

# Signatures of Coherent Phonon Transport in Ultralow Thermal Conductivity Two-Dimensional Ruddlesden–Popper Phase Perovskites

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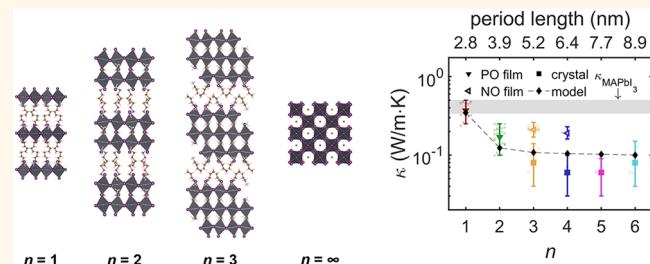
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**ABSTRACT:** An emerging class of methylammonium lead iodide ( $\text{MAPbI}_3$ )-based Ruddlesden–Popper (RP) phase perovskites,  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  ( $n = 1–7$ ), exhibit enhanced stability to environmental conditions relative to  $\text{MAPbI}_3$ , yet still degrade at elevated temperatures. We experimentally determine the thermal conductivities of these layered RP phases for  $n = 1–6$ , where  $n$  defines the number of repeated perovskite octahedra per layer. We measure thermal conductivities of  $0.37 \pm 0.13/0.12$ ,  $0.17 \pm 0.08/0.07$ ,  $0.21 \pm 0.05/0.04$ , and  $0.19 \pm 0.04/0.03$   $\text{W/m}\cdot\text{K}$  in thin films of  $n = 1–4$  and  $0.08 \pm 0.06/0.04$ ,  $0.06 \pm 0.04/0.03$ ,  $0.06 \pm 0.03/0.03$ , and  $0.08 \pm 0.07/0.04$   $\text{W/m}\cdot\text{K}$  in single crystals of  $n = 3–6$ . With the exception of  $n = 1$ , these thermal conductivities are lower than the range of  $0.34–0.50$   $\text{W/m}\cdot\text{K}$  reported for single-crystal  $\text{MAPbI}_3$ . Reduced-order lattice dynamics modeling suggests that the initially decreasing trend of thermal conductivity in similarly oriented perovskites with increasing  $n$  may result from the transport properties of coherent phonons, emergent from the superstructure, that do not scatter at the interfaces of organic butylammonium chains and perovskite octahedra. Reduced group velocity of coherent phonons in  $n = 3–6$ , a consequence of band flattening in the phonon dispersion, is primarily responsible for their ultralow thermal conductivities. Similar effects on thermal conductivity have been experimentally demonstrated in deposited superlattices, but never in naturally defined materials such as RP phases. GIWAXS measurements reveal that higher  $n$  RP phase thin films are less orientationally controlled and therefore possess apparently elevated thermal conductivities relative to single crystals of the same  $n$ .

**KEYWORDS:** thermal transport, methylammonium lead iodide, 2D perovskites, layered materials, photovoltaics, optoelectronics

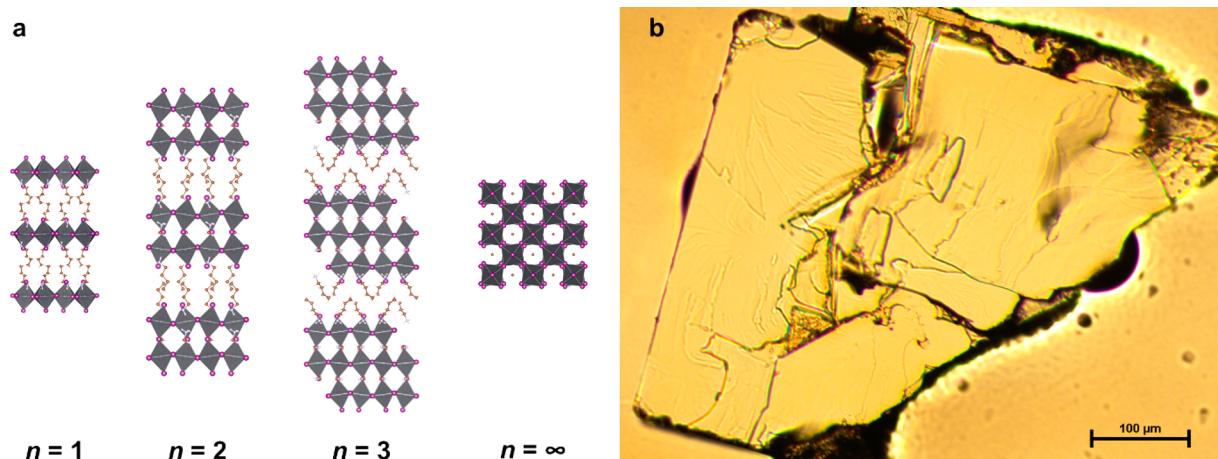


Methylammonium lead iodide ( $\text{MAPbI}_3$ ), a hybrid organic–inorganic perovskite (HOIP) belonging to the lead halide perovskite family, is a semiconducting material that has been widely considered for next-generation photovoltaic (PV) and optoelectronic (OE) applications.<sup>1–7</sup> Researchers have exploited its facile processability,<sup>7</sup> notable defect tolerance,<sup>4,6,8</sup> long carrier lifetime,<sup>4,6,9,10</sup> high absorption coefficient,<sup>1</sup> and suitable optical bandgap<sup>2</sup> to develop  $\text{MAPbI}_3$ -based solar cells that have improved in power conversion efficiency (PCE) from less than 3% to 24% in just over a decade.<sup>1,3,11</sup> The impressive external luminescence efficiency and color quality of this HOIP have also made it a material of interest in light-emitting and lasing applications.<sup>1,3,4</sup>

Despite such promising characteristics,  $\text{MAPbI}_3$  is inherently unstable and tends to rapidly degrade into solid  $\text{PbI}_2$  and vaporous  $\text{MA}^+$  and  $\text{I}^-$ .<sup>12,13</sup> This process occurs even in dark vacuum environments and is accelerated by oxygen,<sup>14</sup> moisture,<sup>14–16</sup> light,<sup>15,17,18</sup> and, of central importance to this study, elevated temperature.<sup>15–18</sup> Careful synthesis,<sup>19</sup> encapsu-

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**Figure 1.** (a) Crystal structure of  $n = 1$ –3 homologous members, where  $n$  represents the number of perovskite octahedra per organic layer and dictates the thickness of the inorganic layers. As  $n$  approaches infinity, the formula describes 3D  $\text{MAPbI}_3$ . (b) Optical microscope image of a Au-coated single crystal of  $n = 6$  ( $\text{BA}_2\text{MA}_5\text{Pb}_6\text{I}_{19}$ ).

lation,<sup>11,20</sup> and pinhole control<sup>21</sup> can increase the material's resilience and lifetime but not significantly enough to make it competitive with more stable alternative PV and OE materials such as Si- or Ga-based compounds. Prior studies have shown that exposing  $\text{MAPbI}_3$  to temperatures as modest as 75–85 °C leads to degradation rates significantly faster than that at room temperature.<sup>12,16–18,22</sup> This thermal instability is responsible for the failure to meet international standards for solar cells, which require that they remain stable up to at least 85 °C (IEC 61646).<sup>23</sup> The exceptionally low thermal conductivity of single-crystal  $\text{MAPbI}_3$ , reported to be  $\kappa = 0.34$ –0.50 W/m·K,<sup>24–27</sup> makes proper thermal management a major challenge to its stability and longevity in devices.

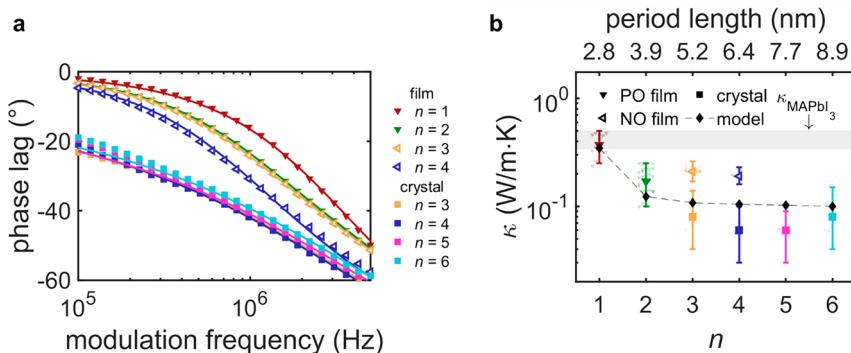
Two-dimensional, layered perovskite structures such as Ruddlesden–Popper (RP) phases have been developed in an effort to retain the desirable features of 3D HOIPs, such as solution processability, and catalyze stability and excitonic effects more akin to conventional PV materials.<sup>28–30</sup> In these structures,  $n$  layers of perovskite octahedral cages are separated by organic cationic spacers. The  $\text{MAPbI}_3$ -based RP phases,  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  (BA = butylammonium) (see Figure 1a), exhibit improved stability in moisture- and light-rich environments due to the presence of hydrophobic BA chains and demonstrate PCEs as high as ~12.5%.<sup>30–32</sup> These RP phases have shown degradation at 80 °C, though at slower rates than  $\text{MAPbI}_3$ .<sup>15</sup> However, their thermal conductivities and the underlying phonon transport mechanisms, which control their ability to dissipate heat, remain unclear. A recent experimental study of multiple lead halide 2D layered perovskites finds that their thermal conductivities are related to the orientation of the organic spacers relative to the inorganic layers.<sup>33</sup> The importance of the inorganic layer thickness and interface density, controlled by  $n$ , was not considered since the structures were not derivatives of the same perovskite family. Meanwhile, Rasel *et al.* hypothesize that the decreasing thermal conductivity they observe in  $(\text{C}_n\text{H}_{2n+1}\text{NH}_3)_2\text{PbI}_4$  2D perovskites with increasing  $n$  may result from phonon transport dependency on organic-chain length.<sup>34</sup>

To that end, interest in the thermal conductivity of  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  RP phases is 2-fold. Practically, the thermal conductivity is important to maintain appropriate temperatures during device operation. Fundamentally, the naturally occurring 2D architecture of these structures allows for the possibility of

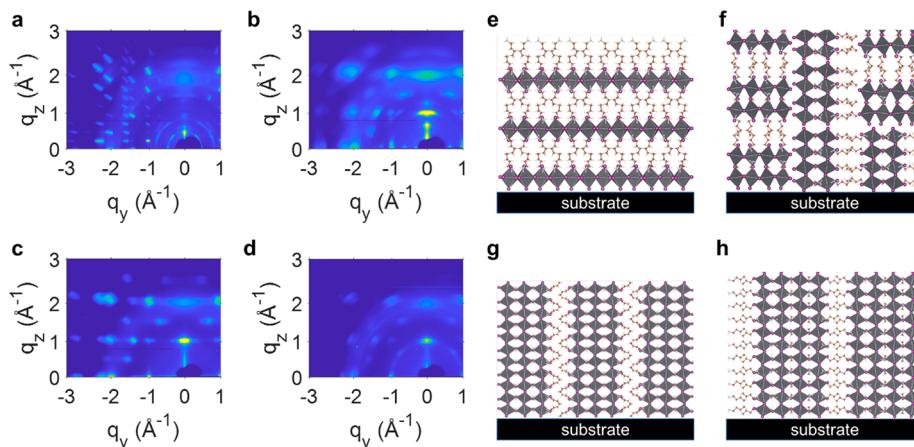
coherent interlayer phonon transport. In the context of 91 superlattices, this occurs when phonon modes emerge from 92 the secondary periodicity rather than scatter at the structure's 93 associated interfaces and therefore exhibit "wave-like" instead of 94 "particle-like" transport.<sup>35,36</sup> The so-called coherent phonons 95 can have mean free paths greater than the superlattice period, 96 thus enabling higher thermal conductivities than would be 97 expected in a purely particle-like regime. However, such 98 coherent phonon enhancements to thermal conductivity of 99 layered materials can be hindered by imperfect interfaces that 100 destroy periodicity<sup>35,36</sup> and thus have only been observed in a 101 few cases such as in very high-quality epitaxial oxide 102 heterostructures<sup>34</sup> and GaAs/AlAs superlattices.<sup>36</sup>

Secondary periodicity and the resulting coherent phonons 104 have been studied in RP phases,<sup>37–39</sup> and their effect on thermal 105 conductivity has been considered with mixed conclusions.<sup>40,41</sup> A 106 recent transient reflectance study describes longer period 107 oscillations in  $(\text{PEA})_2\text{Pb}_n\text{I}_{3n+1}$  RP phases with increasing  $n$ .<sup>108</sup> While they do not consider how this affects phonon speed, they 109 speculate that it will cause thermal conductivity to increase with 110 increasing  $n$ .<sup>40</sup> By contrast, through atomic-level simulations, a 111 separate study concluded that the thermal conductivity of a 112  $\text{SrTiO}_3$ -based RP phase should decrease with increasing  $n$ .<sup>41</sup> 113 Clearly, more experimental thermal conductivity data are 114 required to understand the complex phonon physics and 115 thermal transport in RP phases.<sup>116</sup>

Here, we determine the cross-layer thermal conductivity of 117 thin film and single-crystal  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  RP phases for  $n =$  118 1–6 using a high-resolution optical pump–probe technique 119 known as frequency-domain thermoreflectance (FDTR).<sup>42</sup> In 120 doing so, we distinguish the relationship between the thermal 121 conductivity of these RP phases and that of  $\text{MAPbI}_3$  to consider 122 the implications on the thermal performance and longevity of 123 devices that may implement this class of perovskite material. 124 Moreover, we experimentally observe a decrease in thermal 125 conductivity with increasing  $n$  in low- $n$  RP phases of similar 126 orientation, suggesting that the contribution of coherent 127 phonons diminishes as the interface density decreases. We 128 reason that this phenomenon, coupled with the other tunable 129 properties of  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$ , identifies pathways for 130 functionality in a wide variety of devices.<sup>131</sup>



**Figure 2.** (a) FDTR phase lag data (markers) and fits (lines) for  $n = 1-4$  thin films and  $n = 3-6$  single crystals. (b) Room-temperature thermal conductivity of  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  as a function of  $n$  for  $n = 1-6$ . Downward and sideways facing triangles represent thin films that have layers of parallel orientation (PO) and normal orientation (NO) with respect to the substrate, respectively. Squares represent single crystals, and black diamonds represent the predicted thermal conductivity by a reduced-order lattice dynamics model. Semitransparent data are individual measurements, and opaque data are medians of all measurements for the respective sample, where error bars represent the 90th and 10th quantiles of fit distributions generated using a Monte Carlo estimation of uncertainty. The gray-shaded region indicates the range of thermal conductivities reported in the literature for  $\text{MAPbI}_3$ . Period length of the respective structure is labeled on the top axis.



**Figure 3.** GIWAXS measurements (a-d) and structural interpretation (e-h) of  $n = 1-4$  thin films. The  $[0\ 1\ 0]$  crystal direction of  $n = 1$  is oriented normal to the substrate, while this same direction in  $n = 3$  and  $n = 4$  thin films is loosely parallel to the substrate.  $n = 2$  appears to be bimodal, possessing a 2:1 ratio of grains with the  $[0\ 1\ 0]$  crystal direction oriented normal and parallel to the substrate.

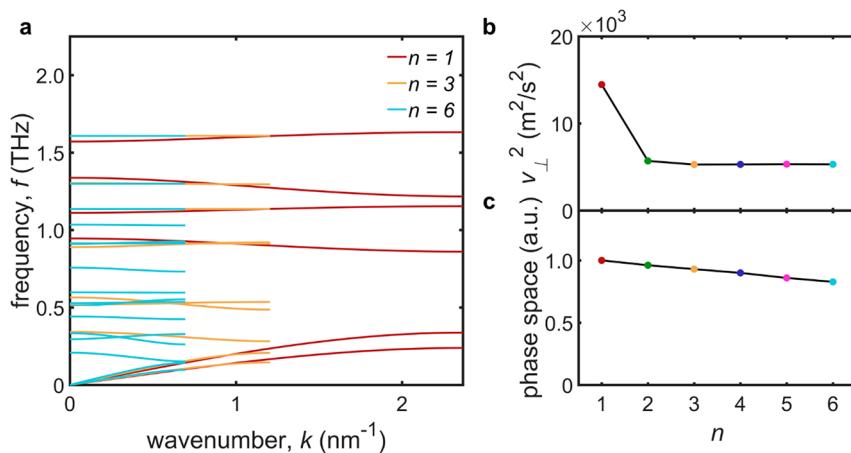
## RESULTS AND DISCUSSION

We examine thin films of  $n = 1-4$  (thickness range of 40–240 nm) and single crystals of  $n = 3-6$  (size range of 0.5–2 mm) (see Figure 1b). Single crystals of  $n = 1, 2$  could not be repeatedly measured due to their typically smaller size (less than 200  $\mu\text{m}$ ), irregular shape, and rough surface topography. We measure thermal conductivity across numerous samples of both single crystals and thin films using FDTR. FDTR periodically heats the sample and monitors the phase lag of surface temperature to heat flux, which is fit using an analytical solution to the heat diffusion equation to extract the sample's unknown thermal conductivity (see Methods for details on sample preparation and FDTR). Fits based solely on thermal conductivities ( $\kappa$ ) of RP phases, shown as solid lines in Figure 2a, consistently match the experimental phase lag data over a wide range of frequencies and support the accuracy of this approach.

The thermal conductivities ( $\kappa$ ) of  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  RP phases are shown as a function of  $n$  for  $n = 1-4$  thin films and  $n = 3-6$  single crystals in Figure 2b. Individual measurements are shown as semitransparent markers, whereas the central tendency, represented by the median, for each  $n$  is shown as an opaque marker. Upper and lower error bars represent the 90th and 10th quantiles of the distribution of fits generated by

Monte Carlo estimation method, which is used to assess the uncertainty in  $\kappa$  from measurement variability and propagated uncertainty from fitting parameters (see SI Section 2.5).<sup>43,44</sup> The  $\kappa$  values of the thin film RP phases of  $n = 1-4$  are ultralow at  $0.37 \pm 0.13/0.12$ ,  $0.17 \pm 0.08/0.07$ ,  $0.21 \pm 0.05/0.04$ , and  $0.19 \pm 0.04/0.03$  W/m·K, and that of the single-crystal RP phases of  $n = 3-6$  are even lower at  $0.08 \pm 0.06/0.04$ ,  $0.06 \pm 0.04/0.03$ ,  $0.06 \pm 0.03/0.03$ , and  $0.08 \pm 0.07/0.04$  W/m·K. The  $\kappa$  values of the thin film RP phases initially decrease as  $n$  increases, consistent with increased coherent phonon contributions to thermal conductivity in lower  $n$  phases. The  $\kappa$  values of  $n = 3-6$  single-crystal phases are among the lowest reported for fully dense solids.<sup>45</sup> Additionally, we note that  $\kappa$  values of thin films are larger than that of single crystals for  $n = 3, 4$ , contrary to the expectation of lower  $\kappa$  due to phonon boundary scattering in thin films.

To discern the origins of the discrepancy between thin films and single crystals, we perform grazing-incidence wide-angle X-ray scattering (GIWAXS) to assess the compositional purity and orientational control of thin film samples of  $n = 1-4$ . As a hybrid of wide-angle scattering and grazing incidence diffraction, in GIWAXS an X-ray beam is directed at an angle near that of total external reflection with respect to the film surface. Lengths on



**Figure 4.** (a) Phonon dispersion relationship of  $n = 1, 3$ , and  $6$  RP phases in the cross-layer  $[0\ 1\ 0]$  direction. (b) Average cross-layer group velocity of  $n = 1\text{--}6$  RP phases. (c) Total phase space, normalized to that of  $n = 1$ , of  $n = 1\text{--}6$  RP phases.

178 the order of tens of angstroms, corresponding to the  $d$ -spacing in  
 179 solid-state materials, can be accessed because of the close  
 180 distance between the detector and the sample. Additionally, the  
 181 use of a 2D detector allows for the determination of the  
 182 orientation of diffraction planes in the sample relative to the  
 183 substrate based on the position along the angular axis  $\chi$  in which  
 184 the peak appears.<sup>15,46</sup>

185 GIWAXS data are shown in Figure 3a for  $n = 1\text{--}4$ . The peaks  
 186 present in the measurement for  $n = 1$  indicate a high level of  
 187 orientational consistency with layers oriented parallel to the  
 188 substrate as shown in Figure 3e. This result confirms our  
 189 observation of ultralow cross-layer thermal conductivity ( $\kappa_{\perp}$ ) in  
 190 this RP phase, since FDTR measurements primarily probe  
 191 thermal transport properties normal to the substrate surface.  
 192 Interestingly, small peaks at low  $q$  indicate that there are some  
 193 impurities in  $n = 1$  samples, possibly resulting from solvated  
 194 phases created during film formation.<sup>47,48</sup> Data for  $n = 2$ , shown  
 195 in Figure 3b, appear bimodal, with the layers oriented normal  
 196 and parallel to the substrate surface, with the normal orientation  
 197 being about twice as common as depicted in Figure 3f. This ratio  
 198 is determined through calculation of the area under the  $(1\ 1\ 1)$   
 199 peak for each orientation (see SI Section 3.2). Data for  $n = 3, 4$   
 200 shown in Figure 3c and d have layers oriented normal to the  
 201 substrate depicted in Figure 3g and h. Notably, the  $n = 4$  member  
 202 has peaks that have been broadened along  $\chi$ , the angular axis,  
 203 which indicates that the layers deviate by a couple of degrees  
 204 from perfectly normal. In this orientation, heat will flow along  
 205 the layers for  $n = 3, 4$ . We expect that the in-layer  $\kappa$  of RP phases  
 206 will more closely resemble that of bulk  $\text{MAPbI}_3$  ( $\kappa = 0.34\text{--}0.50$   
 207  $\text{W}/\text{m}\cdot\text{K}$ ) as phonons travel along the inorganic lead iodide  
 208 layers. Hence, higher measured values of thermal conductivity  
 209 for  $n = 3, 4$  thin films, relative to single crystals, are not a true  
 210 reflection of  $\kappa_{\perp}$ , but are rather a consequence of the films' grain  
 211 orientations.

212 In addition to GIWAXS, we characterize the composition and  
 213 orientation of structures in  $n = 1\text{--}4$  RP thin films using powder  
 214 X-ray diffraction, or PXRD (see SI Section 4). We find that peaks  
 215 in the  $n = 1$  measurement correspond to planes parallel to the  
 216 substrate and that there are no features consistent with other  
 217 orientations. Our measurement of  $n = 2$  corroborates the  
 218 bimodal distribution of orientations observed in the GIWAXS  
 219 measurement, with peaks being associated with planes both  
 220 perpendicular and parallel to the substrate. The major peak  
 221 found in the measurements of  $n = 3, 4$  thin films corresponds to

222 the  $(2\ 0\ 2)$  plane, and the minor peak is associated with the  $(1\ 1\ 223$   
 224 1) plane that lies at an angle with respect to the substrate. Given  
 225 that the former peak is significantly stronger than the latter, we  
 226 conclude that the majority of the structure is oriented  
 227 perpendicular to the substrate in both films.

228 While our measurements are consistent with the value  
 229 reported by Giri *et al.* for the  $n = 4$  thin film with similar  
 230 orientation ( $0.19 \pm 0.04/0.03 \text{ W}/\text{m}\cdot\text{K}$  vs  $0.17 \pm 0.03 \text{ W}/\text{m}\cdot\text{K}$ ),<sup>33</sup> we find lower values of  $\kappa_{\perp}$  in  $n = 4$  single crystals due to  
 231 transport being exclusively cross-layer. We measure a com-  
 232 paratively higher  $\kappa_{\perp}$  in  $n = 1$ , or  $(\text{CH}_3\text{NH}_3)_2\text{PbI}_4$ , thin films than  
 233 that reported by both Giri *et al.* for thin films ( $0.18 \pm 0.04 \text{ W}/\text{m}\cdot\text{K}$ )<sup>33</sup> and Rasel *et al.* for single crystals ( $0.125 \pm 0.089 \text{ W}/\text{m}\cdot\text{K}$ ).<sup>34</sup> Notably, the steady-state temperature rise in samples of  $n = 1$  resulting from our laser heating (14.6 K, see SI Section 2.6) is similar to that of Giri *et al.* (14 K) and is lower than that of Rasel *et al.* (30 K). It is possible that the lower thermal conductivity reported by Rasel *et al.* may arise from laser heating induced structural rearrangements that they hypothesize exist at and beyond  $\sim 325$  K based on their heat capacity data. Such structural rearrangements could hinder phonon transport and therefore reduce apparent thermal conductivity. By comparison, the difference between our reported value and that of Giri *et al.* may originate from variation in film preparation, particularly the use of different solvents and substrate temperatures during deposition, which are well known to affect film morphology, homogeneity, and composition.<sup>31,48–50</sup>

240 The overarching trend in Figure 2b is that  $\kappa_{\perp}$  (filled opaque  
 241 data in Figure 2b;  $n = 1, 2$  thin films and  $n = 3\text{--}6$  single crystals)  
 242 of the RP phases initially decreases as  $n$  and the interface spacing  
 243 increases and levels off at higher  $n$ . Generally, our findings  
 244 suggest that thermal conductivity is possibly related to layer  
 245 spacing by way of coherent phonon transport. In any superlattice  
 246 there will be a coexistence of emergent coherent phonons that  
 247 transmit through interfaces, and incoherent phonons that  
 248 maintain the character of one constituent layer and scatter at  
 249 the interfaces. The particle description of phonons suggests that  
 250 increased interface spacing enables longer phonon mean free  
 251 paths and therefore higher thermal conductivity. Since we  
 252 observe the opposite trend, it appears that coherent phonons  
 253 may contribute significantly to the thermal conductivity of  $n = 1, 2$  RP phases. We hypothesize that phonon coherence plays a less  
 254 significant role in the thermal conductivities of  $n = 3\text{--}6$  phases  
 255 given their relative insensitivity to  $n$ .

266 The cross-layer thermal conductivity can be expressed as

$$\kappa_{\perp} = \sum_{\beta} C_{\beta} v_{\perp, \beta}^2 \tau_{\beta} \quad (1)$$

267

268 where  $\beta$  indexes the phonon mode and  $C$ ,  $v_{\perp}$ , and  $\tau$  represent the  
269 modal heat capacity, cross-layer component of group velocity,  
270 and relaxation time. To quantitatively understand the effect of  
271 coherent phonon group velocity on  $\kappa_{\perp}$  in  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$ , we  
272 perform a reduced-order harmonic lattice dynamics calculation.  
273 To limit computational cost and modeling complexity,<sup>51</sup> we  
274 group atoms together to form octahedron-like and BA-like beads  
275 (see SI Section 5.1) that interact harmonically according to the  
276 equations of motion. Three spring constants are invoked to  
277 generate the equations of motion in this system: octahedron–  
278 octahedron, BA–BA, and BA–octahedron. The first is fit from  
279 the experimental dispersion of  $\text{MAPbI}_3$ ,<sup>52</sup> whereas the other two  
280 are derived from experimentally determined sound speeds.<sup>53</sup>  
281 These equations of motion are used in an assumed plane wave  
282 solution to determine the coherent phonon dispersion  
283 relations.<sup>54–57</sup> With BA omitted, the model accurately  
284 reproduces the acoustic phonon dispersion of  $\text{MAPbI}_3$  (see SI  
285 Section 5.3).<sup>52</sup> By using a reduced-order model, we ignore high-  
286 frequency incoherent phonon modes due to the localized  
287 internal vibrations of the  $\text{MAPbI}_3$  or BA molecules.

288 The nonintuitive trend in  $\kappa_{\perp}$  with  $n$  can be explained by the  
289 lattice dynamics that capture the effects of emergent coherent  
290 phonons. In Figure 4a we show the phonon dispersion  
291 relationships for  $n = 1, 3$ , and  $6$  in the cross-layer [0 1 0]  
292 direction. As  $n$  increases there is more band flattening at high  
293 wavevectors and an increased number of phonon bandgaps  
294 resulting from the increased bead number density. Generally,  
295 this band flattening reduces the cross-layer coherent phonon  
296 group velocities and is especially pronounced between  $n = 1$  and  
297  $n = 2$ . The Brillouin zone averaged  $v_{\perp}^2$  decreases by more than  
298 60% from  $n = 1$  to  $n = 2$ , then decreases more gradually with  
299 increasing  $n$ , as shown in Figure 4b. Phonon scattering trends  
300 with  $n$  may, however, produce a competing effect on thermal  
301 conductivity. The fraction of the phonon frequency range  
302 occupied by bandgaps increases with increasing  $n$ , which reduces  
303 the phase space for scattering of coherent phonons (*i.e.*, the  
304 number of possible three-phonon scattering events that  
305 conserve energy and momentum) as shown in Figure 4c.  
306 Reduced phonon phase space typically causes increased  
307 relaxation times and thus increased thermal conductivity, but  
308 the gradual reduction in phase space with  $n$  may be offset by  
309 reduced  $v_{\perp}^2$  and an 8% reduction in  $C_{\beta}$  (see SI Section 5.4) to  
310 create a flat  $\kappa_{\perp}$  trend for  $n = 3–6$ .

311 Our harmonic model cannot be used to directly predict  $\kappa_{\perp}$   
312 since the average phonon lifetime  $\bar{\tau}_n$  for  $n = 1–6$  is not modeled.  
313 However, the correspondence of  $\kappa_{\perp}$  data to the average  $v_{\perp}^2$  and the  
314 relative invariance of phase space led us to fit eq 1 to the  $\kappa_{\perp}$  data  
315 by choosing a single  $\bar{\tau}$  across all  $n$  that minimizes the mean  
316 square error. We find a  $\bar{\tau}$  for coherent phonons across  $n = 1–6$   
317 RP phases of  $\sim 100$  ps, resulting in a predicted thermal  
318 conductivity that agrees well with experimental data across all  
319  $n$  (excluding films with  $n = 3, 4$ ), as shown in Figure 2b. While  
320 phonon relaxation times typically span orders of magnitude, the  
321 close fit of  $\kappa_{\perp}$  among all  $n$  to a single  $\bar{\tau}$  suggests that those of  
322 coherent phonons that may contribute heavily to  $\kappa_{\perp}$  have a  
323 narrower distribution. An average relaxation time of 100 ps  
324 corresponds to average cross-layer mean free paths ( $\bar{\Lambda}_{\perp} = \bar{\tau} \sqrt{v_{\perp}^2}$ )

) of coherent phonons spanning 7 nm for  $n = 6$  to 12 nm for  $n = 325$   
1, which are larger than or similar to the period length.<sup>326</sup>

## CONCLUSIONS

In summary, we determine thermal conductivity perpendicular to the layers,  $\kappa_{\perp}$ , of  $\text{BA}_2\text{MA}_{n-1}\text{Pb}_n\text{I}_{3n+1}$  RP phases using FDTR and find that it decreases with increasing  $n$ , particularly at low  $n$ . We predict that the observed trend in  $\kappa_{\perp}$  is due to a reduction in coherent phonon transport in higher  $n$  RP phases. According to our measurements, single crystals of  $n = 3–6$  all present ultralow thermal conductivities on the order of the lowest ever observed in fully dense solids. Our coarse-grain 3D lattice dynamics calculations reveal that the average of the square of cross-layer sound velocity,  $\bar{v}_{\perp}^2$ , of coherent phonons decreases with  $n$  at a rate consistent with our experimental  $\kappa_{\perp}$  data. Our findings suggest that while these RP phases are more stable than  $\text{MAPbI}_3$  at elevated temperatures, their ultralow  $\kappa_{\perp}$  may make maintaining serviceably low temperatures challenging. However, varying  $n$  allows for tunability in thermal conductivity and other material properties, which unlocks a myriad of possibilities for design in PV, OE, and thermal transport applications.

## METHODS

**Sample Preparation.** Thin film RP phases with thicknesses of 40–240 nm are spin coated onto Si substrates. Single crystals, typically 0.5–2.0 mm in major dimension (as shown in Figure 1b), are precipitated from aqueous solution and epoxied to  $\text{SiO}_2$  substrates. Single crystals are exfoliated using Kapton tape to expose a pristine layer of material. Thin films and single crystals are then sputtered or evaporated with 60–110 nm of Au. Profilometry is used to determine the thickness of the deposited Au layer, as well as that of the underlying perovskite layer in the case of the thin films. Samples are kept in a dark Ar glovebox environment except for transport, metal deposition, and measurement to minimize the possibility of contamination or exposure.

**FDTR.** In FDTR, the sample is heated by a 488 nm continuous-wave (CW) pump laser that is intensity-modulated over frequencies ranging from 100 kHz to 5 MHz. Periodic heating generates a periodic change in the sample's surface temperature, with a phase lag that depends on the thermal conductivity of the RP phase sample. Thermoreflectance of the Au coating causes modulation of a reflected 532 nm CW probe laser, and its phase lag relative to the pump is monitored by a lock-in amplifier. The phase lag of the probe to pump (temperature to heating) is fit to a solution of the heat diffusion equation for a periodically heated layered structure to determine the unknown RP phase thermal conductivity, as shown in Figure 2a.<sup>58</sup>

The analytical solution used to fit the FDTR data relies on thermophysical properties of the sample such as its thickness and specific heat. The RP phases' volumetric heat capacities are not directly measured, so they are estimated based on the molar heat capacities of the structure's three constituent materials (BA,  $\text{MAPbI}_3$ , and  $\text{PbI}_4$ ) and the volume of the unit cell. In the case of the thin films, the fit solution is insensitive to this parameter within the range of our measurements (see SI Section 2.4), so imprecision in this approximation does not significantly impact the quality of fit, quantified as a mean-squared error.

**GIWAXS.** GIWAXS is performed at Beamline 12-ID-B of the Advanced Photon Source at Argonne National Laboratory. A PerkinElmer XRpad (PerkinElmer Inc.) detector is employed with the sample-to-detector distance set to 18 cm. The energy of X-ray radiation is 13.3 keV. The samples used in GIWAXS measurements are deposited on silicon wafer substrates. The substrates are first aligned to be parallel to the X-ray beam, and the GIWAXS data are collected at an X-ray beam incidence angle of  $\sim 0.1^\circ$ . Curves are fit to the data using the LineFit toolbox, while plots are generated using the GIXSGUI program.<sup>59</sup> Simulations of  $\text{MAPbI}_3$  and BA at different orientations are created by LeeTool, a MATLAB-software package written by

389 Byeongdu Lee, available at the 12-ID-B beamline of the Advanced  
390 Photon Source (APS) at Argonne National Lab.

## 391 ASSOCIATED CONTENT

### 392 Supporting Information

393 The Supporting Information is available free of charge at  
394 <https://pubs.acs.org/doi/10.1021/acsnano.0c03595>.

395 Sample preparation and characterization, frequency-  
396 domain thermoreflectance model parameters, sensitivity,  
397 uncertainty, heating analysis, GIWAXS and PXRD  
398 acquisition and analysis, lattice dynamics model frame-  
399 work ([PDF](#))

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### 443 Notes

444 The authors declare no competing financial interest.

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