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FLEXO: Development of a Portably Performant AMR Code for XMHD

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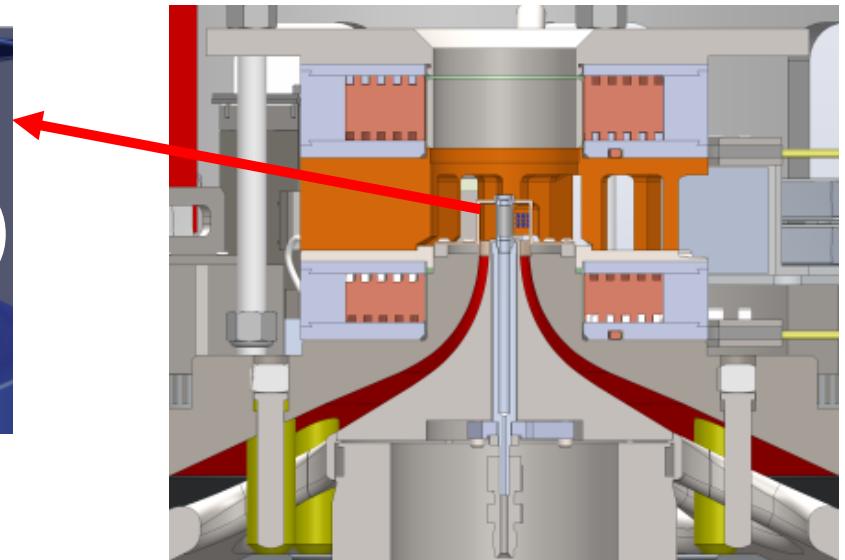
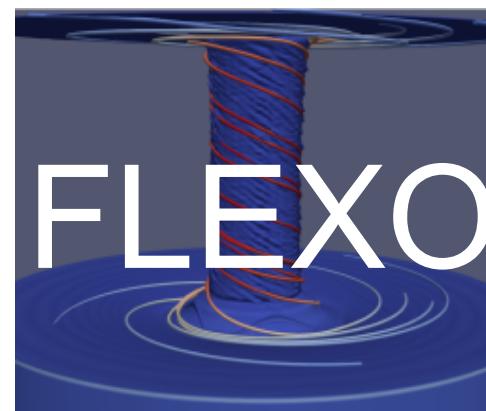
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Background and Motivation

- PERSEUS
 - Design code for experiments to investigate the origins of helical instabilities in MagLIF
 - Validation tests on Z experimental data bringing new insights into previously unexplained data
 - Results indicate the importance of Hall physics in target applications

- FLEXO
 - Next-generation of PERSEUS with expanded feature set for target design
 - Improve performance: NGP from inception
 - Improve fidelity: AMR to capture fine-scale features
 - Additional physics: multi-material to capture containment effects
 - Additional physics: tabular equations of state and conductivities for predictive material response



Governing Equations + Time Advancement Strategy

- Governing Equations

$$\partial_t[\rho] + \nabla \cdot [\rho \mathbf{v}] = 0,$$

$$\partial_t[\rho \mathbf{v}] + \nabla \cdot [\rho \mathbf{v} \mathbf{v} + p \mathbf{I}] = \mathbf{J} \times \mathbf{B},$$

$$\partial_t[\mathcal{E}] + \nabla \cdot [\mathbf{v}(\mathcal{E} + p)] = \mathbf{v} \cdot (\mathbf{J} \times \mathbf{B}) + \eta \mathbf{J}^2,$$

$$\partial_t[\mathbf{B}] + \nabla \times \mathbf{E} = \mathbf{0},$$

$$\partial_t[\mathbf{E}] - c^2 \nabla \times \mathbf{B} = -c^2 \mu_0 \mathbf{J},$$

$$\partial_t[\mathbf{J}] = \frac{n_e e^2}{m_e} \left(\mathbf{E} + \mathbf{v} \times \mathbf{B} - \frac{1}{n_e e} \mathbf{J} \times \mathbf{B} - \eta \mathbf{J} \right).$$

Hall term



- Discretization Strategy

- Space: DG P0/P1/P2

- Time:

- Fields explicitly advanced to intermediate stage (*), where all source terms except energy are neglected.

- Implicit (element-local) correction:

$$\mathbf{E}^{n+1} = \mathbf{E}^* - \Delta t c^2 \mu_0 \mathbf{J}^{n+1},$$

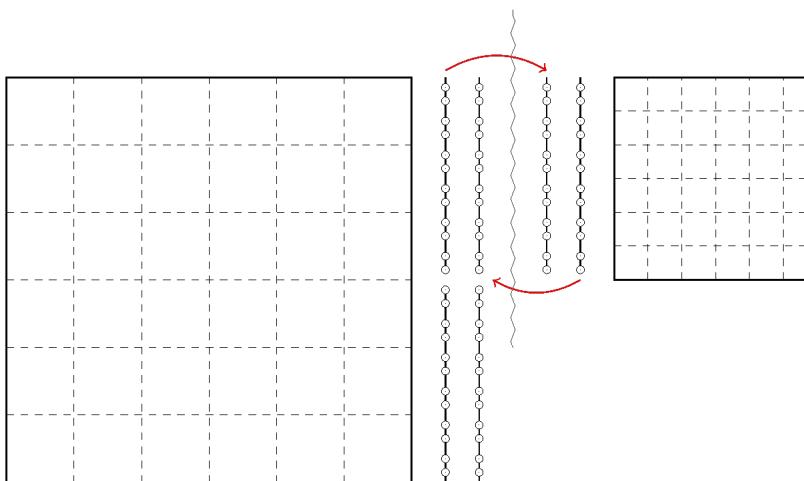
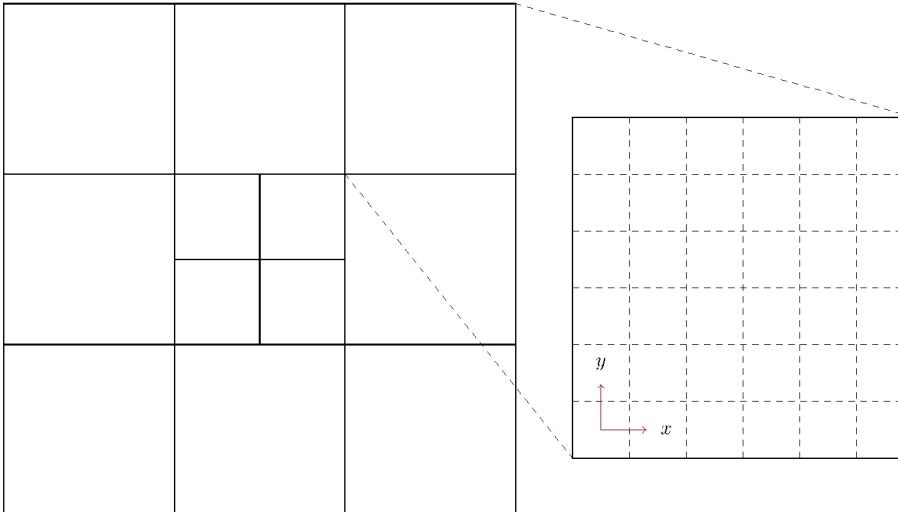
$$[\rho \mathbf{v}]^{n+1} = [\rho \mathbf{v}]^* + \Delta t [\mathbf{J} \times \mathbf{B}],$$

$$\begin{aligned} \mathbf{J}^{n+1} = \mathbf{J}^* + \Delta t \left(\frac{n_e e^2}{m_e} \right) & [\mathbf{E}^{n+1} + \mathbf{v}^* \times \mathbf{B}^* \\ & - \frac{1}{n_e e} \mathbf{J}^{n+1} \times \mathbf{B}^* - \eta^* \mathbf{J}^{n+1}]. \end{aligned}$$

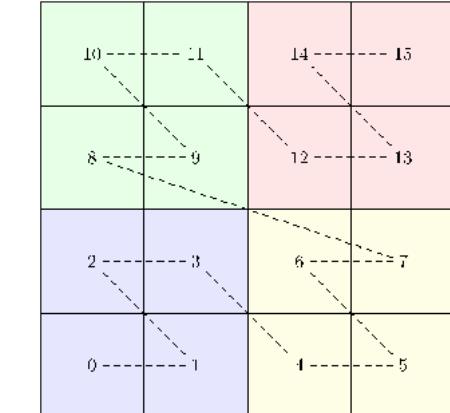
For details see: Seyler, Martin, Physics of Plasmas 18, 012703 (2011)



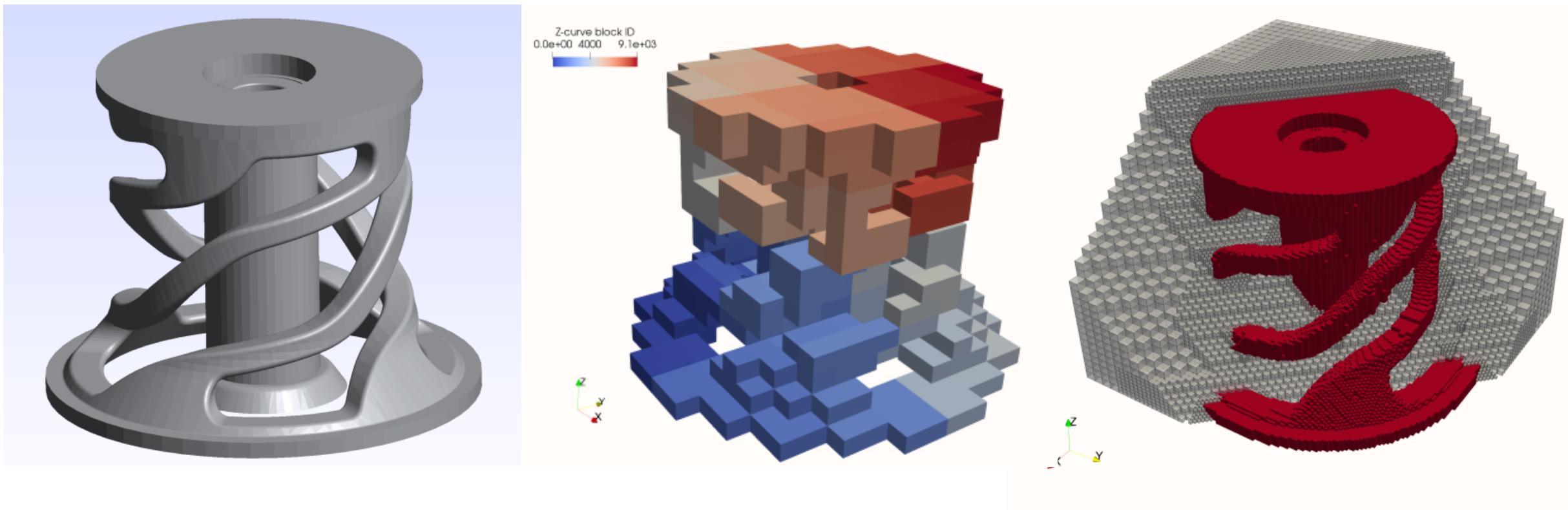
DEVELOPMENT EFFORT: AMR Framework



- Octree mesh data structure
 - MPI parallelized leaves
 - Each leaf is called a “block”
 - Each block represents a structured (i,j,k) Cartesian grid
 - Physics is evaluated over each block
 - Fluxes across block boundaries couple block physics
 - Shared memory parallelism -> kernels over block entities (cells, sides)
 - MPI parallelism -> solution information transferred at block borders, Z-curve block partitioning
 - Block adjacencies restricted to at most one finer or coarse level (2-1 interfaces)



AMR Framework Mesh Example



STL “CAD” geometry



Octree refined to STL
geometry definition



Material initialization in
refined octree mesh

Illustrates the difference between “block-based” and “cell-based” AMR

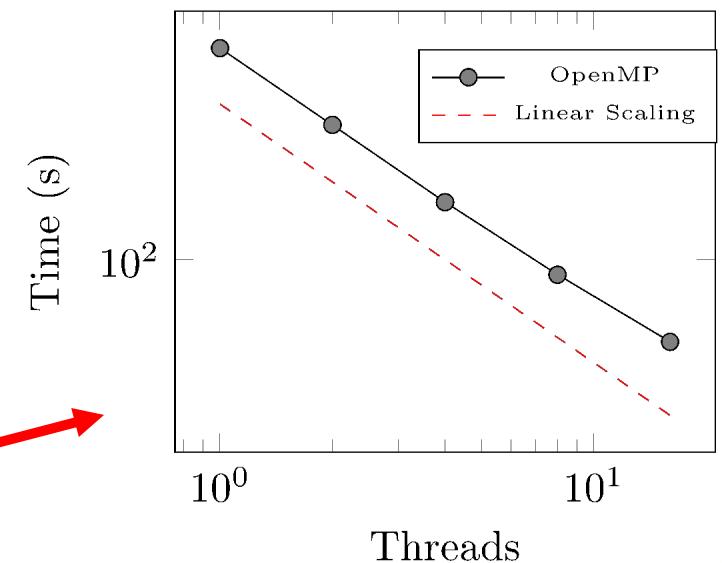
DEVELOPMENT EFFORT: NGP Execution

- Shared-memory parallelism occurs over block entities (cells, sides)
 - A parallel-for construct (flexo::for_each) calls a functor that defines physics behavior
 - flexo::for_each
 - wrapper around Kokkos::parallel_for to parallelize over (i,j,k) grid indices
 - made possible with the use of Kokkos::MDRangePolicy
 - All functors run in a single execution space (GPU, OpenMP, etc...) depending on compilation
 - However, Kokkos makes mixing + matching execution spaces possible

```
grid3 const cell_grid = block.cell_grid();
auto f = KOKKOS_INLINE_FUNCTION (vector3<int> const& cell_loc) {
    int const cell = cell_grid.index(cell_loc);
    for (int basis = 0; basis < num_basis(polynomial_order); ++basis) {
        residual(cell, RHO, basis) += 1.0;
    }
};
flexo::for_each(cell_grid, f);
```

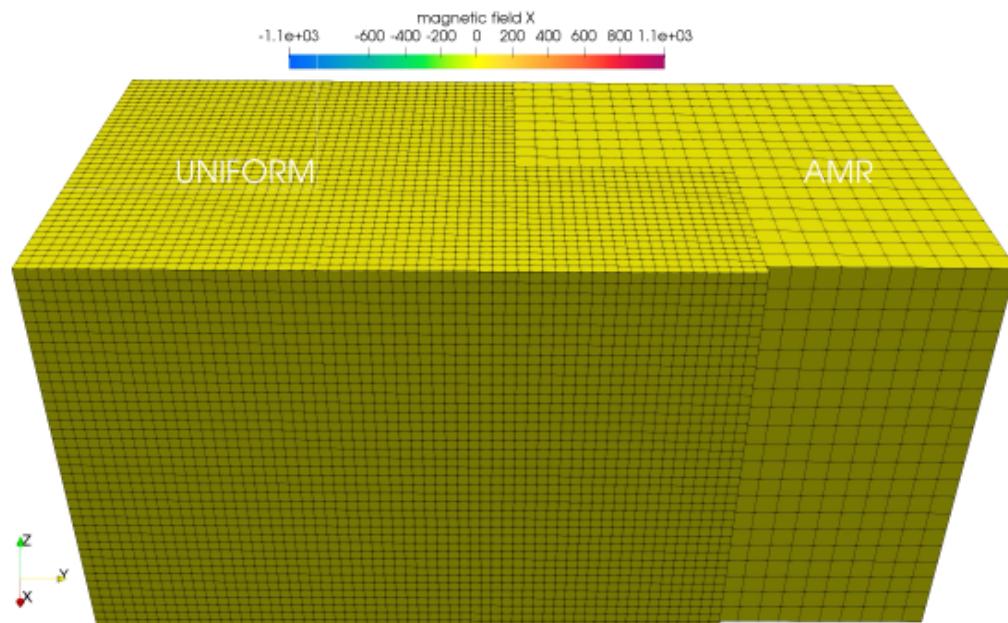
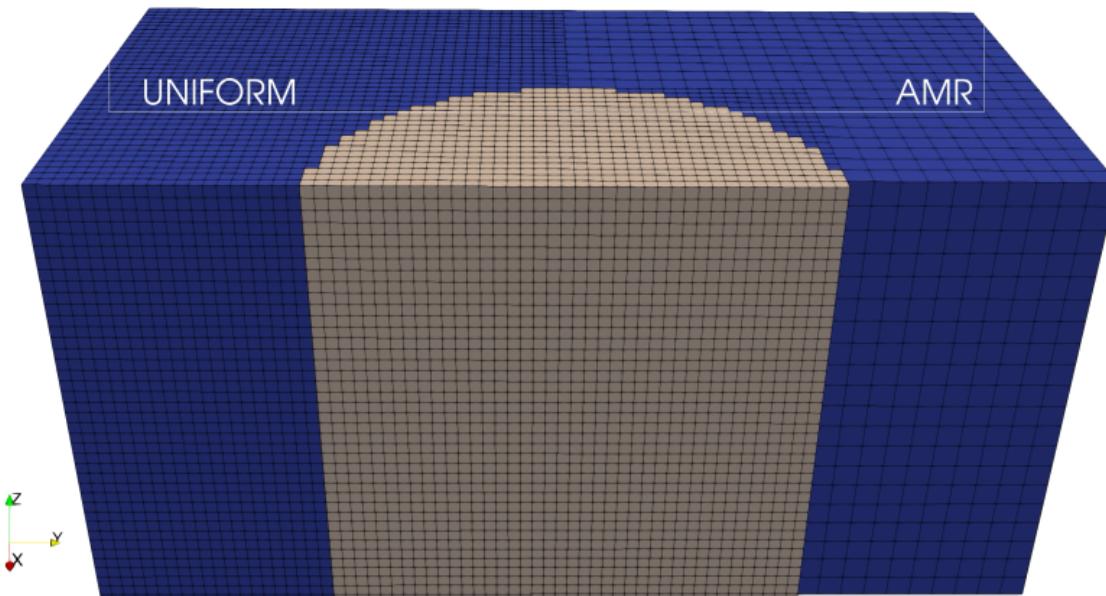
Nearly ideal shared-memory scaling for ENTIRE simulations, not just a single functor

Timings for wire example (100x100x100 cells)



NGP Execution Example

- Magnetically driven implosion
 - 80x80x80 cells in uniform grid cases
 - Cylinder with sinusoidally perturbed surface
 - Poynting inflow, momentum outflow



SMR (static mesh refinement) results agree nicely to uniform grid results

Table 1: Cylindrical Implosion Timings (80x80x80 cells, 10 steps)

PERSEUS	FLEXO
Intel(R) Xeon(R) CPU E7-4880	Tesla V100-SXM2-16GB
343.935s	2.177s

158 times faster!

DEVELOPMENT EFFORT: Multi-Material Extensions

- Governing equations
 - Per-material evolution equations: volume fraction, mass conservation, energy
 - Single mixture velocity, and thus momentum
 - Non-conservative source terms handled through Riemann solver * quantities

$$\partial_t[\alpha_k] + \mathbf{v} \cdot \nabla \alpha_k = 0,$$

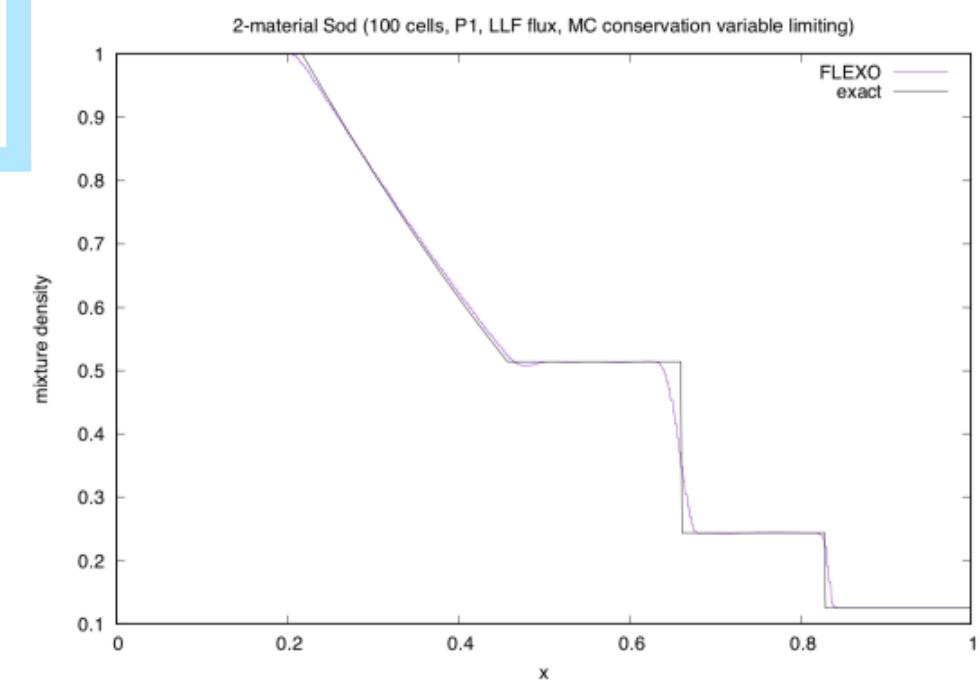
$$\partial_t[\rho_k] + \nabla \cdot [\rho_k \mathbf{v}] = 0,$$

$$\partial_t[\bar{\rho}\mathbf{v}] + \nabla \cdot [\bar{\rho}\mathbf{v}\mathbf{v} + \bar{p}\mathbf{I}] = \mathbf{J} \times \mathbf{B}$$

$$\partial_t[\rho_k \mathcal{E}_k] + \nabla \cdot [\mathbf{v}(\rho_k \mathcal{E}_k + \alpha_k p_k)] = \mathbf{v}^* \cdot \nabla [\alpha_k p_k]^* - \frac{\rho_k}{\bar{\rho}} \mathbf{v}^* \cdot \nabla [\bar{p}]^*$$

For details see: Pandare et al., DOI: 10.1002/fld.4810 (2019)

$$\rho_k := \alpha_k \tilde{\rho}_k, \quad \bar{\rho} := \sum_{k=1}^{n_{\text{mat}}} \rho_k, \quad \bar{p} := \sum_{k=1}^{n_{\text{mat}}} \alpha_k p_k.$$





DEVELOPMENT EFFORT: Tabular Equations of State

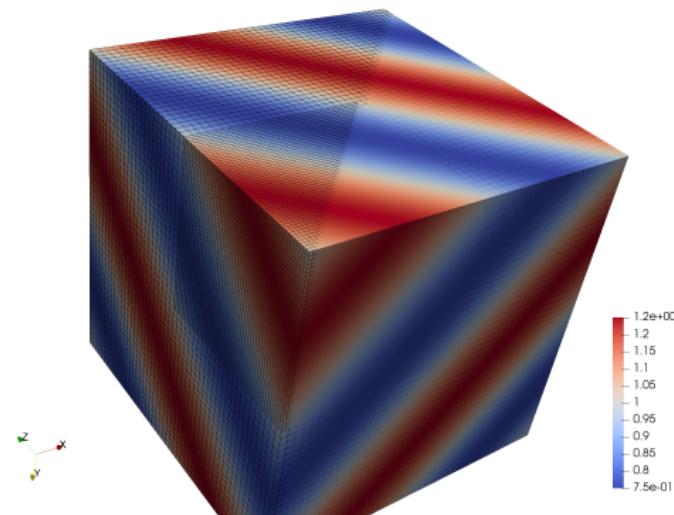
- Use tabular EOS's (SESAME) for more predictive material response
- Requires modernization of tabular read / interpolation routines for NGP execution
 - SESAME table data must be moved to device memory for GPU execution
 - Interpolation / reverse interpolation methods have been re-written to execute on device
- Have an initial implementation of SESAME EOS tables for hydrodynamic variables
 - Higher-order interpolation / reverse interpolation routines
 - Will allow novel performance assessments for tabular EOS evaluations in NGP settings
 - Ongoing collaboration with EOS + plasma physics experts to improve:
 - tabular interpolation
 - response at density / temperature floors
- Mock ideal gas SESAME table (301) part of test harness
- TODO: conductivity + ionization state from SESAME tables (601)

```
This is a simple single cell ideal gas table using the values
gamma = 1.25, cv = 1.0
rho_min = 1.0e-6, rho_max = 1.0e+6
T_min = 1.0e-6, T_max = 1.0e+6
1 9999 301 42 3032010 3032010 1 1
4.0000000E+00 4.0000000E+00 1.0000000e-06 3.3333333e+05 6.6666667e+0511211
1.0000000e+06 1.0000000e-06 3.3333333e+05 6.6666667e+05 1.0000000e+0612111
2.5000000e-13 8.3333333e-02 1.6666667e-01 2.5000000e-01 8.3333333e-022111
2.7777778e+10 5.5555556e+10 8.3333333e+10 1.6666667e-01 5.5555556e+1011111
1.1111111e+11 1.6666667e+11 2.5000000e-01 8.3333333e+10 1.6666667e+111111
2.5000000e+11 1.0000000e-06 1.0000000e-06 1.0000000e-06 1.0000000e-0612111
3.3333333e+05 3.3333333e+05 3.3333333e+05 3.3333333e+05 6.6666667e+0511111
6.6666667e+05 6.6666667e+05 6.6666667e+05 1.0000000e+06 1.0000000e+0611111
1.0000000e+06 1.0000000e+06 11000
```

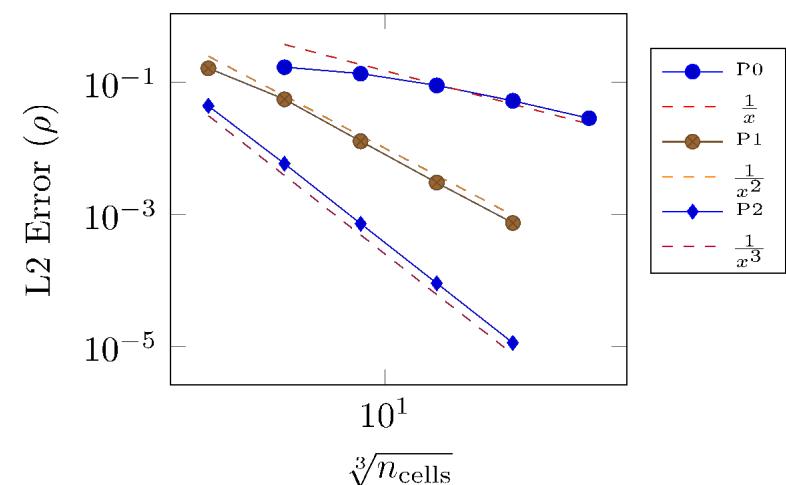


DEVELOPMENT EFFORT: Verification & Validation

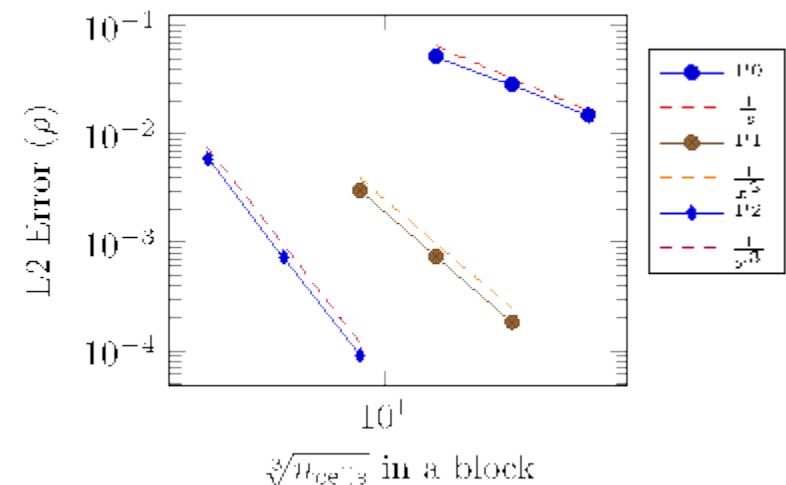
- Desire for a strong V&V culture in development cycle
- TDD/integration in accordance with modern practices
- Broad computational physics space must be verified
 - DG \rightarrow P0/P1/P2 cells
 - Pure hydrodynamics
 - Pure electromagnetics (EM)
 - Coupled XMHD physics
 - AMR interfaces
 - Execution spaces (GPU/CPU)
- Validation efforts *forthcoming*
 - Match Z experimental results
 - Helical instability with XMHD
 - Integrate PERSEUS validation tests into development cycle



Convergence for oblique 3D wave



Convergence for oblique 3D wave w/ AMR





SUMMARY

- FLEXO is next-generation production effort based on PERSEUS
- Development efforts in FLEXO:
 - “Productionizing” current PERSEUS XMHD algorithms
 - Developing and demonstrating a portably performant (MPI + X) AMR framework
 - Including tabular equations of state for material response
 - Extending single material XMHD formulation to a 6-equation multi-material model
 - Rigorous verification & validation tests closely integrated with the development cycle using modern software tools and practices
- Some future work
 - Fully time-transient AMR (coarsening / refining blocks as the simulation evolves)
 - Demonstrate validity of multi-material XMHD via comparisons to Z experimental data
 - Right on the cusp of providing features for user-friendliness + transitioning to an eager user base