

# Quantum Transport Simulations for Si: P $\delta$ -layer Tunnel Junctions

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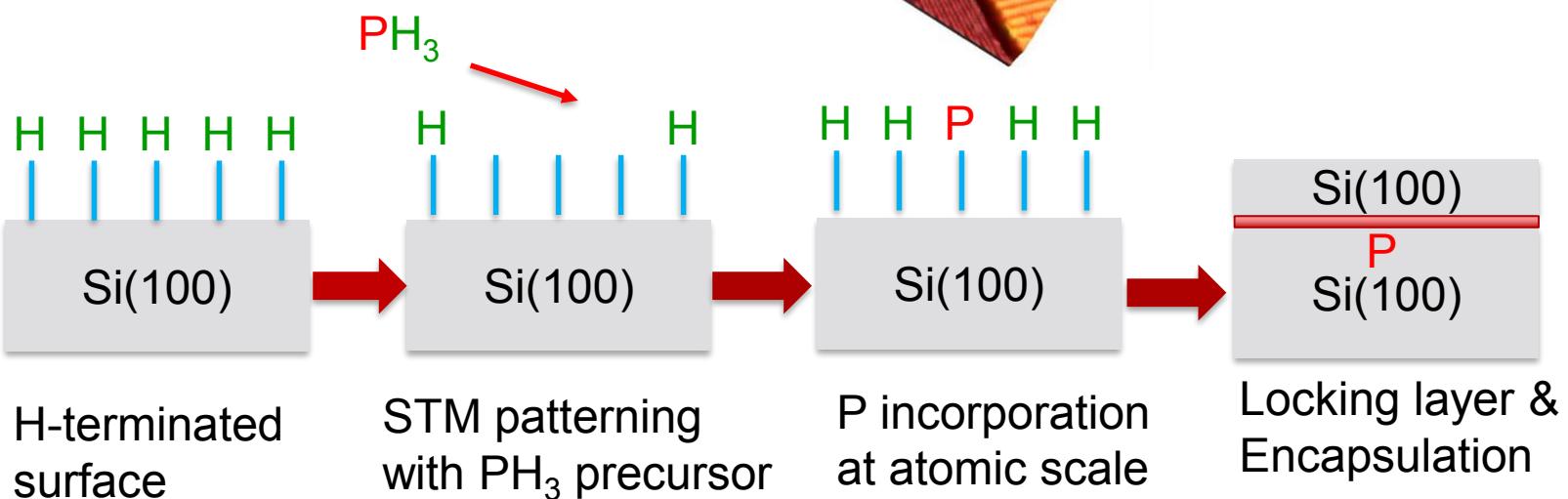
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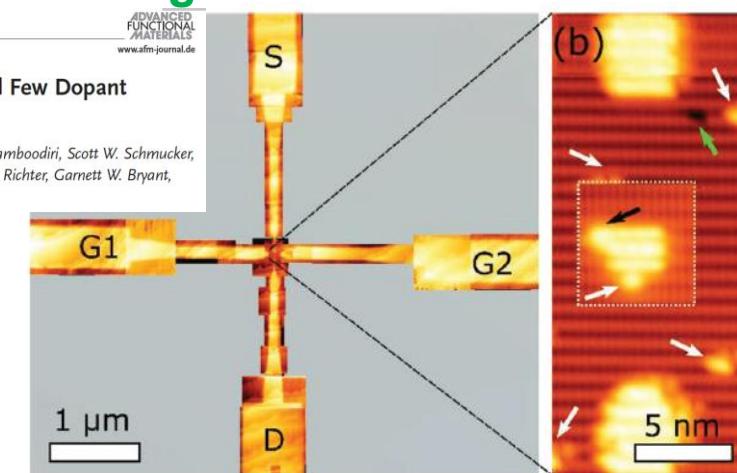
# Motivation

## Atomic Precision Advanced Manufacturing (APAM)

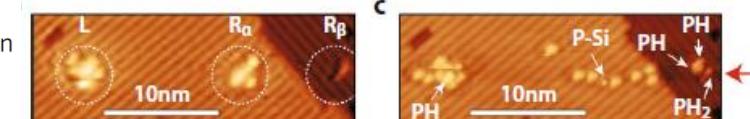
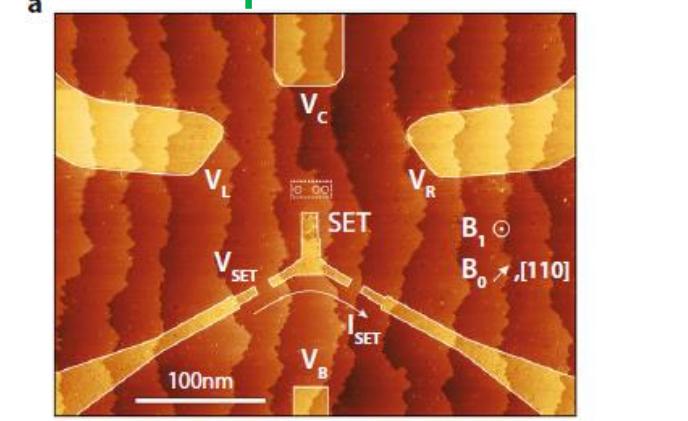
is a process of area-selective dopant incorporation at the atomic scale



## Single atom transistor

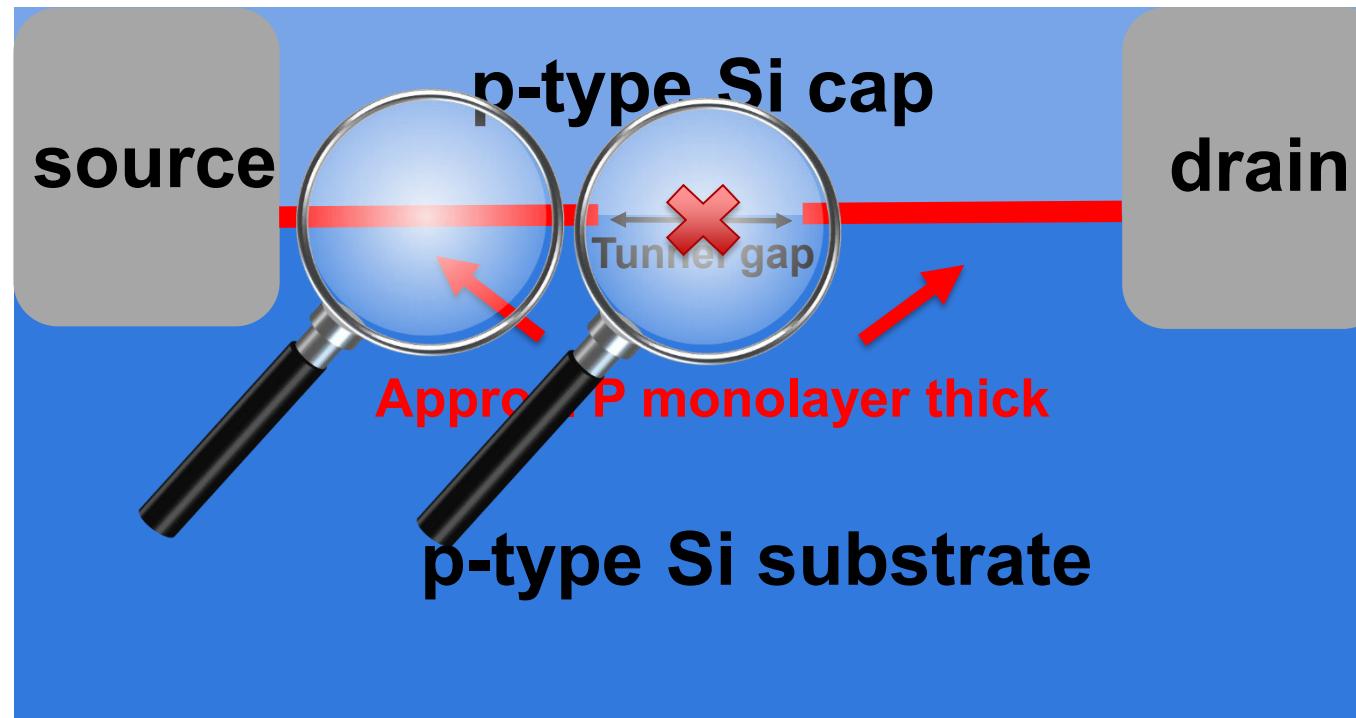


## Two-qubits device



# Si: P delta-layer Tunnel Junction

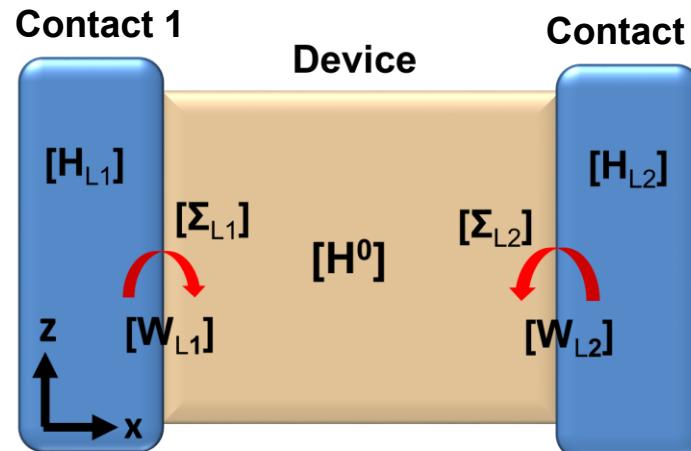
- High potential for **quantum computing** and **advanced microelectronic devices**



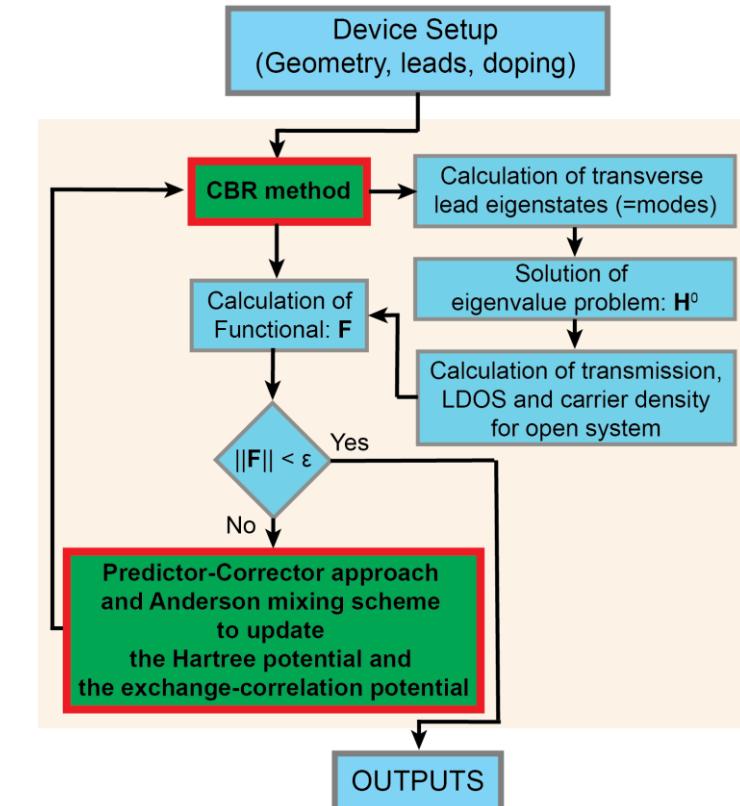
# Open-system Quantum Transport Framework

Our quantum transport simulator is based on **Non-Equilibrium Green's function (NEGF)** formalism with

- **Fully charge self-consistent solution of Poisson-open system Schrödinger equation**
- **Single-band ( $\Gamma$  valley) effective mass approximation**
- **Predictor-corrector approach and Anderson mixing scheme**
- Contact Block Reduction (CBR) method for fast numerical efficiency



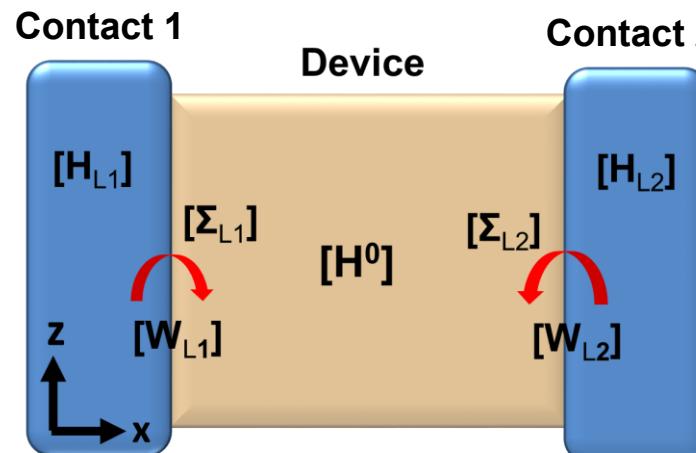
## Quantum transport simulator



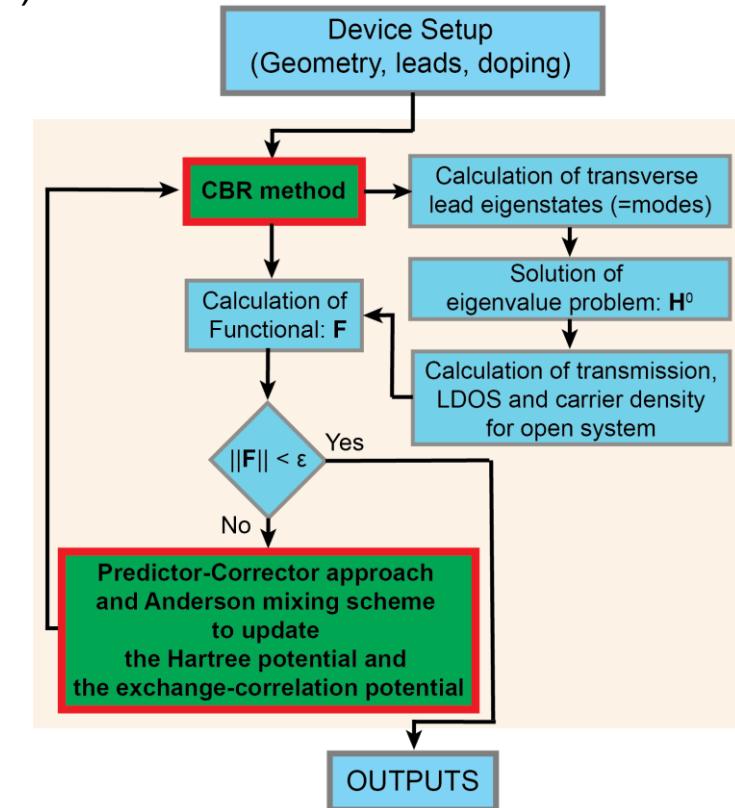
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## Quantum transport simulator



- D. Mamaluy *et al.*, J. Appl. Phys., vol. 93, no. 8, p. 4628-4633, 2003.
- D. Mamaluy *et al.* Phys. Rev. B, vol. 71, p. 245321, 2005.

# Non-Equilibrium Green Function

- Current from leads  $\lambda$  to  $\lambda'$

$$J_{\lambda\lambda'} = \frac{2e}{h} \int T_{\lambda\lambda'}(E) (f_\lambda(E) - f_{\lambda'}(E)) dE$$

$$T_{\lambda\lambda'}(E) = \text{Tr} [\Gamma_\lambda G_D \Gamma_{\lambda'} G_D^\dagger]$$

Self-energy matrix of lead

$$\Gamma_\lambda = i(\Sigma_\lambda - \Sigma_\lambda^\dagger)$$

Open-device Hamiltonian matrix

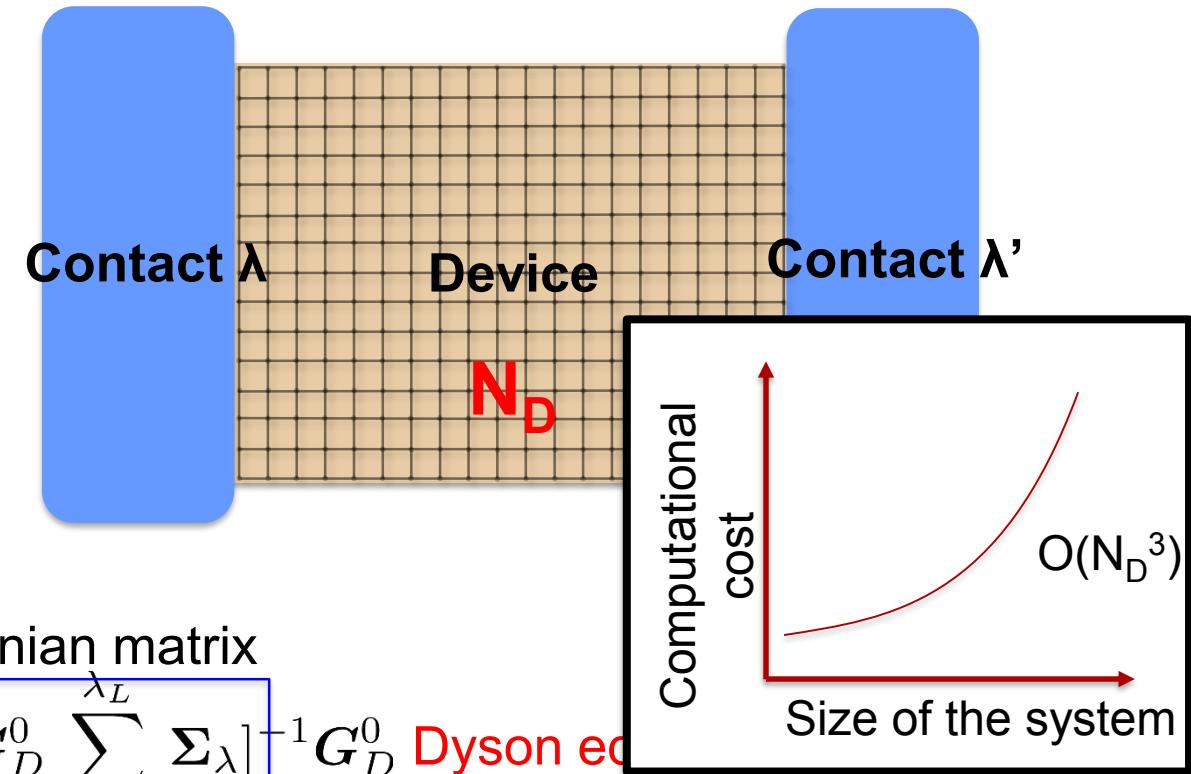
$$G_D = [I - G_D^0 \sum_{\lambda=\lambda_1}^{\lambda_L} \Sigma_\lambda]^{-1} G_D^0$$

Dyson eq

- Electron density

$$\rho(\mathbf{r}_i) = \sum_{\lambda} \int_{-\infty}^{\infty} \rho_{\lambda}(\mathbf{r}_i, E) f_{\lambda}(E) dE$$

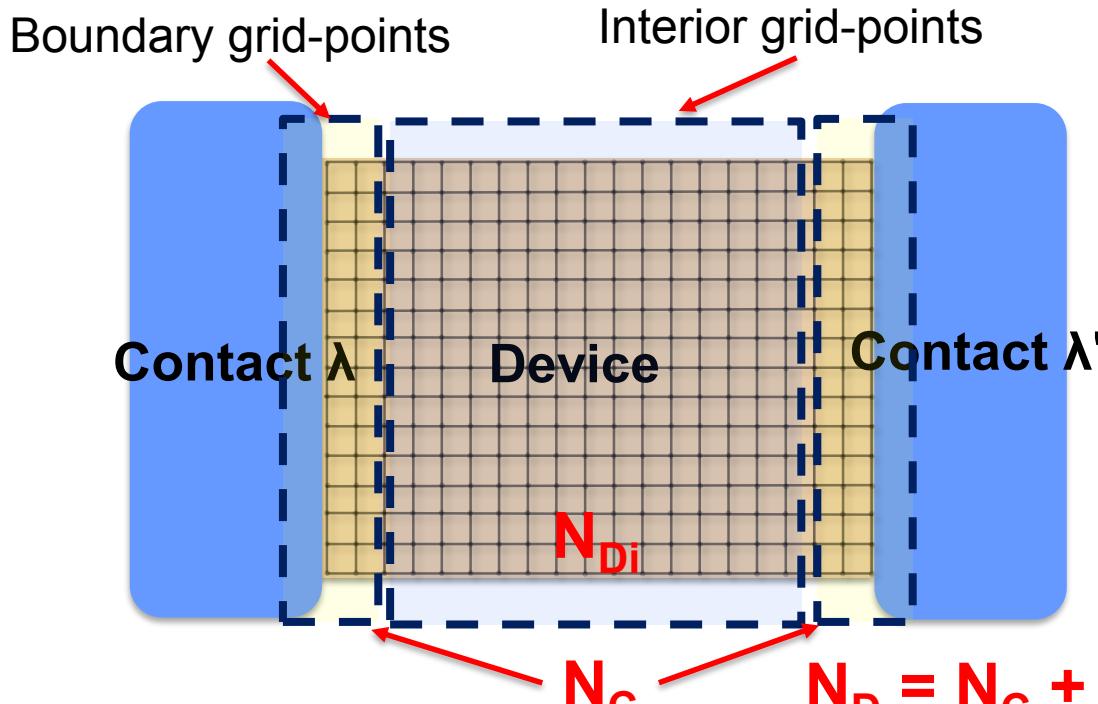
$$\rho_{\lambda}(\mathbf{r}_i, E) = \frac{1}{2\pi} G_D \Gamma_{\lambda} G_D^\dagger$$



$$G_D^0 = [E^+ - H_D^0]^{-1} = \sum_{\alpha} \frac{|\phi_{\alpha}\rangle\langle\phi_{\alpha}|}{E^+ - E_{\alpha}}$$

$(N_D \times N_D)$

# Contact Block Reduction Method



$$H_D = \begin{pmatrix} (N_C \times N_C) & (N_C \times N_{D_i}) \\ (H_C & H_{CD_i} \\ H_{D_i C} & H_{D_i}) & (N_{D_i} \times N_{D_i}) \end{pmatrix}$$

$$G_D = \begin{pmatrix} G_C & G_{CD_i} \\ G_{D_i C} & G_{D_i} \end{pmatrix}$$

$$\Sigma = \sum_{\lambda=\lambda_1}^{\lambda_L} \Sigma_\lambda = \begin{pmatrix} \Sigma_C & 0 \\ 0 & 0 \end{pmatrix}$$

- **Electrical current:**

$$J_{\lambda\lambda'} = \frac{2e}{h} \int T_{\lambda\lambda'}(E) (f_\lambda(E) - f_{\lambda'}(E)) dE, \quad T_{\lambda\lambda'}(E) = \text{Tr}(\Gamma_{C_\lambda} G_C \Gamma_{C_{\lambda'}} G_C^\dagger), \quad G_C = [I - G_C^0 \Sigma_C]^{-1} G_C^0$$

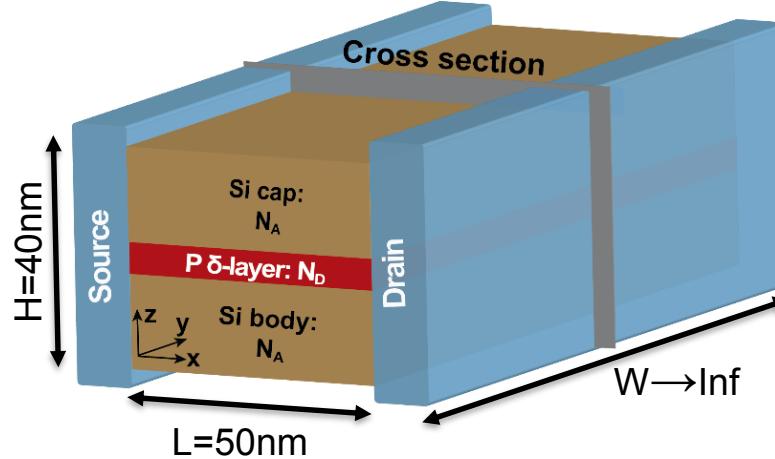
- **Electron density:**

$$\rho(\mathbf{r}_i) = \int_{-\infty}^{\infty} \Xi(E) f_\lambda(E) dE, \quad \Xi(E) = \frac{1}{2\pi} \frac{\text{Tr}[B_C^{-1} \Gamma_C B_C^{-1\dagger}]}{(E^+ - E_\alpha)(E^- - E_\alpha)}, \quad B_C = \mathbf{1}_C - \Sigma_C G_C^0$$

↗  $(N_C \times N_C)$

# Last year in SISPAD 2020 ...

## Infinite-width $\delta$ -layer systems:



$$N_D = 1.2 \times 10^{14} \text{ cm}^{-2}, N_A = 10^{17} \text{ cm}^{-3}$$

## communications physics

### ARTICLE

<https://doi.org/10.1038/s42005-021-00705-1>

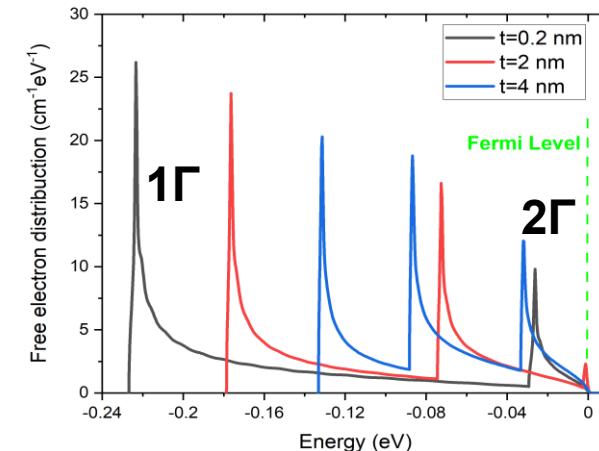
OPEN

Revealing quantum effects in highly conductive  $\delta$ -layer systems

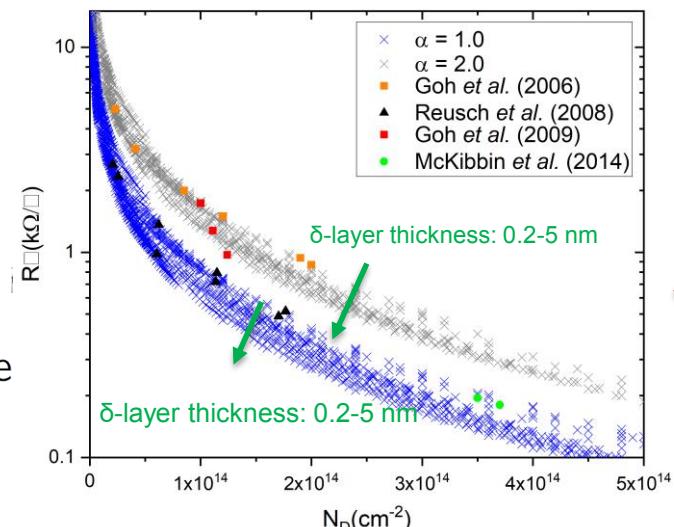
Denis Mamaluy<sup>1</sup> , Juan P. Mendez<sup>1</sup> , Xujiao Gao<sup>1</sup> & Shashank Misra<sup>1</sup>

<https://www.nature.com/articles/s42005-021-00705-1>

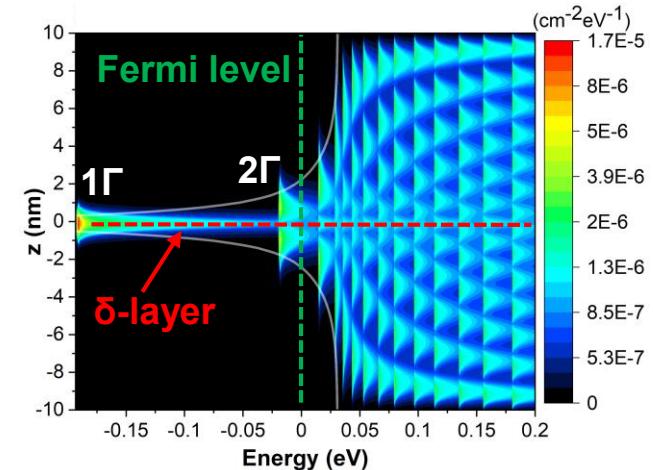
- Prediction of shallow Sub-bands



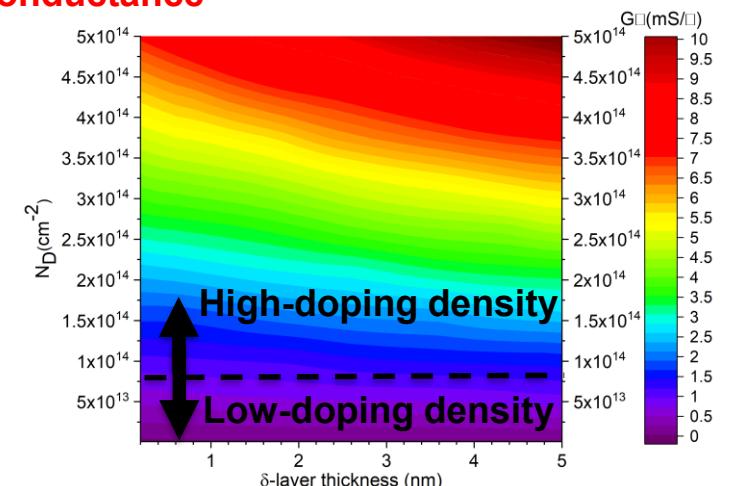
- Good agreement with experiments at 4K!!



- The so-called “quantum menorah”: LDOS(E,z)



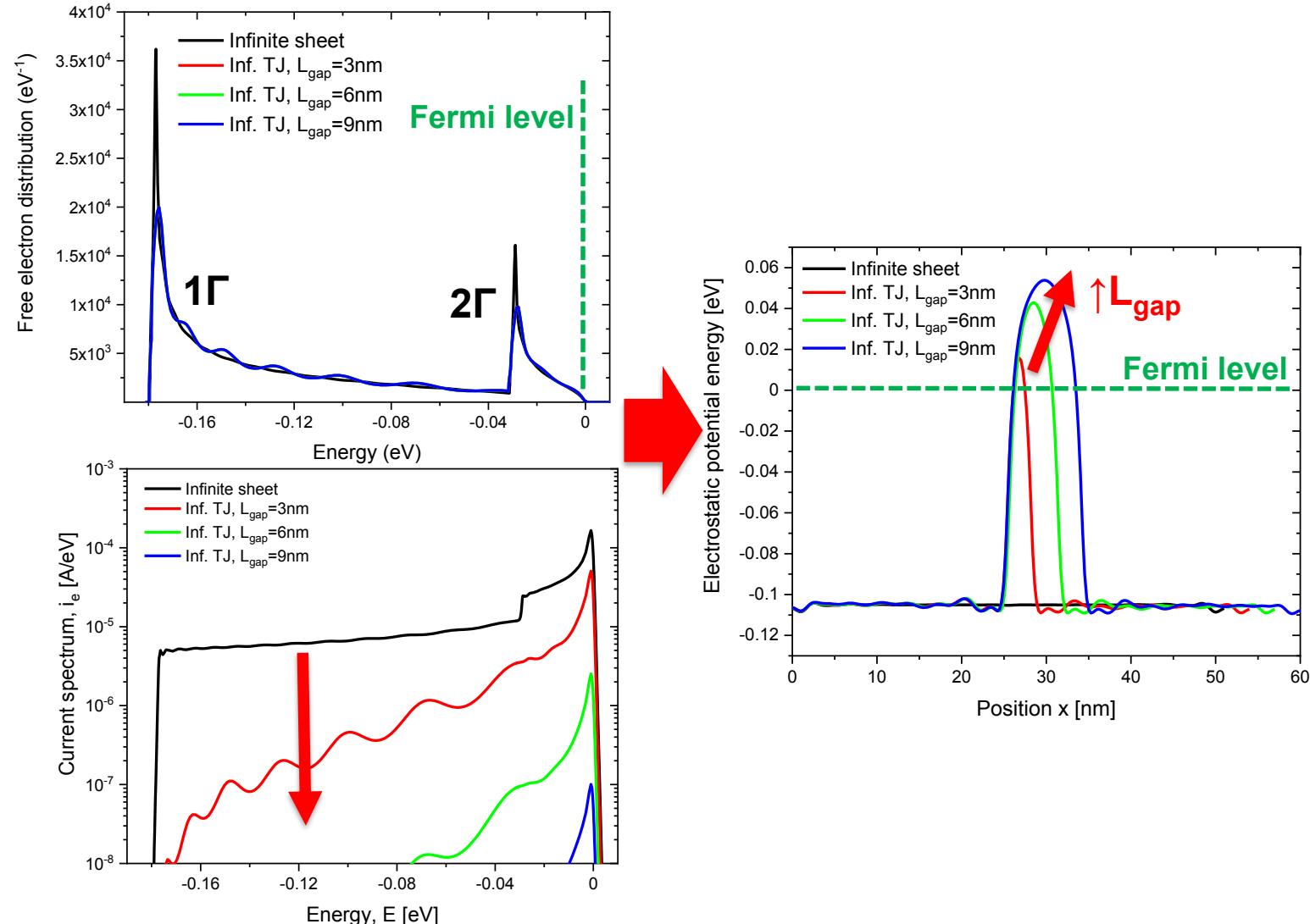
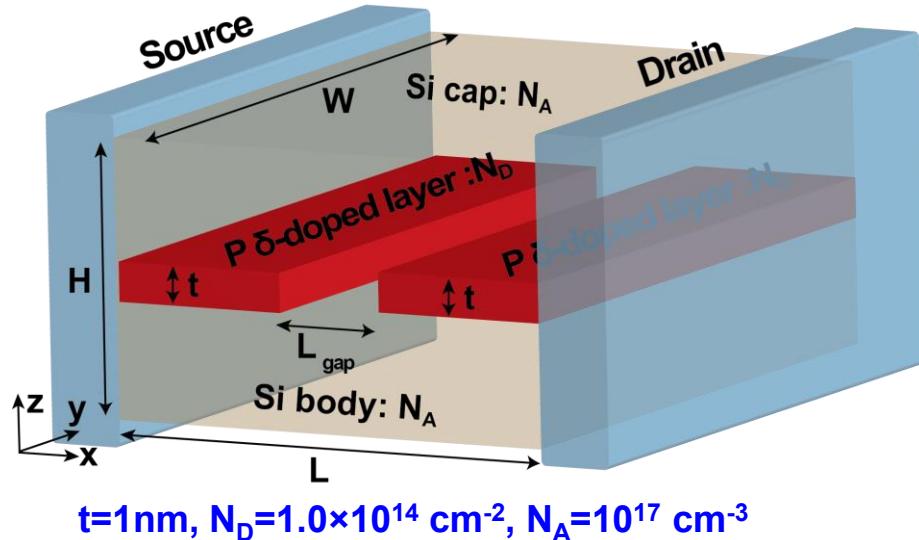
- Quantum thickness dependence on the sheet conductance



# Conductive Properties for Ideal Tunnel Junctions

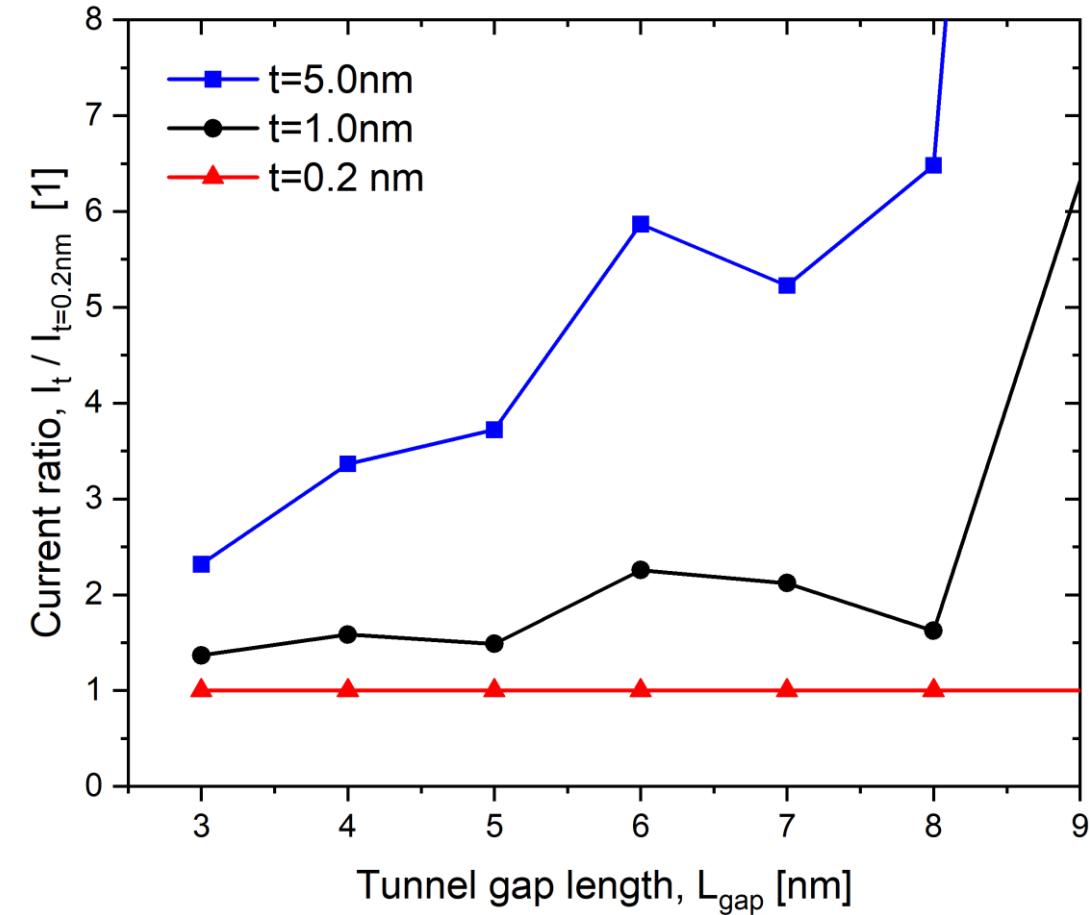
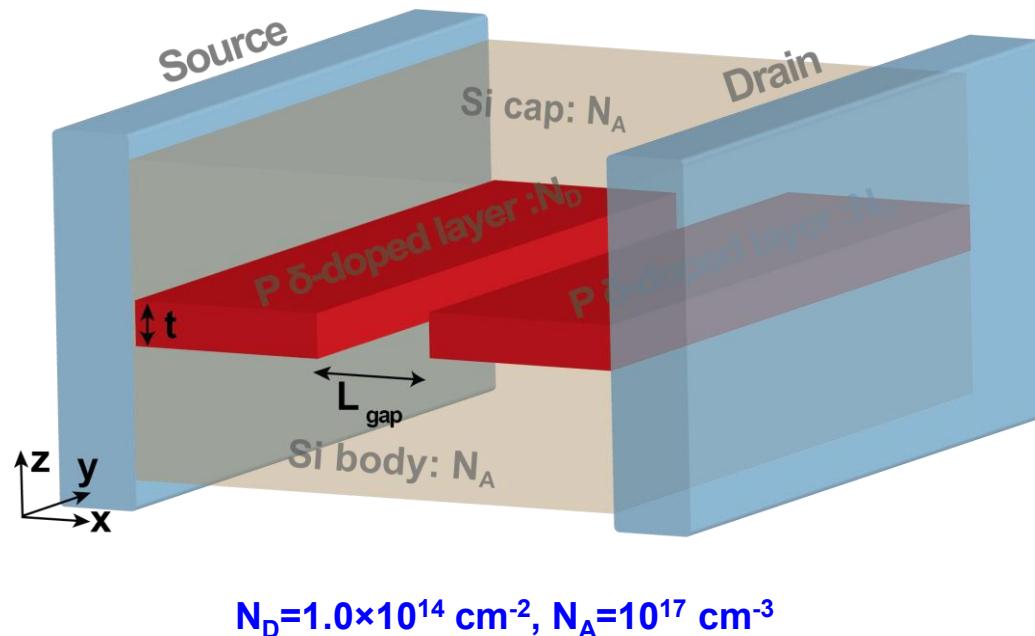
- Low-energy electrons contribution on the current is depressed with the tunnel gap

## Infinite-width $\delta$ -layer Tunnel Junctions



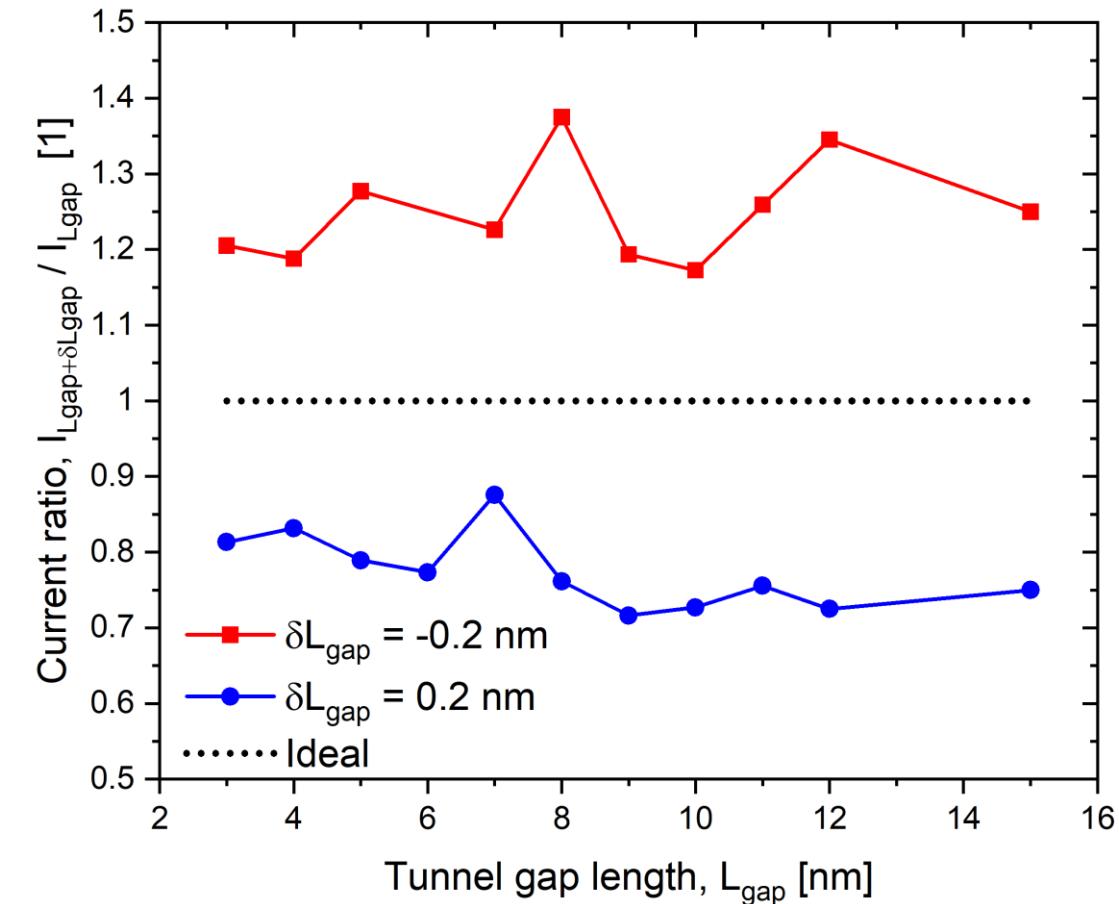
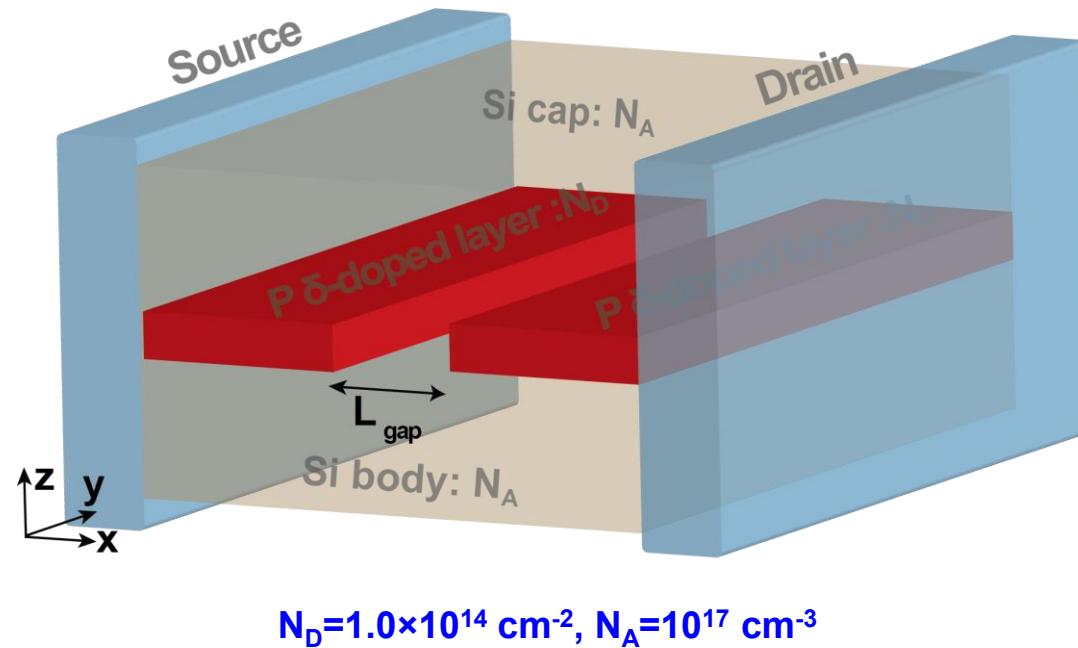
# Variation of the $\delta$ -layer thickness

- The tunneling rate considerably increases with the  $\delta$ -layer thickness, specially for larger tunnel gaps



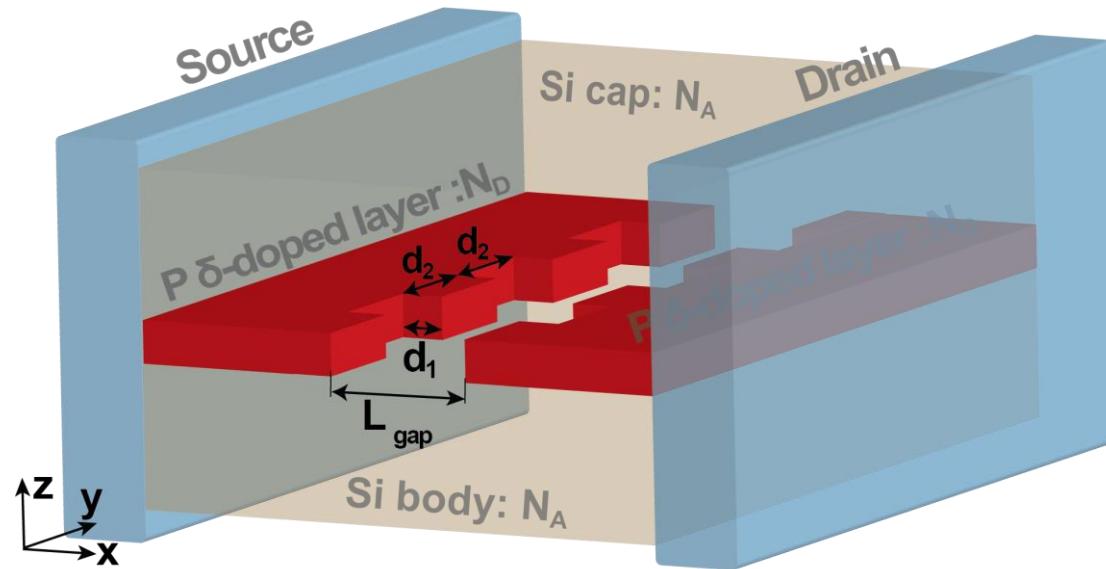
# Variation of the tunnel gap length

- Small variations of the gap length (around 0.2 nm) leads to a tunneling rate change of around 20%-30%

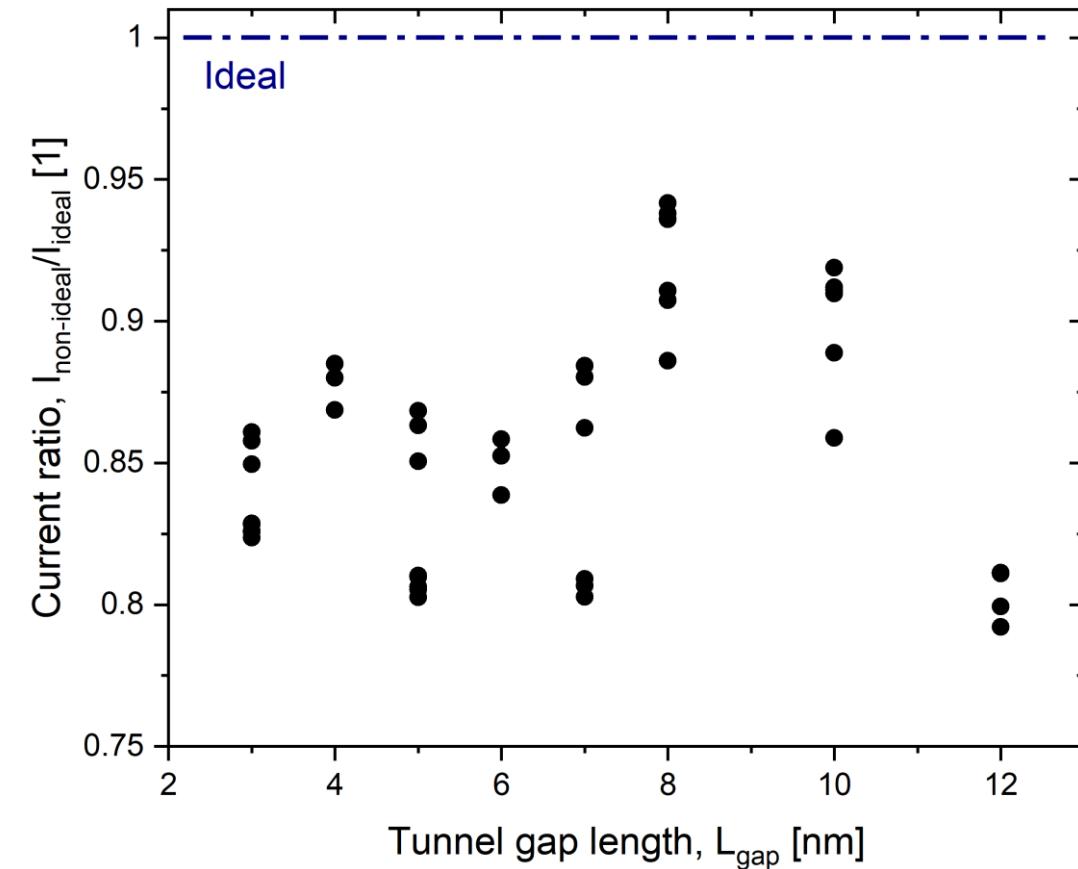


# Effects of Edge roughness

- Edge roughness might lead to a decreases of the tunneling rate up to 5%-25%

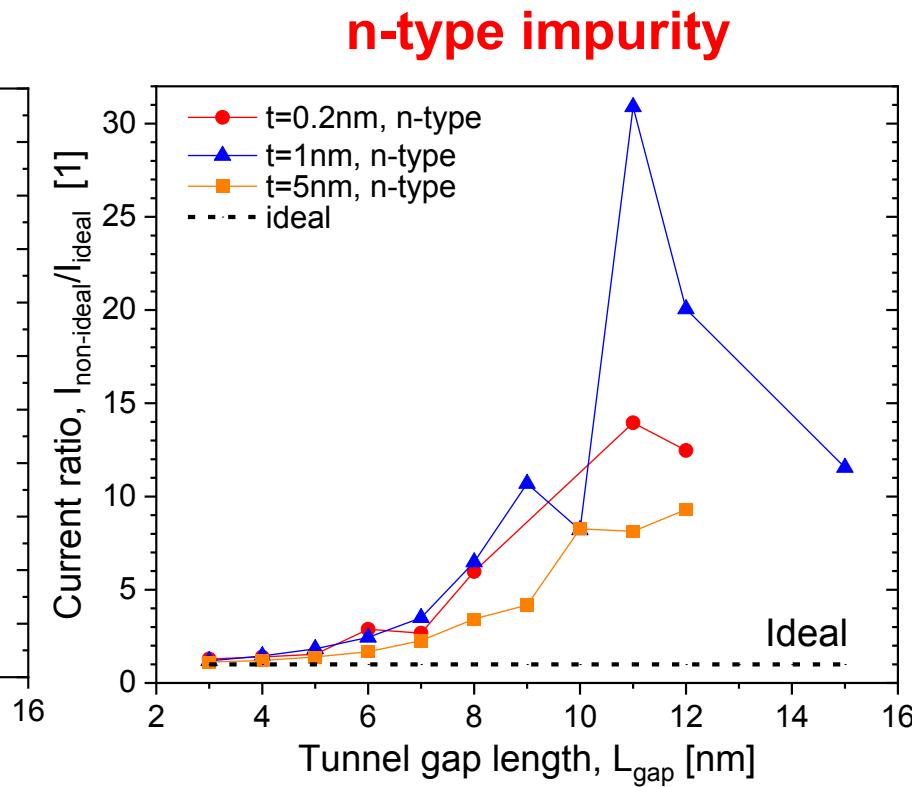
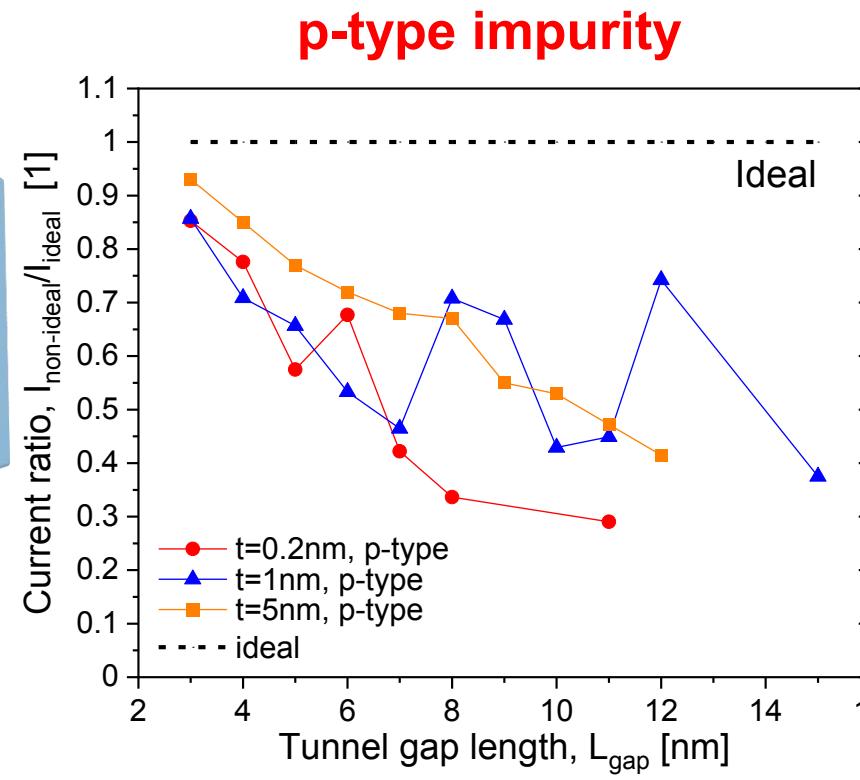
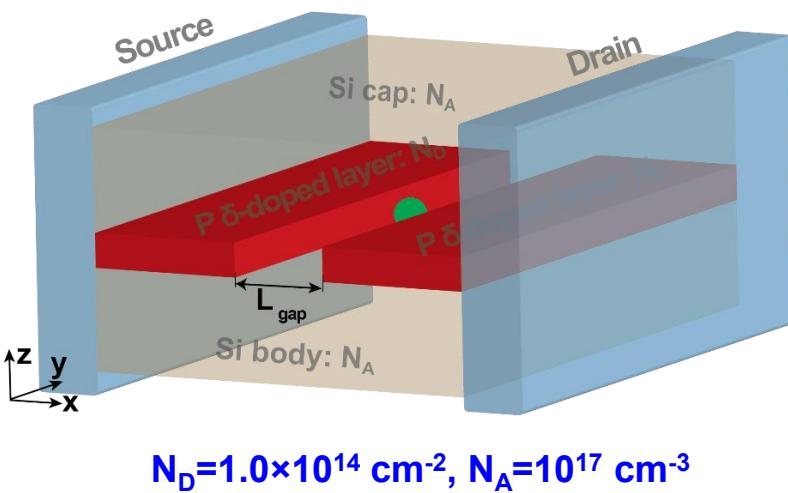


$N_D = 1.0 \times 10^{14} \text{ cm}^{-2}$ ,  $N_A = 10^{17} \text{ cm}^{-3}$   
 $d_1 = 0.8\text{-}2.0 \text{ nm}$  and  $d_2 = 0.6\text{-}3.4 \text{ nm}$



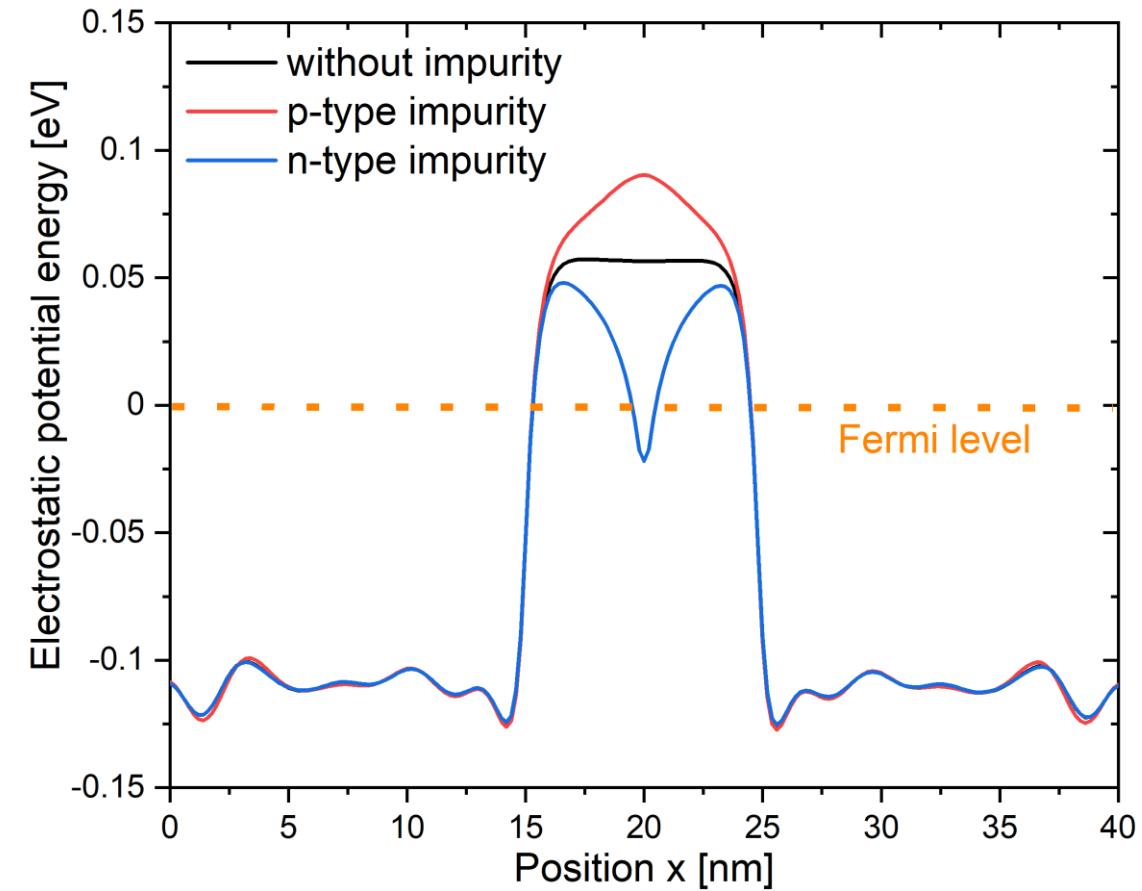
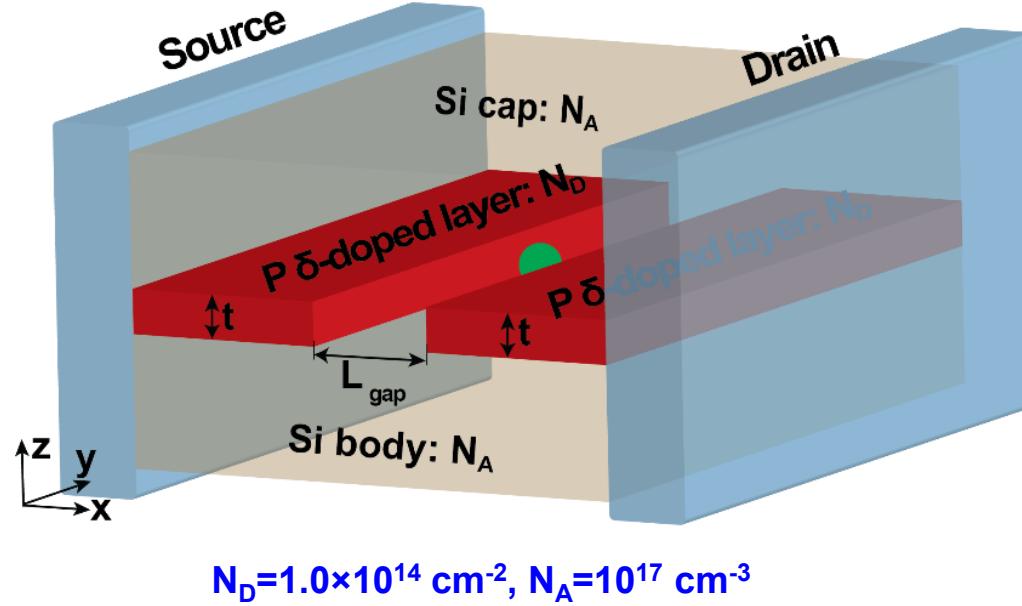
# Effects of a Single Impurity in the Tunnel Gap

- While p-type impurities might moderately reduce the tunneling rate, n-type impurities might dramatically increase the tunneling rate, specially for tunnel gaps of the order of 10 nm



# Effects of a Single Impurity in the Tunnel Gap

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# Summary

- ❑ Presented an **efficient quantum open-system transport framework** for  $\delta$ -layer tunnel junctions
- ❑ While most of the non-idealities moderately affect the tunneling rate, a **single charged impurity** in the tunnel gap can alter the tunneling rate by more than an **order of magnitude**, even for relatively large tunnel gaps
- ❑ The electric **sign of impurity** plays an important role in the tunneling rate: the change of current due to an n-type impurity is an order of magnitude stronger than for p-type impurity
- ❑ Overall these simulations suggest that **geometric fidelity of the device fabrication is less important than mitigation of defects inside of the junction**

A large, colorful word cloud centered around the word "thank you" in various languages. The word "thank" is in red, "you" is in green, and "thank you" together is in red. Surrounding these are numerous other words in different languages, each with its meaning in English. The languages include German (danke), Chinese (謝謝), Spanish (gracias), English (thank you), French (merci), Italian (grazie), Portuguese (obrigado), Polish (dziękuje), Russian (спасибо), Korean (감사합니다), Japanese (ありがとうございます), and many others like Dutch, Swedish, and many Asian languages.

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