



Nonequilibrium Simulations of Ion Dynamics in Ionomer Melts

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Sandia National Laboratories

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*Exceptional
service
in the
national
interest*



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Acknowledgments



Lisa Hall
(now at OSU)



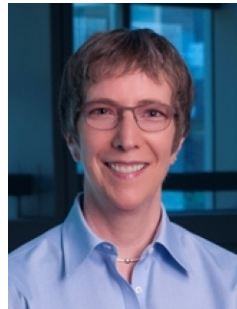
Christina Ting



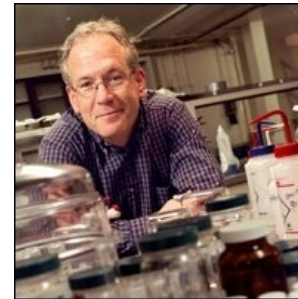
Karen Sorensen-Unruh



Mark Stevens



Karen Winey
U Penn



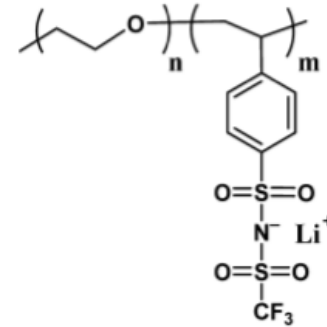
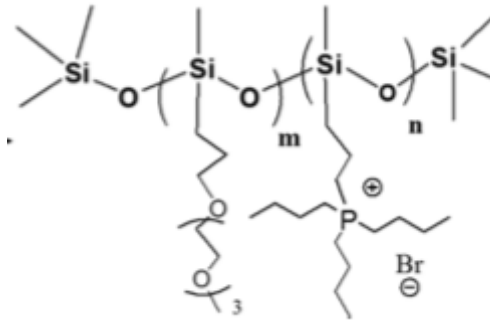
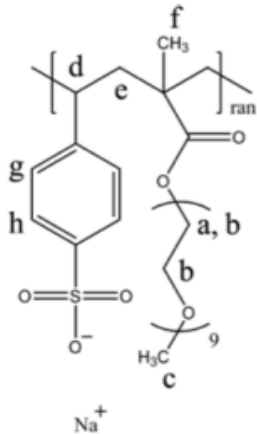
Jim Runt
Penn State

The “Ionomers” LDRD team
Funding: Sandia LDRD Program
CINT



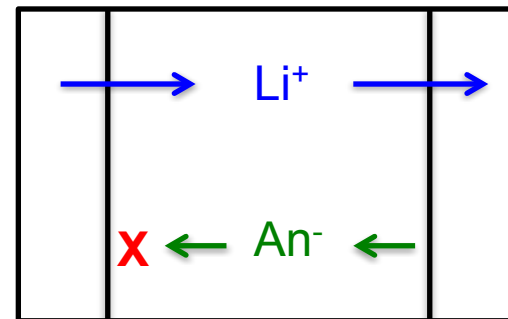
Ionomers as Single-Ion Conductors

(no solvent)



why single-ion?

- high transference number
- no concentration gradients



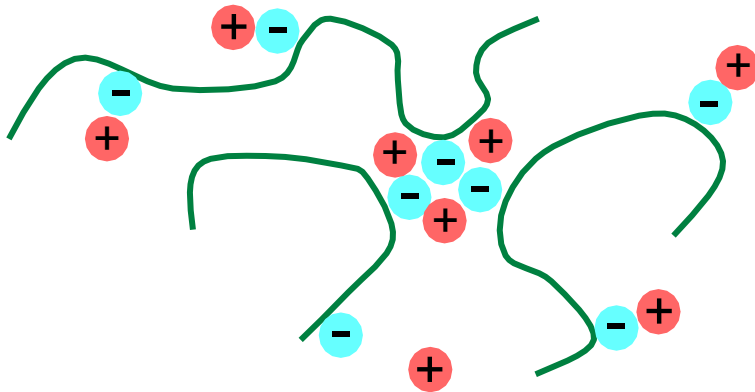
Wang, J.-H. H. *et al. Macromolecules* **48**, 7273–7285 (2015).

Liang, S. *et al. Macromolecules* **47**, 4428–4437 (2014).

Rojas, A. A. *et al. Macromolecules* **48**, 6589–6595 (2015).

Ionic Aggregates in Ionomers

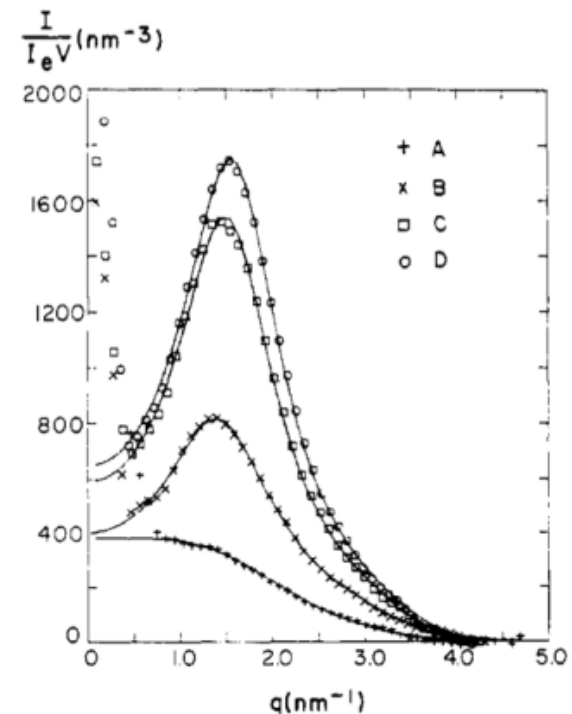
Coulombic forces favor aggregates
polymer entropy limits size



nm-scale ionic aggregates

“ionomer peak”

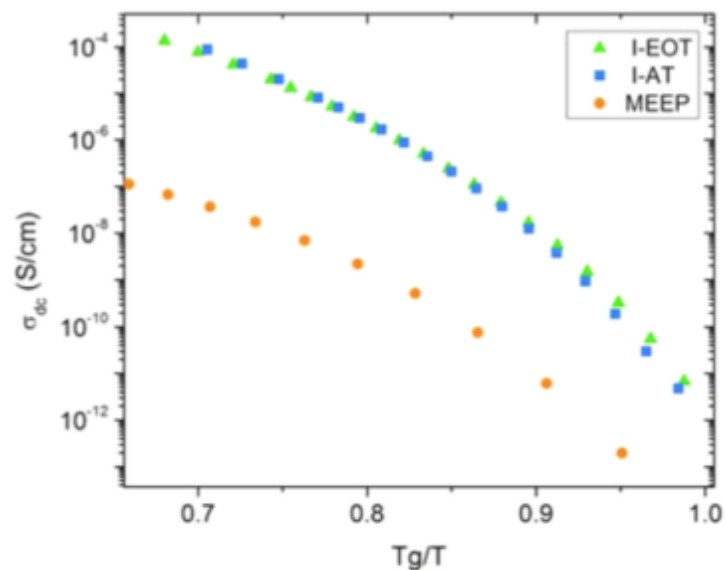
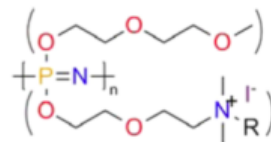
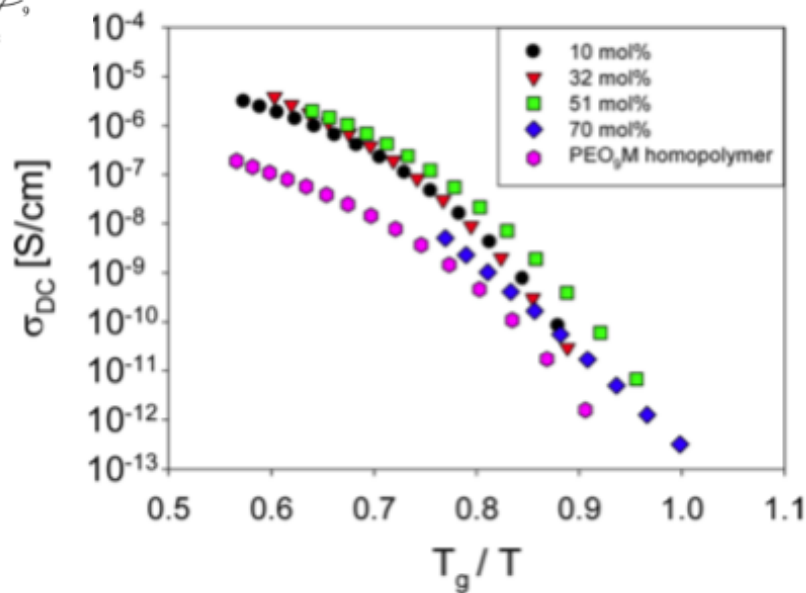
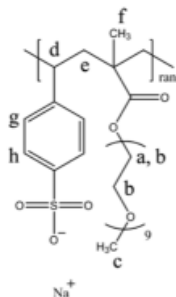
- ubiquitous
- low wavevector peak in scattering
- from inter-aggregate scattering



Yarusso & Cooper, Macromolecules, 1983

Ionic Conductivity in Ionomers

low due to low ϵ , slow polymer motion, ionic aggregates

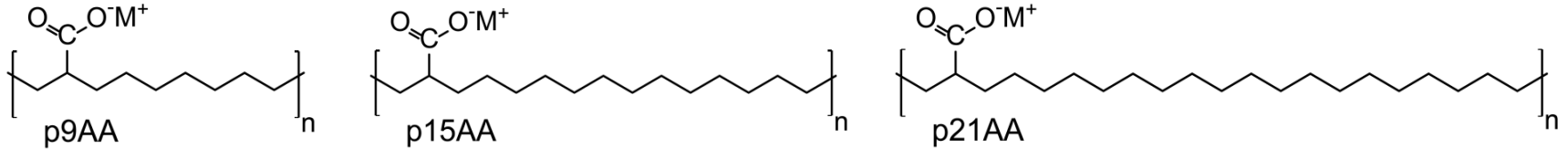


Wang, J.-H. H. *et al. Macromolecules* **48**, 7273–7285 (2015)

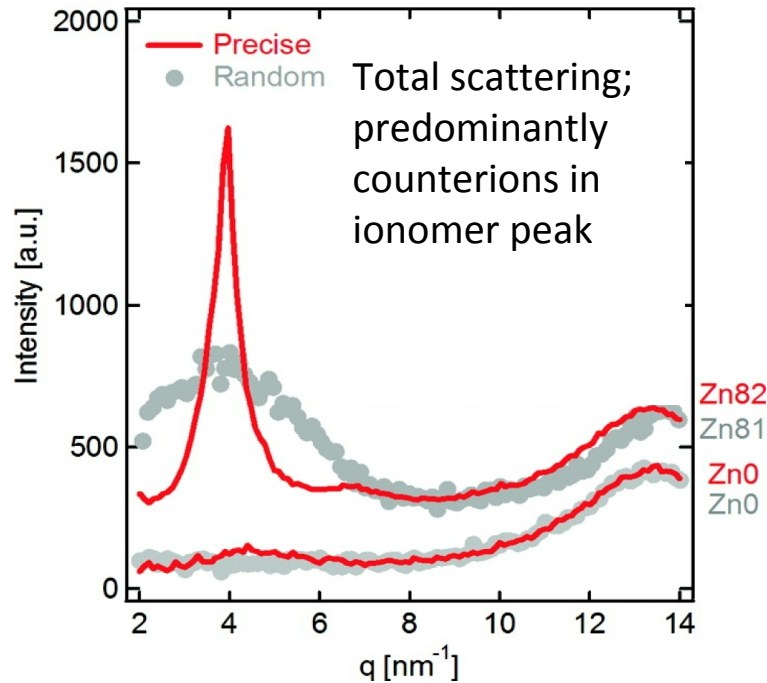
Bartels, J. *et al. Macromolecules* **48**, 111–118 (2015)

need $\sigma_{DC} > 10^{-3}$ S/cm for applications

PE backbone with **precisely** spaced carboxylic acid functional groups



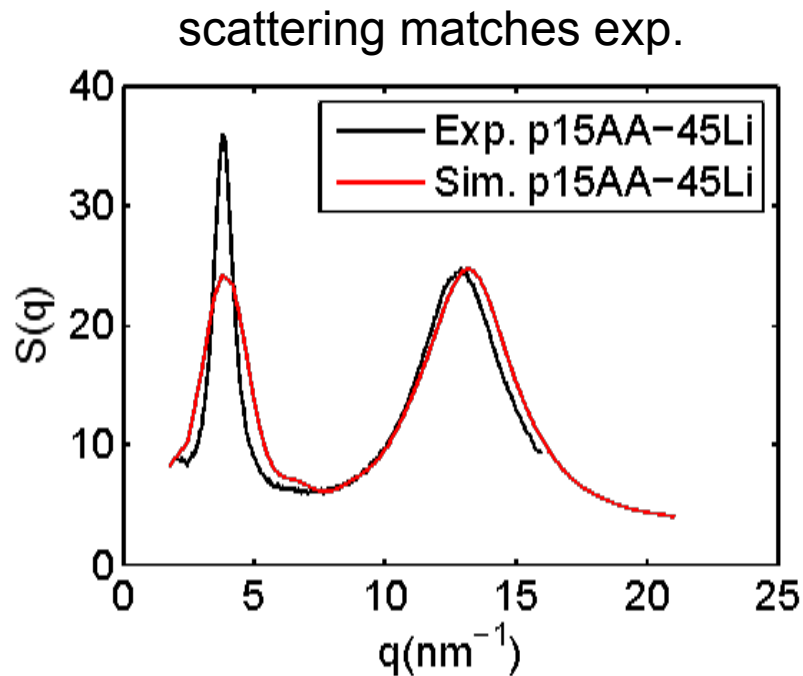
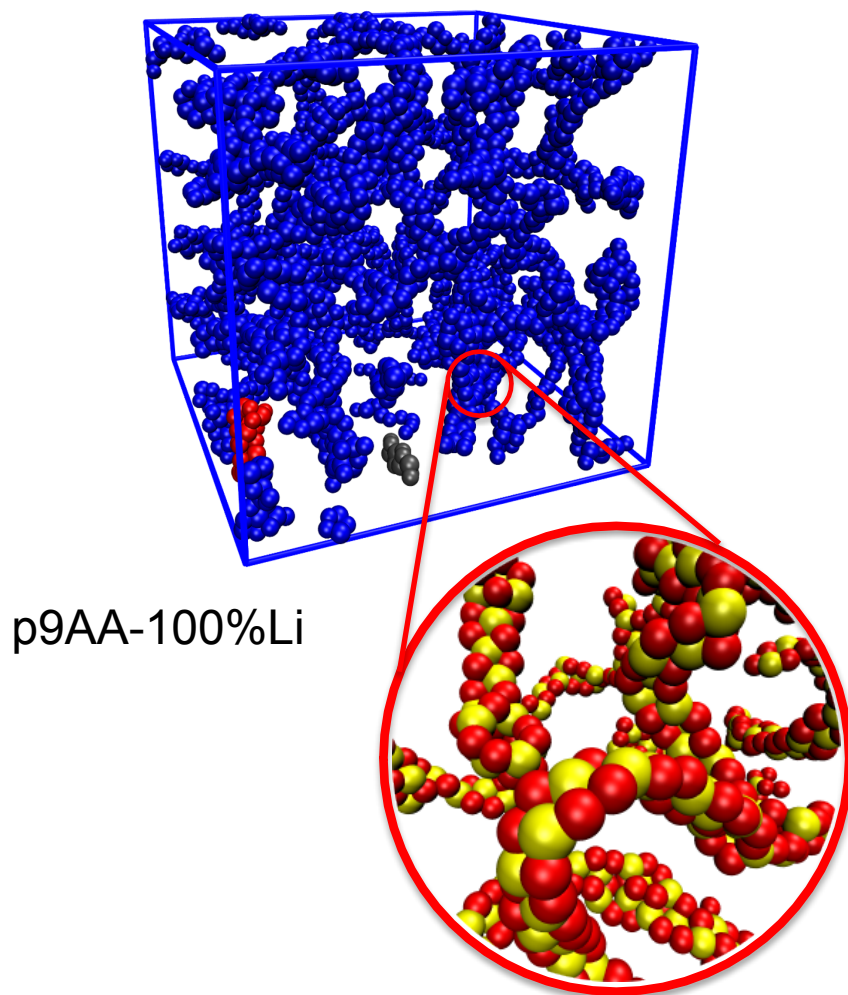
Wagner group, University of Florida



M. E. Seitz et al., *J. Am. Chem. Soc.* **2010**, 132, 8165-8174.

Atomistic Simulations

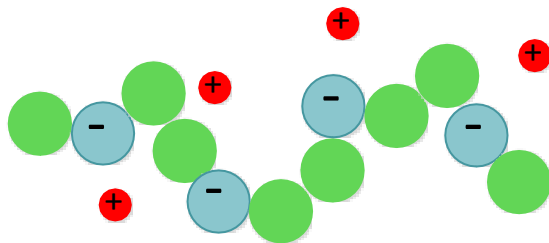
often see stringy aggregate morphologies



Bolintineanu et al., *ACS Macro Lett.* **2**, 206 (2013)
Buitrago et al, *Macromolecules* **48**, 1210 (2015)

Coarse-Grained Simulations

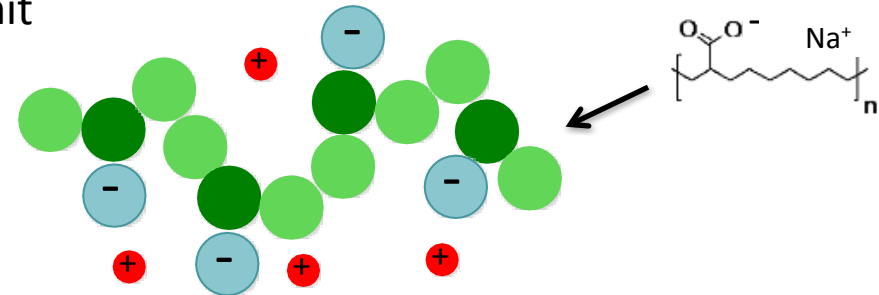
Ions in the polymer backbone:
“**ionenes**”



backbone beads
per repeat unit

$N = 3$

Ions pendant to the backbone:
“**pendants**”



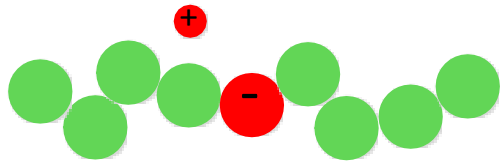
$N = 3, 5, 7, 9 (11)$
35 or 36 backbone beads
800 polymers
counterion size = 0.5σ

bulk dielectric constant = 4
Bjerrum length = 35.7σ
when Coulomb energy = kT

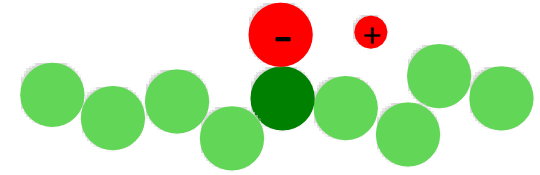
$$\lambda_B = \frac{e^2}{4\pi\epsilon_0\epsilon_r kT} = 35.7 \sigma$$

$$R_g \approx 3.1 - 3.3 \sigma$$

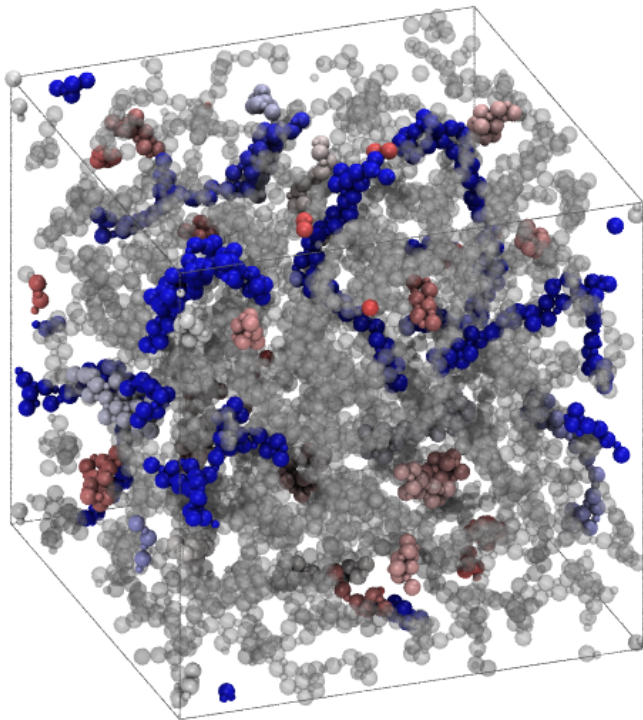
CG Simulations: Architecture Matters



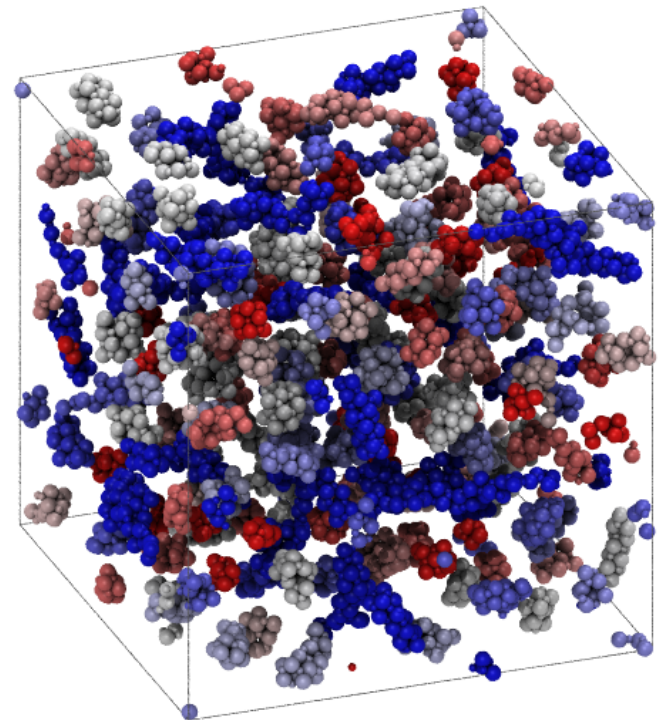
Ionenes: percolated



Pendants: not percolated



$N = 9$



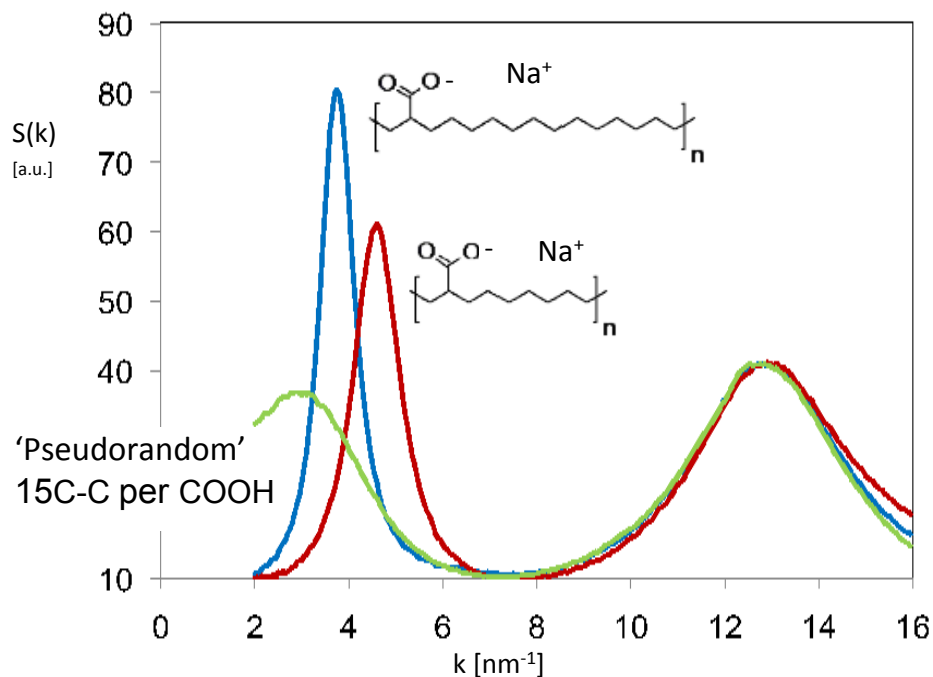
Small clusters  Large clusters

Only charged beads shown

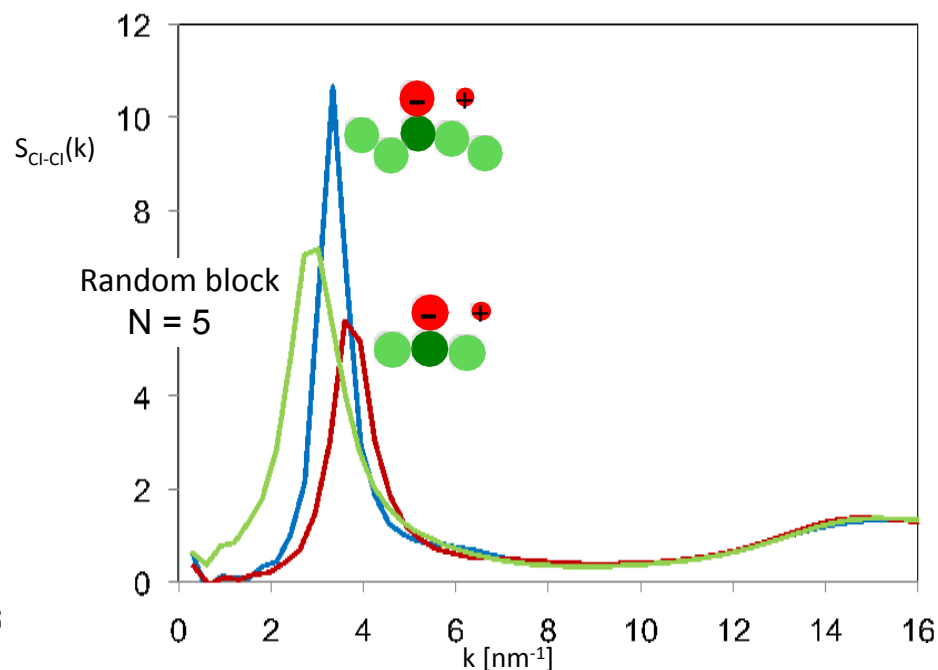
CG MD: Comparison to X-ray Scattering

- Experimental/simulation agreement for pendants
 - Peak location similar
 - Increasing spacing moves peak to left
 - Random spacing moves and broadens peak

Experiment

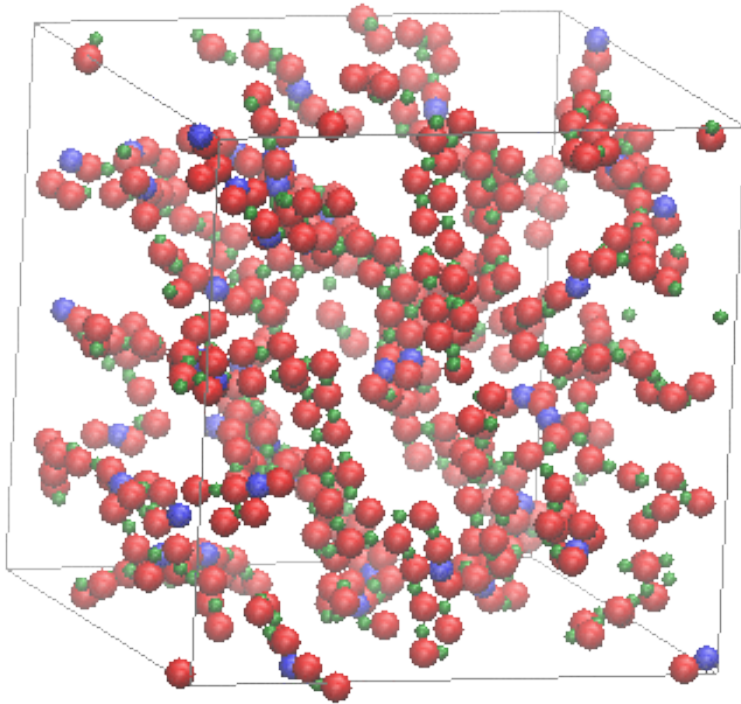


Simulation

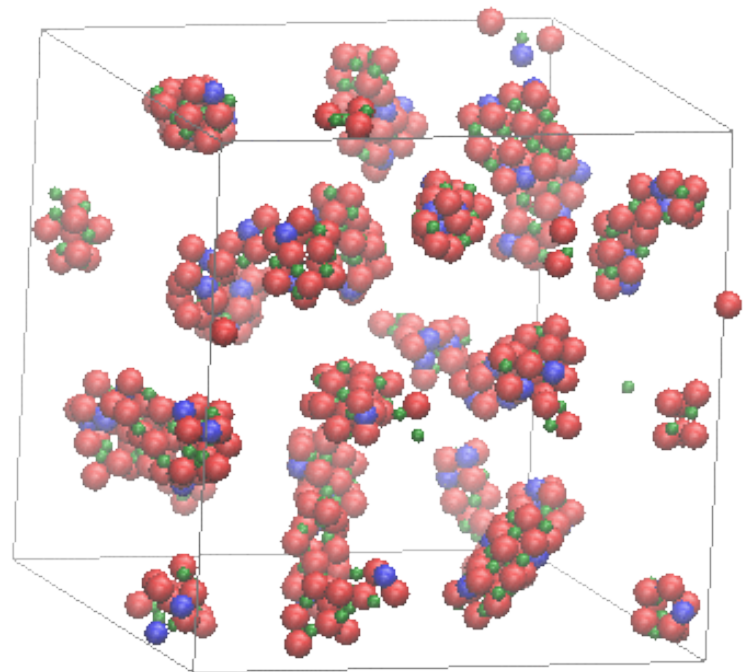


Hall et al., *J. Am Chem. Soc.* (2012)

ionenes $N = 9$



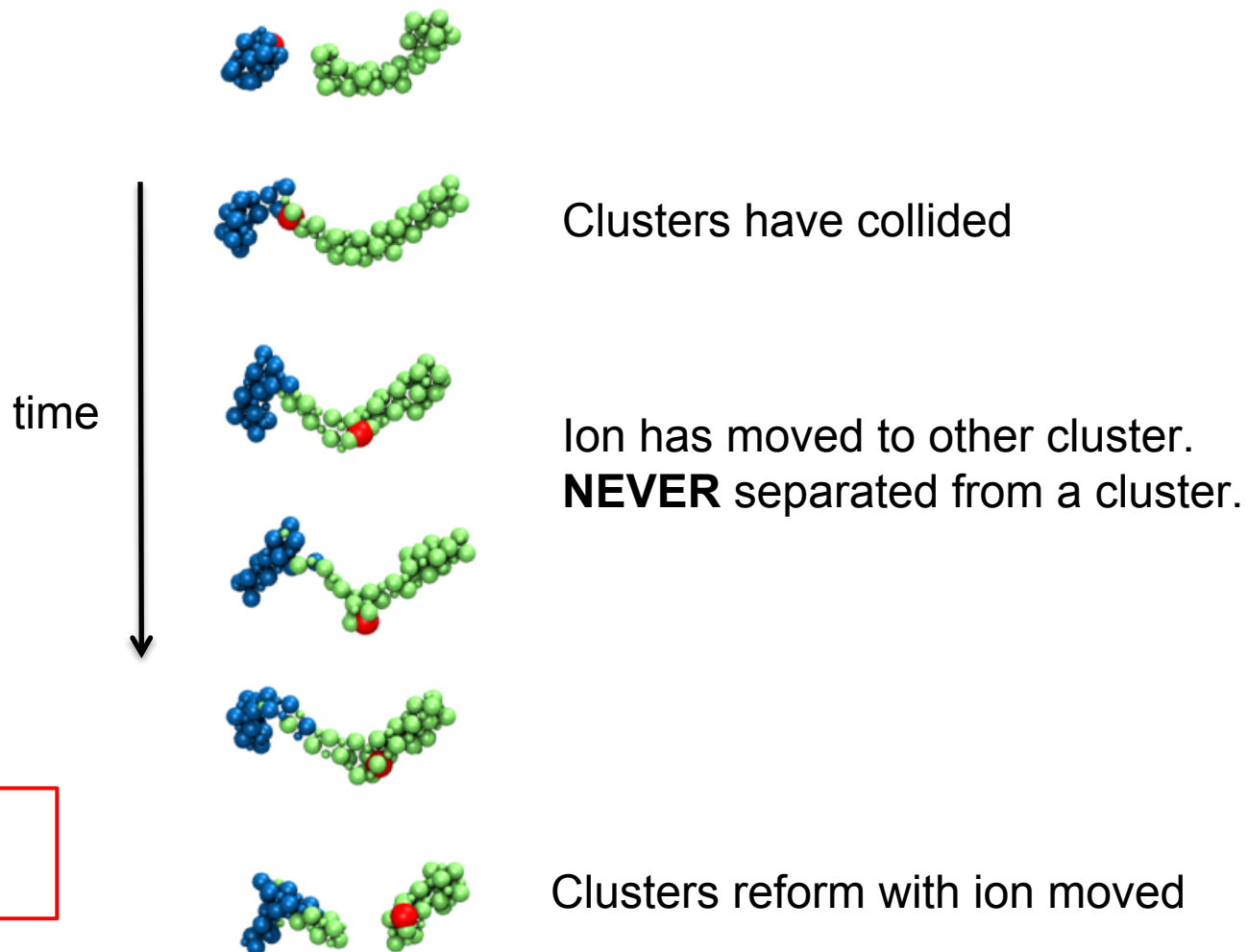
pendants $N = 9$



Ion Trajectories

periodic pendants $N = 9$

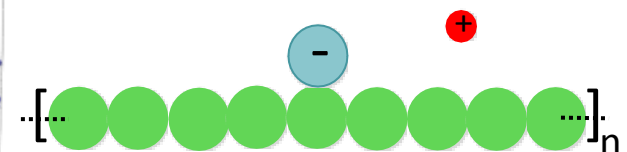
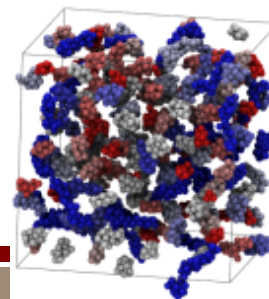
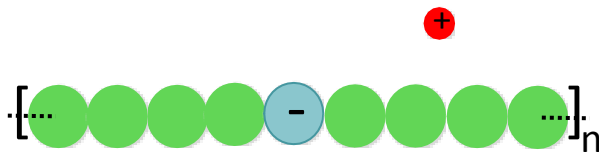
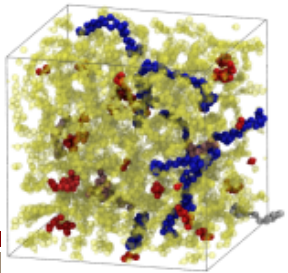
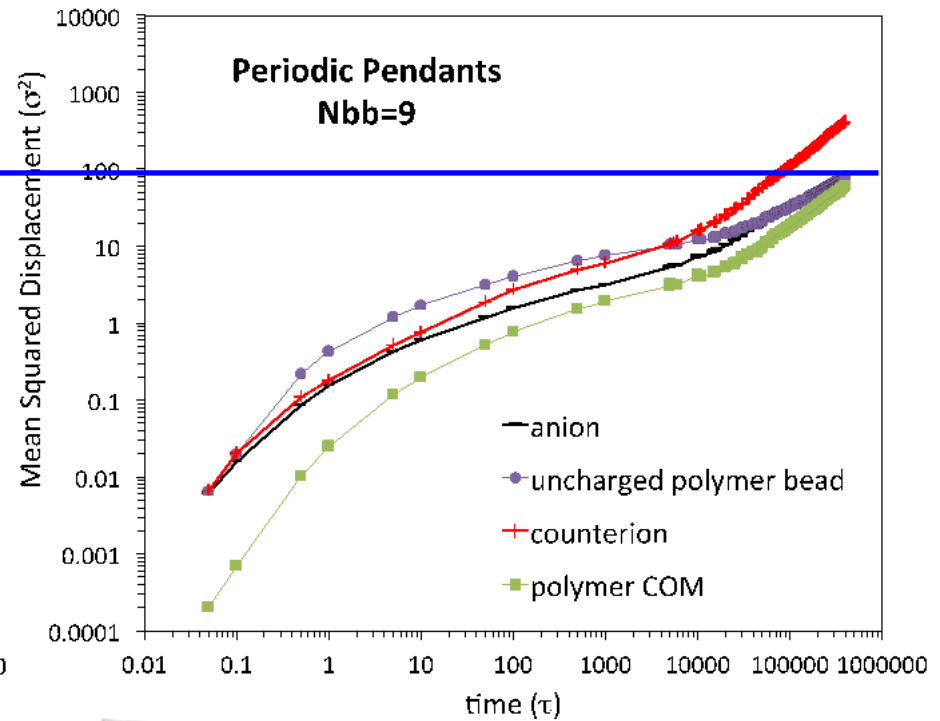
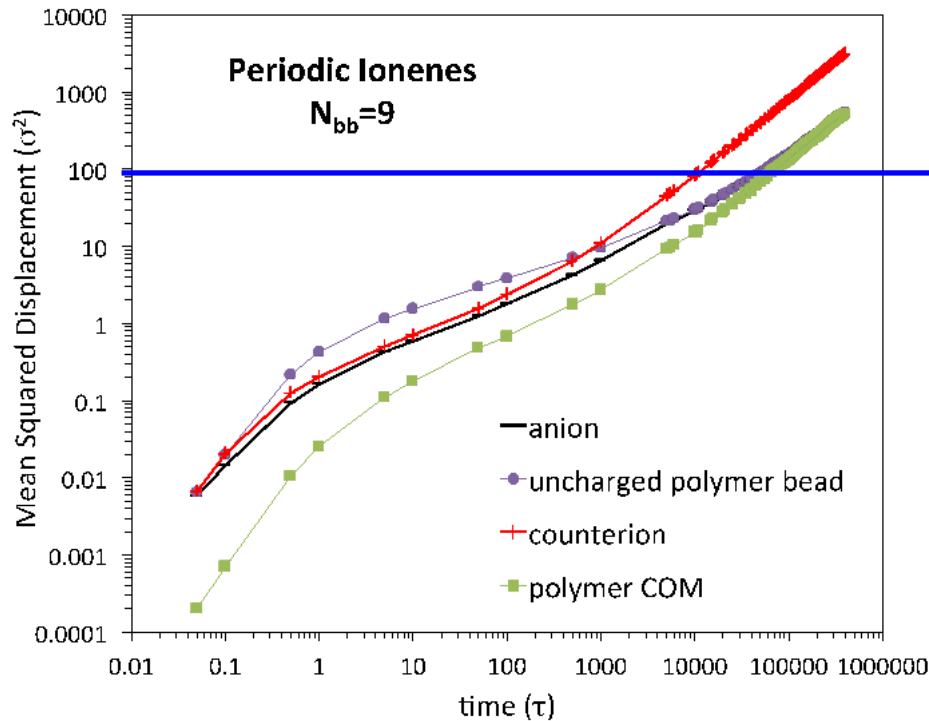
2 separate clusters
Follow one **cation**



ions move by cluster
rearrangement/collision

Mean Squared Displacements

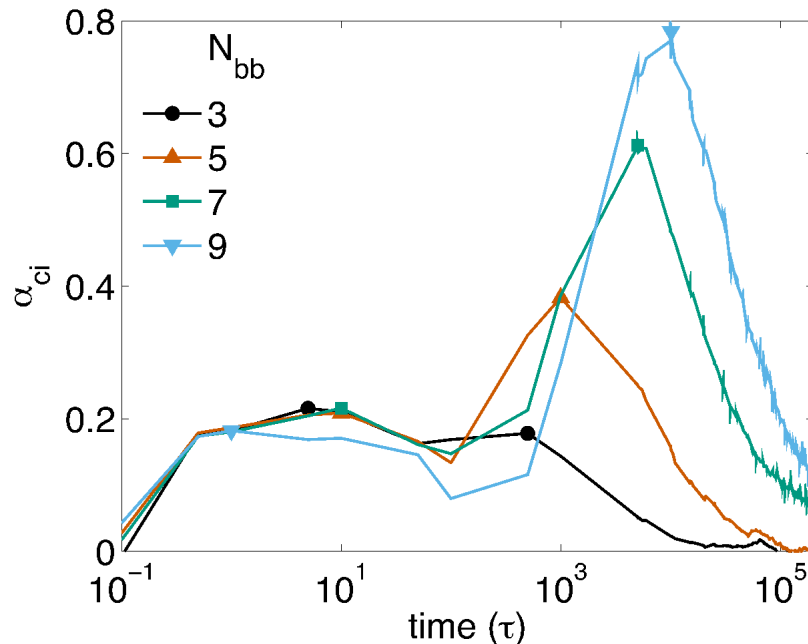
- Ionenes, pendants similar at short times
- Pendants slower but qualitatively similar at long times



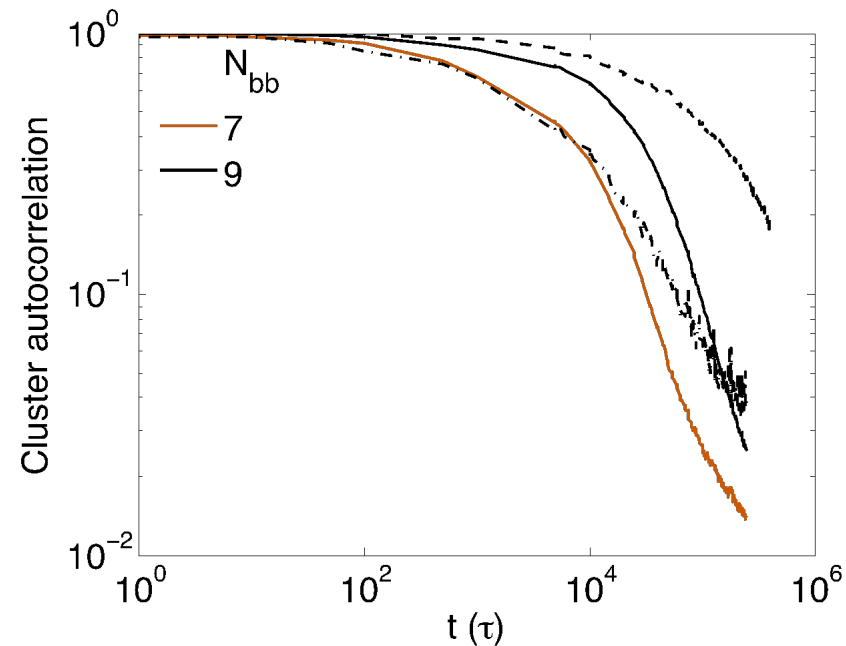
non-Gaussian
parameter

$$\alpha(t) = \frac{3 \langle (r(t))^4 \rangle}{5 \langle (r(t))^2 \rangle^2} - 1$$

cations in periodic pendants



ion cluster auto-correlation



indicative of 2 time scales:

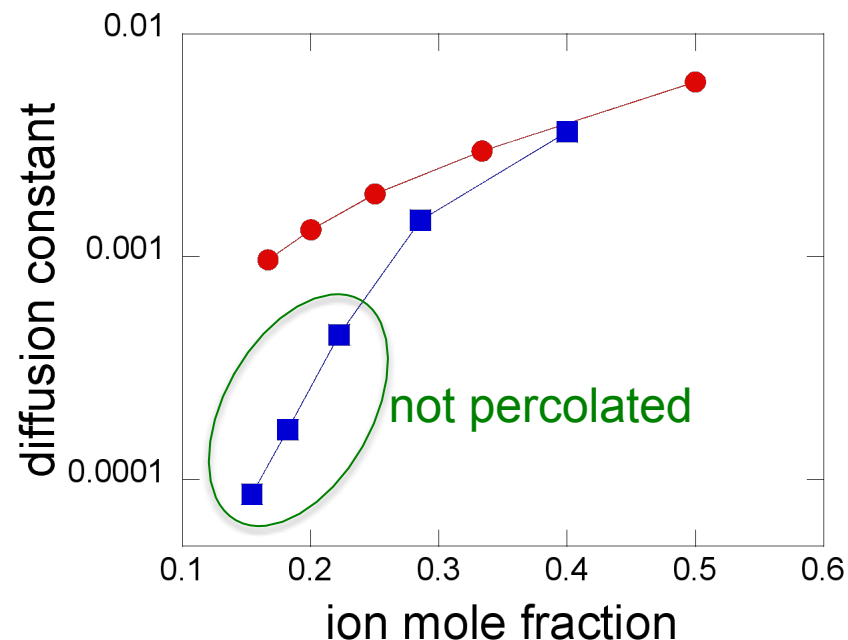
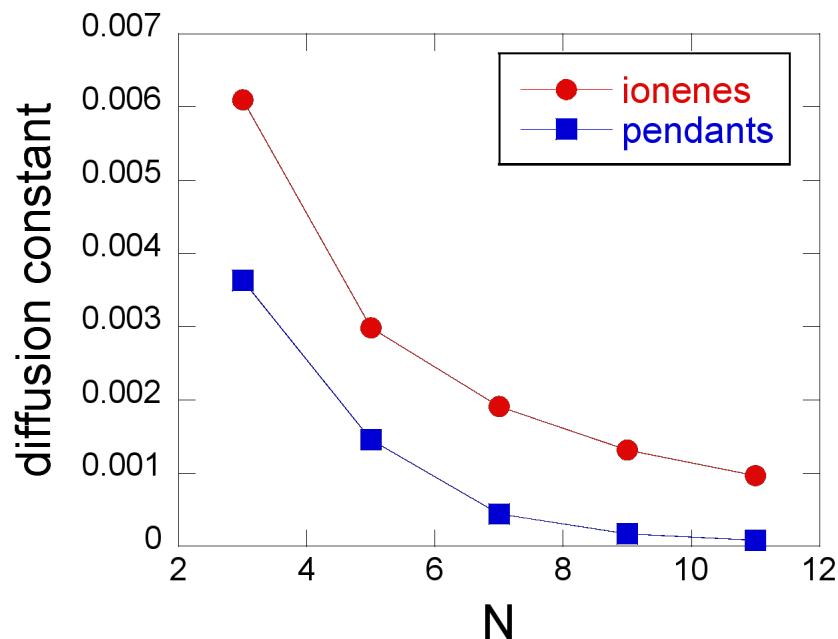
- local motion in clusters
- slower rearrangement between clusters

p7: $\tau_c = 8000 \tau$

p9: $\tau_c = 31000 \tau$

Counterion Diffusion Constants

$$\langle \mathbf{r}^2(t) \rangle = 6Dt$$

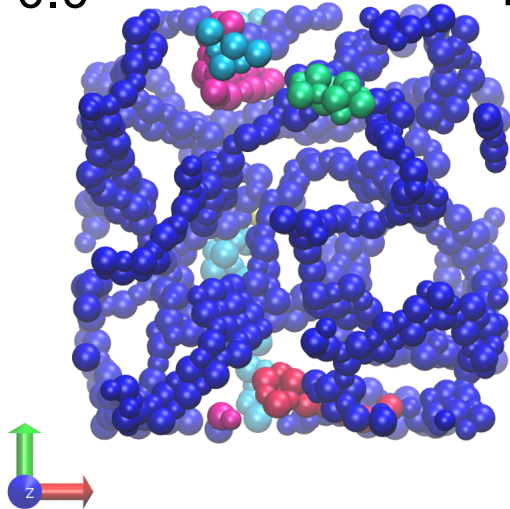


- Ionenes have faster diffusion than pendants
- Percolated systems have faster diffusion

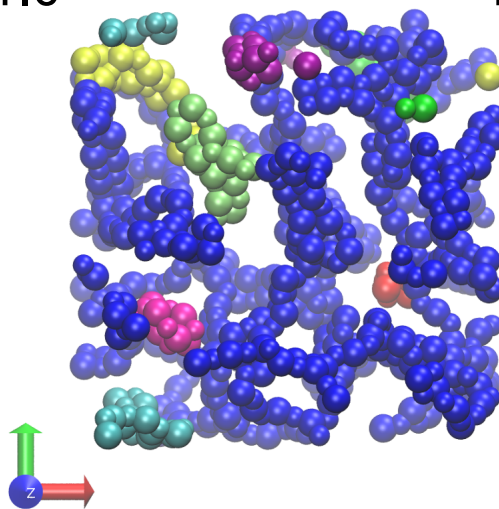
Effect of Field: Ionenes

add force $F_x = qE_x$ to each ion

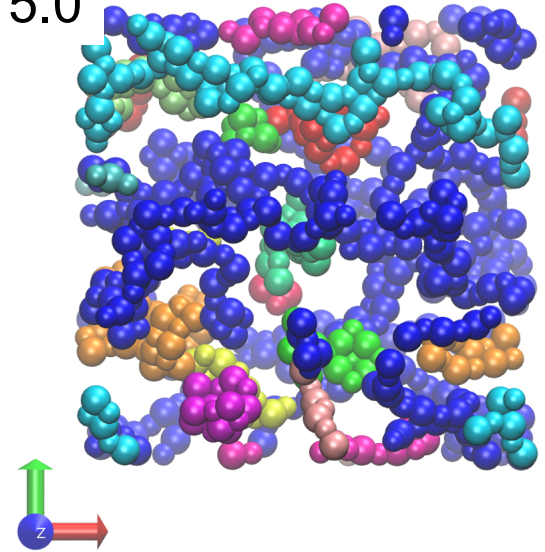
$E = 0.0$



$E = 1.0$



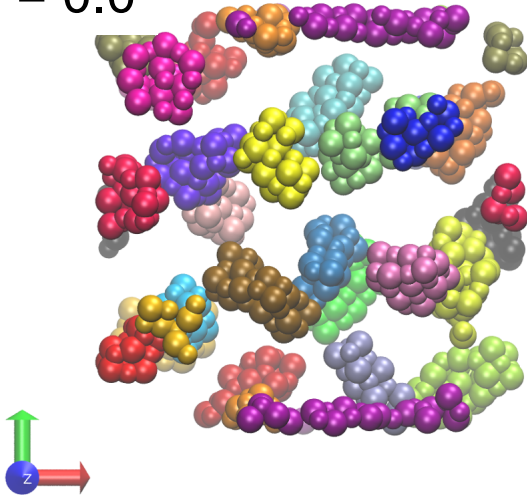
$E = 5.0$



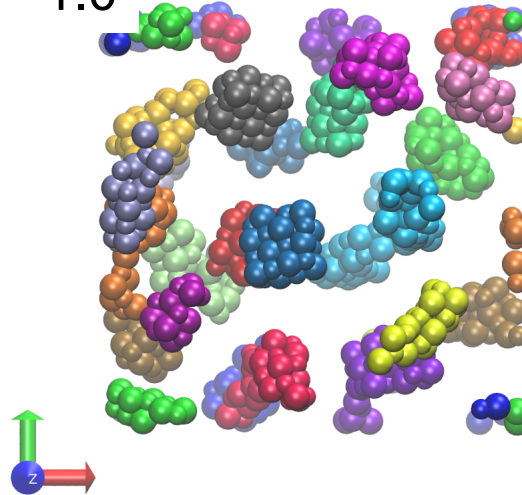
field direction

Effect of Field: Pendants

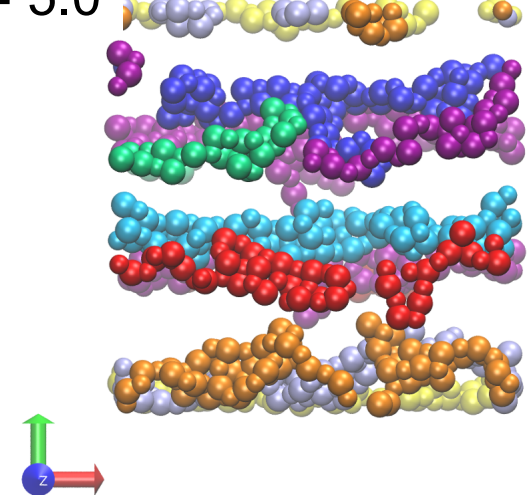
$E = 0.0$



$E = 1.0$



$E = 5.0$



field direction

MSDs in the Field

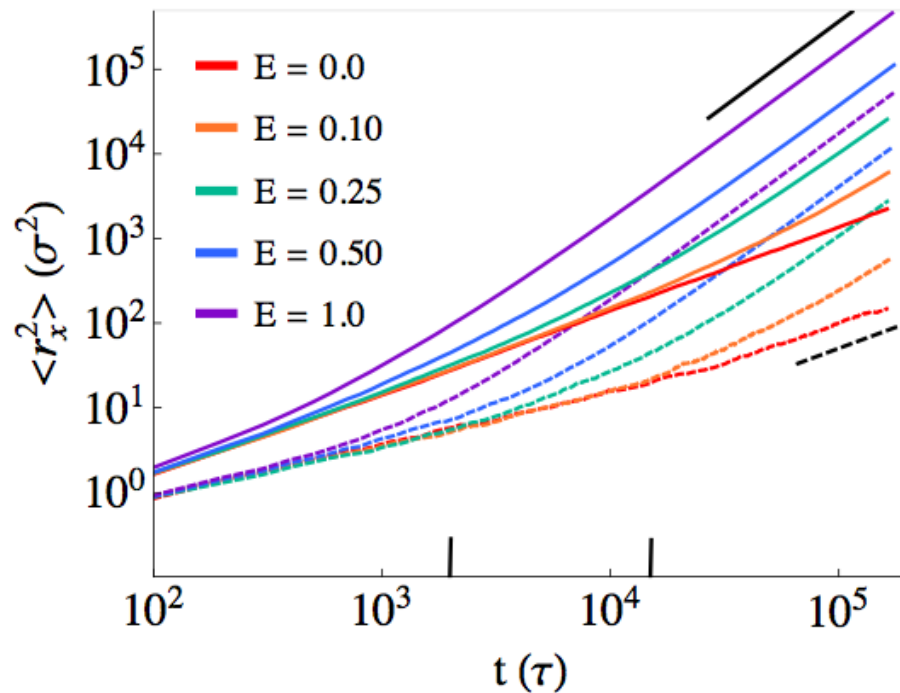
diffusion

$$\langle r_x^2 \rangle \sim Dt$$

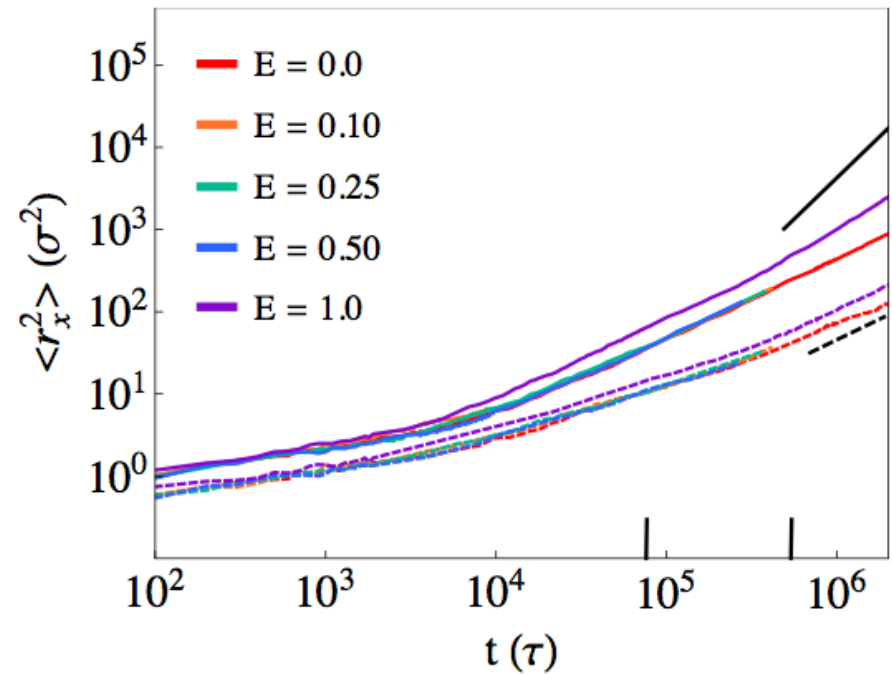
drift in the E field

$$\langle r_x(t)^2 \rangle_E - \langle r_x(t)^2 \rangle_0 = \langle v_x^2 \rangle t^2$$

ionene N = 3



pendant N = 9



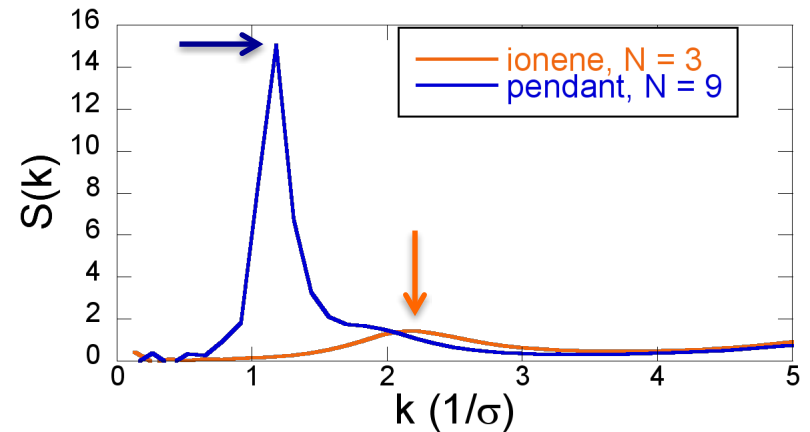
dashed = anion, solid = cation

Time-dependent Structure Factors

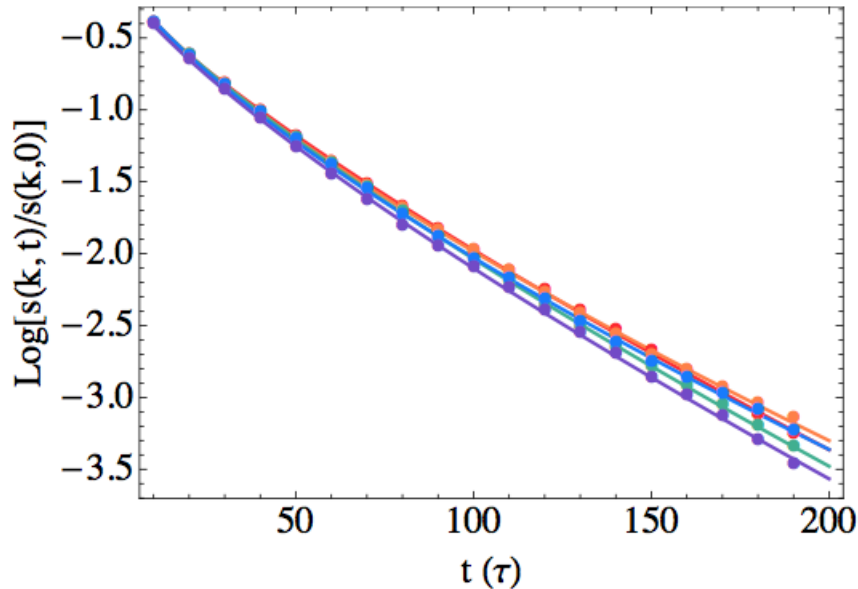
decay of counterion-counterion
scattering peak

$$S(k, t)/S(k, 0) = \exp[(-t/\tau)^\beta]$$

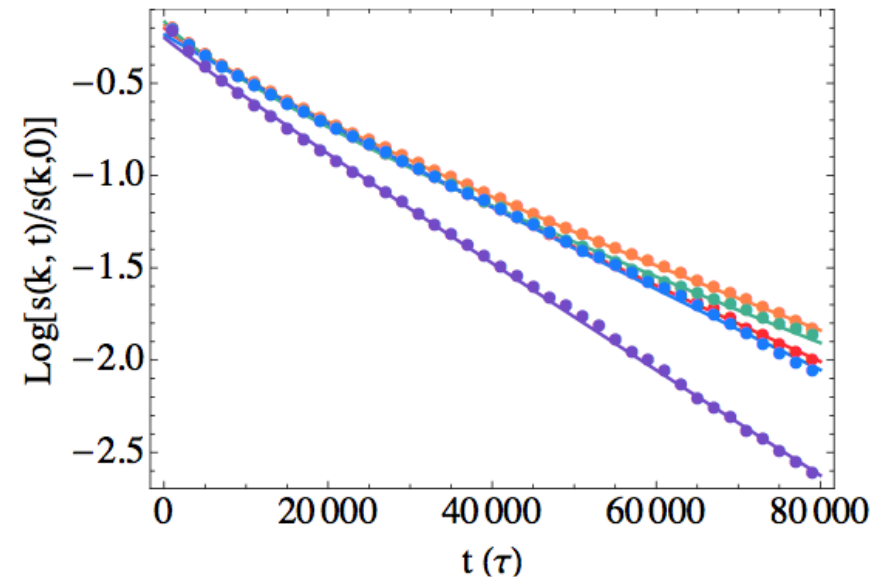
$$0.66 < \beta < 0.96$$



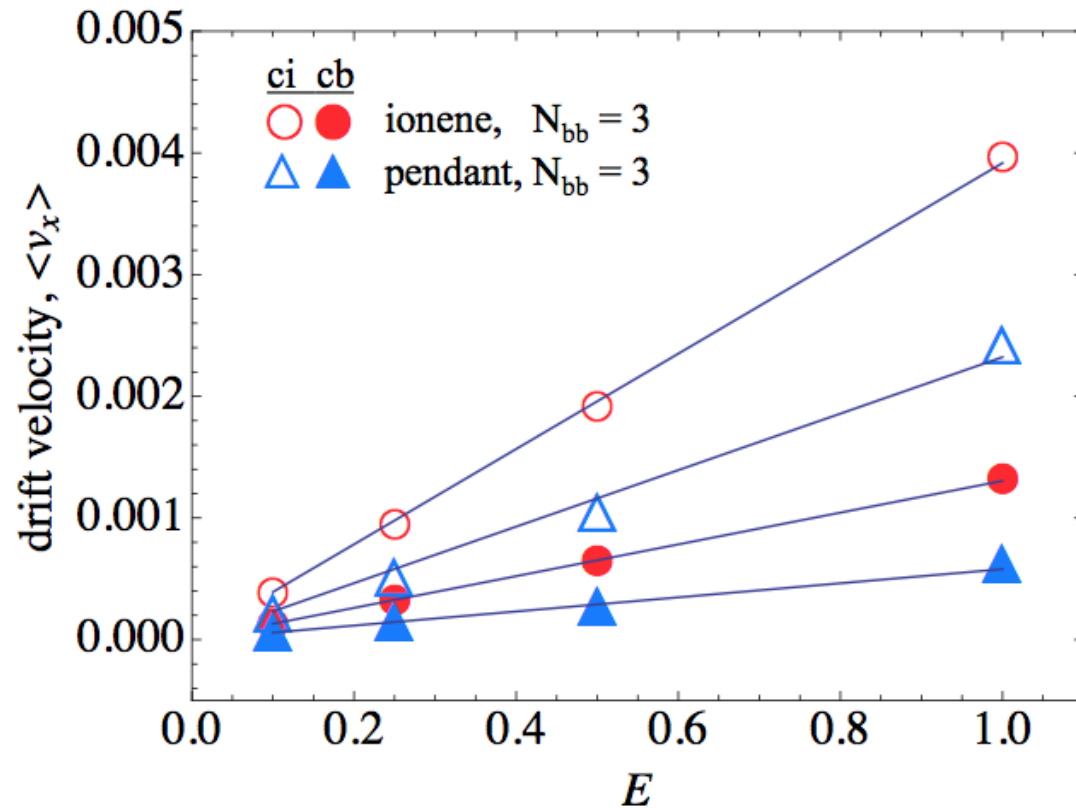
ionenes $N = 3$



pendants $N = 9$



Drift Velocity

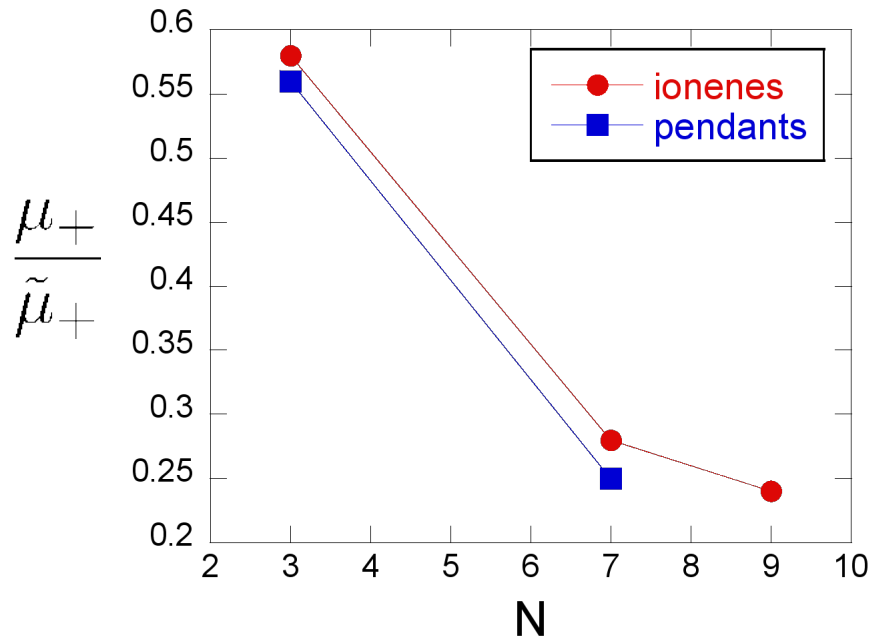


in linear response regime
polymers are short so they also move

Ion Mobilities

from non-equilibrium simulation in field: $\mu_i = \langle v_{x,i} \rangle / E$

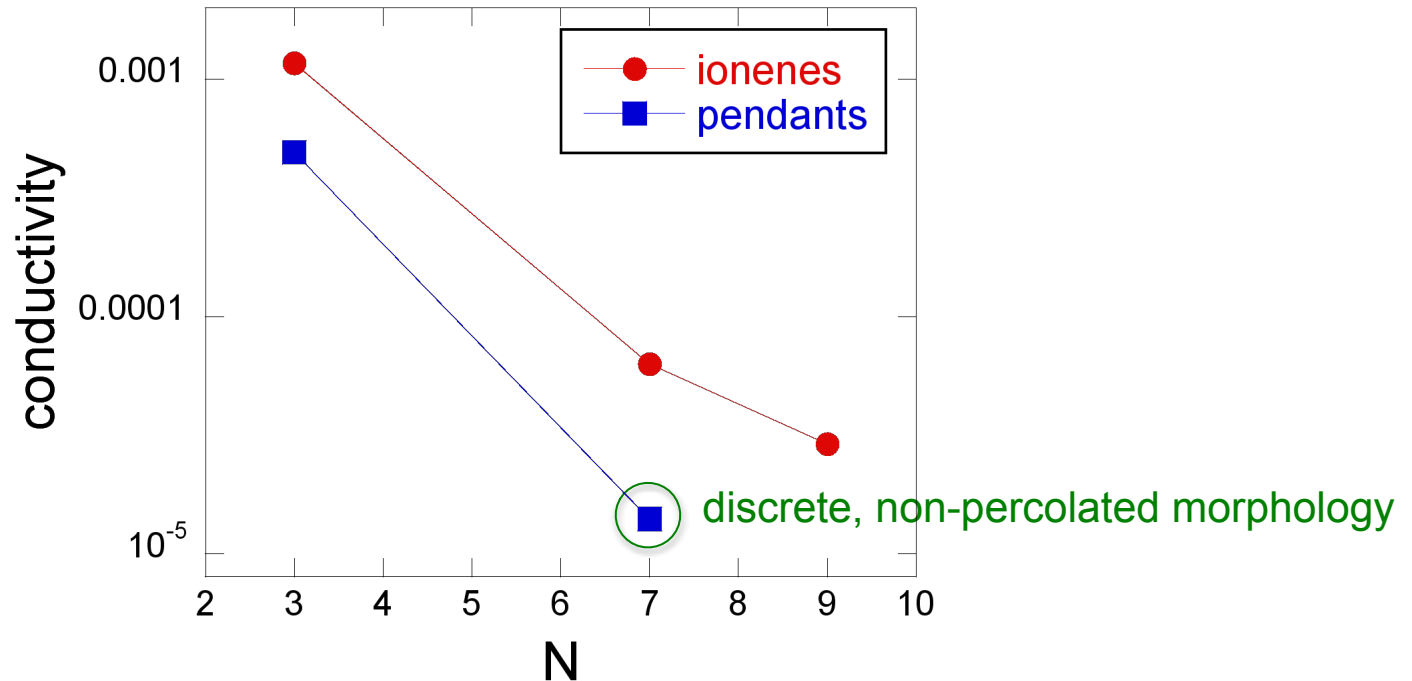
from equilibrium Einstein relation $\tilde{\mu}_i = zeD_i/kT$



ion motion is correlated

Conductivity

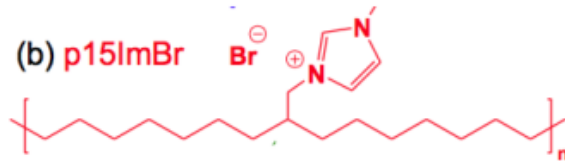
$$\lambda = \rho e(\mu_+ - \mu_-)$$



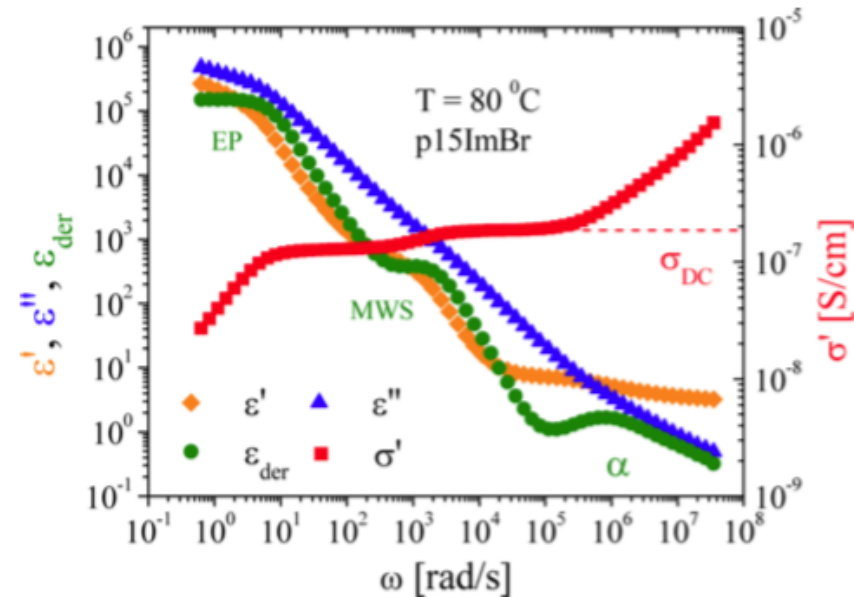
- conductivity decreases with decreasing ion concentration
- lowest for non-percolated aggregate morphology

Oscillating fields

Why? would like to understand DRS experiments



$$\epsilon_{der} = -\frac{\pi}{2} \frac{\partial \epsilon'(\omega)}{\partial \ln \omega}$$



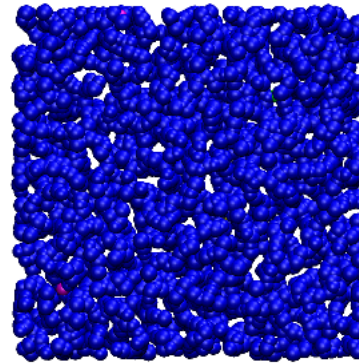
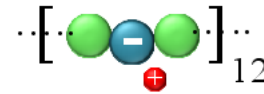
- how many free ions? ion pairs? aggregates?
- what molecular motions lead to the α relaxation?
- how is the MWS relaxation related to the aggregate morphology?

Oscillating Electric Fields

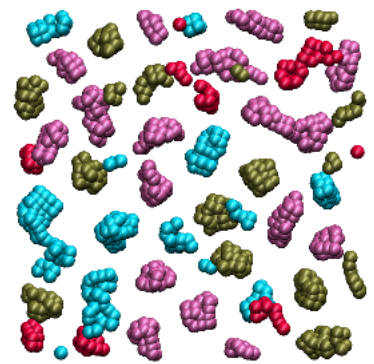
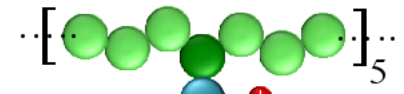
systems simulated

- a fast, percolated system: ionenes with $N = 3$, “i3”
- a isolated cluster system: pendants with $N = 7$, “p7”
- polymers have 36 (i3) and 35 (p7) backbone beads
- also simulate 1 repeat unit of each, the “monomers”

a) ionene, $N = 3$



b) pendant, $N = 7$



apply field in
x direction

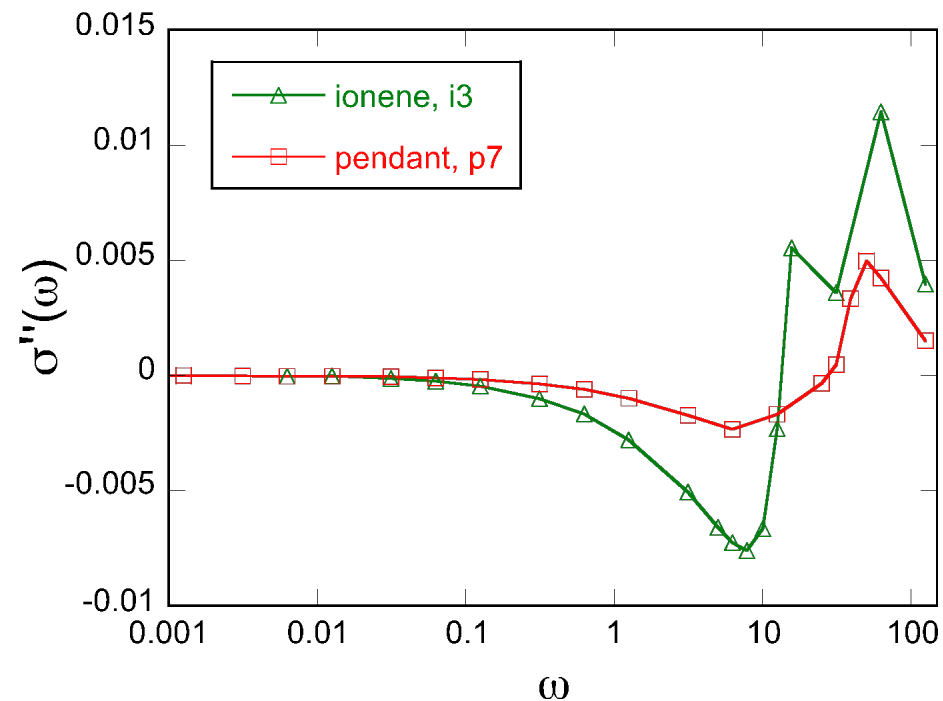
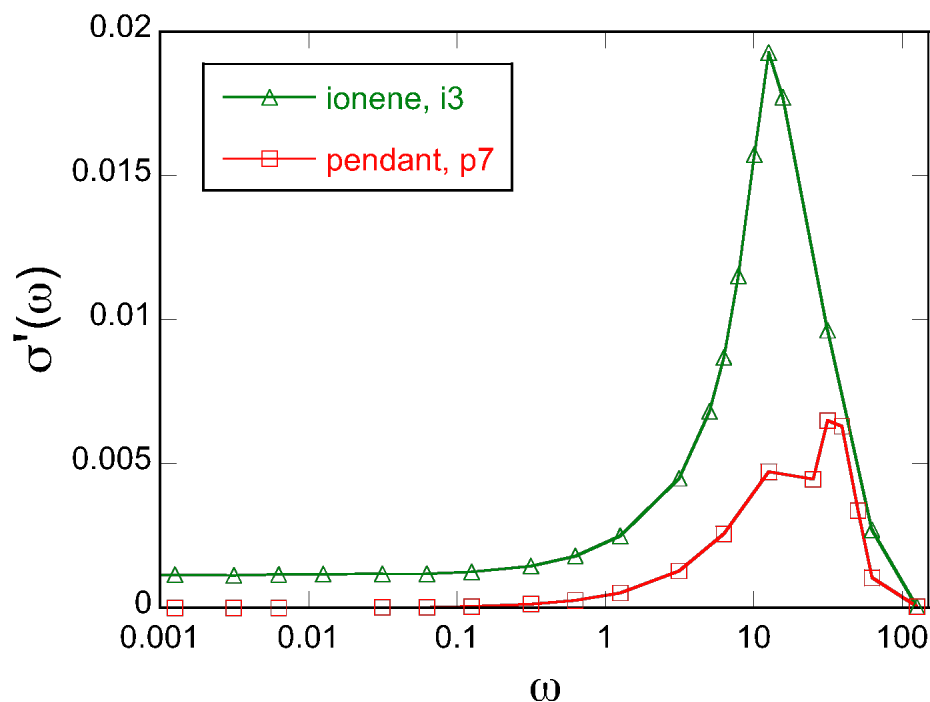
$$E_x = E_0 \sin \omega t = \text{Re} \left(E_0 i e^{-i\omega t} \right)$$

$E_0 = 1$ is in linear response regime

Frequency-dependent $\sigma(\omega)$

apply field $E_x = E_0 \sin \omega t = \text{Re} (E_0 i e^{-i\omega t})$

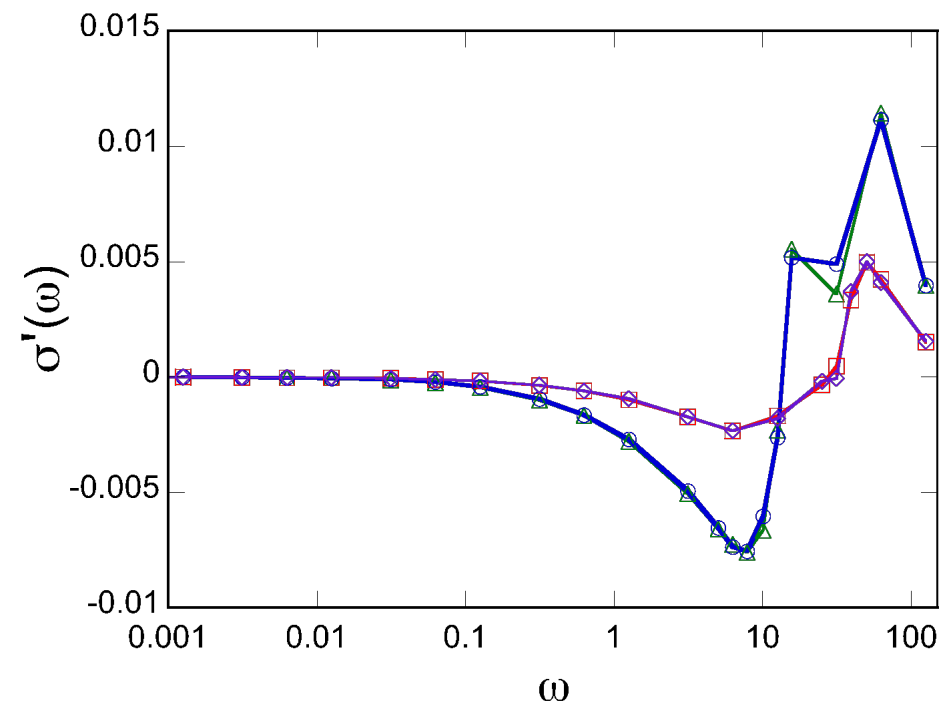
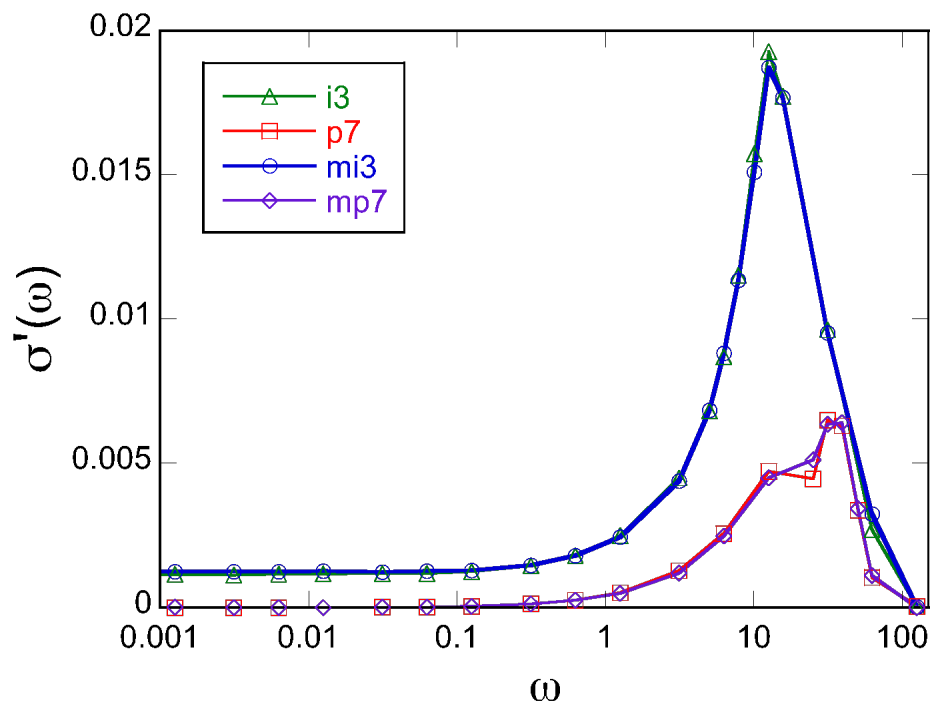
calculate current $j_x(\omega, t) = \frac{e}{V} \sum_i z_i v_{x,i} = \sigma(\omega) E_x(\omega, t)$



Frequency-dependent $\sigma(\omega)$

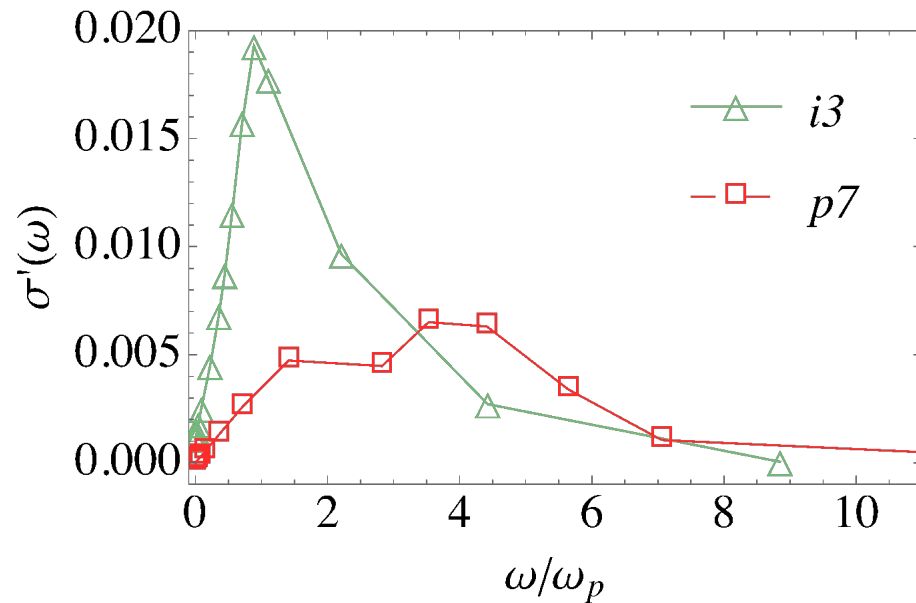
apply field $E_x = E_0 \sin \omega t = \text{Re} (E_0 i e^{-i\omega t})$

calculate current $j_x(\omega, t) = \frac{e}{V} \sum_i z_i v_{x,i} = \sigma(\omega) E_x(\omega, t)$

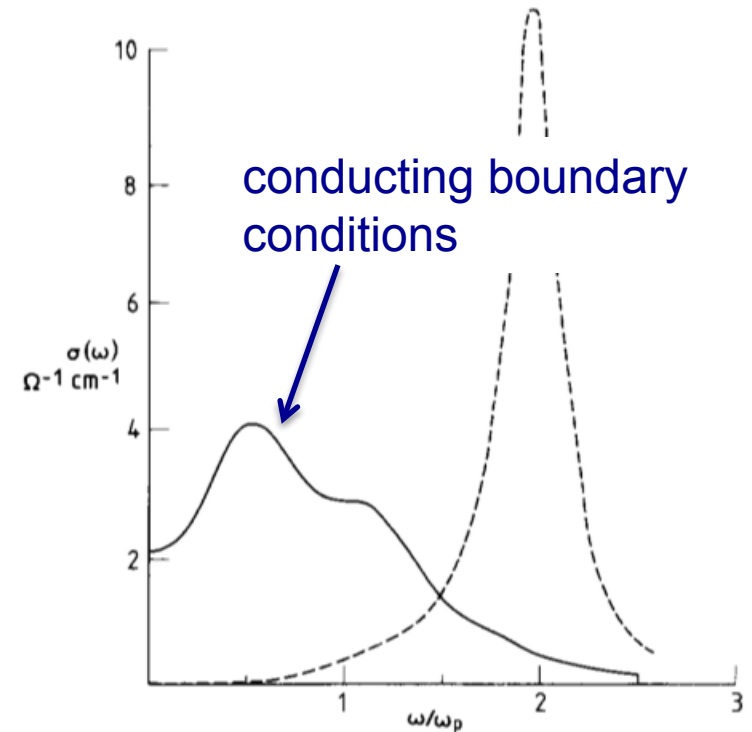


Plasma Oscillations

peak near plasma frequency ω_p



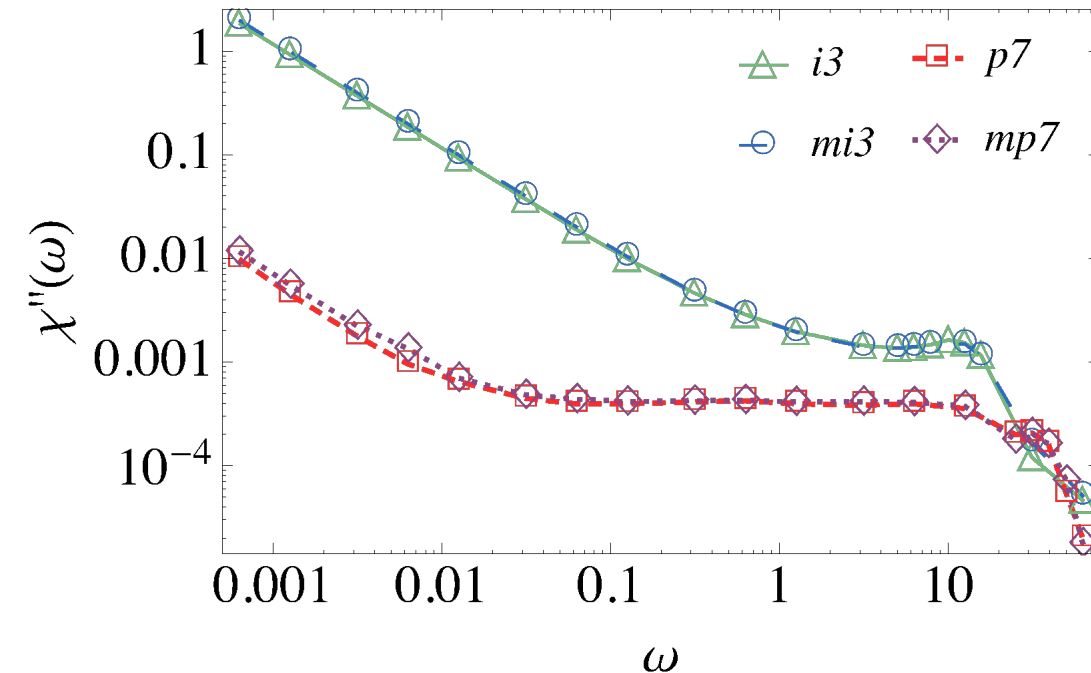
MD simulations of molten salt



De Leeuw, S. W. & Perram, J. W. *Physica A* 107A, 179 (1981)

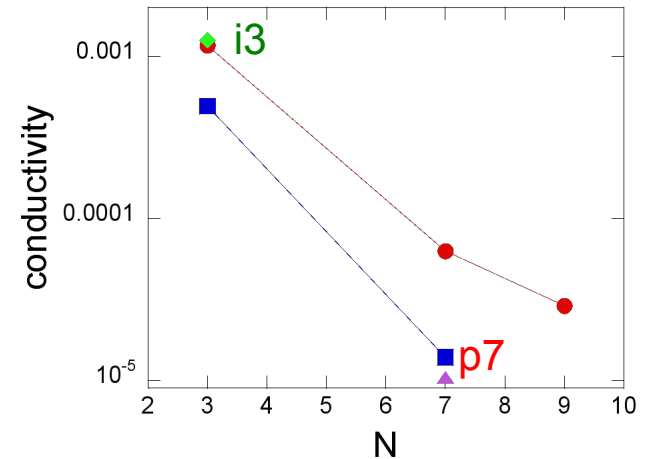
Lower Frequencies

$$P_x(\omega, t) = \frac{e}{V} \sum_i z_i r_{x,i} = \chi(\omega) E_x(\omega, t)$$



$$\sigma(\omega) = -i\omega\chi(\omega)$$

$$\sigma'(0) = \lim_{\omega \rightarrow 0} (\omega\chi''(\omega))$$

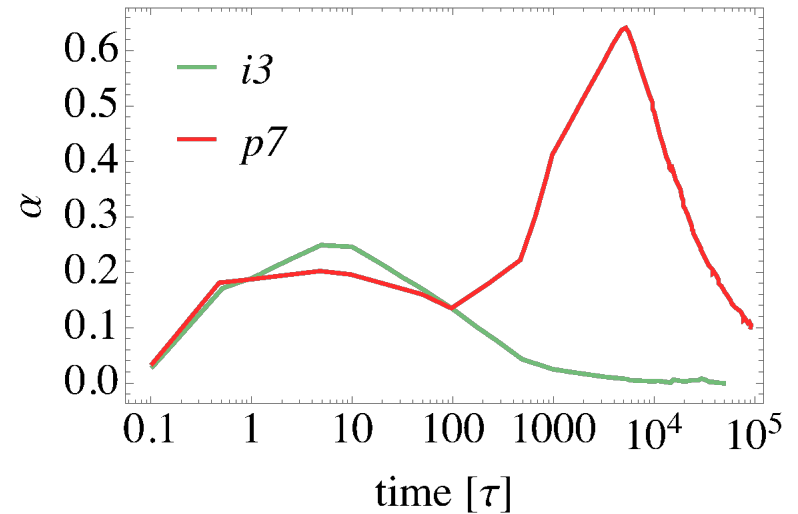
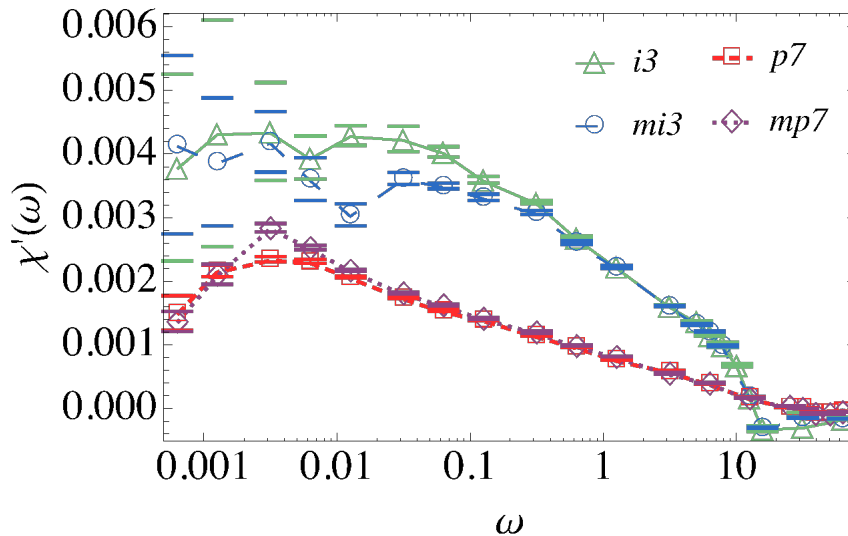


scales as $1/\omega$ as $\omega \rightarrow 0$

conductivity agrees with static calculation

Lower Frequencies

$$P_x(\omega, t) = \frac{e}{V} \sum_i z_i r_{x,i} = \chi^*(\omega) E_x(\omega, t)$$



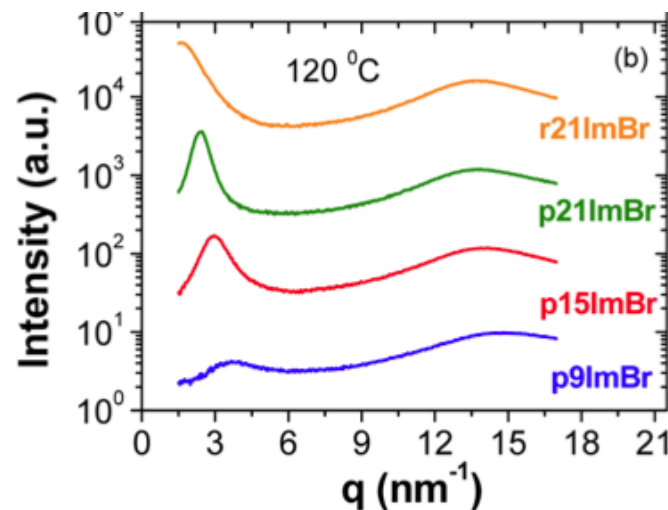
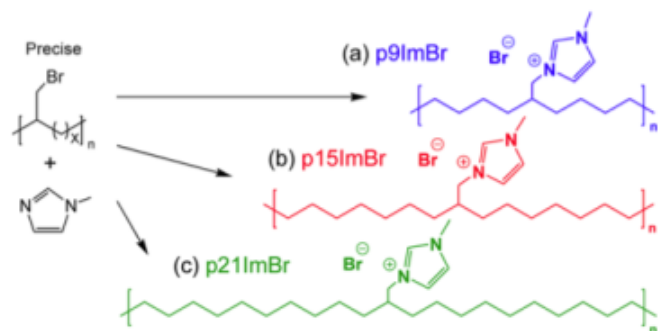
cluster relaxation times from $S(k, t)$

iN3 $1/\tau^* \approx 0.02/\tau$
pN7 $1/\tau^* \approx 0.0001/\tau$

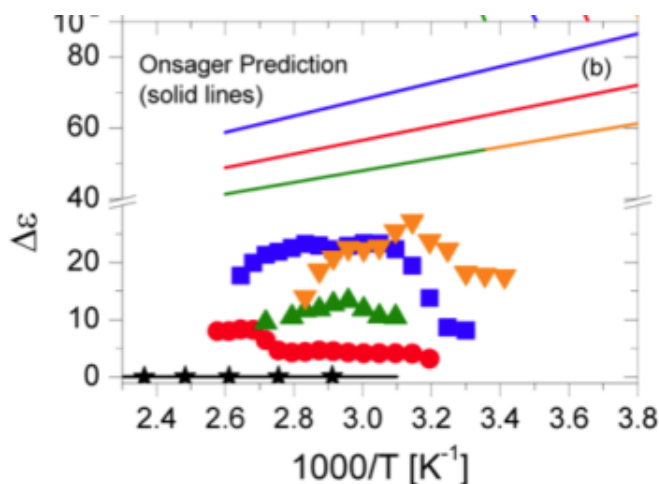
- can't resolve cluster rearrangements in p7
- do see chain/cluster dynamics in i3, mi3

Compare to Experiment

precise PE-ImBr ionomers

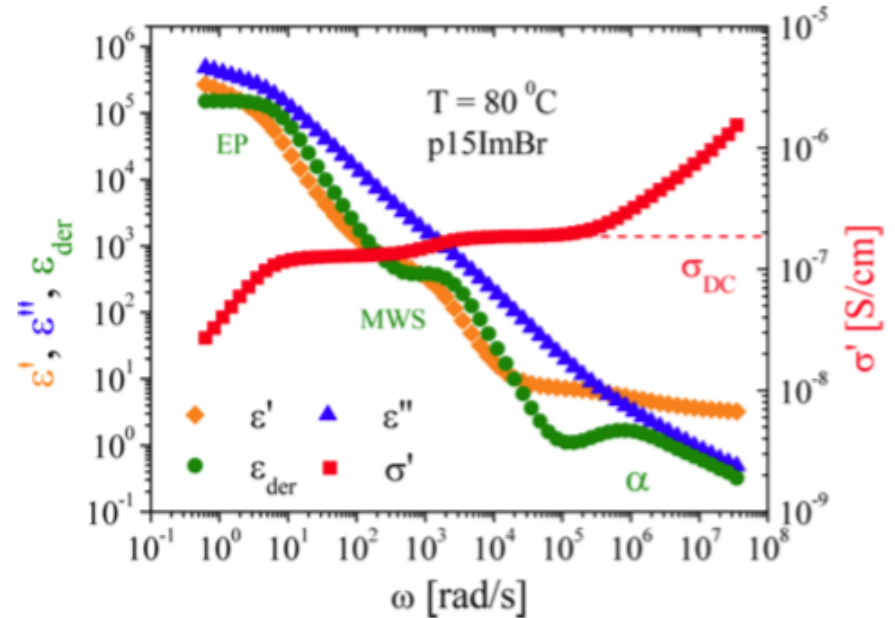
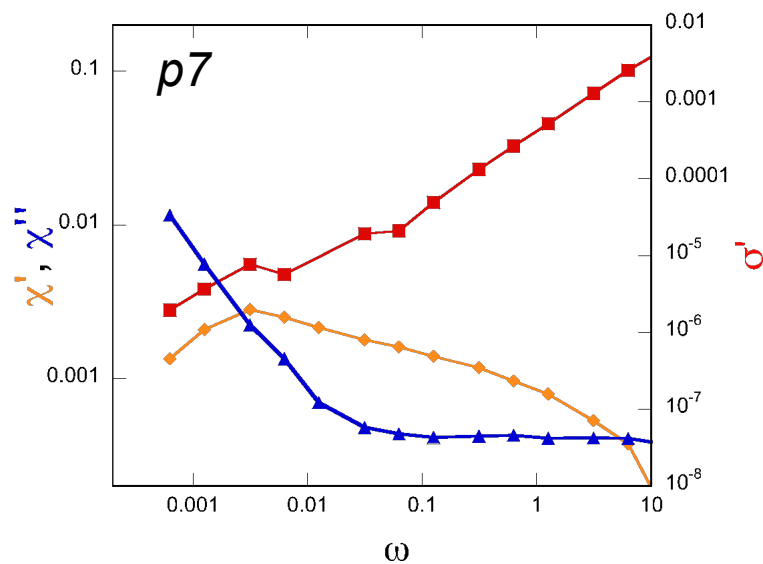
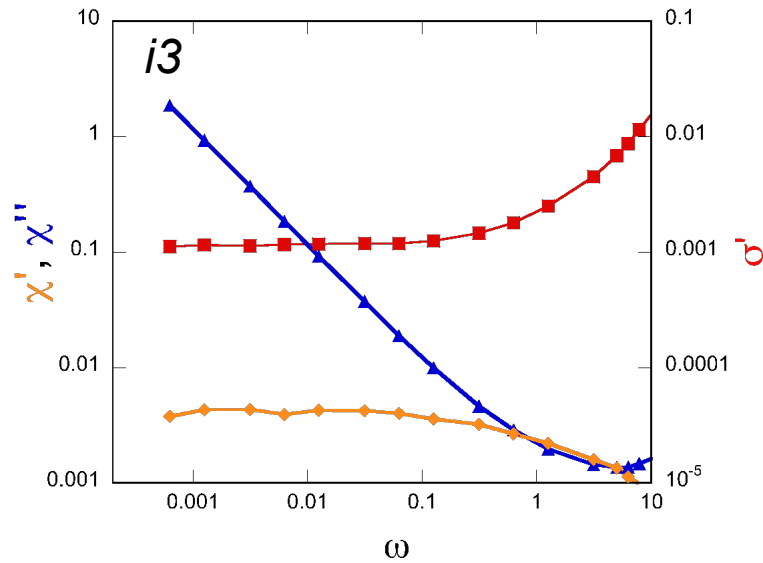


dielectric strength of α process



- ImBr form ionic aggregates
- dielectric response primarily due to ions
- some fraction of ions participate in α process

Compare to Experiment



simulations too noisy to resolve α process
shapes of spectra similar to experiment

Conclusions

- molecular architecture important
 - isolated aggregates for pendants or large spacing
 - percolation for ionenes or short spacing
- ion motion by cluster rearrangement
- ion motion is correlated
- higher conductivity in percolated morphologies
- methodology for extracting $\sigma(\omega)$, $\chi(\omega)$ from simulations

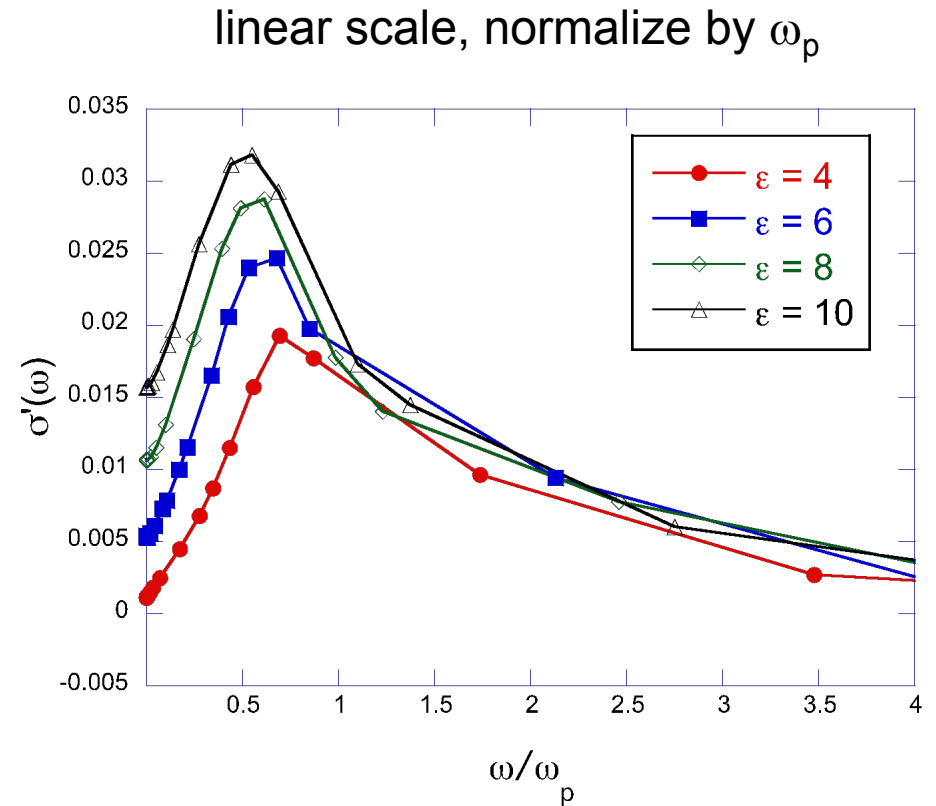
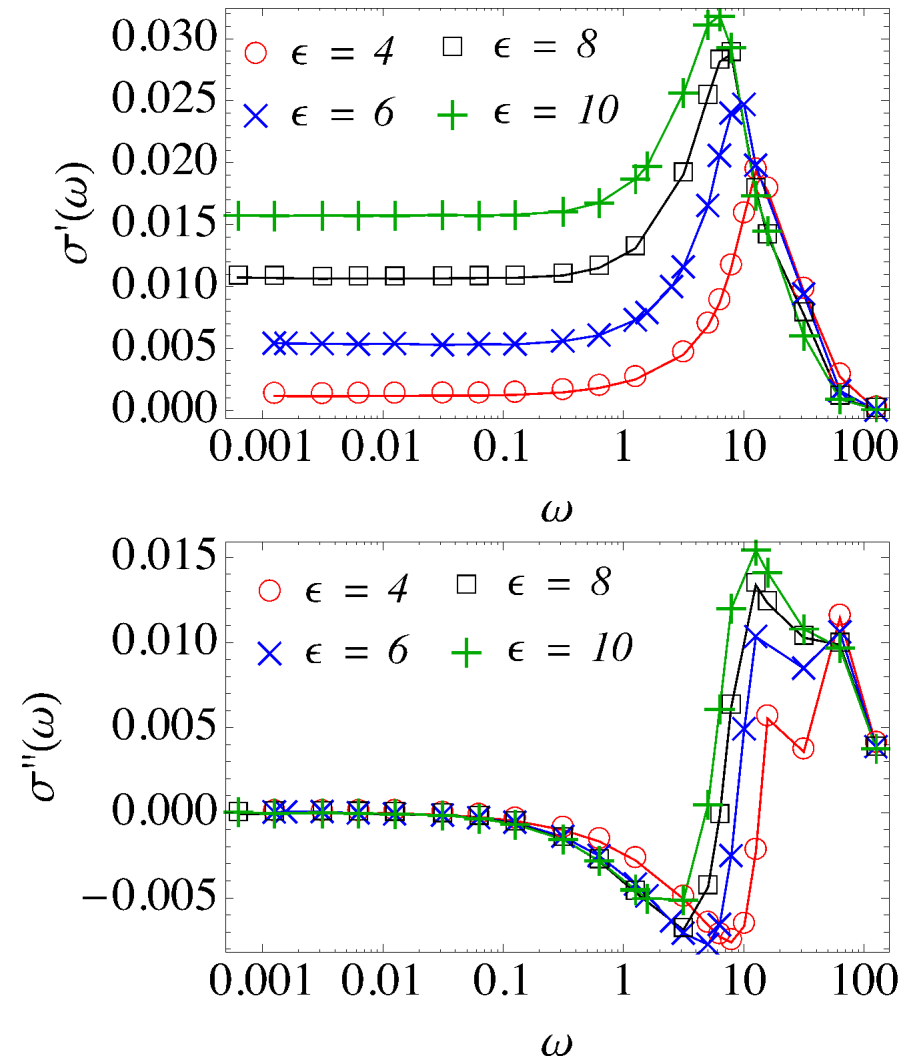
coarse-grained

Hall, et al., *Phys Rev Lett* 106, 127801 (2011);
JACS 134, 574 (2012);
Macromolecules, 45, 8097 (2012);
Ting et al., *Macromolecules* 48, 809 (2015);
Ting et al., in preparation (2016)

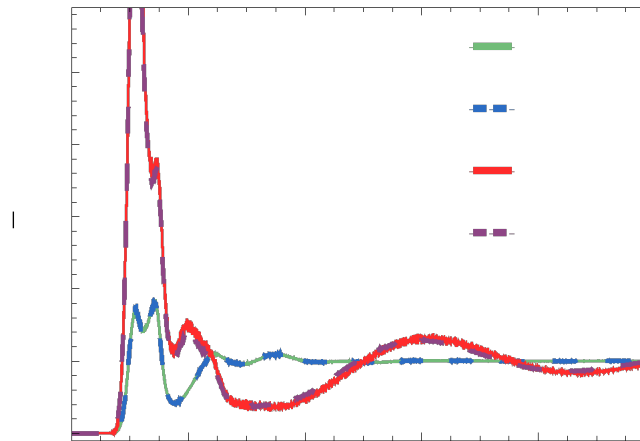
atomistic

Bolintineanu et al., *ACS Macro Lett.* 2, 206 (2013);
Bolintineanu et al., *Macromolecules* 46, 5381 (2013);
Lueth et al., *J Chem Phys* 140, 054902 (2014);
Buitrago et al., *Macromolecules* 48, 1210 (2015)

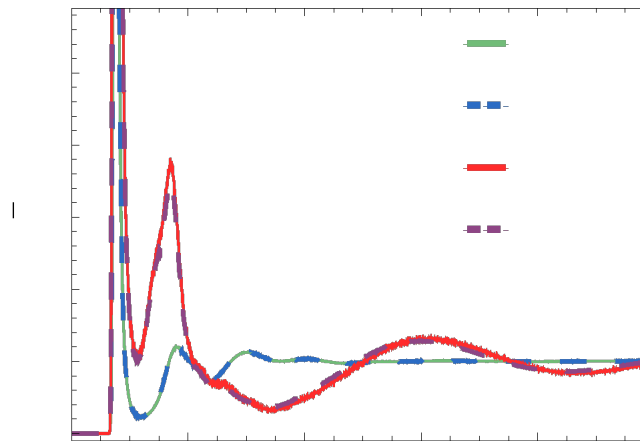
Dependence on ϵ : iN3



Monomer vs Ionomer Structure

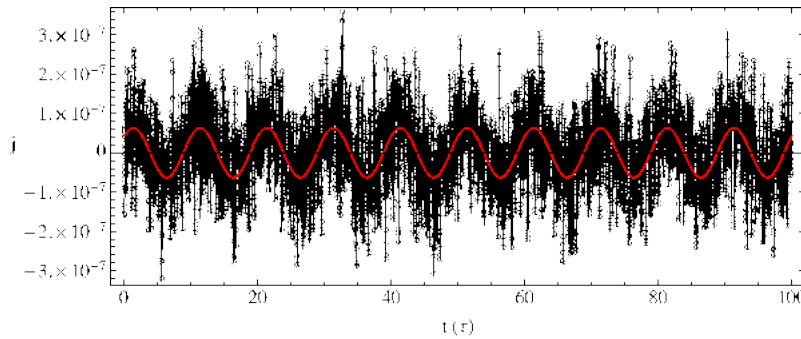


$[\sigma]$



$[\sigma]$

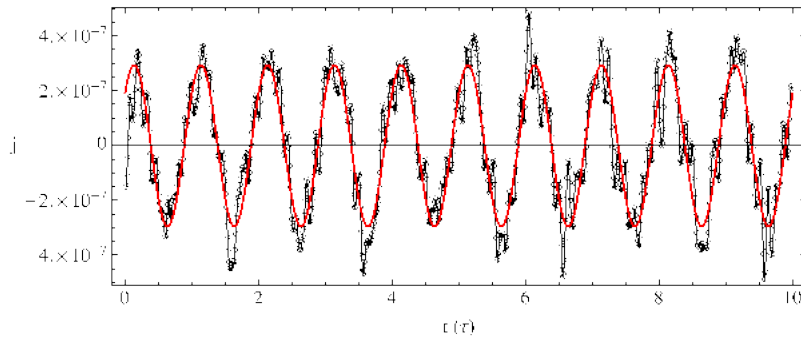
Current Density



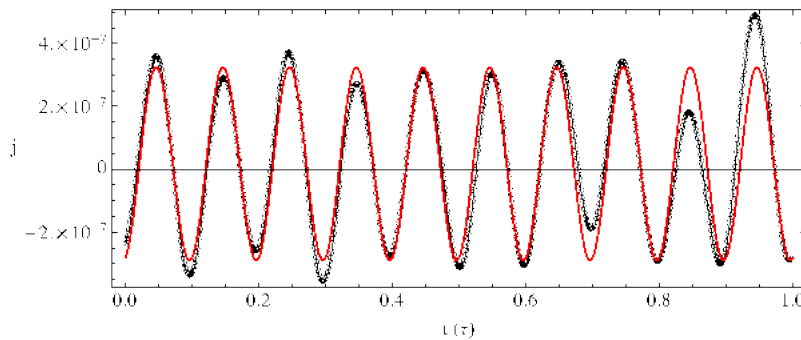
$$\omega = 0.1/\tau$$

i3 system

$$\omega_p = 14.2/\tau$$



$$\omega = 1.0/\tau$$



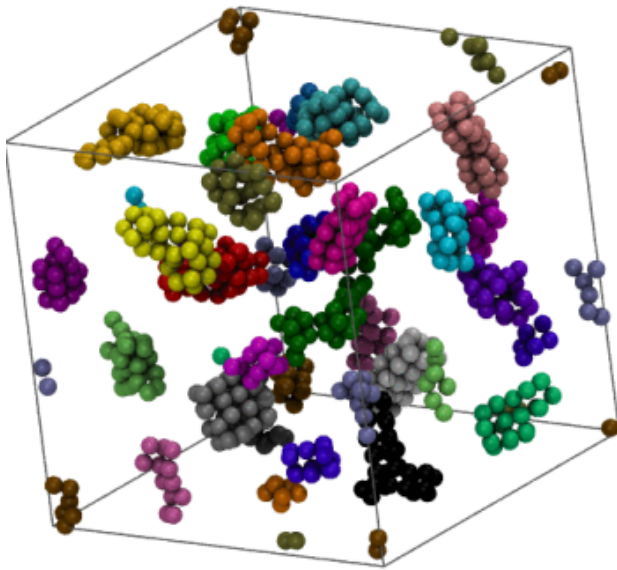
$$\omega = 10.0/\tau$$

Cluster Dynamics

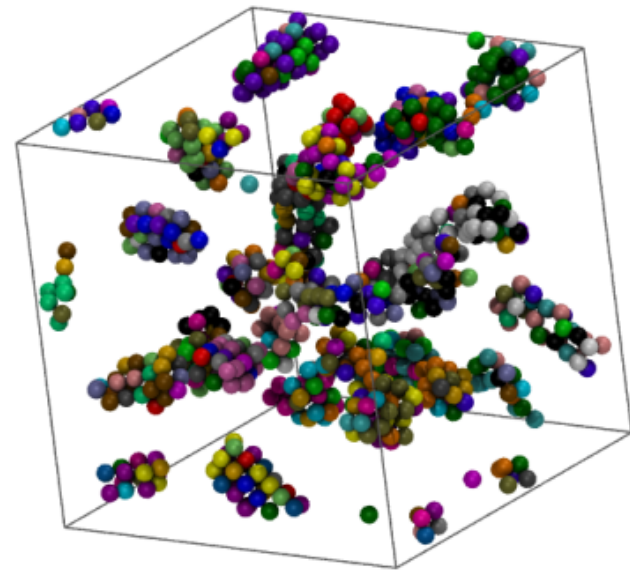
Is there any?

Color distinct clusters by
different color

Start



Finish (10^7 steps later)
 $t = 50,000 \tau$

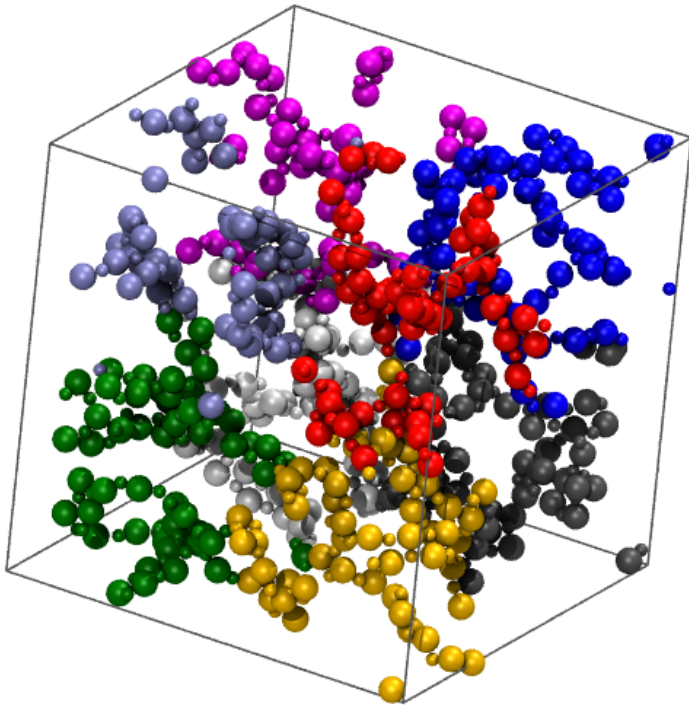


Ions move.

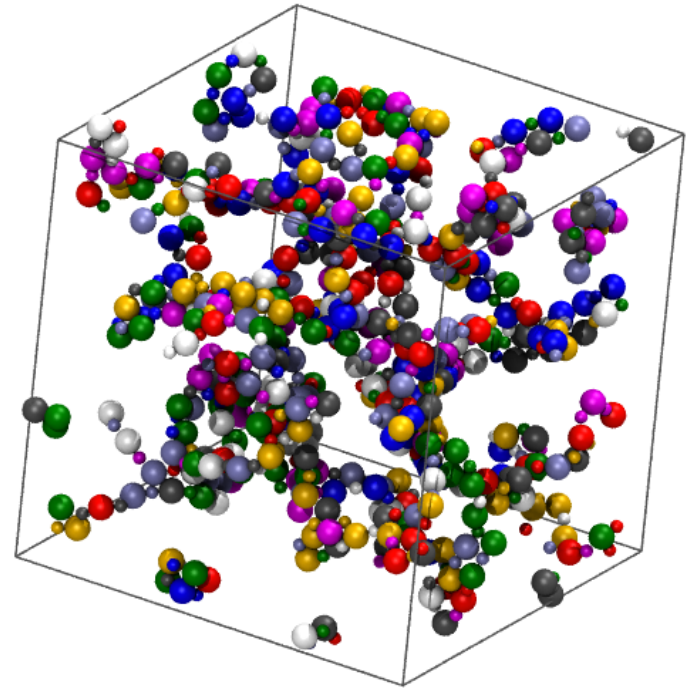
Cluster Dynamics

ionenes

Start

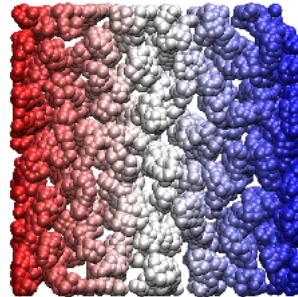


Finish (10^7 steps later)



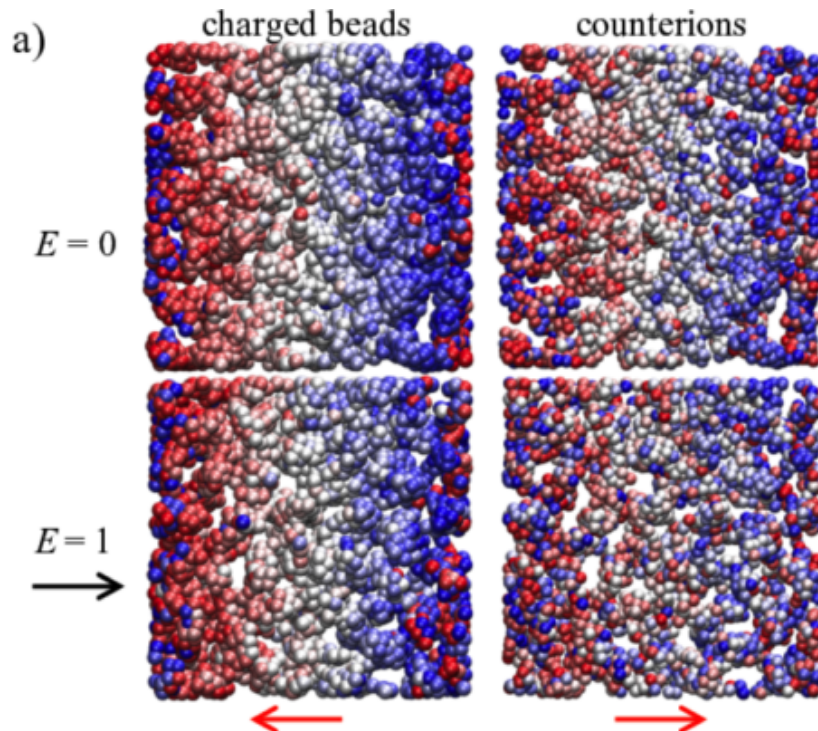
Field does not enhance mixing

$t = 0$



pendants, $N = 9$

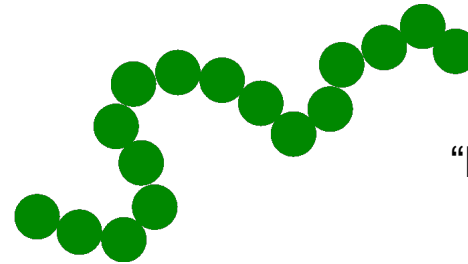
$t = 7.5 \times 10^4 \tau$, $\langle r_x^2 \rangle_0 \approx 25$



- field biases ion motion in field direction
- mixing occurs once $\langle r_x^2 \rangle_0 \approx 100$
 - independent of field
 - mixing by thermal motion

Molecular Dynamics Simulations

bead-spring polymer model
(Kremer & Grest, 1990)

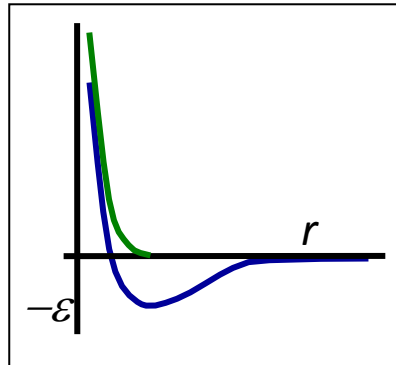


“bead” diameter σ

interactions between all “beads”

Lennard-Jones potential:

$$u_{LJ} = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]$$



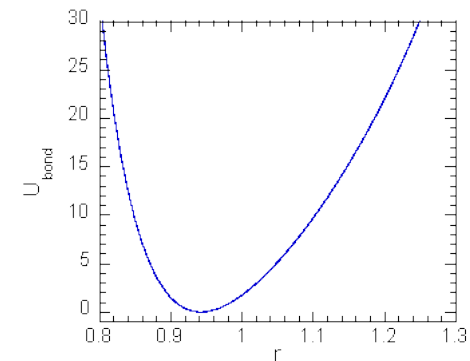
+ Coulomb interactions

$$U(r) = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon r}$$

interactions between bonded beads

FENE springs $u(r) = -kR_0^2 \ln \left(1 - (r / R_0)^2 \right)$

$$U_{\text{bond}} = u_{LJ} + u$$



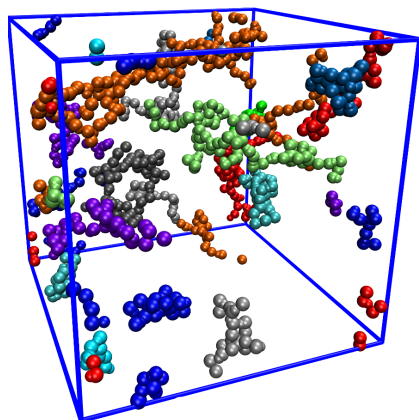
+ temperature

$$f_i = -m_i \Gamma \nu_i + W_i(t)$$

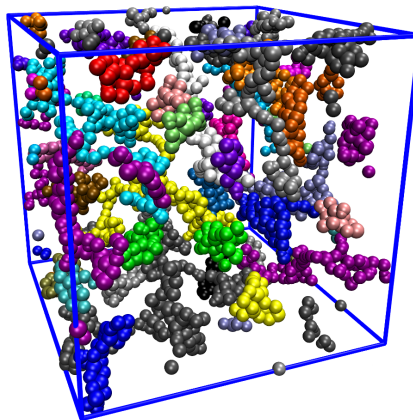
Morphology: Li-neutralized pAA

coloring by cluster

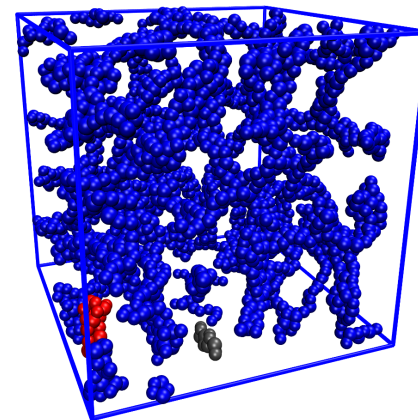
p9AA-10%Li



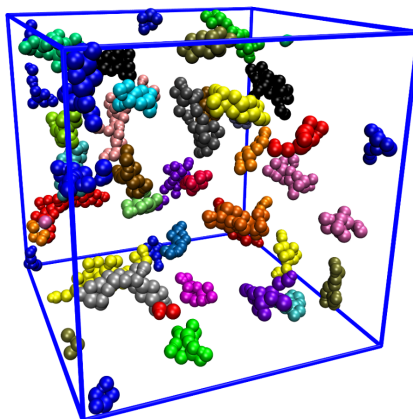
p9AA-43%Li



p9AA-100%Li

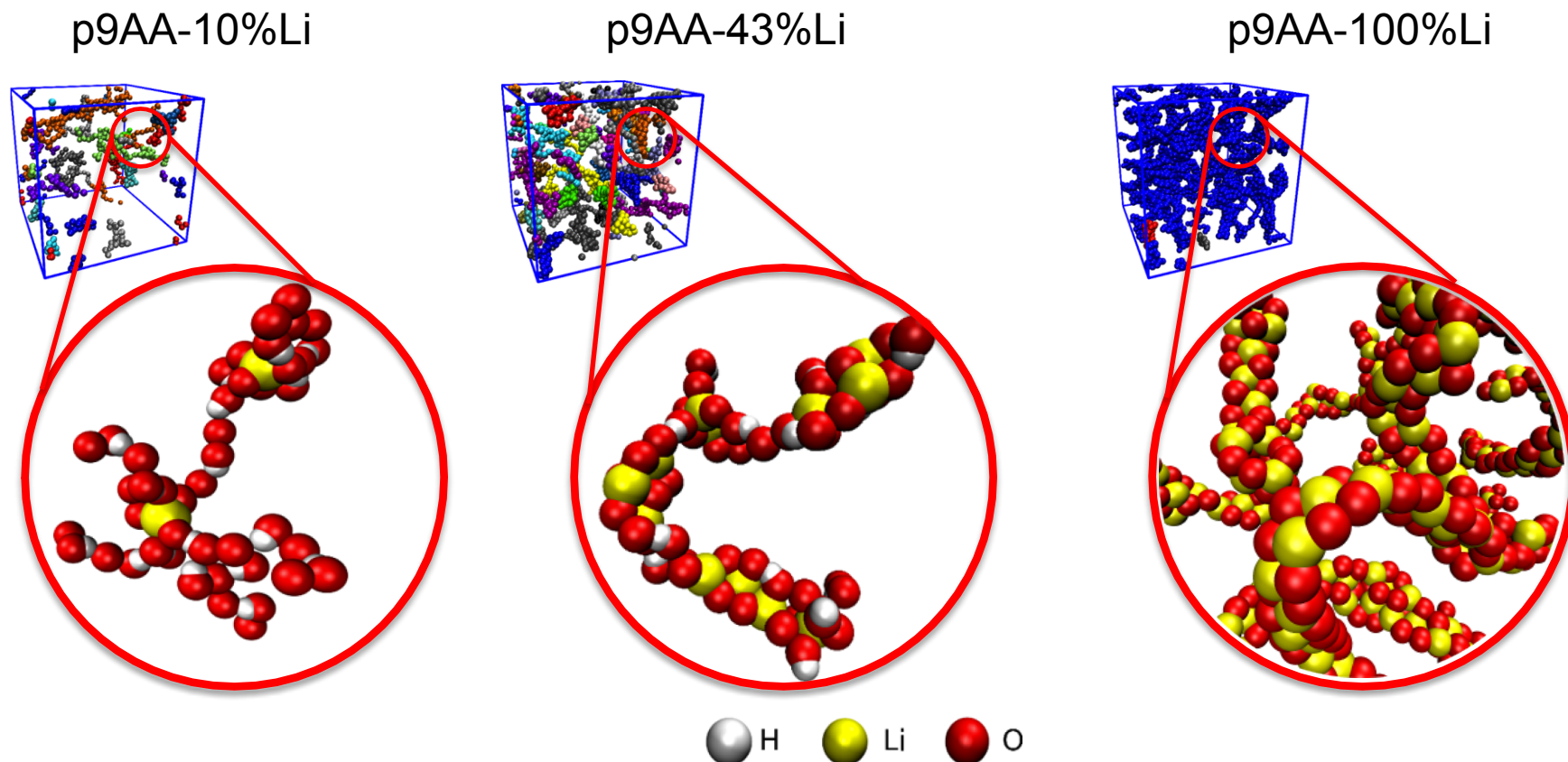


p21AA-43%Li



Bolintineanu et al, *ACS Macro Lett*, 2013

Closer look at aggregates

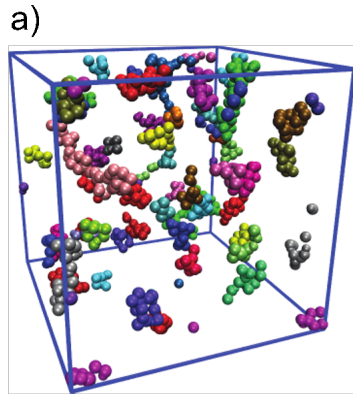


Two mechanisms of aggregate formation:

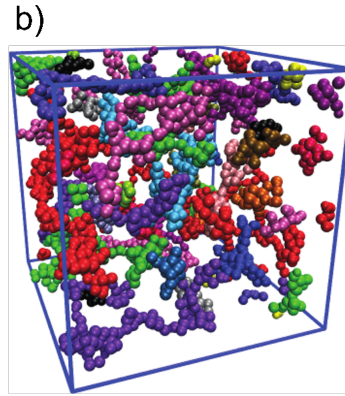
1. Counterion-oxygen association → dominant at **moderate to high** neutralization
2. Hydrogen-bonded networks → dominant at **low** neutralization

Comparison to X-ray Scattering

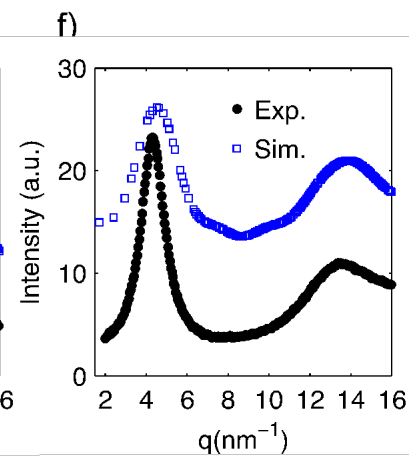
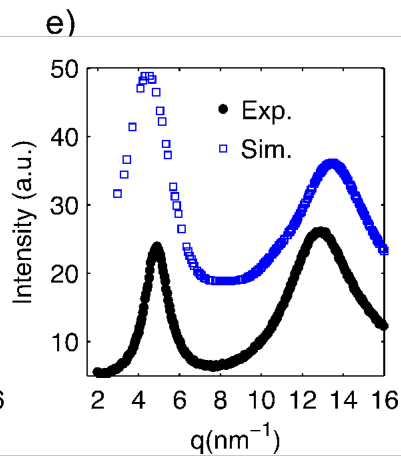
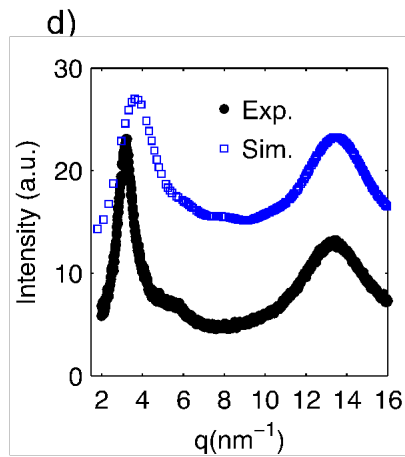
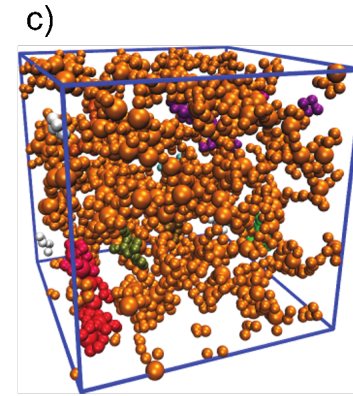
p21AA-56%Zn
Type 1



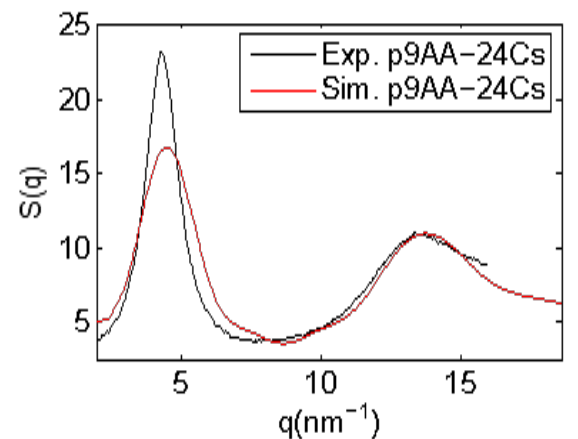
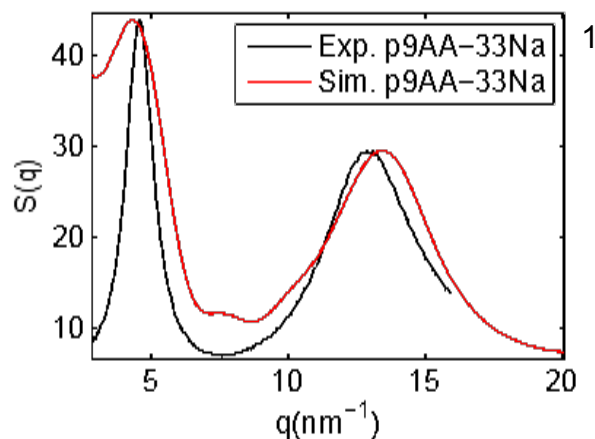
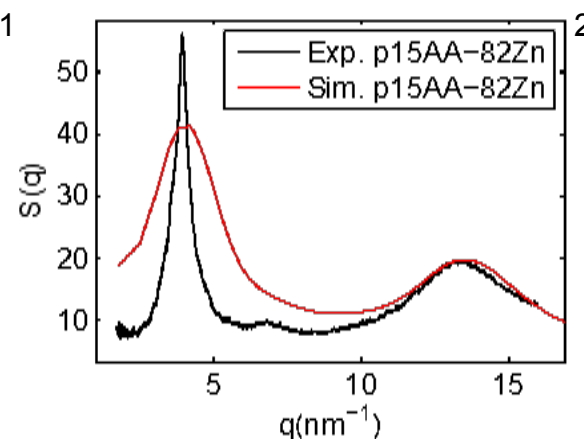
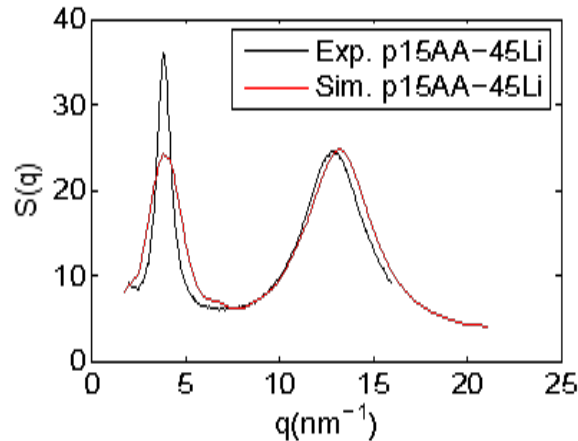
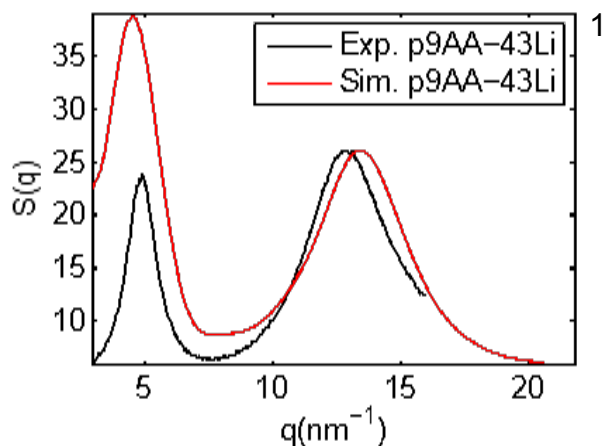
p9AA-43%Li
Type 2



p9AA-24%Cs
Type 3



Direct Comparison



- 120°C, same neutralization
- $S(q)$ scaled to match amorphous halo height

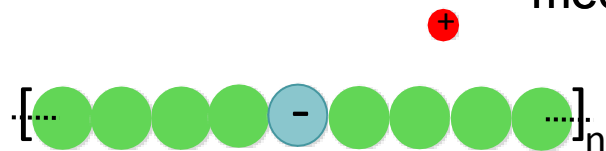
¹ Buitrago et al, Macromolecules 48, 1210 (2015)

² Seitz et al, JACS 132, 8165 (2010)

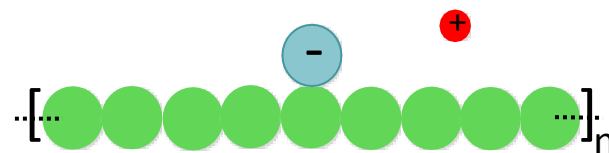
- excellent agreement in peak positions
- good agreement in peak shapes

Ion Trajectories

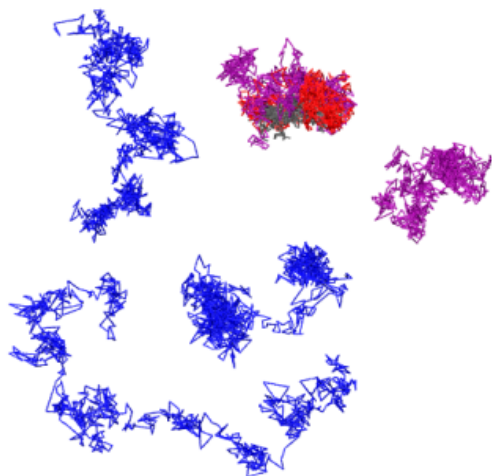
mechanism is not standard hopping



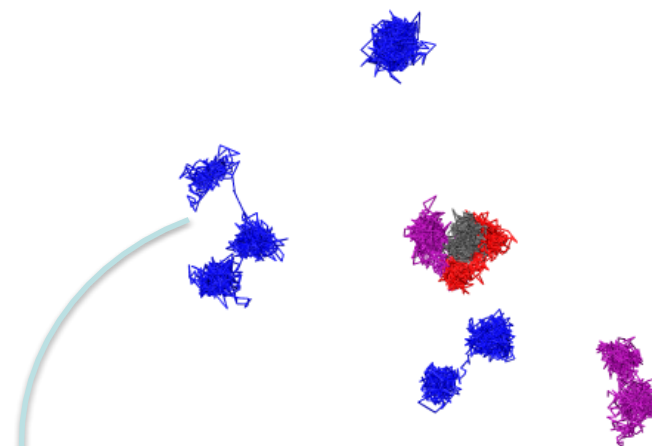
periodic ionenes $N = 9$



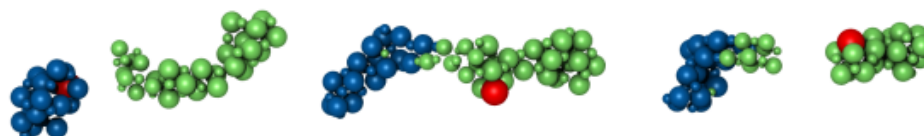
periodic pendants $N = 9$



4 counterion trajectories (blue)
and 3 anion trajectories
(red and purple on one polymer, polymer
center of mass in grey, another anion in
purple)
1000 steps of 50τ each



this counterion (enlarged in red)
and nearby clusters
before, during, and after its "hop"
(total time 1000τ)



Static Electric Field

add force $F_x = qE_x$ to each ion

how strong a field should we add?

electrostatic force $\frac{F}{kT\sigma} = -\frac{q_i q_j \ell_B}{r^2 \sigma}$

LJ units: $|q| = 1$, $kT = 1$, $\sigma = 1$; $\ell_B/\sigma = 35.7$

at contact, $r = 0.75\sigma$: $F = -63/kT\sigma$

for field $E^* = \frac{kT}{q\sigma} = 1$ $F = 1/kT\sigma$

rough estimate in real units:

$\sigma = 0.4$ nm, $T = 298$ K, $E = 0.8$ V/nm = 8×10^6 V/cm

Ionomer MD Simulations

repulsive LJ interactions + FENE springs ...

+ Coulomb interactions

$$U(r) = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon r} \quad \epsilon = 4$$

+ temperature

NVT ensemble: Langevin thermostat

$$f_i = -m_i\Gamma\nu_i + W_i(t)$$

noise W sets temperature

- 800 chains of 35-36 beads
- 4-12 charges per chain
- 1 cation per charged bead (anion)
- equilibrate for 10^7 timesteps
- collect averages for 4×10^7
- 1M CPU-hours $\approx$ 325 days on 128 cores

LAMMPS: open source MD code from Sandia
<http://lammps.sandia.gov/>



2,816 nodes / 22,528 cores

