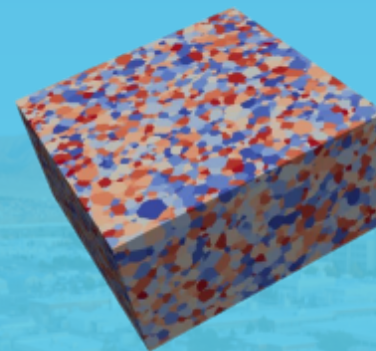
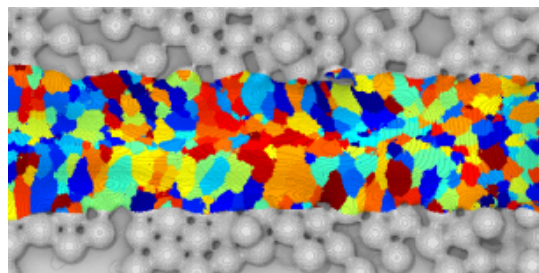
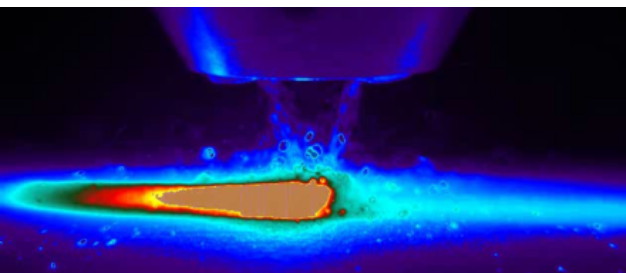
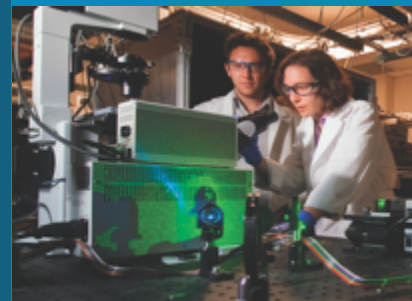




Multiscale Modeling of Microstructure and Damage Evolution in the Performance of Additively Manufactured Parts



PRESENTED BY

Kyle Johnson, **Jonathan D. Madison**, Theron Rodgers, Joseph Bishop, Bradley Jared, and John Emery

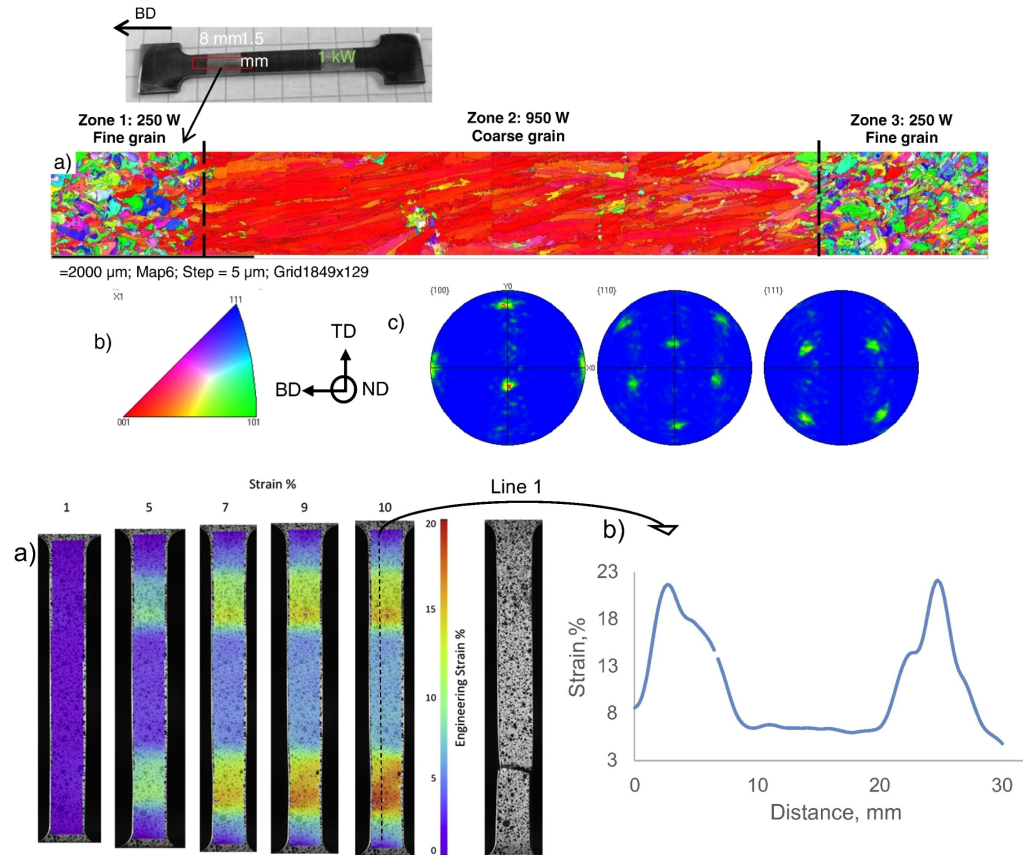
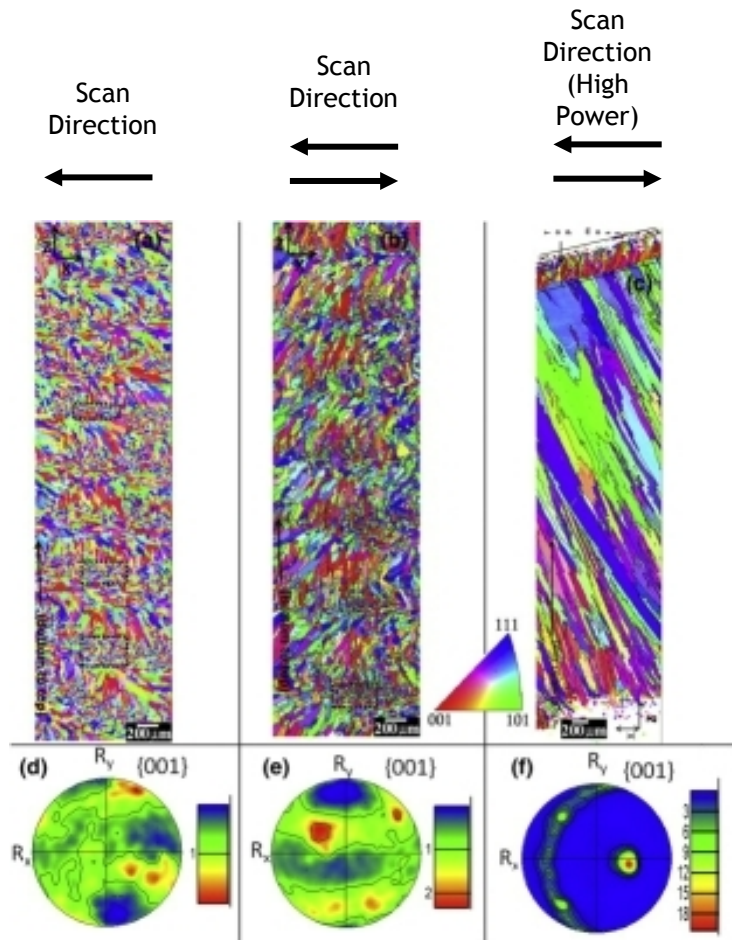


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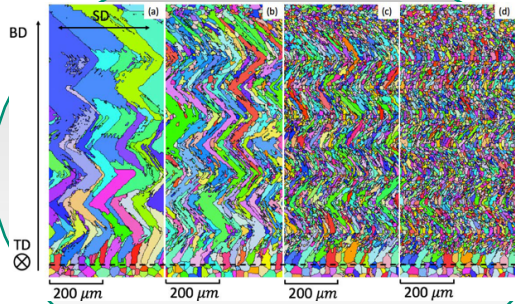


- Background
- Microstructure Prediction
- Upscaling Microstructure Data
 - Direct Numerical Simulations
 - Error Estimation Techniques
- Implementing Voids and Damage
- Summary

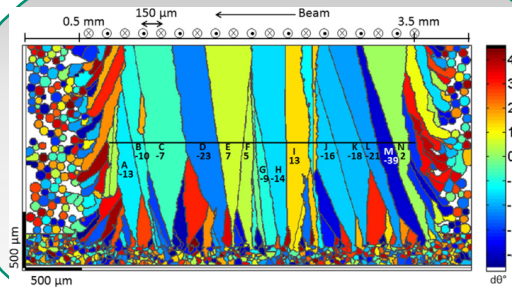
Different Process Settings Cause Different Microstructures and Performance



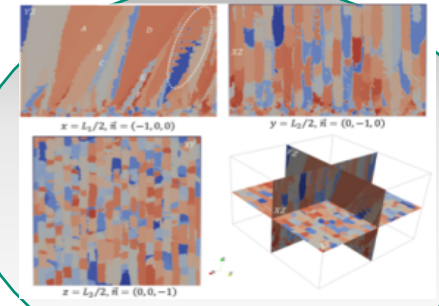
Microstructure Prediction – Cellular Automata Approaches



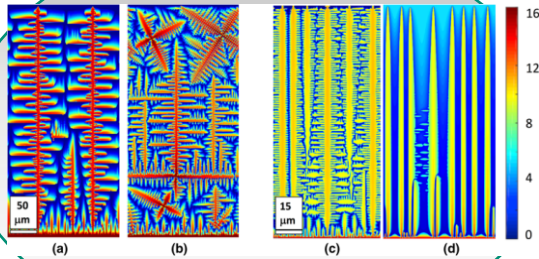
X. Li and W. Tan (U of Utah), SFFS 2017



Rai and Körner (U. Erlangen), Add Manu 2017



Zinovieva et al (U. of Bremen), CMS 2017

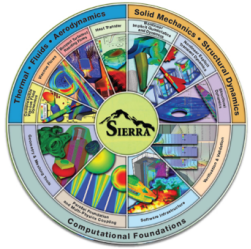


Rolchigo and LeSar (ISU), Met Trans A 2017

Publication	Pros/Included physics	Cons/Missing physics
Li & Tan	<ul style="list-style-type: none"> Nucleation 3D Multi-pass/Layer Coupled thermal solver 	<ul style="list-style-type: none"> No solid state evolution Not parallelized (?) Closed source No fluid flow
Lian and Wagner	<ul style="list-style-type: none"> Parallelized Nucleation 3D Coupled thermofluid solver 	<ul style="list-style-type: none"> Single-pass/layer No solid state evolution Closed source
Zinovieva et al	<ul style="list-style-type: none"> Texture 3D Multi-pass/Layer Coupled thermal solver 	<ul style="list-style-type: none"> No solid state evolution No nucleation Closed source No fluid flow
Rai and Körner	<ul style="list-style-type: none"> Texture Multi-pass/Layer Coupled thermofluid solver (LBM) 	<ul style="list-style-type: none"> No solid state evolution No nucleation 2D Closed source
Rolchigo and LeSar	<ul style="list-style-type: none"> Microscale Dendrite model Component segregation 	<ul style="list-style-type: none"> Single-pass/layer No solid state evolution 2D Closed source

Lian and Wagner (Northwestern), Comp. Mech 2017

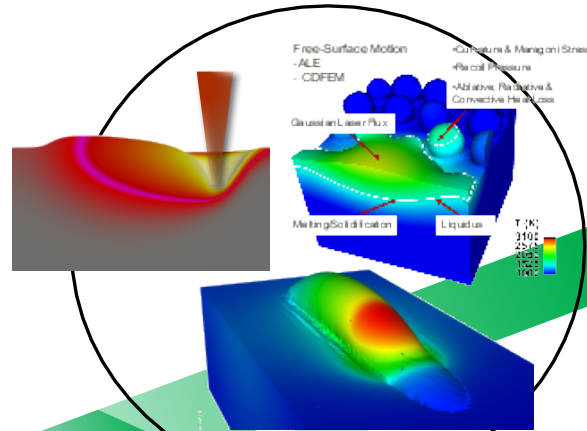
Bridging Length Scales – Informed Relevance



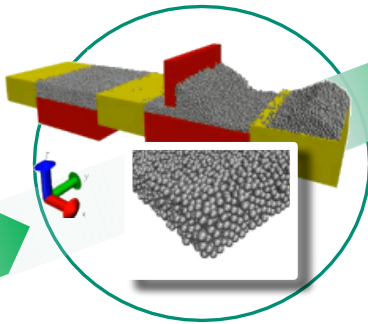
LAMMPS
ARIA
ADAGIO
SPPARKS

Build Scale Thermal + Mechanics
K. Johnson, K. Ford & J. Bishop

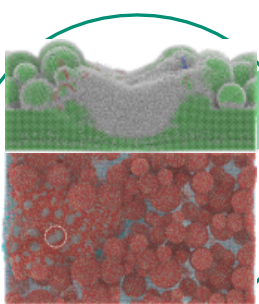
Solidification Scale Thermal
M. Martinez, B. Trembacki, D. Moser



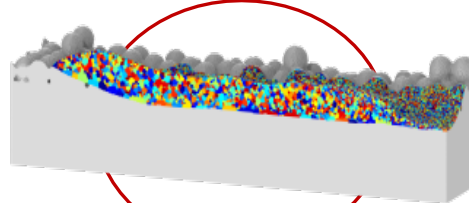
Powder Spreading
D. Bolintineanu



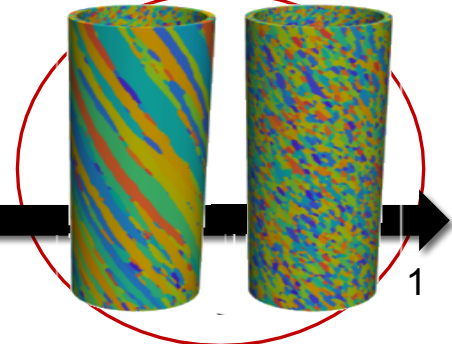
Powder Behavior
M. Wilson



Mesoscale Texture/Solid Mechanics
T. Rodgers, J. Brown, K. Ford



Build Scale Microstructure
T. Rodgers, J. Madison



10^{-6}

10^{-3}

Length Scale (m)

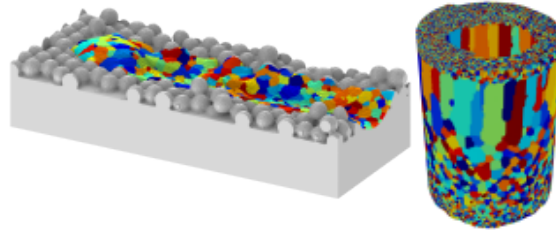
1

Process – Structure – Property – Performance Linkages via *Microstructurally Aware Simulation*



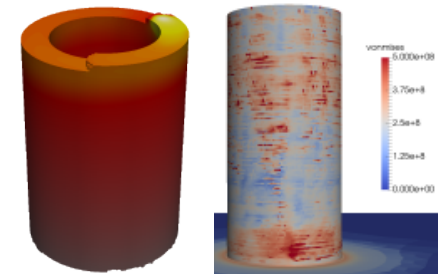
Mesoscale Texture/Solid Mechanics/CX

T. Rodgers, J. Brown, K. Ford



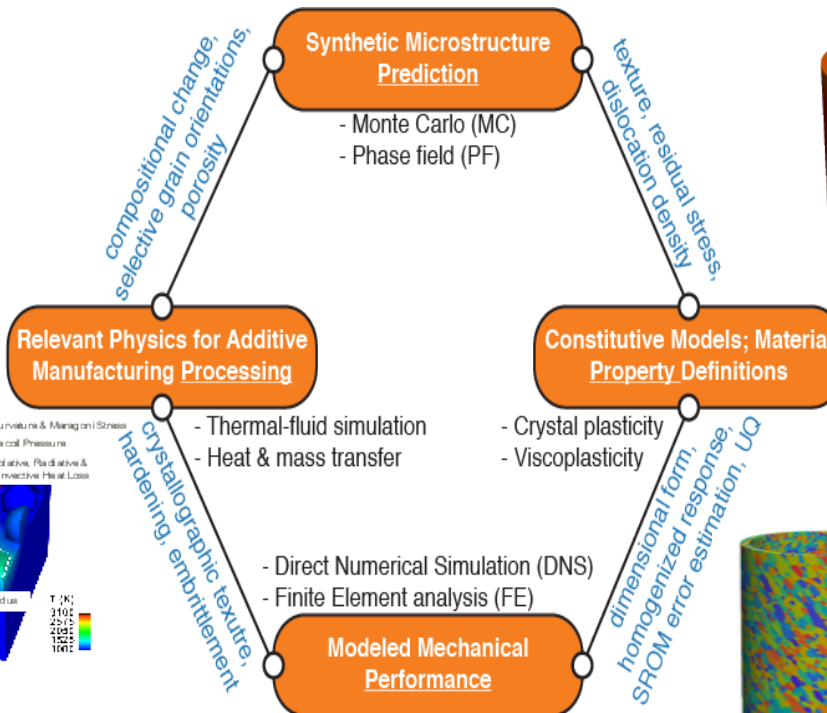
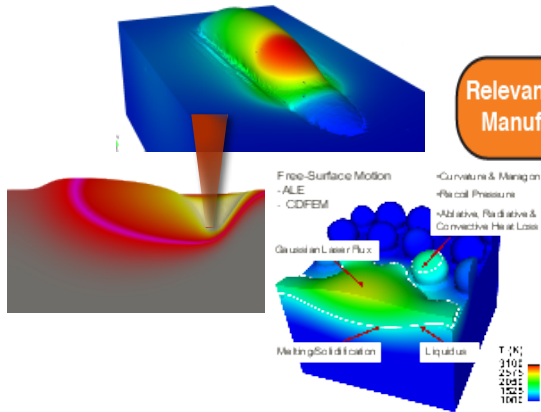
Build Scale Thermal + Mechanics

Kyle Johnson, Kurtis Ford & Joe Bishop



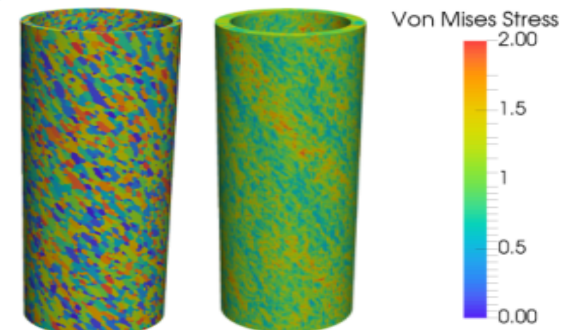
Solidification Scale Thermal

M. Martinez, B. Trembacki, D. Moser

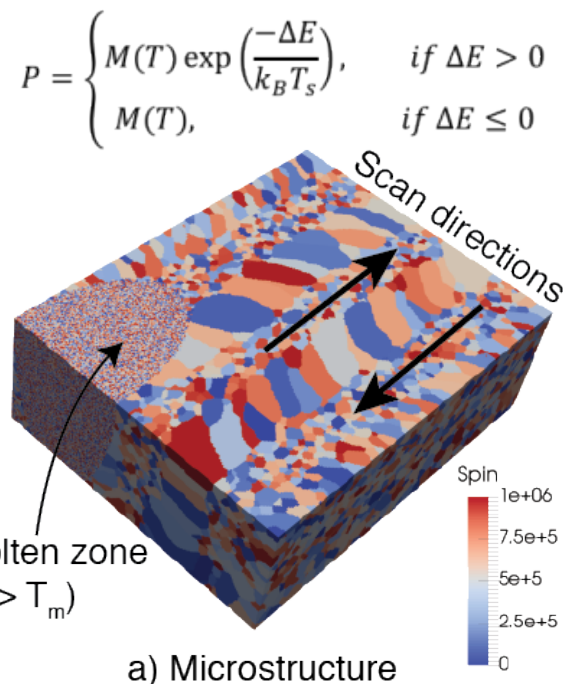
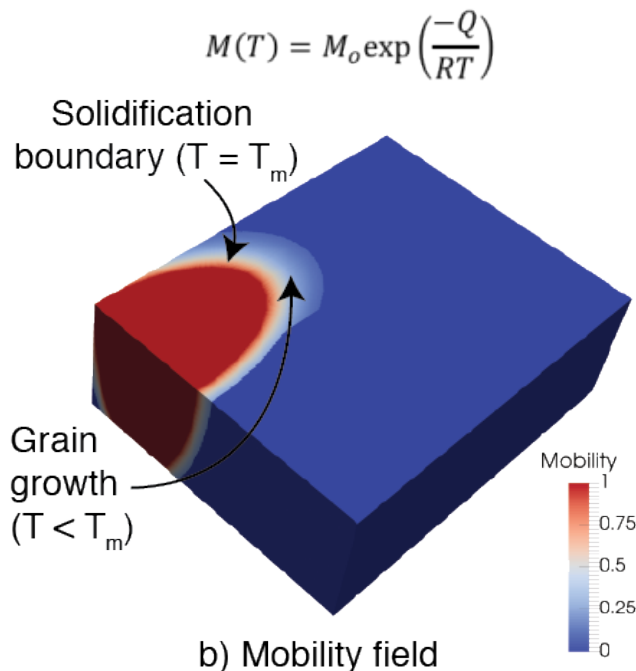
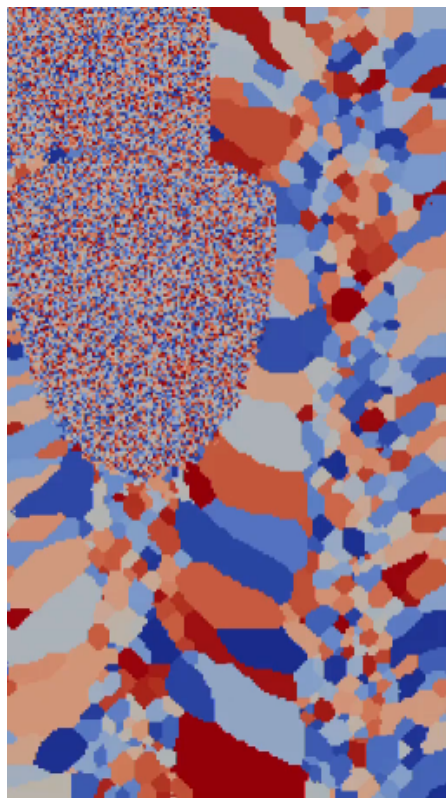


Direct Numerical Simulation

Theron Rodgers, Joe Bishop & Jon Madison



Microstructure Prediction in **Stochastic Parallel** **PART**icle **K**inetic **S**imulator (SPPARKS)

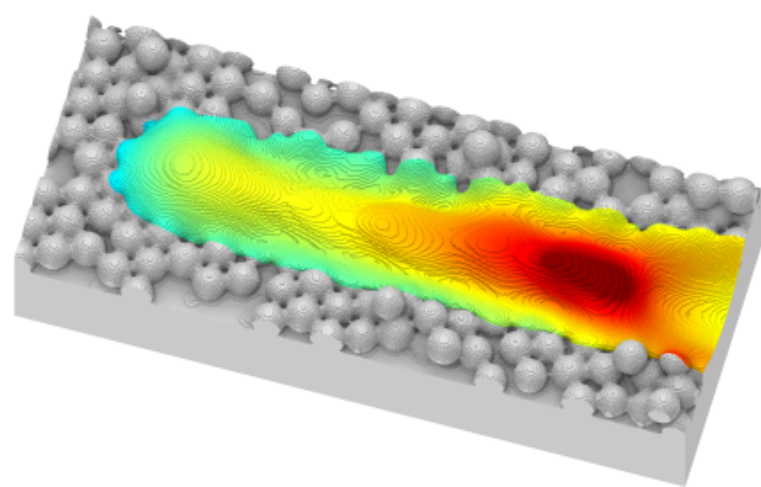


kMC & Solidification Structure

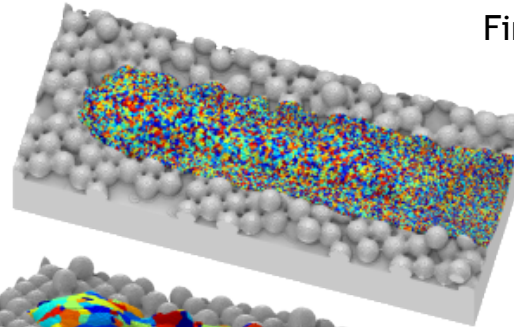
- The molten zone randomizes grain identities when it enters a region.
- Along the trailing surface, voxels either join existing columnar grains or form new grains.
- The temperature gradient creates a corresponding gradient of grain boundary mobilities via an Arrhenius relationship.



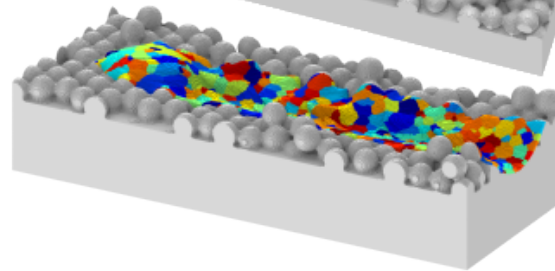
Final temperature field of thermofluid simulation (M. Martinez)



Final microstructure with old nucleation



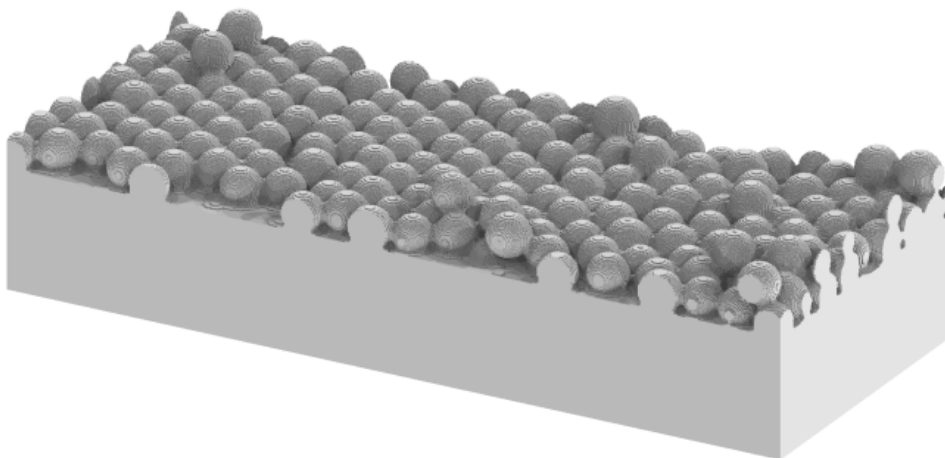
Final microstructure with $N_o = 10^{15}$

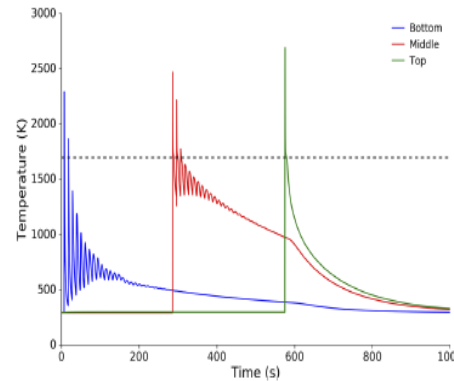
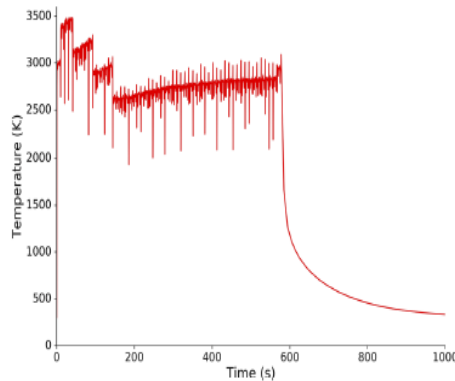
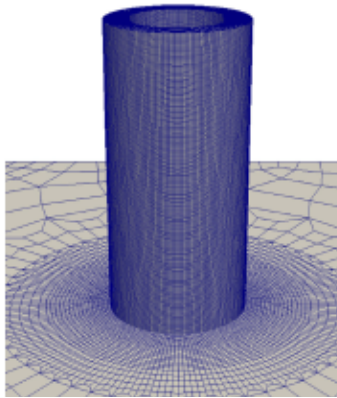


Effect of nucleation site density:

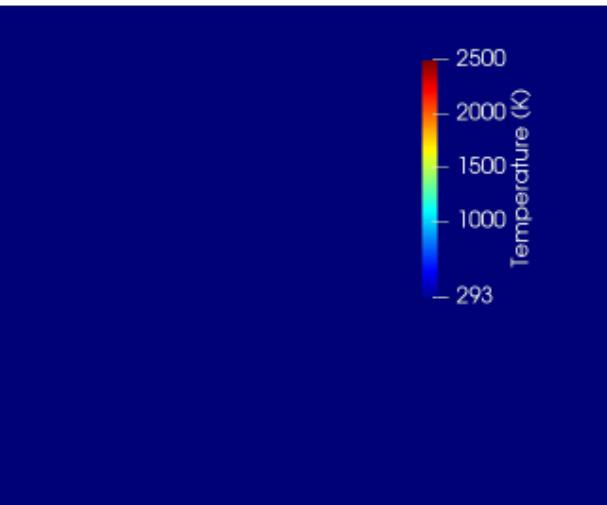
Particle-scale powder bed simulations used a much smaller lattice size than previous work (0.75 μm vs $\sim 20 \mu\text{m}$). With the old nucleation approach, these led to a large overprediction of nucleating grains, which resulted in a fine equiaxed structure (top).

Introducing a N_o -dependent nucleation rule allowed only 1 nucleation site per 2,500 lattice sites and resulted in larger grains that grew from the substrate structure.

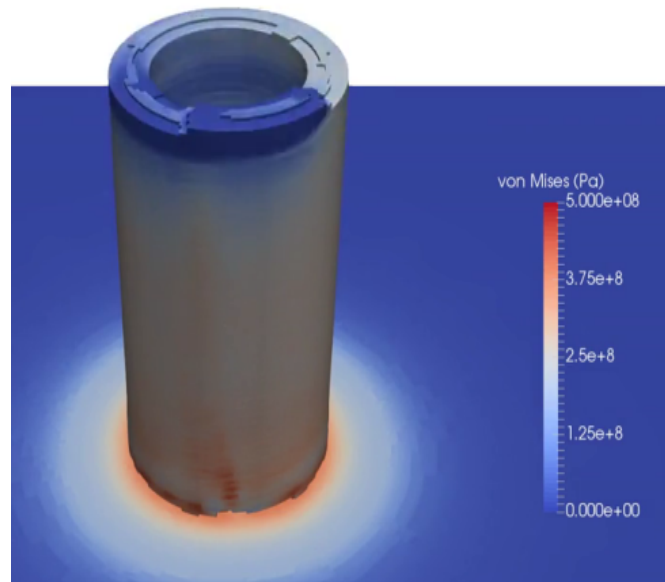




Using a radiative, conduction model we can estimate not only the build scale thermal field and history, but also the effective residual stresses within the build as a function of thermal history.



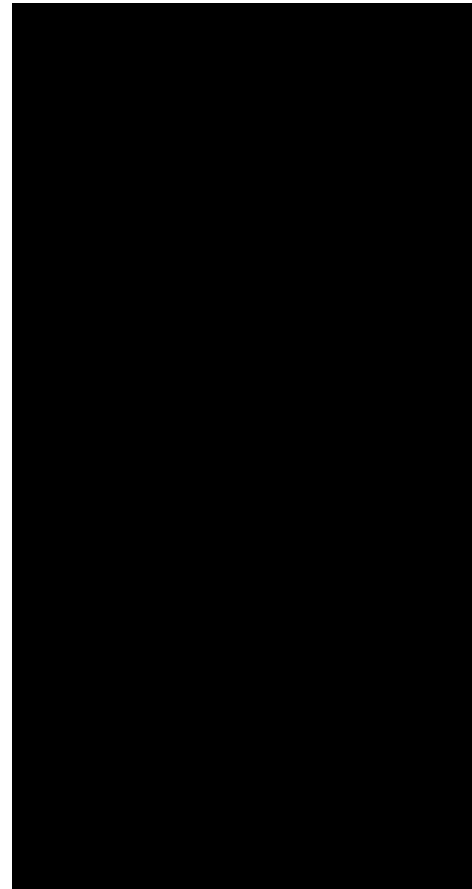
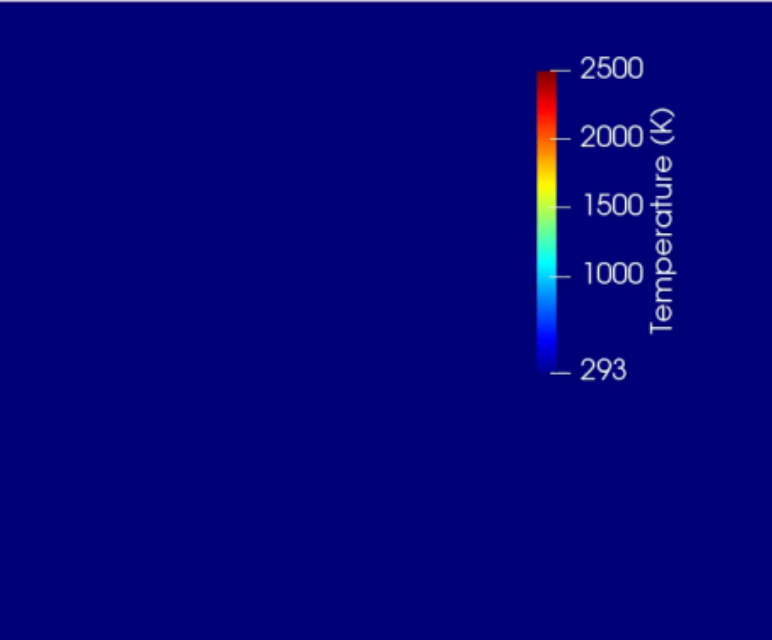
thermal



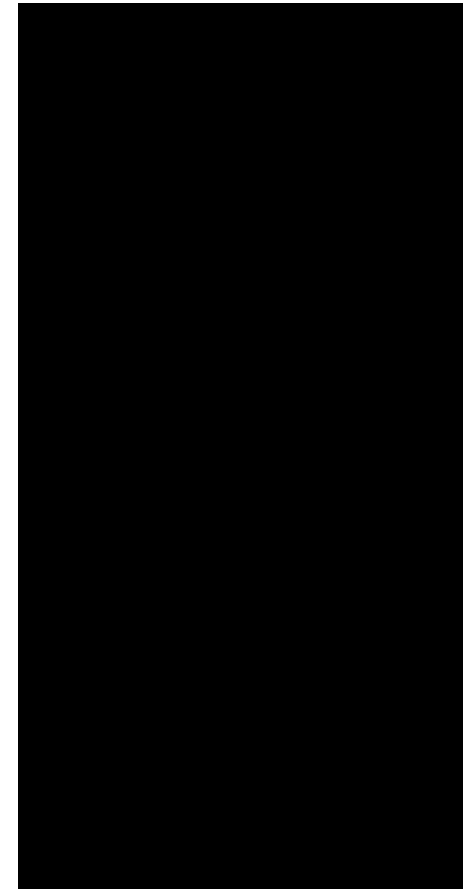
residual stress

This goes beyond the local melt-scale solidification front phenomena to provide build scale understanding across appreciable intervals of time and physical space.

Sandia – Conduction & Radiation Model + Grain Prediction

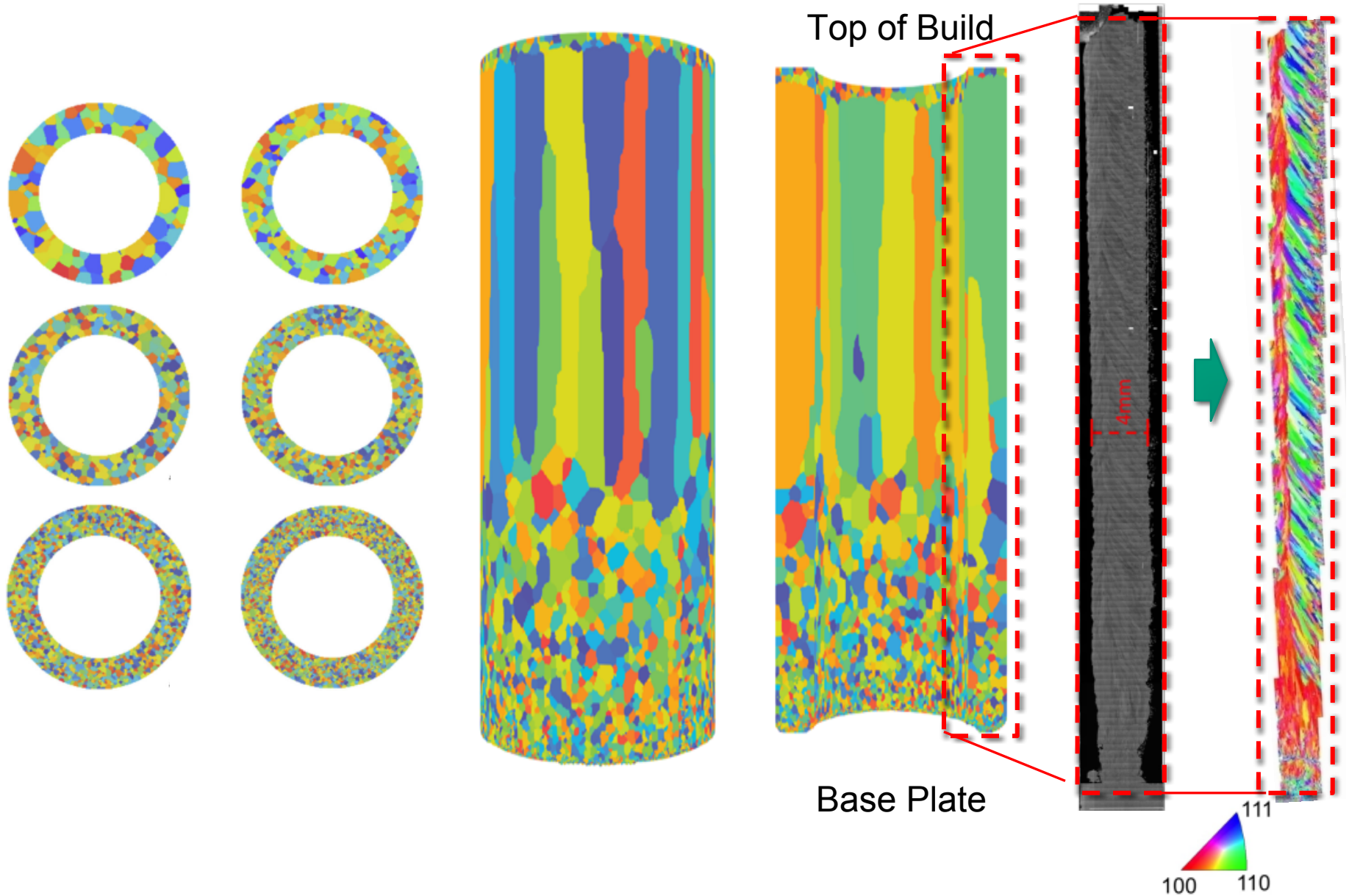


Single
Continuous
Build

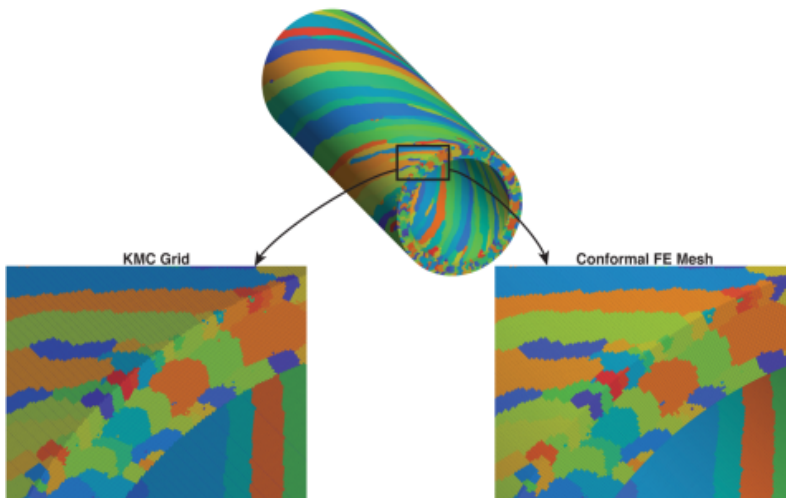
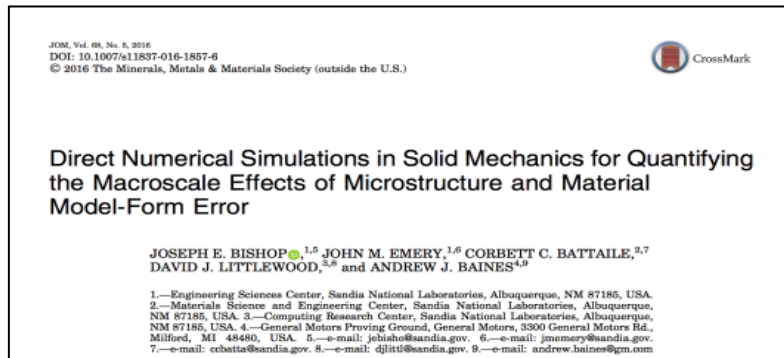
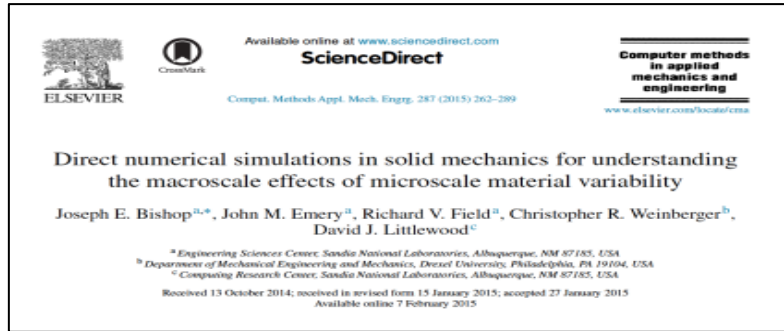


Double Build
(8 second delay in
between layers)

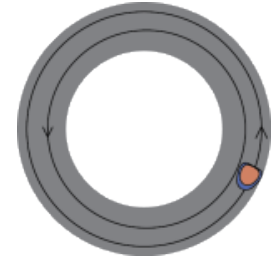
Sandia – Comparison with Experiment



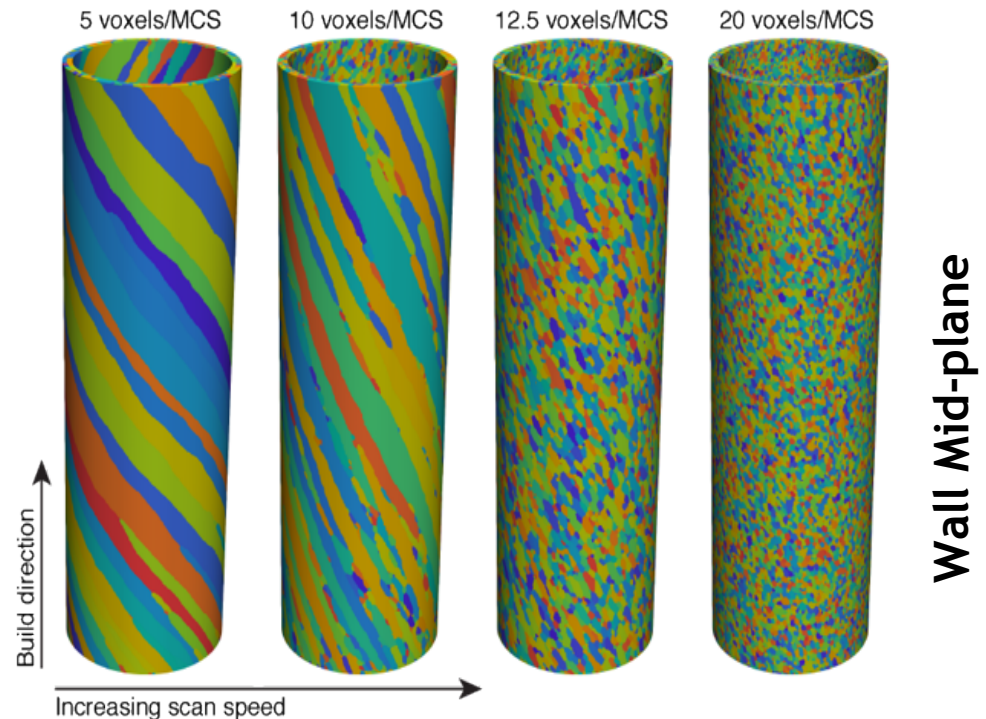
Direct Numerical Simulation on Additive Microstructures



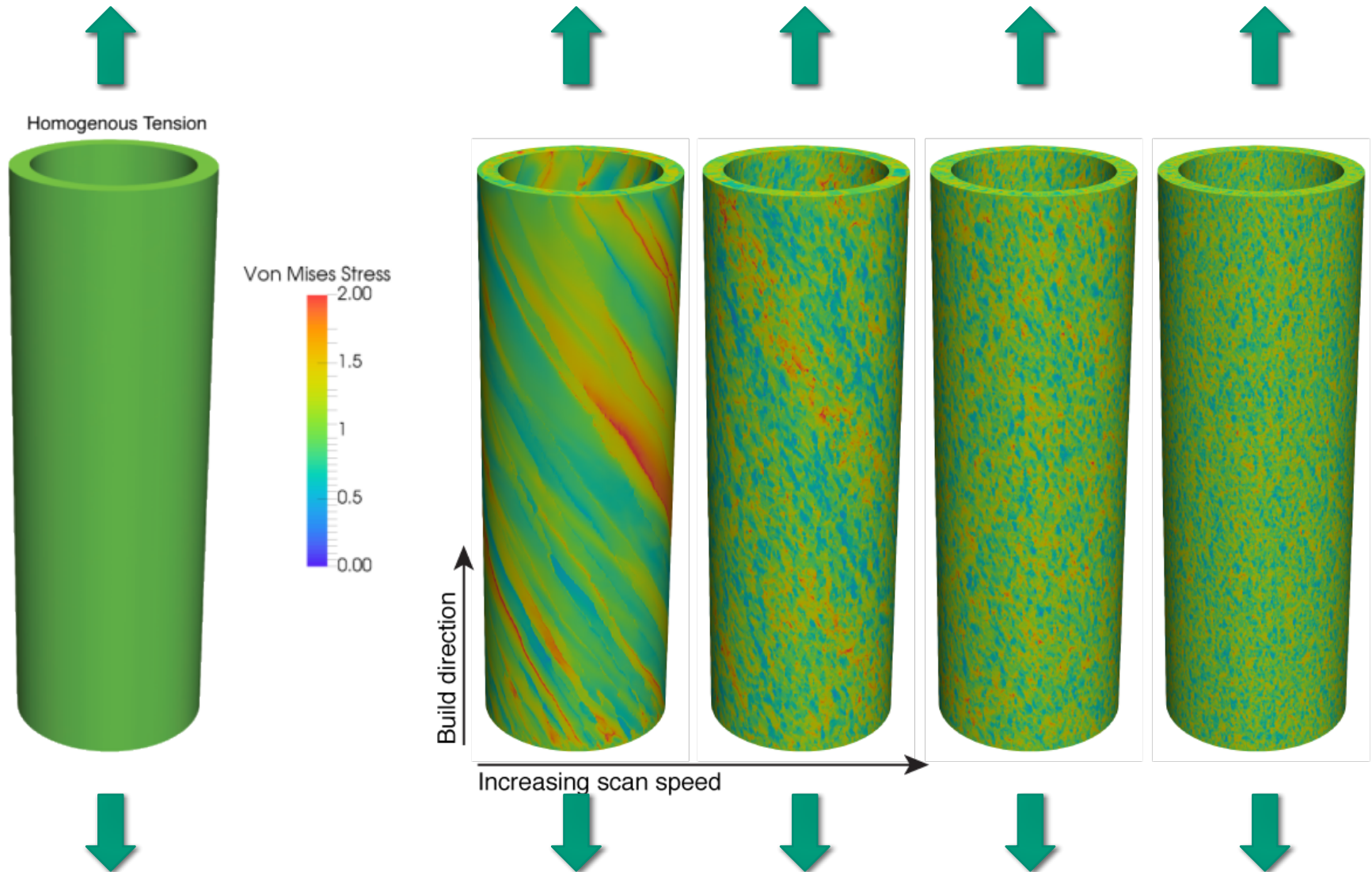
Synthetic AM builds



- 4 scan velocities.
- 2 concentric circular scan paths per layer.
- Idealized molten pool
- Significant microstructure variation w.r.t. scan velocities and w.r.t. wall thickness.

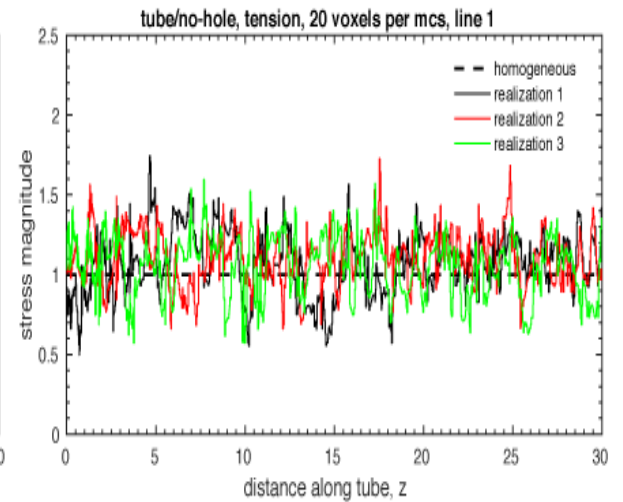
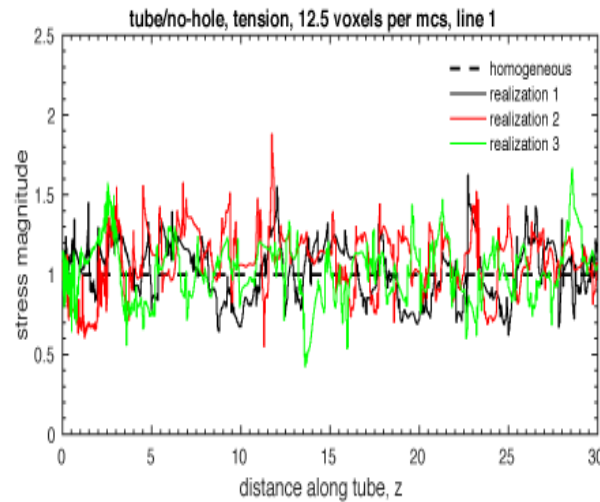
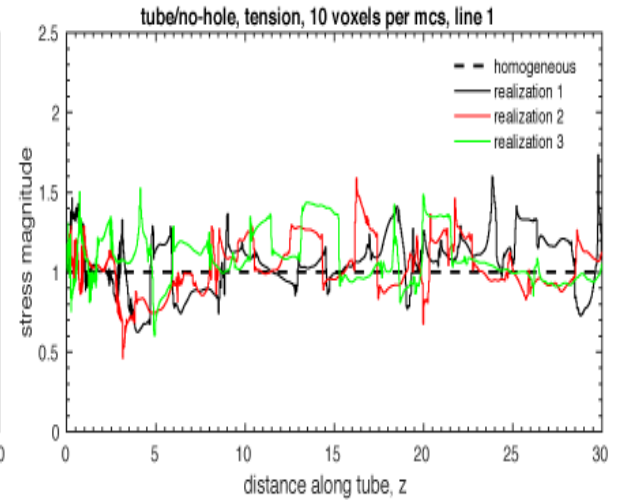
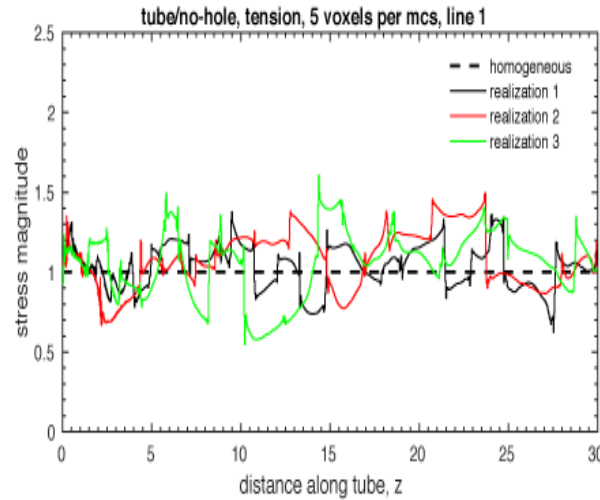
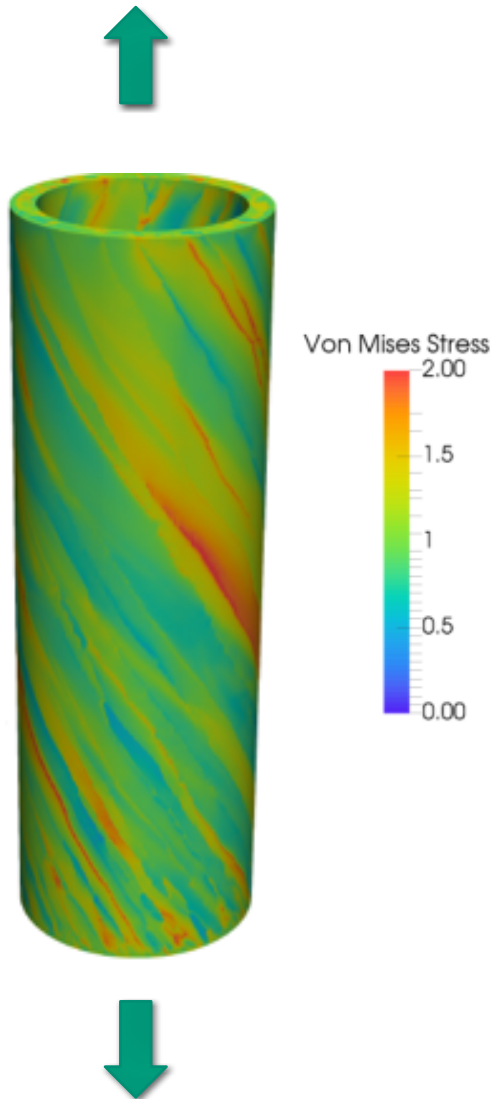


Direct Numerical Simulation on Additive Microstructures



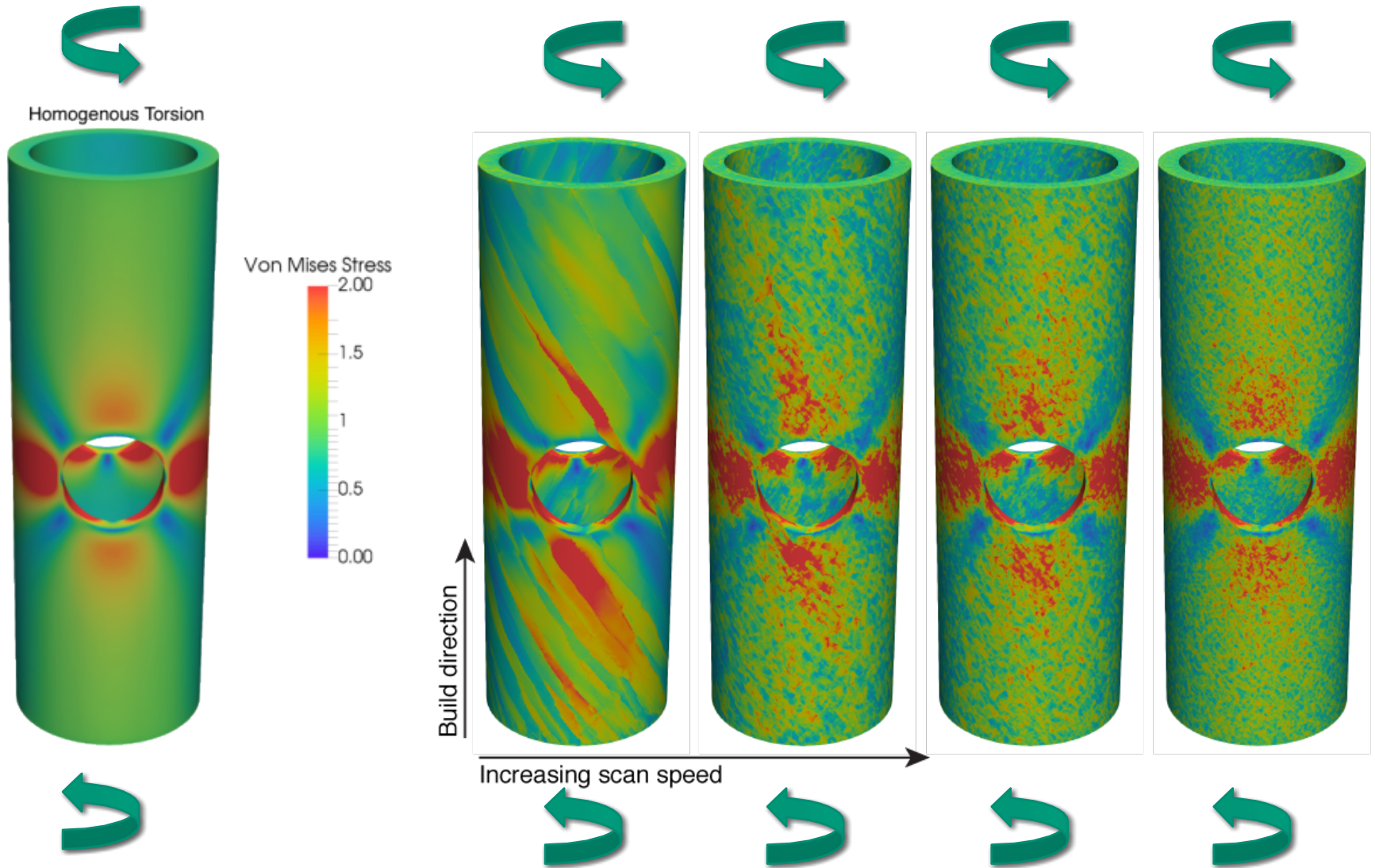
Stress response in tension

Direct Numerical Simulation on Additive Microstructures



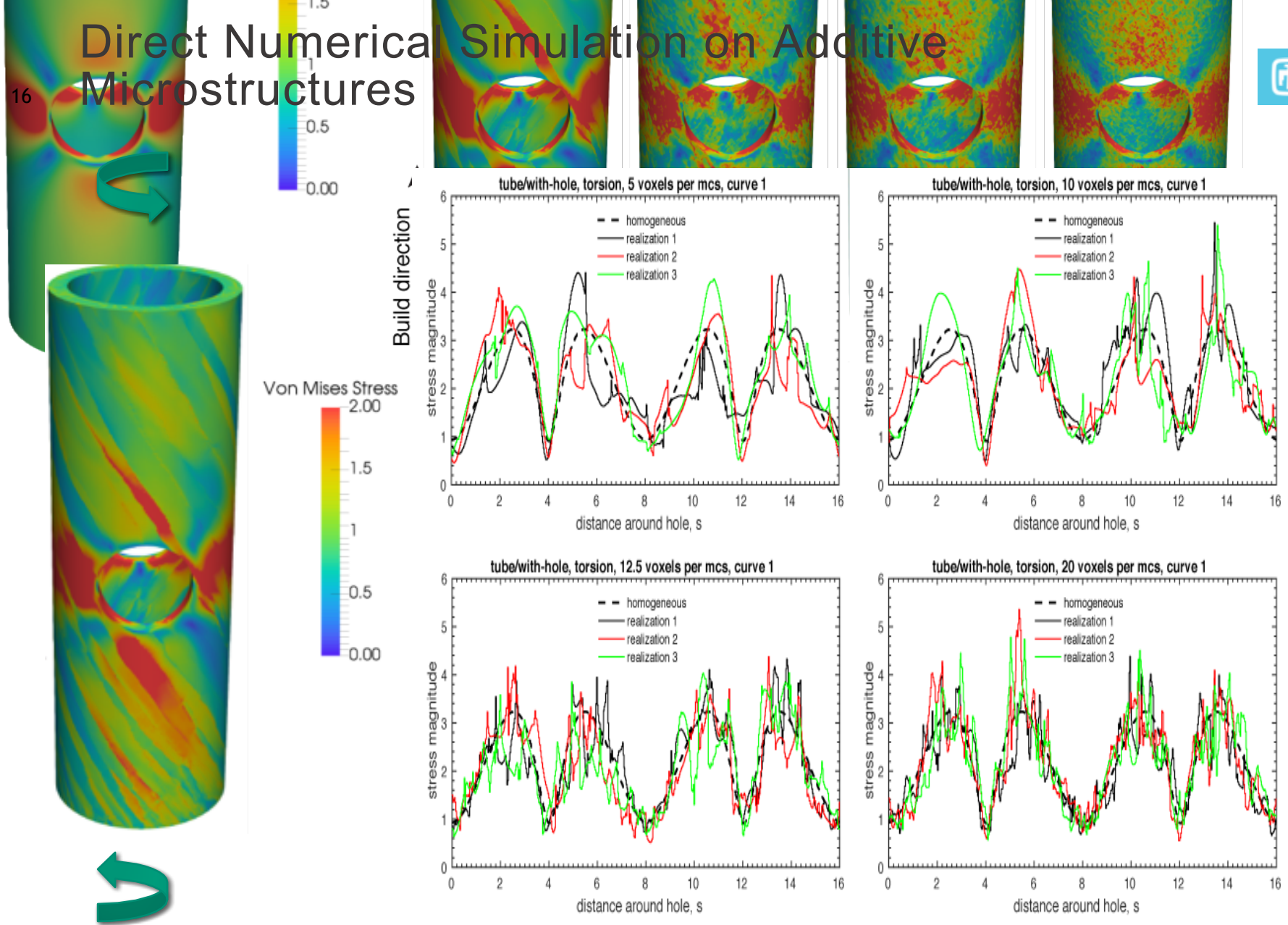
Stress response in tension

Direct Numerical Simulation on Additive Microstructures



Stress response in torsion

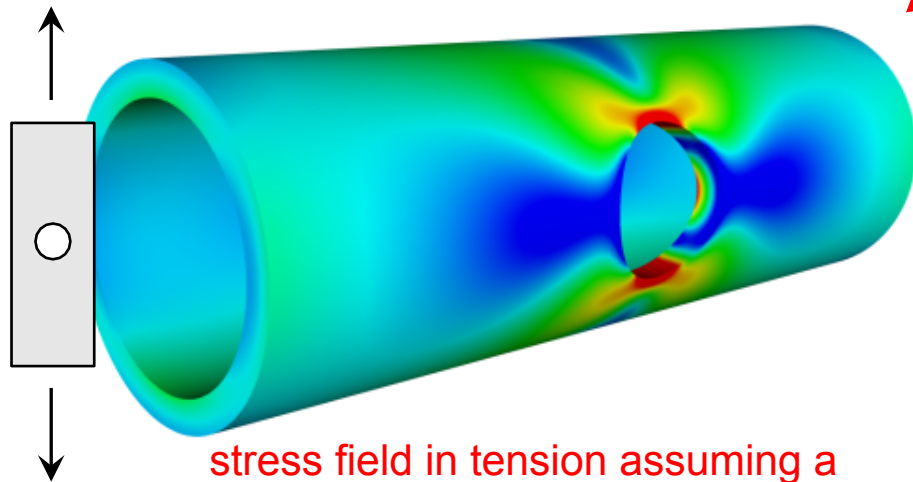
Direct Numerical Simulation on Additive Microstructures



Stress response in torsion

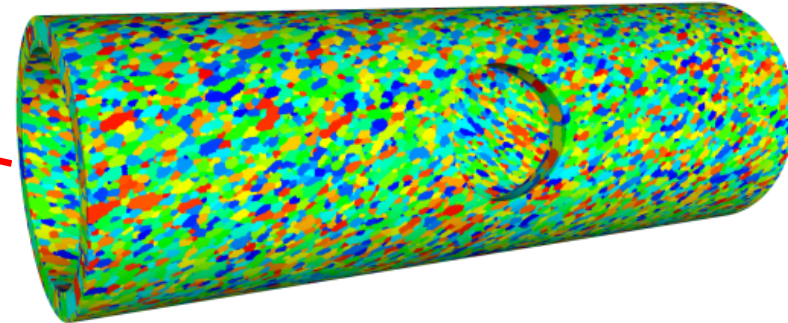
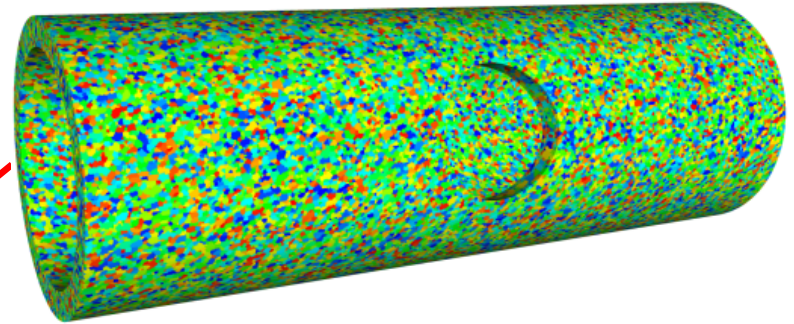


- simple macroscale model
- deterministic (**simulate once**)
- assess error *a posteriori*



stress field in tension assuming a homogeneous isotropic material

variable microstructure



time to failure

stochastic
bound

$$t_f(\omega) \longrightarrow t_f \leq \eta(\omega)$$



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in applied
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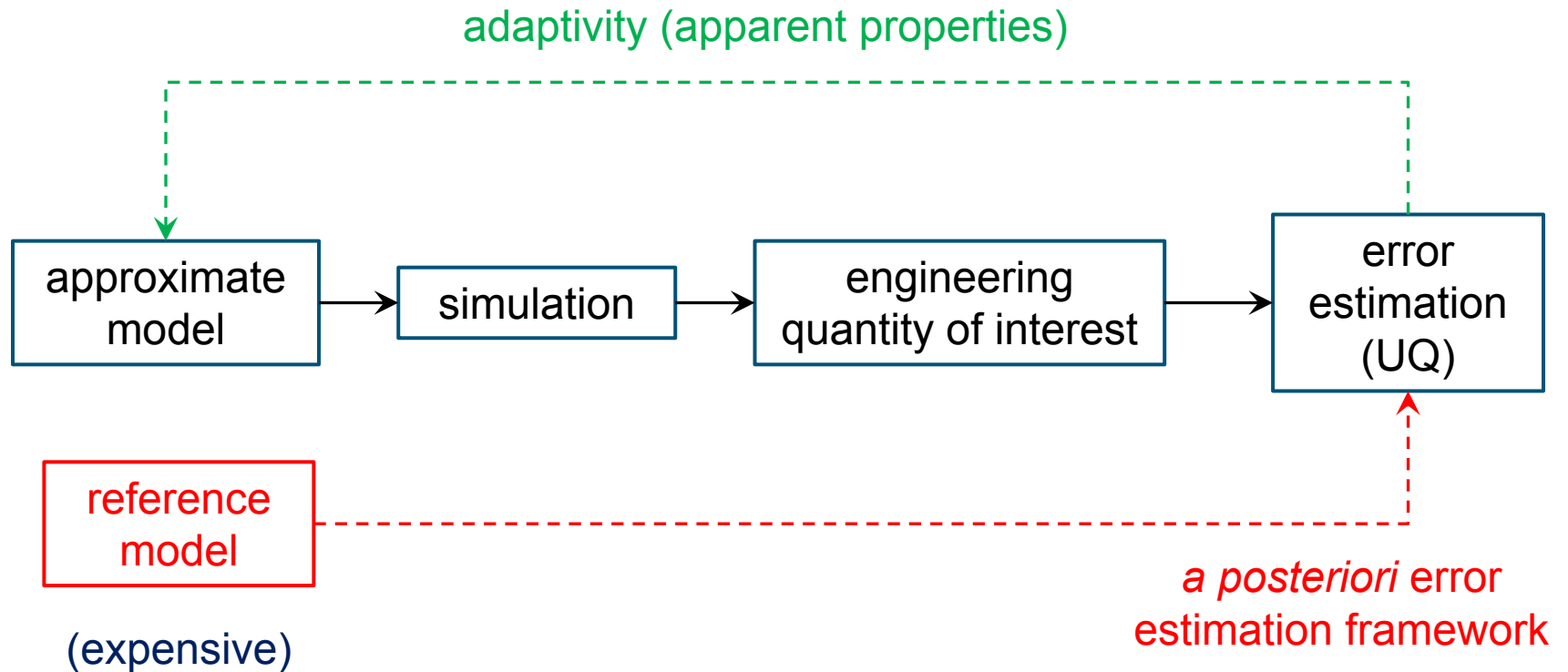
Adaptive reduction of constitutive model-form error using
a posteriori error estimation techniques

Joseph E. Bishop*, Judith A. Brown

Solid Mechanics Department, Engineering Sciences Center, Sandia National Laboratories, Albuquerque, NM 87185, USA

Received 18 November 2017; received in revised form 9 April 2018; accepted 5 June 2018

Available online 15 June 2018



time to failure

$$t_f(\omega) \longrightarrow t_f \leq \overset{\text{stochastic bound}}{\eta(\omega)}$$

Error estimation: material-model error



(Zohdi, Oden, Rodin, 1996, “Hierarchical modeling of heterogeneous bodies”, CMAME)

$$\|\mathbf{u} - \mathbf{u}^0\|_E^2 \leq \int_{\Omega} (\boldsymbol{\varepsilon}^0 - \bar{\boldsymbol{\varepsilon}}) : (\bar{\boldsymbol{\sigma}} - \boldsymbol{\sigma}^0) d\Omega$$

displacement field
using true material
model

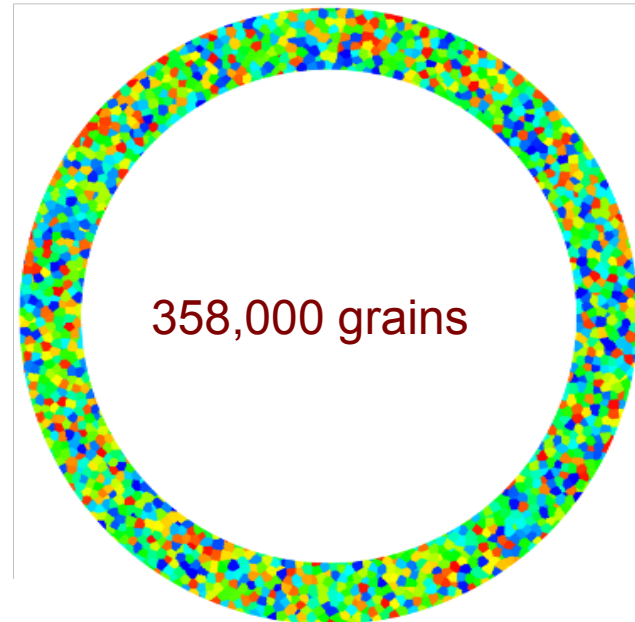
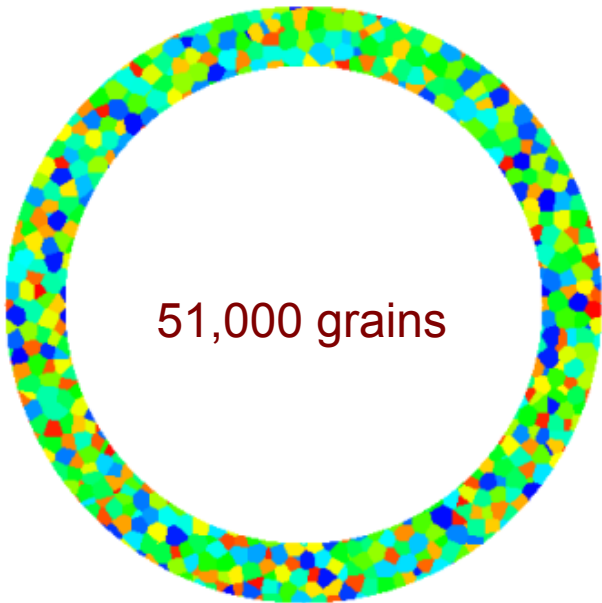
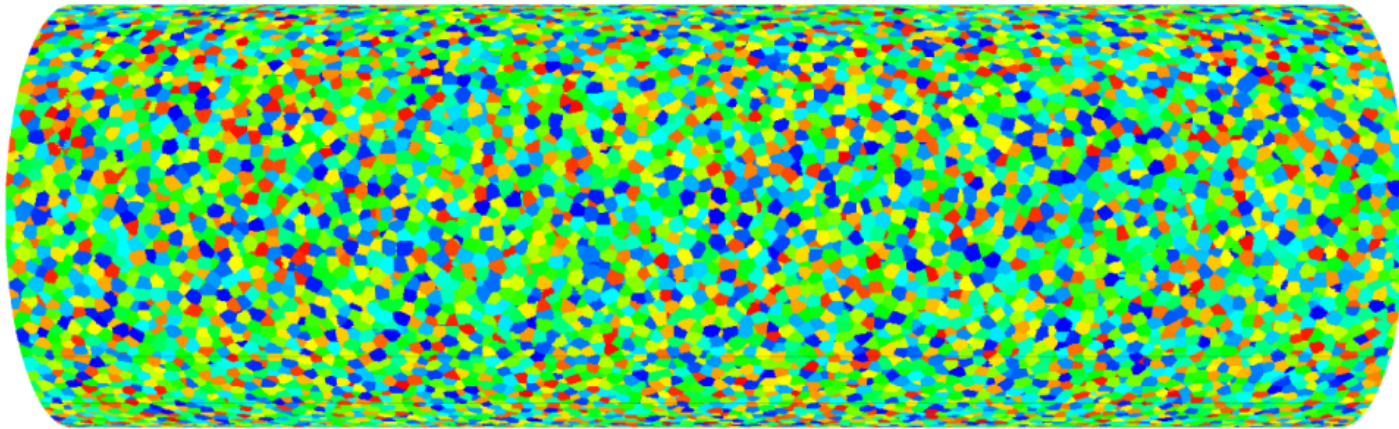
approximate displacement
field from simplified or
approximate material model

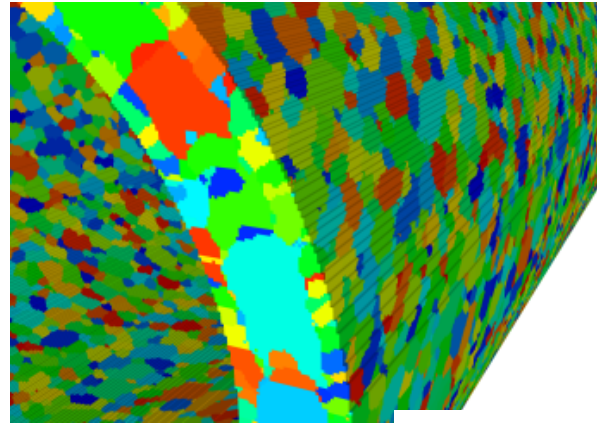
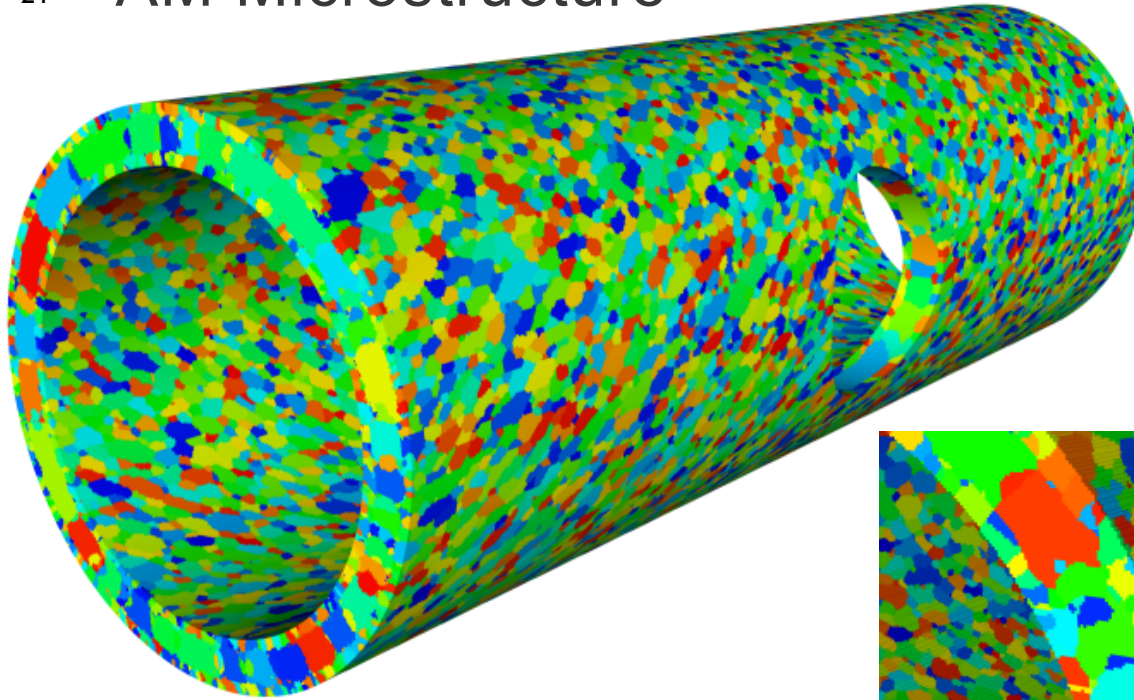
strain field resulting from
approx. stress field but true
material model

stress field resulting from
approx. strain field but true
material model

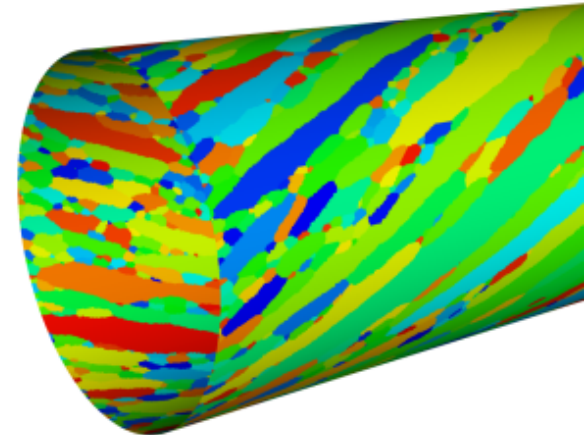
Key point: Can bound error using only known quantities from the approximate simulation. Don't need to run “true” model simulation.

Equiaxed microstructure



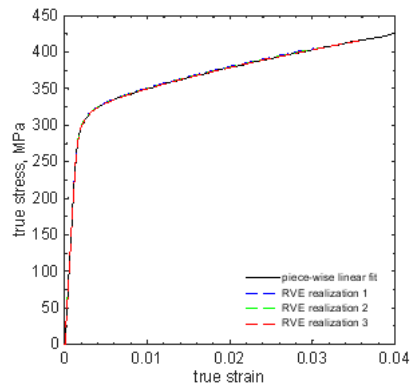
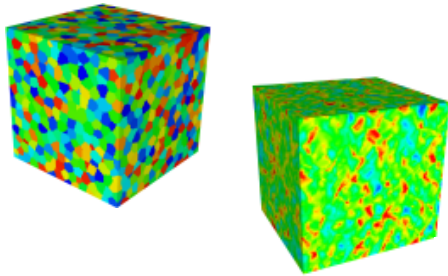


- KMC (SPPARKS) voxelated geometry
- 55M voxels
- two laser passes per layer (difference between surface and interior microstructure)
- map to conformal finite-element mesh
- 30M finite elements

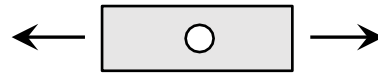




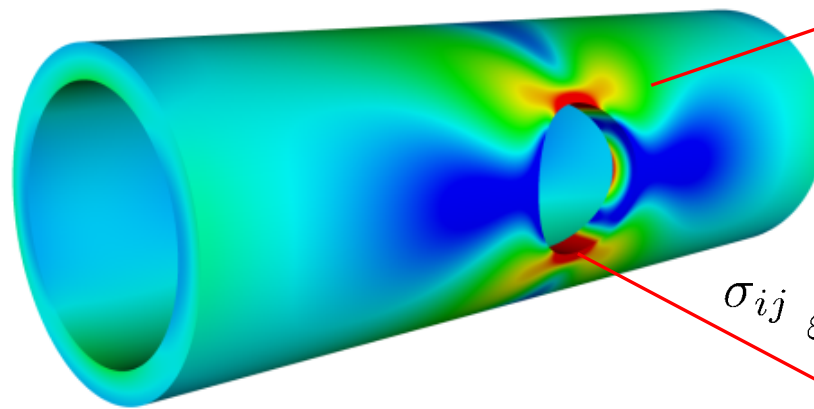
Homogenize Using
Crystal Plasticity
(filter fine scale)



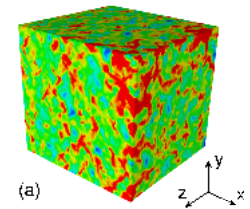
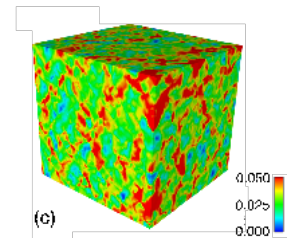
Macroscale simulation



$$\frac{\partial \mathbf{P}}{\partial \mathbf{X}} : \mathbf{I} + \rho_o \mathbf{b} = \rho_o \ddot{\mathbf{u}} \quad \text{in } \Omega$$



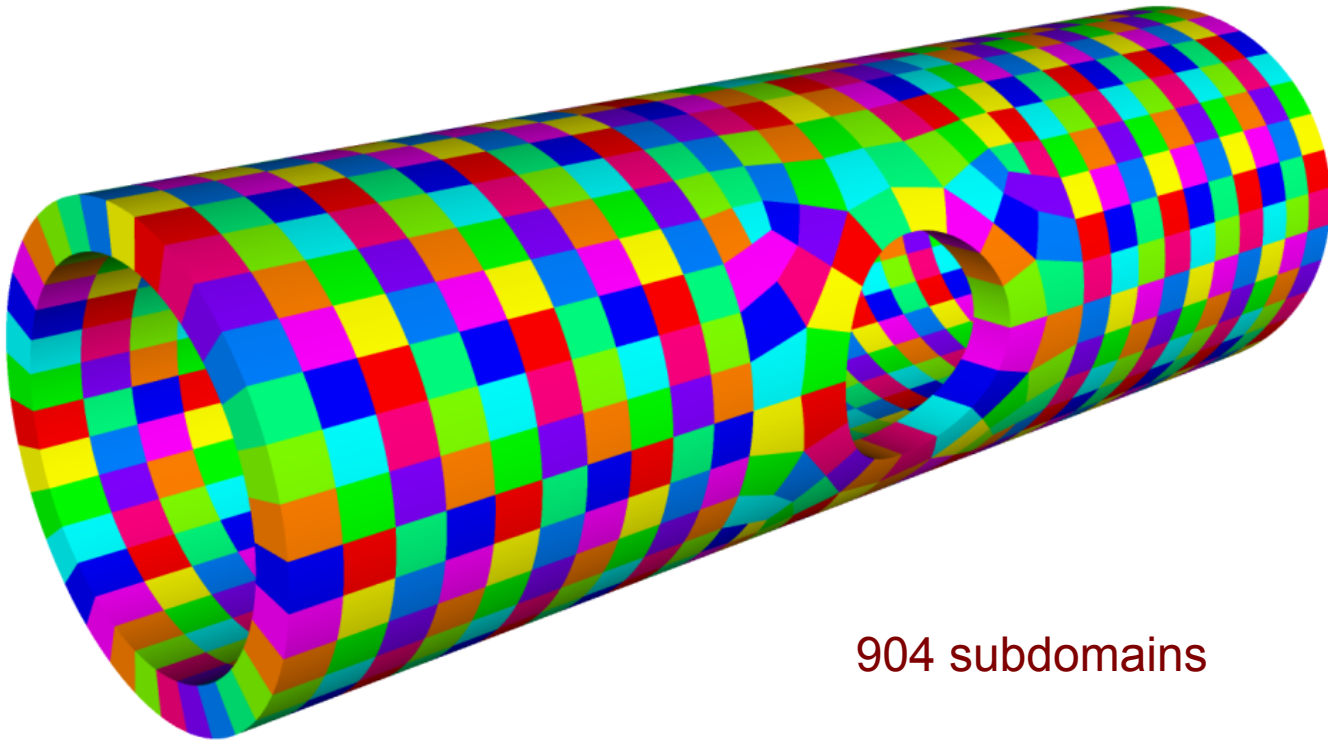
Localization
(recover fine scale)



Assumptions:

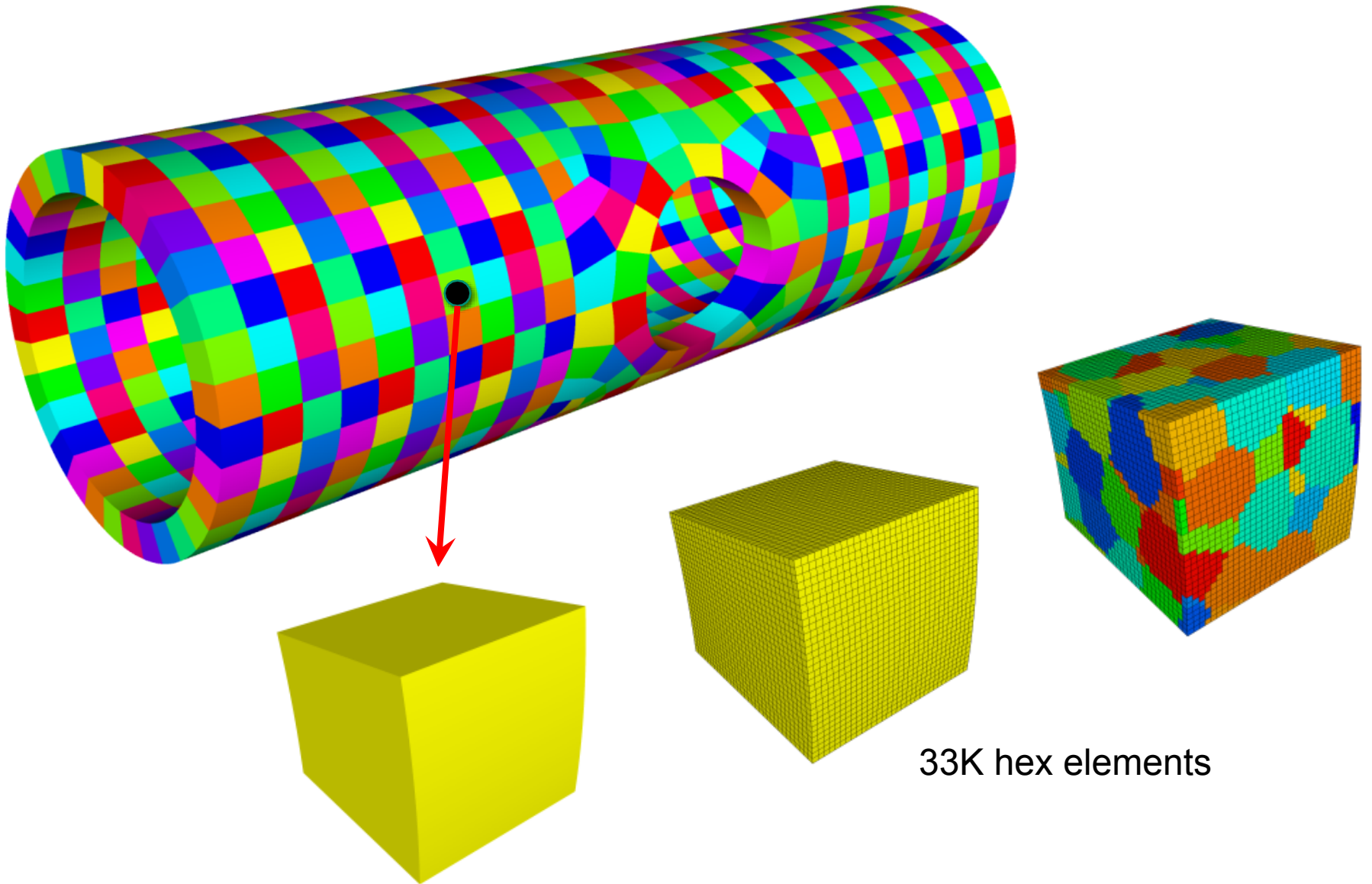
- scale separation
- RVE well defined
- no surface effects

First, partition structure into non-overlapping subdomains.



904 subdomains

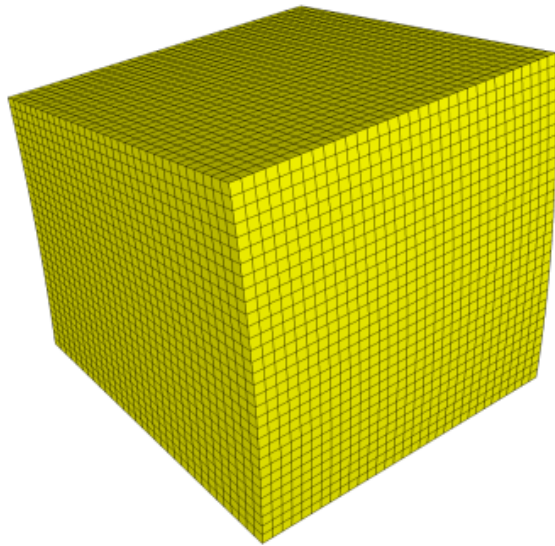
Type 1 localization



Type 1 localization

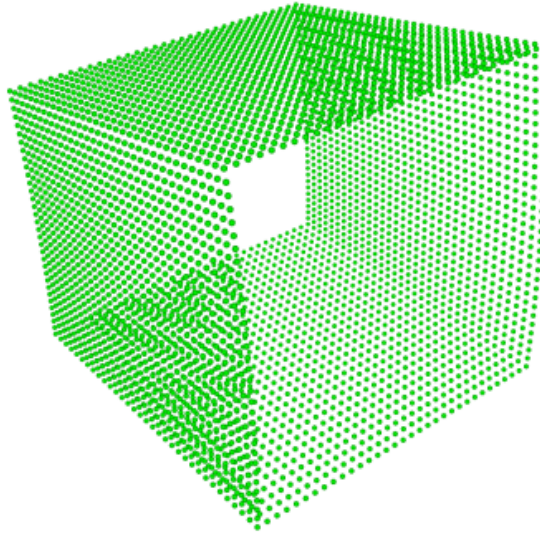


submodel

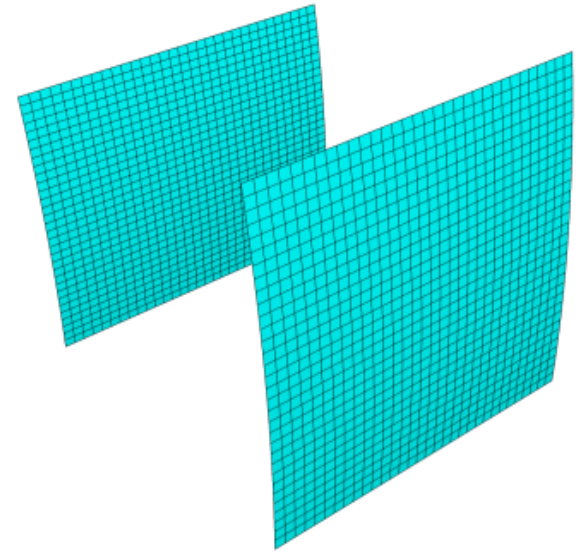


33K hex elements

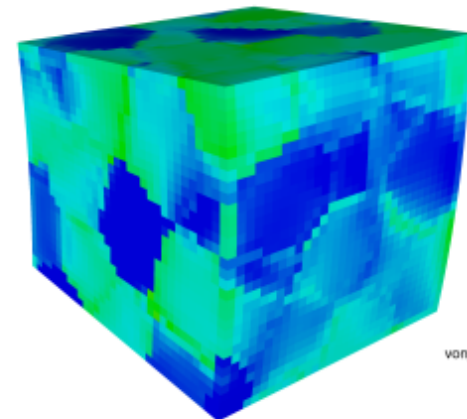
displacement b.c.s



traction b.c.s

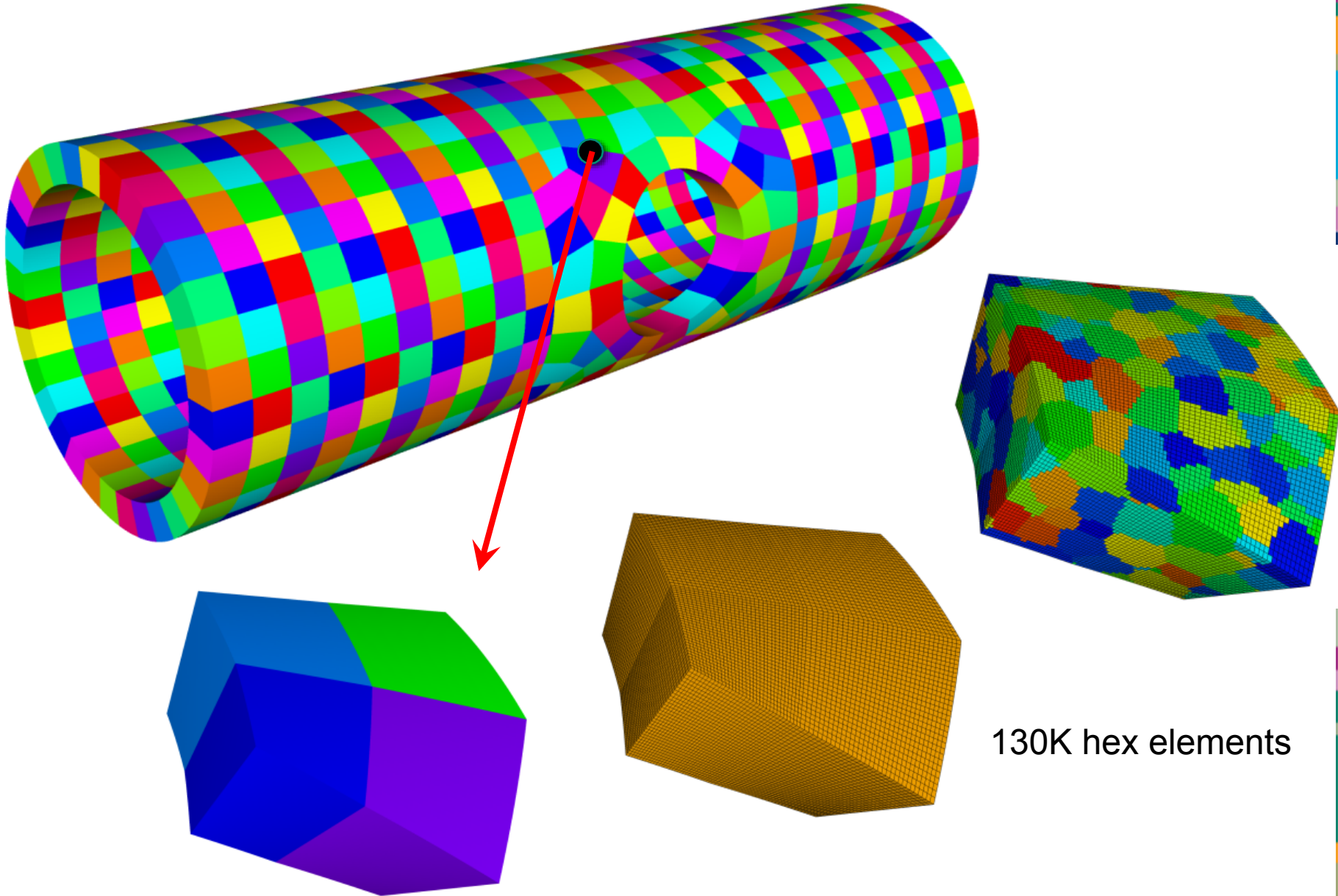


local stress field



von_mises_elem_avg
2.500e+00
2.000e+00
1.500e+00
1.000e+00
5.000e-01

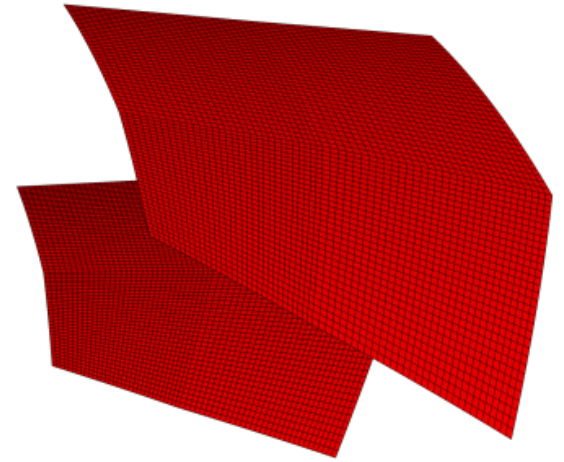
Type 2 localization (overlapping)



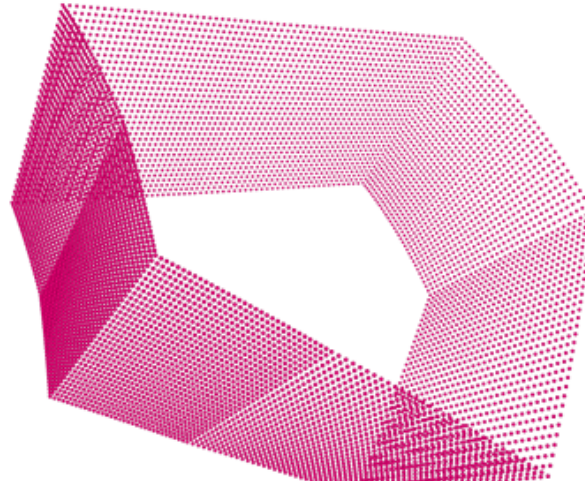
Type 2 localization



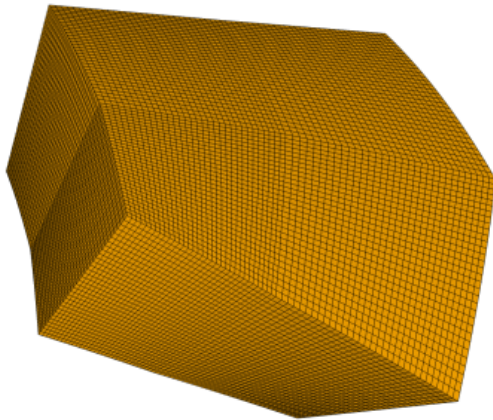
traction b.c.s



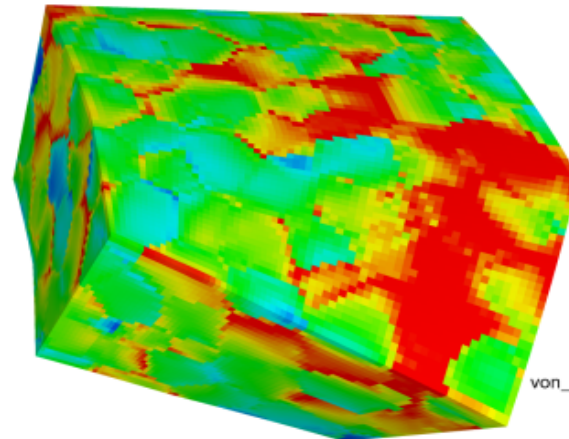
displacement b.c.s



submodel



local stress field



von_mises_elem_avg

2.500e+00
2.000e+00
1.500e+00
1.000e+00
5.000e-01

Localization results (equiaxed)

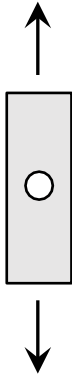
homogeneous
isotropic

type 1 projection

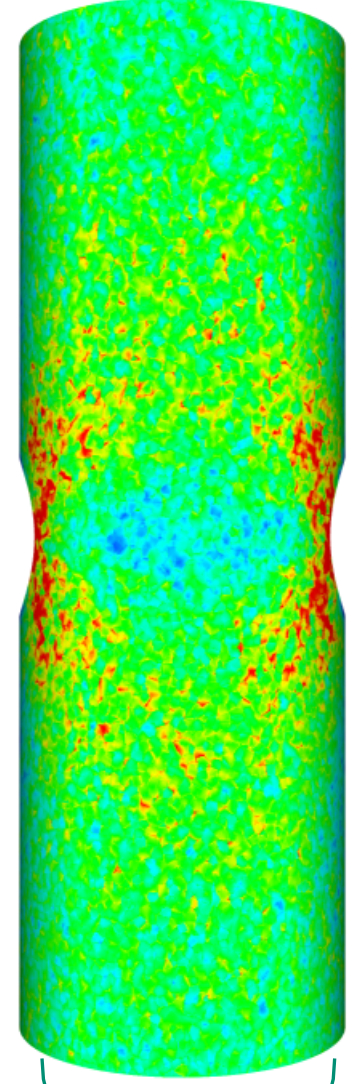
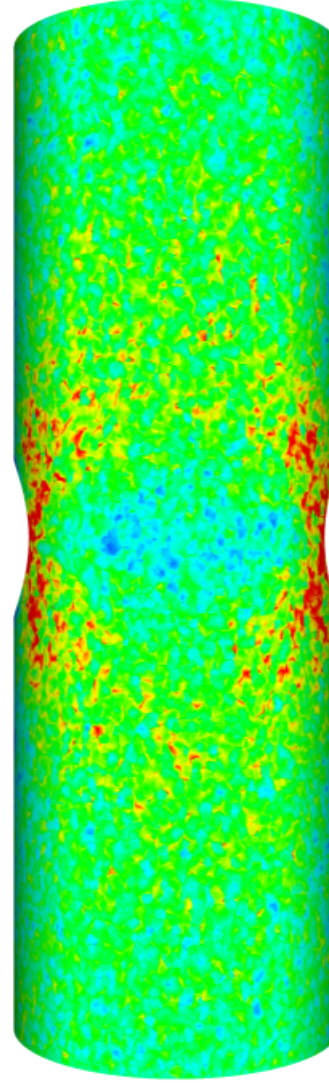
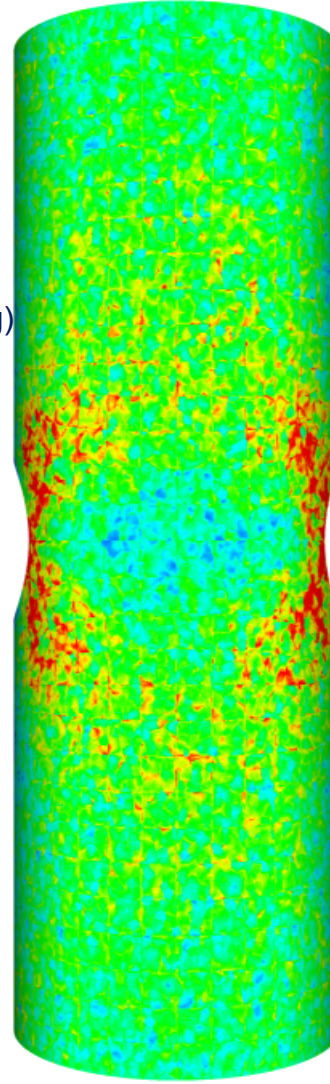
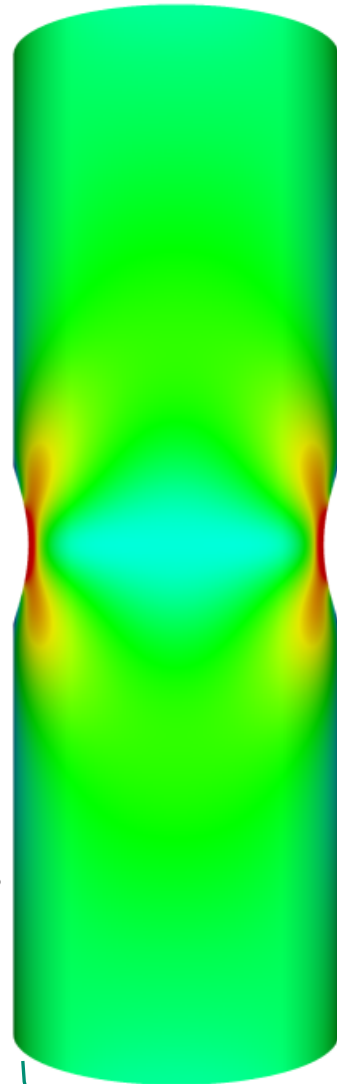
type 2 projection
(1 Schwarz iteration)

exact

Dirichlet
projection
(submodeling)



von Mises
400
200
0



Minutes

~4 days on 2048 cpus



Localization results (AM)



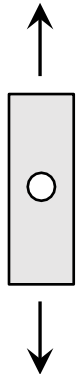
homogeneous
isotropic

type 1 projection

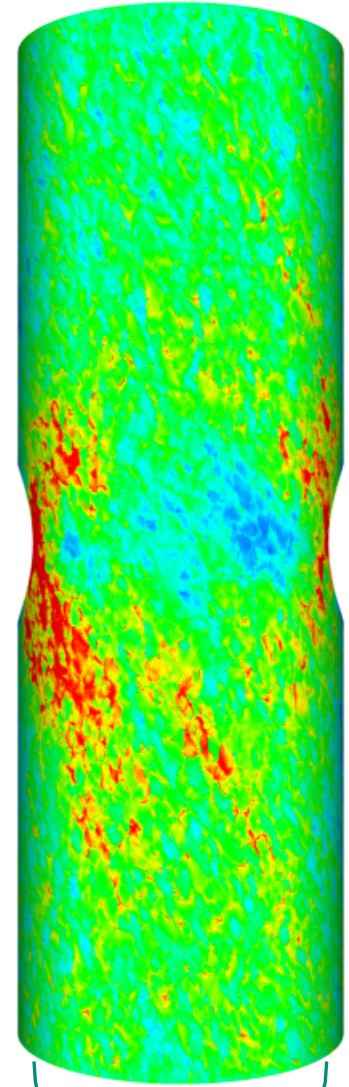
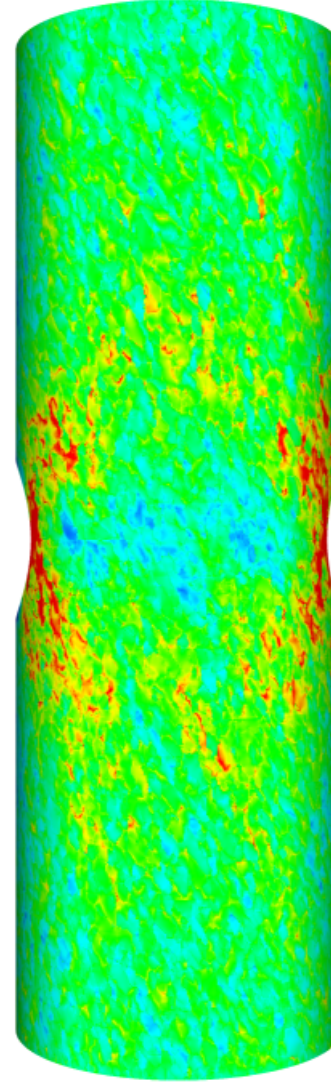
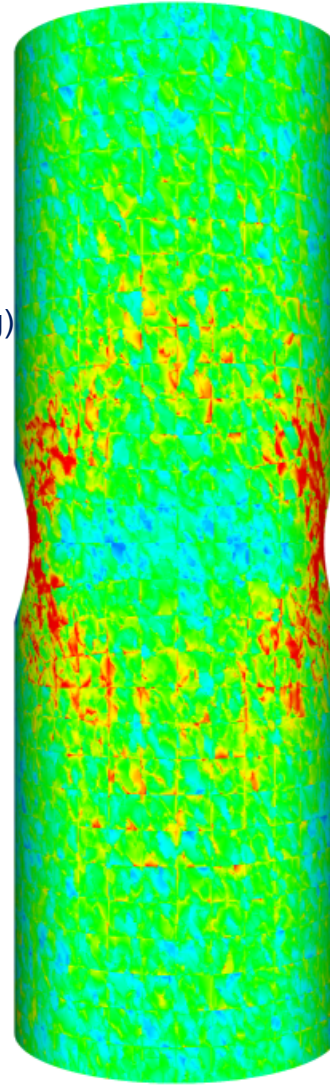
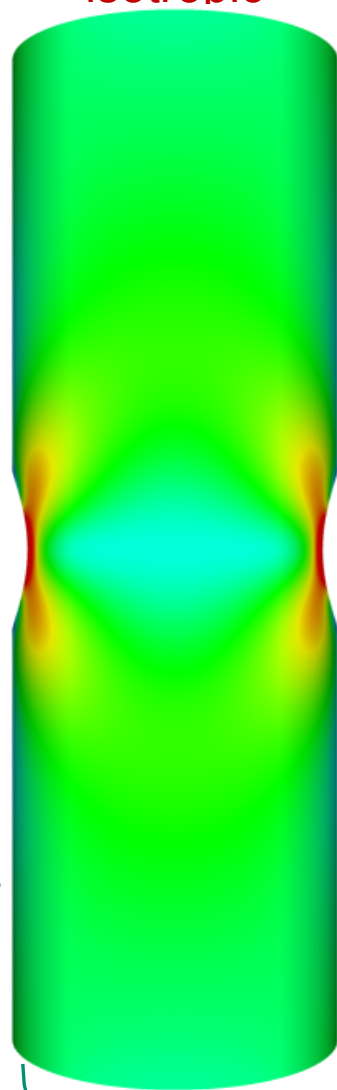
type 2 projection
(1 Schwarz iteration)

exact (DNS)

Dirichlet
projection
(submodeling)



von Mises
400
200
0



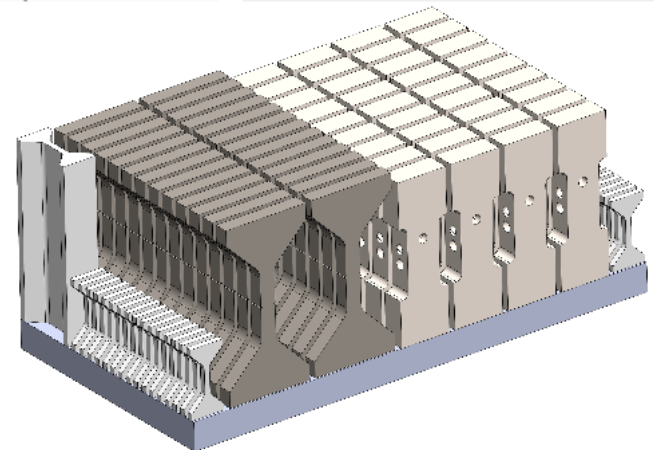
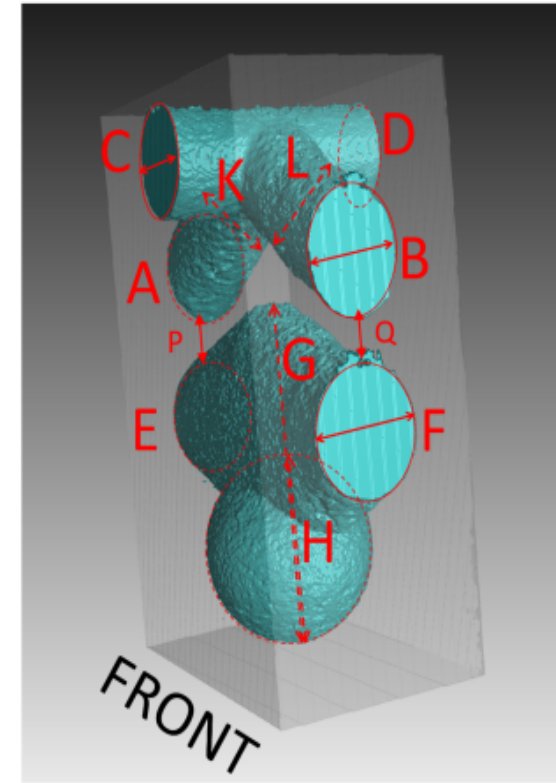
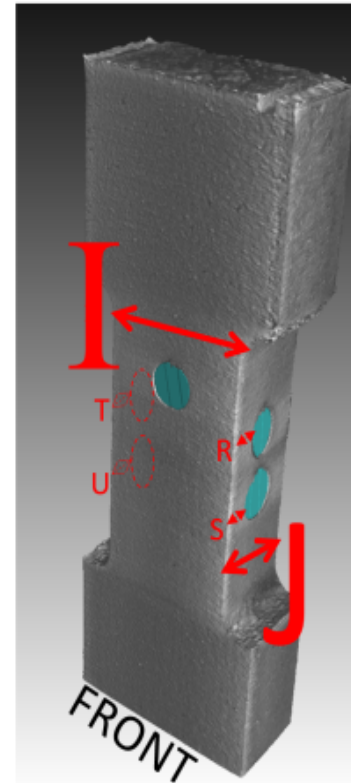
Minutes

~4 days on 2048 cpus

Sandia Fracture Challenge



- 316L Stainless Steel LPBF Part
- Complex geometry with internal channels and spherical cavity
- Loaded in tension
- Given CT data along with smooth tension and notched tension data
- Challenge Questions:
 - Force at four different displacements
 - Force and log strain at four points on front face
 - Total force-displacement curve
 - Force and log strain along four horizontal lines on front face
 - Images of front surface at crack initiation and complete failure
- 21 Participant Teams



Sandia/NM Predictive Approach



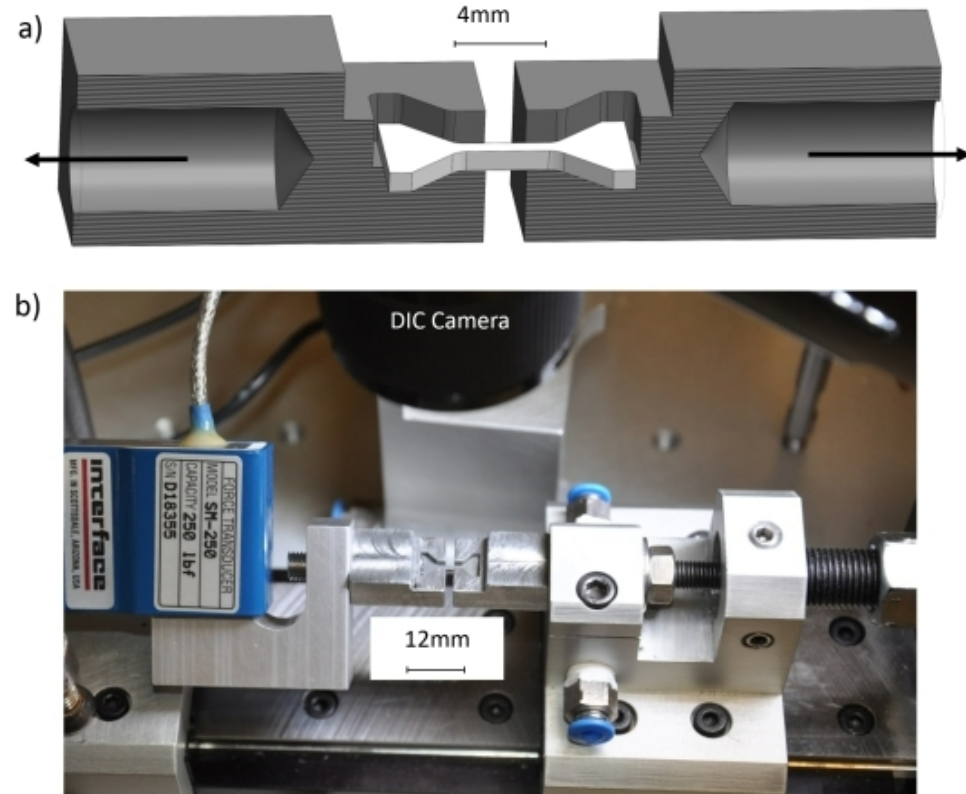
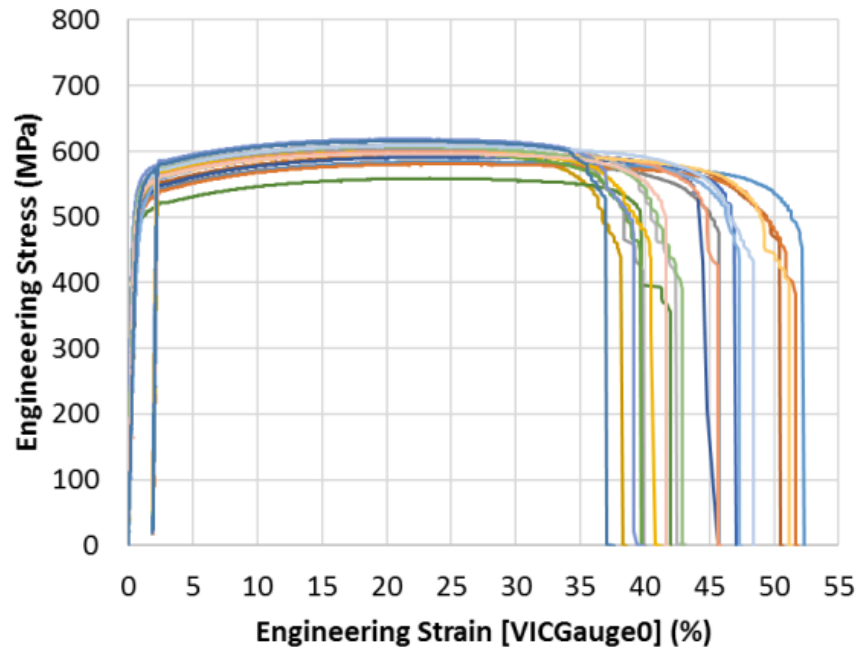
1. Fit robust plasticity model to calibration test data with porosity distributions as initial damage
2. Run many iterations of challenge geometry with many porosity distributions
3. Perform statistical analysis on results to enrich result distributions

SNL/NM Team Members: Kyle Johnson, John Emery, Kurtis Ford, Joe Bishop, Judy Brown, Chris Hammetter, Spencer Grange
Additional help from Kyle Karlson (SNL/CA)

Tension Data Was Taken Using High Throughput Test Method



Longitudinal Tensile Tests



a) Model of Additive Manufactured Tensile Specimen in grips (cut-away). b) Mechanical Test Set-up.
[Salzbrenner, *et.al*, JMPT 2017]



- Temperature and history-dependent viscoplastic internal state variable model
- Stress is dependent on damage ϕ and evolves according to

$$\dot{\sigma} = \left(\frac{\dot{E}}{E} - \frac{\dot{\phi}}{1 - \phi} \right) \sigma + E(1 - \phi)(\dot{\epsilon} - \dot{\epsilon}_p)$$

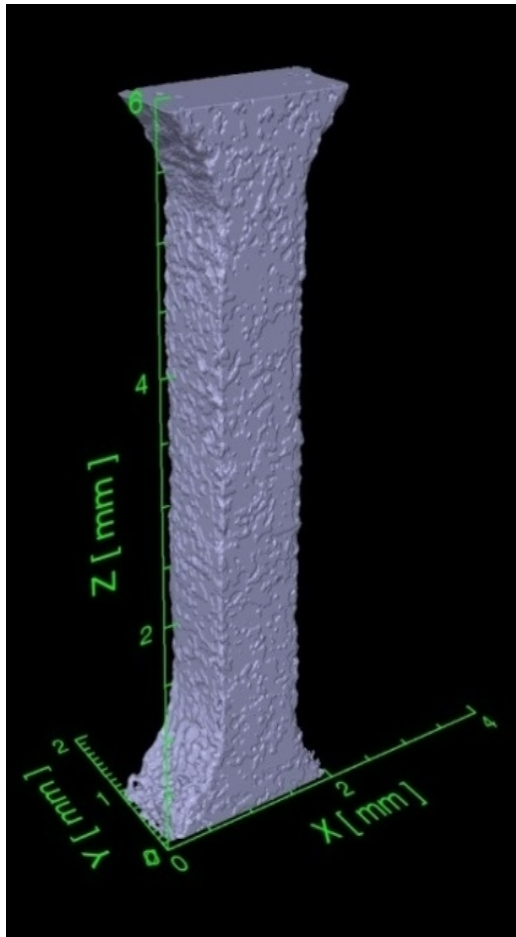
- Flow rule includes yield stress and internal state variables for hardening and damage

$$\dot{\epsilon}_p = f \sinh^n \left(\frac{\frac{\sigma_e}{1 - \phi} - \kappa}{Y} - 1 \right)$$

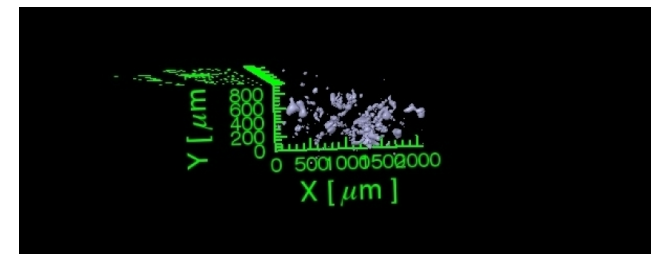
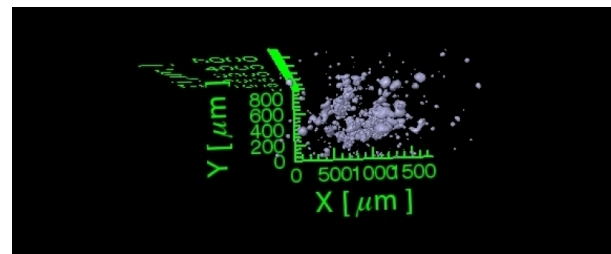
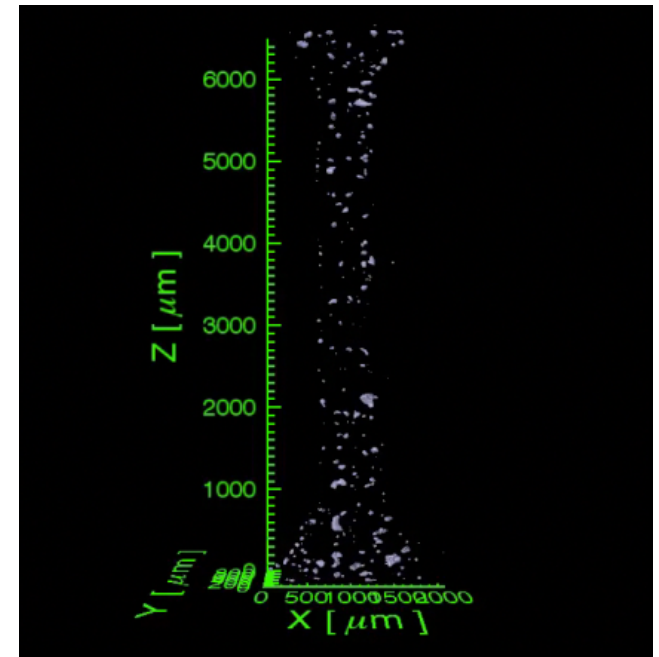
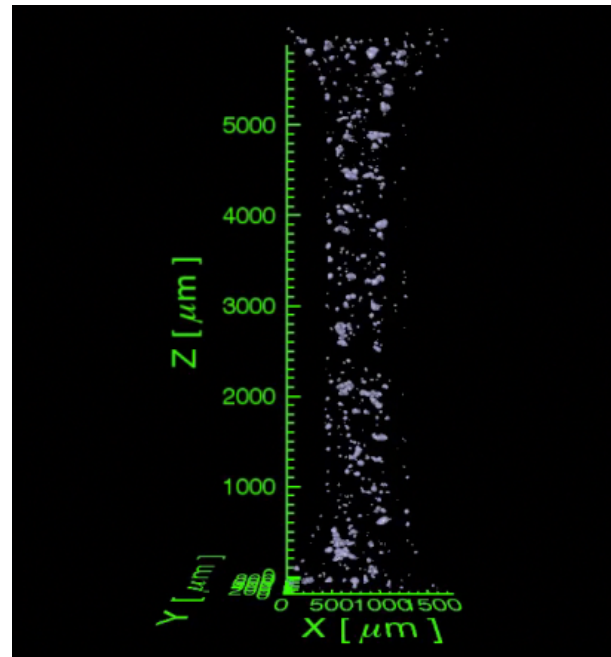
- The isotropic hardening variable κ evolves in a hardening minus recovery form.

$$\dot{\kappa} = \kappa \frac{\dot{\mu}}{\mu} + (H(\theta) - R_d(\theta)\kappa)\dot{\epsilon}_p$$

3D Reconstruction & Characterization of Pore Defects

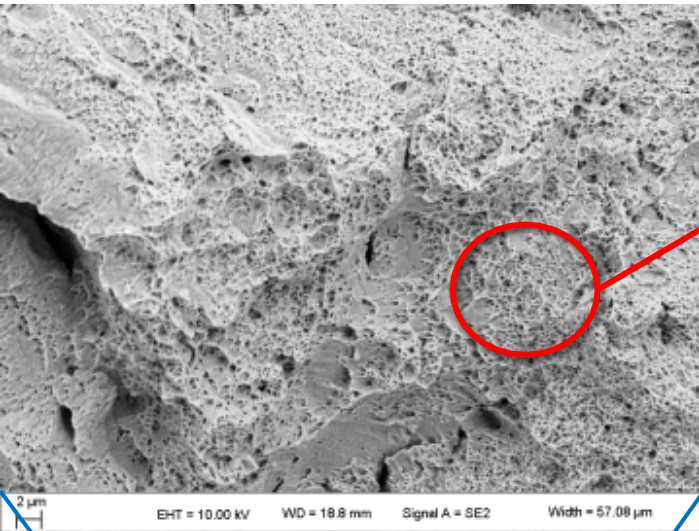


3D μ CT surface render



3D μ CT internal porosity

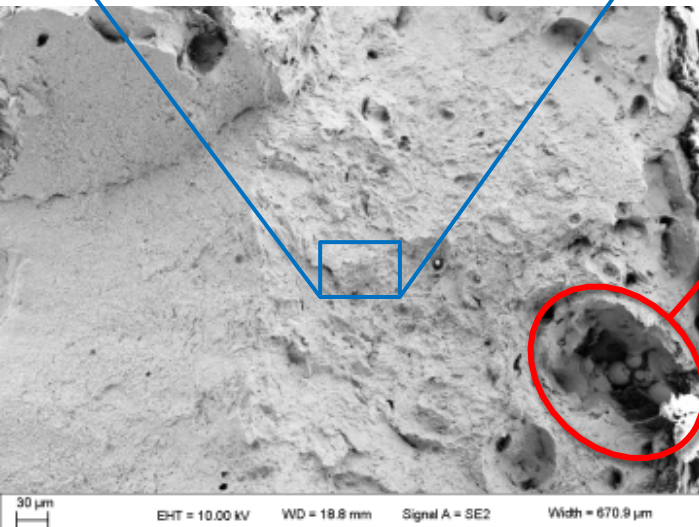
Tremendous variation in pore content from sample to sample
Pore locations reminiscent of AM laser raster pattern



Void Nucleation

Fine scale voids ($< 1\mu\text{m}$) indicate nucleation

$$\dot{\eta} = \eta \dot{\epsilon}_p \left(N_1 \left[\frac{4}{27} - \frac{J_3^2}{J_2^3} \right] + N_2 \frac{J_3}{J_2^3} + N_3 \frac{\langle p \rangle}{\sigma_e} \right)$$

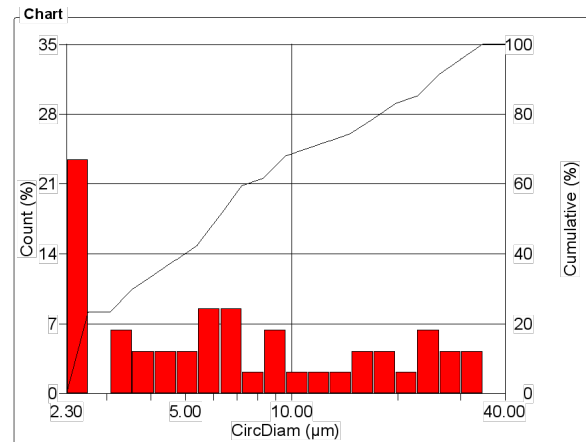
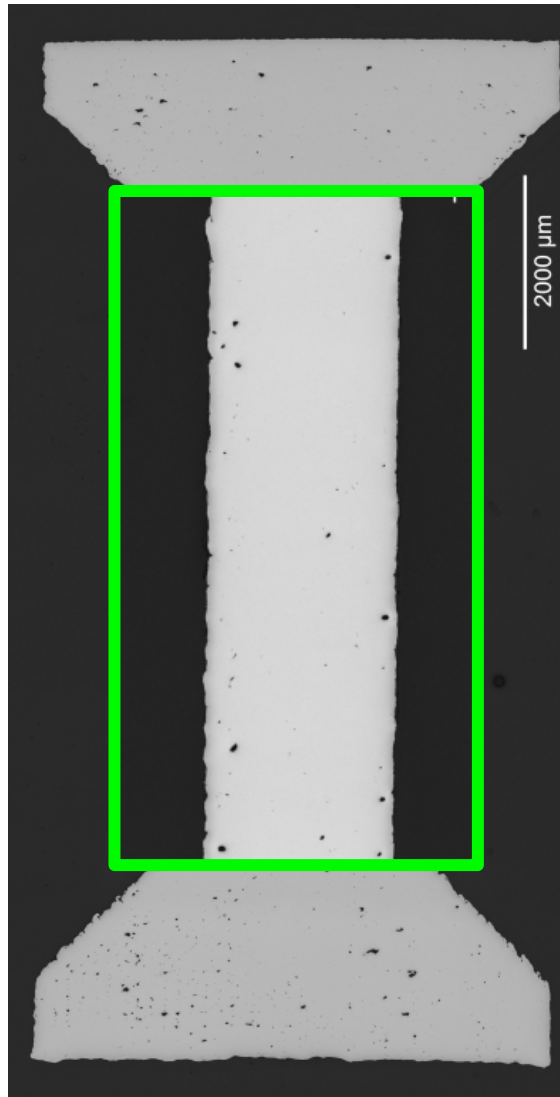


Void Growth

Pre-existing voids captured by void growth

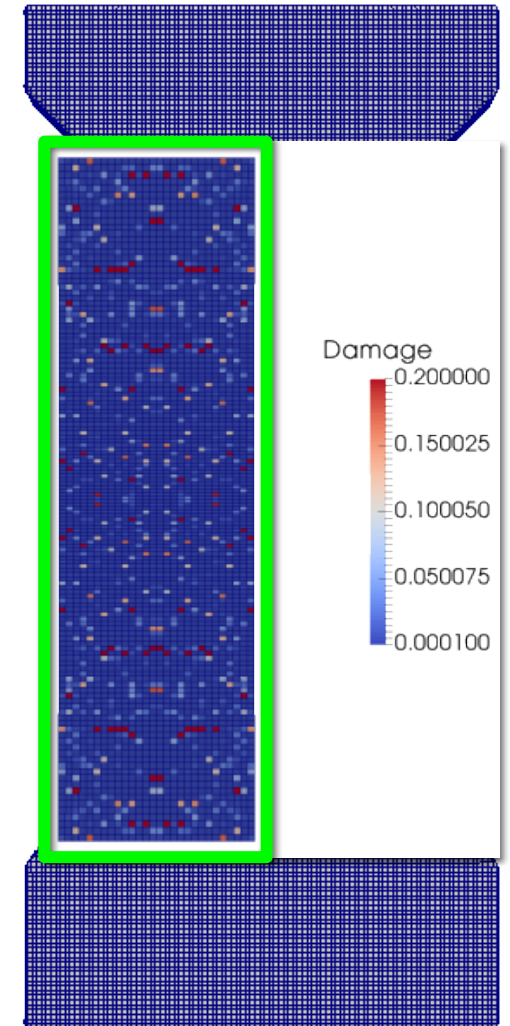
$$\dot{\phi} = \sqrt{\frac{2}{3}} \dot{\epsilon}_p \frac{1 - (1 - \phi)^{m+1}}{(1 - \phi)^m} \sinh \left[\frac{2(2m - 1)}{2m + 1} \frac{\langle p \rangle}{\sigma_e} \right]$$

Porosity Distribution Directly Mapped to Mesh

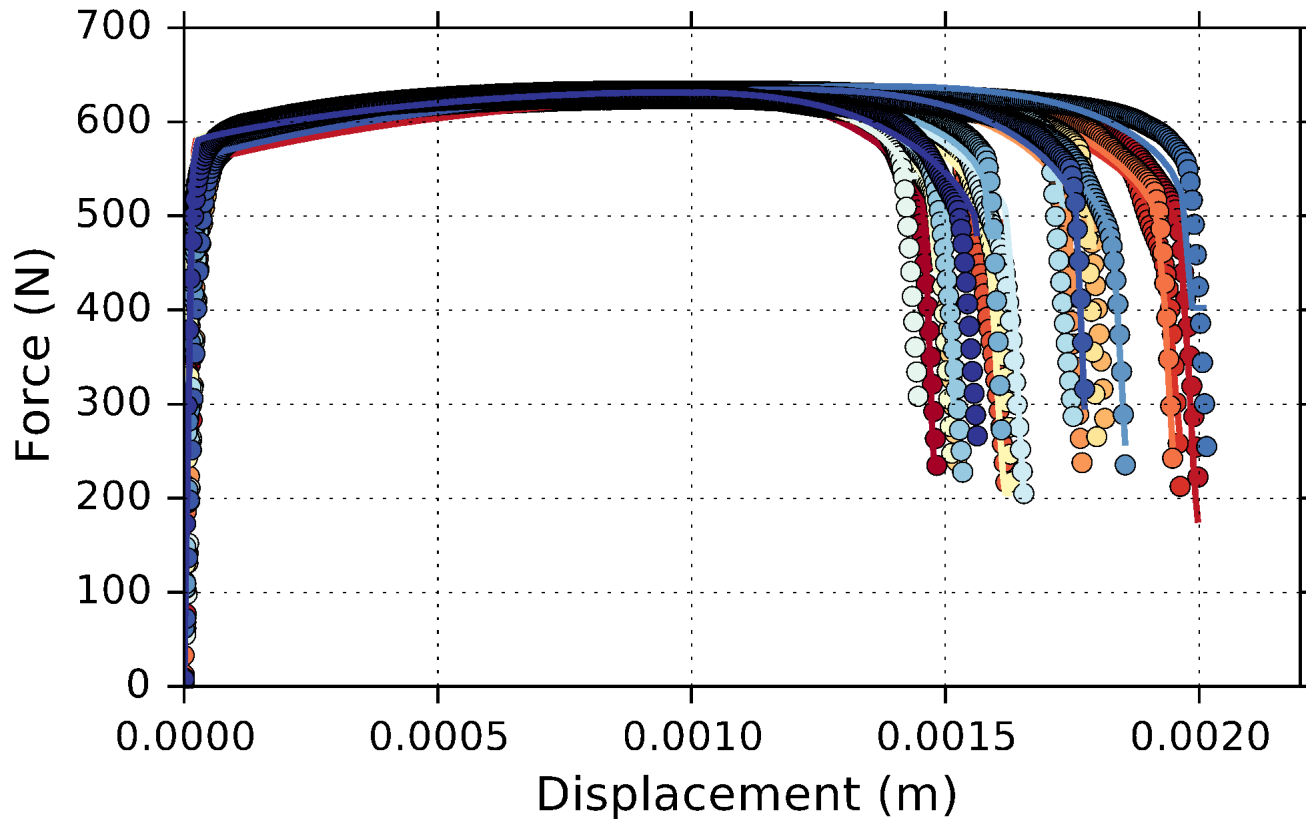


Porosity Mapping

x, y, z, r_{pore}

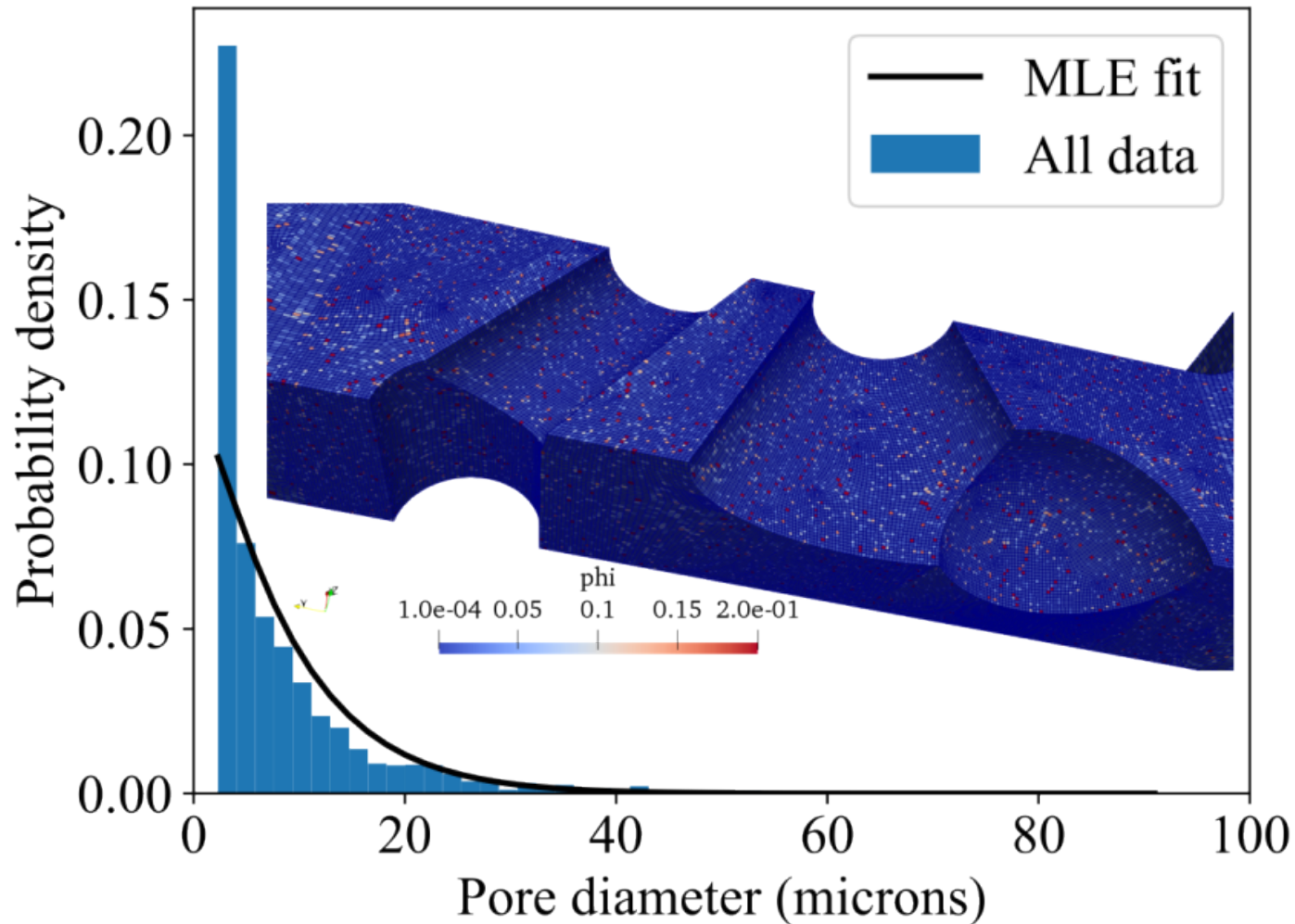


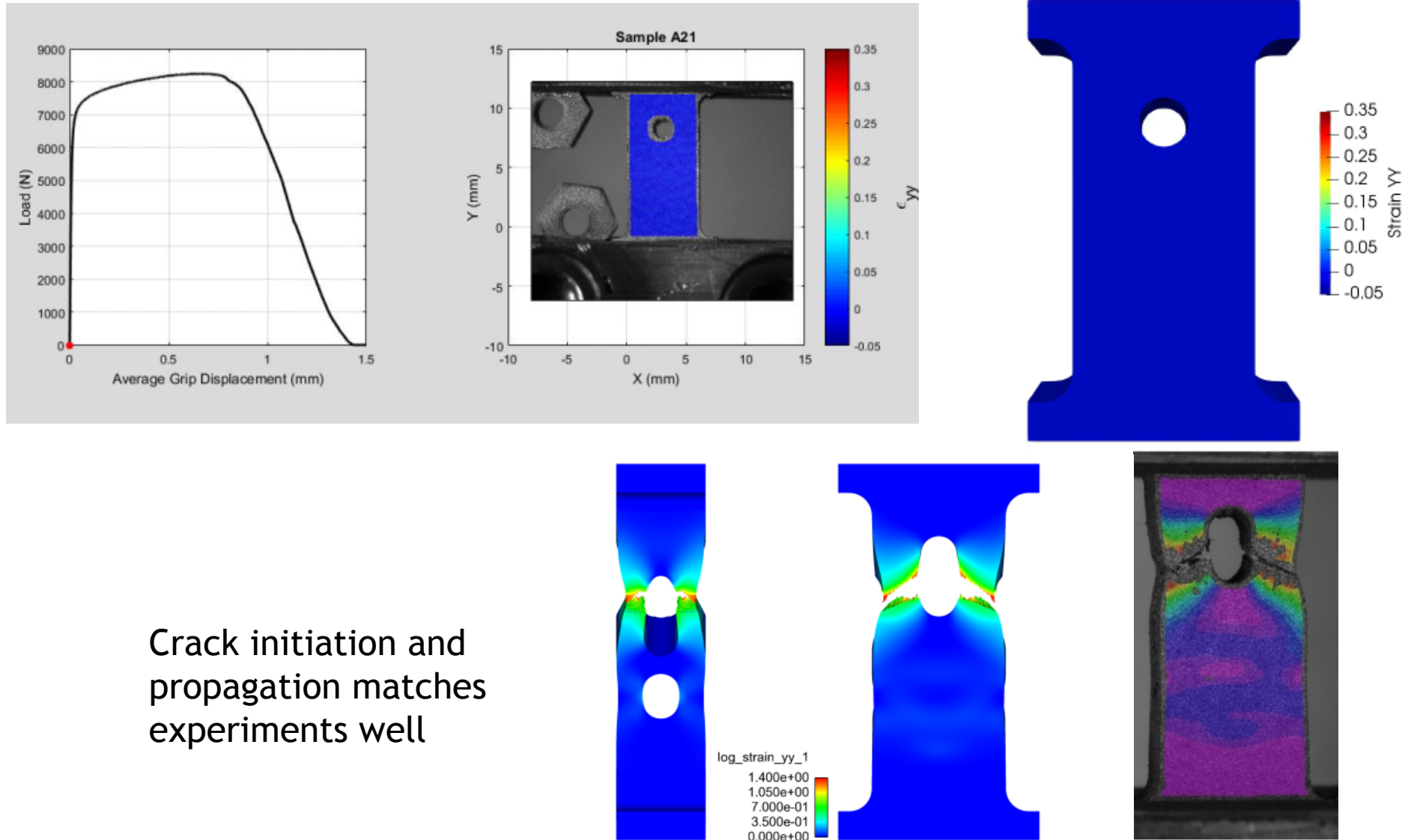
Calibration Results With Void Growth and Nucleation



- Each test has unique parameter set

Porosity Distribution Directly Mapped to Challenge Geometry

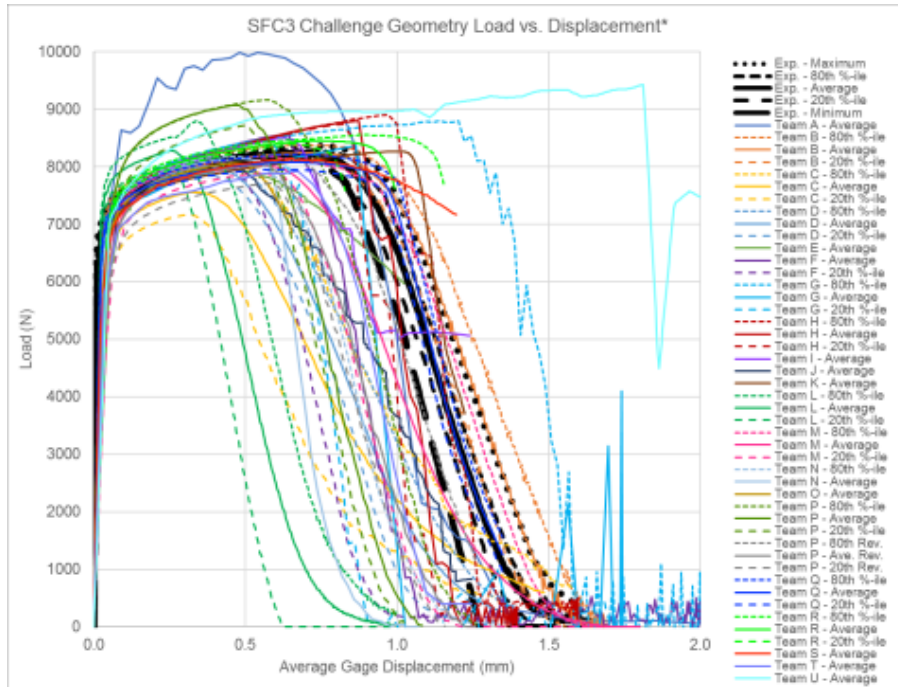




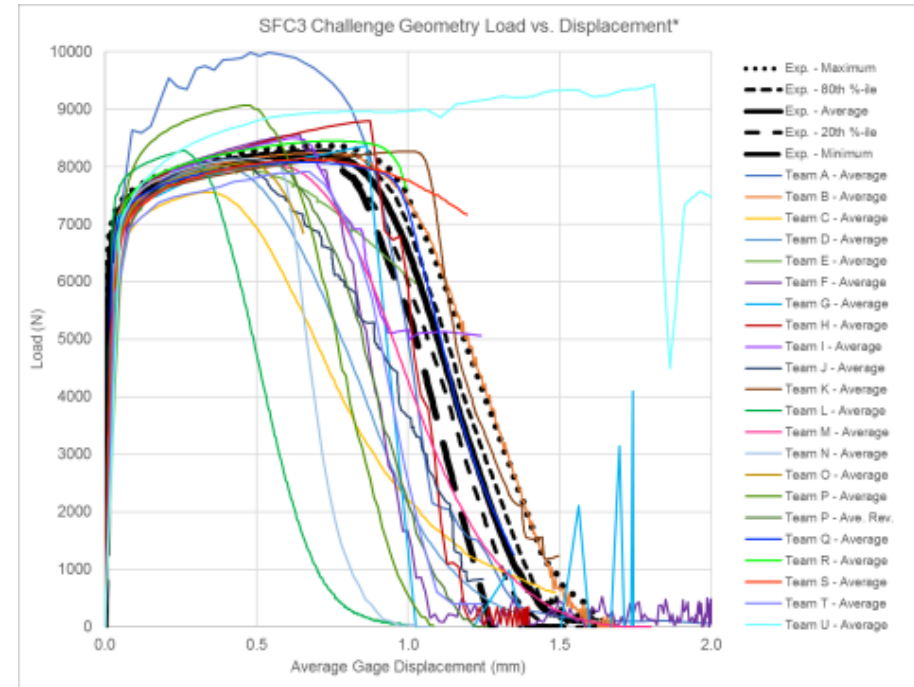
21 Participant Predictions Covered A Wide Range of Responses



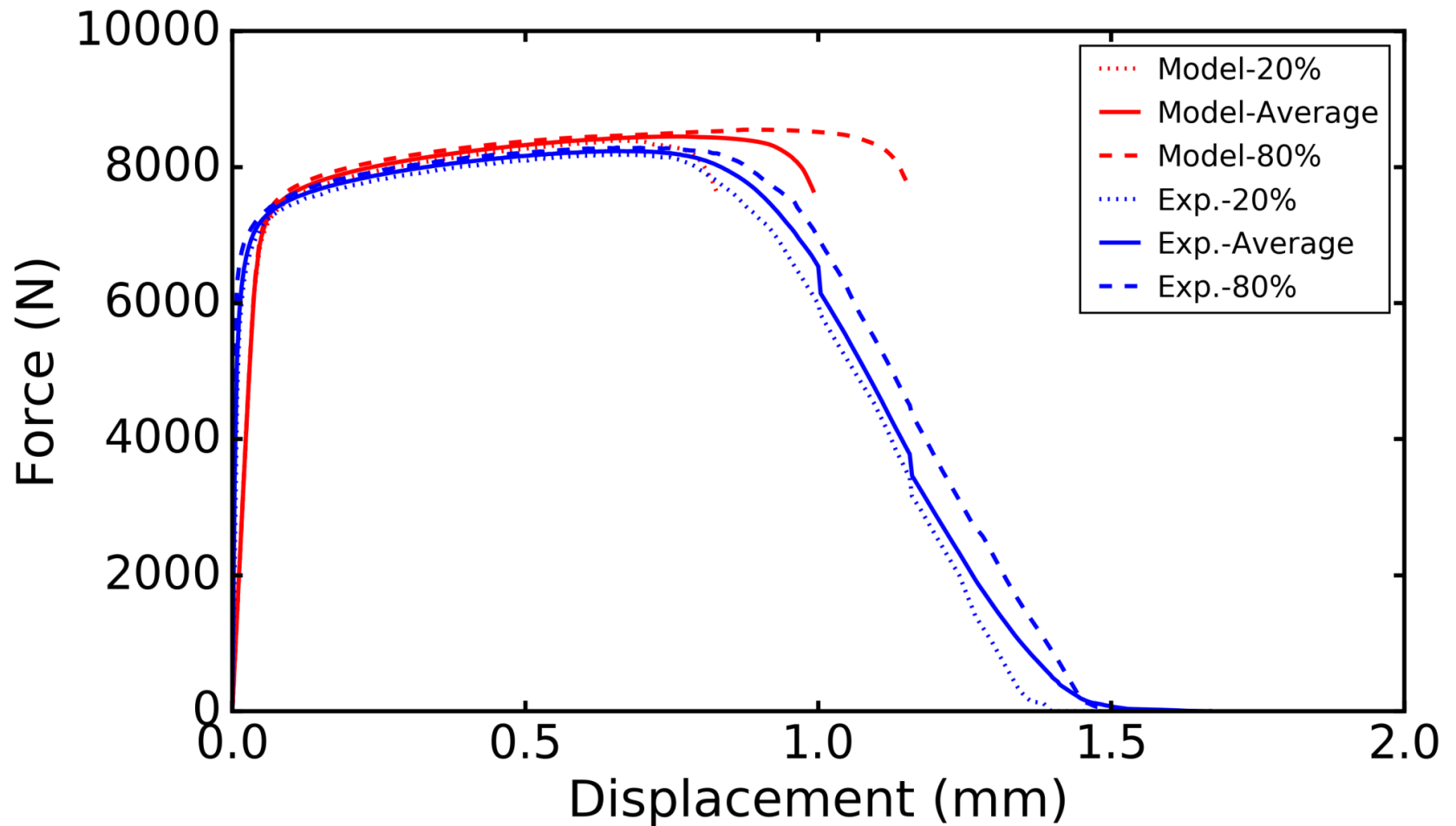
21 Predictions and Bounds with Exp. Average and Bounds



21 Nominal Predictions with Exp. Average and Bounds



Blind Predictions of Force-Displacement Curves Compare Reasonably Well With Experiments



Summary



- Process models offer insight into phenomena such as melt pool dynamics, thermal histories, and residual stress
- Microstructure prediction using SPPARKS code has been performed at several different length scales and AM processes
- Texture prediction is being incorporated
- Initial approaches of coupling microstructure to continuum models show importance of microstructure consideration
- Investigating use of a posteriori error estimation techniques for quantifying homogenization errors and other model-form errors
- Continuum scale modeling of AM part performance compared well in blind predictions
- Porosity can be accounted for using a damage formulation