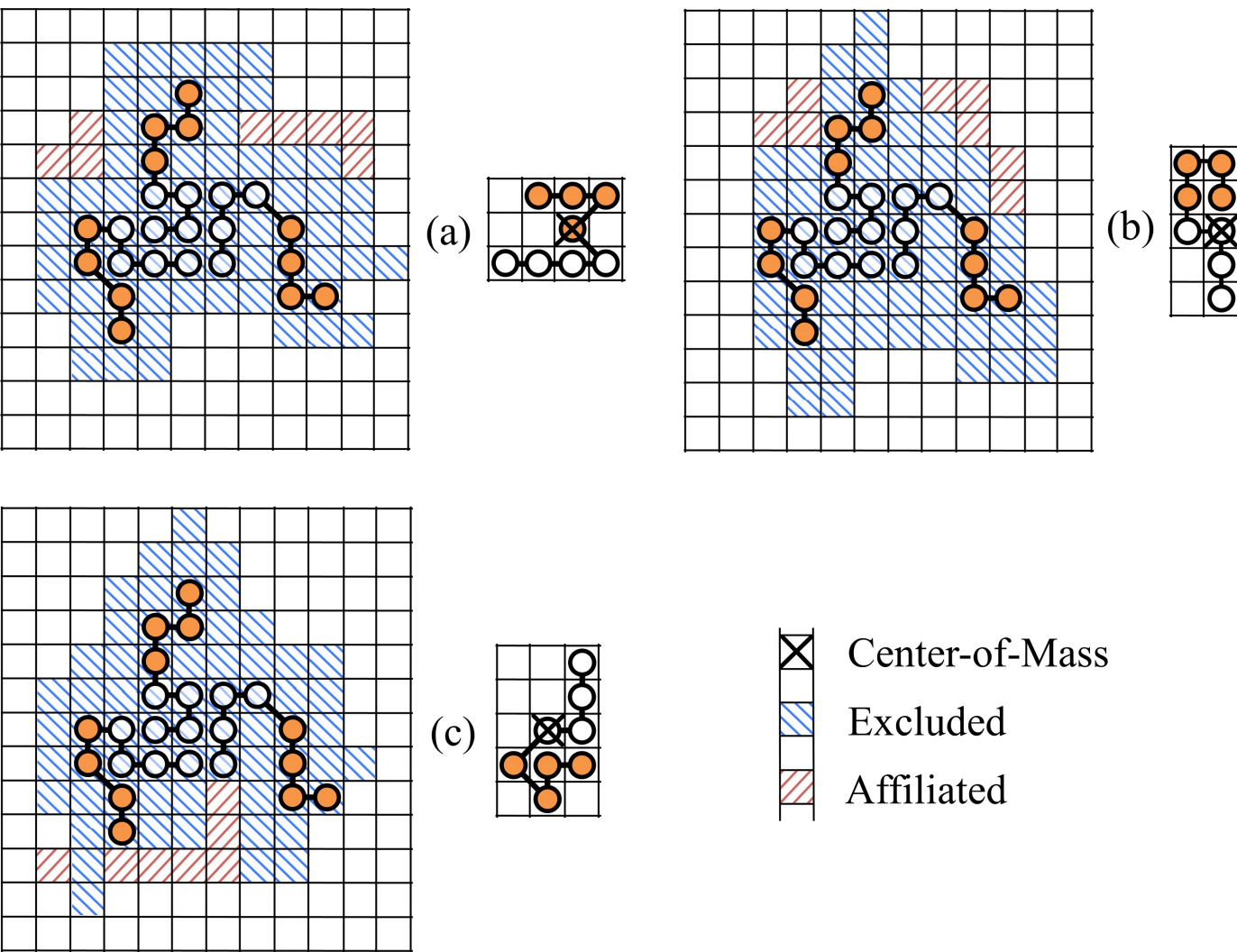
Ensemble \ Move	Reptations	Insertion/deletions	Cluster moves
NVT	99.5%	0%	0.5%
μVT	39.5%	60%	0.5%

Free surfactant concentration

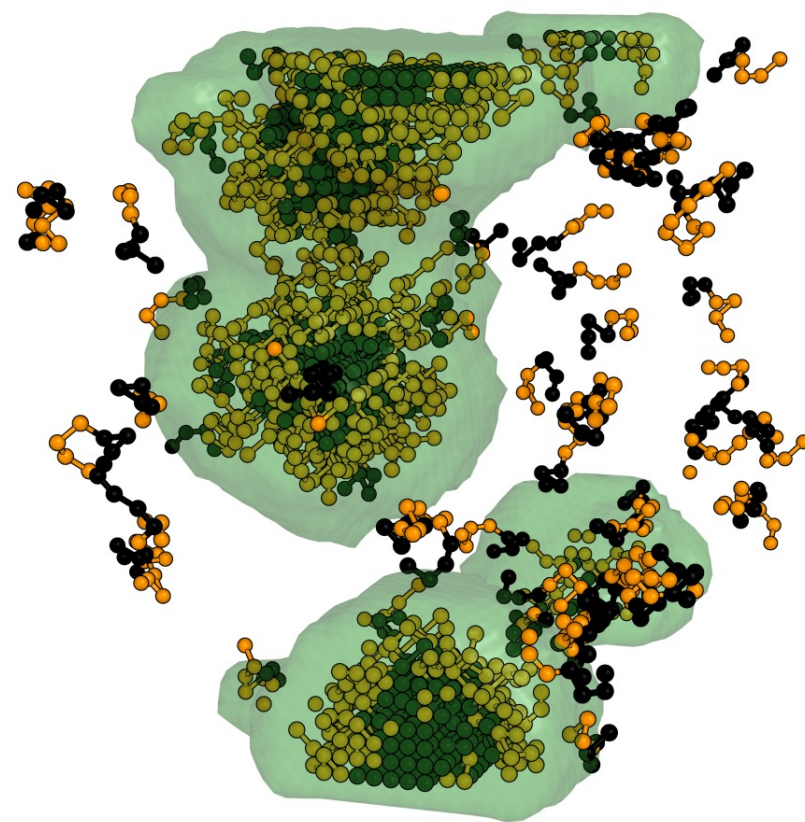


Free volume

Free volume calculation method

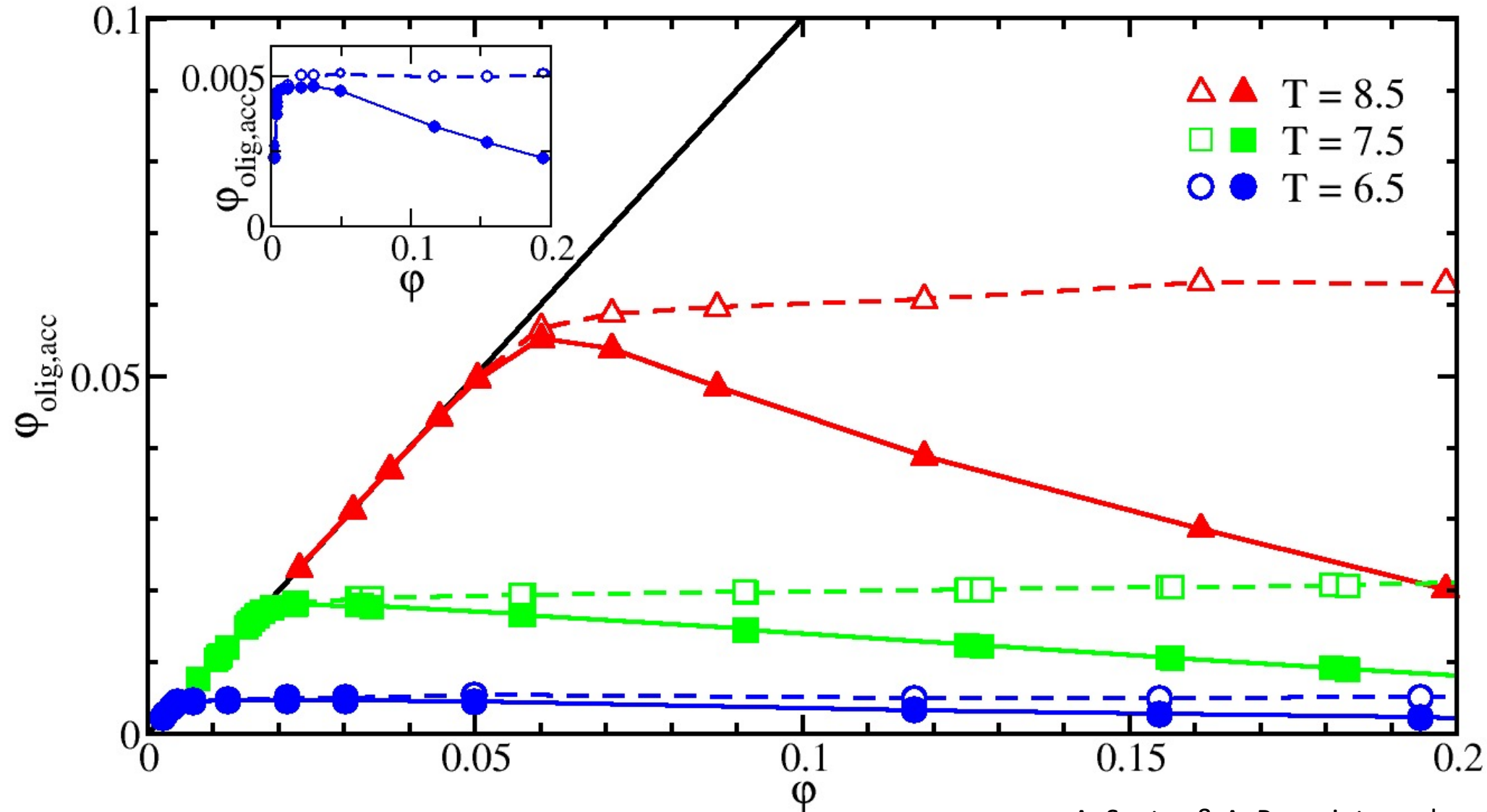


Free volume of a typical micellar system



Correcting the nonionic free surfactant volume fraction

15

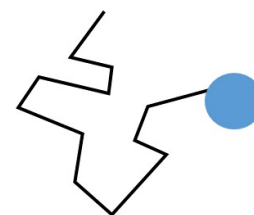
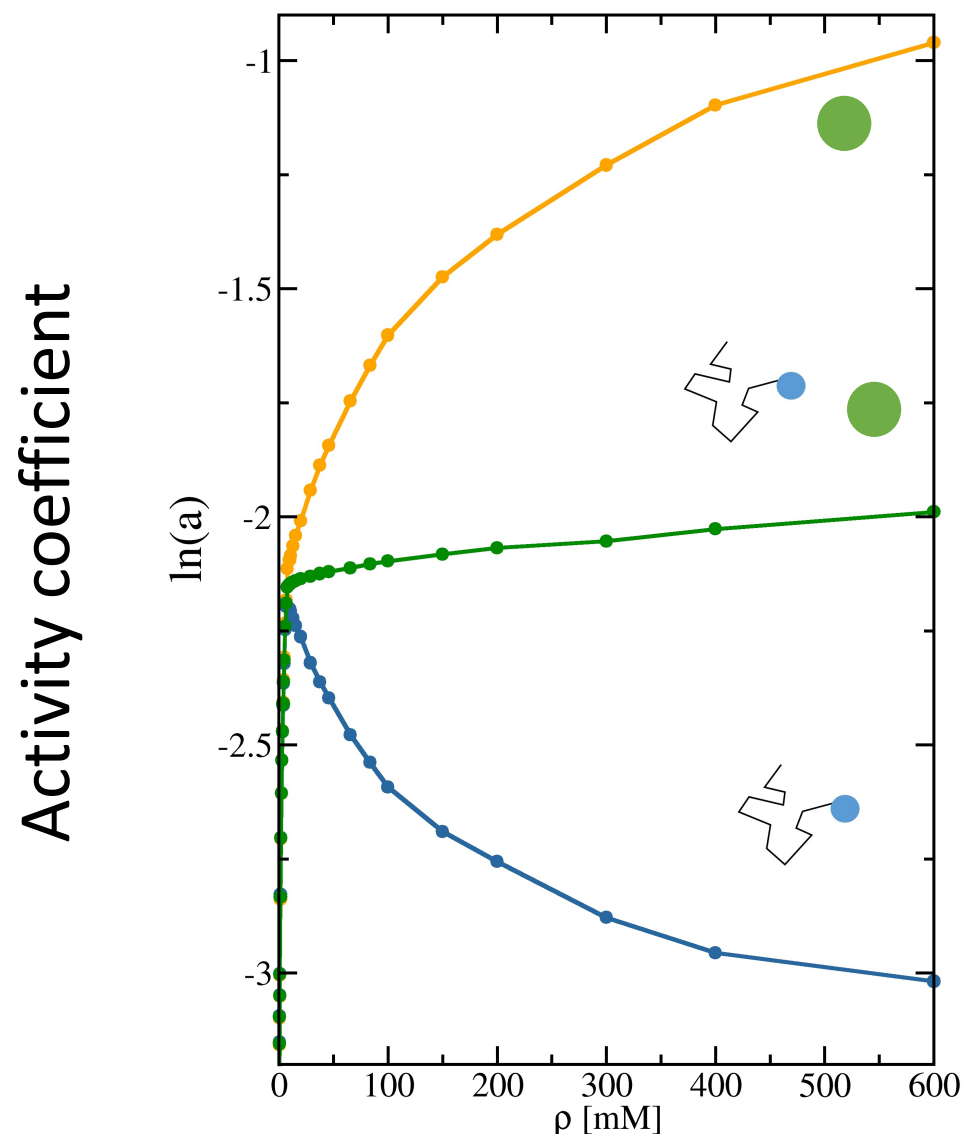


Summary – Nonionic surfactants

- The decrease in the free amphiphile oligomer volume fraction is an equilibrium phenomena.
- The inaccessible volume successfully accounts for decrease in the volume fraction.
- Similar results were found for other surfactant architectures:

S. Jiao, A. Santos & A. Panagiotopoulos, *Fluid Phase Equilibria*, 470, 2018

Experimental evidence



Ionic surfactant

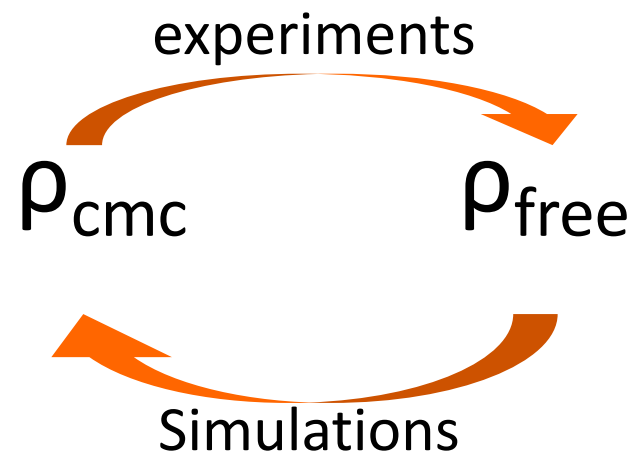


counterion

Phenomena:

- Free volume
- “Salting-in” via the degree-of-association (α)

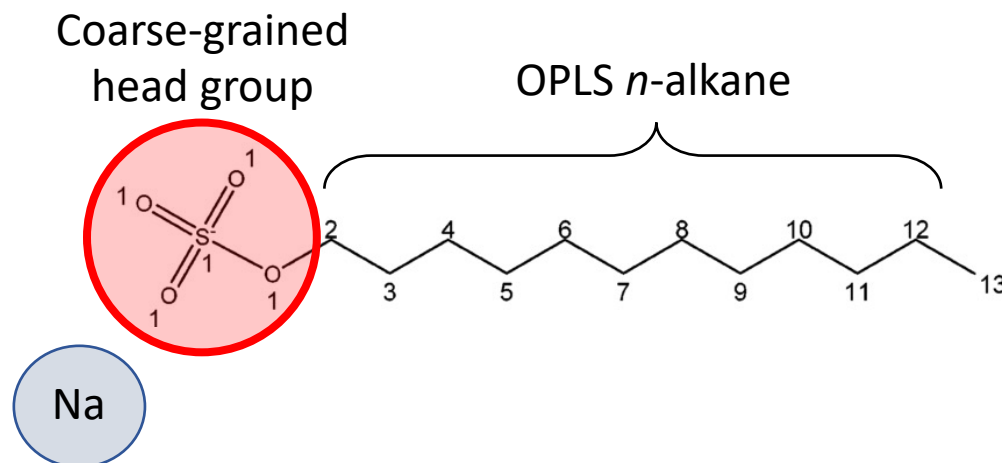
Experimental evidence



$$\rho_{\text{cmc}} = \exp \left[\frac{1}{(1 + \alpha)} \left(\ln \rho_{\text{free}} + \alpha \ln \left(\frac{(1 - \alpha)(\rho - \rho_{\text{free}}) + \rho_{\text{free}}}{V_{\text{accessible}}} \right) \right) \right]$$

- | | |
|---|----------------|
| Bales, <i>J. Phys. Chem. B</i> , 105, 2001 | } experimental |
| Quina <i>et al.</i> , <i>J. Phys. Chem.</i> , 99, 1995 | |
| Gunnarsson <i>et al.</i> , <i>J. Phys. Chem.</i> , 84, 1980 | } theory |
| Jusufi <i>et al.</i> , <i>J. Phys. Chem. B</i> , 116, 2012 | |
| LeBard <i>et al.</i> , <i>Soft Matter</i> , 8, 2012 | } simulations |
| Sanders <i>et al.</i> , <i>J. Phys. Chem. B</i> , 116, 2012 | |

Simulation model



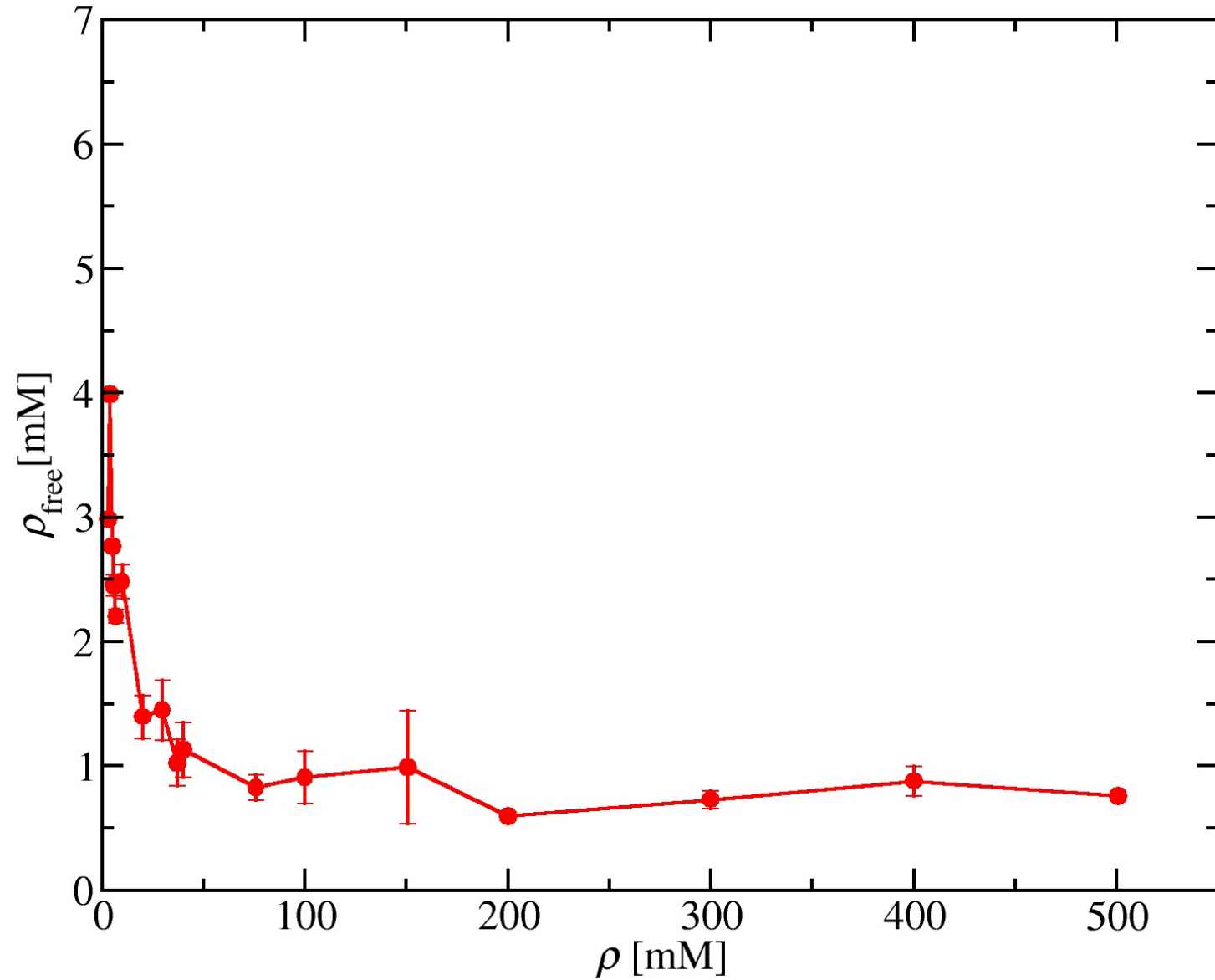
- Sodium Dodecyl Sulfate
- Off-lattice, 3D
 - Implicit-solvent (no water)

NVT MD simulations

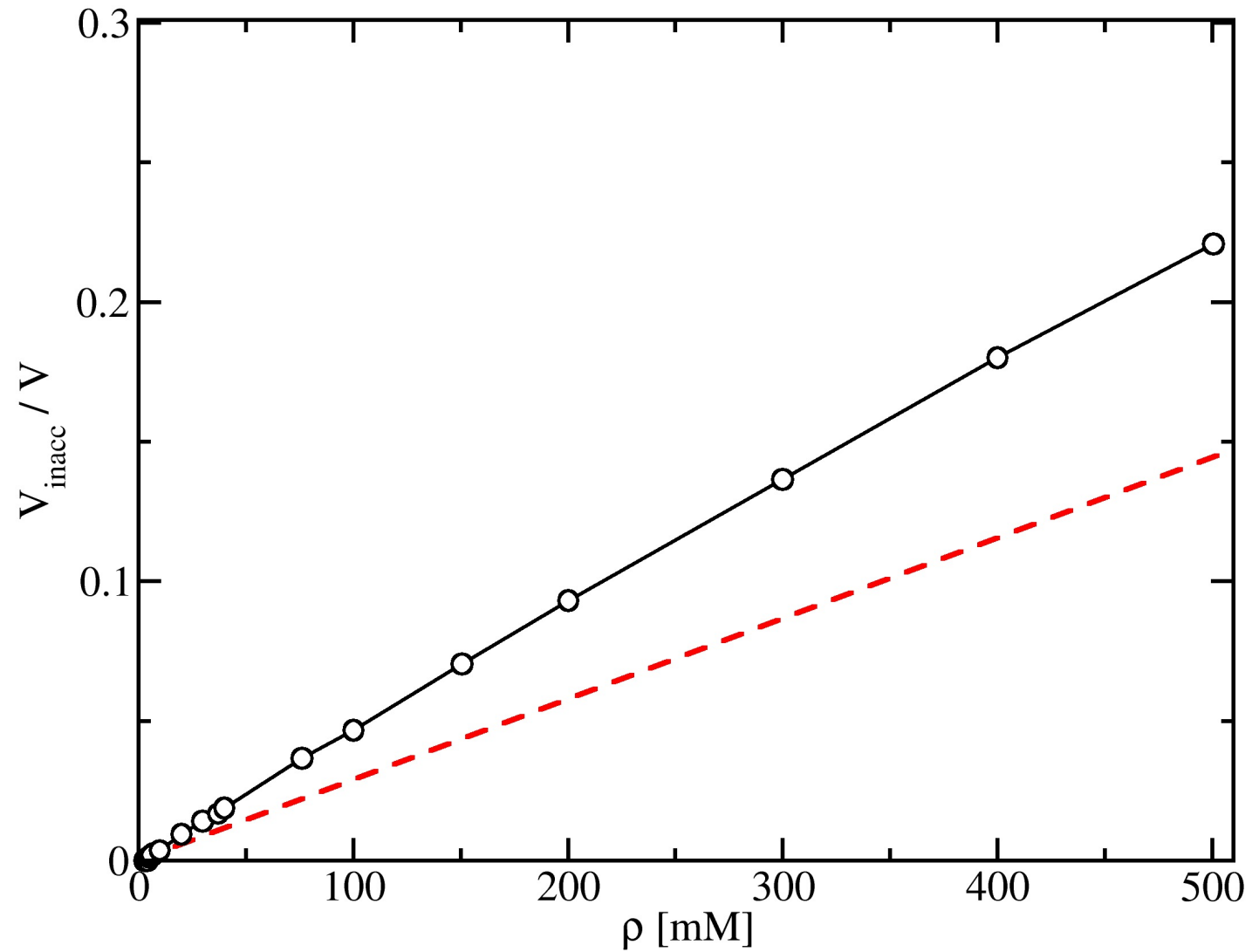
surfactant	cmc [mM]		<i>M</i>	
	sim.	exp.	sim.	exp.
LiDS	9.1	8.7, ^b 8.9 ^c	49	50, ^c 54 ^e
NaDS	9.3	7.7, ^f 8.2, ^b 8.3, ^c 9.3 ^g	57	50, ^h 53, ^e 64 ⁱ
KDS	10	6.7, ^g 7.2 ^c	55	60 ^c
DTAB	16.4	14.6, ⁱ 14.9 ^j	35	49, ⁱ 55 ^j
DTAC	22.2	17.2, ^k 20.3, ^j 21.3 ^l	31	45 ^j

A. Jusufi, A. Hynninen and A. Z. Panagiotopoulos,
J. Phys. Chem. B, 112, 2008

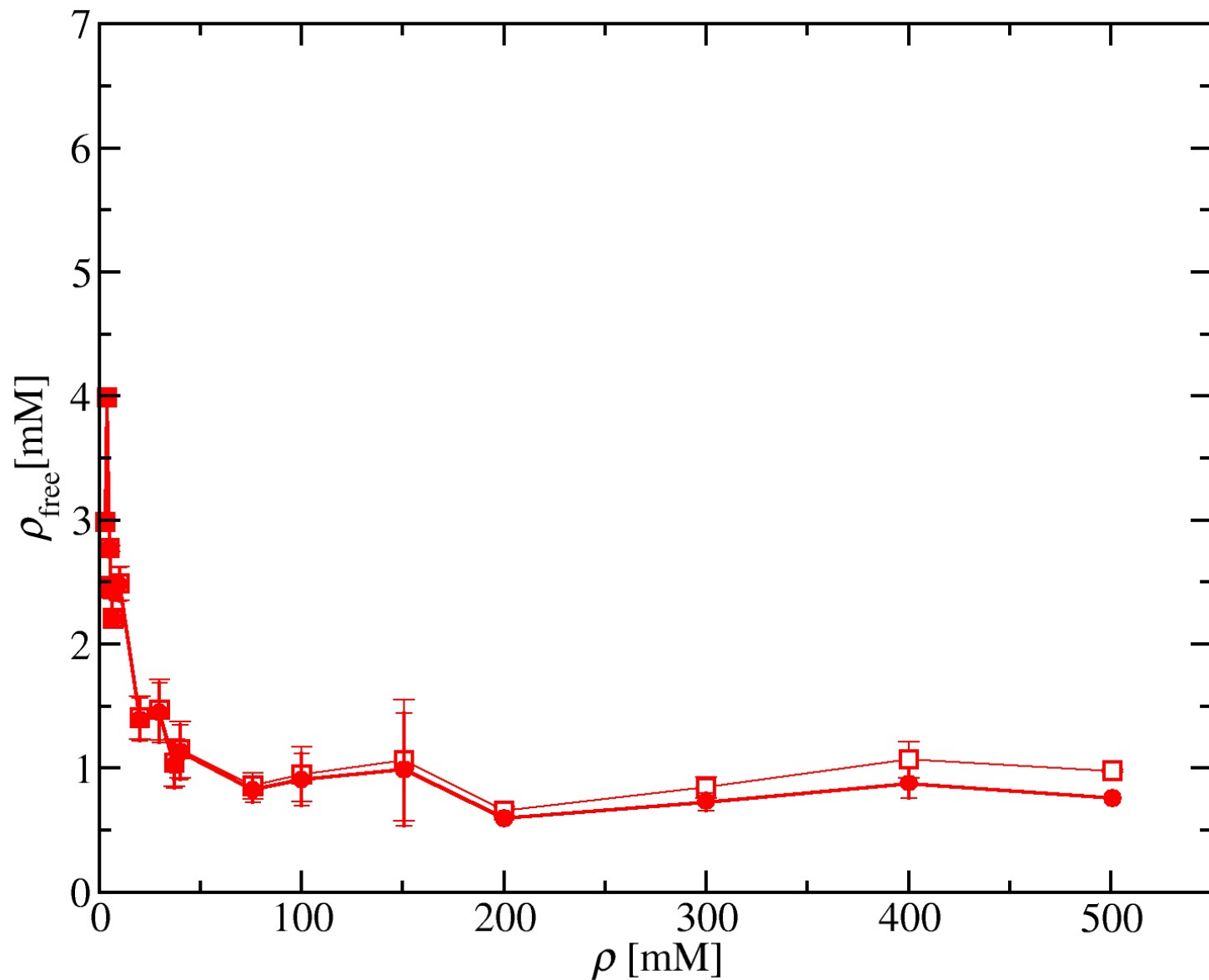
Free surfactant concentration



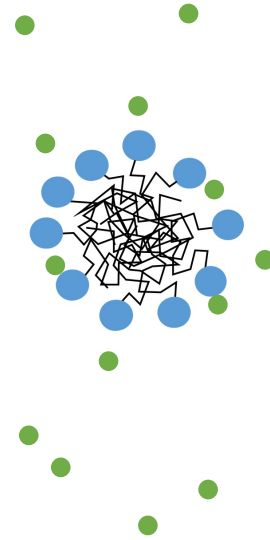
Excluded volume



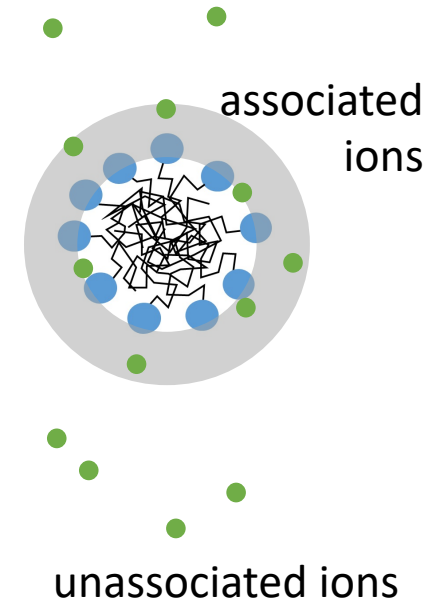
Excluded volume correction



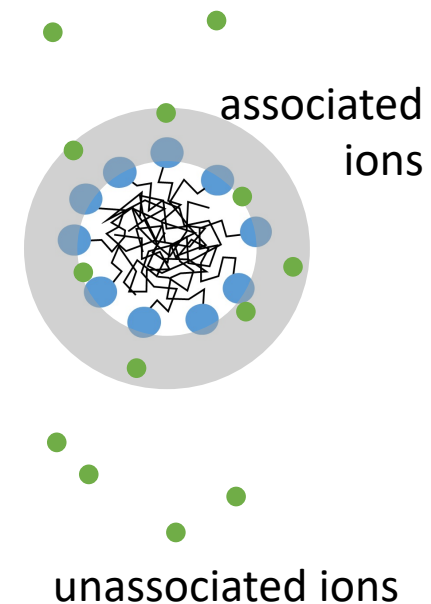
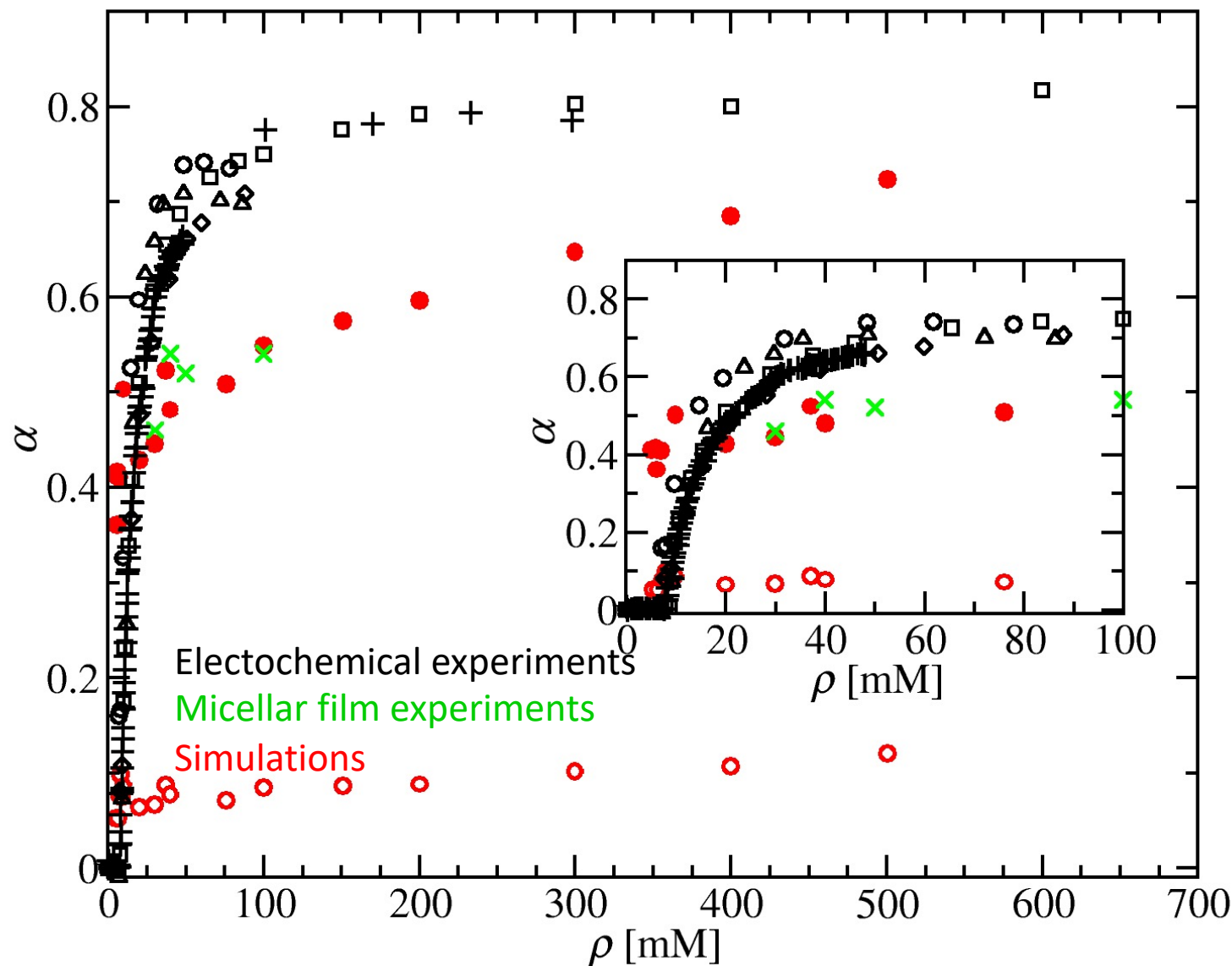
Degree of counterion association



Degree of counterion association

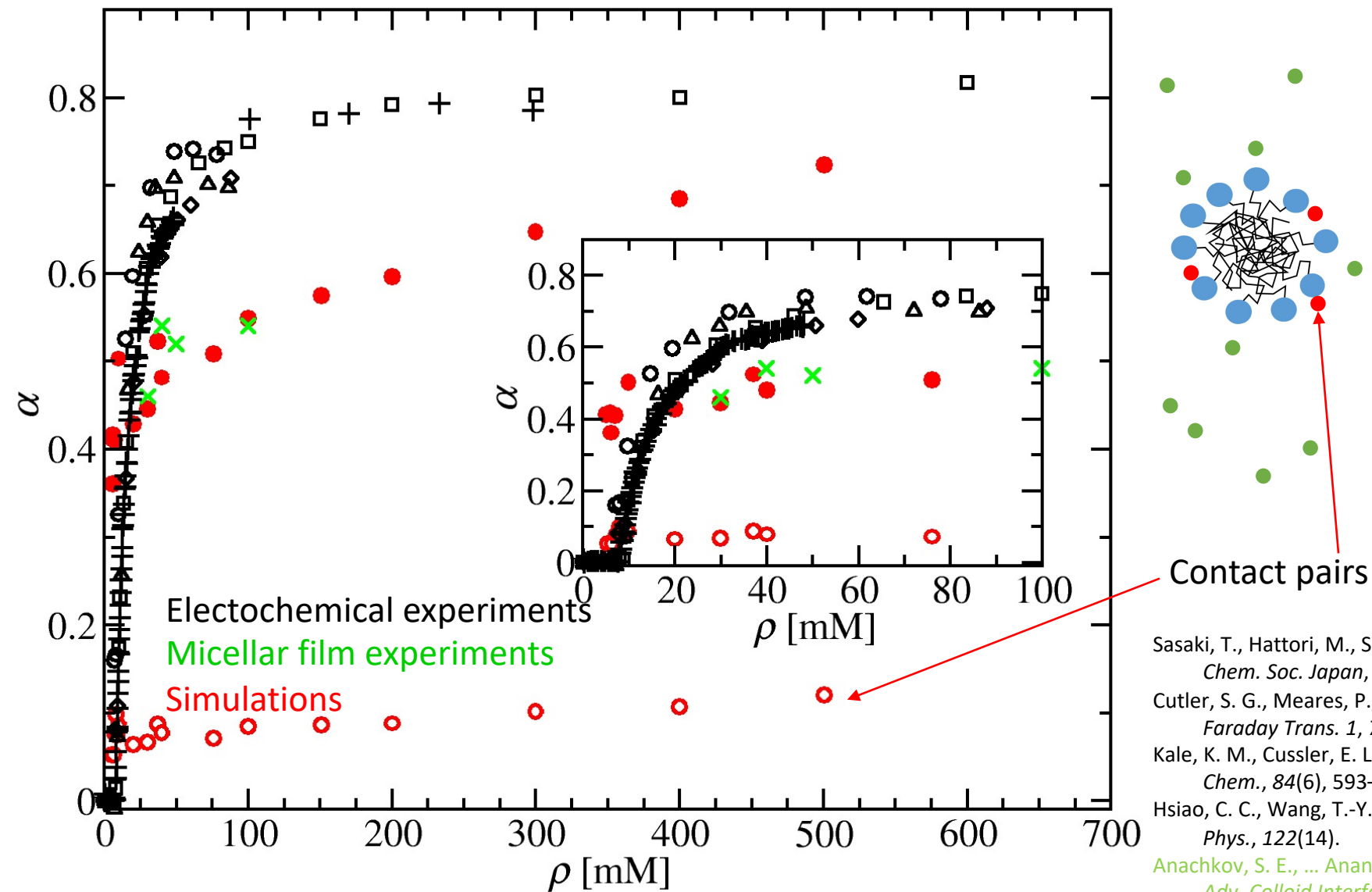


Degree of counterion association



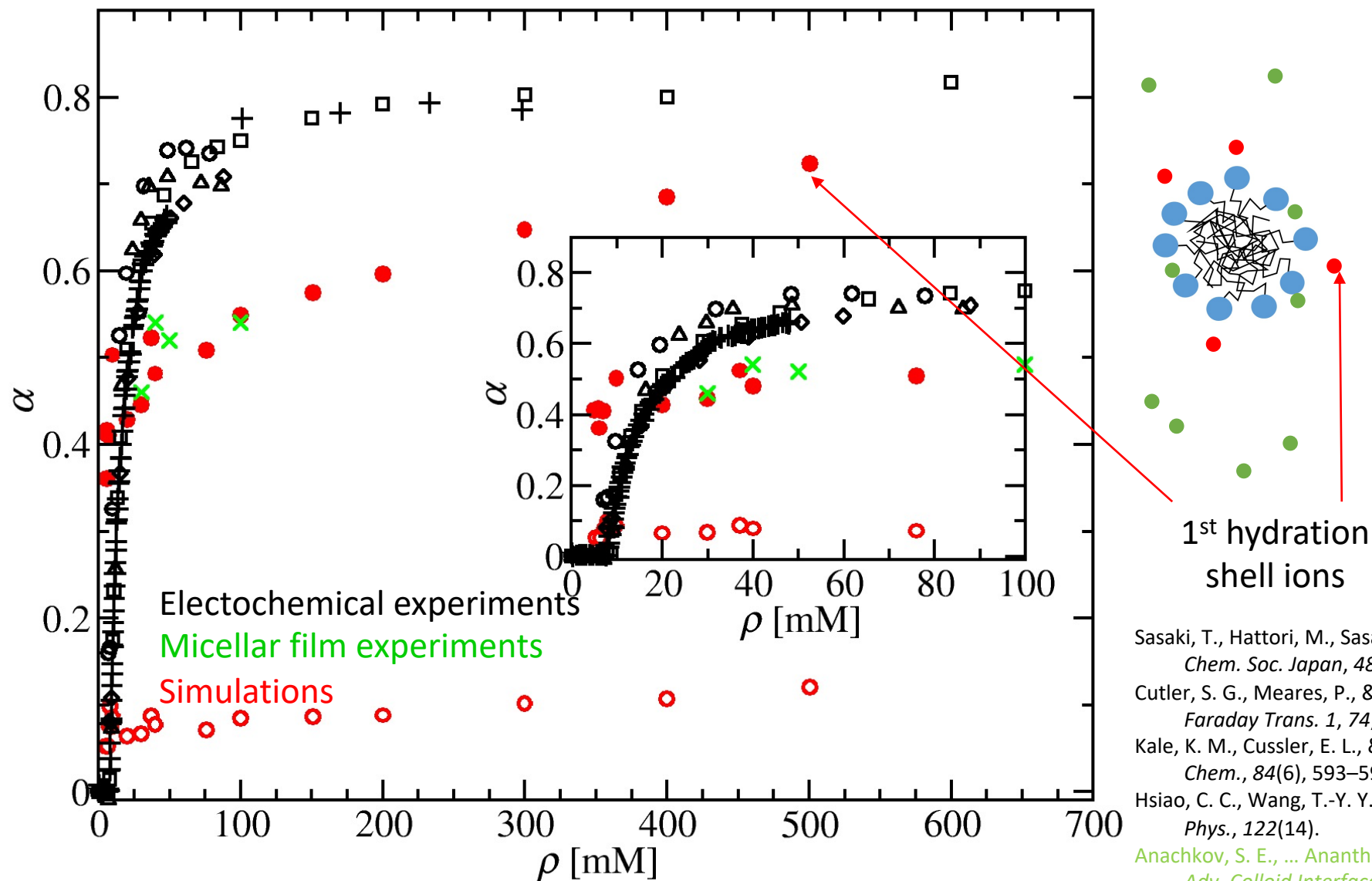
- Sasaki, T., Hattori, M., Sasaki, J., & Nukina, K. (1975). *Bull. Chem. Soc. Japan*, 48(5), 1397–1403.
- Cutler, S. G., Meares, P., & Hall, D. G. (1978). *J. Chem. Soc., Faraday Trans. 1*, 74, 1758–1767.
- Kale, K. M., Cussler, E. L., & Evans, D. F. (1980). *J. Phys. Chem.*, 84(6), 593–598.
- Hsiao, C. C., Wang, T.-Y. Y., & Tsao, H.-K. K. (2005). *J. Chem. Phys.*, 122(14).
- Anachkov, S. E., ... Ananthapadmanabhan, K. P. (2012). *Adv. Colloid Interface Sci.*, 183–184, 55–67.

Degree of counterion association



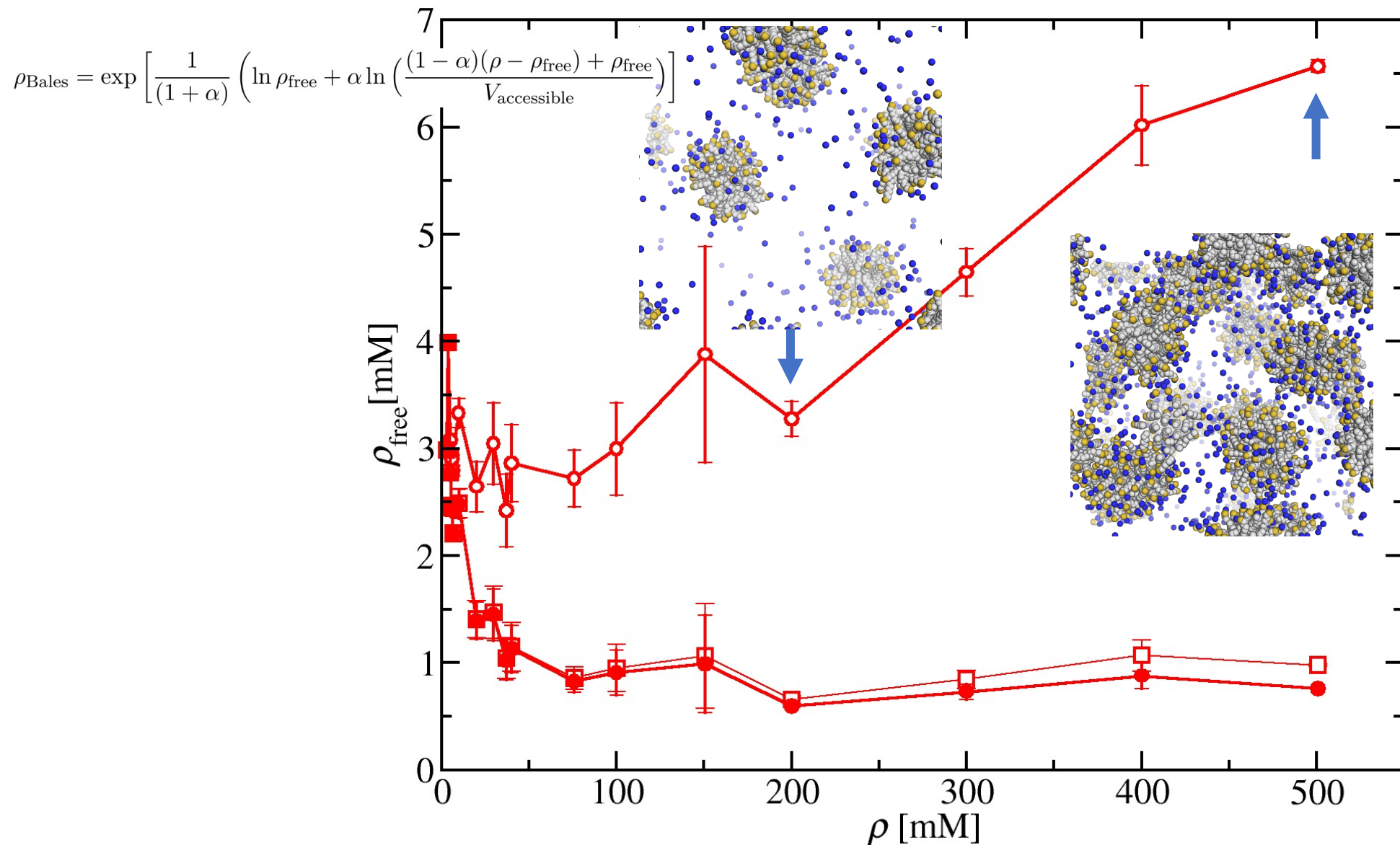
- Sasaki, T., Hattori, M., Sasaki, J., & Nukina, K. (1975). *Bull. Chem. Soc. Japan*, 48(5), 1397–1403.
- Cutler, S. G., Meares, P., & Hall, D. G. (1978). *J. Chem. Soc., Faraday Trans. 1*, 74, 1758–1767.
- Kale, K. M., Cussler, E. L., & Evans, D. F. (1980). *J. Phys. Chem.*, 84(6), 593–598.
- Hsiao, C. C., Wang, T.-Y. Y., & Tsao, H.-K. K. (2005). *J. Chem. Phys.*, 122(14).
- Anachkov, S. E., ... Ananthapadmanabhan, K. P. (2012). *Adv. Colloid Interface Sci.*, 183–184, 55–67.

Degree of counterion association



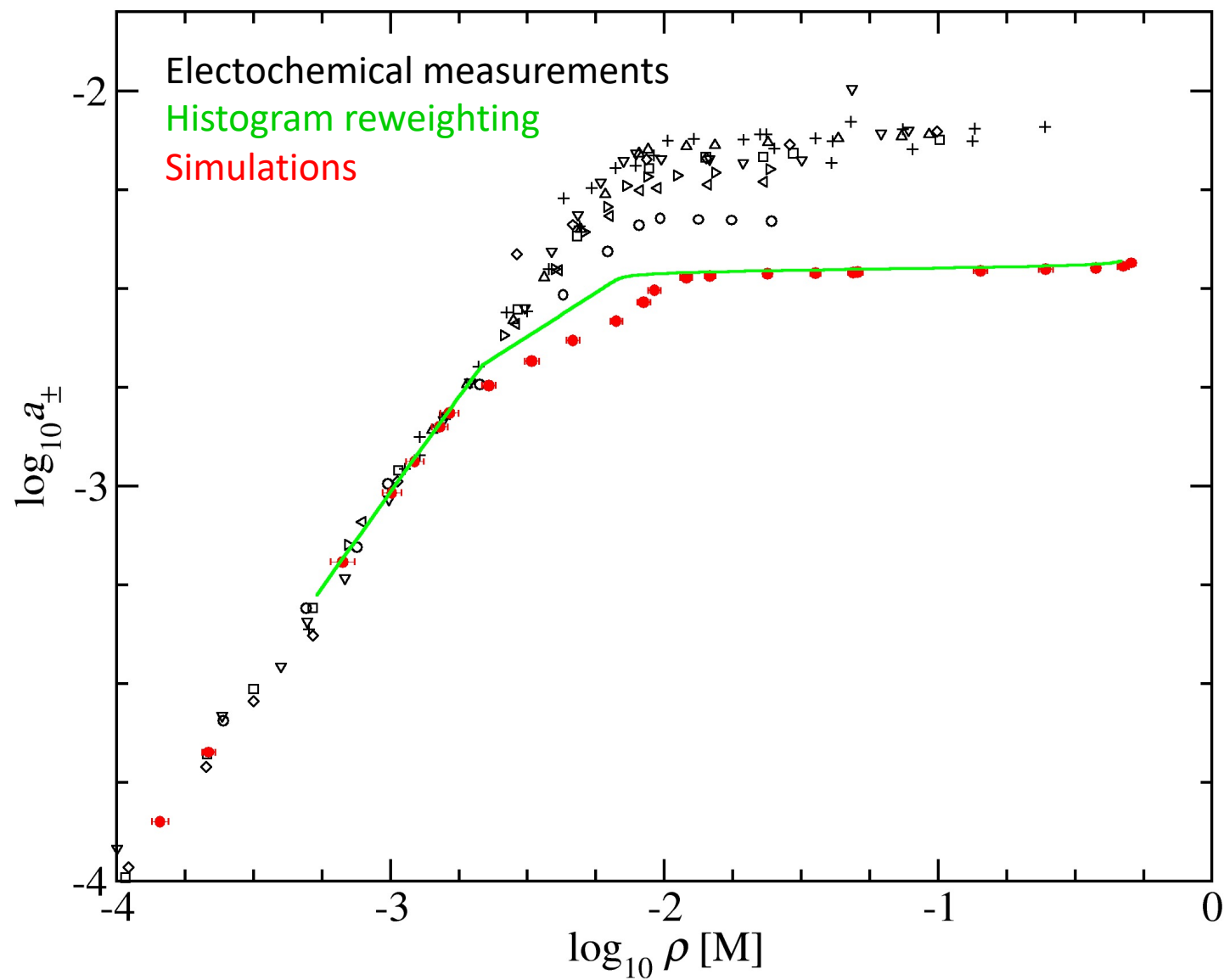
- Sasaki, T., Hattori, M., Sasaki, J., & Nukina, K. (1975). *Bull. Chem. Soc. Japan*, 48(5), 1397–1403.
- Cutler, S. G., Meares, P., & Hall, D. G. (1978). *J. Chem. Soc., Faraday Trans. 1*, 74, 1758–1767.
- Kale, K. M., Cussler, E. L., & Evans, D. F. (1980). *J. Phys. Chem.*, 84(6), 593–598.
- Hsiao, C. C., Wang, T.-Y. Y., & Tsao, H.-K. K. (2005). *J. Chem. Phys.*, 122(14).
- Anachkov, S. E., ... Ananthapadmanabhan, K. P. (2012). *Adv. Colloid Interface Sci.*, 183–184, 55–67.

Full correction

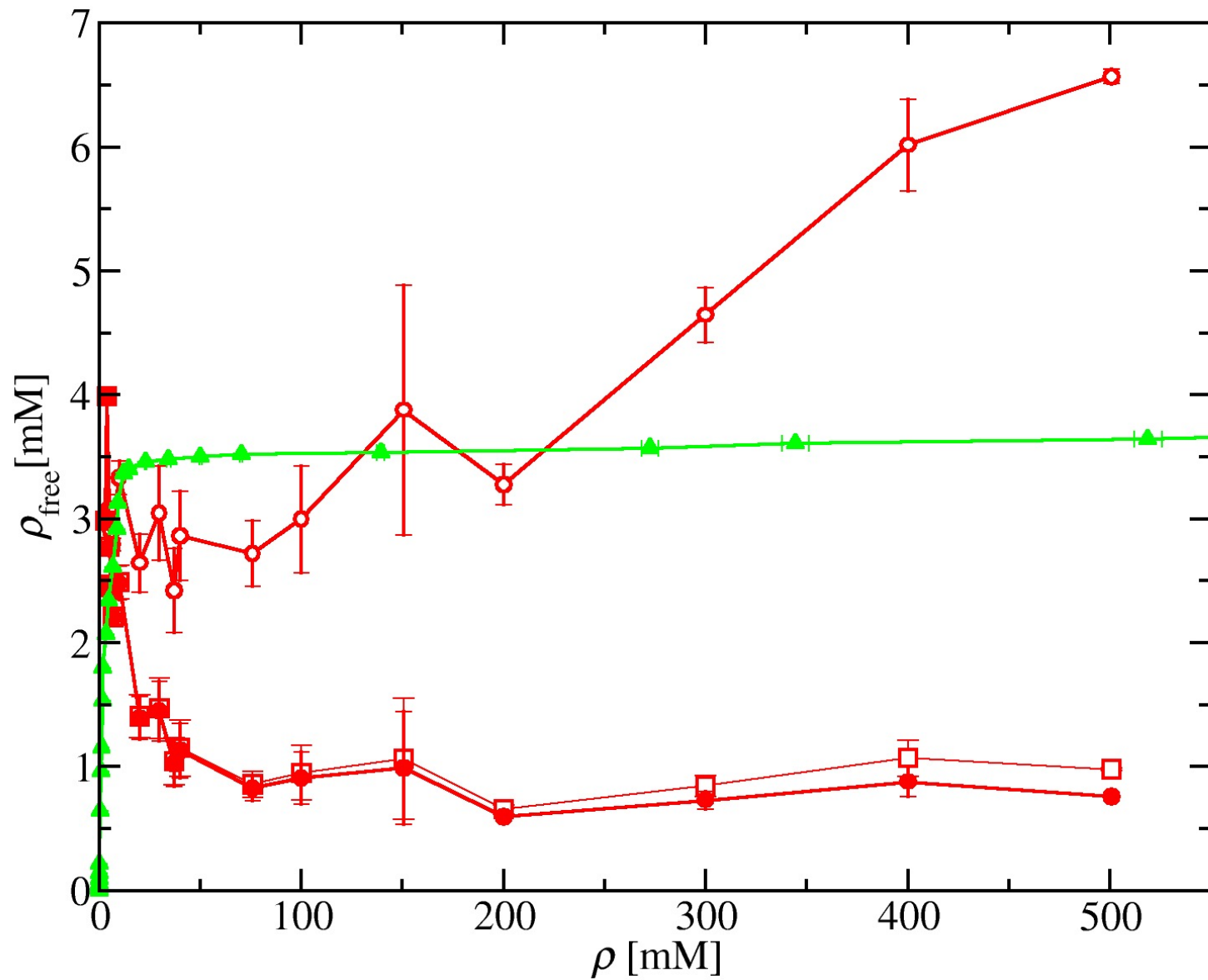


Second critical
micelle
concentration

Surfactant activity



CMC measured by activity



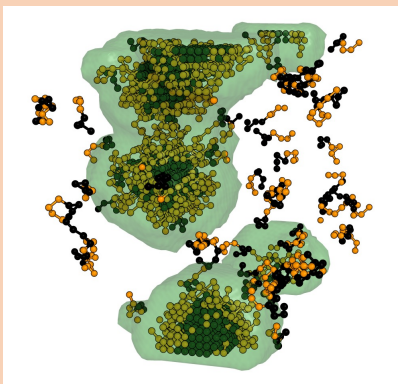
Summary – Ionic Surfactants

- The **inaccessible volume** and **counter-ion condensation** leads to the decrease of the free surfactant concentration for **ionic surfactants**
- The **mean ionic activity** predicts the cmc and the behavior is captured by the model
- The CMC extrapolation is effective at concentrations below higher-order micellar effects

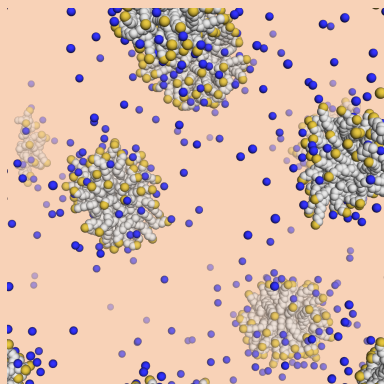
Materials

Surfactants

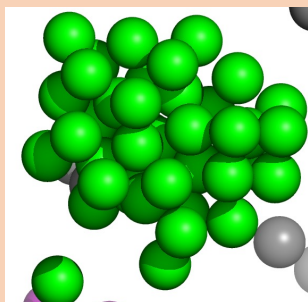
nonionic



ionic

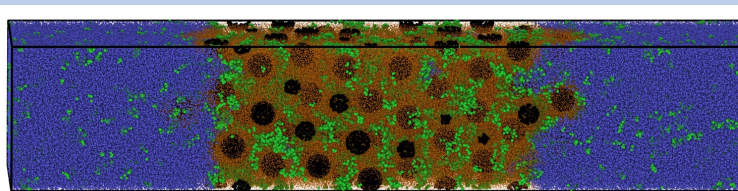


Colloids

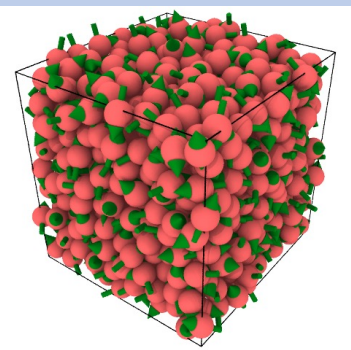


Nanocomposites

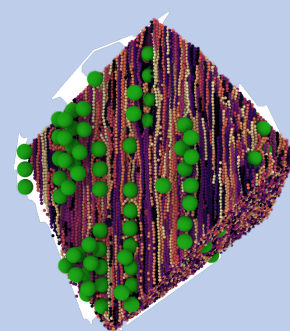
Grafted-NP



Magnetic

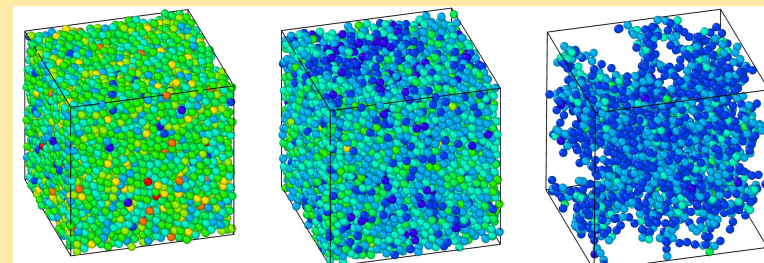


Bare NPs

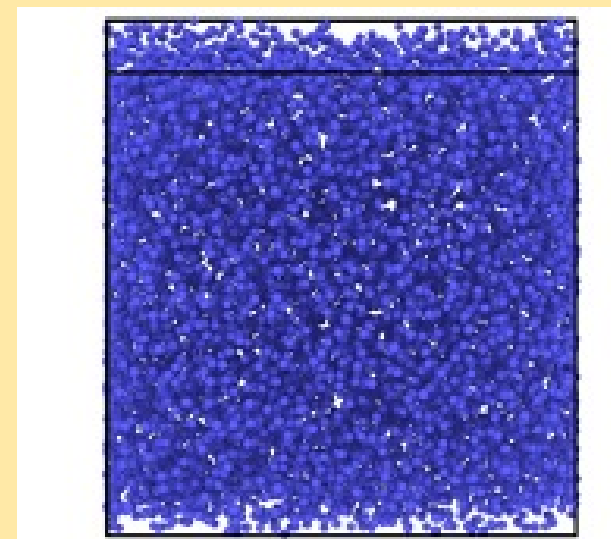


Granular

Packings



Flow



Actualizing Nanocomposites

Application

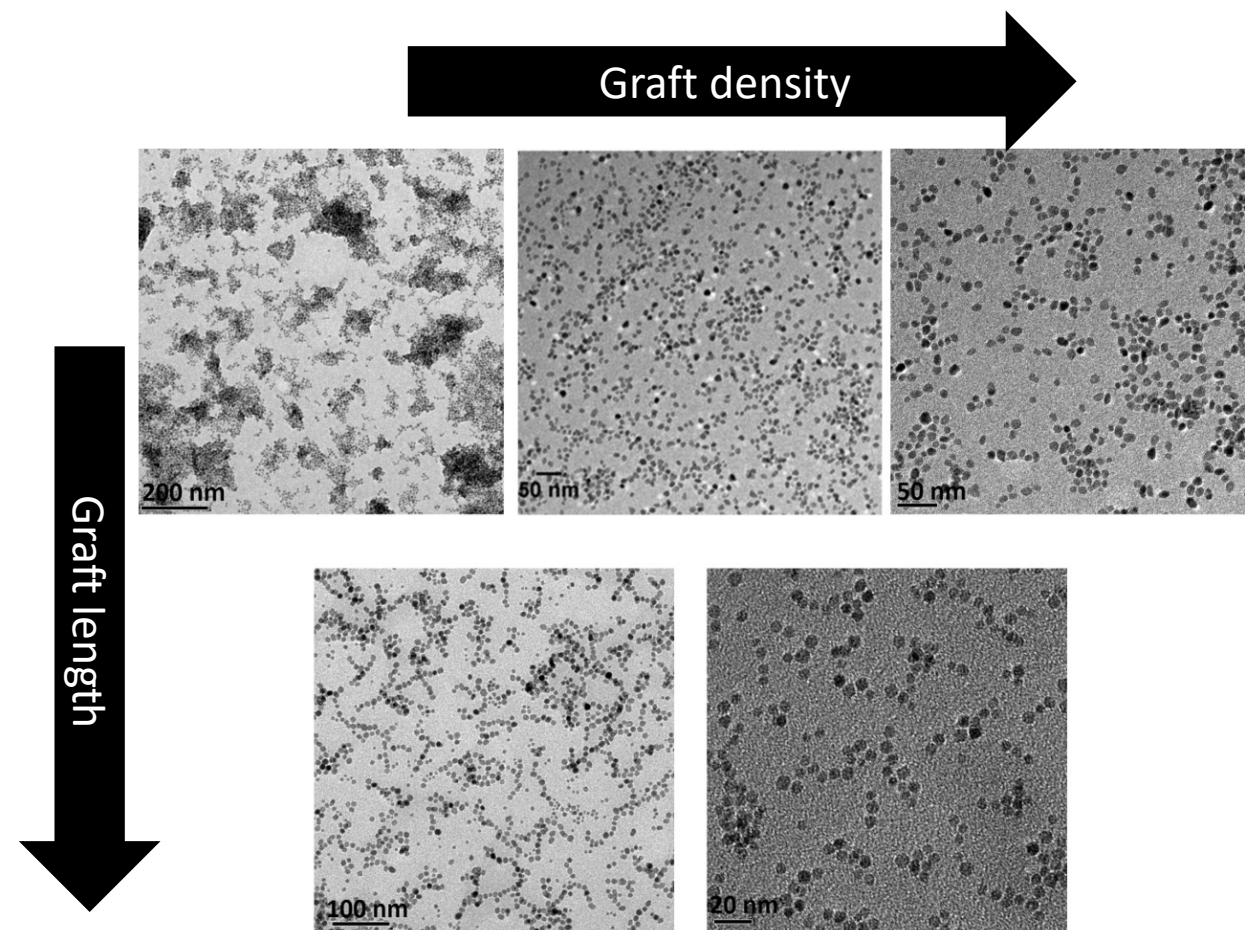
- Sensors (nanoantennae)
- Stronger materials (filled rubbers)
- Filtration (membranes)

Goal

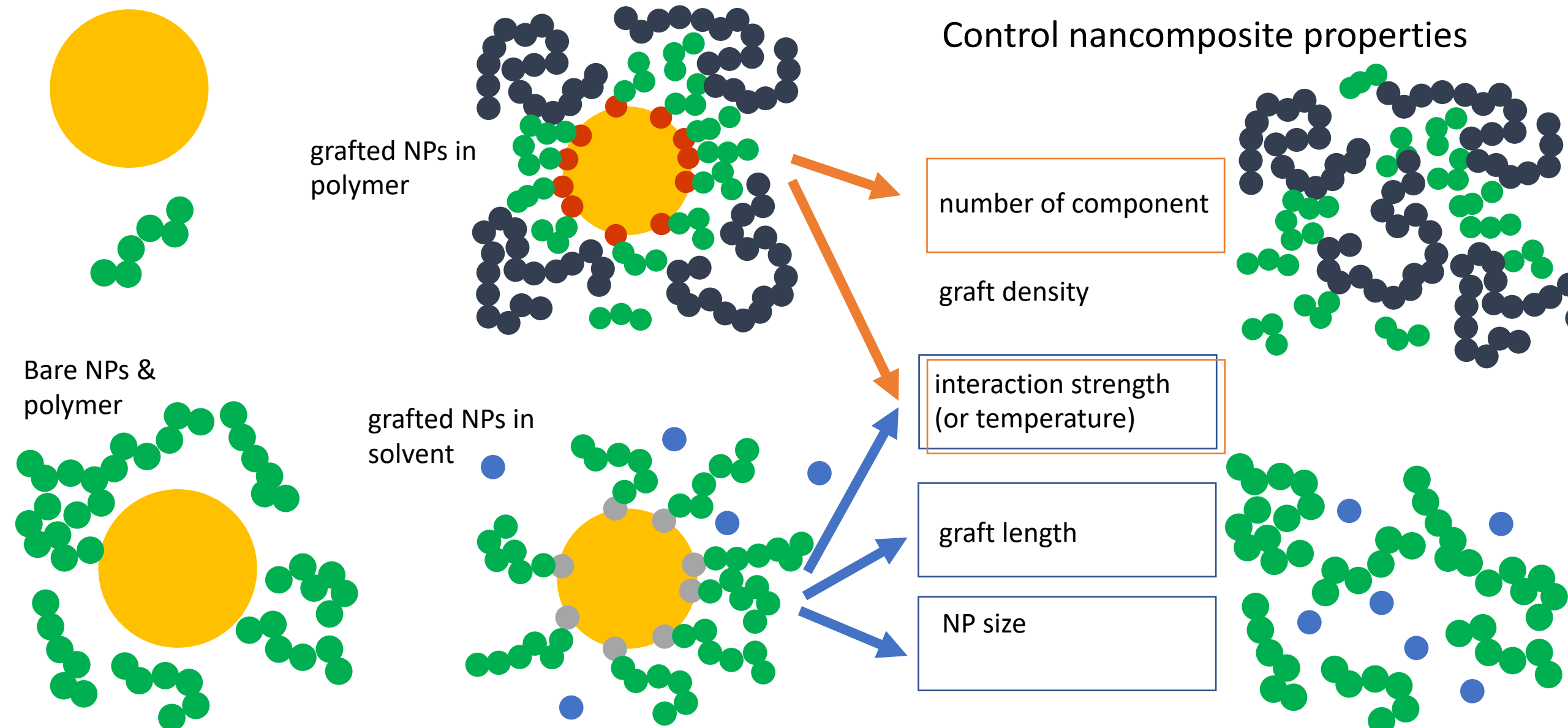
- Combine the properties from each component (nanoparticles NPs and polymer):
 - Photonic
 - Mechanical
 - Electrical
 - Magnetic

Challenges

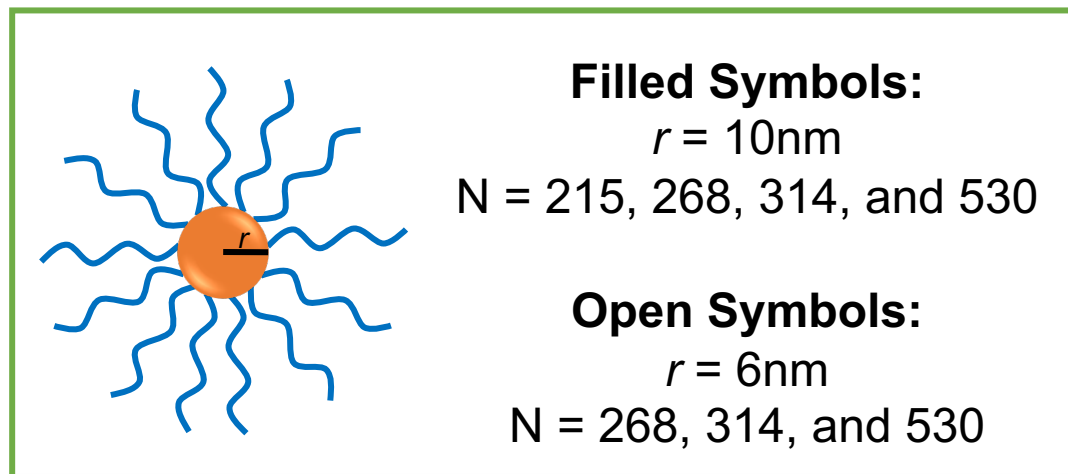
- Design can control final nanoparticle morphology.
- Morphology dominates properties and applicability.
- Limited molecular solvent-polymer-grafted nanoparticle phase coexistence data



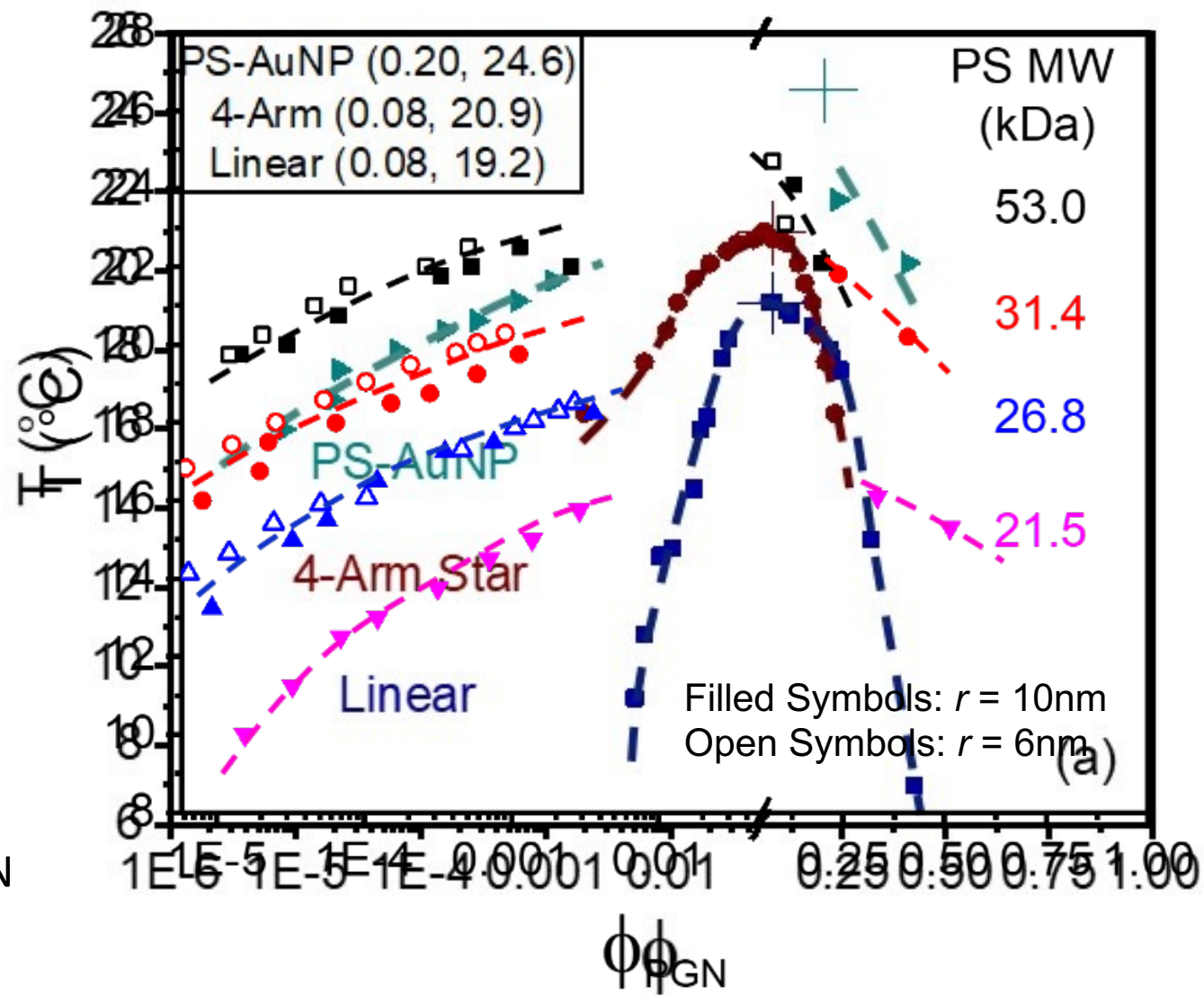
Nanocomposite systems overview



Experimental solvent system (PS-g-Au in cyclohexane)



- UV-vis spectroscopy
- SAXS
- Polymer grafted-NPs (PGNs) differ from stars
- Higher PGN miscibility is observed for lower N
- Similar miscibility at different core sizes



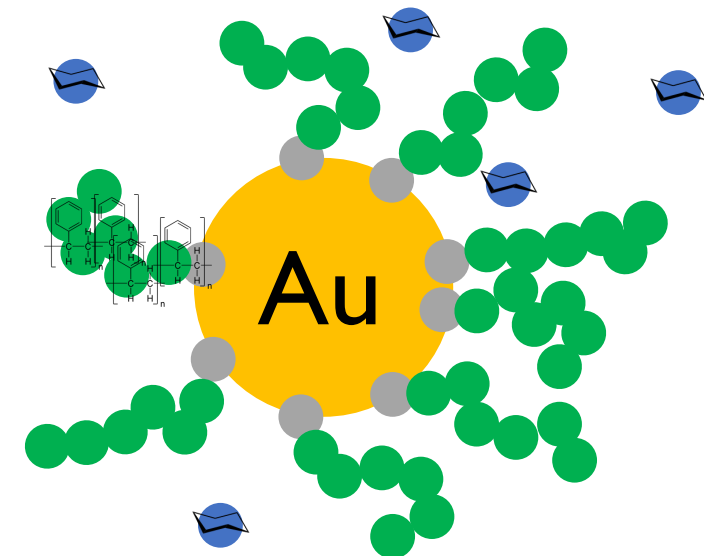
Coarse-graining solvent system

Experimental to Simulation system

1. Pick graft length (N_G) for convenience
2. By matching reduced grafting density (σ^*) get density (ρ_0), length (b) and nanoparticle radius (R_{NP})

System property	Experimental	TILD simulations
NP radius	10, 6 nm	7.47, 4.48 b
Graft mol. weight	21.5 kDa	51 beads
	26.8 kDa	63 beads
	31.4 kDa	74 beads
	53 kDa	126 beads
Grafting density	1.01-0.59 chains/nm ²	0.18 chains/b ² (266-2462 chains/NP)

match
grafting
density



Polystyrene-grafted gold nanoparticles in cyclohexane



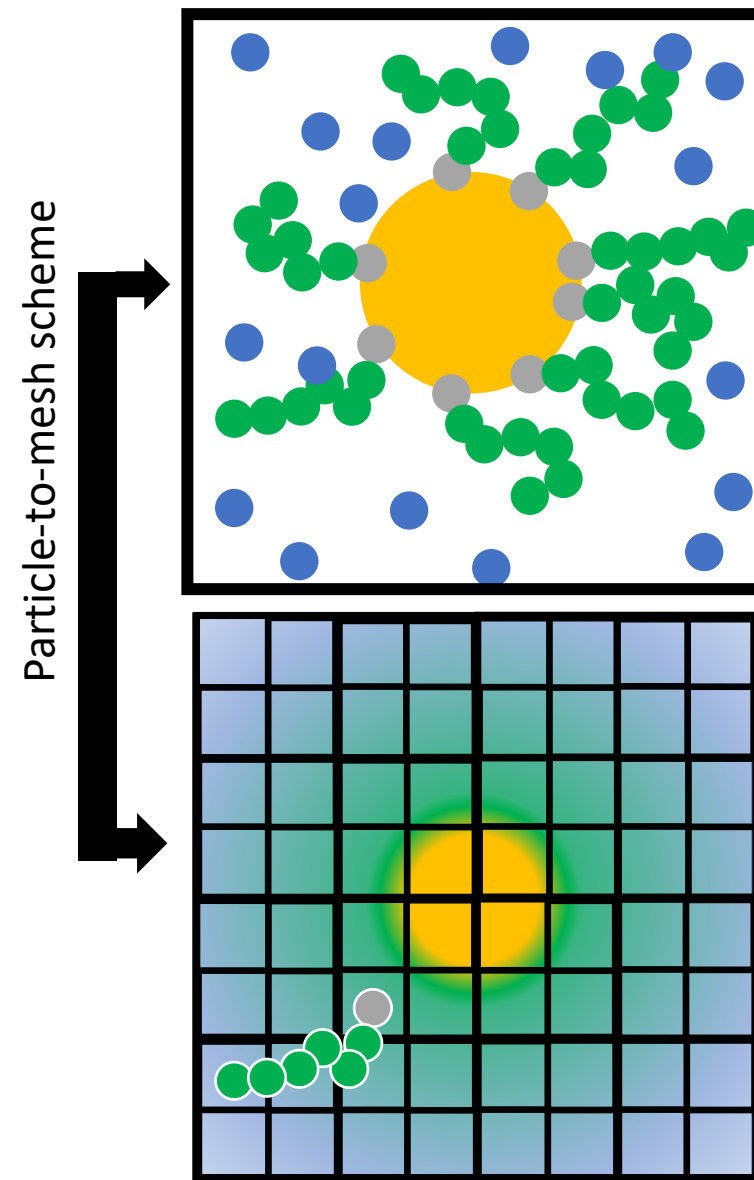
Theoretically-informed Langevin Dynamics (TILD)

Method	TILD	Self-consistent mean field (SCMF)	Coarse-grained MD
Easy access to free energy			
Accurate dynamics			
Thermal fluctuations			
Accurate solvent modeling			
Field theory comparison			
Long polymers and multiple NPs			

Procedure

- Molecular Dynamics evolves simulation of soft, point-based particles using 2nd Law, in the *NVT* ensemble
- *T* is controlled with Langevin thermostat
- Force on each particle is calculated by field-based interaction

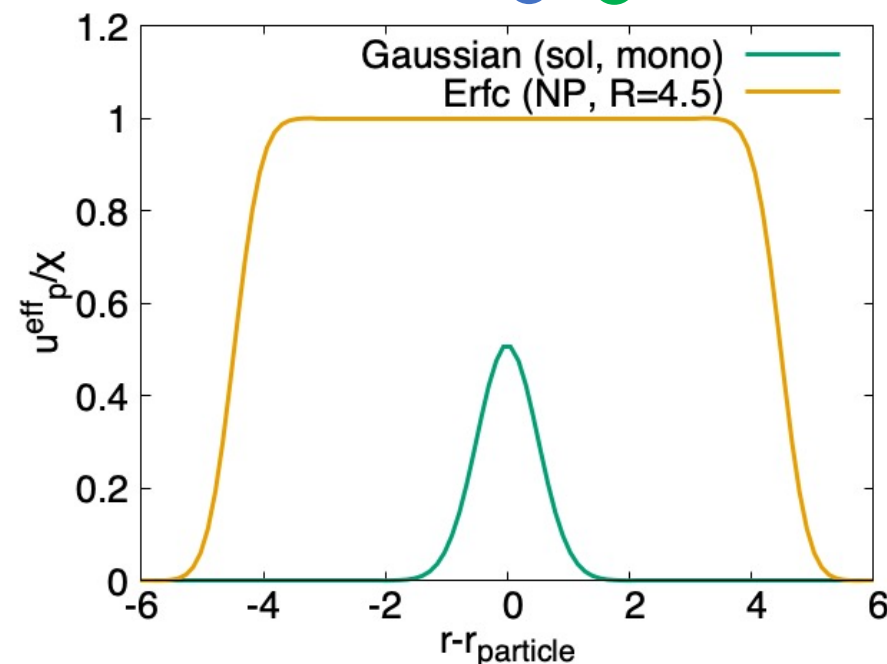
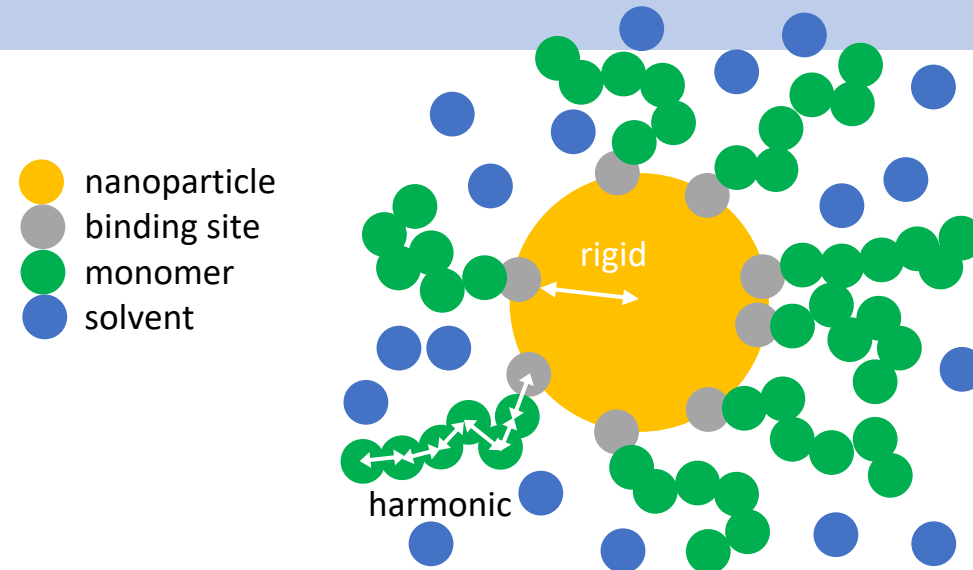
Chao, H., Koski, J., & Riggleman, R. A. (2017). *Soft Matter*, 13(1), 239–249.
 Martin, T. B., & Jayaraman, A. (2016). *Macromolecules*, 49(24), 9684–9692.
 Koh, C., Grest, G. S., & Kumar, S. K. (2020). *ACS Nano*, 14(10), 13491–13499.



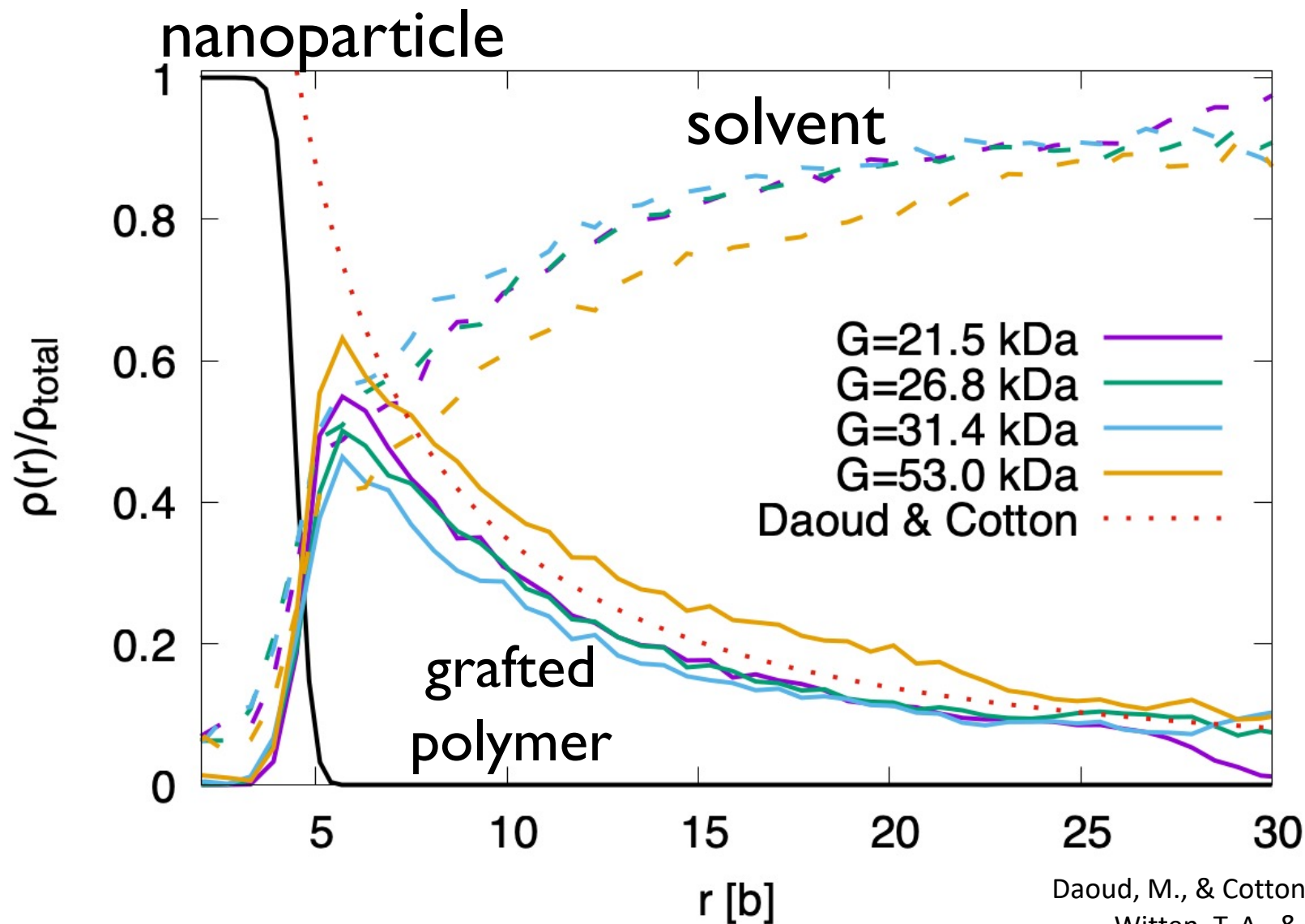
Theoretically-informed Langevin Dynamics (TILD)

Parameters

- Nonbonded interaction parameters
 - Interaction parameter: $\chi_{sol-mono} = \chi$
 - Compressibility: $\kappa = 25$
 - Otherwise nanoparticles are non-interacting
- Harmonic bonds
 - $k_{bond} = 1.5$
- Langevin Gronbech-Jensen/Farago formulation thermostat applied to polymer and solvent
 - $T = 1, T_{damp}^{trans} = T_{damp}^{rot} = 1$
 - $m_{solvent} = m_{monomer} = 1, m_{NP} = \rho_0 / V_{np}$
- PPM
 - mesh density = $1b^3$
 - grid order = 2



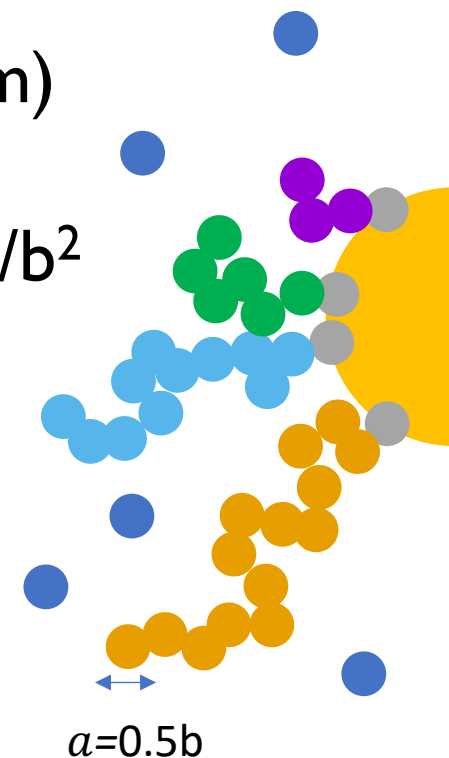
Brush profile



$$R_{\text{NP}} = 4.48b \text{ (6nm)}$$

$$\chi = 0.25$$

$$\sigma = 0.18 \text{ chains}/b^2$$



$$\rho_{\text{Daoud-Cotton}}(r) = \left(\frac{a R_{\text{NP}} \sqrt{\sigma}}{r} \right)^{4/3} a^{-3}$$

Daoud, M., & Cotton, J. P. (1982). *J. Phys. France*, 43(3), 531–538.

Witten, T. A., & Pincus, P. A. (1986). *Macromolecules*, 19(10)

Direct phase coexistence

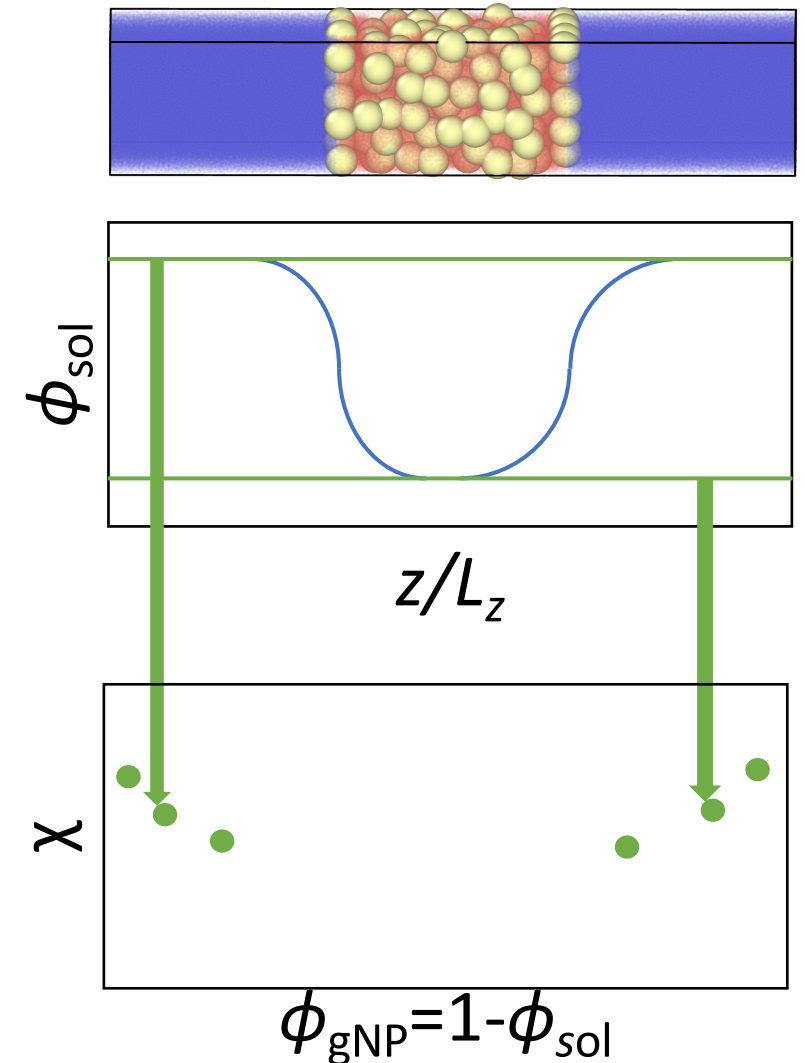
Direct coexistence
simulation configuration

Density profile
of each state point, fit gives phase-
coexistence

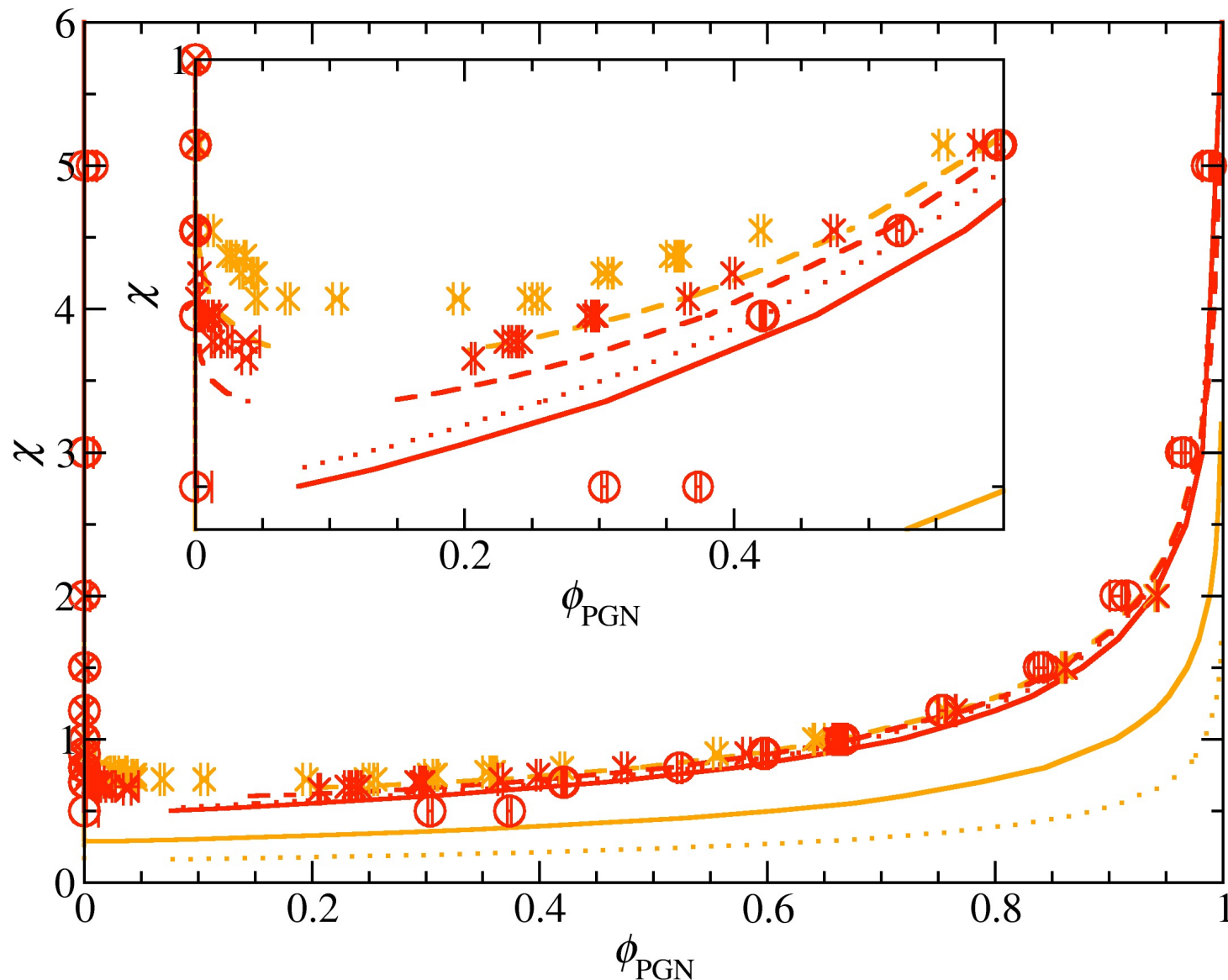
$$\phi_{\text{sol}}(z) = \boxed{\phi_{\text{sol}}} + \frac{\boxed{\phi_{\text{gNP}}} - \phi_{\text{sol}}}{2} \left(\text{erf} \left[\frac{z - L_z/2 + z_0}{\boxed{\Delta\sqrt{2}}} \right] - \text{erf} \left[\frac{z - L_z/2 - z_0}{\Delta\sqrt{2}} \right] \right)$$

fits Δ Interface width

Phase diagrams
from ϕ_{gNP} and ϕ_{sol} to density profile



Phase behavior



symbols: TILD
 star: homopolymer
 circle: PGN
 lines: Flory-Huggins theory

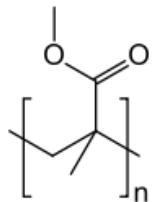
short graft, $N_g = 21.5$ kDa (51 beads)
 long graft $N_g = 53$ kDa (126 beads)

Summary – GNPs in solvent

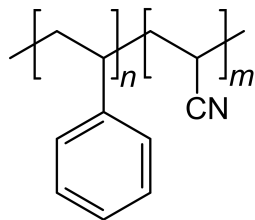
- Graft radial density profile obeys Dauod & Cotton
- Flory-Huggins better predicts homopolymer than PGN phase behavior
- Our method equilibrates long polymers in tractable times
- Nanoparticle size has little effect on phase separation
- Phase separation is induced by:
 1. Increasing polymer-solvent interaction
 2. Increasing grafted polymer length

Experimental homopolymer blend system (PMMA-g-SiO₂ in SAN/PMMA)

PMMA

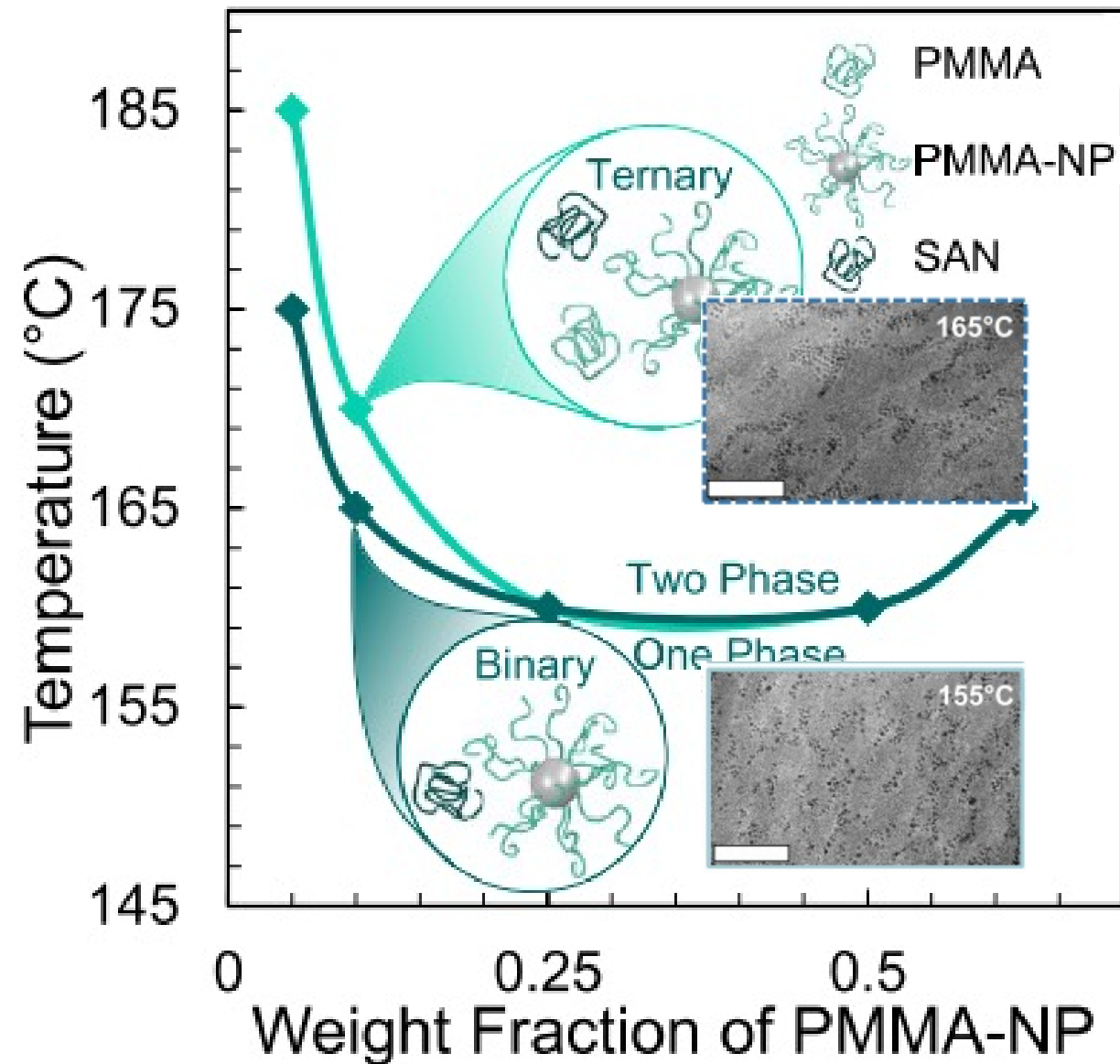


SAN



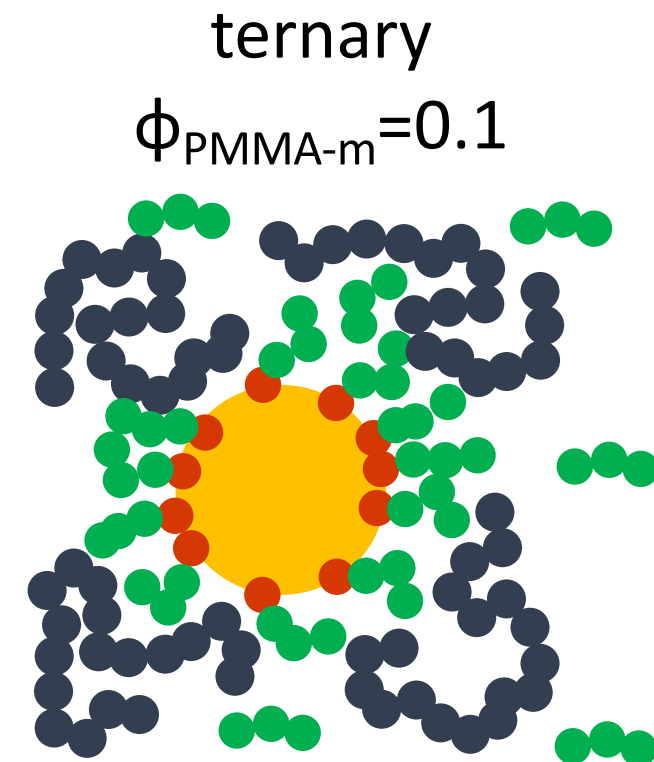
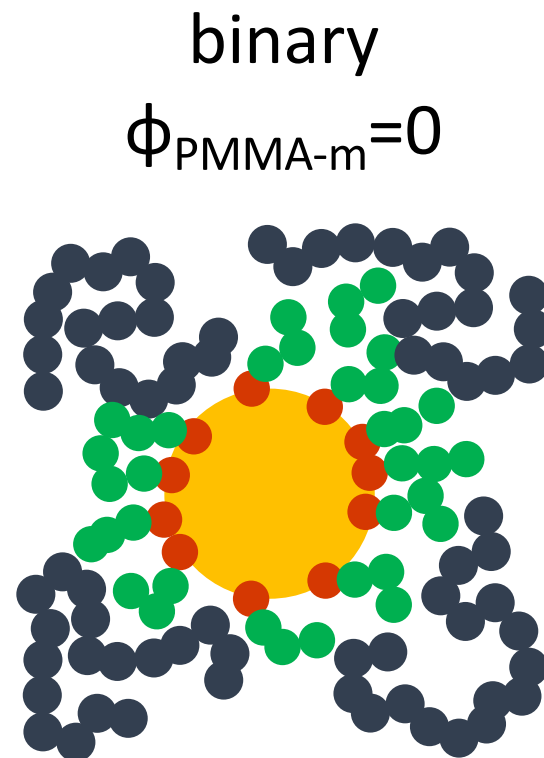
Poly(methyl methacrylate)-grafted
Silica Nanoparticles in
poly(styrene-co-acrylonitrile) [33% AN]

- Optical turbidity
- TEM
- SAXS
- Phase envelope opens with ternary component
- Interfacial compatibilization



Coarse-graining homopolymer blend system

Property	Experimental	TILD
N_G	19 kDa	17
N_M	118 kDa	123
ρ_0		3.41
b		2.29 nm
σ	0.7 chains/nm ²	3.69 chains/b ² (0.27 chains/nm ²)
R_{np}	7.5 nm	3.27 b (7.5 nm)

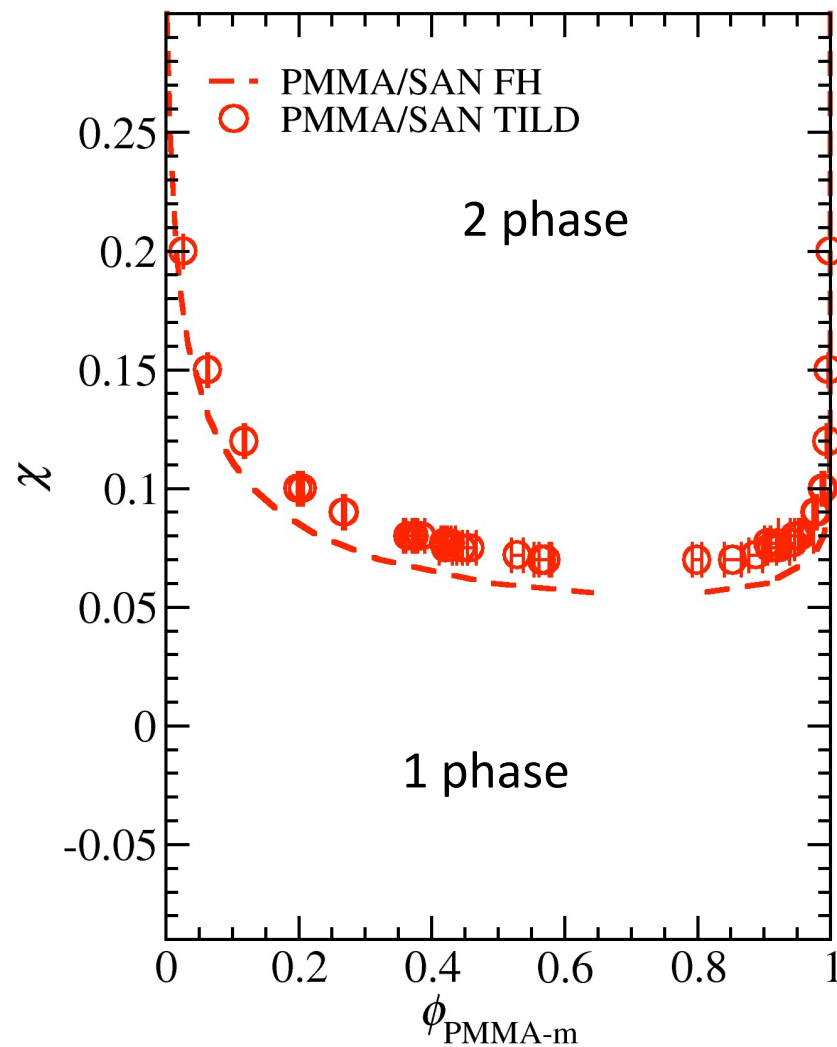


PMMA and SAN (33% Nitrile) ρ , b and χ from:

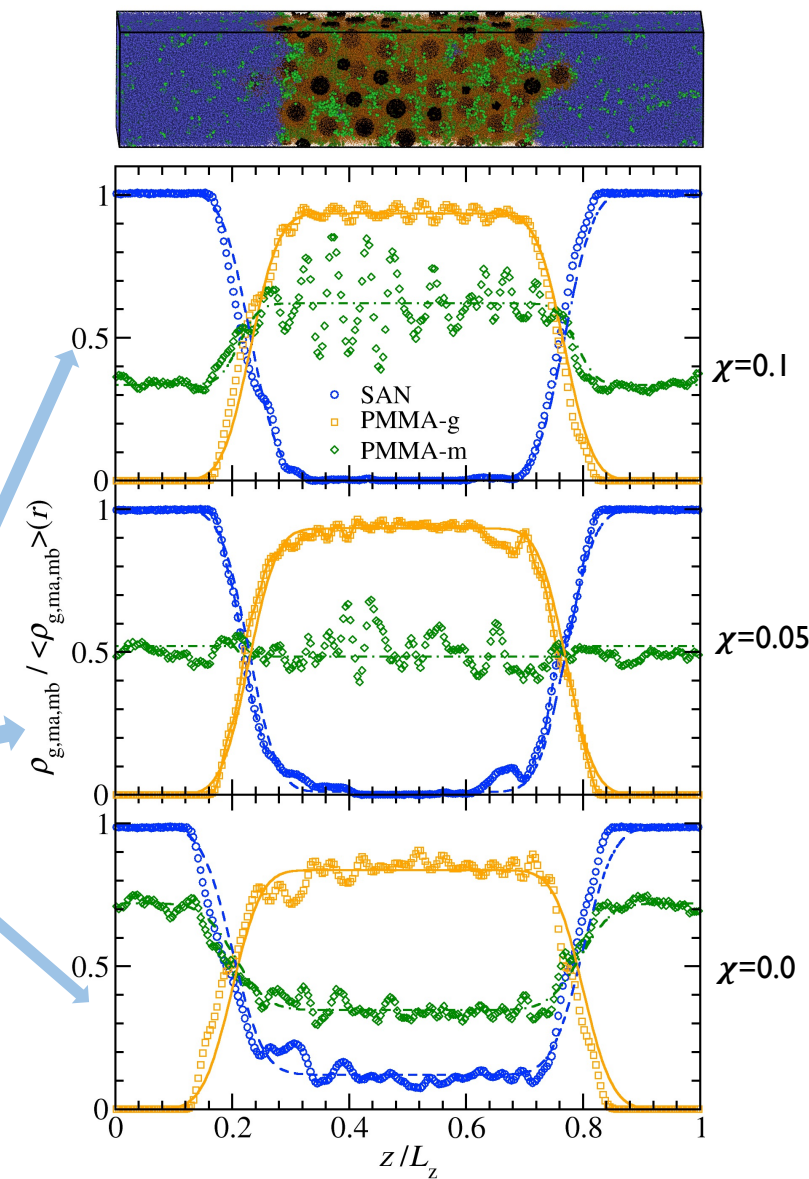
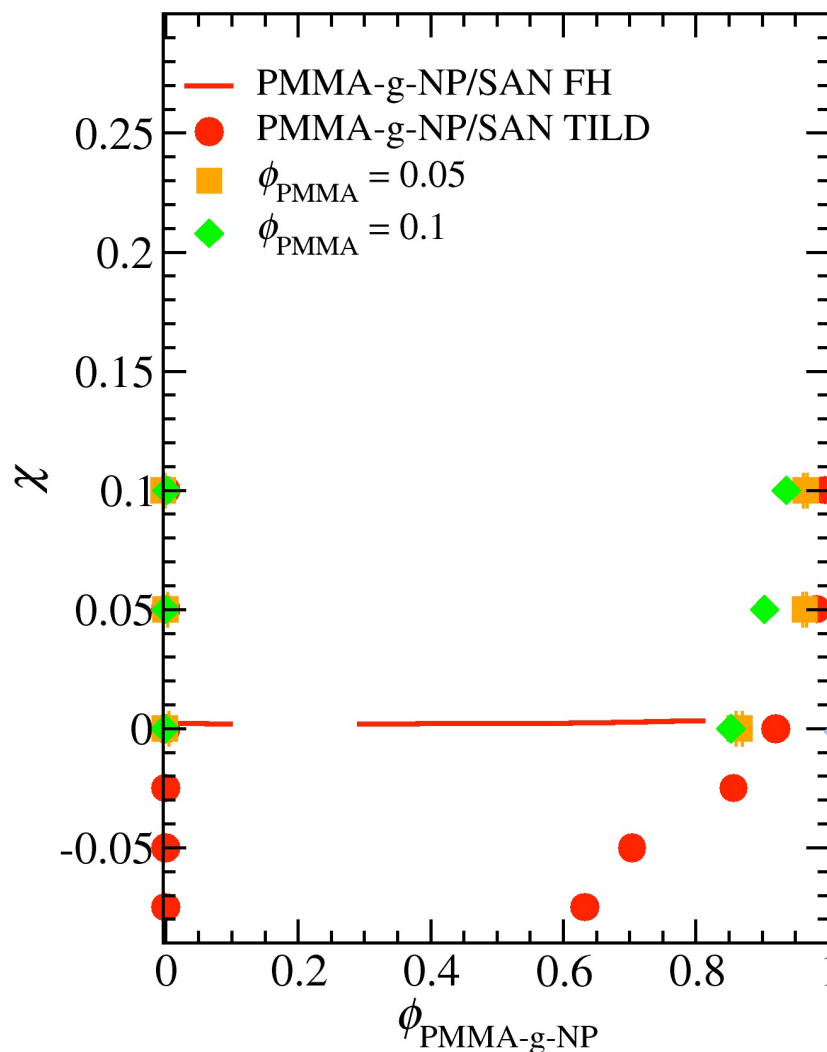
Aoki et al. Macromolecules, 52, 3, 1112-1124
(2019). 10.1021/acs.macromol.8b02431

Phase behavior

Homopolymer blend



Polymer-grafted nanoparticles



PGN brush profile

Polymer-grafted nanoparticles

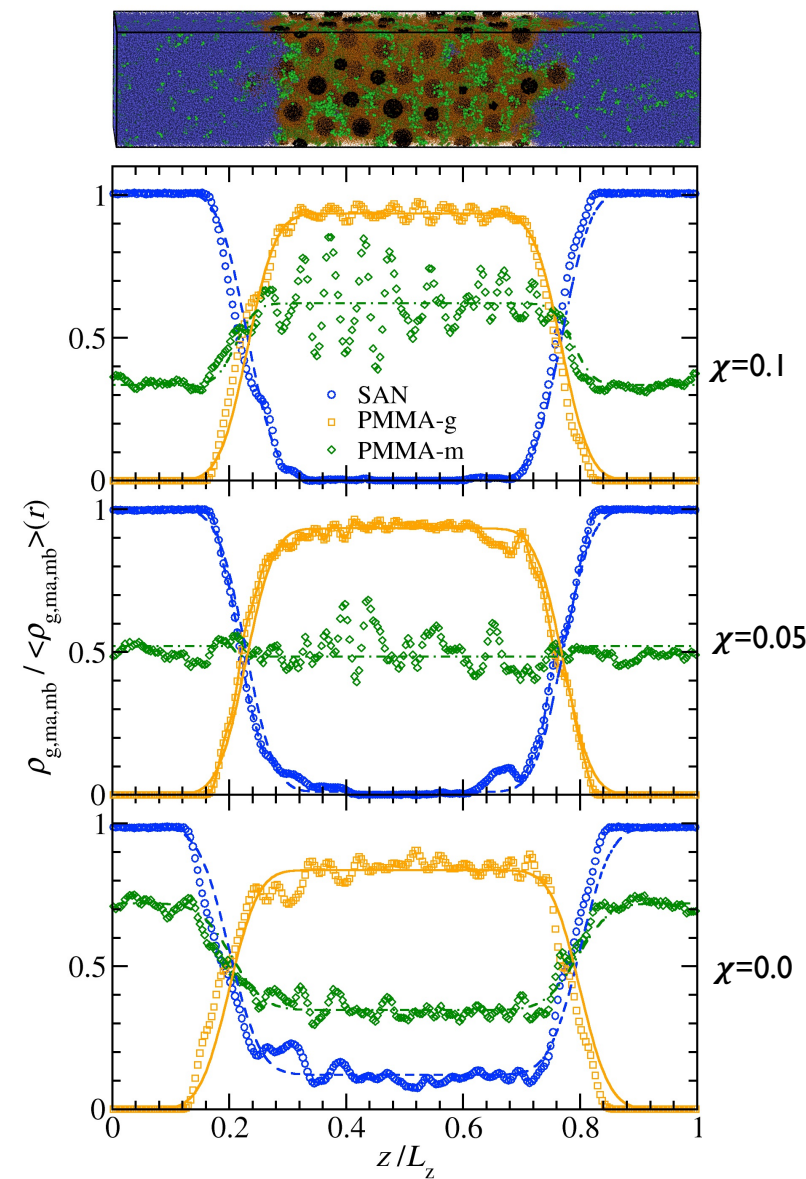
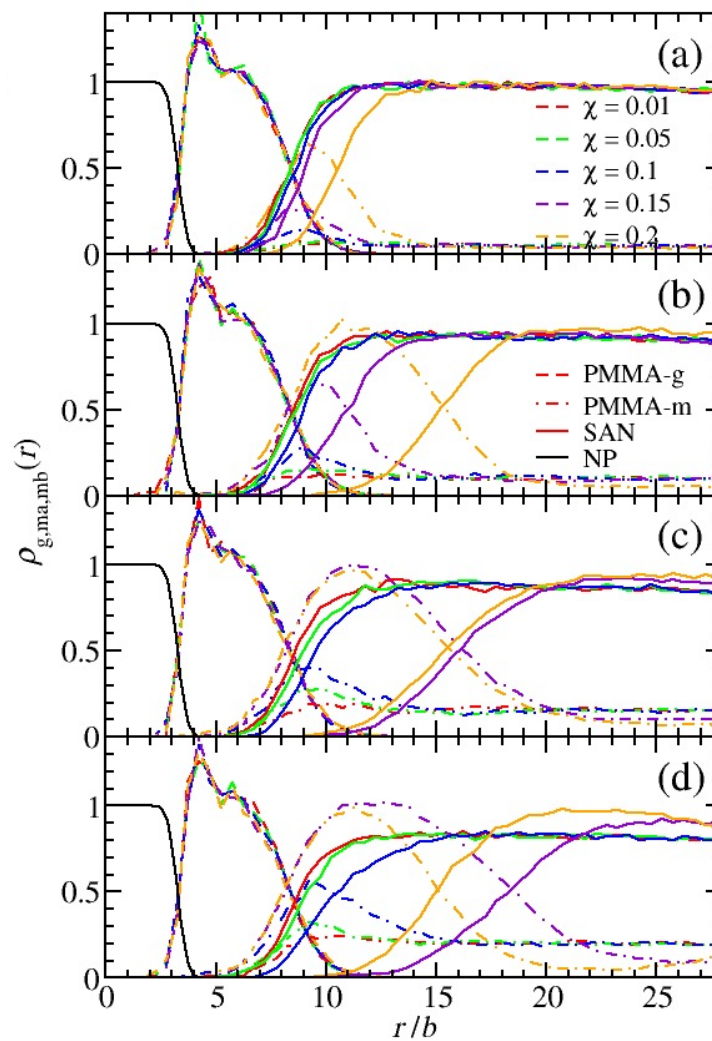
 $\phi_{\text{PMMA-m}}$

0.05

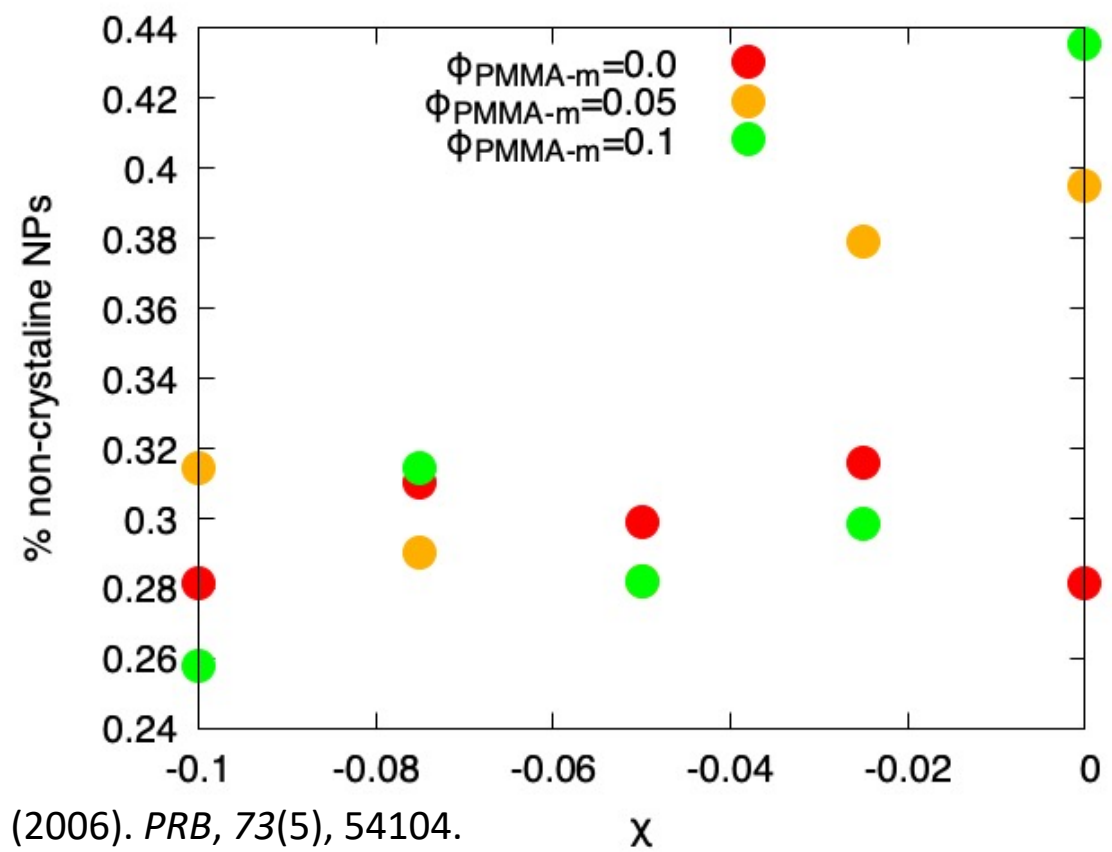
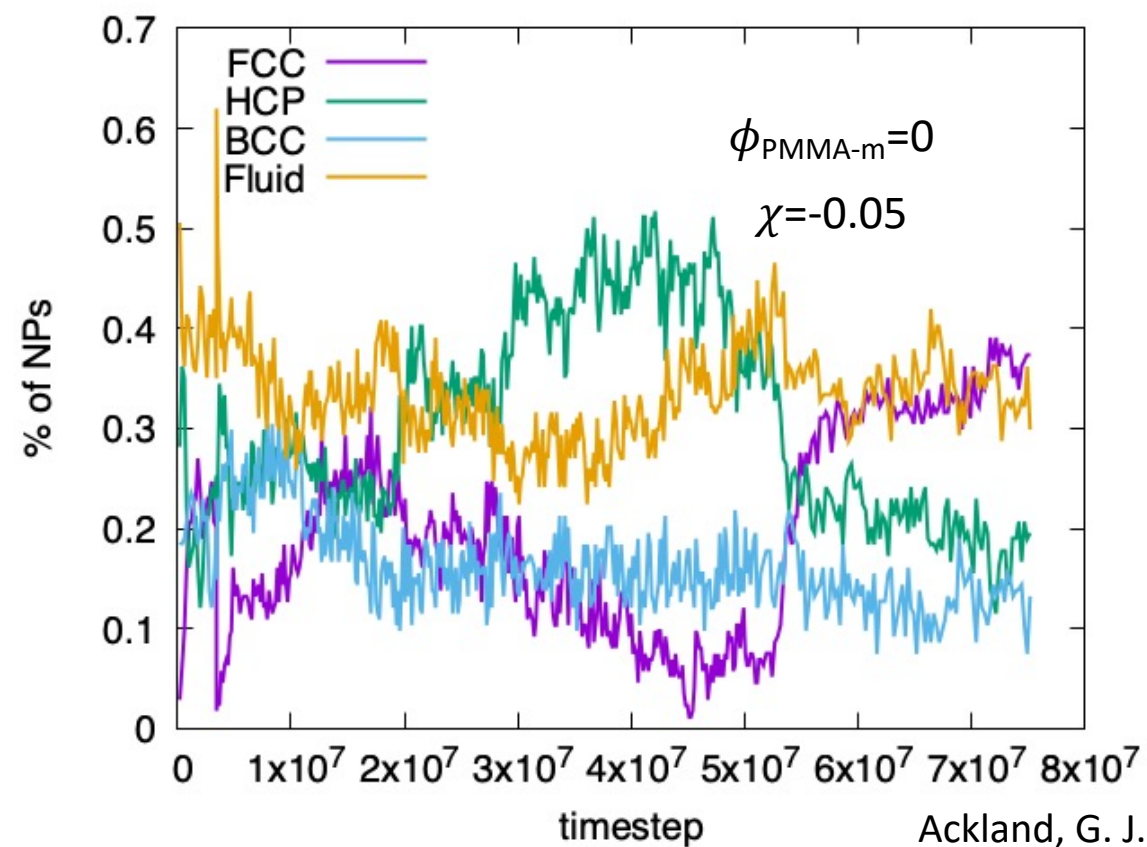
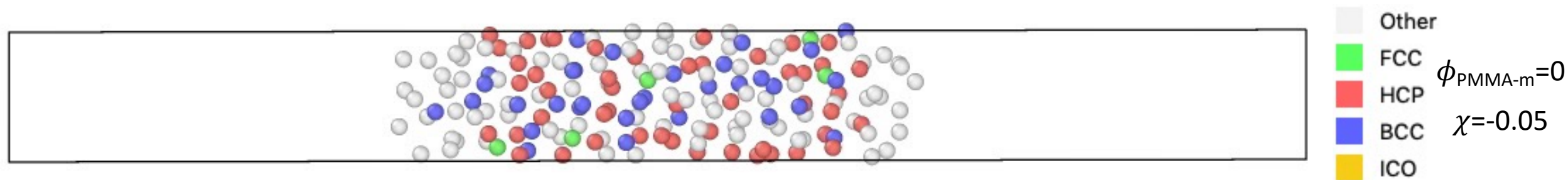
0.1

0.15

0.2



Crystallization



Summary – GNPs in homopolymer

- Nanoparticles order in dense phase
- PMMA/SAN homopolymer phase transition determines:
 - high density of PMMA matrix at graft-melt interface
 - PMMA matrix preference in SAN- or PGN-dense phases
- Flory-Huggins PNC theory does not capture low critical point

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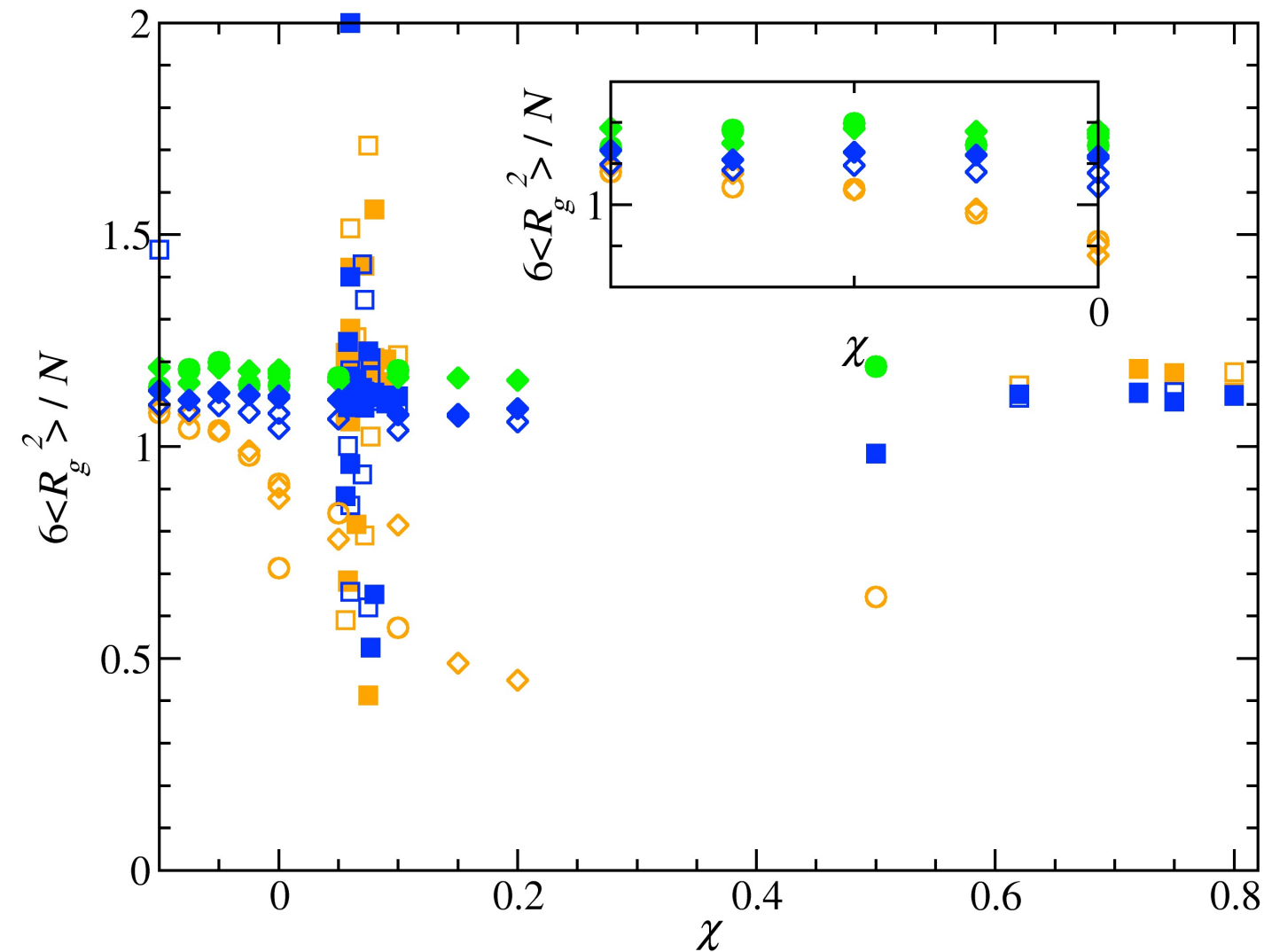


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DOE Basic Energy Sciences DE-SC0002128

Radius of gyration (PMMA/SAN)



- SAN in SAN-dense (PMMA/SAN)
- SAN in SAN-dilute (PMMA/SAN)
- PMMA in SAN-dense (PMMA/SAN)
- PMMA in SAN-dilute (PMMA/SAN)
- SAN in SAN-dense (PGN $\phi_{\text{PMMA-m}}=0.0$)
- SAN in SAN-dilute (PGN $\phi_{\text{PMMA-m}}=0.0$)
- PMMA-g in SAN-dilute (PGN $\phi_{\text{PMMA-m}}=0.0$)
- ◇ SAN in SAN-dense (PGN $\phi_{\text{PMMA-m}}=0.05$)
- ◆ SAN in SAN-dilute (PGN $\phi_{\text{PMMA-m}}=0.05$)
- ◆ PMMA-g in SAN-dilute (PGN $\phi_{\text{PMMA-m}}=0.05$)
- ◇ PMMA-m in SAN-dense (PGN $\phi_{\text{PMMA-m}}=0.05$)
- ◆ PMMA-m in SAN-dilute (PGN $\phi_{\text{PMMA-m}}=0.05$)

- Grafts have a higher radius of gyration than the matrix in any phase
- Grafts are similar in binary and ternary mixtures
- PMMA matrix is longer in GNP phase
- SAN is longer in GNP phase
- Blend system gets weird near critical point (needs investigation)

Coarse-graining homopolymer blend system

Property	Experimental	TILD	CG MD
N_G	19 kDa	17	17
N_M	118 kDa	123	75
ρ_0		3.41	-
b		2.29 nm	1.53 nm (Kuhn length)
σ	0.7 chains/nm ²	3.69 chains/b ² (0.27 chains/nm ²)	0.76 chains/d ² (0.32 chains/nm ²)
R_{np}	7.5 nm	3.27 b (7.5 nm)	2.5 d (3.4 nm)

PMMA and SAN (33% Nitrile) ρ , b and χ from:

Aoki et al. Macromolecules, 52, 3, 1112-1124
(2019). 10.1021/acs.macromol.8b02431