



Subcritical Fracturing of Calcite Single Crystals and Grain Packs

Anastasia G. Ilgen,¹ R. Charles Choens,² and Jennifer Wilson²

¹Geochemistry Department; ²Geomechanics Department
Sandia National Laboratories



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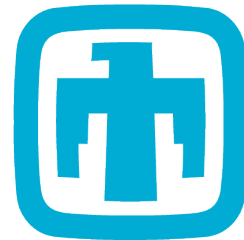
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Overview: theory of chemically-assisted fracturing



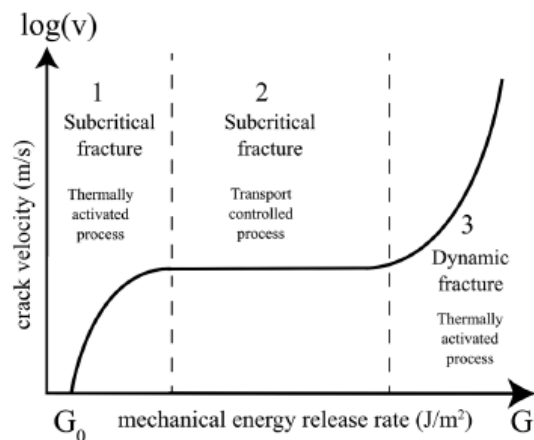
Griffith theory:

$$U = (U_E - W_L) + U_S$$

the internal energy of the system (U), the elastic potential energy (U_E), the external work (W_L), the energy from the added surface area of the crack (U_S).

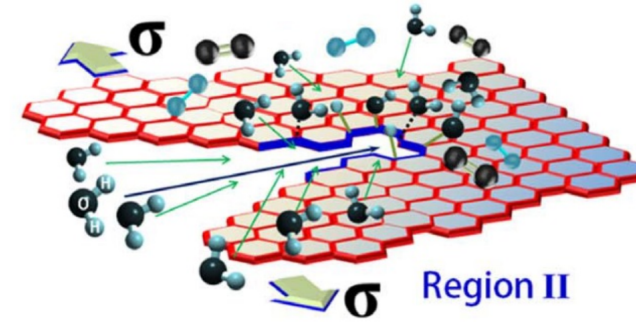
Constitutive modeling of subcritical crack growth:

$$v = 2 \frac{kT}{h} a_0 \exp\left(\frac{-\Delta F}{kT}\right) \sinh\left(\alpha \frac{G - G_0}{kT}\right)$$

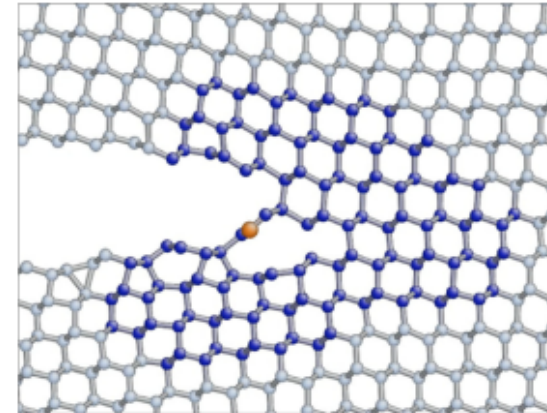


v is crack velocity, k is Boltzmann's constant, h is Plank's constant, G is mechanical energy release (G_0 is theoretical limit), a_0 is characteristic atomic spacing, α is activation area, ΔF is apparent activation barrier.

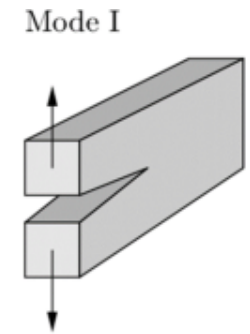
Bergsaker et al., 2016



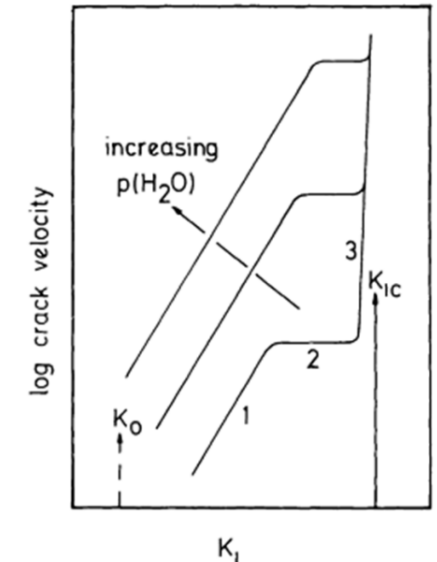
Hwangbo et al., 2014



Bitzek et al., 2005



Atkinson and Meredith, 1987



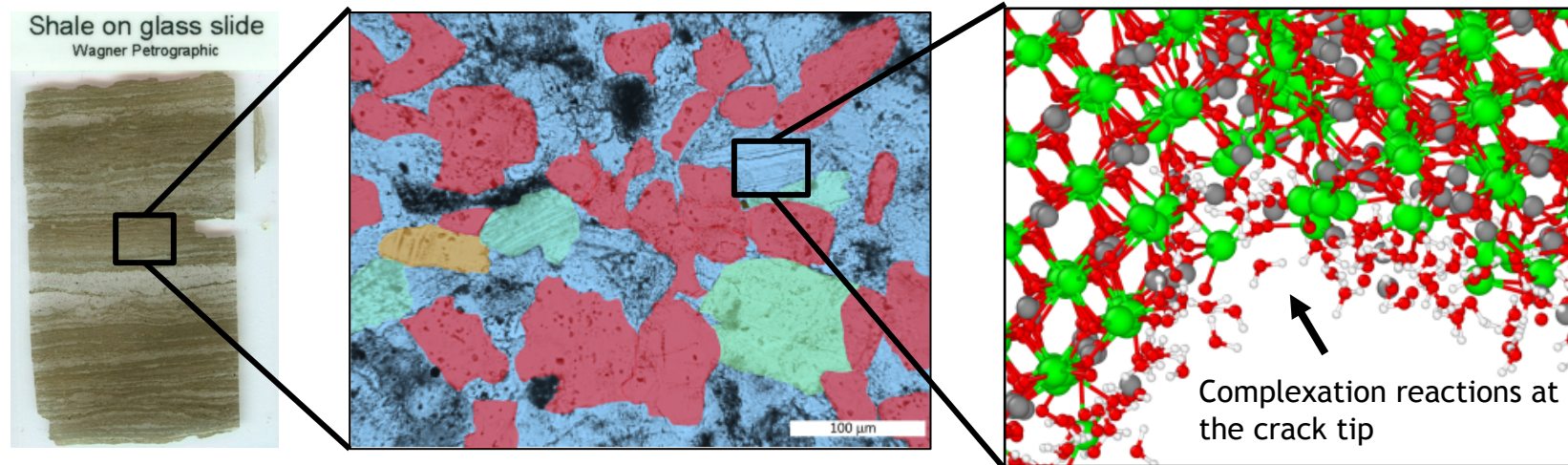
Schematic stress intensity factor (K_i) and crack velocity diagram for tensile crack growth by stress corrosion. K_{ic} is the fracture toughness and K_0 is the stress corrosion limit.

Chemically-assisted fracturing in calcite: hypothesis



Science Question: How and why do chemical complexation reactions at a single crack tip change *in situ* fracture behavior?

Hypothesis: With increasing favorability of the cation-ligand complex, the velocity of subcritical crack growth decreases, and the effective fracture toughness increases.



- Fracturing in rocks can occur through intergranular cement, or through mineral grains. Calcite (CaCO_3) and quartz (SiO_2) cements are common intergranular phases in sedimentary rocks;
- Previous studies on subcritical fracture show that:
 - Activity of H_2O controls weakening of chalk ^[1]
 - Dissolution at fracture tip controls fracture growth ^[2,3]
 - Changes in surface energy control fracture propagation ^[4-7]

[1] Risnes et al., 2005

[2] Atkinson, 1984

[3] Royne et al., 2011

[4] Rostom et al., 2012

[5] Griffith, 1921

[6] Kermode et al., 2013

[7] Bergsaker et al., 2016

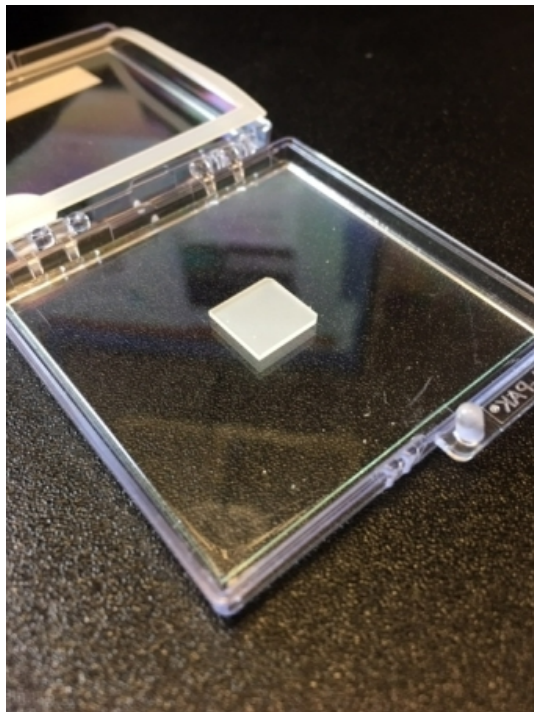
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Chemical controls on the propagation rate of fracture in calcite

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A. G. Ilgen¹, W. M. Mook², A. B. Tigges¹, R. C. Choens¹, K. Artyushkova¹ & K. L. Jungjohann²



micron → centimeter

minutes → days

single crystal → grain pack

dilute aqueous solutions

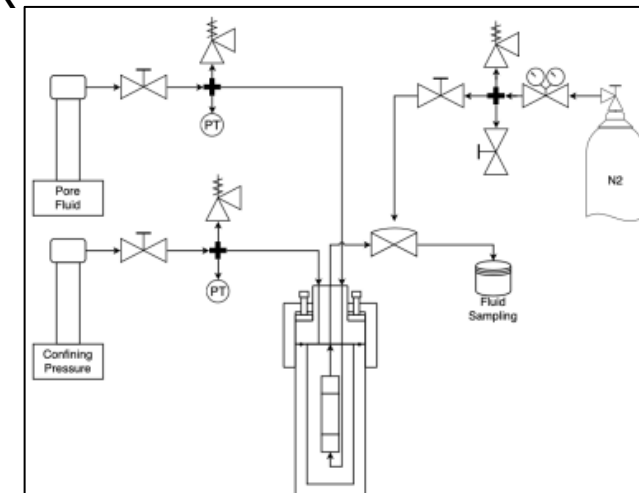
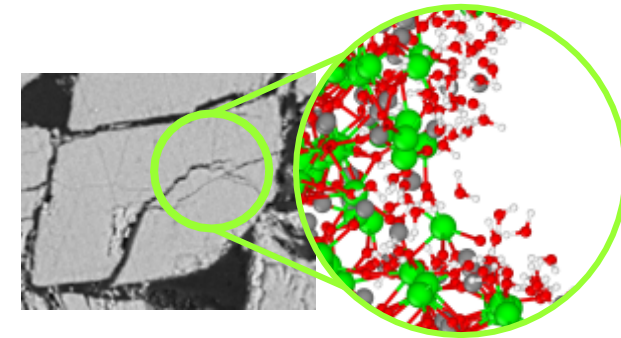
→ 0.5M

brines

Submitted paper:

Strengthening of Calcite Assemblages through Chemical Complexation Reactions

R. C. Choens, J. Wilson, and A. G. Ilgen

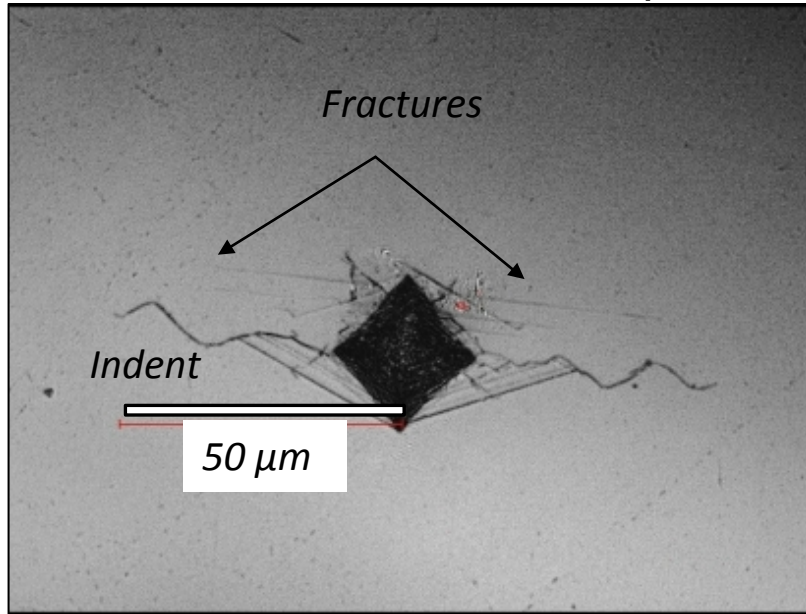


Part I: Chemical controls on subcritical fracture in calcite

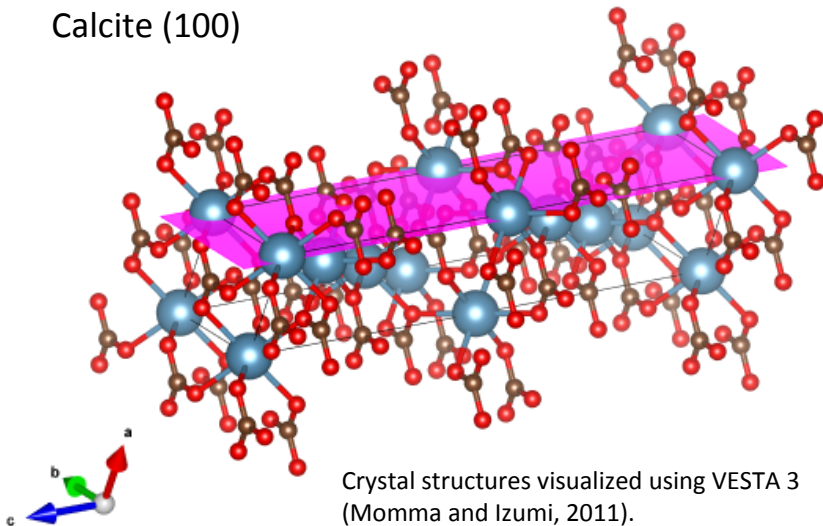
Methods: nanoindentation and in situ crack growth



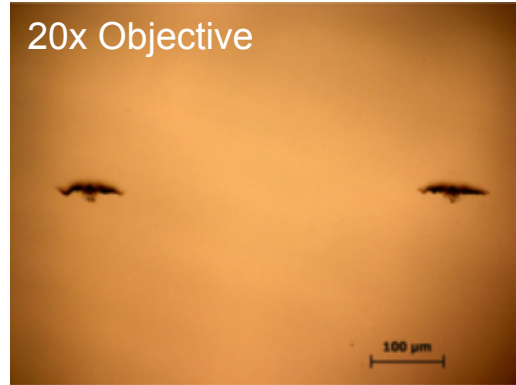
Calcite Indentation, Vickers tip, 400 mN



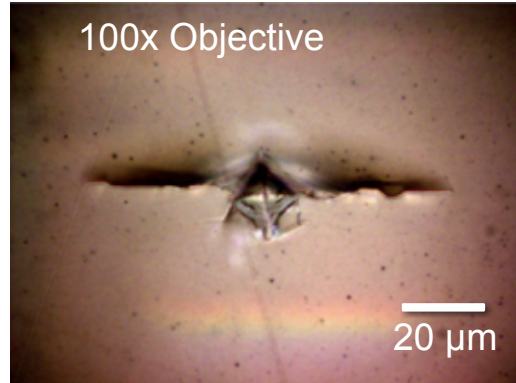
Calcite (100)



20x Objective



100x Objective



Fracture toughness ^[1]:

$$\frac{P}{c^{3/2}} = \frac{1}{\xi} \times \left(\frac{H}{E}\right)^{1/2} \times T$$

[1] Lawn and Cook, 2012

Vickers tip

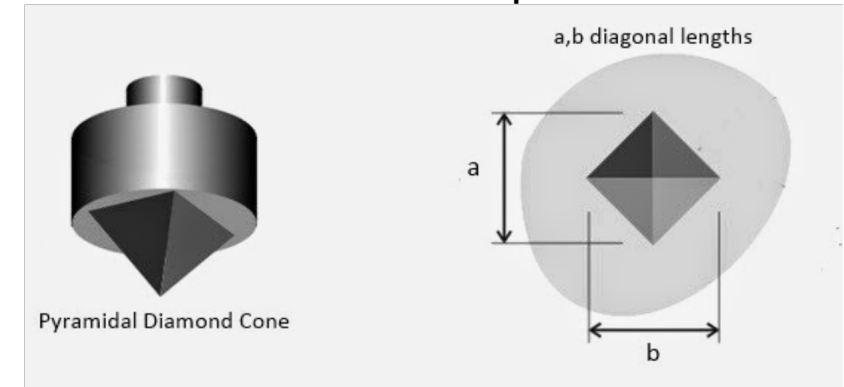


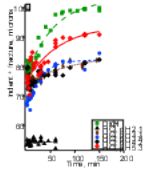
Image from: <http://www.weldpedia.com/2014/10/macrosopic-and-microscopic-examination.html>

- Laboratory experiments to measure fracture propagation rate *in situ* as a function of chemical composition of the fluid;
- Single crystal calcite (100) indented using Vickers indenter tip at 400 mN force to induce cracking;
- Fractures are imaged *in situ* using optical microscope Nikon Eclipse 80i and SPOT 7.2 camera **Hagen, et al., 2018**

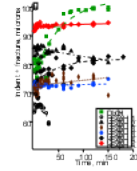
Results: fracture growth rate



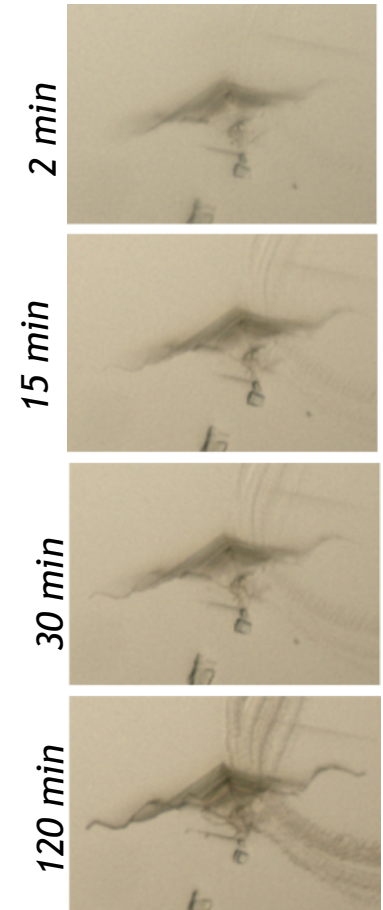
HCl



H₂SO₄



pH 5

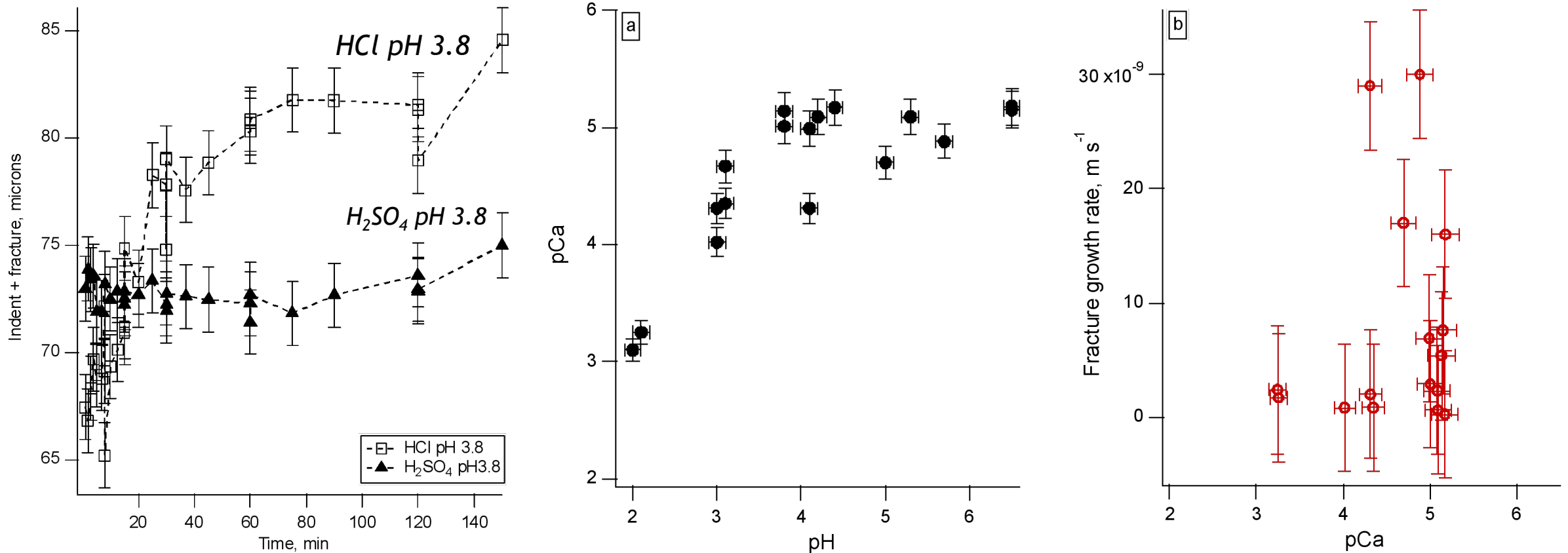


- The propagation rate of subcritical fracture measured *in situ* varied from $1.6 \times 10^{-8} \text{ m s}^{-1}$ to $2.4 \times 10^{-10} \text{ m s}^{-1}$.

Ilgen, et al., 2018

Scientific Reports, 8, 164656.

Results: what controls crack growth?



- Propagation rate of fracture in calcite is dependent on the anion.
- No correlation between the dissolution rate of calcite and subcritical fracture growth.
- Positive correlation between pCa and pH for all examined reactors; $pCa = -\log_{10}[Ca^{2+}]$;
- No correlation observed between pCa (proxy for the ξ -potential) and fracture propagation rates

Ilgen, et al., 2018

Scientific Reports, 8, 164656.

Results: what controls fracture growth?



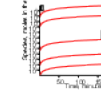
H₂O



HCl



H₂SO₄

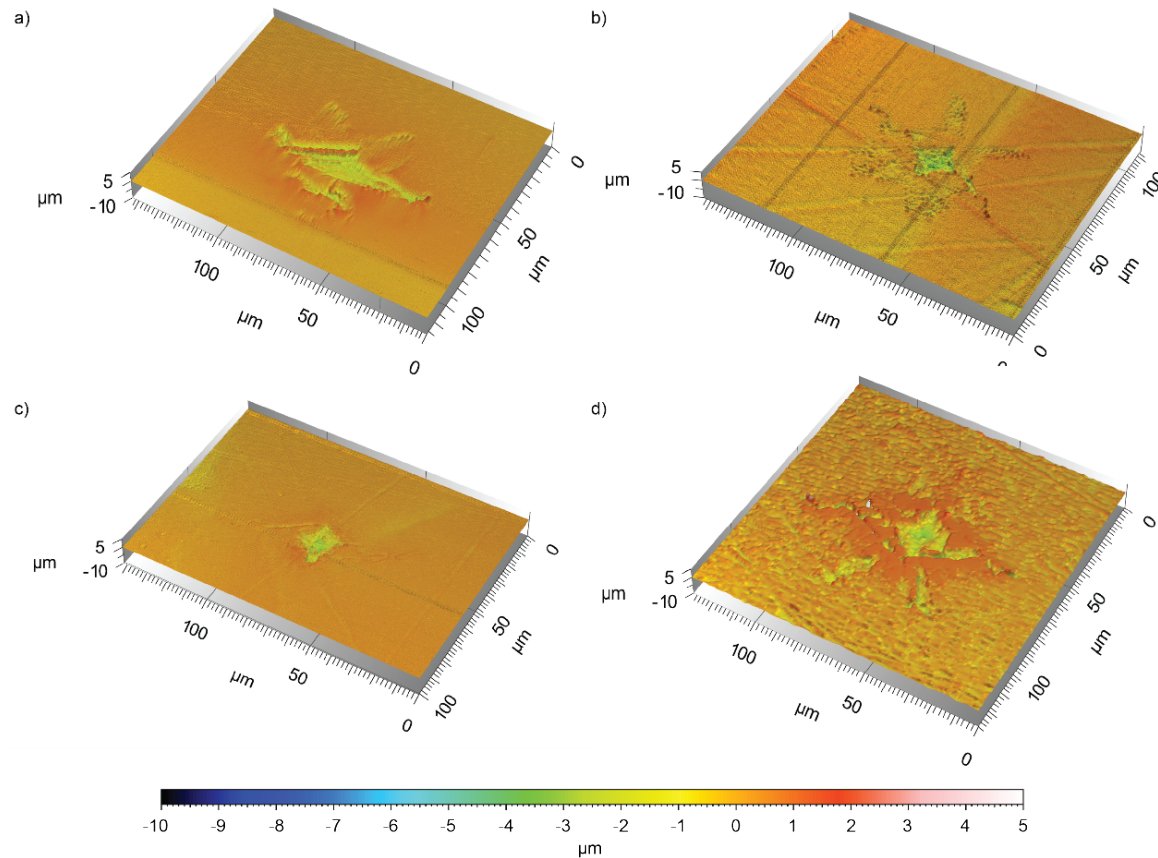


K_{β} for CaCO_3 is $10^{-7.128}$; K_{β} for CaCl^+ is $10^{0.7}$; and K_{β} for CaSO_4 is $10^{2.32}$

Ilggen, et al., 2018

Scientific Reports, 8, 164656.

Results: surface morphology and fracture toughness



(a) Sample exposed to H₂SO₄ at pH 2.0 for 150 minutes; (b) Sample exposed HCl at pH 3.8 for 120 minutes; (c) Sample exposed to fracking fluid at pH 4.1 for 180 minutes; and (d) Sample exposed to DI H₂O for 1140 minutes.

[1] Lawn and Cook, 2012

Fracture toughness ^[1]:

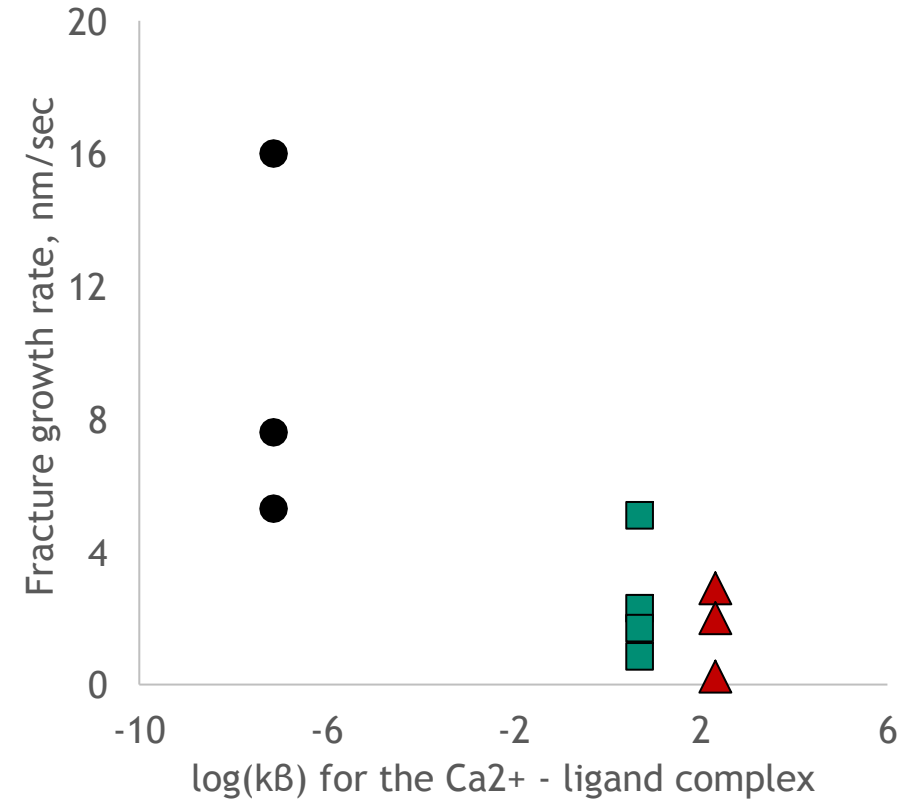
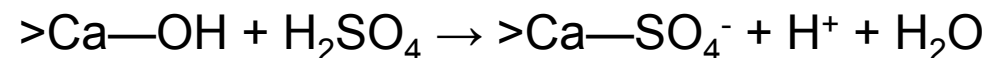
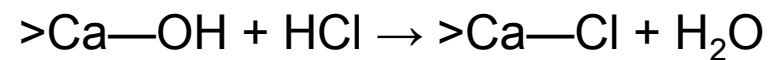
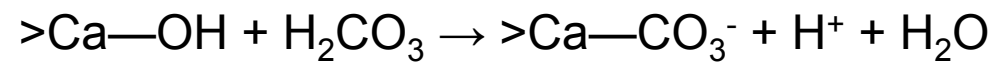
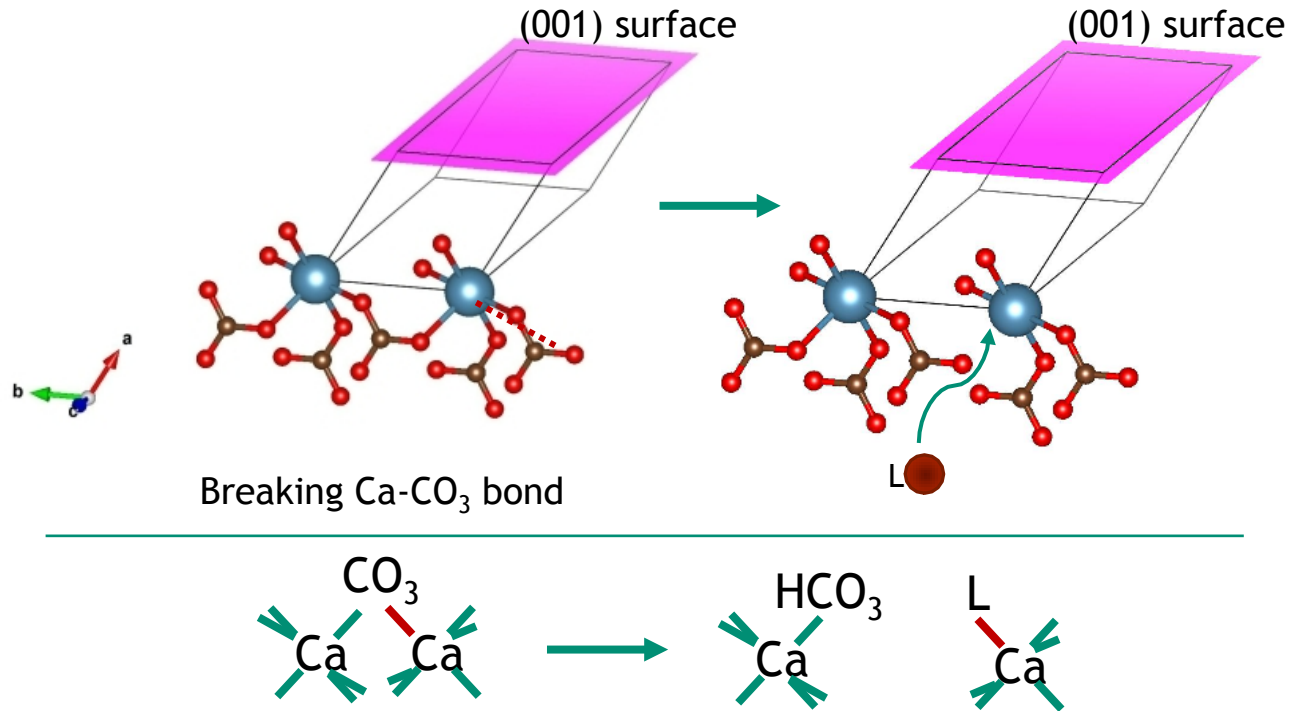
$$\frac{P}{c^{3/2}} = \frac{1}{\xi} \times \left(\frac{H}{E}\right)^{1/2} \times T$$

- The estimated fracture toughness prior to *in situ* fracture growth experiment was 0.10 – 0.16 MPa m^{1/2}
- Fracture toughness at the end of the fracture growth experiment decreased by 0.01-0.05 units.
- The fracture width, measured on the surface of the sample, increased with decreasing pH, in agreement with enhanced calcite surface dissolution with decreasing pH.

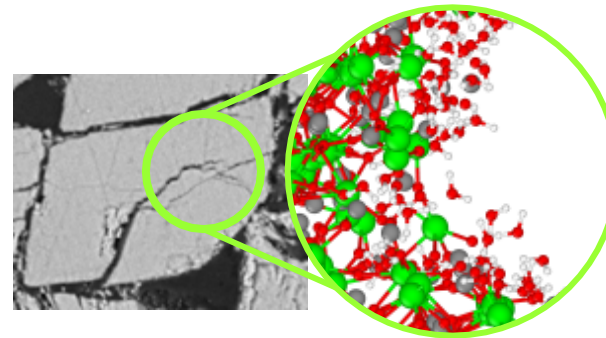
Ilgen, et al., 2018

Scientific Reports, 8, 164656.

Results: Conceptual model



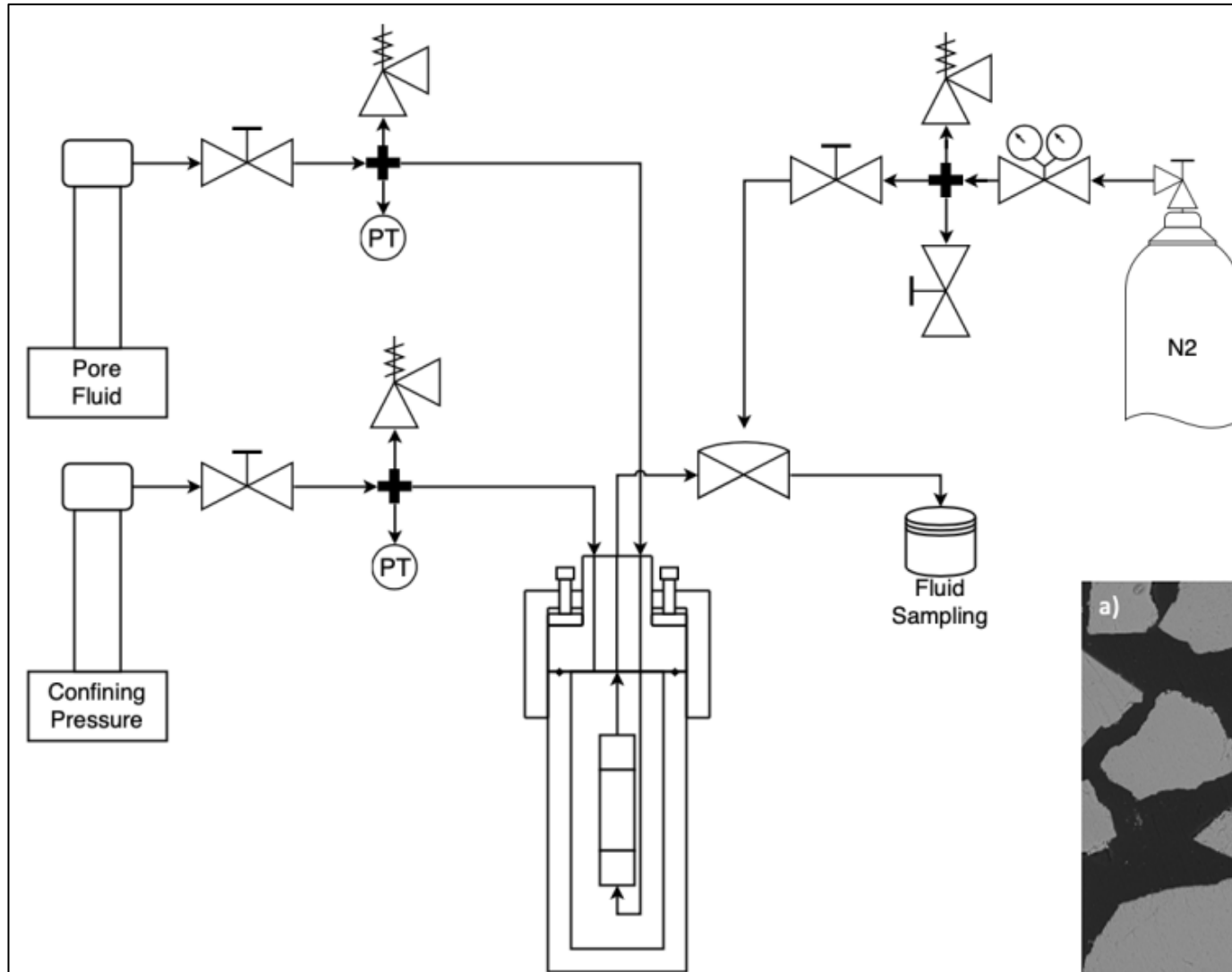
Part II: Strengthening of Calcite Assemblages through Chemical Complexation Reactions



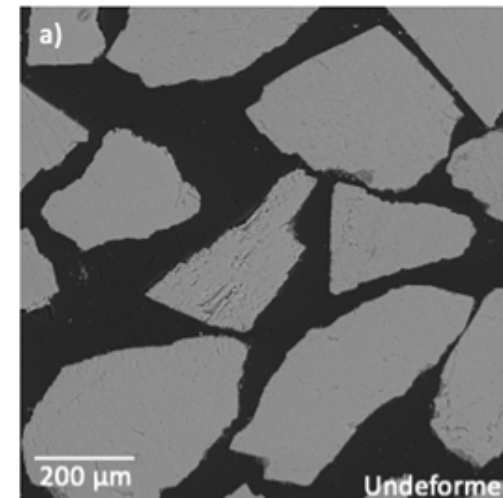
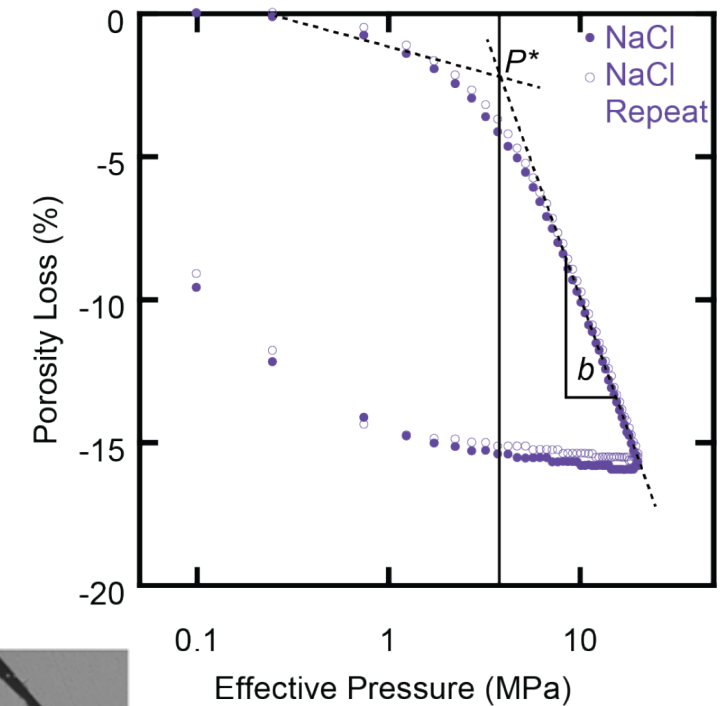
Experimental apparatus for consolidation tests



Schematic of consolidation apparatus

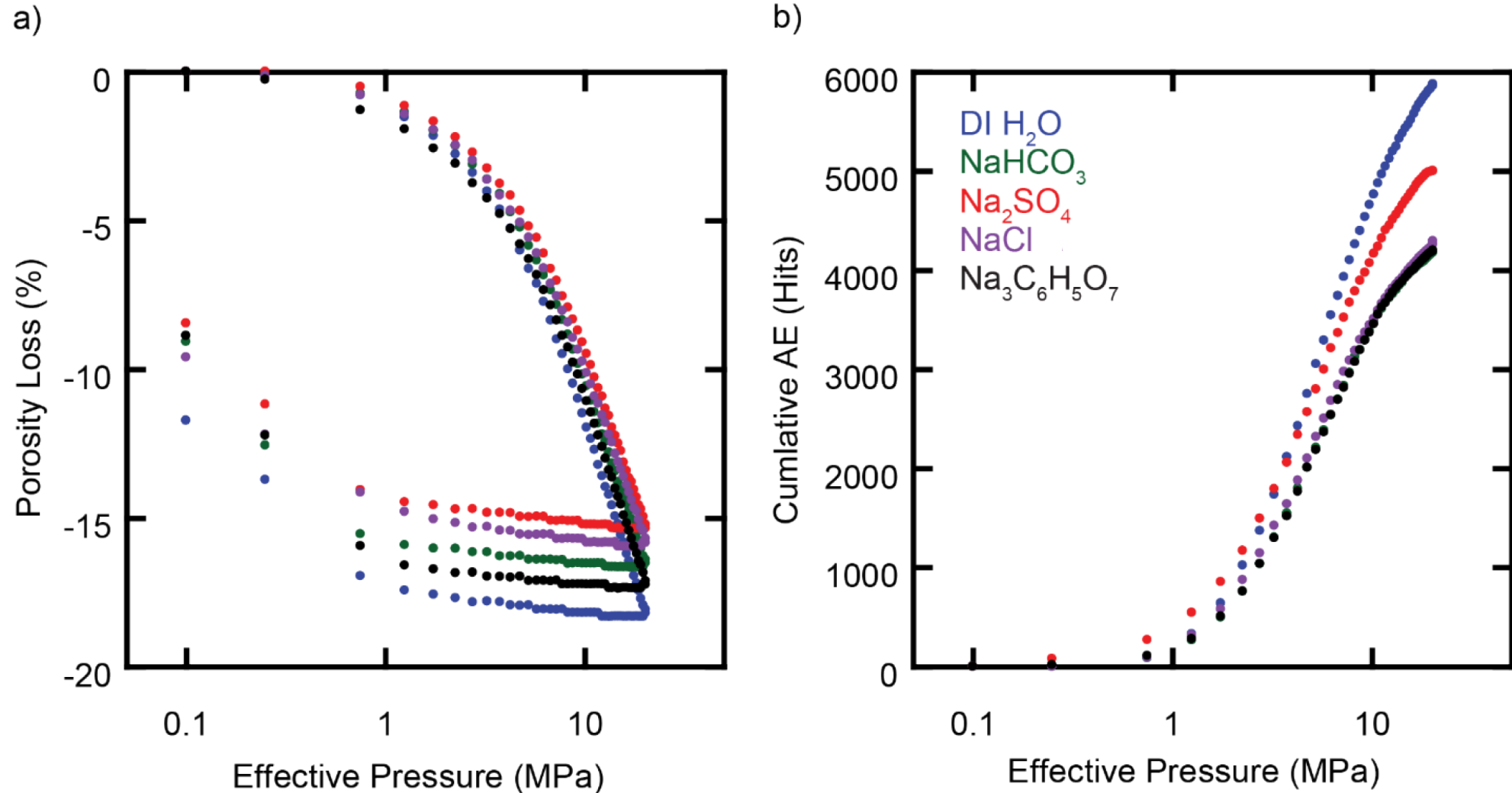


Consolidation curves



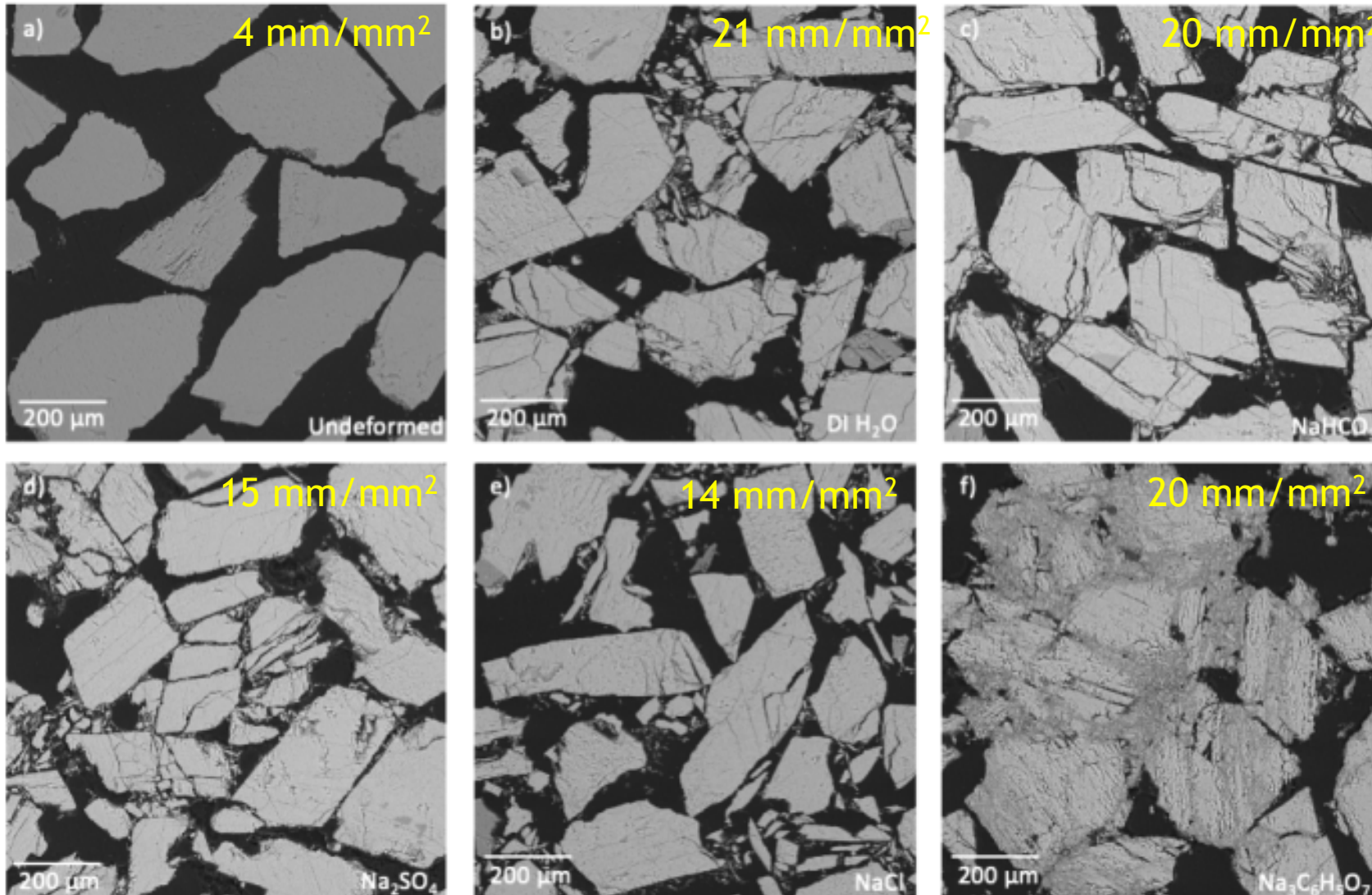
Starting calcite material, sieved to a grain size of 300-355 μm .

Results: porosity loss and acoustic emissions



a) Consolidation curves for granular calcite deformed with different interstitial pore fluids, showing porosity loss versus log effective pressure. b) Cumulative Acoustic Emissions (AE) during consolidation versus log effective pressure.

Results: microfracturing



- Scanning electron microscopy (SEM): a) Starting calcite material, sieved to a grain size of 300-355 μm .
- Samples consolidated in the presence of b) DI H₂O, c) NaHCO₃, d) Na₂SO₄, e) NaCl, and f) Na₃C₆H₅O₇.
- Fragmentation of grains and incorporation of crushed grains into interstitial pore spaces in all consolidated samples.
- Na₃C₆H₅O₇ diffusion is slower compared to other anions, it doesn't reach crack tip as it propagates.

Microfracture density depends on the fluid type and follows the sequence:

DI H₂O > Na₃C₆H₅O₇ > NaHCO₃ > Na₂SO₄ > NaCl

Choens, et al., 2021

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Results: microfracturing



Table 1. Consolidation results for granular calcite.

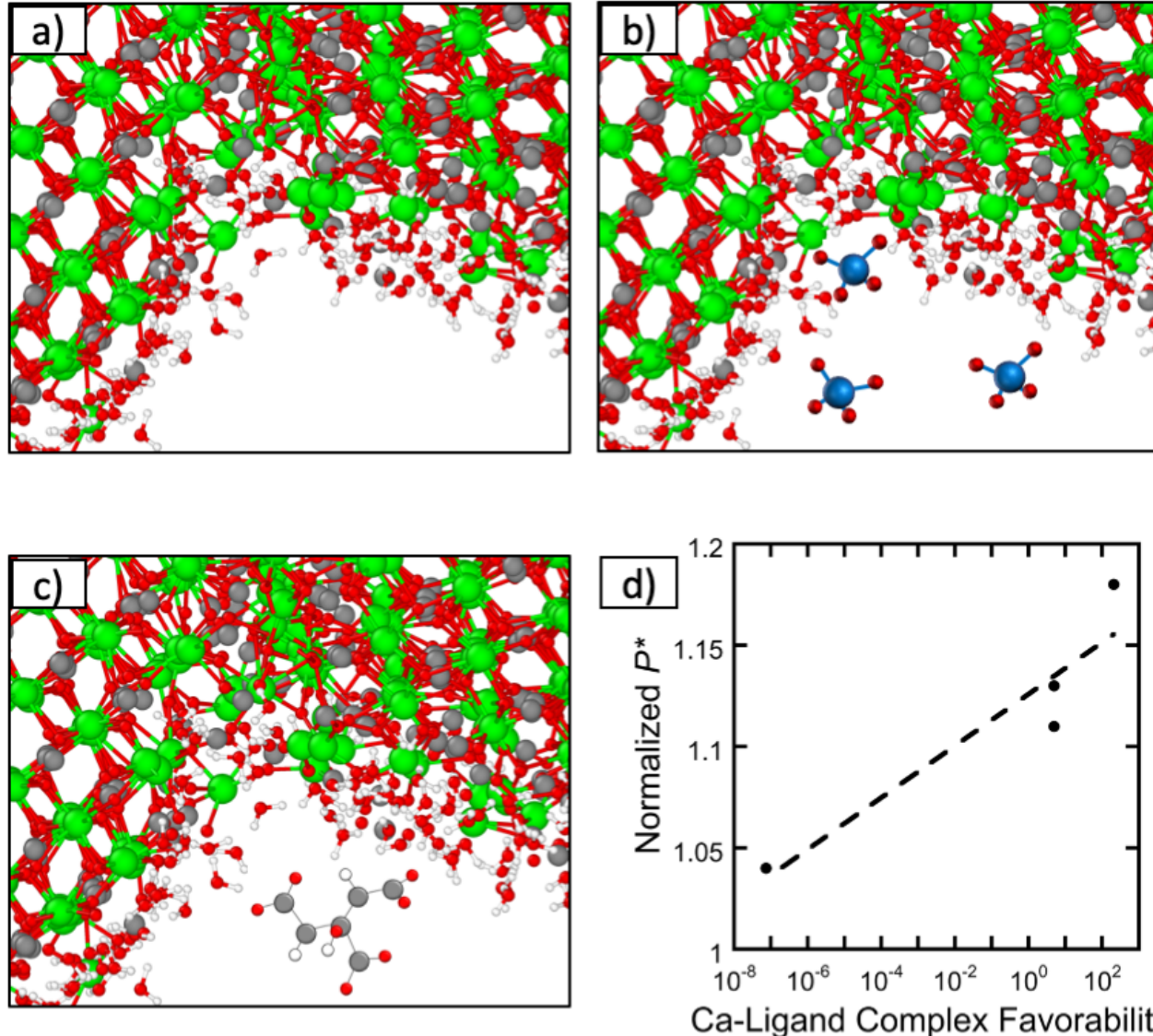
Sample	P* (MPa)	Normalized P* by DI H ₂ O	Porosity Loss (%)	Consolidation Slope (%/MPa)	Total Microfracture Density (mm/mm ²)	% Grains affected by compaction	Modal Grain Size (grain diameter in
Starting CaCO ₃	--	--	--	--	3.5	0	325.0
DI H ₂ O	3.5	1	-18	20.5	21.1	71	29.0
NaHCO ₃	3.65	1.04	19.3	19.3	19.9	80	28.0
Na ₂ SO ₄	4.12	1.18	18.7	18.7	15.4	78	32.6
NaCl	3.90	1.11	18.6	18.6	13.5	75	28.2
NaCl Repeat	3.94	1.13	18.6	18.6	--	--	--
Na ₃ C ₆ H ₅ O ₇	4.07	1.16	19.8	19.8	20.2	90	43.0

Microfracture density depends on the fluid type and follows the sequence:
 DI H₂O > Na₃C₆H₅O₇ > NaHCO₃ > Na₂SO₄ > NaCl

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Results: Conceptual model



- Molecular-scale schematic of crack tip in calcite: red – oxygen, green – calcium, grey – carbon, blue – sulfur, white – hydrogen.
- (a) Calcite consolidation in de-ionized H_2O , with water hydrolyzing $Ca-CO_3$ bonds and promoting crack growth;
- (b) consolidation in $0.5M Na_2SO_4$ with sulphate forming an $Ca-SO_4$ complex at the crack tip preventing hydrolysis reaction;
- (c) consolidation in $0.5M Na_3C_6H_5O_7$ with citrate anion not reaching the crack tip before water does due to slower diffusion, compared to sulphate;
- (d) normalized P^* versus Ca-anion complex favorability (K_β constant).

Choens, et al., 2021

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Thank you.

