

# Supervisory Optimal Control for Photovoltaics Connected to an Electric Power Grid

This study was funded by the Laboratory Directed Research & Development (LDRD) program at Sandia National Laboratories.

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Special thanks to Dr. Ray Byrne at Sandia, for his technical review and programmatic leadership for this LDRD project.  
This paper approved as SAND2021-XXXX C.



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**Venue: 11th Solar & Solar Integration Workshop**  
**Presentation Number: Microgrid PR2021-06**

**Version: 1.0.0**

**Release Date: September 28, 2021**

**Revision Date: September 28, 2021**

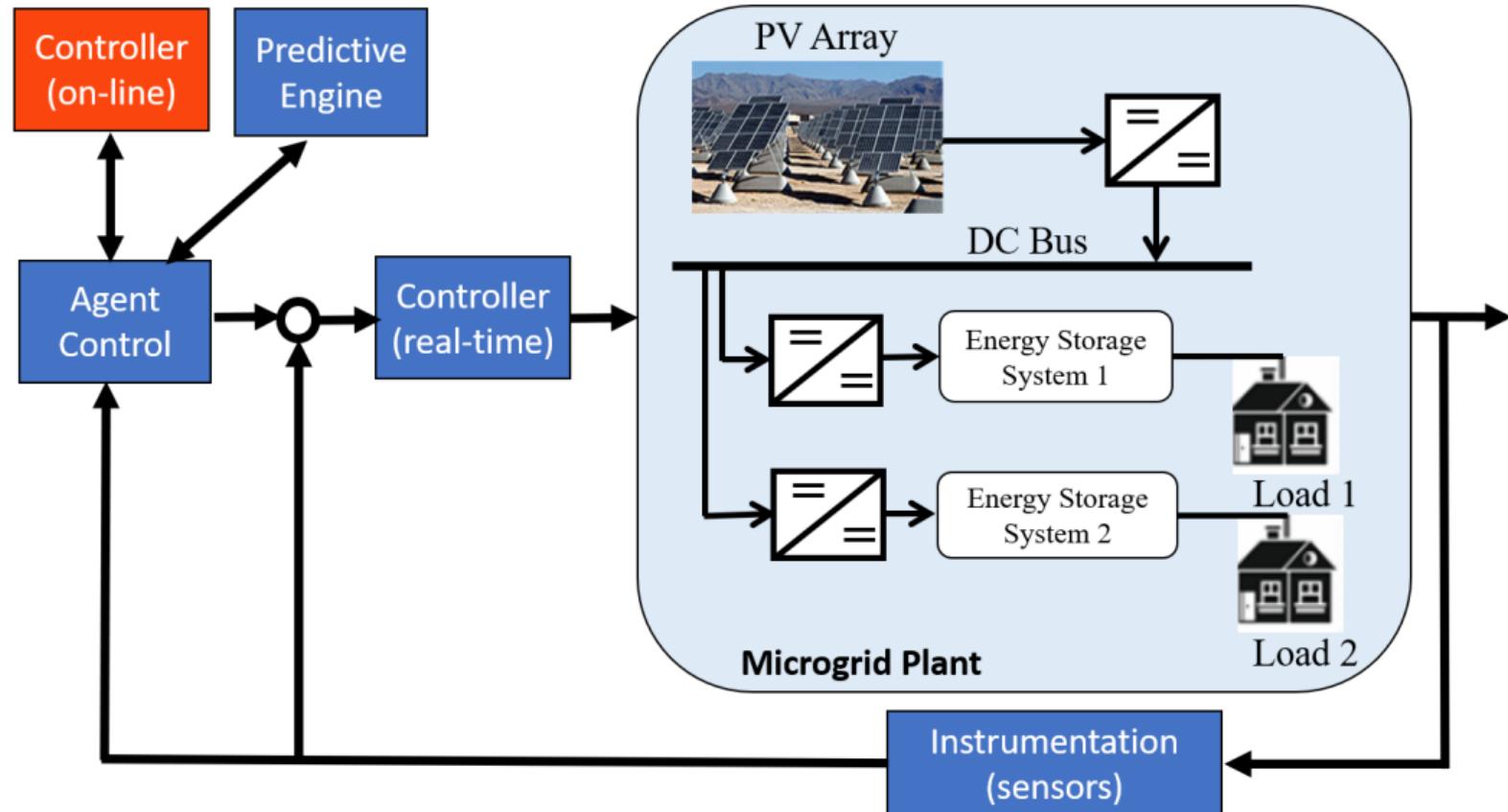
Control Design

Discretization

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Summary

# Summary of control design



## Summary of control design

- ▶ **Microgrid** - Single or networked power grid
- ▶ **Agents** - Software that coordinates how the different controls operate the microgrid based on information from the sensors and its own internal algorithms
- ▶ **Sensors** - Any instrumentation that provide information about the microgrid
- ▶ **Real-time Controller** - Control that provides fast, subsecond updates
- ▶ **On-line Controller** - Control that provides medium to long term planning
- ▶ **Predictive Engine** - Algorithm that provides long term forecasting for the microgrid

# Summary of control design

## On-line

- ▶ Executes in a variable amount of time
- ▶ Solves for new control while the system is in operation

## Optimal Control

- ▶ Control based on an optimization formulation
- ▶ Generally, solution time only deterministic for a linear-quadratic control

## Receding Horizon Control

- ▶ Behavior of system predicted over a time period called the planning horizon
- ▶ Control based on this prediction
- ▶ Control executed for as long as the prediction remains accurate, which is called the execution horizon

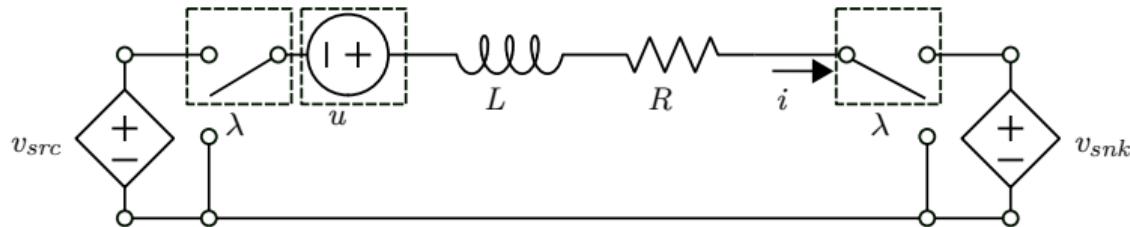
This presentation details an [optimal control](#) algorithm based on an [on-line optimization engine](#) that solves for a [receding-horizon control](#)

## High-level view of optimal control

<b>Minimize</b>	Use of storage devices Deviation from dispatchable load
<b>Subject to</b>	Series DC component dynamics Parallel DC component dynamics

Detail of microgrid components to come next

## Series DC components (S)



$$[\lambda]v_{src} + [u] = Li' + Ri + [\lambda]v_{snk}$$

$$i(0) = i_0$$

$$i_{min} \leq i \leq i_{max}$$

$$w' = -ui$$

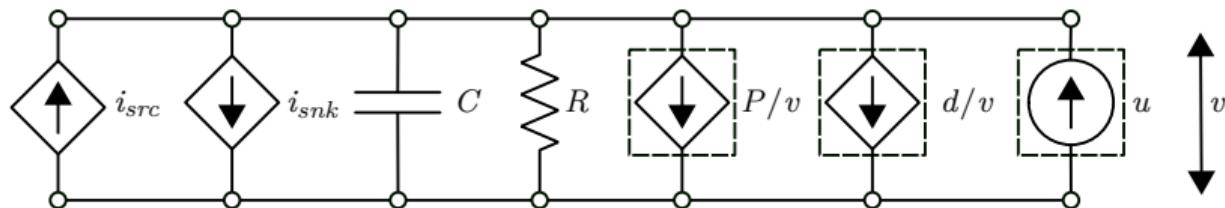
$$w(0) = w_0$$

$$0 \leq w \leq w_{max}$$

$$0 \leq \lambda \leq 1$$

Dotted squares denote optional components

## Parallel DC components (P)



$$\sum[\lambda_{src}]i_{src} + [u] = \sum[\lambda_{snk}]i_{snk} + Cv' + \frac{v}{R} + \left[ \frac{P}{v} \right] + \left[ \frac{d}{v} \right]$$

$$v = \text{const}$$

$$w' = -vu$$

$$w(0) = w_0$$

$$0 \leq w \leq w_{max}$$

$$0 \leq d$$

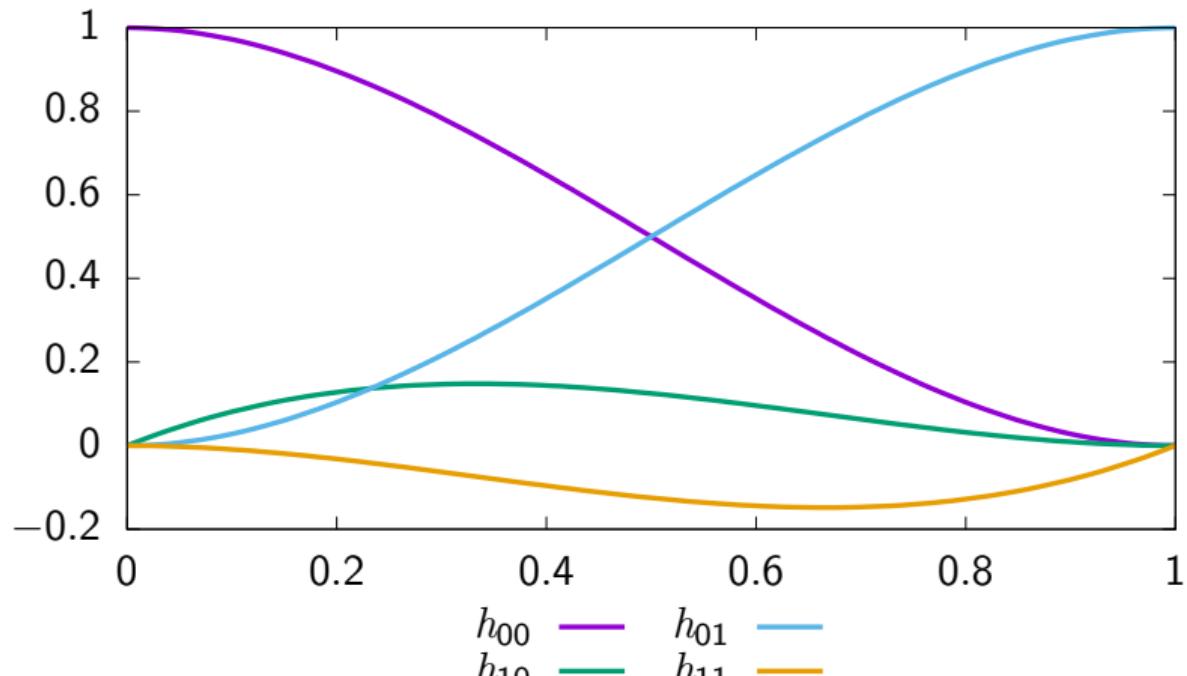
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## Hermite cubic splines



$$h_{00}(t) = (1 + 2t)(1 - t)^2$$

$$h_{01}(t) = t^2(3 - 2t)$$

$$h_{10}(t) = t(1 - t)^2$$

$$h_{11}(t) = t^2(t - 1)$$

## Orthogonal spline collocation method (OSCM)

- ▶ Represent each function by a Hermite cubic spline
- ▶ Satisfy dynamics at Gaussian quadrature (collocation) points
- ▶ Practical approach uses evaluation,  $E$ , and derivative,  $D$ , operators that map spline coefficients to collocation points. Allows differential equation

$$u' = -u$$

to be discretized as

$$D\alpha = -E\alpha$$

where  $\alpha$  represents the spline coefficients

- ▶ Convergence rate  $O(h^4)$  where  $h$  largest interval in mesh

## Useful Hermite spline properties

- ▶ Constant Bounds - Hermite polynomial

$$p(t) = \alpha_1 h_{00}(t) + \alpha_2 h_{10}(t) + \alpha_3 h_{01}(t) + \alpha_4 h_{11}(t)$$

is bounded between  $l$  and  $u$  on the interval  $[0, 1]$  whenever

$$3l \leq 3\alpha_1 + \alpha_2 \leq 3u$$

$$3l \leq 3\alpha_1 - \alpha_2 \leq 3u$$

$$3l \leq 3\alpha_3 + \alpha_4 \leq 3u$$

$$3l \leq 3\alpha_3 - \alpha_4 \leq 3u$$

- ▶ Nonlinear Bounds - Approximate nonlinear bound with Hermite spline and then bound the difference between the original polynomial and this approximation
- ▶ Integration - Given the mesh  $\Omega = (t_0, \dots, t_{\text{nele}})$ , spline  $s$ , and collocation points  $C$ , then

$$\int_{t_0}^{t_{\text{nele}}} s(t) dt = \sum_{k=0}^{\text{nele}-1} (t_{k+1} - t_k)(s(C_{2k+1}) + s(C_{2k+2}))$$

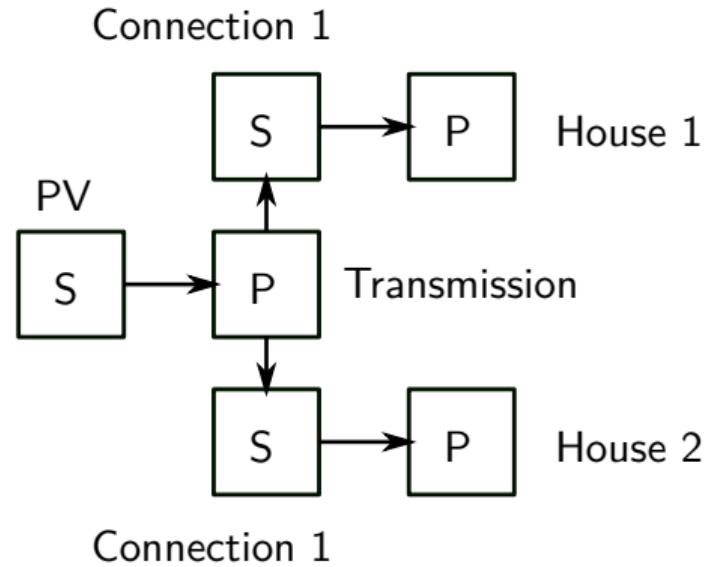
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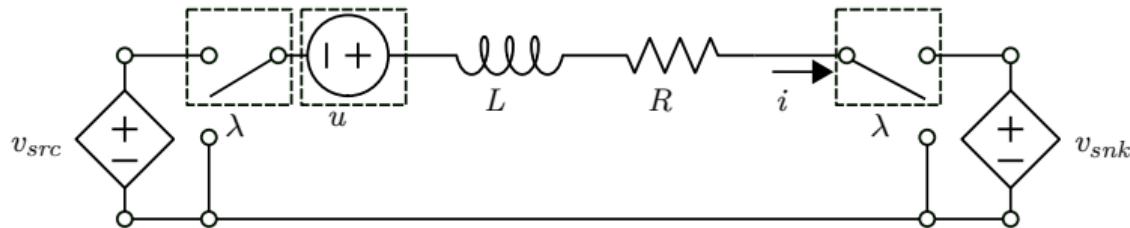
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## Topology of the microgrid

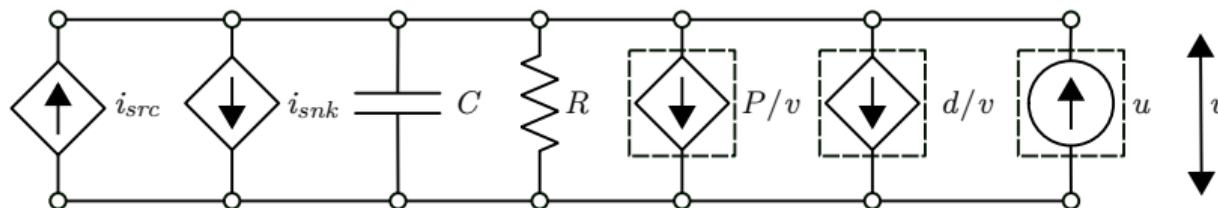


## Microgrid parameters (PV)



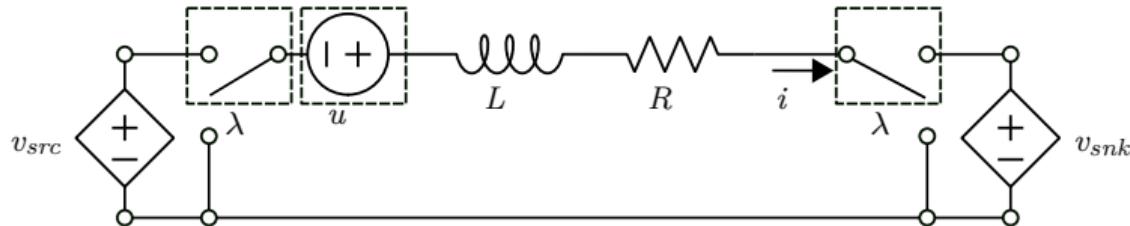
Parameter	Value	Info
$v_{src}$	110 V	
$v_{snk}$	$v_{trans}$	Transmission
$[i_{min}, i_{max}]$	[0,Variable] A	Generation given by the NREL code SAM with 5 kW max power
$L$	0.001 H	
$R$	0.121 $\Omega$	250 W parasitic loss @ 5 kW
$w_{max}$	_____	No storage, $u$

## Microgrid parameters (Transmission)



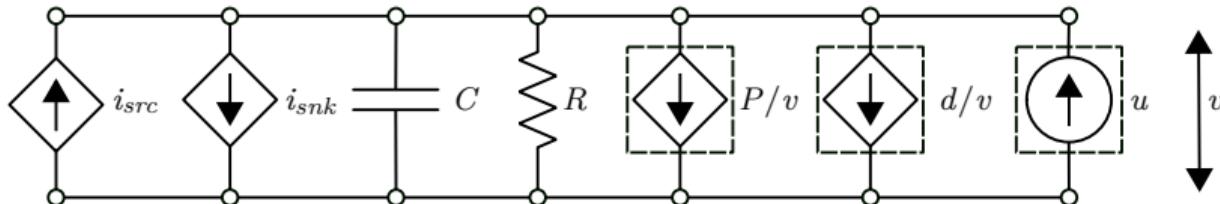
Parameter	Value	Info
$i_{src}$	$i_{pv}$	PV
$i_{snk}$	$i_{conn\ 1\ and\ 2}$	Connection
$v$	200 V	
$C$	_____	Constant voltage
$R$	160 $\Omega$	250 W parasitic loss
$P$	_____	None
$D$	_____	None
$w_{max}$	_____	No storage, $u$

## Microgrid parameters (Connection)



Parameter	Value	Info
$v_{src}$	$v_{trans}$	Transmission
$v_{snk}$	$v_{house\ 1\ or\ 2}$	House
$[i_{min}, i_{max}]$	_____	No bounds on power transfer
$L$	0.001 H	
$R$	0.05 $\Omega$	
$w_{max}$	_____	No storage, $u$

## Microgrid parameters (House)



Parameter	Value	Info
$i_{src}$	$i_{conn\ 1\ and\ 2}$	Connection
$i_{snk}$	_____	None
$v$	220 V	
$C$	_____	Constant voltage
$R$	193.6 $\Omega$	250 W parasitic loss
$P$	Variable	Load profile taken from sampled data collected from houses in Albuquerque, NM
$D$	_____	None
$w_{max}$	3 or 4 MJ	Local storage at each house, 0.83 kWh for house 1 and 1.11 kWh for house 2

## Scenario overview

### Goal

- ▶ Meet demand when combined loads exceed generation capacity
- ▶ Coordinate use of storage to minimize storage use and keep storage 90% full

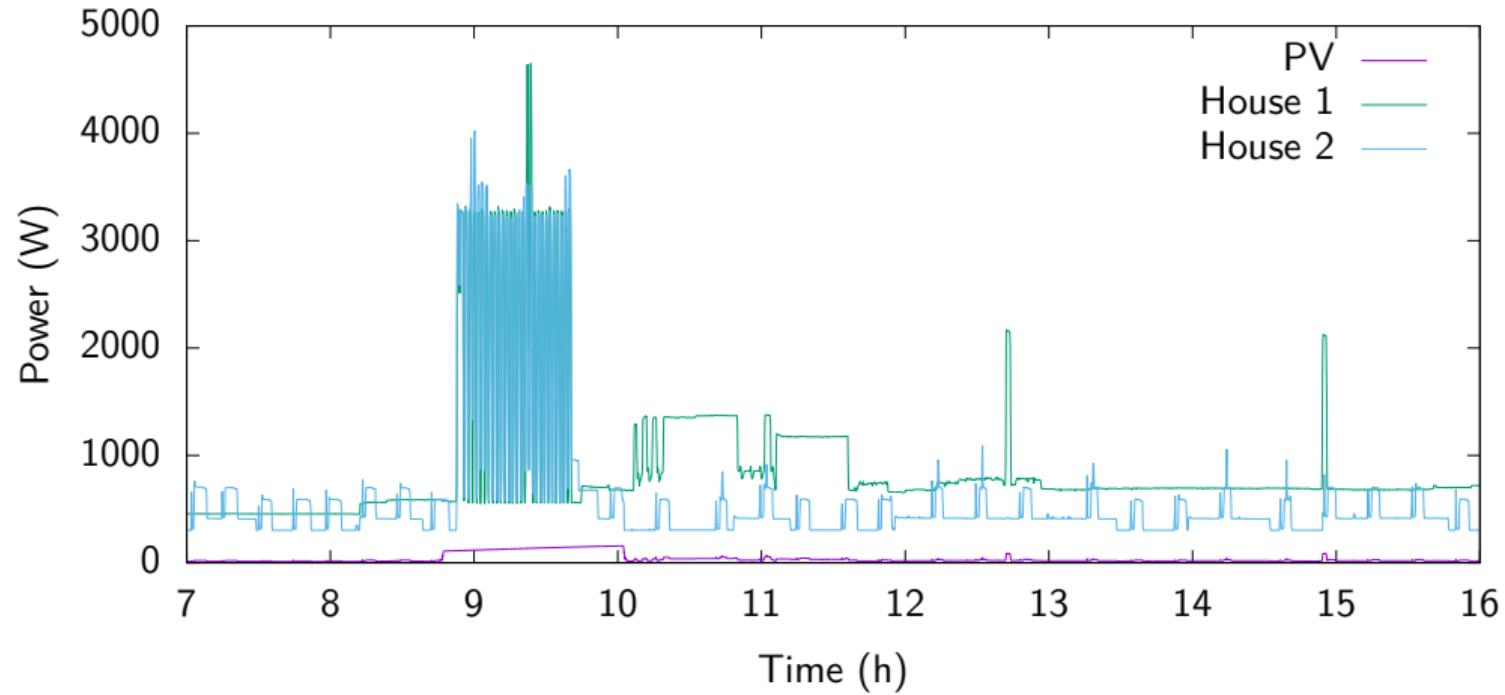
### Setup

- ▶ Scenario lasts for 9 h, 0700-1600
- ▶ Generation capacity estimated using the NREL code SAM with 5 kW max generation using averaged historical weather information for Albuquerque, NM on a typical May 1
- ▶ Load sampled directly from two houses in Albuquerque, NM in 1 s intervals and averaged over 15 s intervals
- ▶ Storage devices located at houses

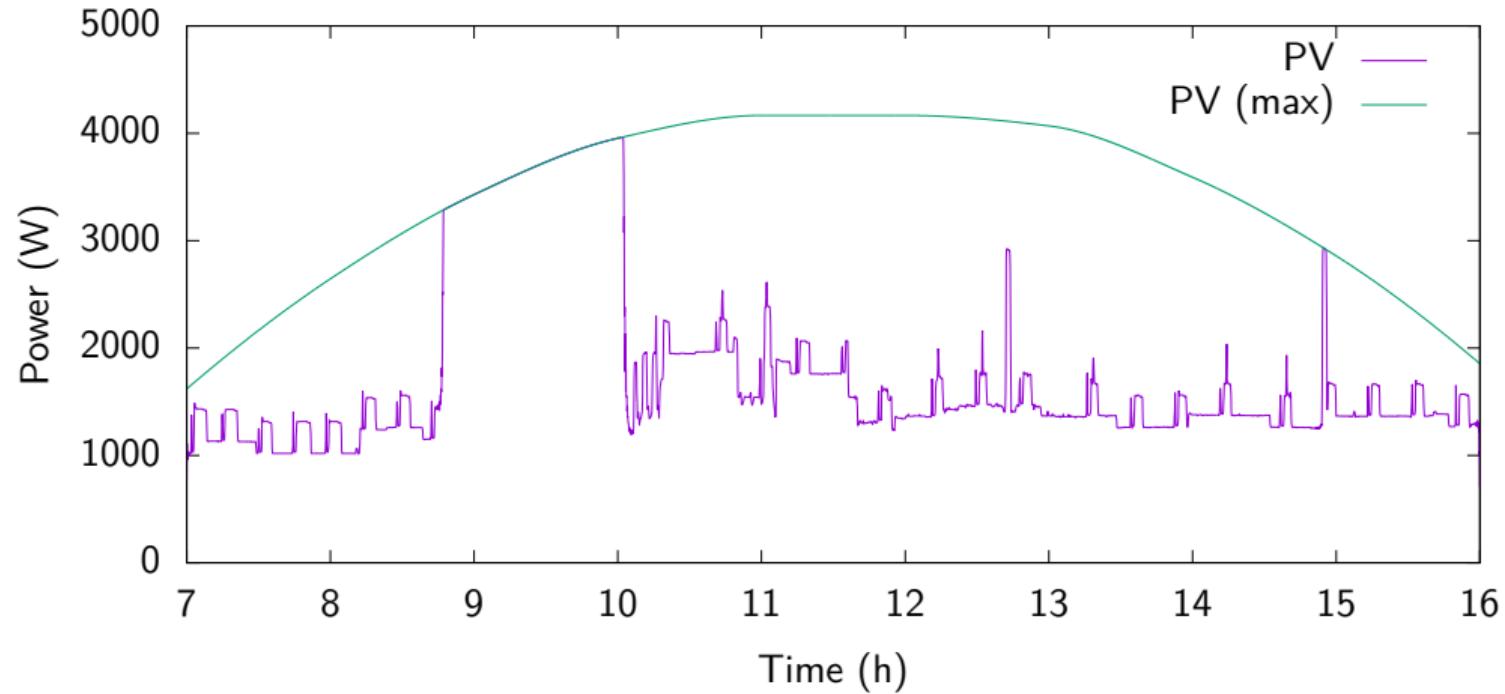
### Results

- ▶ Load demands met
- ▶ Storage only used when generation exceeded demand

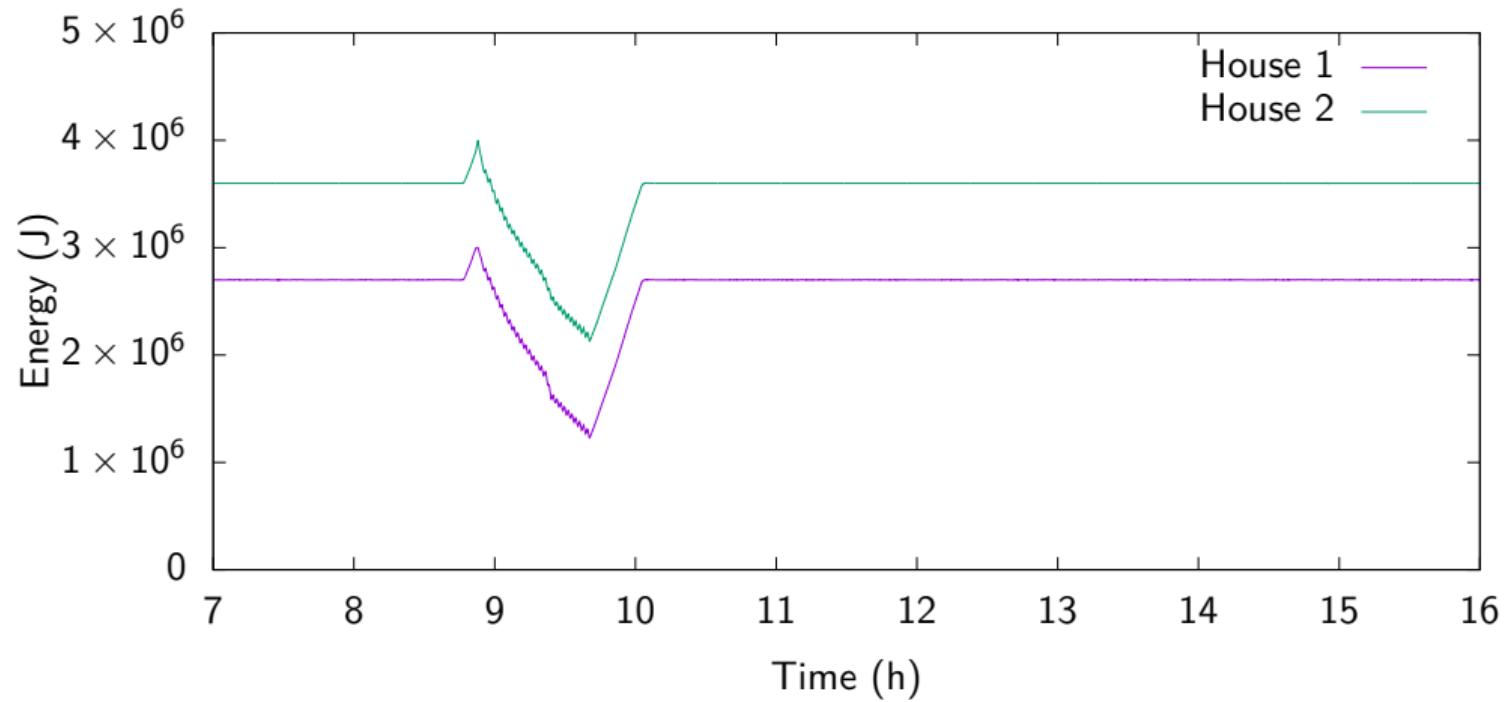
## Power used by loads



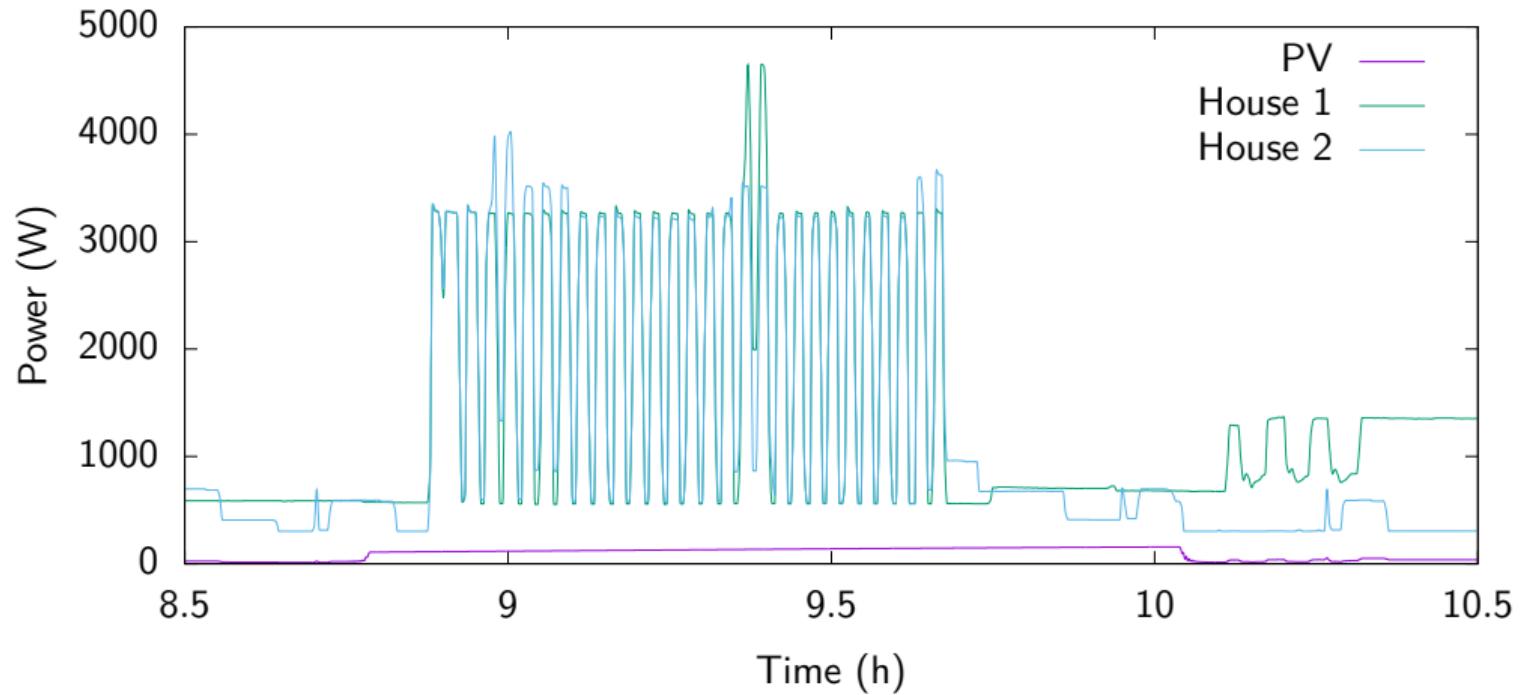
## Power generation



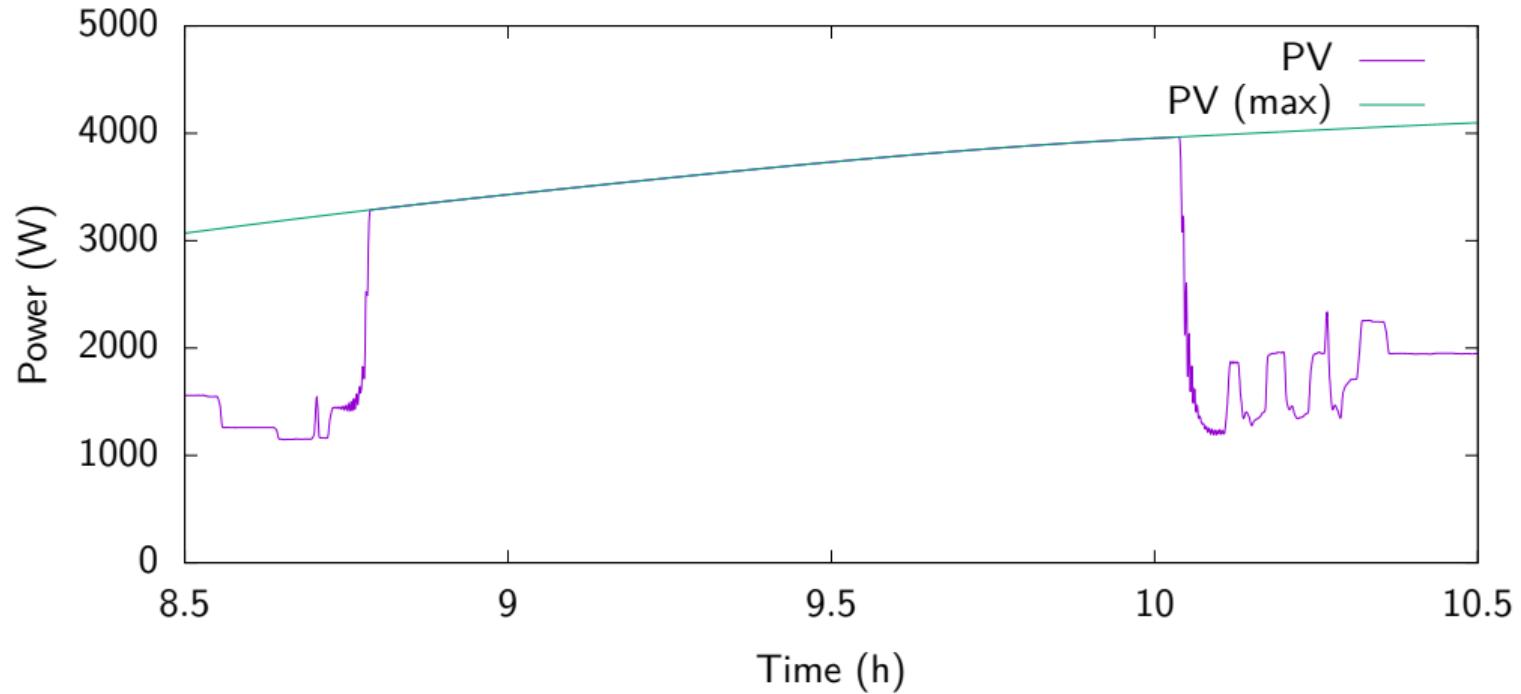
## Energy in the storage



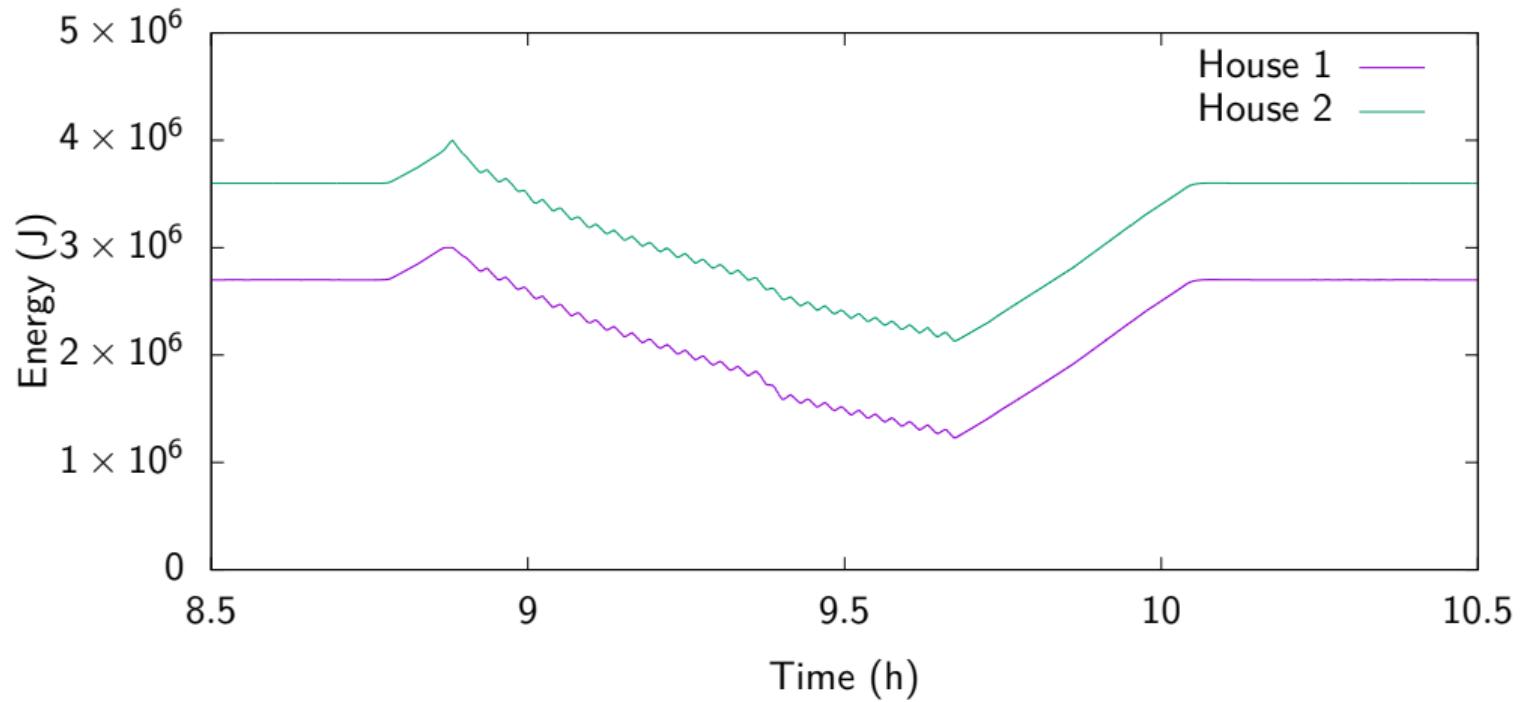
## Power used by loads (zoomed)



## Power generation (zoomed)



## Energy in the storage (zoomed)



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# Summary

## Current Results

- ▶ Nested control architecture consisting of
  - ▶ Agents that coordinate information between the microgrid and the various control algorithms
  - ▶ Real-time controller
  - ▶ Predictive engine
  - ▶ On-line controller
- ▶ Hermite cubic splines used to discretize DAE and bound state, control parameters
- ▶ Obtained the optimal control of a microgrid driven by collected, real-world data
- ▶ Coordinated use of storage devices

## Future Work

- ▶ Perform additional case studies with other scenarios
- ▶ Run scenarios with entire, combined control framework
- ▶ Refine and mature software stack

## Contact



For additional questions or interest please contact [joe@optimojoe.com](mailto:joe@optimojoe.com)