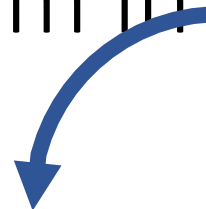


Using symmetry band structure in the continuum in recreate bound nuclear crystals



Alexander Cerjan,* Christina Jörg,* Sachin Vaidya, Shyam Augustine, Wladimir A. Benalcazar, Chia Wei Hsu, Georg von Freymann, and Mikael C. Rechtsman

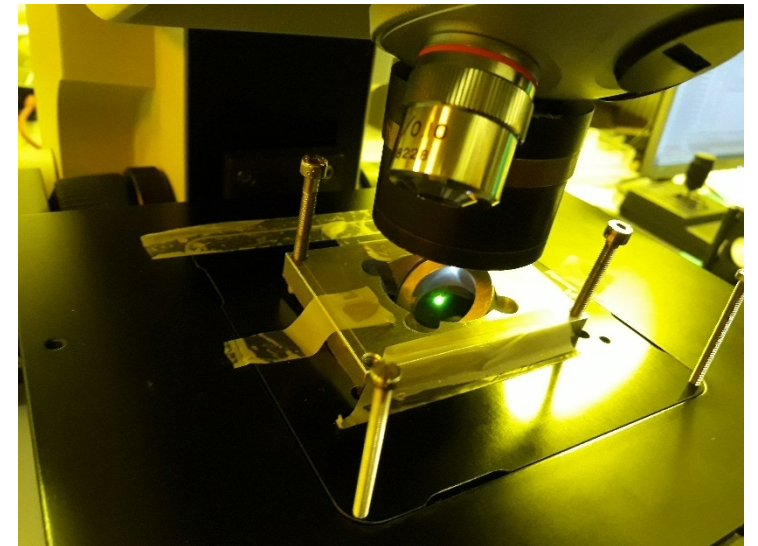
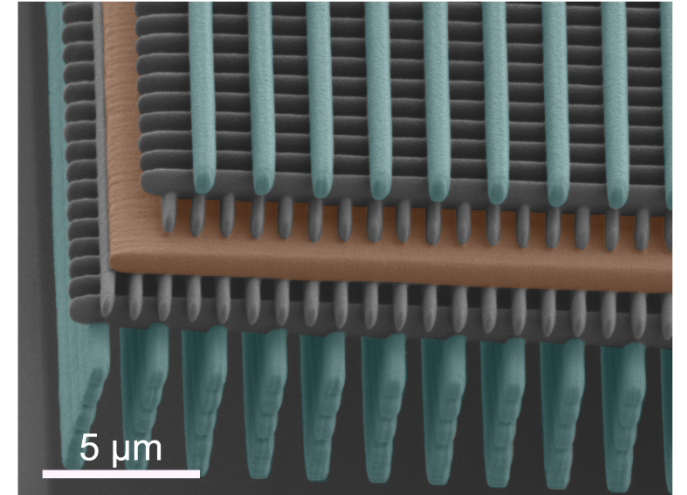
CLEO 2021, May 13th

FTh1M.5



Outline

- Review the differences between resonances and bound states in the continuum (BICs) in photonic crystal slabs and metasurfaces
 - Applications
 - Limitations
- Analytical proof of the limitations of symmetry-protected BICs in homogeneous, isotropic radiative environments
- Overcoming these limitations using a 3D photonic crystal as the radiative environment
 - Theory and experiment



Types of states in photonic crystal slabs

Outside the slab:

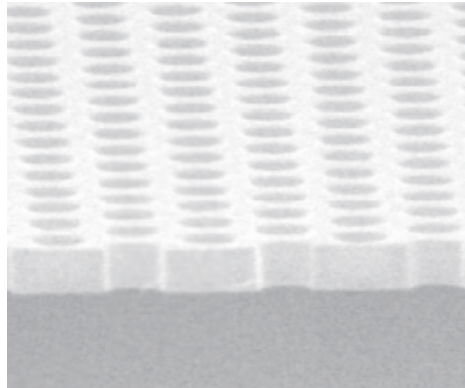
$$\omega = c|\mathbf{k}|$$

Conservation of momentum during radiation,
 $\mathbf{k}_{\parallel,\text{in}} = \mathbf{k}_{\parallel,\text{out}}$

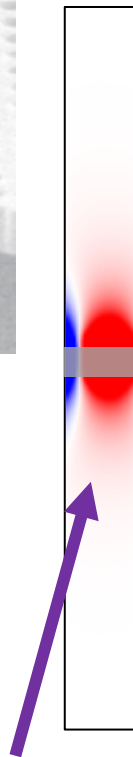
Minimum allowed frequency to radiate $\omega = c|\mathbf{k}_{\parallel}|$

Bound modes: $\omega < c|\mathbf{k}_{\parallel}|$

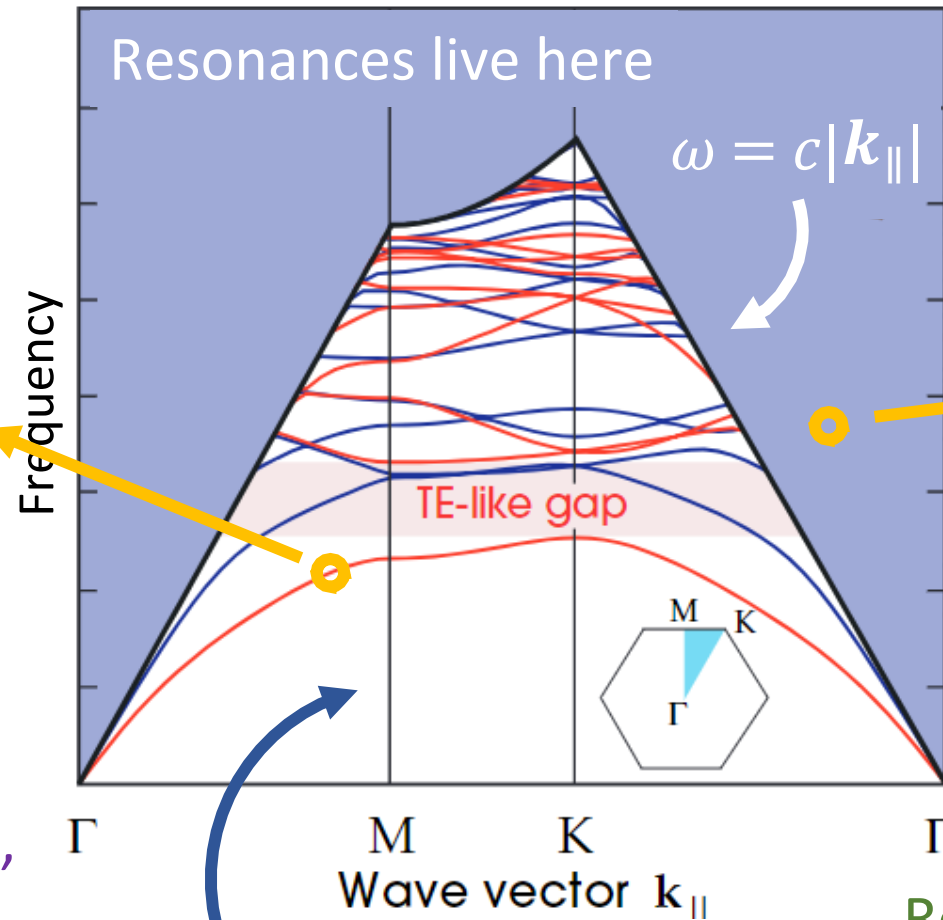
Resonances: $\omega > c|\mathbf{k}_{\parallel}|$



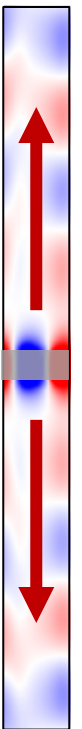
Sugimoto et al.,
Opt. Express 2004



Bound mode,
exponential
confinement



Bound modes live here



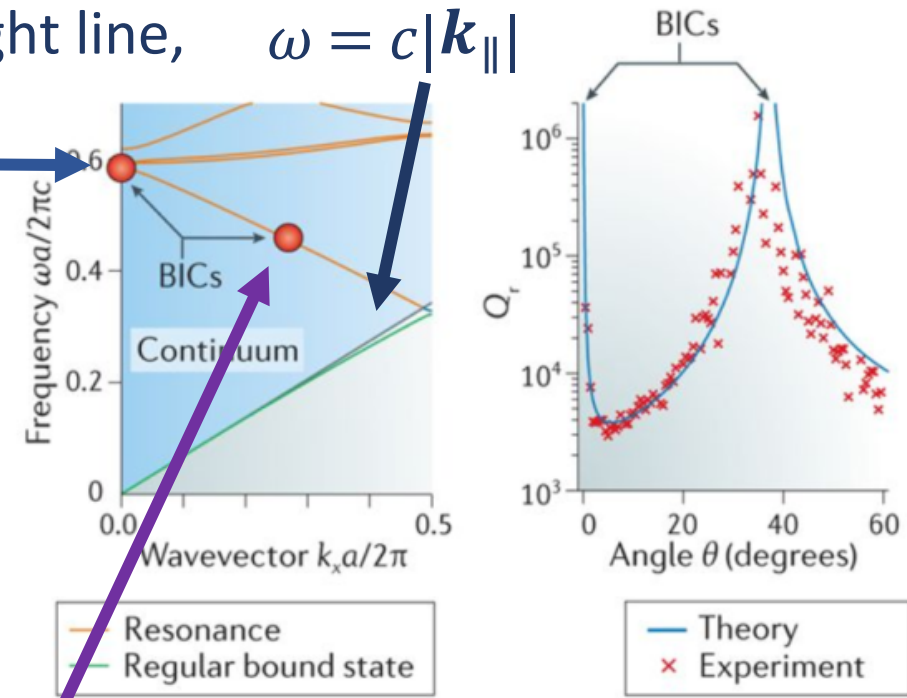
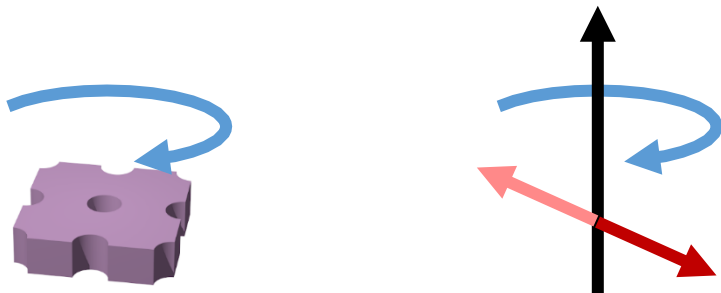
Resonances
radiate

Bound states in the continuum (BICs)

Bound modes above the light line, $\omega = c|\mathbf{k}_{\parallel}|$

Could be symmetry protected from leaking

- Common in slabs at $k_x = k_y = 0$
- Requires rotational symmetry about z-axis
 - Results in a BIC



Could not leak 'accidentally'

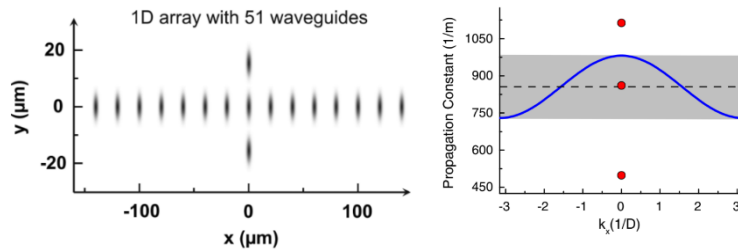
- 2 constraints, d_s, d_p ➤ BIC when $d_s = d_p = 0$
- 2 degrees of freedom, k_x, k_y
 - Results in a BIC

Hsu, Zhen et al., *Nature* **499**, 188 (2013)

Hsu, Zhen et al., *Nat. Rev. Mater.* **1**, 16048 (2016)

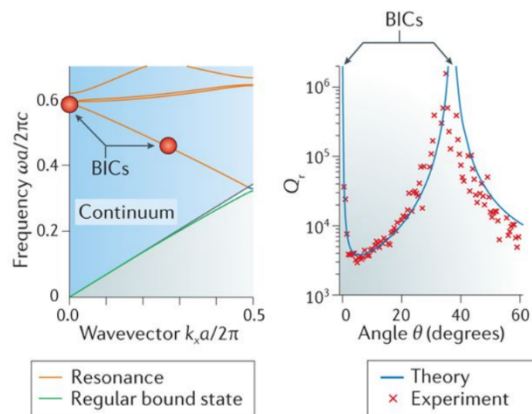
Mechanisms for creating BICs

Symmetry protection



Plotnik et al., *PRL* **107**, 183901 (2011)

Accidentally

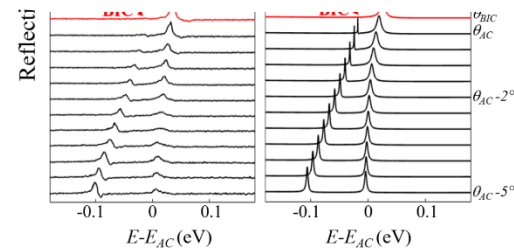


Hsu, Zhen et al., *Nature* **499**, 188 (2013)

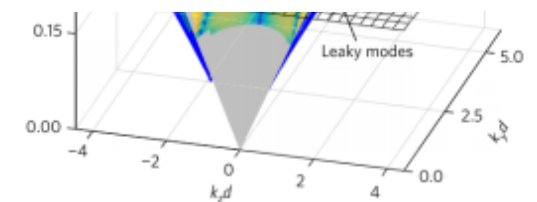
Zhen et al., *PRL* **113**, 257401 (2014)

Applications have almost exclusively focused on symmetry protection

- Predictable
- No fine-tuning required
- Only requires isotropic materials



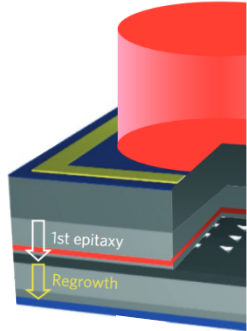
Mermet-Lyaudoz, arXiv:1905.03868



Gomis-Bresco et al., *Nat. Photon.* **11**, 232 (2017)

Uses of symmetry-protected BICs

Photonic Crystals



Hirose et al

Limitations of symmetry-protected BICs:

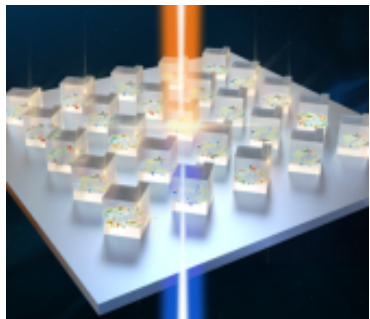
- Only exist at normal incidence
 - Always isolated
- **Forces single frequency, single wavevector operation**

ation

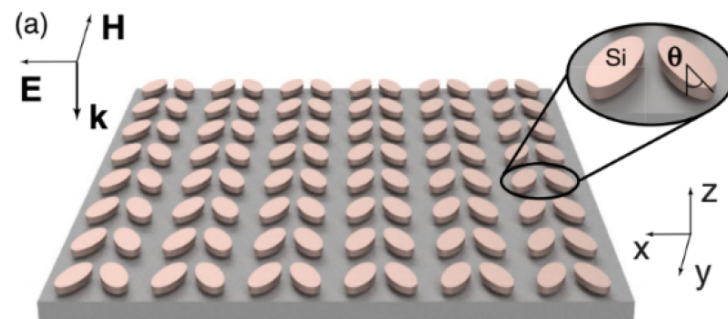


6, 1039 (2019)
7, 1126 (2020)

Controlling reflection and transmission spectra

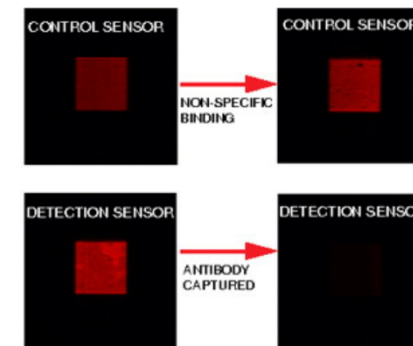


Campione et al., *ACS Photonics* **3**, 2362 (2016)

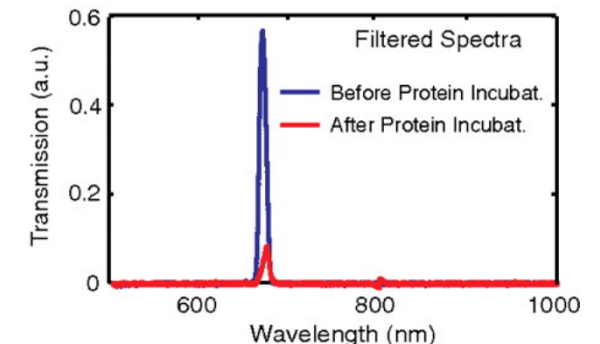


Koshelev et al., *PRL* **121**, 193903 (2018)

sensors



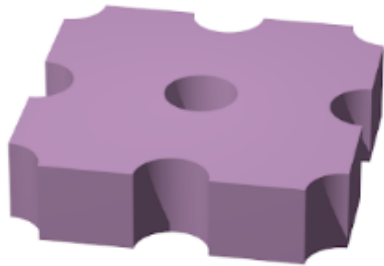
Yanik et al., *Proc. Natl. Acad. Sci.* **108**, 11784 (2011)



Limitations on symmetry-protected BICs

Theorem: In a planar system embedded in isotropic, homogeneous environments, symmetry protected BICs only appear at Γ , below the diffractive limit.

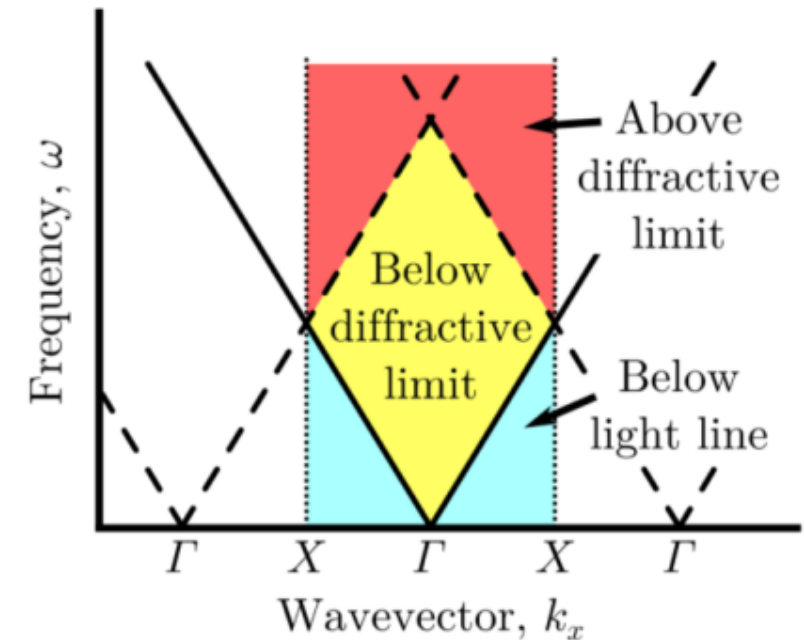
Example: photonic crystal slab surrounded by air



Diffractive limit is

$$\frac{n\omega}{c} \geq |\mathbf{k}_{\parallel} \pm \mathbf{b}_m|$$

(can change momentum when radiating from lattice)



First diffractive order radiative channels span all possible slab symmetries

\mathbf{k}_{\parallel} is the in-plane wavevector

\mathbf{b}_m are the in-plane reciprocal lattice vectors

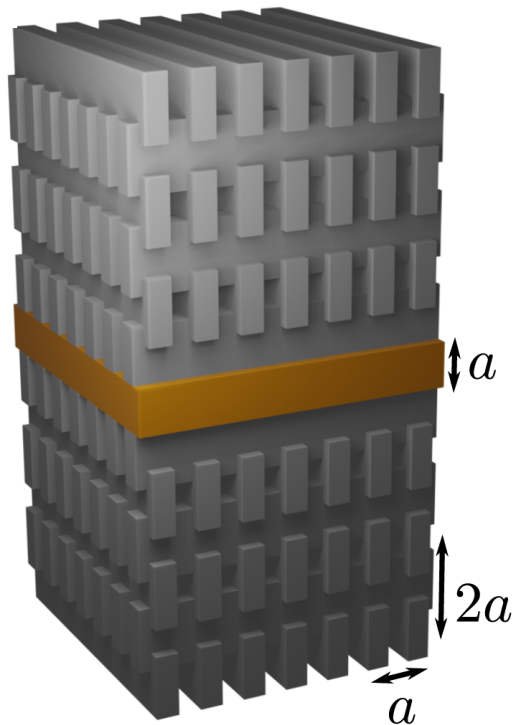
Overcoming this limitation

Need to either break:

isotropy – using birefringent materials in the environment

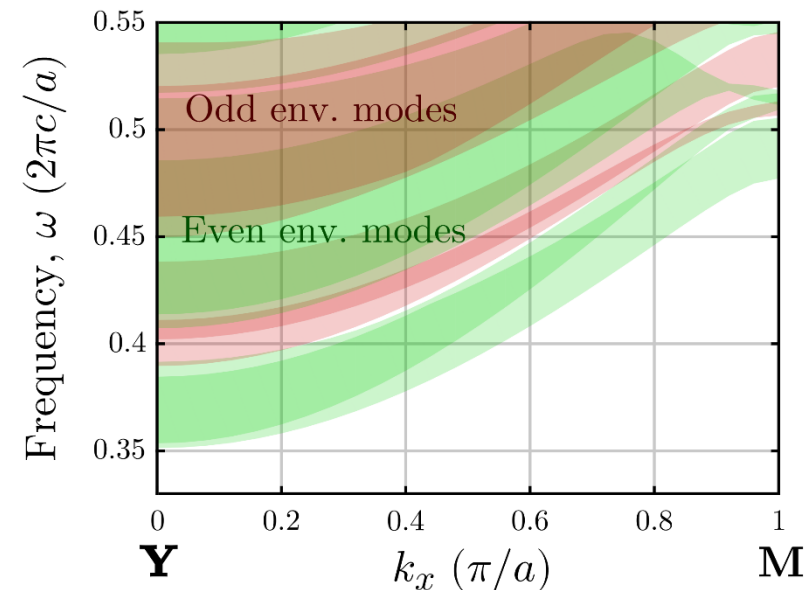
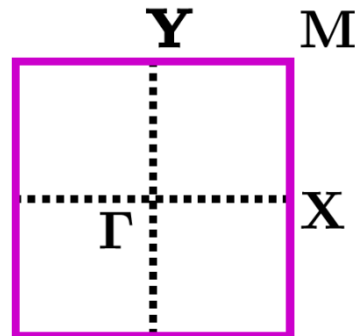
homogeneity – by patterning the environment

Embed slab in a 3D photonic crystal ➤ Changes the radiative channels to be the photonic crystal's projected-in- k_z bands, $\omega_n(\mathbf{k}_{\parallel})$



Remember – Looking for a slab symmetry not in the environment

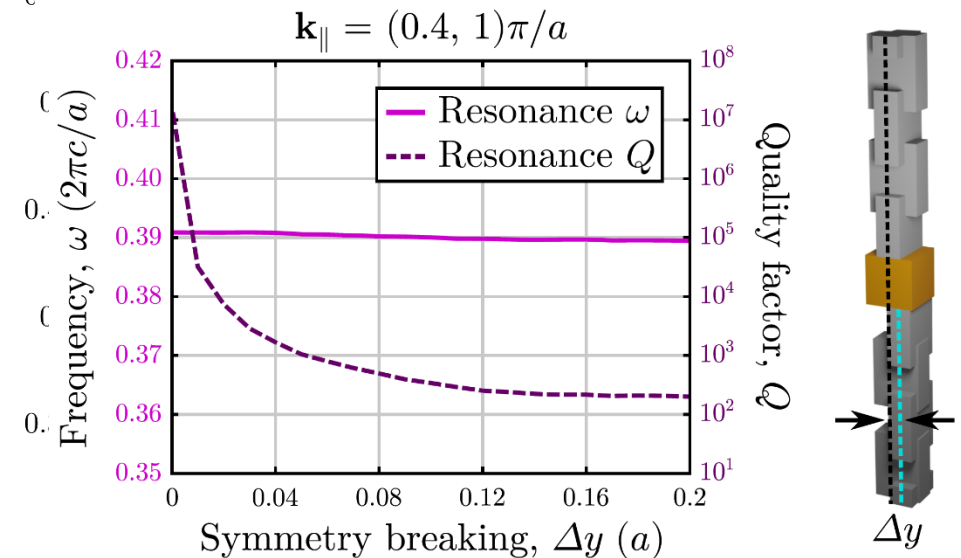
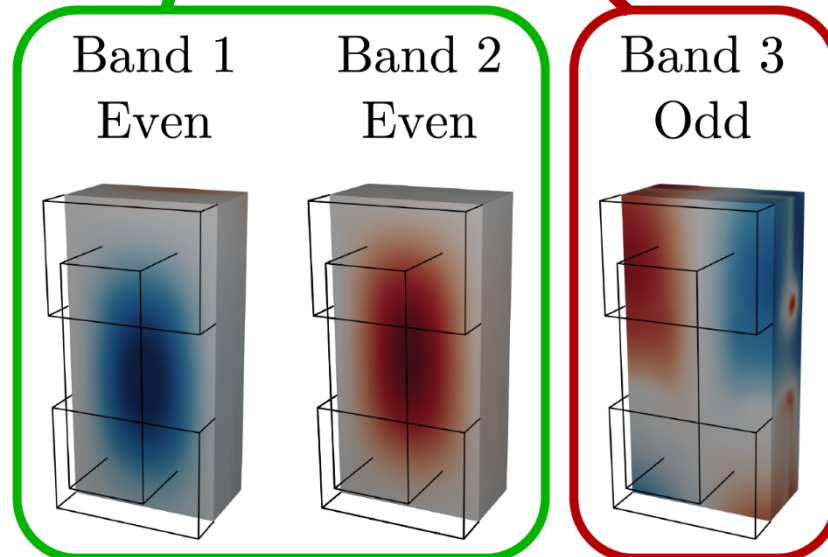
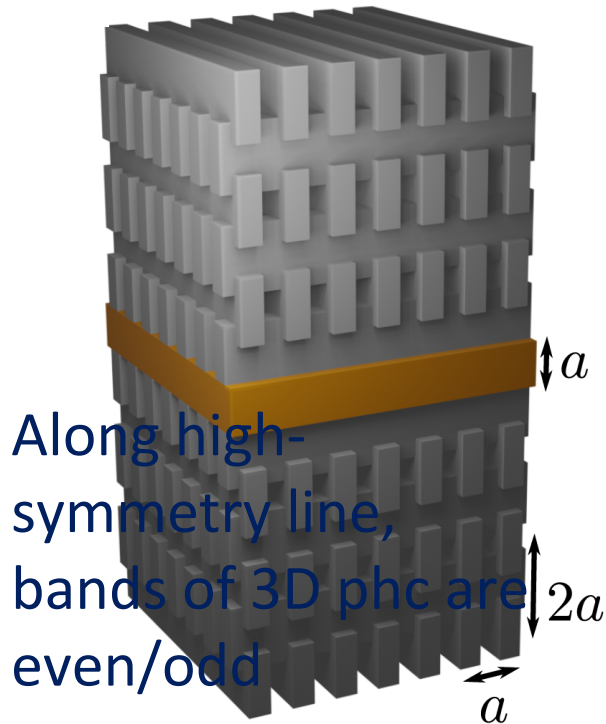
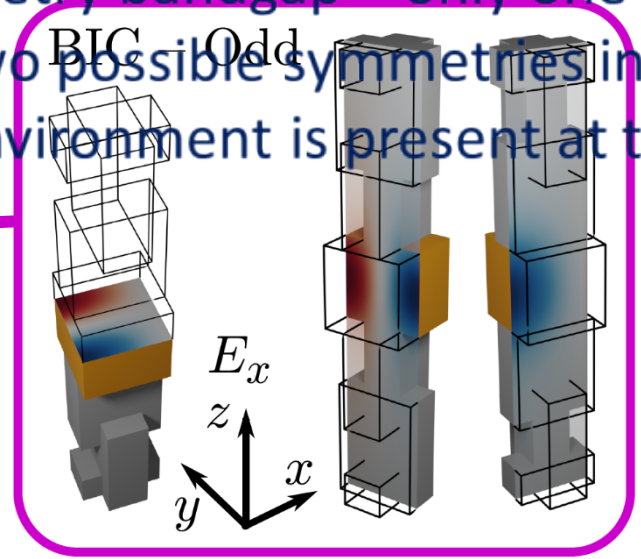
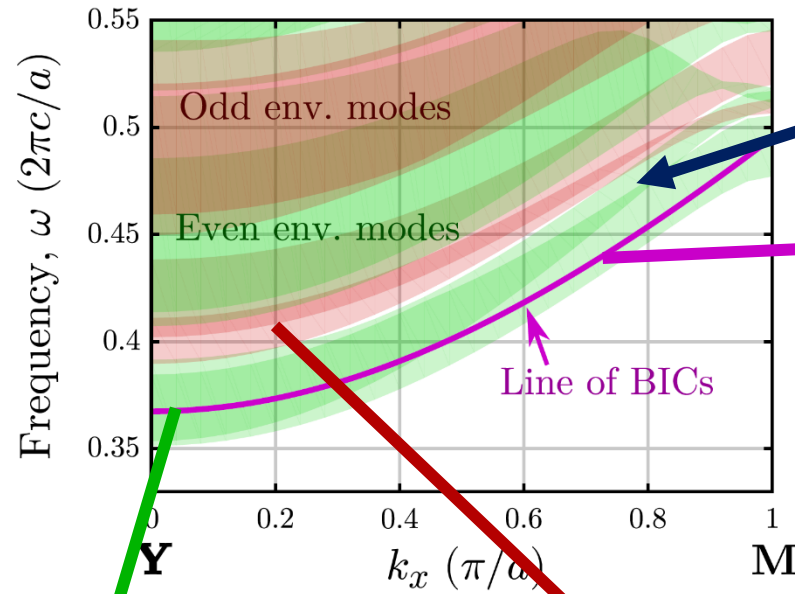
So, look along
high-symmetry
lines:



Overcoming this limitation

Can find a line of BICs against the continuum with the wrong symmetry

Symmetry bandgap – only one of the two possible symmetries in the environment is present at this

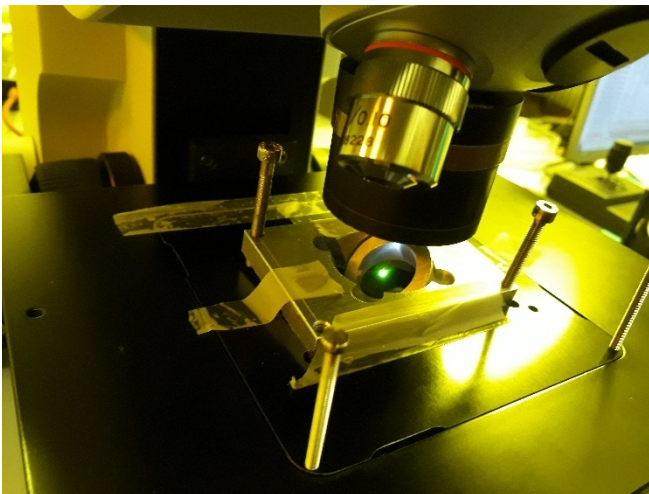
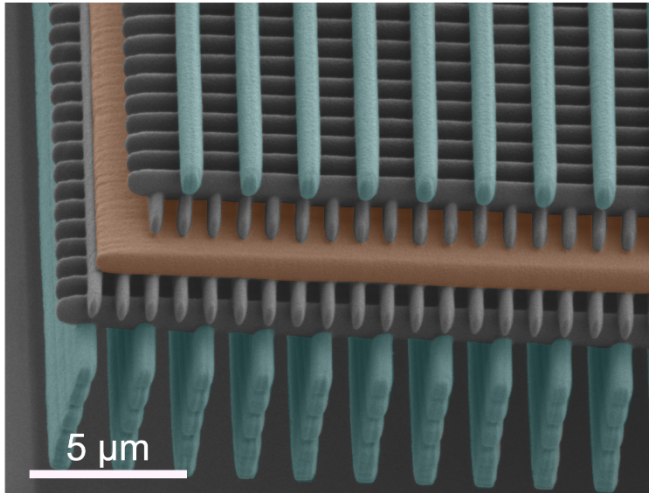


Observing a line of BICs

Effect can still be observed with just a single complete

Fabricate using
a Nanoscribe

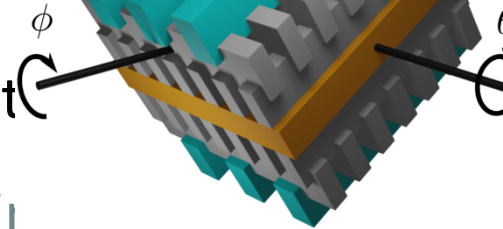
Observe with
an FTIR



Grating

Woodpile
environment

Slab



In simulation

$\theta = 15^\circ$

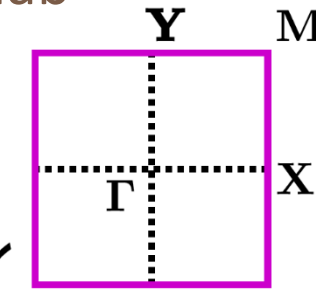
Comment

$$\theta = k_x \quad \phi = k_y$$

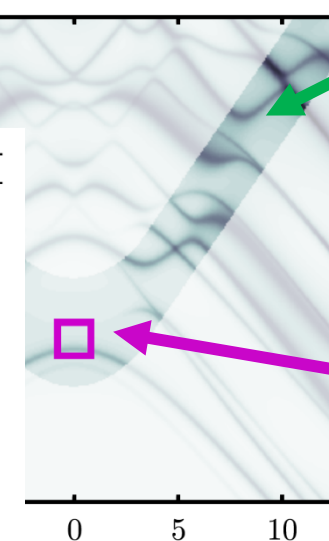
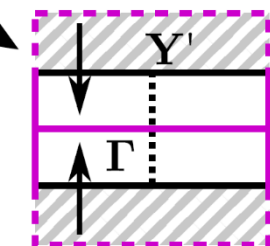
$\Gamma - X$ line at $\phi = 0$

Slab resonance
away from BIC

Period doubling grating in y



Line of BICs

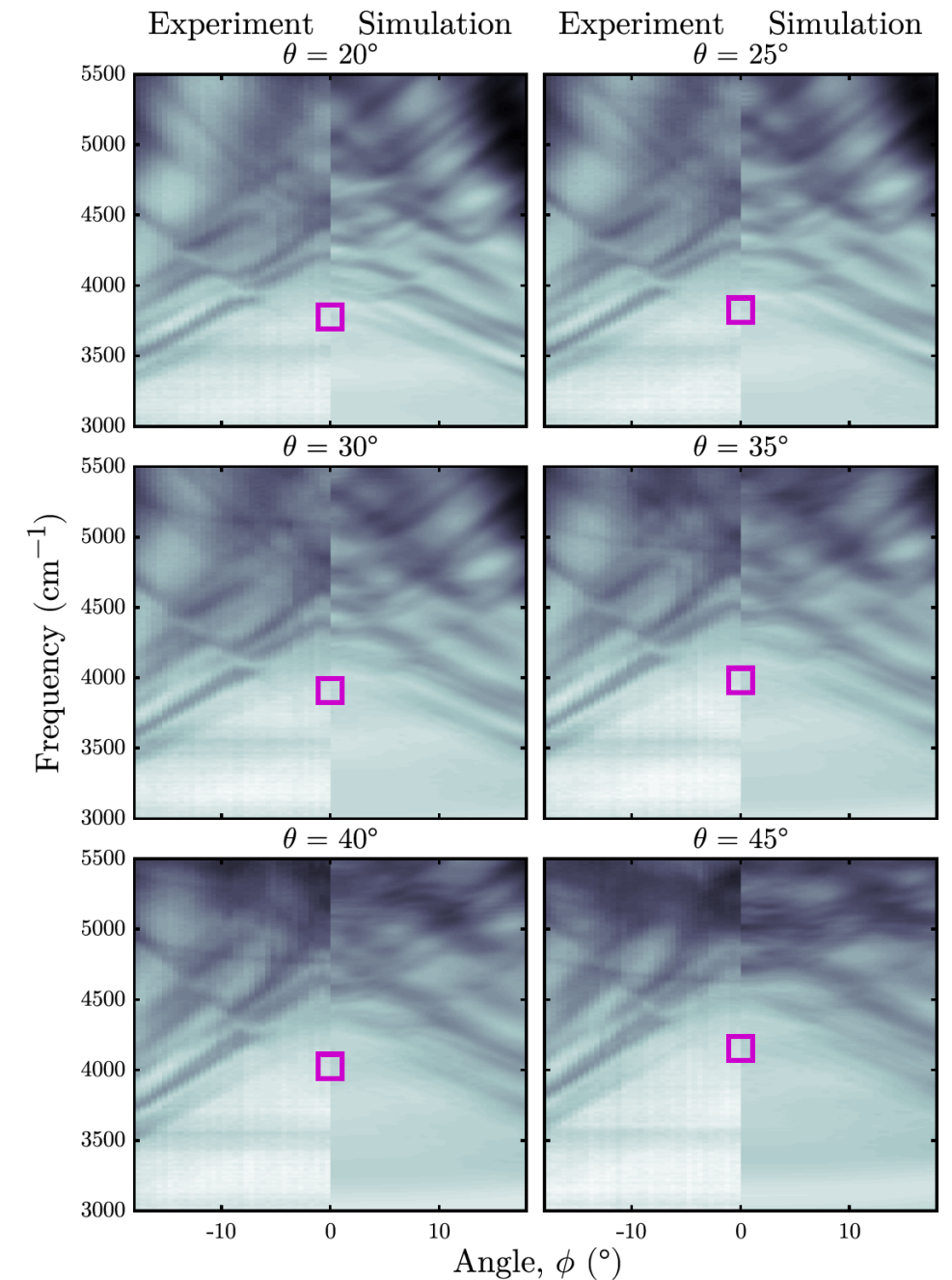
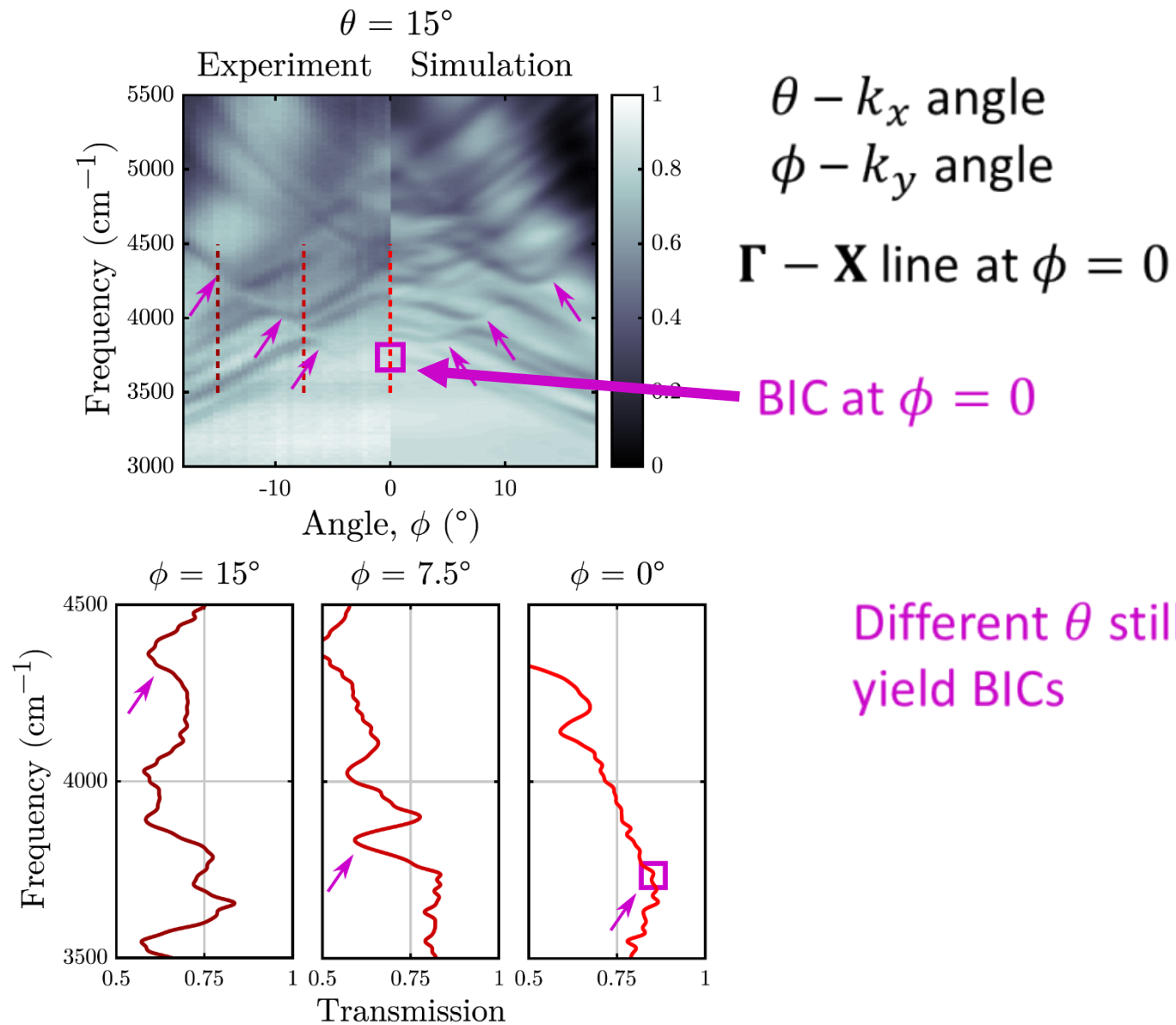


$Q \rightarrow \infty$ as $\phi \rightarrow 0$
Disappearance
implies BIC

angle, ϕ ($^\circ$)

voided crossings

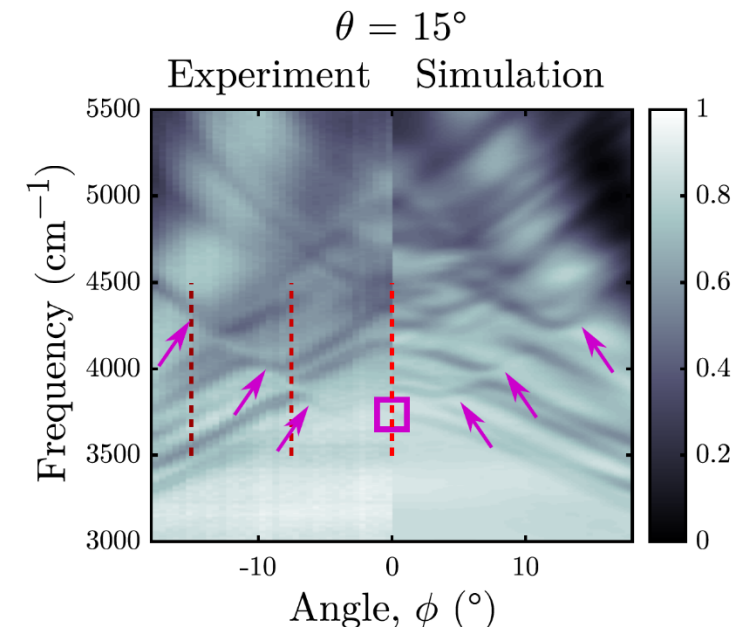
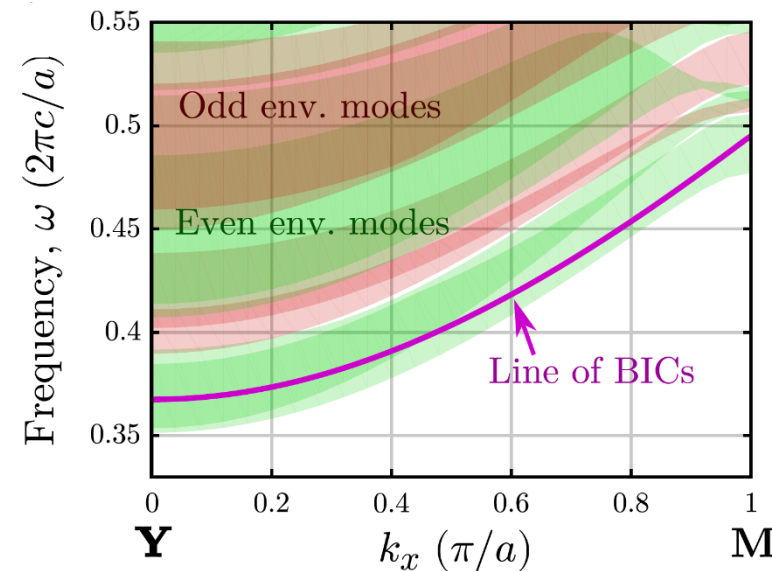
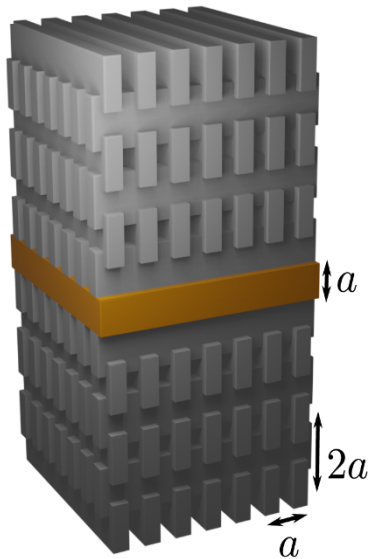
Observing a line of BICs



Summary

AC,* Jörg,* et al., arXiv:2104.09603

- Analytical argument of the limitations of symmetry-protected BICs in photonic crystal slabs and metasurfaces surrounded by air
 - Full proof can be completed using representation theory
- Can achieve multi-frequency, multi-wavevector BICs in a monolithic device using a single layer of a 3D photonic crystal surrounding the slab



Acknowledgements



Christina Jörg
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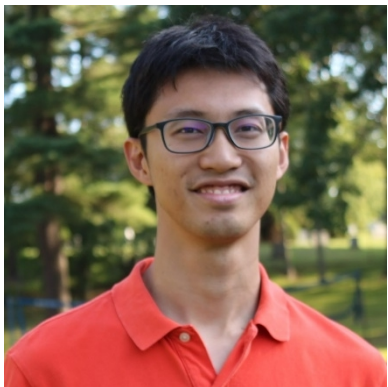
Sachin Vaidya
Penn State



Shyam Augustine
TU Kaiserslautern



Wladimir Benalcazar
Penn State



Chia Wei Hsu
USC



Georg von Freymann
TU Kaiserslautern



Mikael Rechtsman
Penn State



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