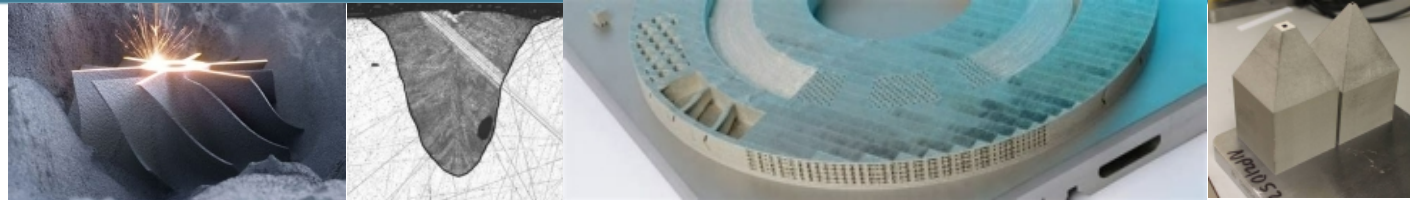




Rapid Computation of Thermal Histories for Laser Powder Bed Fusion Additive Manufacturing Processes



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- Laser Power Bed Fusion (LPBF) is seeing increasing use as a technology for producing functional parts
- Wanted: End-to-end modeling of LPBF process to predict part performance
 - Reduce experimental workload
 - Inform process design and qualification
 - Stand up new materials/machines/processes
- Fully resolved build predictions remain largely intractable, causing reliance on phenomenological models
 - Inherent strain
 - Agglomeration
- Presented here: Green's function technique for fully time-resolved part-scale thermal predictions

Green's Function



- Analytical Green's function solution exists for linear, 3D, time-dependent heat equation
- Analytical spatial integral
- Solution via 1D numerical integral
- **Embarrassingly parallel!**
- Previous AM applications:
 - Wolfer et al (Add. Manuf. 2019)
 - Farwell et al (FEF 2019)
- Full part thermal histories achieved here through use of 4D adaptive grids

Green's function:

$$G = H(t - s) \left(\frac{1}{4\pi\alpha(t - s)} \right)^{\frac{3}{2}} e^{-\frac{(x-x')^2 + (y-y')^2 + (z-z')^2}{4\alpha(t-s)}}$$

Ellipsoidal Gaussian:

$$Q = \frac{P}{\pi^{3/2}\sigma_x\sigma_y\sigma_z} e^{-\frac{(x-x_l)^2}{\sigma_x^2} - \frac{(y-y_l)^2}{\sigma_y^2} - \frac{(z-z_l)^2}{\sigma_z^2}}$$

Temperature Solution:

$$T_i + \frac{2P}{\pi^{3/2}\rho c} \int_0^t \frac{\exp \left\{ -\frac{(x - x_l(s))^2}{\sigma_x^2 + 4\alpha(t - s)} - \frac{(y - y_l(s))^2}{\sigma_y^2 + 4\alpha(t - s)} - \frac{(z - z_l)^2}{\sigma_z^2 + 4\alpha(t - s)} \right\}}{\sqrt{\sigma_x^2 + 4\alpha(t - s)} \sqrt{\sigma_y^2 + 4\alpha(t - s)} \sqrt{\sigma_z^2 + 4\alpha(t - s)}} ds$$

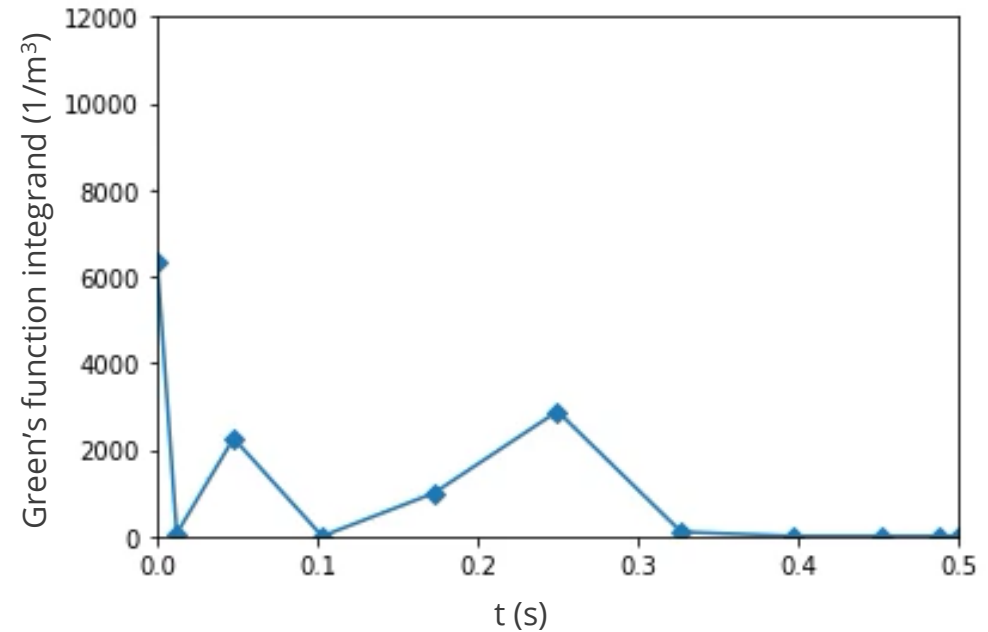
Assumptions:

- Material properties k, ρ, c do not depend on T, x, y, z , or t
- Domain is semi-infinite

Methodology



- Piecewise linear discretization of laser source
- Numerical integration via adaptive Clenshaw-Curtis quadrature
 - Nested quadrature orders with adaptive interval splitting
 - Efficient integration of highly localized integrand over long time intervals
- Time-parallel computation of each layer
- Fully time resolved laser action
- Implemented on CPU and GPU using Kokkos

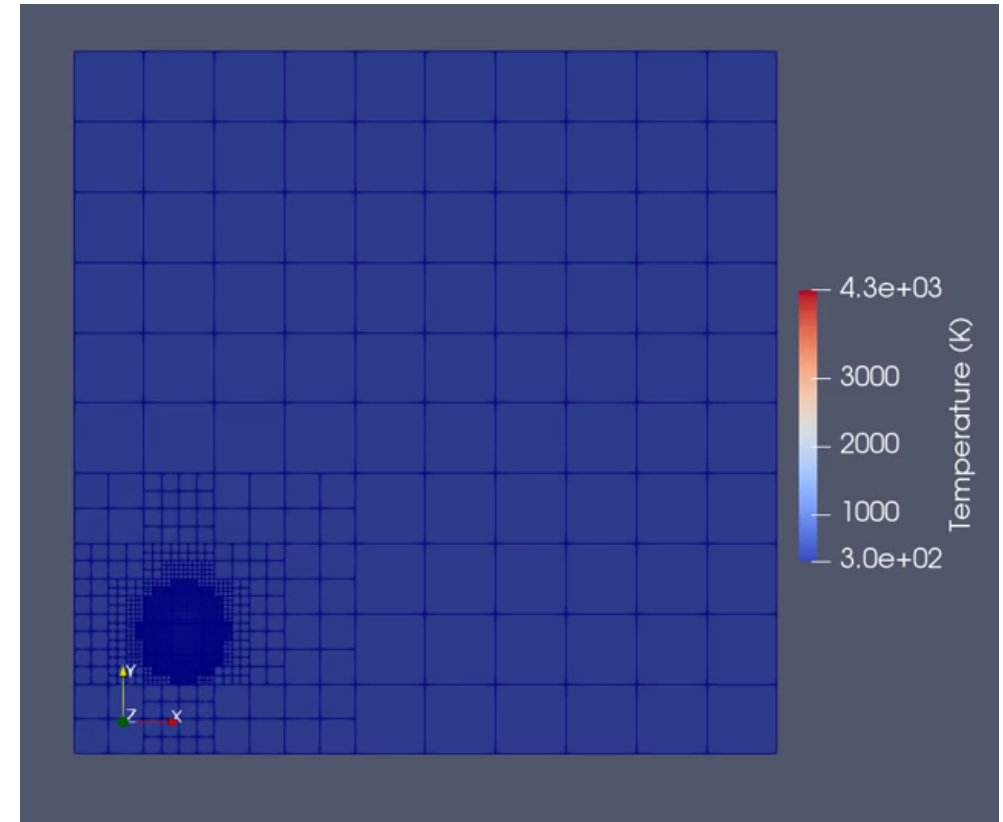


Adaptive integration of Green's function for a point

Adaptive Space-Time Grid



- Independent T evaluations decouple resolution and accuracy
 - Initial coarse sampling on uniform grid
 - Refine each space-time cell
 - Cell-by-cell evaluation of interpolated and actual fine solution
 - Further refine cells where interpolant is inaccurate
- CPU/GPU mesh adaptivity
- Compact(ish) solution representation
- Decomposition with **no communication across ranks**



Adaptive 4D Grid projected onto 3D mesh

Comparison to FEM



- Benchmark problem: square scan pattern
 - 0.6s of simulated time
 - 10 μ m x 100 μ s resolution
- 12x/72x speedup on CPU/GPU
 - CPU comparison is equal # of procs
 - Green's function method effectively scales to many more procs
- 84GB vs 4.5TB (uncompressed) to represent solution on adaptive space-time grid vs fixed resolution

Solver	Platform	# Procs	Time
FEM	CPU	360	6 hrs
Green	CPU	360	33 mins
Green	GPU	16	4.3 mins

Full Build

- Full size (big) part
 - 5x5x10cm
 - 3086 layers
- Time resolved solution intractable with FEM
- **~3 days on 2400 CPU processes**
 - No large enough GPU cluster!
- Approx. 100TB of data (compressed)
 - File writes/compression significant cost
 - More compact representation needed

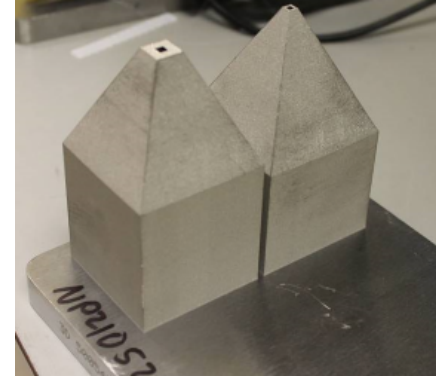
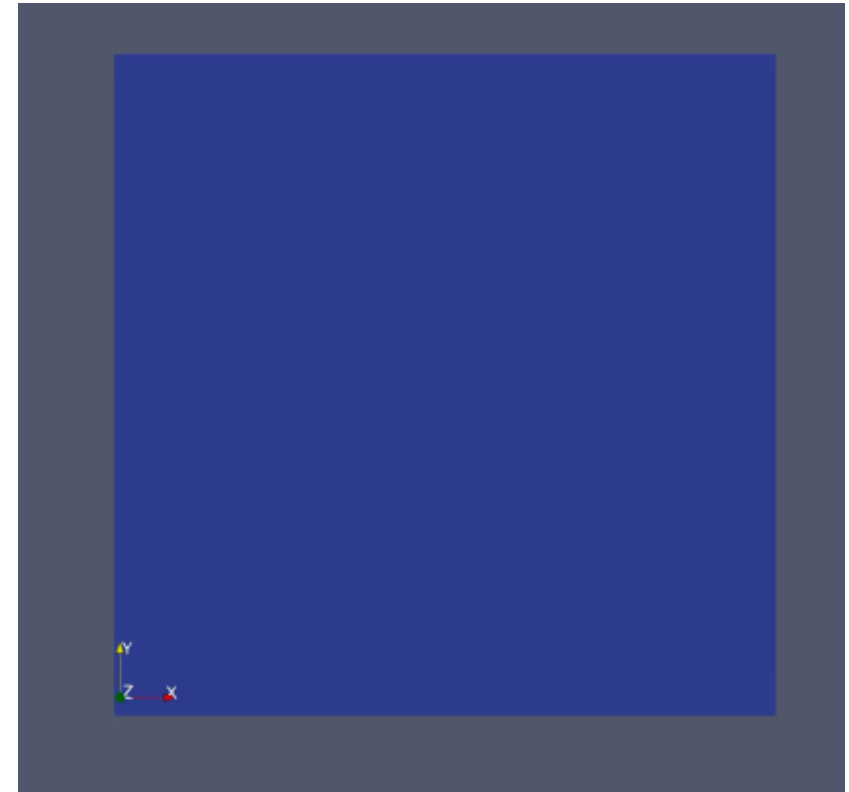


Photo of simulated part

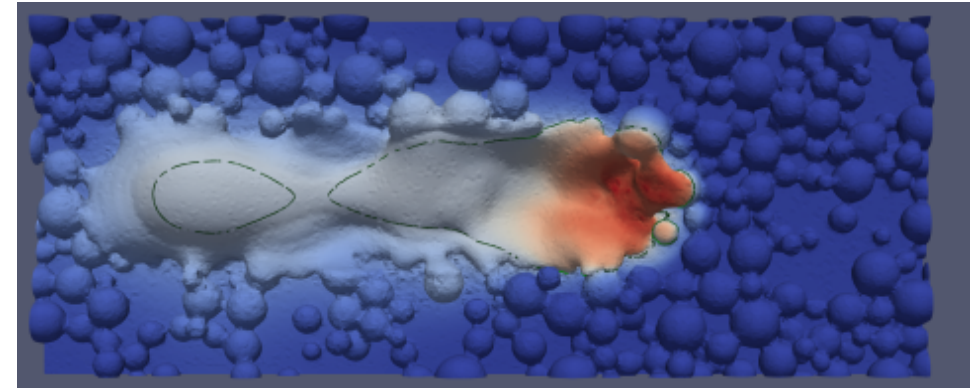


Temperature history of a full layer scan

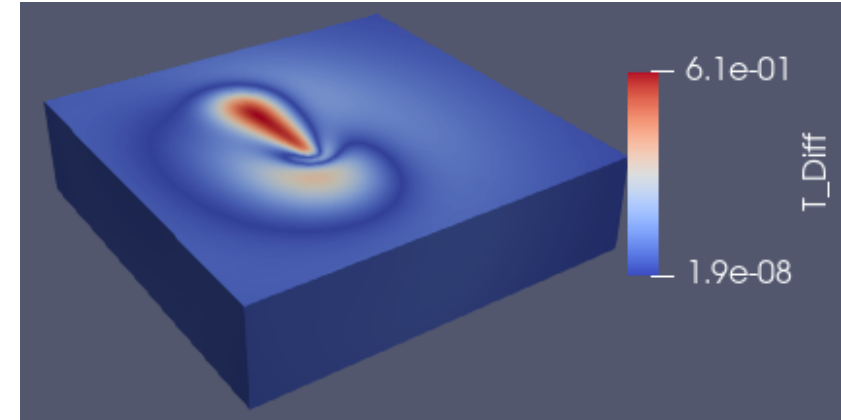
Calibration/Temperature Comparisons



- Linear model can be calibrated to match desired melt pool dimensions
 - Non-linear conduction models, thermal/fluid models, experimental data
- L1/L2 temperature norm calibration
- Differences in temperature history regardless of method
 - Non-linear heat capacity effects in trailing edge of melt pool
- Multi-grid Jacobi-type methods to iterate out non-linearities and complex BCs
- Model form uncertainty quantification



Melt pool simulated using mesoscale thermal/fluid model

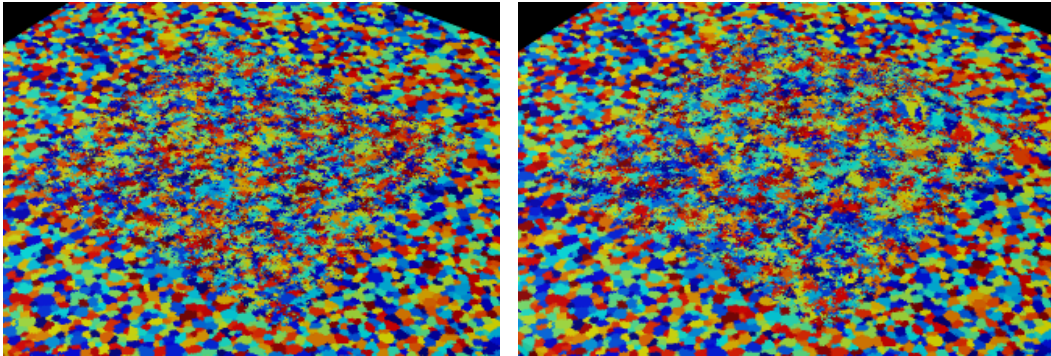


Normalized temperature difference between calibrated linear and non-linear models

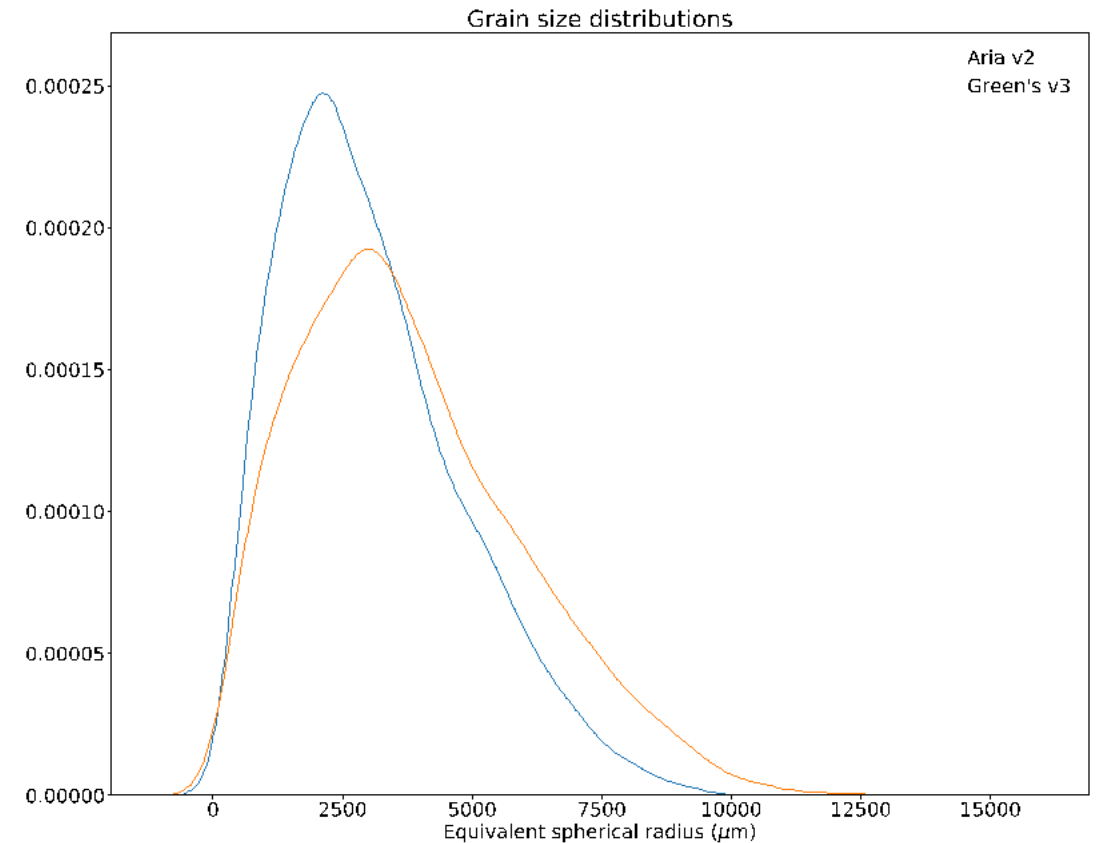
Microstructure Comparisons



- Both models show fine grain structures
 - Small melt pool w/limited remelting
- Linear Green's results show shift towards larger grain sizes
 - Differences in thermal gradients due to latent heat/variable specific heat



Comparison of microstructures computed for single layer using (a) non-linear and (b) linear thermal models

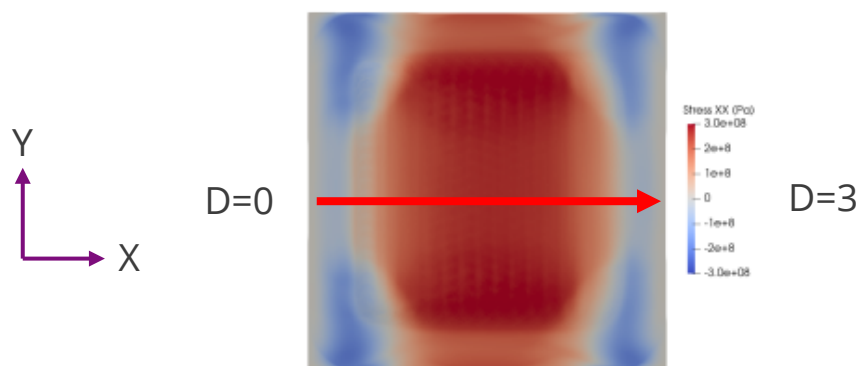


Equivalent spherical radius grain populations for non-linear (blue) vs linear (brown) temperature histories

Residual Stress Comparisons

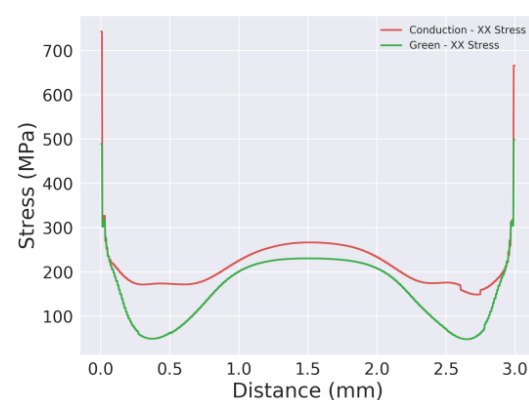


- Agreement in part interior is good
- Biggest differences at edges
 - Different applied BCs
- Temperature differences don't always translate to large stress or microstructure differences

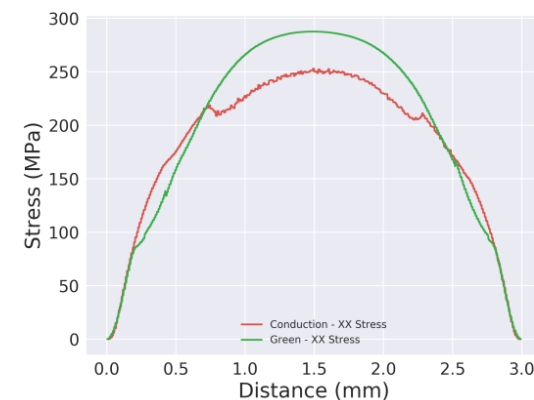


Location of residual stress line contours

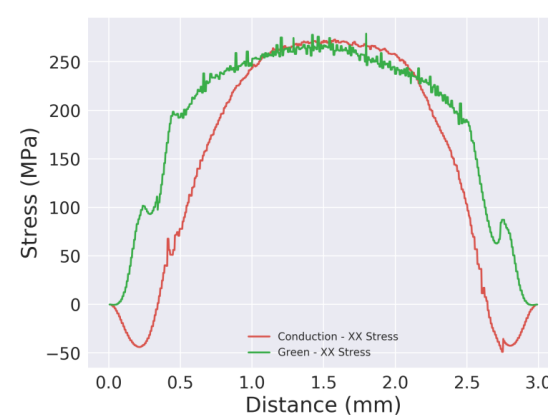
XX Stress Across Build - X Direction Bottom



XX Stress Across Build - X Direction Middle



XX Stress Across Build - X Direction Top



Comparisons of XX residual stress perpendicular to scan direction at three different depths

- Green's function solver implemented
 - Highly parallel
 - CPU/GPU capable
 - CPU/GPU adaptive 4D grid
 - 12x/72x CPU/GPU speedup vs FEM
- **Fully time resolved large (5x5x10cm) part build in ~3 days**
- Future work
 - Compact data representation
 - Resolve non-linearities, complex BCs
 - **Uncertainty estimation**

