

3D Characterization of the Columnar-to-Equiaxed Transition in Additively Manufactured Inconel 718

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Outline

- Background
- Three-dimensional Characterization
- Calibrating a Microstructure-Processing Map
- Summary

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Additive manufacturing (AM) provides enormous flexibility in design

Aerospace



Images courtesy Fraunhofer IWU, Lawrence Livermore National Lab, EOS, Added Scientific, and Imperial Machine & Tool Co.

Additive manufacturing (AM) provides enormous flexibility in design

Aerospace



Biomedical



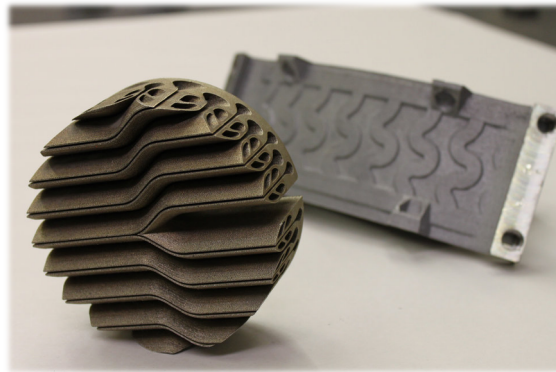
Images courtesy Fraunhofer IWU, Lawrence Livermore National Lab, EOS, Added Scientific, and Imperial Machine & Tool Co.

Additive manufacturing (AM) provides enormous flexibility in design

Aerospace



Industrial



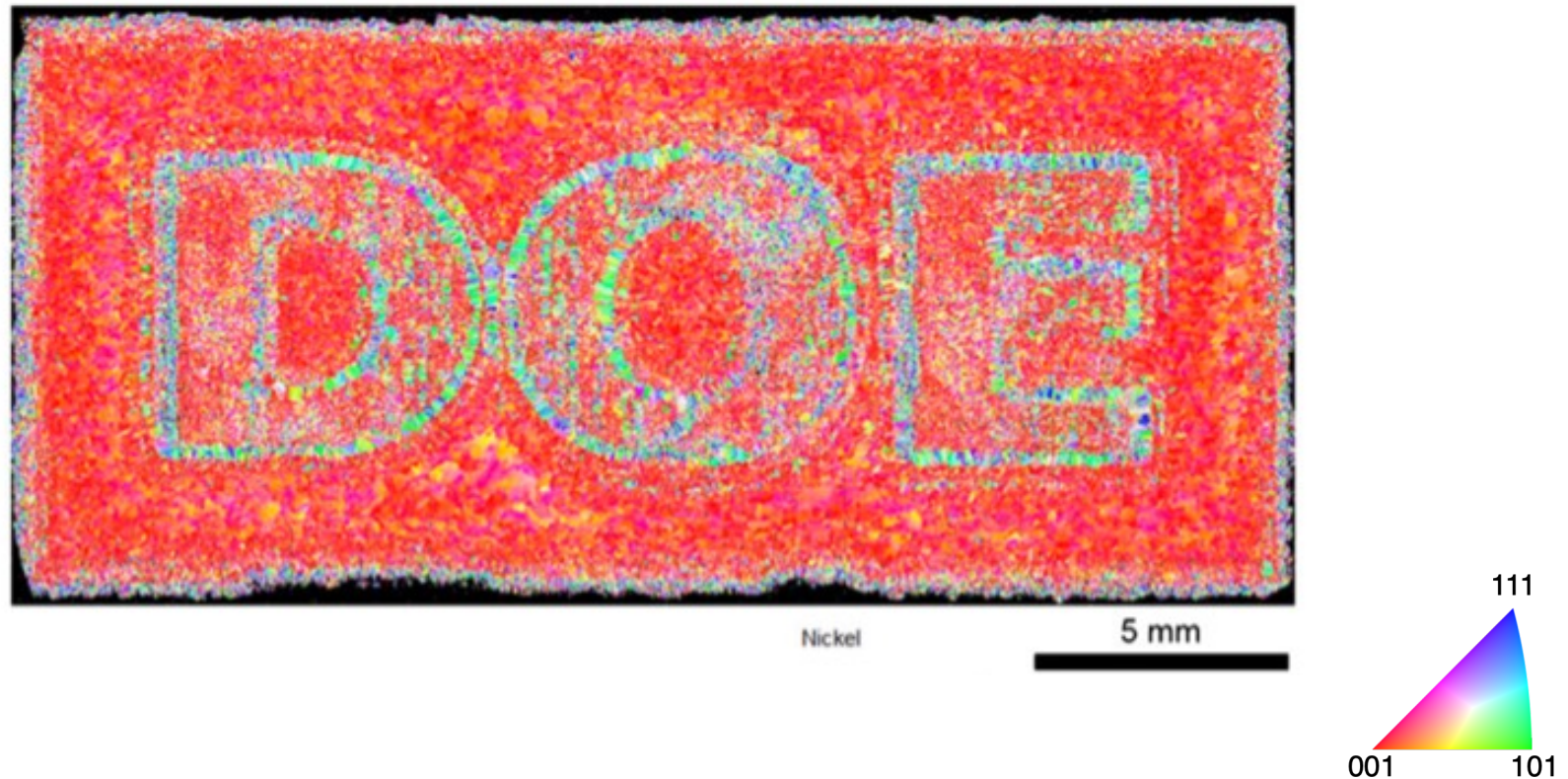
Biomedical



Images courtesy Fraunhofer IWU, Lawrence Livermore National Lab, EOS, Added Scientific, and Imperial Machine & Tool Co.

Scan strategy can be manipulated for site-specific microstructure

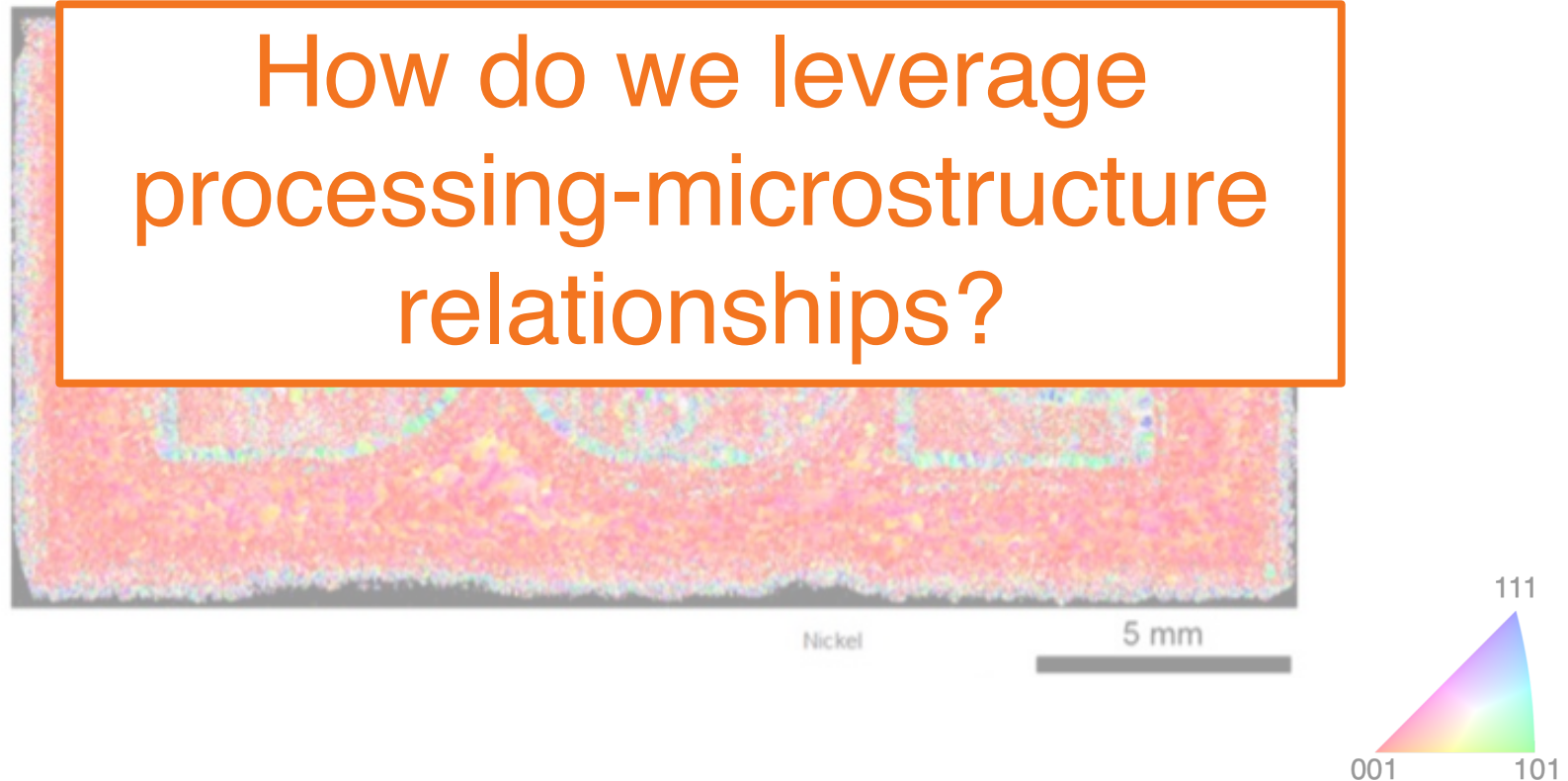
- Founded in parametric studies that are not easily generalizable to complex geometries



Scan strategy can be manipulated for site-specific microstructure

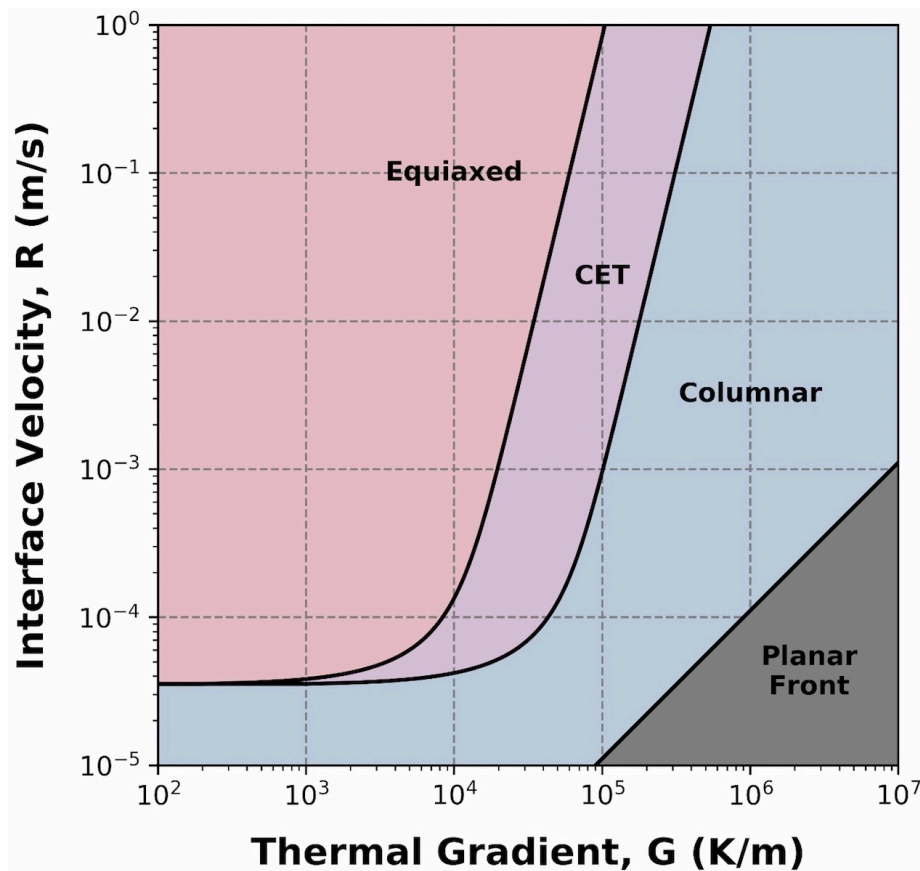
- Founded in parametric studies that are not easily generalizable to complex geometries

How do we leverage processing-microstructure relationships?



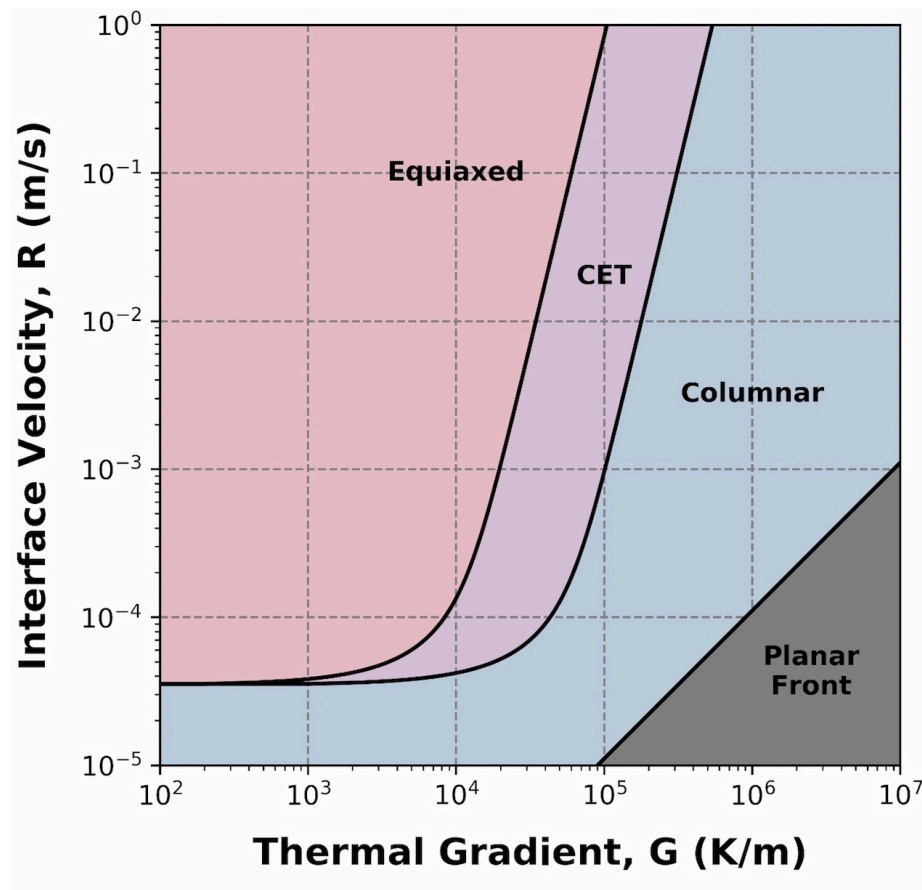
Local microstructure control relies on understanding solidification conditions

- Processing maps help predict microstructure

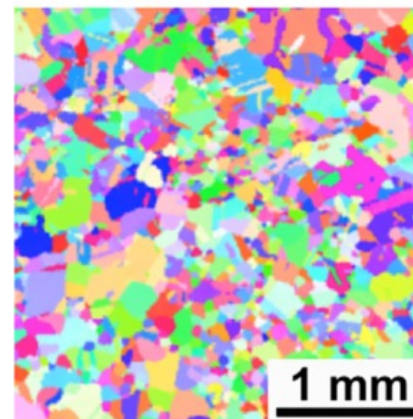


Local microstructure control relies on understanding solidification conditions

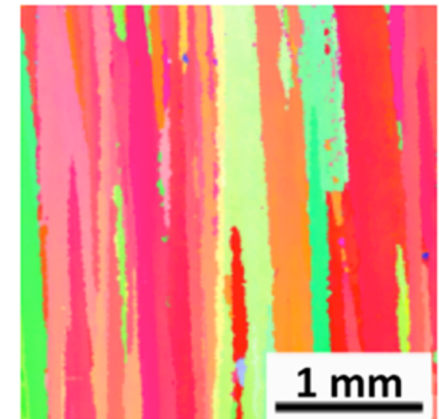
- Processing maps help predict microstructure



Equiaxed

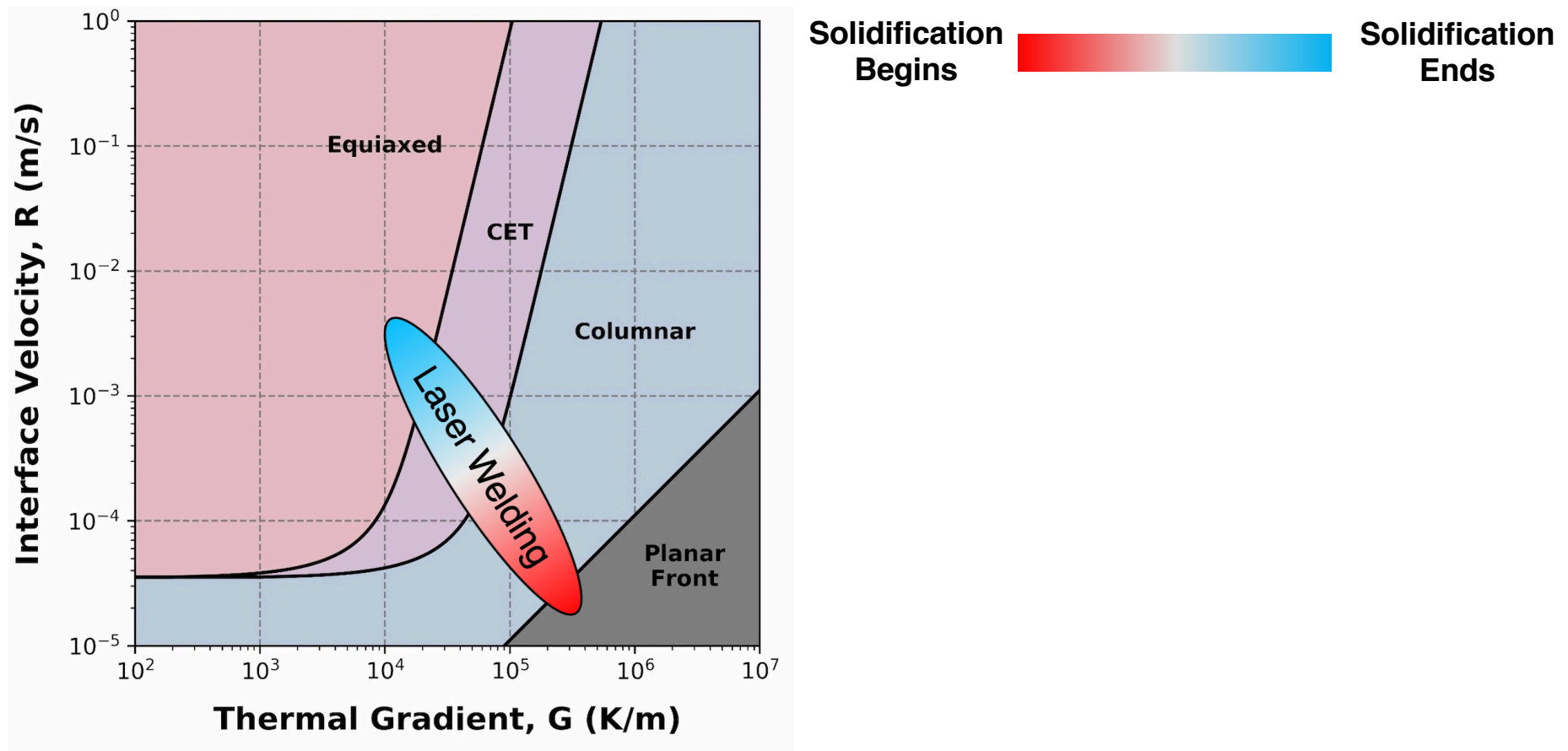


Columnar



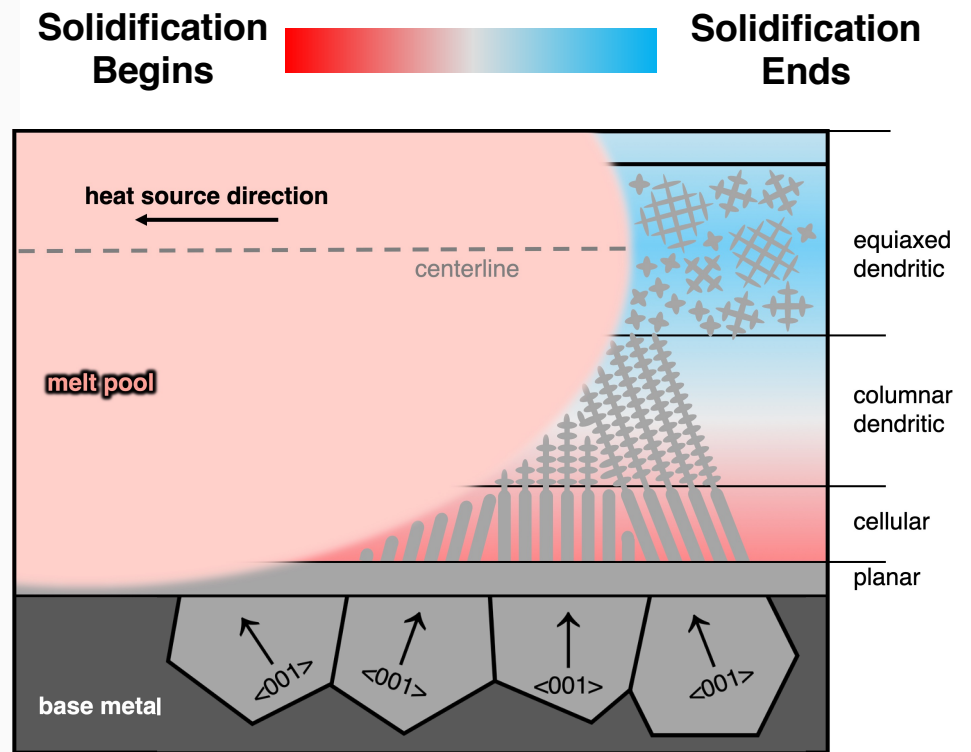
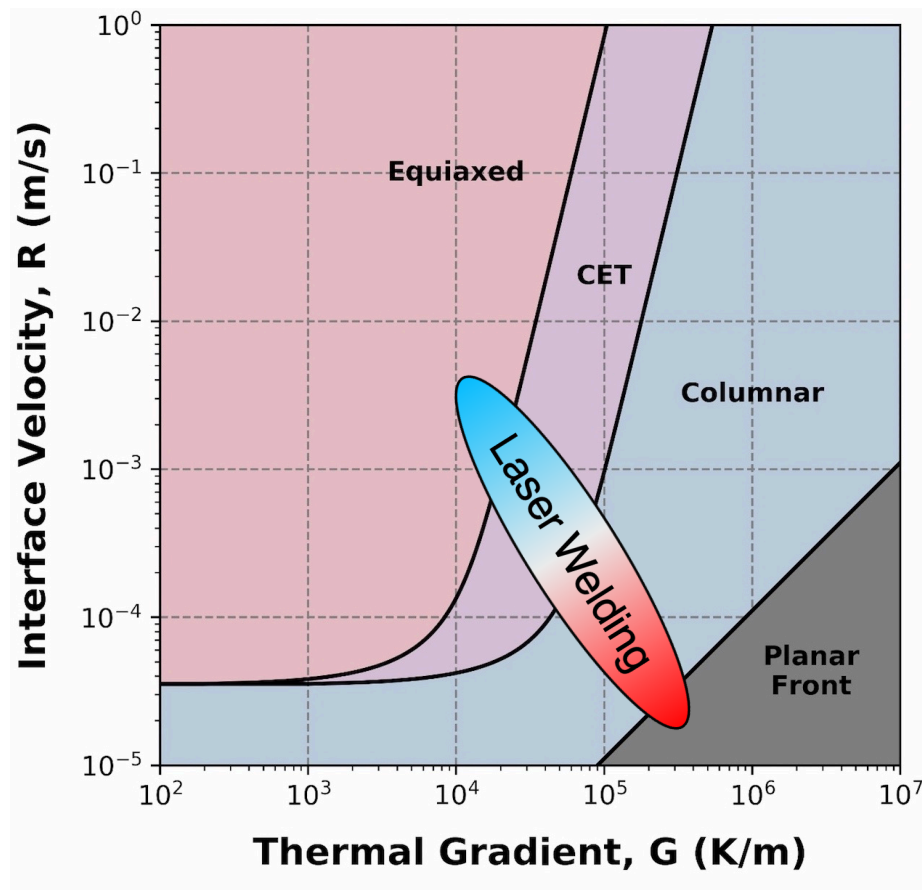
Local microstructure control relies on understanding solidification conditions

- Solidification conditions are not static



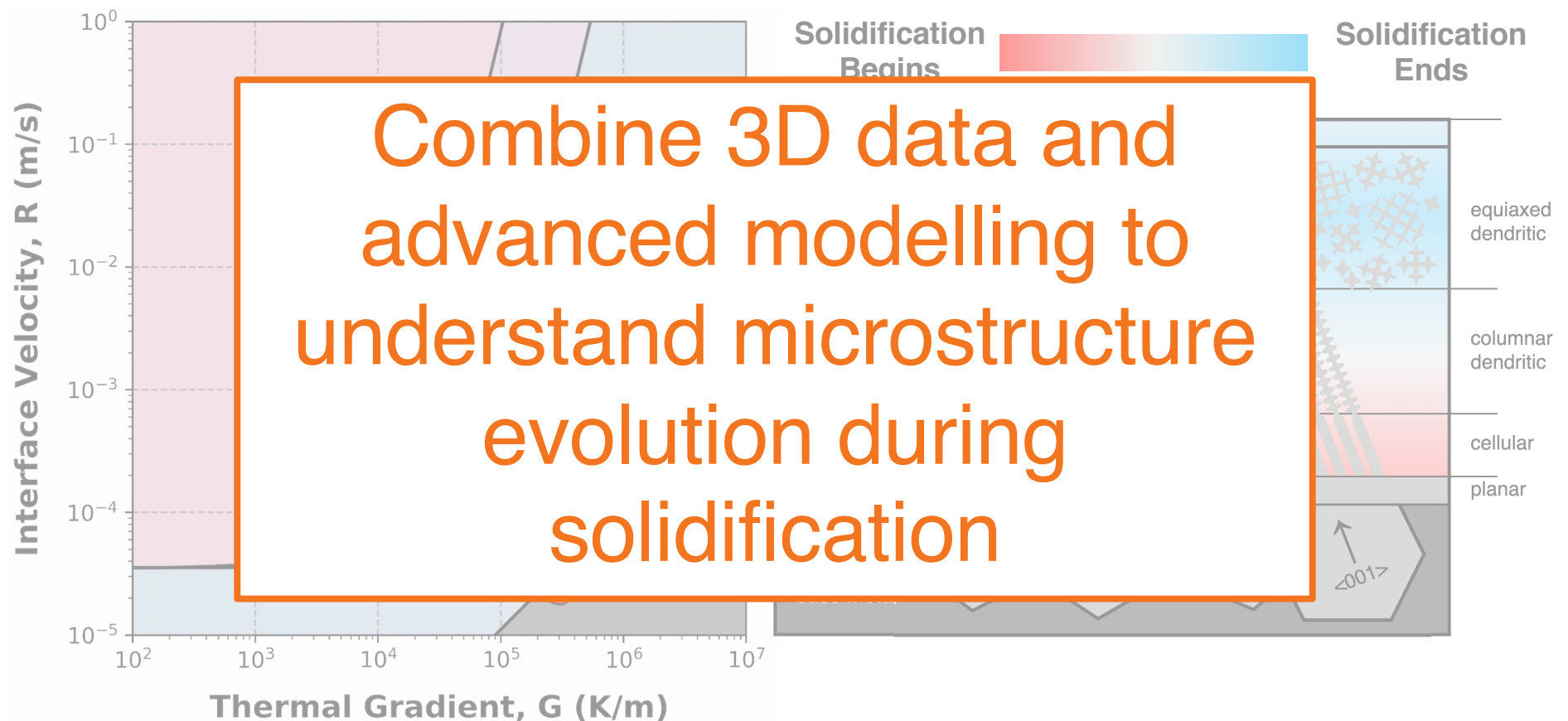
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Local microstructure control relies on understanding solidification conditions

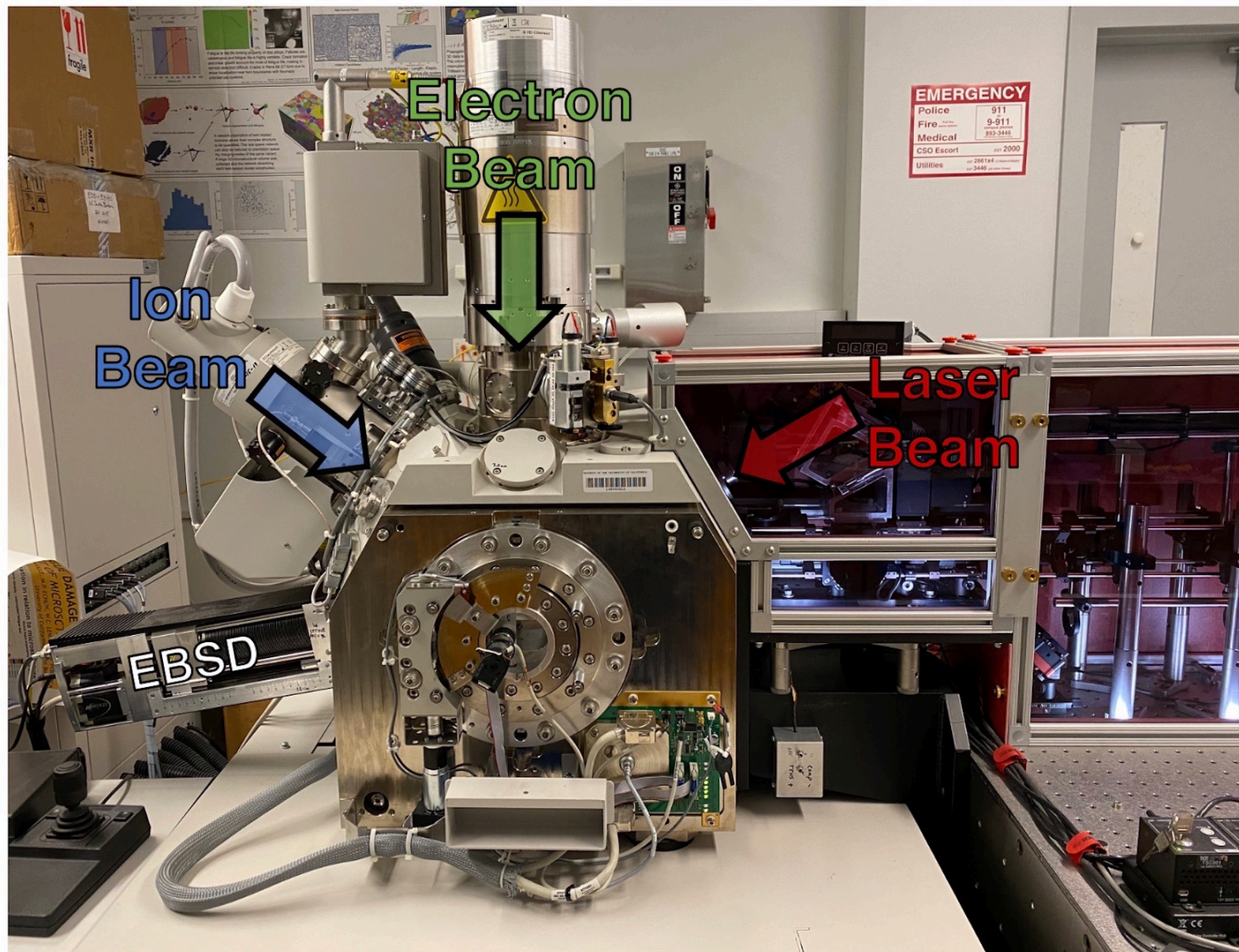
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Outline

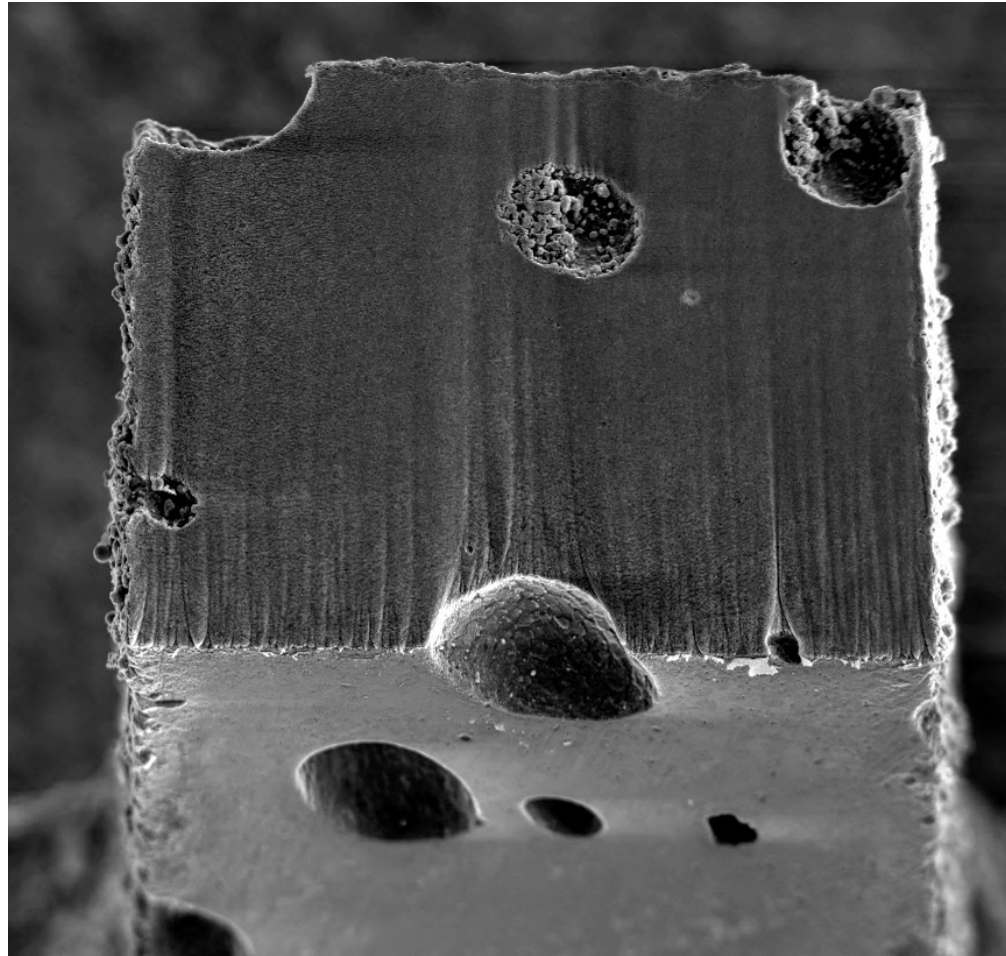
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The TriBeam collects rich multi-modal datasets in three dimensions



TriBeam tomography generates data in a set of slices

- Secondary electron images taken after laser machining*

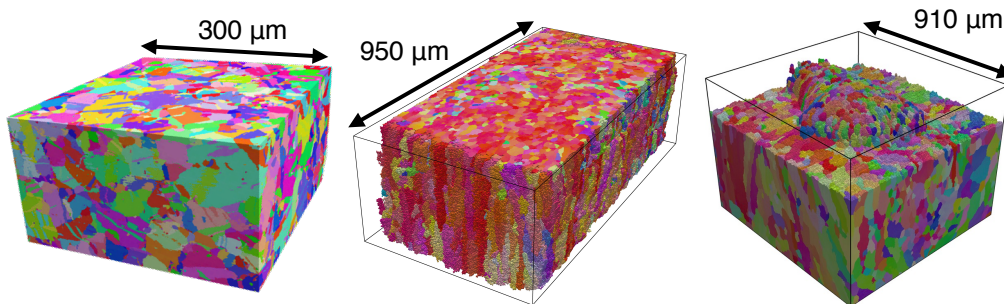


250 μm

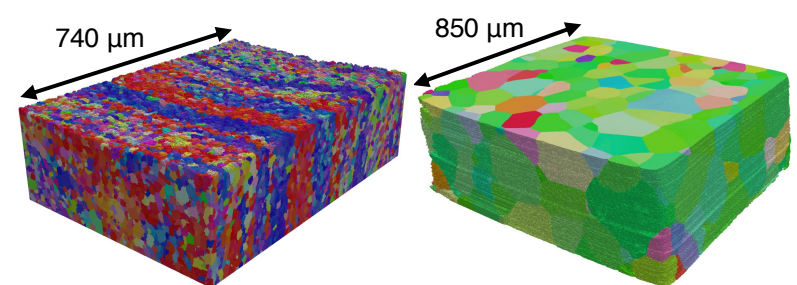
*Additively Manufactured AlNiCo magnet

Femtosecond laser ablation makes the TriBeam material agnostic

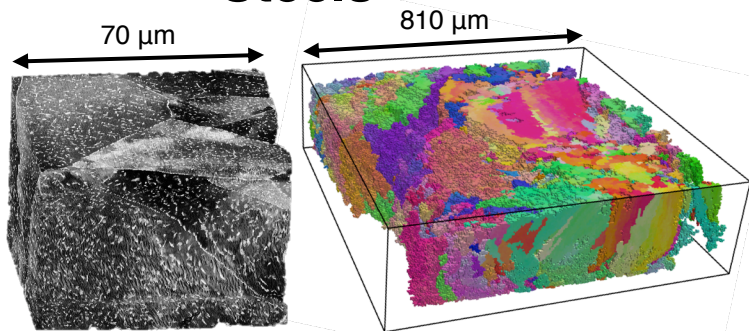
Nickel Superalloys



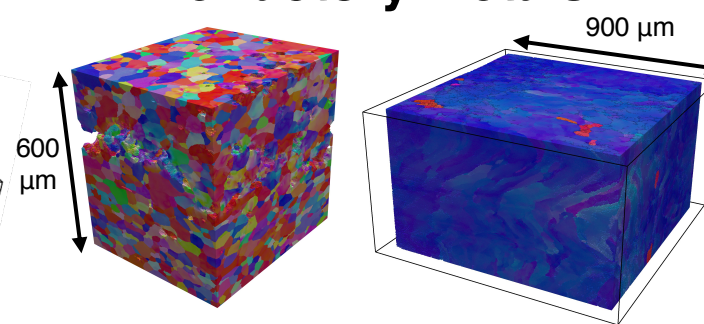
Titanium Alloys



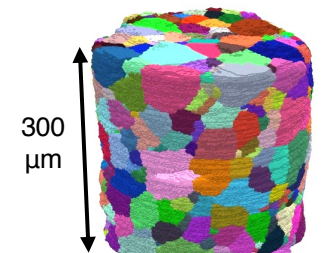
Steels



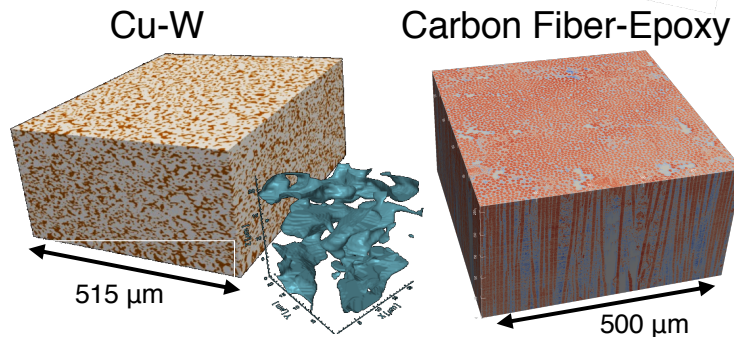
Refractory Metals



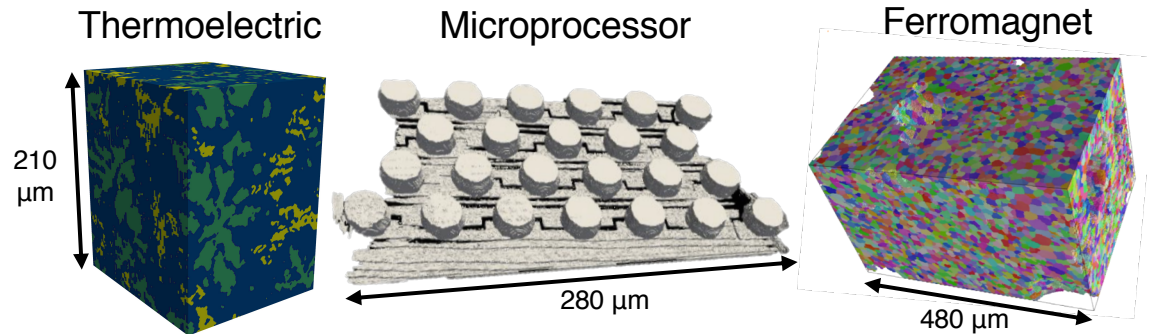
Ceramics



Composites

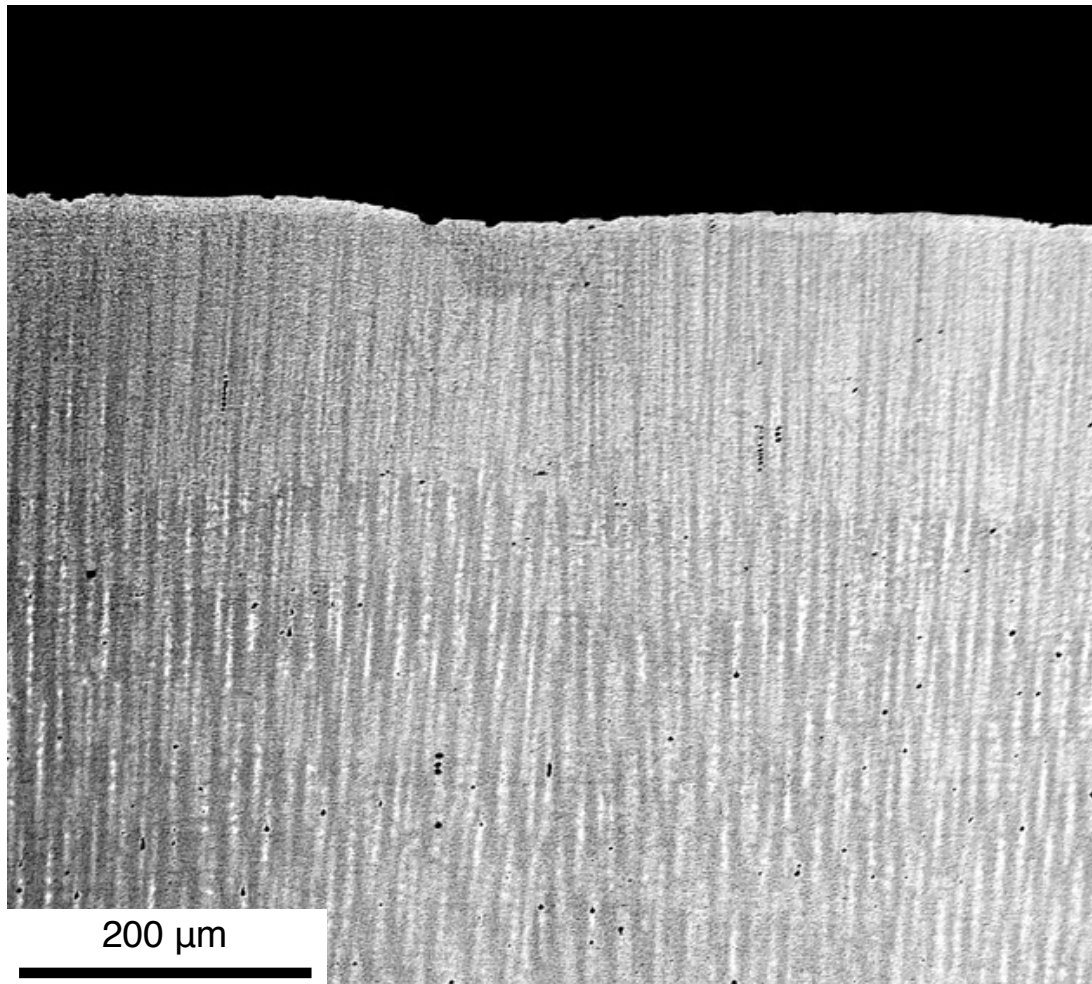


Electronic Materials

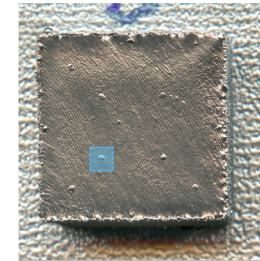


Isolated melt pool on a bulk raster block

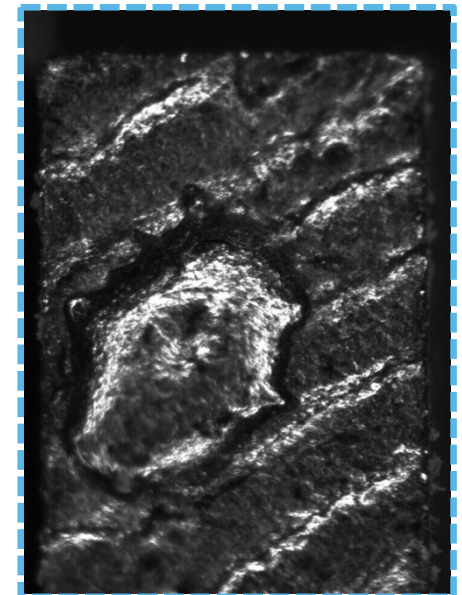
↑
Build
Direction



Raster Melt



10 mm

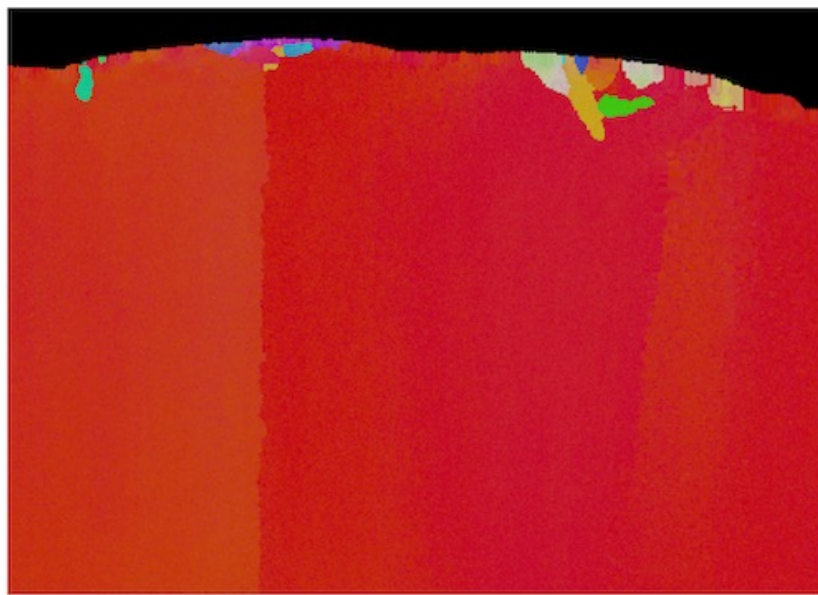


0.5 mm

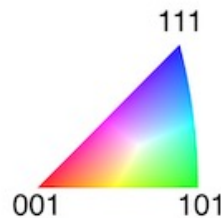
Build Direction

EBSD data shows nucleated grains, BSE data shows melt pool boundary

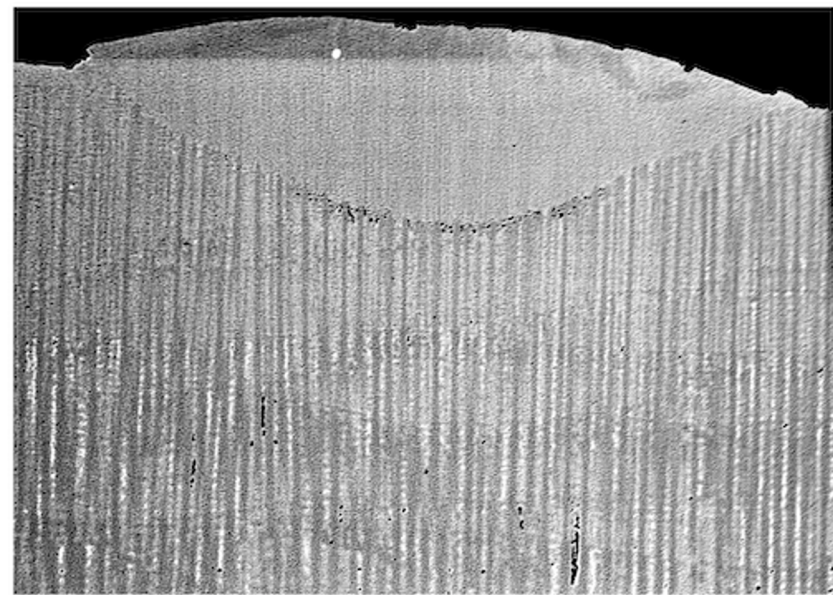
- Can fuse data modalities using TPS algorithm in 3D
- Also removes any distortions in EBSD data



↑ Build
Direction



250 μm



250 μm

Data fusion can be achieved via the Thin Plate Spline Algorithm (TPS)*

Distorted frame is a function of the reference frame

$$(X, Y, Z) = f(x, y, z)$$

$$(X, Y, Z) = f(x, y, z) = \overbrace{a_1 + a_x x + a_y y + a_z z}^{\text{Affine Portion}} + \overbrace{\sum_{i=1}^n w_i U(|P_i - (x, y, z)|)}^{\text{Bending Portion}}$$

- Radial basis function:

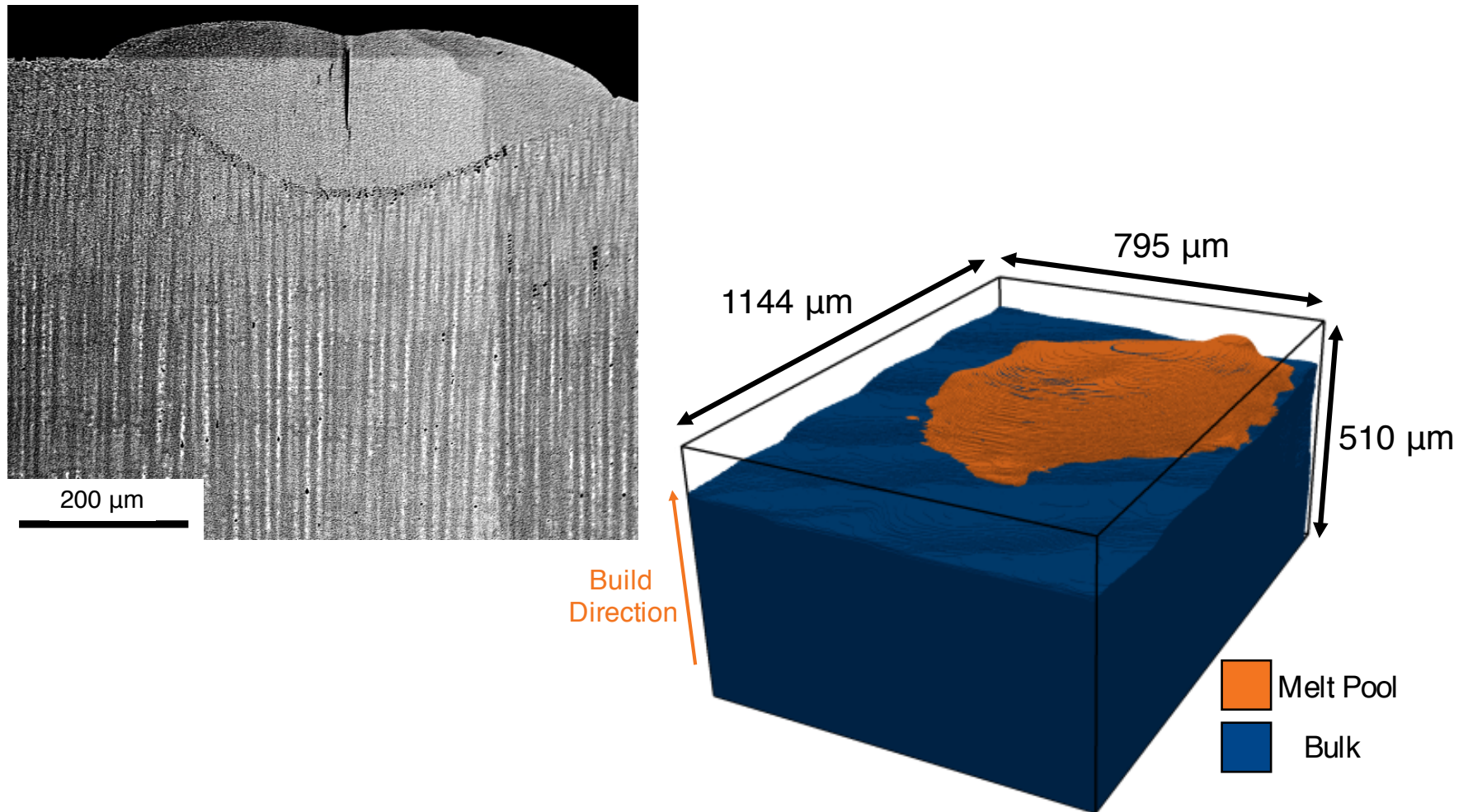
$$U(r) = r^2 \log(r^2)$$

- Solve for weighting coefficients w_i and a_1 , a_x , a_y , and a_z using n control points (CP) to create a system of $n+4$ equations
 - CPs are shared locations in distorted (X_i, Y_i, Z_i) and reference (x_i, y_i, z_i) images
 - Triple points, voids, precipitates, sample edges

*Extended to 3D using 2D form described in Y. B. Zhang, A Elbrond, F. X. Lin, *Materials Characterization* (2014)

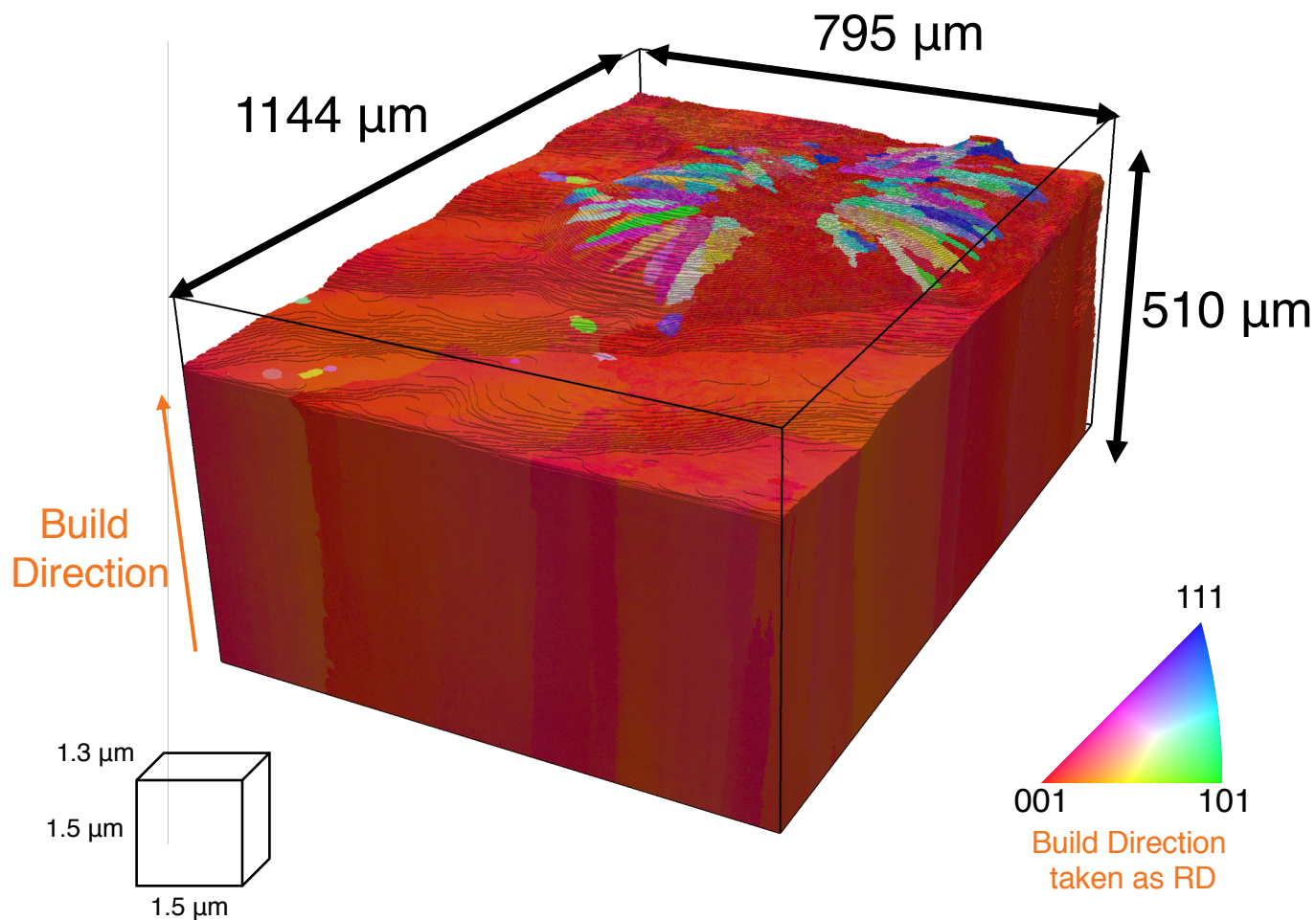
EBSD aligned with BS imaging using TPS, allowing melt pool segmentation

- 3894 control points used for thin plate spline algorithm

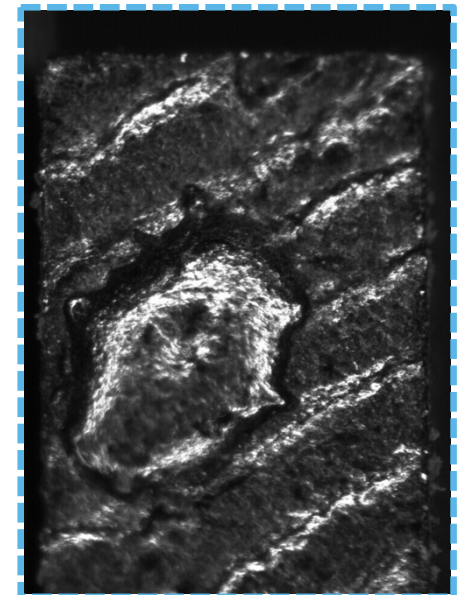
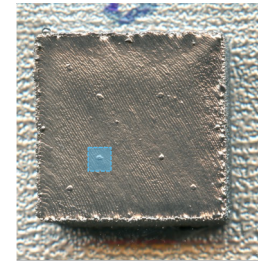



Reconstruction of isolated melt pool on a bulk raster block

- 878 slices collected (~20 minutes per slice)
 - 3.6 TB of data



Raster Melt



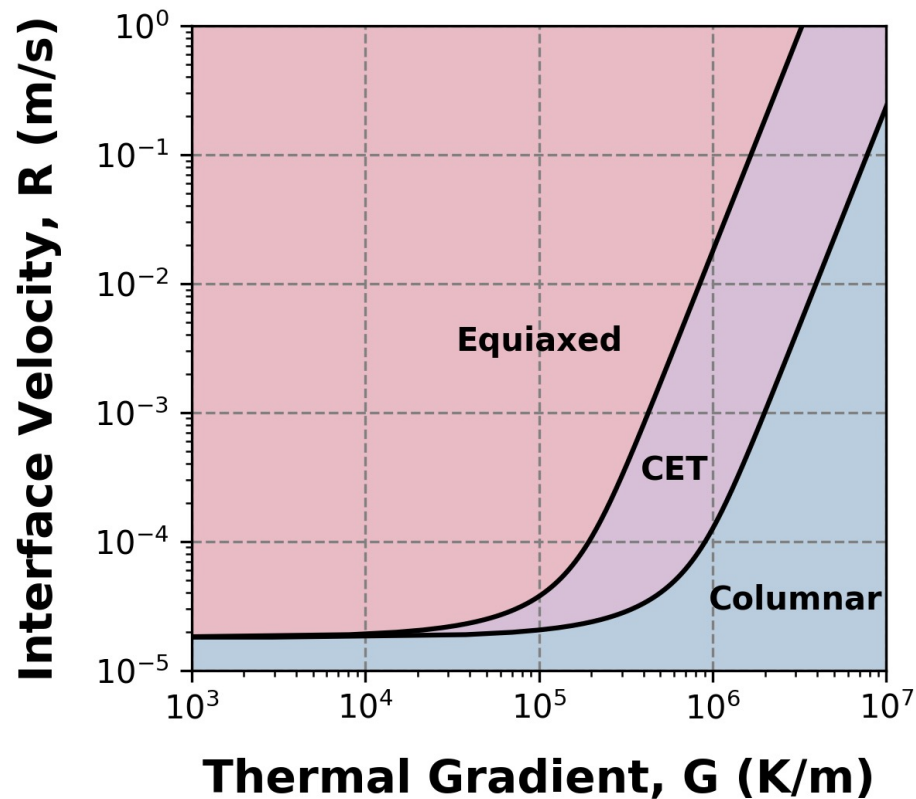
Build Direction 

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Need to accurately predict the columnar to equiaxed transition (CET)

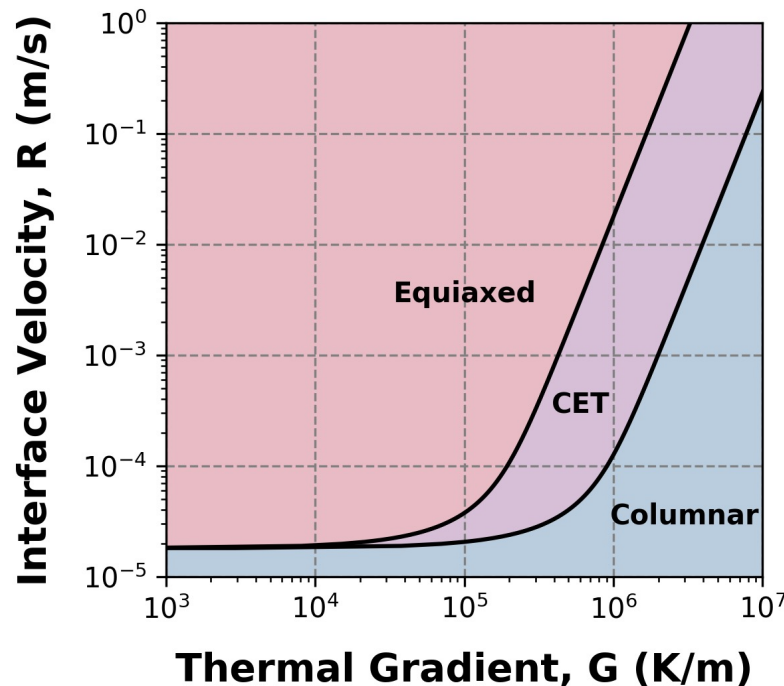
$$G = \frac{1}{n+1} \sqrt[3]{\frac{-4\pi N_0}{3 \ln [1 - \phi]}} \cdot \left(1 - \frac{\Delta T_n^{n+1}}{(a \cdot R)^{(n+1)/n}} \right) \cdot (a \cdot R)^{1/n}$$



Need to accurately predict the columnar to equiaxed transition (CET)

- Gäumann's modification of Hunt's CET model at high G
 - Developed for laser deposition on single-crystal Ni superalloys

$$\frac{G^n}{R} = a \left\{ \sqrt[3]{\frac{-4\pi N_0}{3 \ln[1 - \phi]}} \frac{1}{n + 1} \right\}^n$$



G = Thermal Gradient

R = Interface Velocity

N_0 = Nuclei density

a, n = Material constants

ϕ = Probability of grain nucleation ahead of interface

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$$\frac{G^n}{R} = a \left\{ \sqrt[3]{\frac{-4\pi N_0}{3 \ln[1 - \phi]}} \frac{1}{n + 1} \right\}^n$$

Rearrange to yield:

$$\phi = 1 - \exp \left\{ \frac{-4\pi N_0 a^{3/n}}{3(n + 1)^3} \left(\frac{R}{G^n} \right)^{3/n} \right\}$$

G = Thermal Gradient

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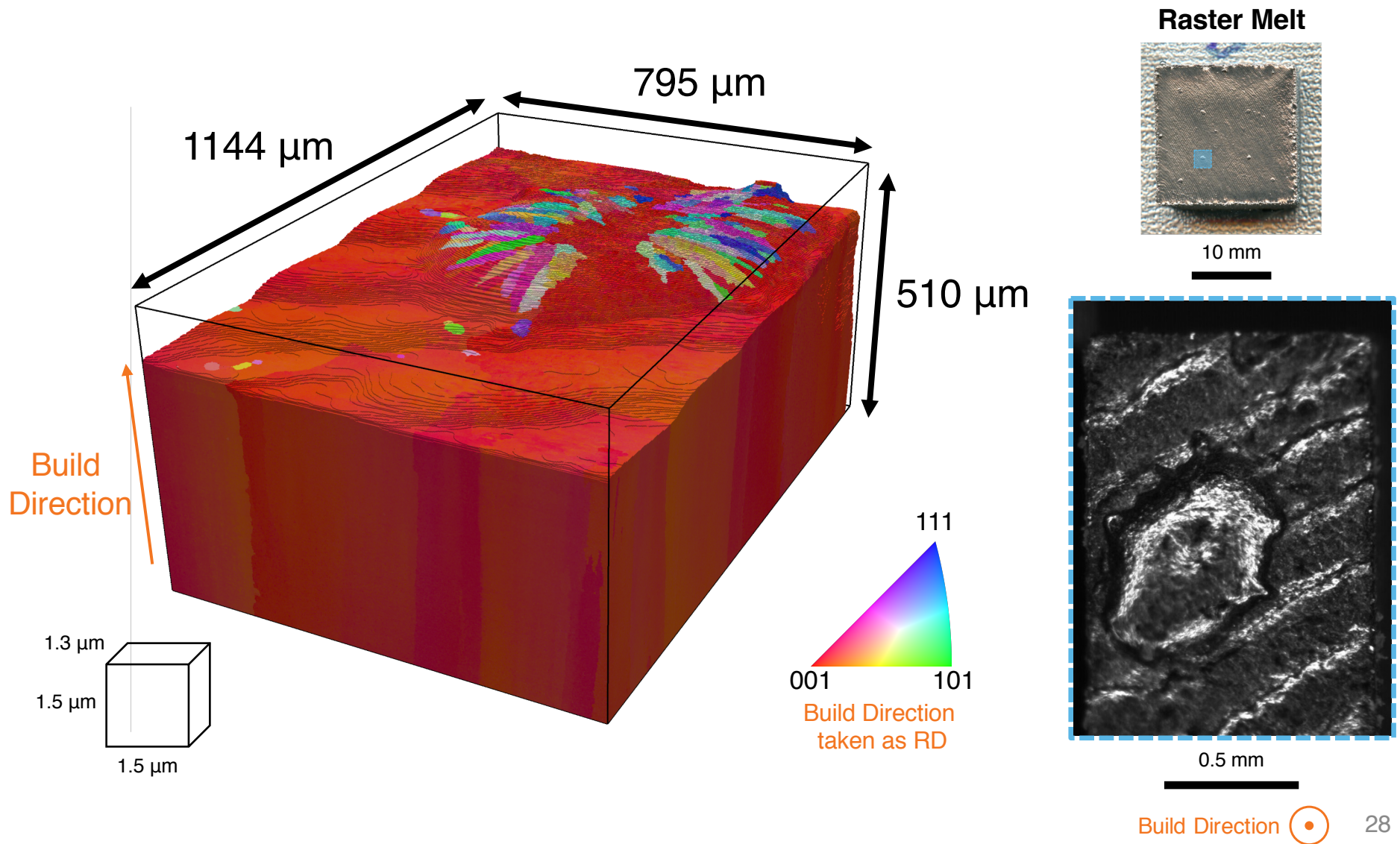
Checklist for Columnar to Equiaxed Transition (CET) Model

- Want to predict the formation of nucleated grains

$$\phi = 1 - \exp \left\{ \frac{-4\pi N_0 a^{3/n}}{3(n+1)^3} \left(\frac{R}{G^n} \right)^{3/n} \right\}$$

- ☐ G = Thermal Gradient
- ☐ R = Interface Velocity
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Apply model to isolated melt pool on top of raster melt block



G and R can be calculated for this solidification event using TRUCHAS

- Want to predict the formation of nucleated grains

$$\phi = 1 - \exp \left\{ \frac{-4\pi N_0 a^{3/n}}{3(n+1)^3} \left(\frac{R}{G^n} \right)^{3/n} \right\}$$

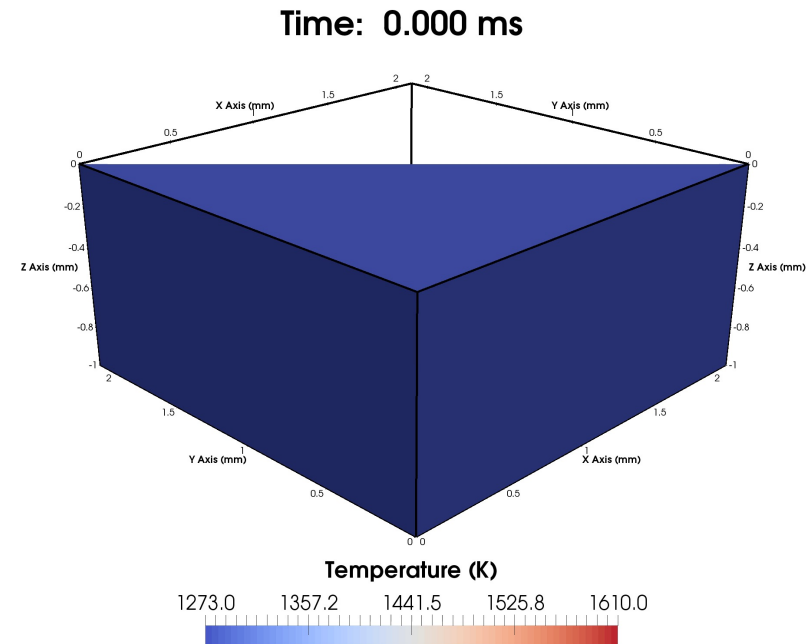
TRUCHAS {

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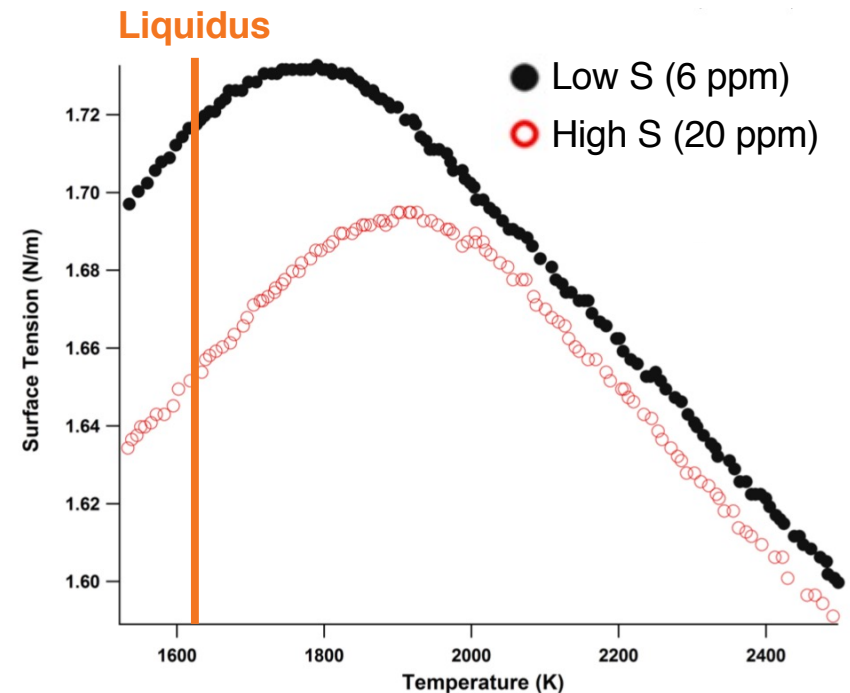
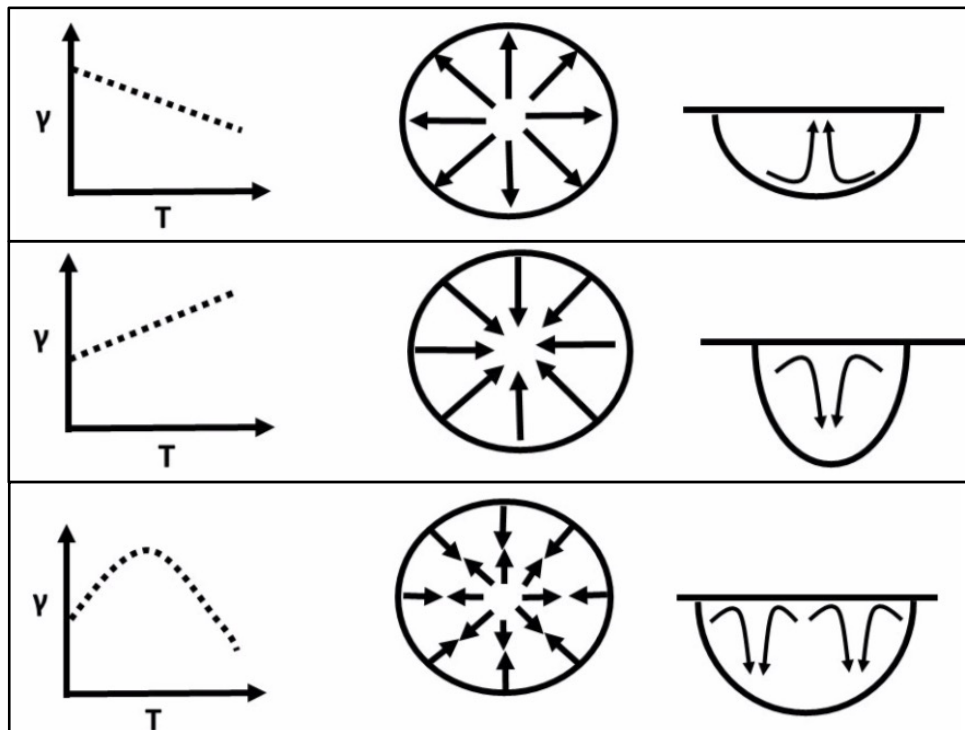
Can use TRUCHAS to model differences in temperature profile during solidification

- Can model heat transfer and fluid flow
 - Designed for casting, so does not currently consider powder-beam interactions or multiple melt layers
- Enables 3D calculation of thermal gradient and solid-liquid interface velocity on μm and ms scales
 - Inaccessible to in-situ monitoring
- Code has been validated against Abaqus and that of Debroy et al.



TRUCHAS Simulations performed with and without fluid flow

- Performed simulations with relevant beam settings
 - 10 mA 0.5 ms dwell, 1273 K preheat
 - All simulations with heat transfer, two also include fluid flow
 - Fluid flow incorporates temperature dependence of surface tension (γ)



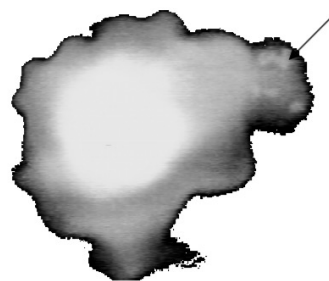
N Raghavan, PhD dissertation, 2017

Adapted from PD Lee, PN Quesed, and M Mclean, *Phil. Trans. R. Soc. Lond.*, 1998

TRUCHAS Simulations performed with and without fluid flow

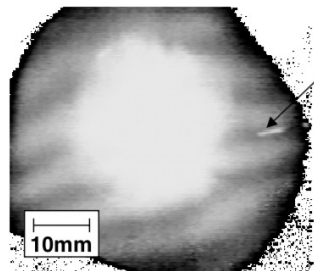
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6 ppm S Alloy

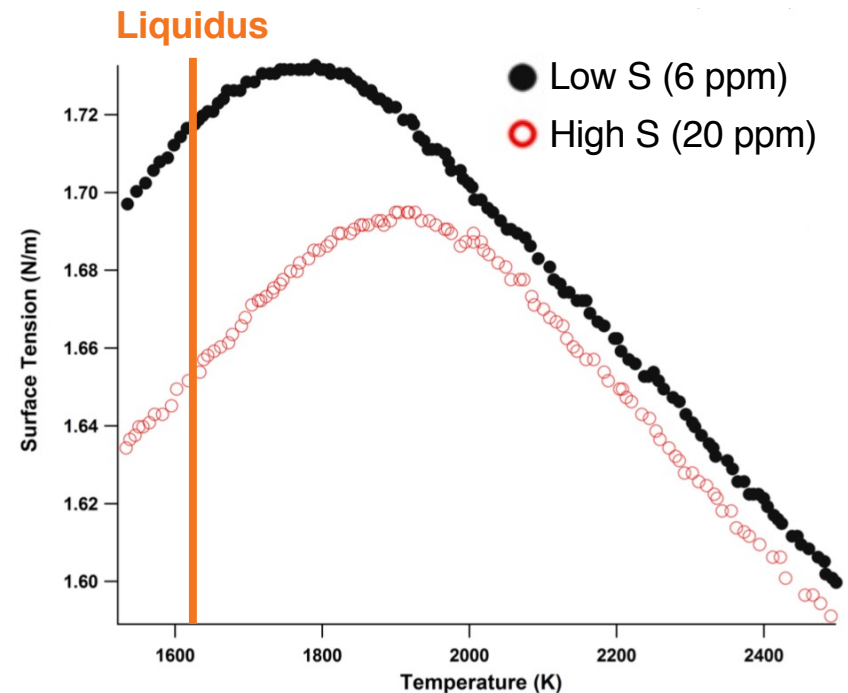


Alumina moves away from beam and then stays at side

20 ppm S Alloy

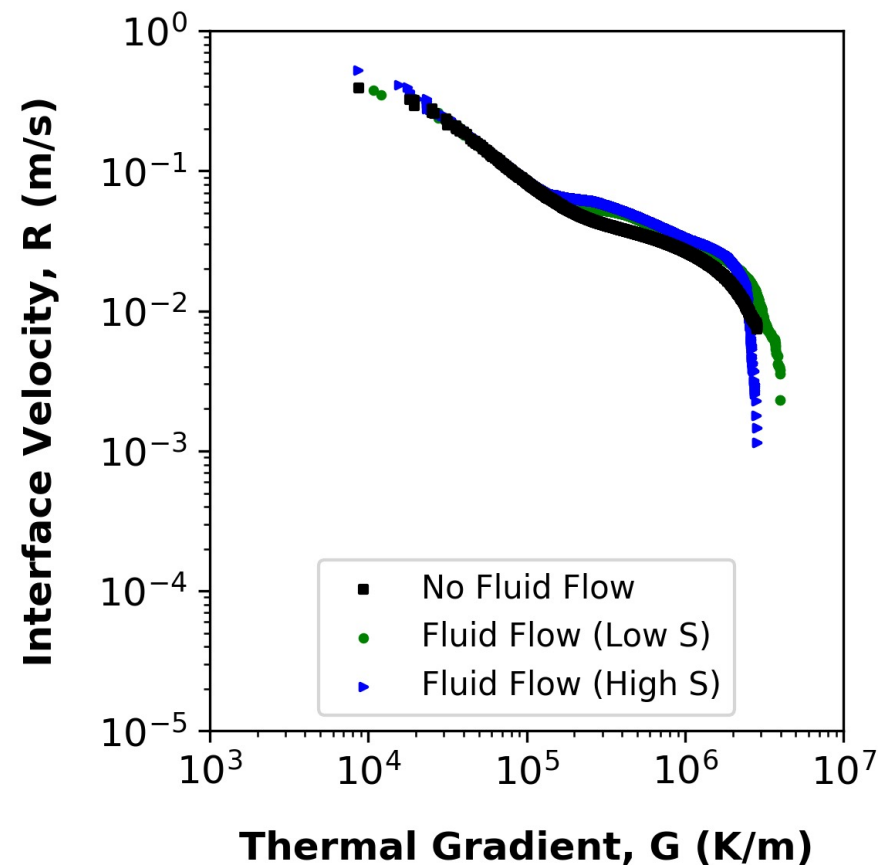


Alumina moves towards the beam and then stays under beam near center



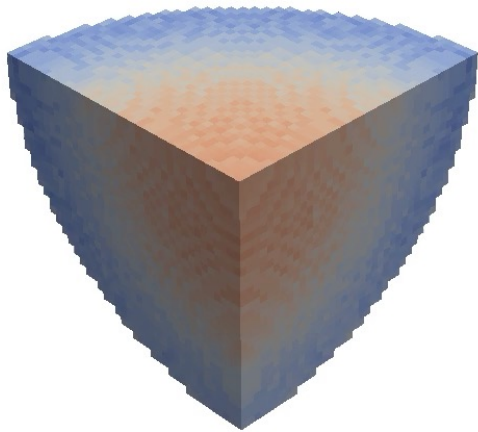
Results of TRUCHAS simulations

- Incorporation of fluid flow increases interface velocity in middle stages of solidification

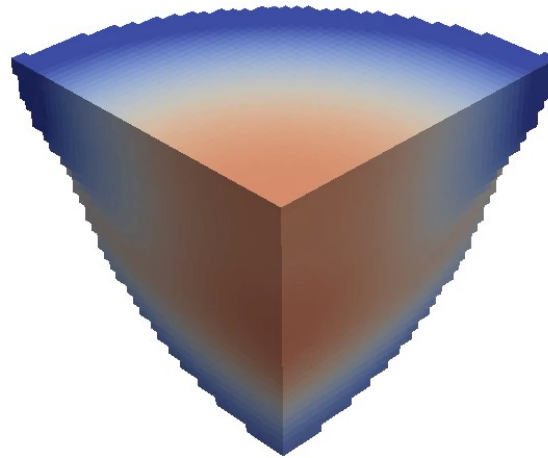


Higher S content increases local solidification time

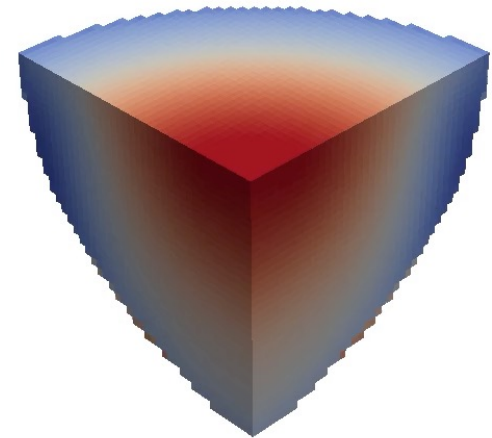
No Fluid Flow



Fluid Flow (Low S)



Fluid Flow (High S)

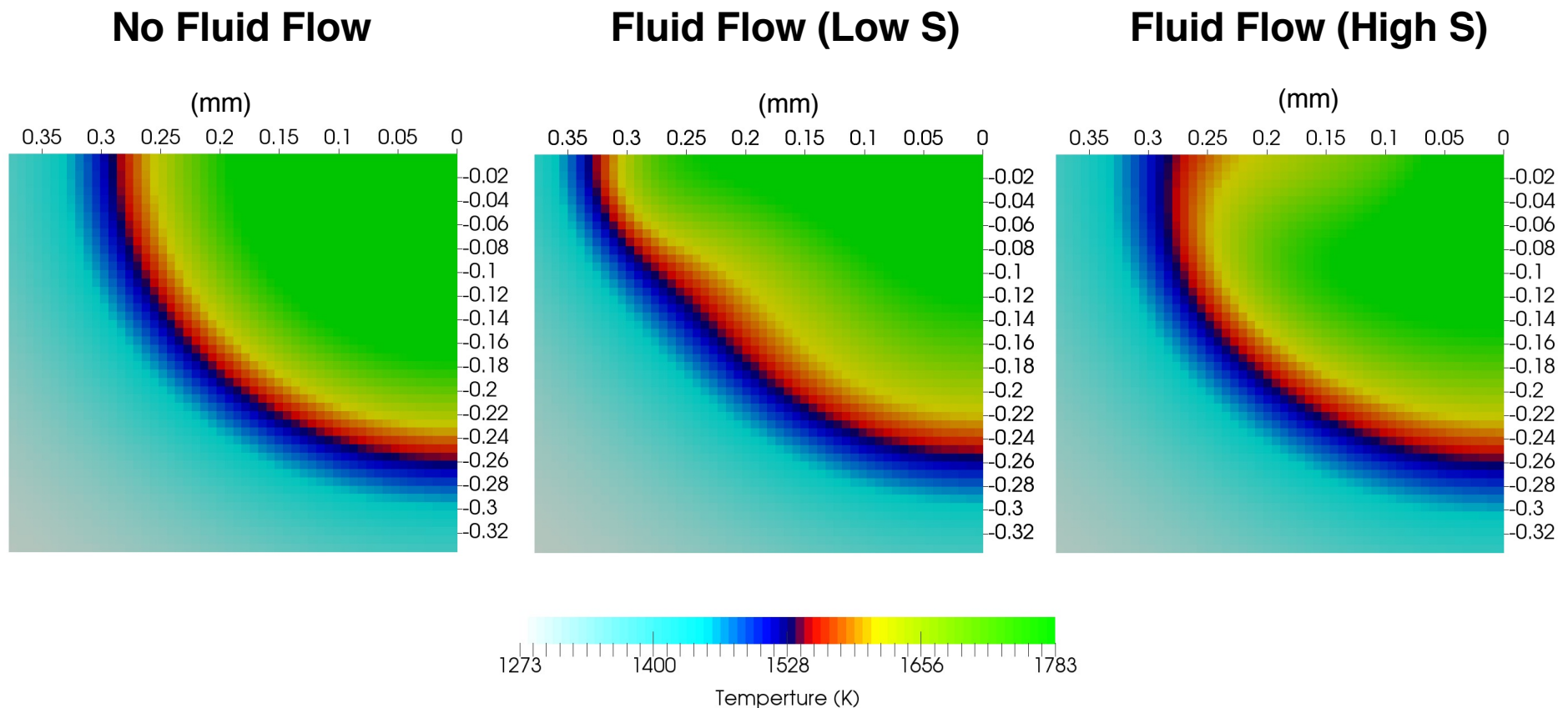


Local Solidification Time (ms)



Pool spreads more with lower S content, which is also seen in 304 steel welds

- Fully Solid, Mushy Zone, and Fully Liquid
- Maximum extent of melt pool at $t \approx 3$ ms



Visualizing fluid flow

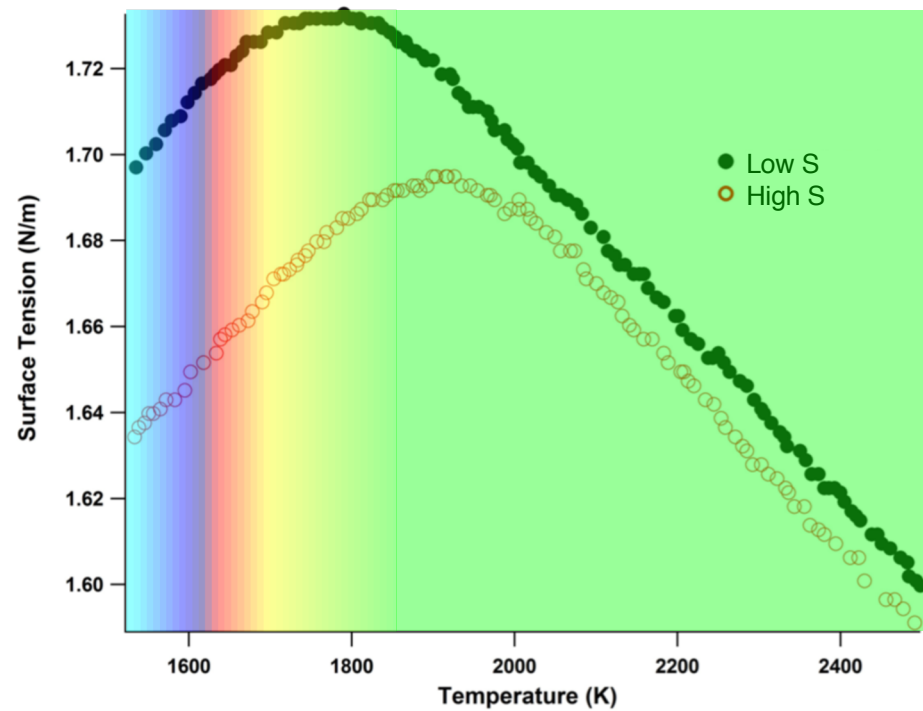
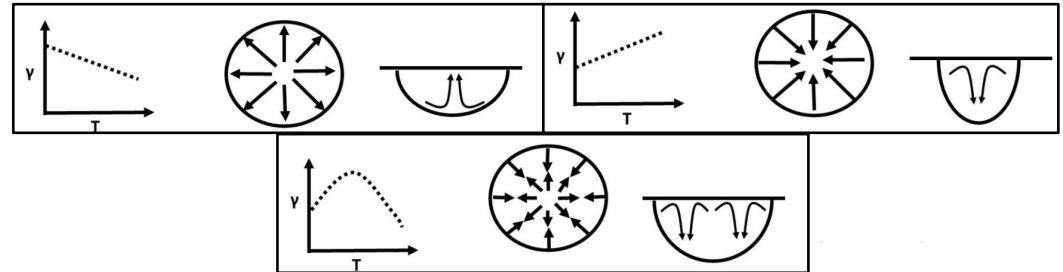
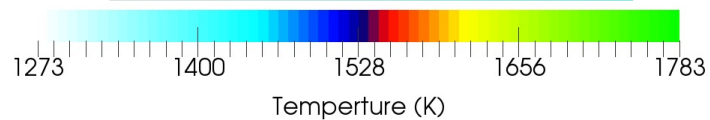
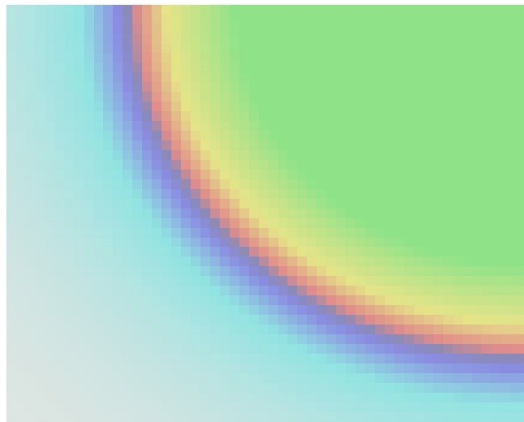
Time: 2.014583

Low S
Fluid
Flow



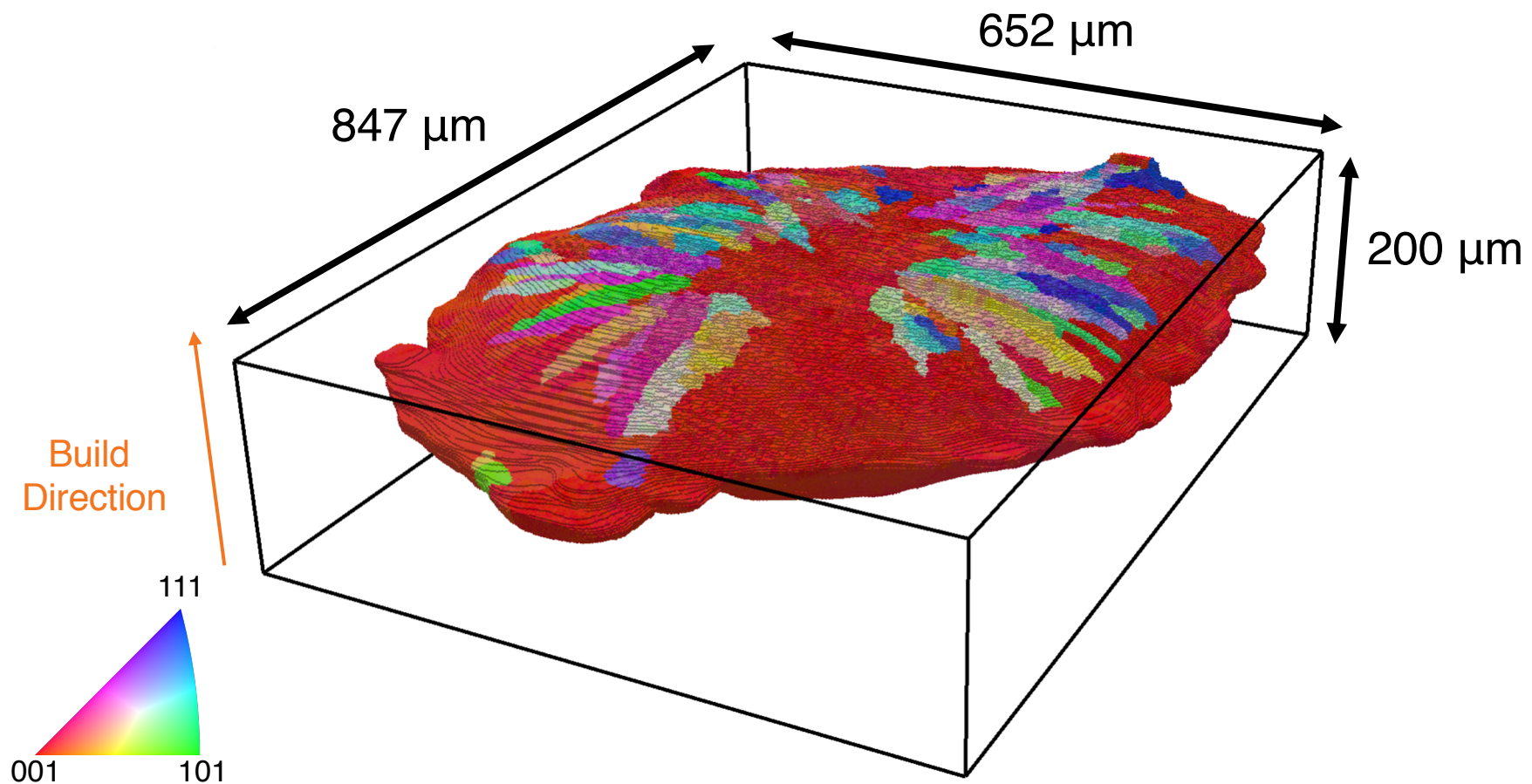
Time: 2.014583

High S
Fluid
Flow



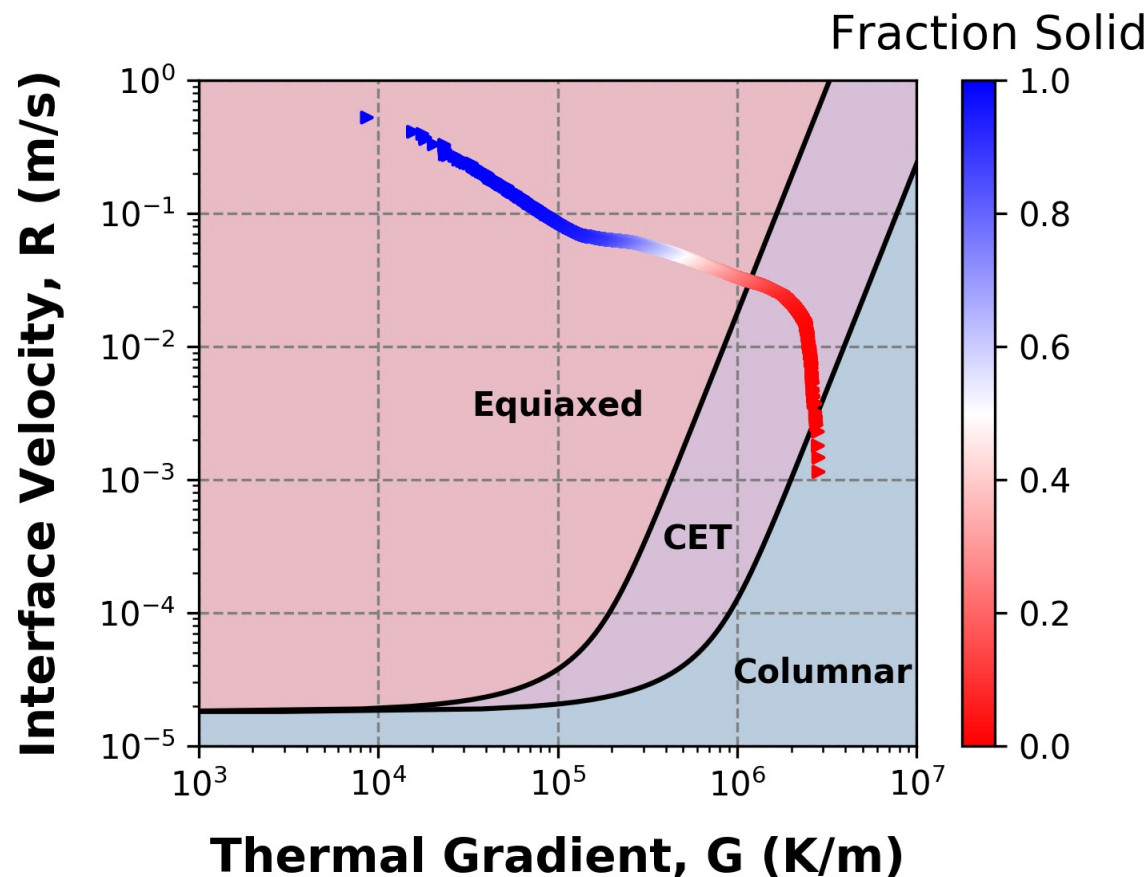
Isolated melt pool from full dataset

- Nucleated grains form radially around center of pool



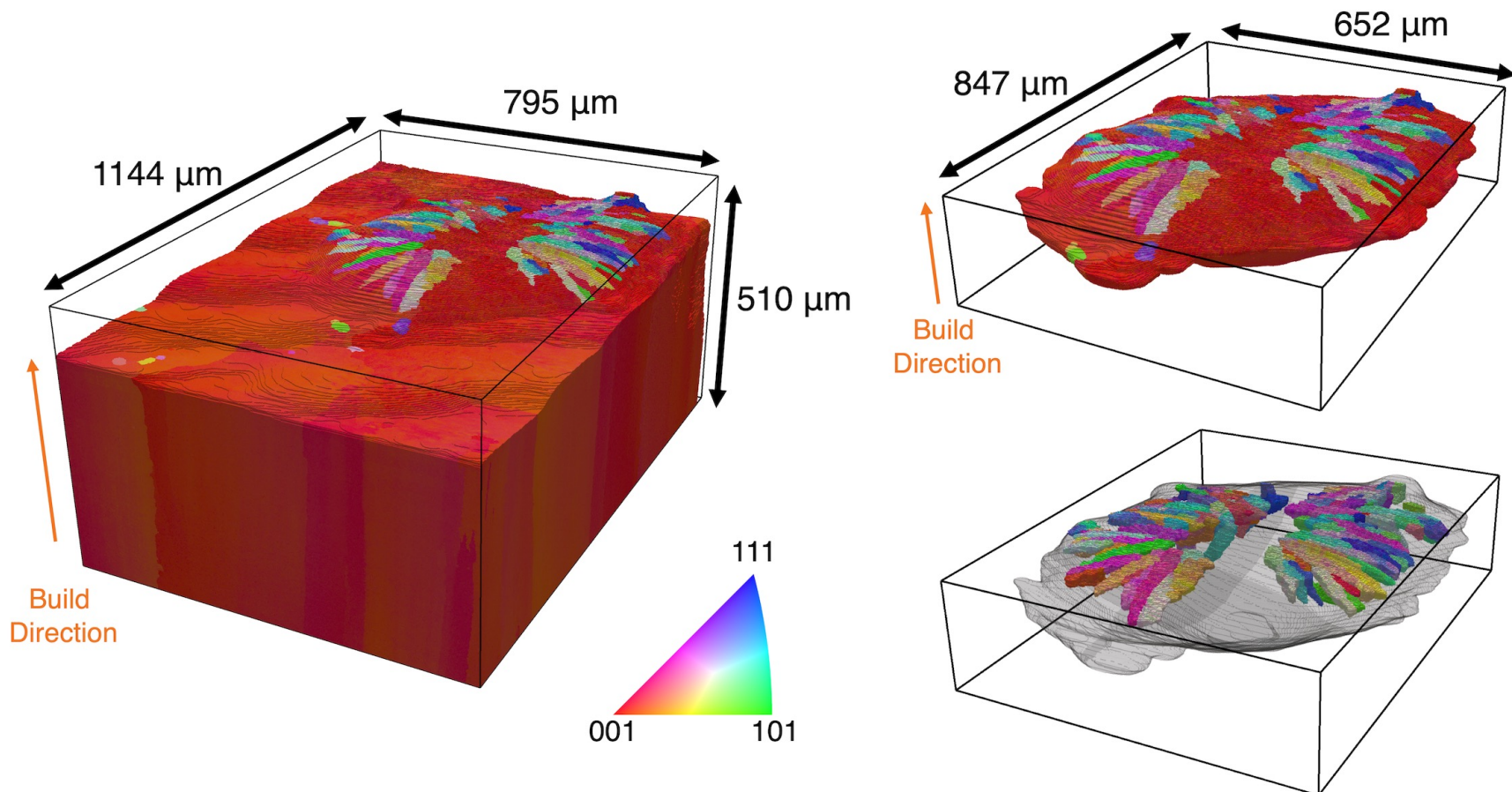
Results of TRUCHAS simulations

- Predicts nucleated grain fraction (Φ) of **80.8%**



Results of TRUCHAS simulations

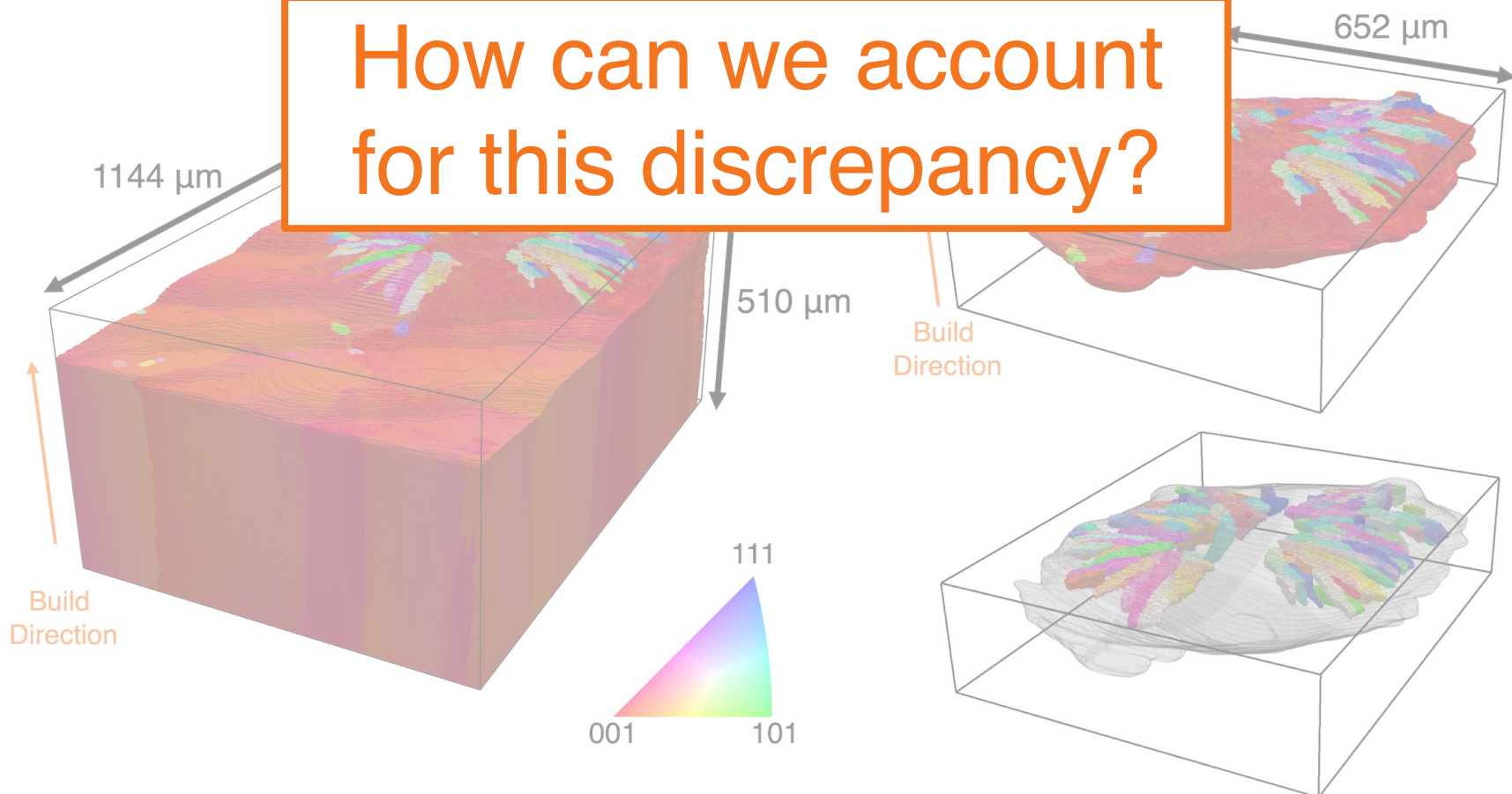
- Predicted nucleated grain fraction (Φ) of **80.8%**
- Measured nucleated grain fraction (Φ) of **11.4%**



Results of TRUCHAS simulations

- Predicted nucleated grain fraction (Φ) of **80.8%**
- Measured nucleated grain fraction (Φ) of **11.4%**

How can we account for this discrepancy?



Checklist for Columnar to Equiaxed Transition (CET) Model

- Want to predict the formation of nucleated grains

$$\phi = 1 - \exp \left\{ \frac{-4\pi N_0 a^{3/n}}{3(n+1)^3} \left(\frac{R}{G^n} \right)^{3/n} \right\}$$

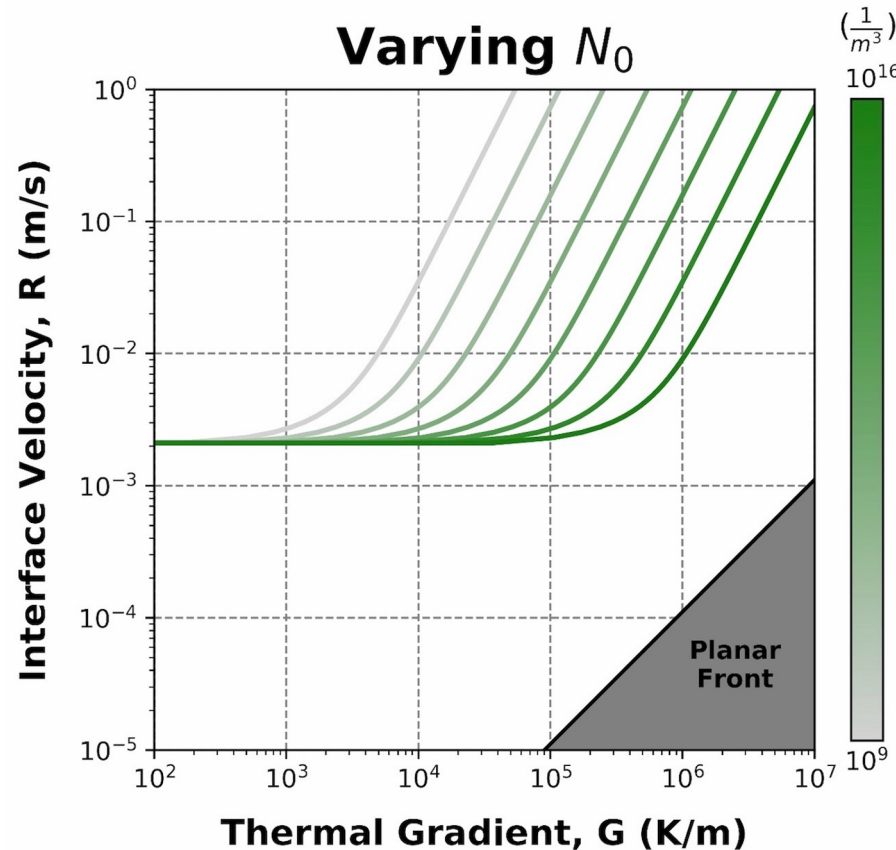
TRUCHAS

<input checked="" type="checkbox"/>	G = Thermal Gradient
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	ϕ = Probability of grain nucleation ahead of interface

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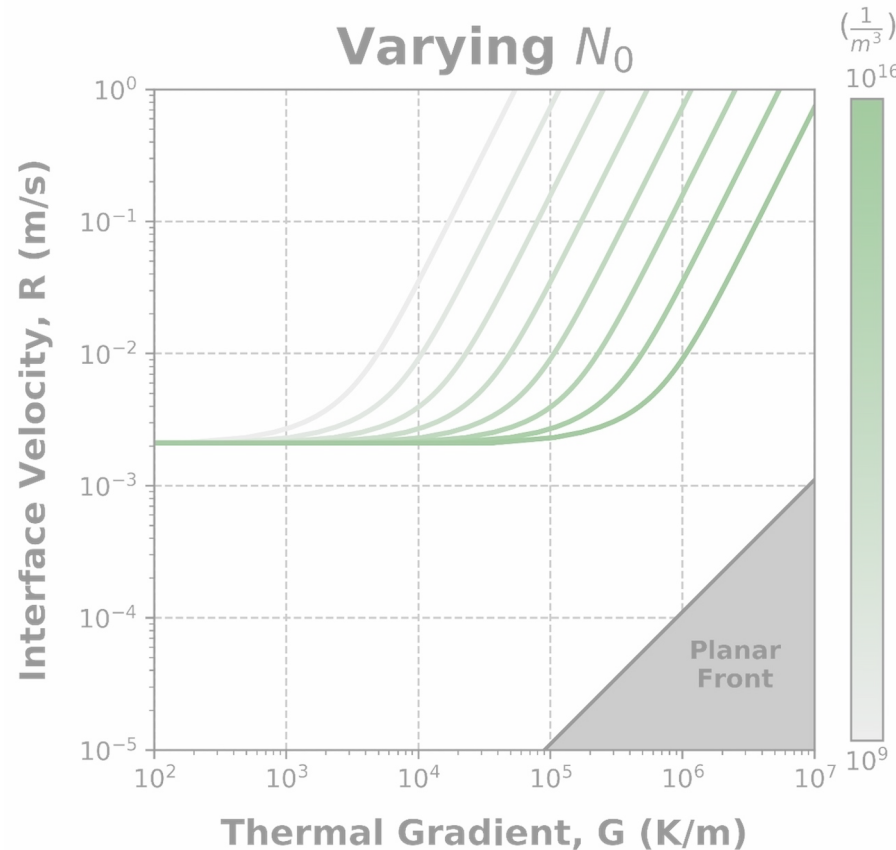
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Varying N_0



3D data shows N_0 is three orders of magnitude lower
 $2 \times 10^{15} \rightarrow 5.3 \times 10^{12} \text{ m}^{-3}$

ahead of interface

Checklist for Columnar to Equiaxed Transition (CET) Model

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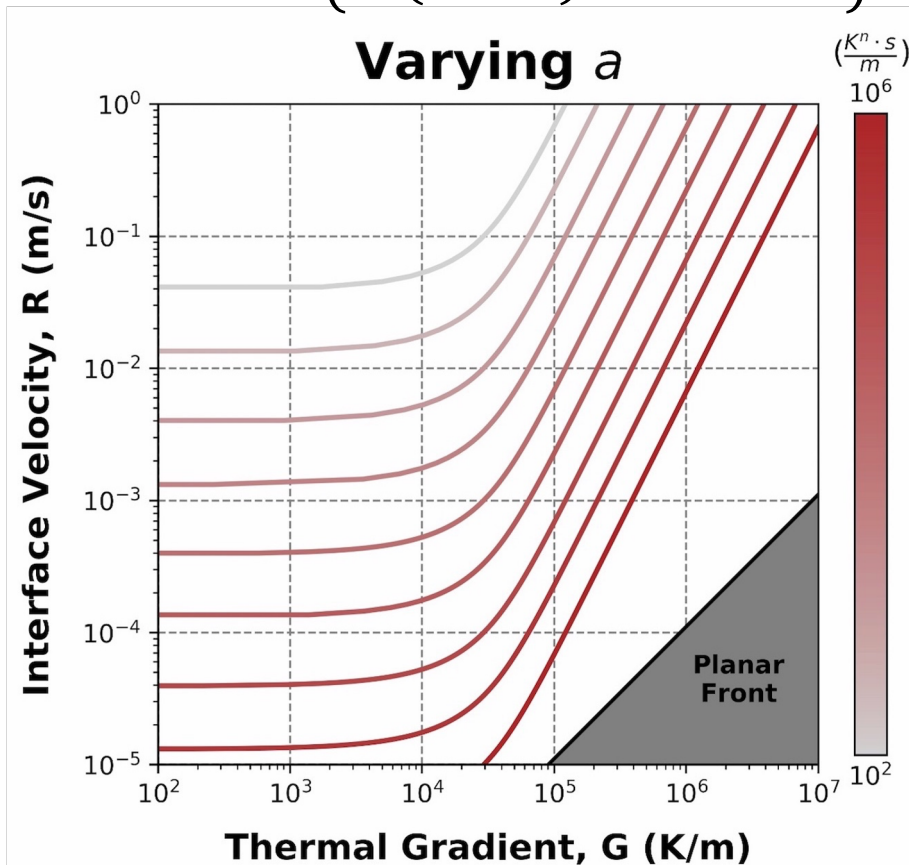
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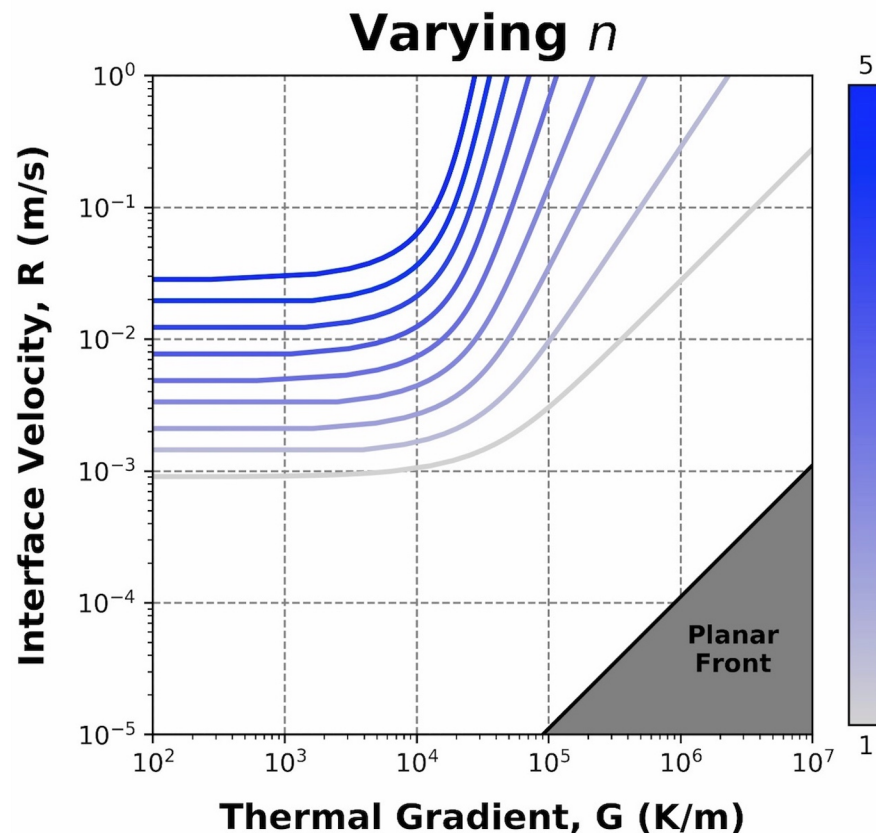


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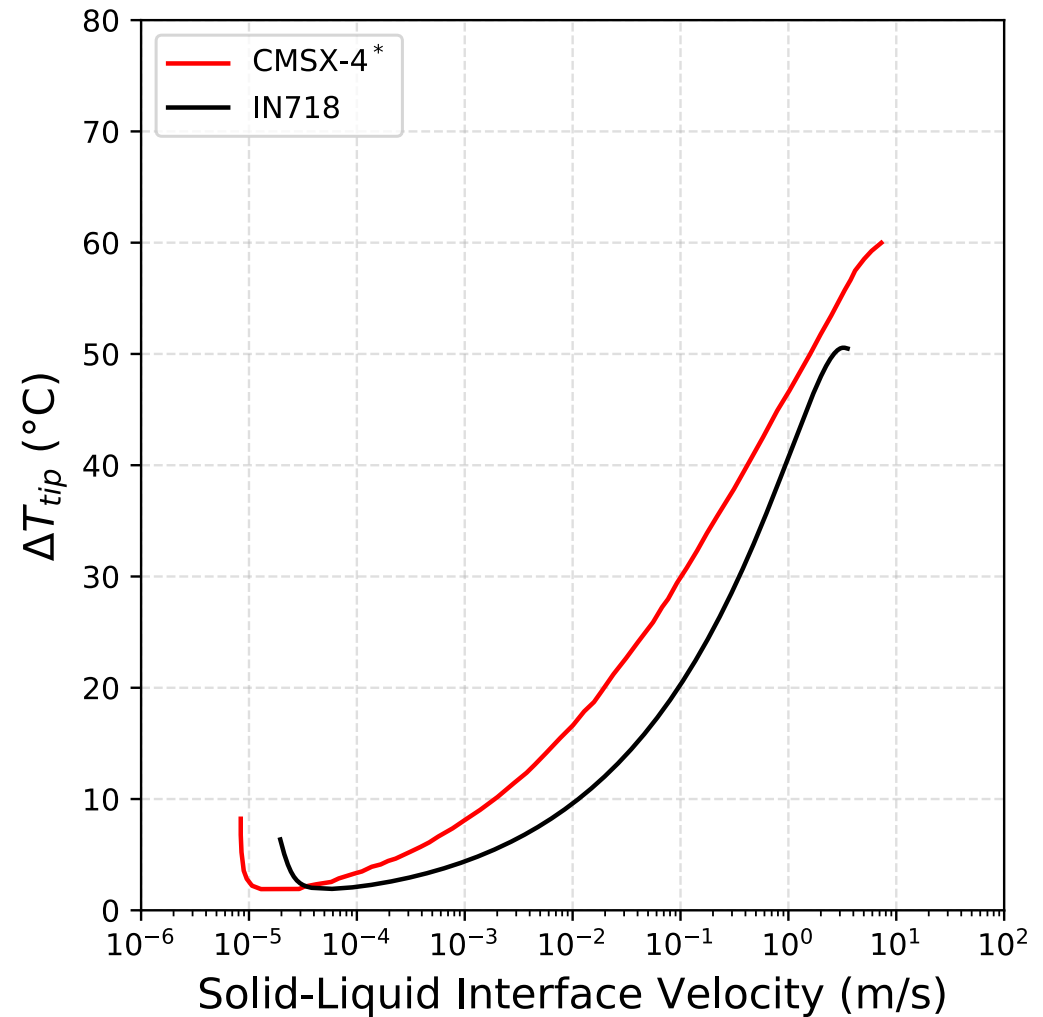
Material constants are alloy dependent, but can be determined using KGT model

- Want to predict the formation of nucleated grains

$$\phi = 1 - \exp \left\{ \frac{-4\pi N_0 a^{3/n}}{3(n+1)^3} \left(\frac{R}{G^n} \right)^{3/n} \right\}$$

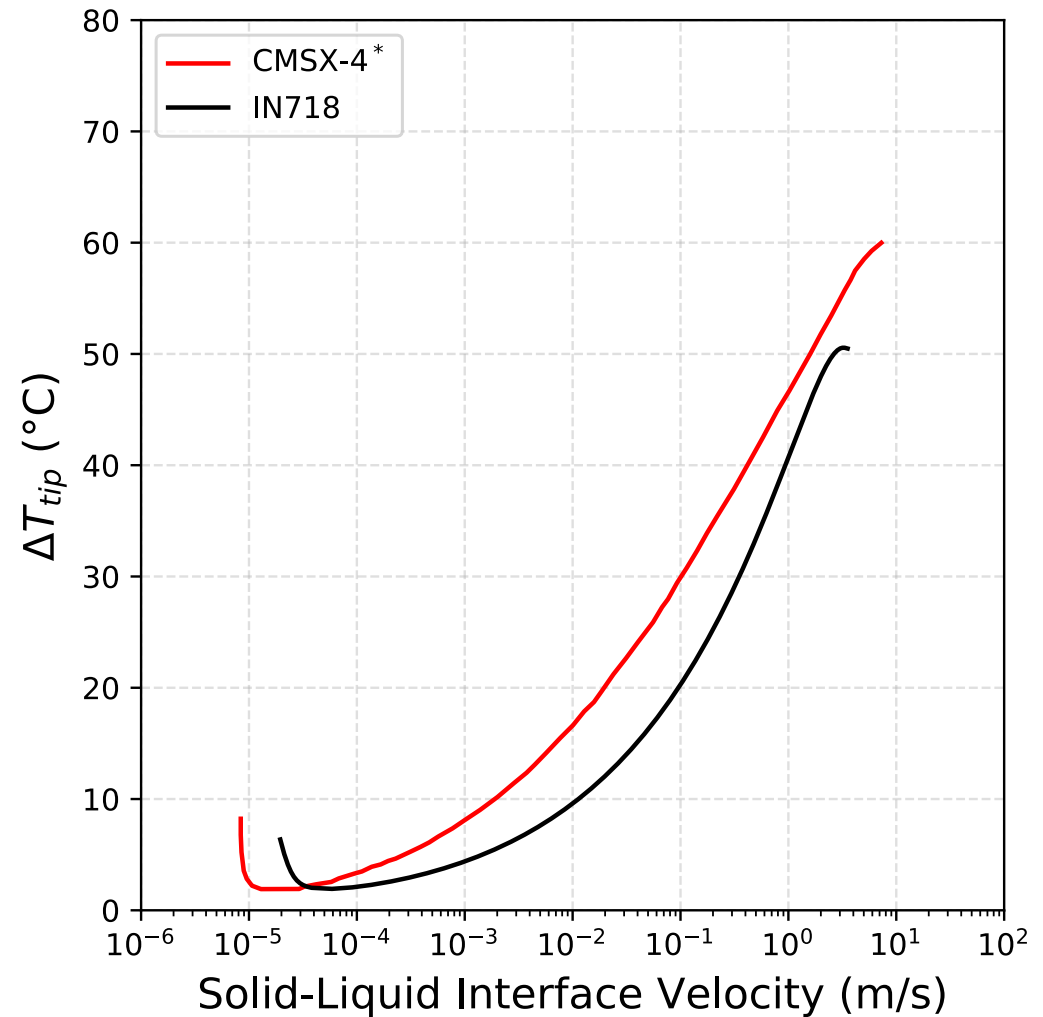
TRUCHAS	<input checked="" type="checkbox"/>	G = Thermal Gradient
	<input checked="" type="checkbox"/>	R = Interface Velocity
3D Data	<input checked="" type="checkbox"/>	N_0 = Nuclei density
KGT Model	<input type="checkbox"/>	a, n = Material constants
		ϕ = Probability of grain nucleation ahead of interface

Kurz Giovanola Trivedi (KGT) model predicts undercooling at the dendrite tip



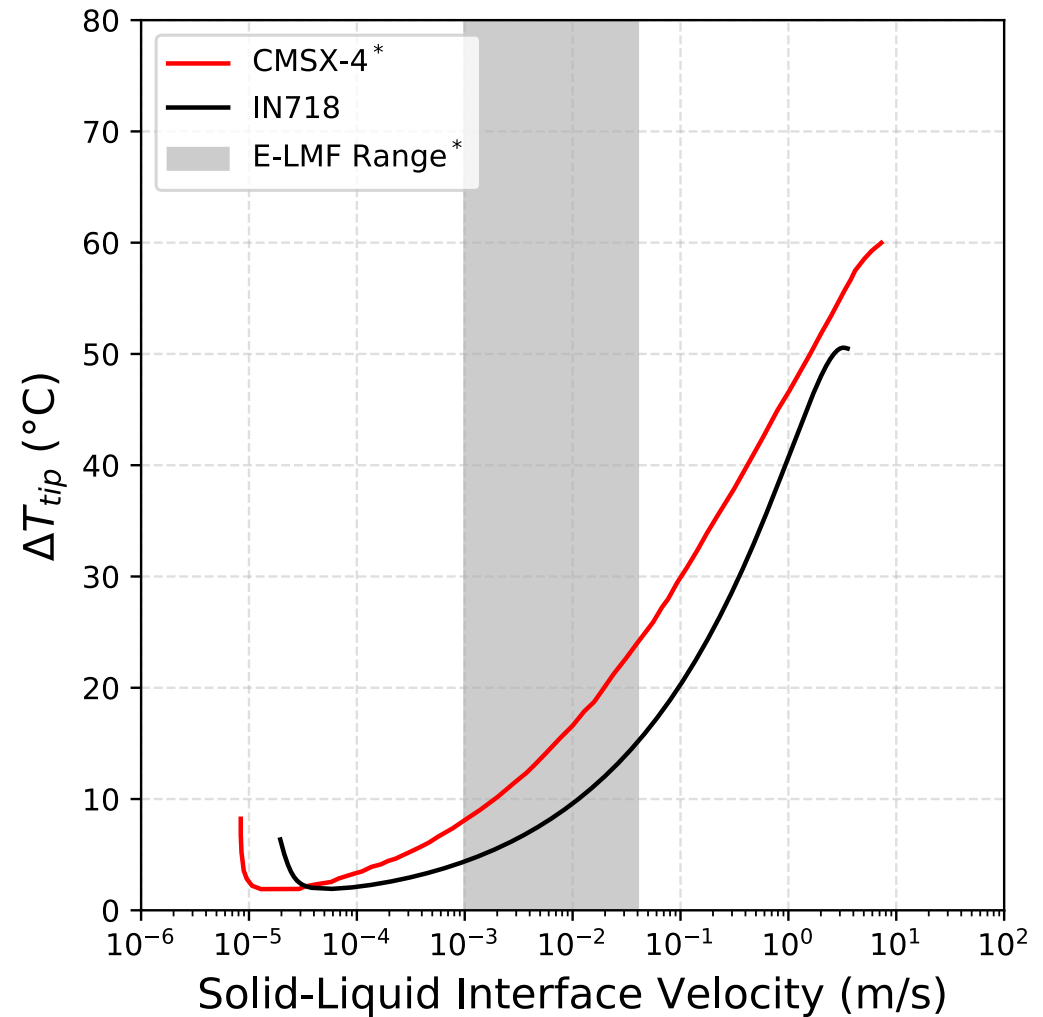
Kurz Giovanola Trivedi (KGT) model predicts undercooling at the dendrite tip

$$\Delta T_{tip} = (a \cdot R)^{1/n}$$



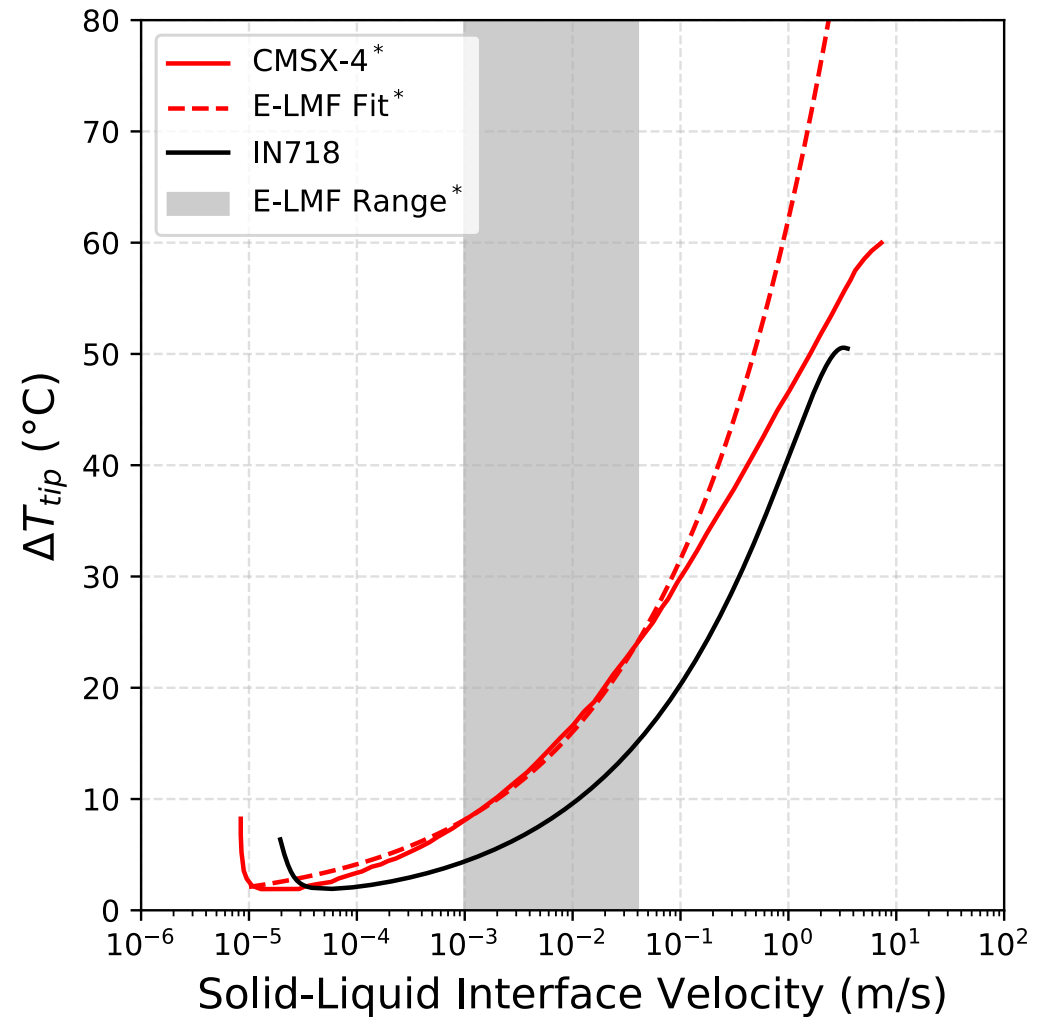
Kurz Giovanola Trivedi (KGT) model predicts undercooling at the dendrite tip

$$\Delta T_{tip} = (a \cdot R)^{1/n}$$



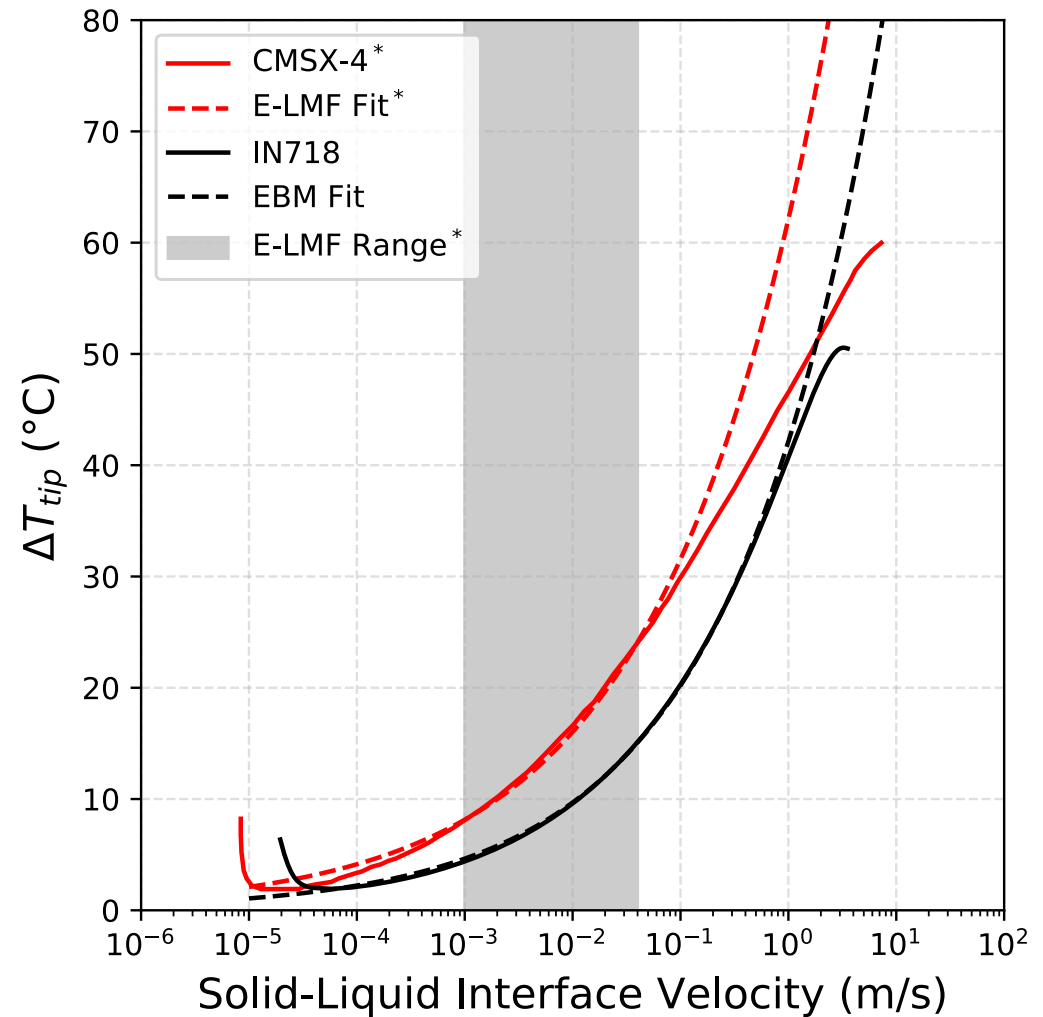
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Kurz Giovanola Trivedi (KGT) model predicts undercooling at the dendrite tip

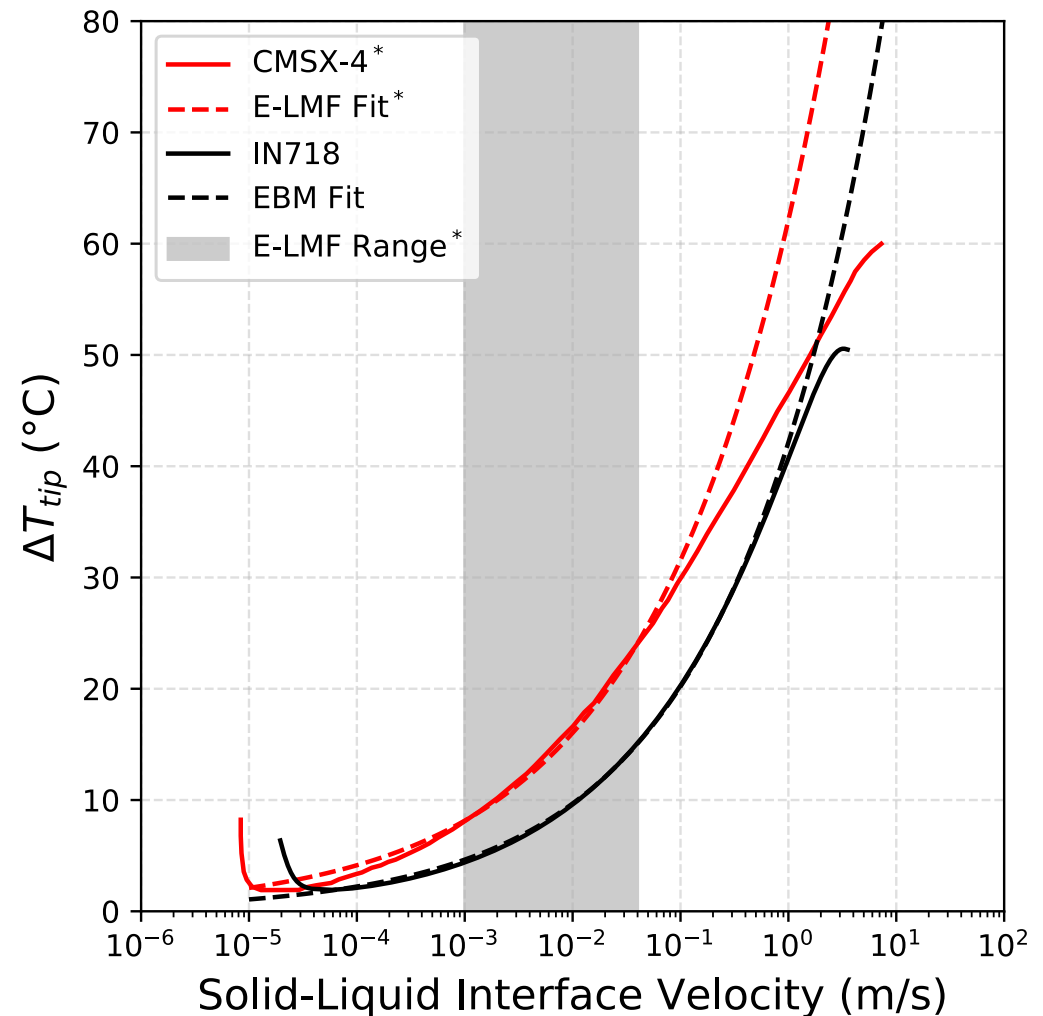
$$\Delta T_{tip} = (a \cdot R)^{1/n}$$



Kurz Giovanola Trivedi (KGT) model predicts undercooling at the dendrite tip

$$\Delta T_{tip} = (a \cdot R)^{1/n}$$

- a decreases by an order of magnitude (smaller equiaxed processing window)
 $1.25 \times 10^6 \rightarrow 1.23 \times 10^5$
- n decreases (larger equiaxed processing window)
 $3.4 \rightarrow 3.13$



Checklist for Columnar to Equiaxed Transition (CET) Model

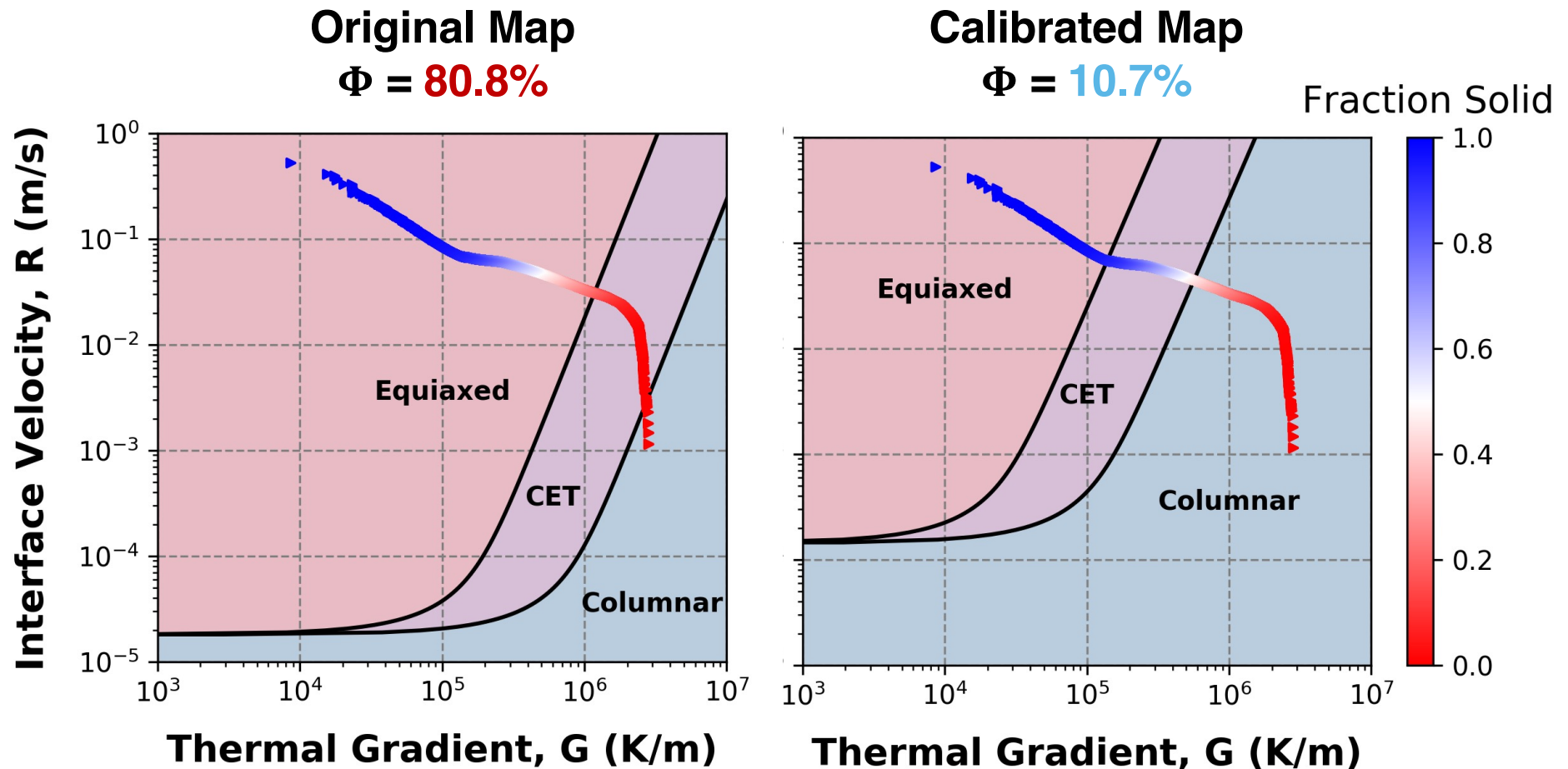
- Want to predict the formation of nucleated grains

$$\phi = 1 - \exp \left\{ \frac{-4\pi N_0 a^{3/n}}{3(n+1)^3} \left(\frac{R}{G^n} \right)^{3/n} \right\}$$

TRUCHAS	<input checked="" type="checkbox"/>	G = Thermal Gradient
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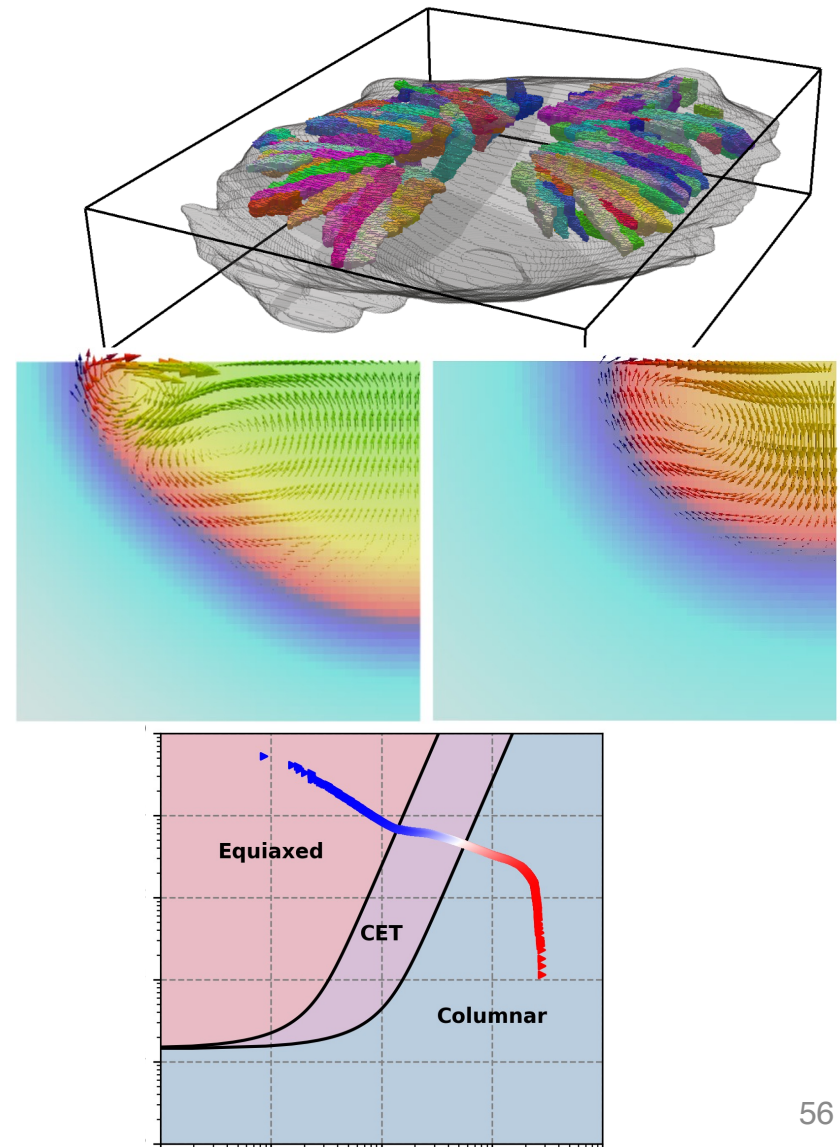
Calibrated processing map accurately predicts microstructure

- Measured $\Phi = 11.4\%$ from 3D data



Summary

- 3D provides direct measurement of ground truth microstructures for calibration of processing maps
- Advanced simulations can provide insight to microstructure evolution during solidification
- Processing maps are alloy- and processing-dependent, and must be calibrated for the specific application of interest



Thanks!

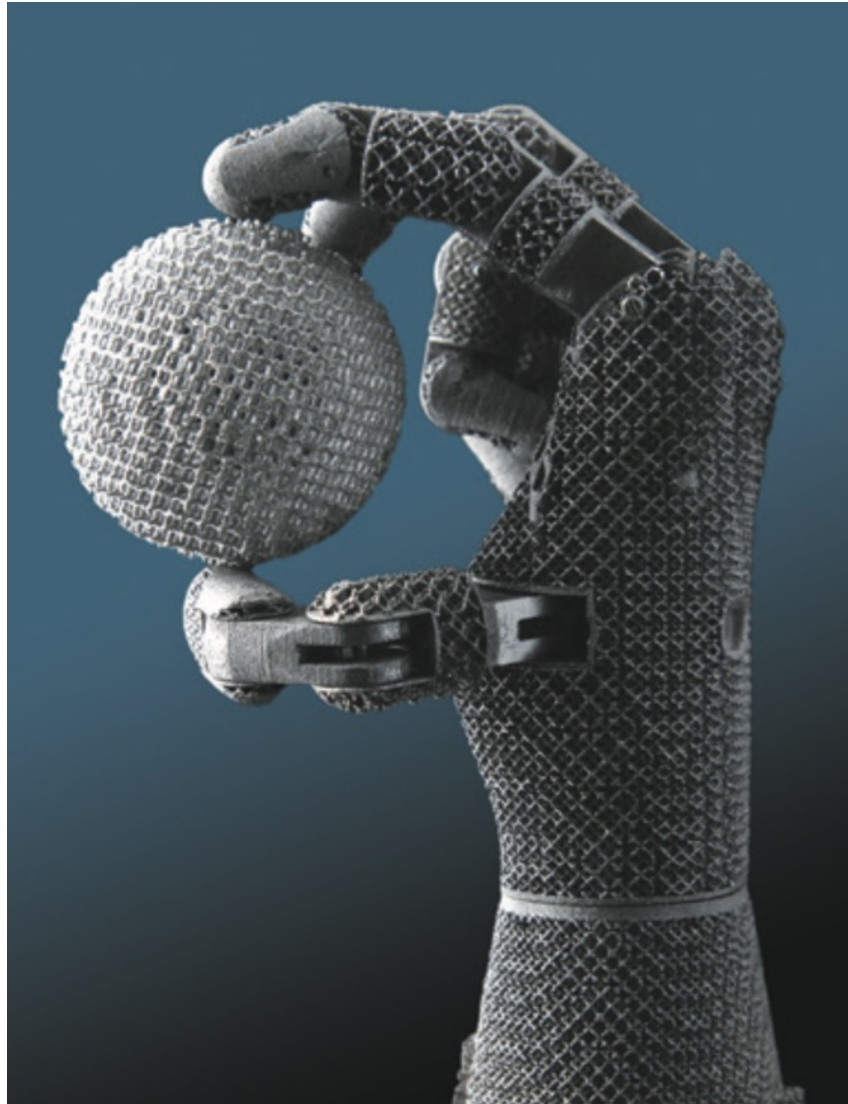


Image courtesy ORNL MDF