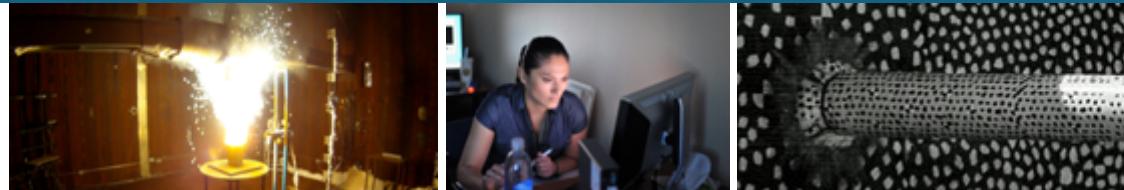




Development of Machine Learned SNAP Potentials for Studying Radiation Damage in Materials



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2021 TMS

March 15 2021

MD Approximations Change Over Time



Twobody (B.C.)

Lennard-Jones, Hard Sphere, Coulomb,

Bonded

Manybody (1980s)

Stillinger-Weber,
Tersoff, Embedded

Atom Method
GPU Timings

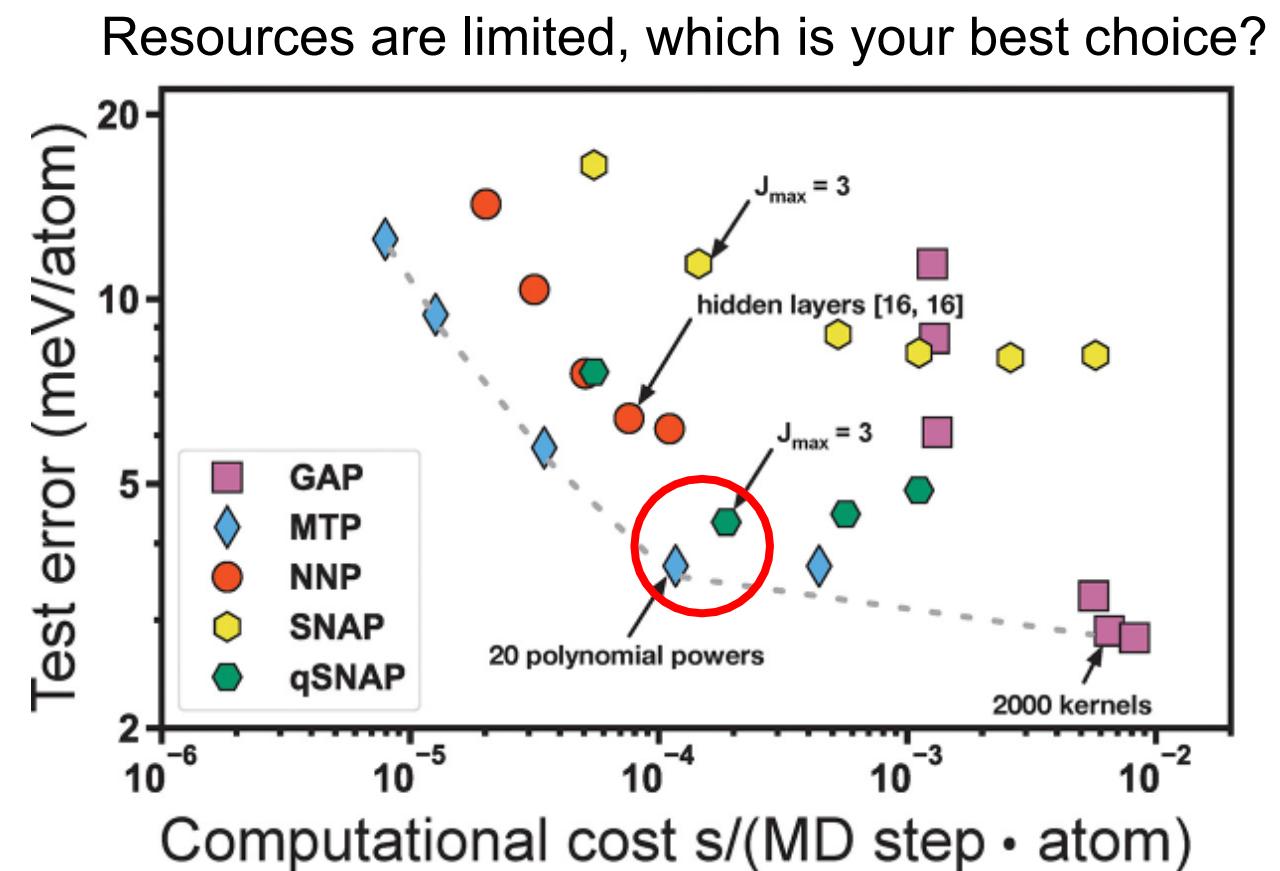
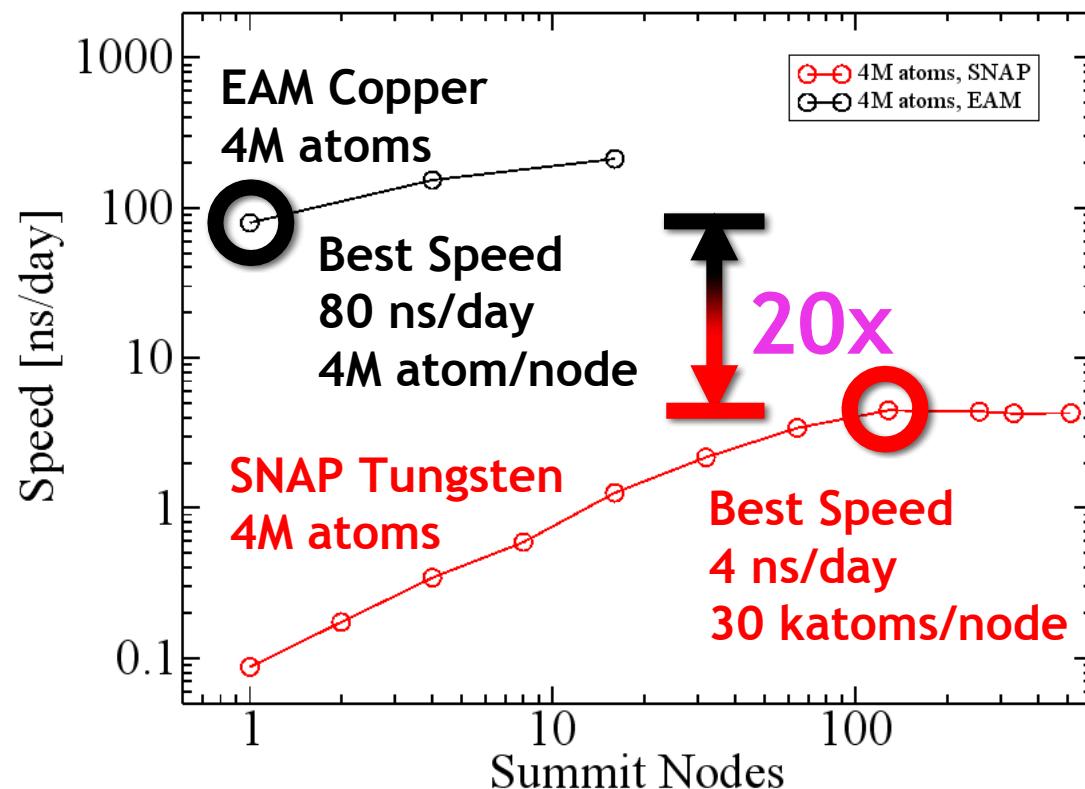
Advanced (90s-2000s)

REBO, BOP, COMB,

ReaxFF

Big Data / Deep / Machine Learning (2010s)

GAP, SNAP, NN,...

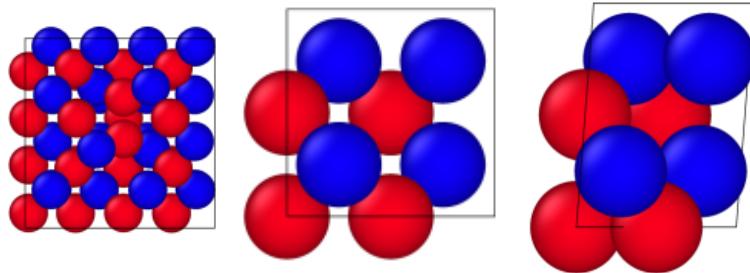


What Makes a Machine Learned Interatomic Potential?



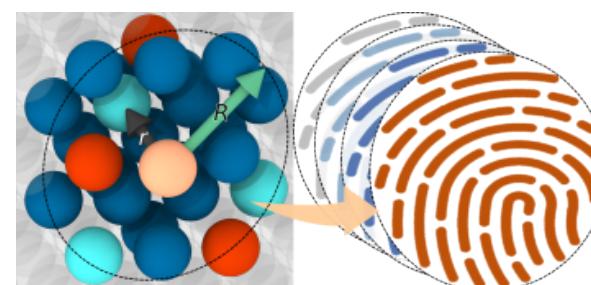
Training Data

- Generated using quantum methods
- Can include:
 - Energies
 - Forces
 - Stresses
- Variety of atomic configurations
 - Bulk structures, liquids, surfaces, defects, etc.



Descriptor

- Describes the local atomic environment
- Requirements
 - Rotation/Translation/. Permutation invariant
 - Equivariant forces
 - Smooth differentiable
 - Extensible
- Some Examples
 - Bispectrum, SOAP, ACE, Moment Tensors, etc.



Regression Method

- Linear regression
- Kernel ridge regression
- Gaussian process
- Non-linear optimization
- Neural Networks

SNAP

- Energies, forces, and stresses from DFT
- Bispectrum component descriptors
- Linear regression

SNAP Definition and Work Flow

Model Form

No image

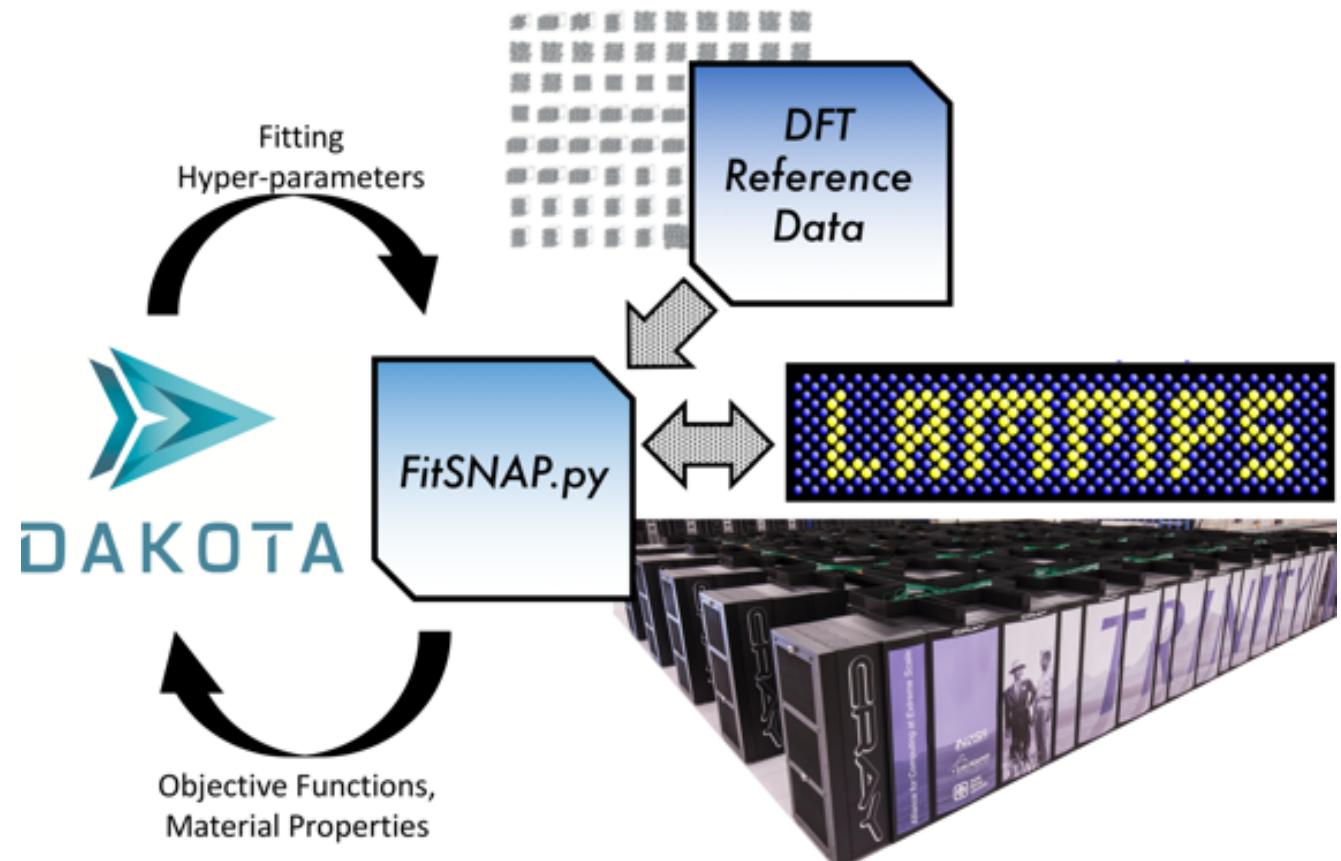
$$E_{SNAP}^i = \beta_0 + \sum_{k=1}^K \beta_k (B_k^i - B_{k0}^i)$$

Regression Method

- β vector fully describes a SNAP potential
- Decouples MD speed from training set size

$$\min(||\mathbf{w} \cdot D\beta - T||^2 - \gamma_n ||\beta||^n)$$

Weights Set of Descriptors DFT Training

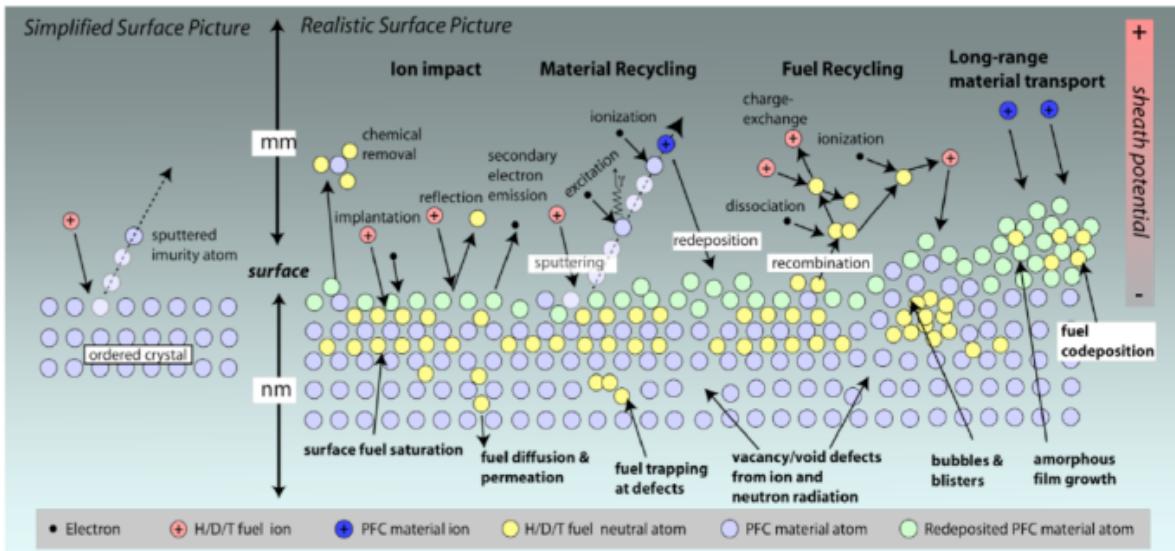


Code available: <https://github.com/FitSNAP/FitSNAP>

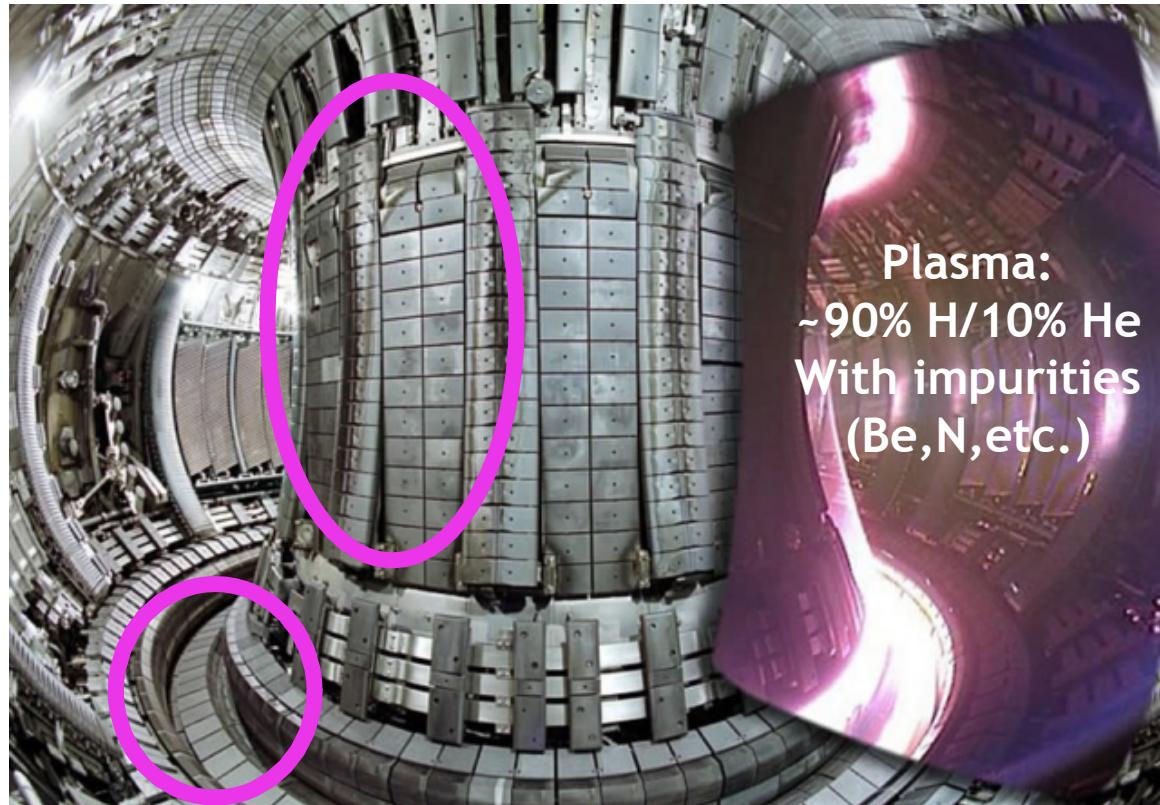
Materials for Fusion Energy



- Difficult to develop materials to handle extreme conditions within tokamak
- Large heat loads of $10\text{-}20 \text{ MW/m}^2$
- High particles fluxes of $\sim 10^{24} \text{ m}^{-2}\text{s}^{-1}$ of mixed ion species (H/He/Be/N etc.)



Beryllium First Wall



Tungsten Divertor

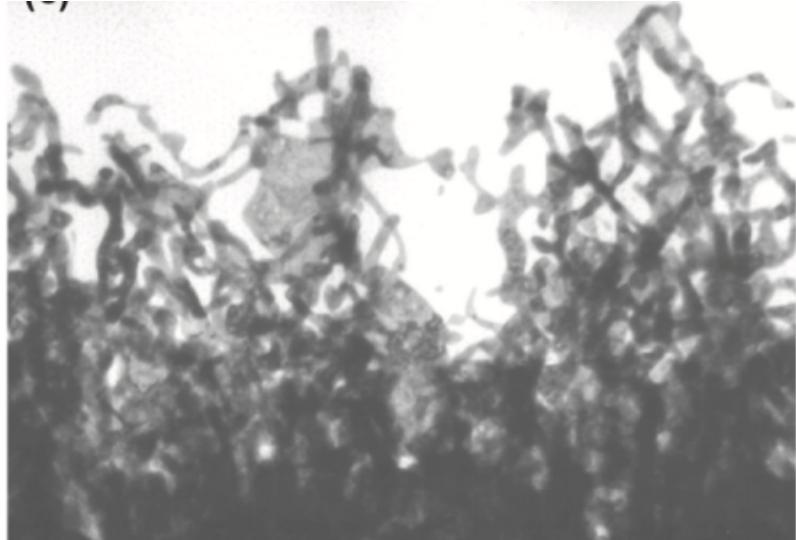
- Many complex processes that occur at the plasma/material interface that can lead to material degradation

Plasma Material Interactions in Tungsten

Tritium Retention



Helium Fuzz Growth



Kajita, et al. J. Nucl. Mater. 418, (2011) 152-158

Material Degredation

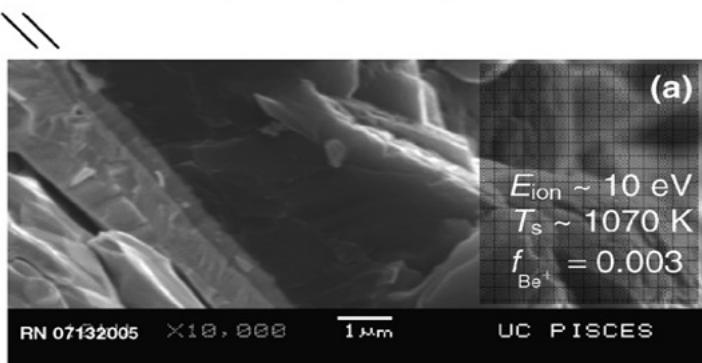


Kajita, et al. Nucl. Fus. 471, 886-890 (2007)

W-Be Intermetallics

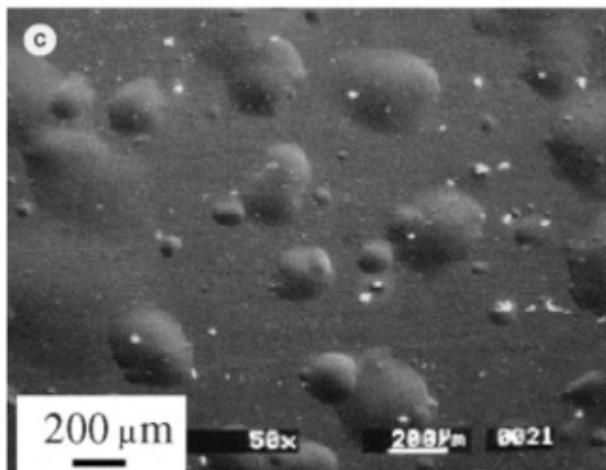
Be_{12}W

Be deposits (surface)



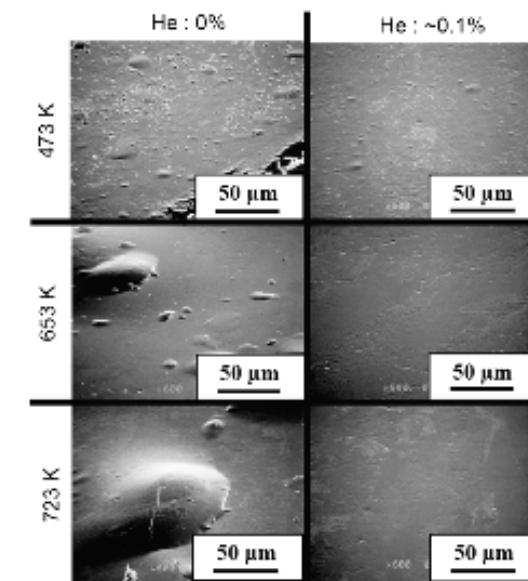
Baldwin, et. al. J. Nucl. Mater. 363-365 (2007) 1179-1183

Hydrogen Blisters



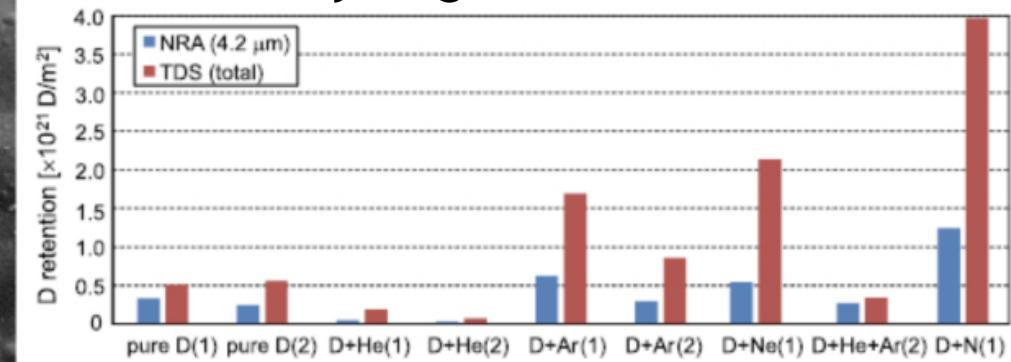
Ye, et al. J. Nucl. Mater. 313-316, 72-76 (2003)

Effect of He on H Blistering



Ueda, et. al. J. Nucl. Mater. 386-388 (2009) 725-728

Effect of Plasma Impurities on Hydrogen Retention



Kreter, et al. Nucl. Fus. 59, 086029 (2019)

7 Tungsten-Beryllium SNAP Fitting W-Be Intermetallic Formation Energies (eV)

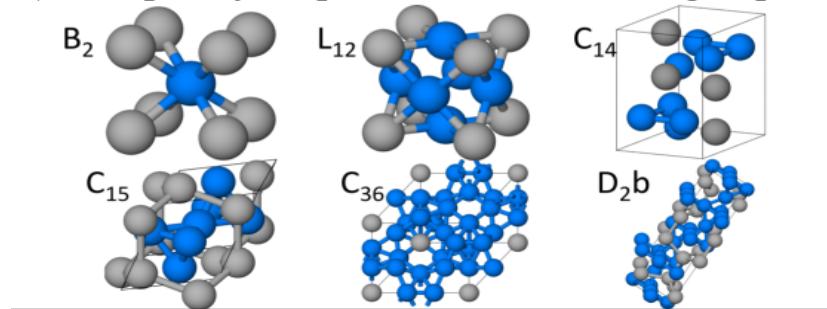
- Initially fit SNAP potential for pure elements
- Making a multi-element SNAP potential does sacrifice some accuracy from either pure component fit.
- Training set includes W-Be intermetallic

Description	N_E	N_F	σ_E	σ_F
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W-Be:

Elastic Deform [†]	3946	68040	$3 \cdot 10^5$	$2 \cdot 10^3$
Equation of State [†]	1113	39627	$2 \cdot 10^5$	$4 \cdot 10^4$
DFT-MD [†]	3360	497124	$7 \cdot 10^4$	$6 \cdot 10^2$
Surface Adhesion	381	112527	$2 \cdot 10^4$	$9 \cdot 10^4$

† Multiple crystal phases included in this group:

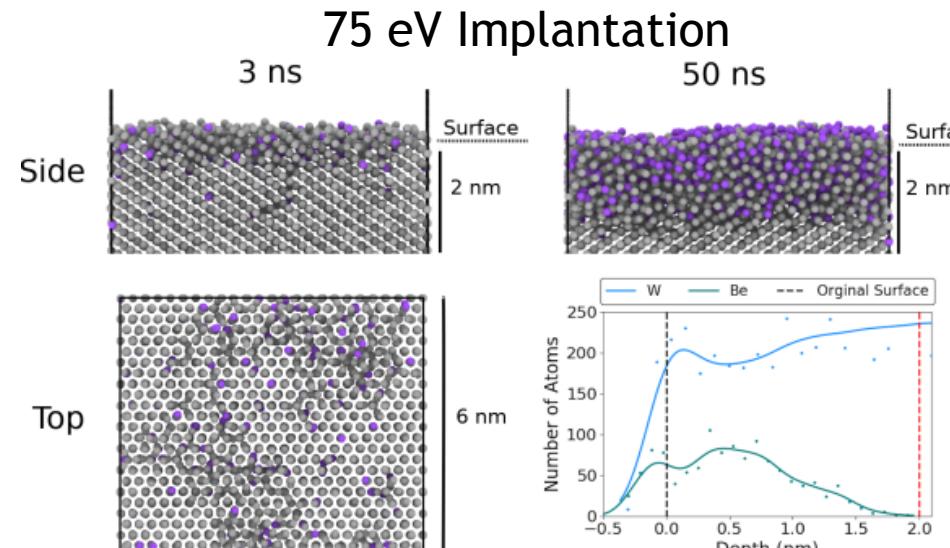


Phase	Composition	DFT ¹	SNAP ¹	BOP ²
B_2	WBe	0.67	0.30	-2.20
C_{14}	WBe ₂	-0.87	-1.27	-4.20
C_{15}	WBe ₂	-0.92	-1.15	-4.19
C_{16}	WBe ₂	-0.90	-1.22	-4.20
L_{12}	WBe ₃	-0.51	-0.15	-4.58
D_2B	WBe ₁₂	-0.96	-0.34	-6.69

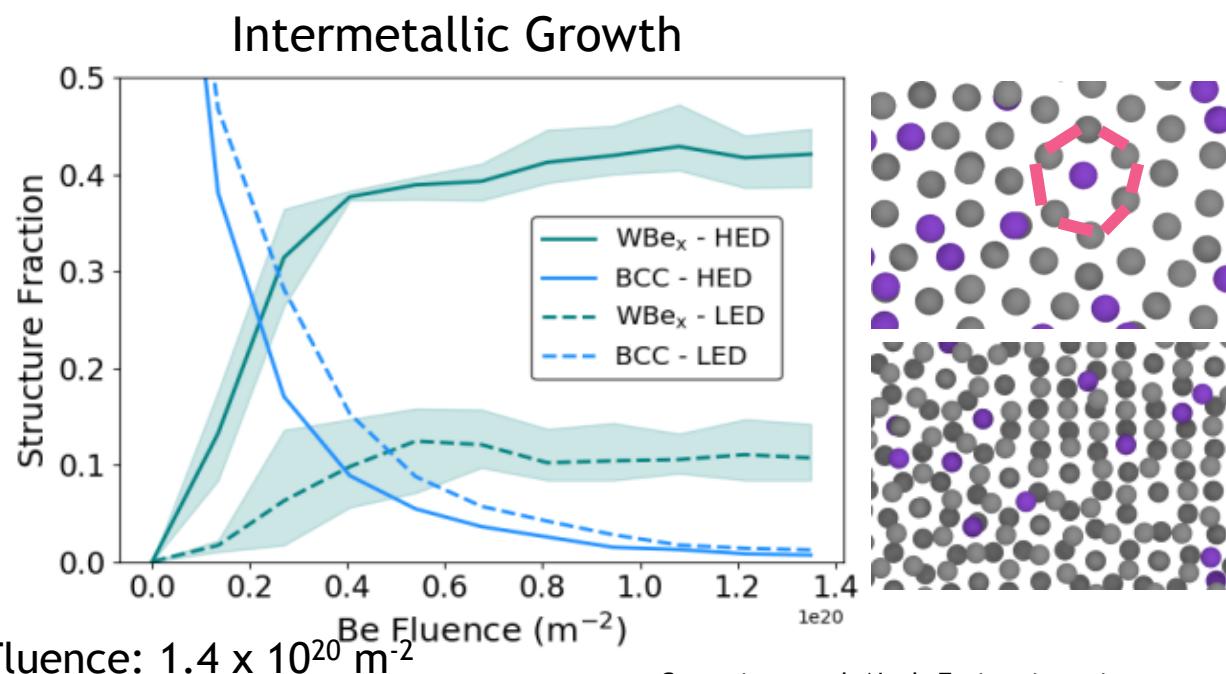
Be Defect Formation Energies in W (eV)

	DFT ¹	SNAP ¹	BOP ²
[111] Dumbbell	4.30	3.66	0.67
Substitution	3.11	3.29	-2.00
Surface Hollow Site	-1.05	-1.39	-3.52
Tetrahedral	4.13	4.20	-0.28
[110] Dumbbell	4.86	4.29	-0.03
Octahedral	3.0	5.11	0.34
Surface Bridge Site	1.01	0.44	-1.30

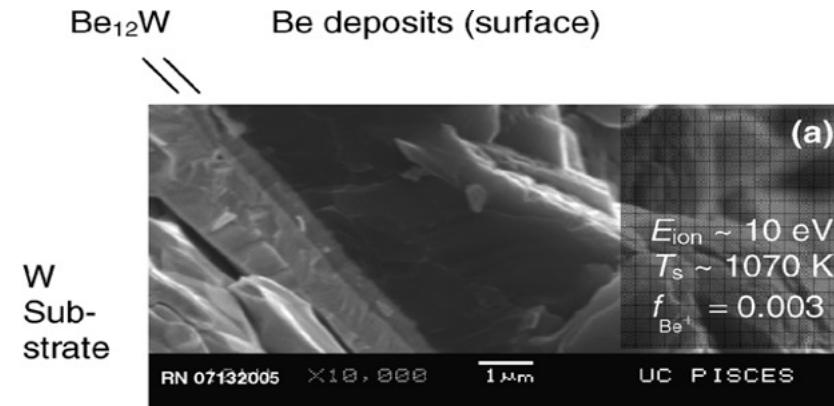
Beryllium Deposition Results in Near Surface Mixed Layer



- High energy (75 eV) and low energy (0 eV) beryllium deposition on tungsten surfaces
- Formation of disordered mixed materials layer in first 2 nm of surface
- Some intermetallic growth observed within mixed materials layer
- However, mixed materials layer appears to be kinetically trapped at MD time scales



Experimentally Observed W-Be Intermetallics

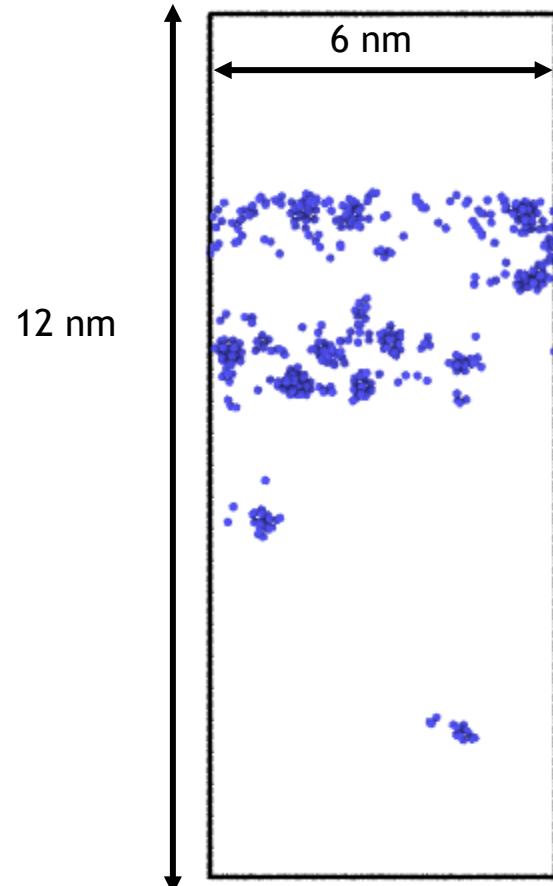
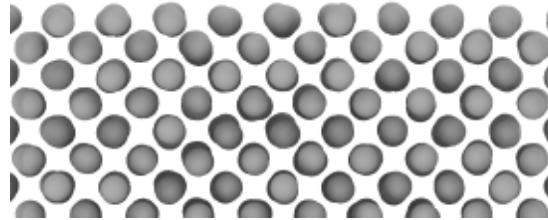


Be Disrupts Helium Diffusion and Bubble Growth in W

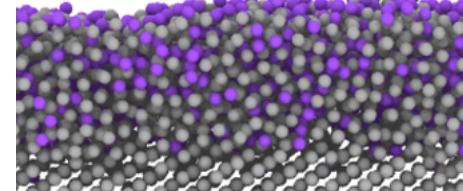


Increasing Time

Crystalline W

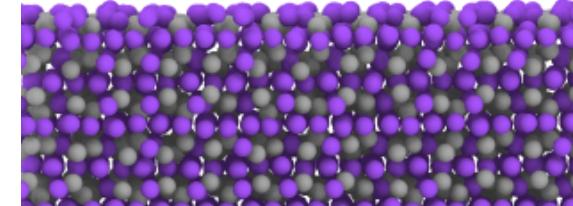


Amorphous W-Be



Blue: He
Purple: Be
Gray: W

WBe₂ C14 Structure



Laves/Deposited Layer:
Smaller He clusters mostly located near the surface

Extending SNAP for W-H and W-N



Pure H or N Data

- Dimer and Trimer binding curve
- Molecular binding curves
- Random configurations of molecules at varying densities
- DFT-MD

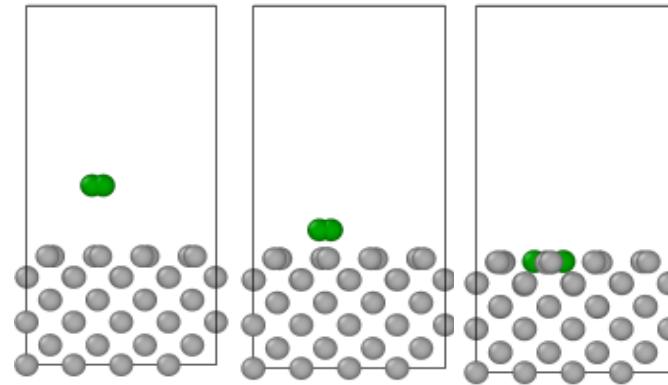
W-H Data

- H and H_2 adsorption on W surface
- H defects in bulk tungsten
- Sheared/Strained configurations of H defects in bulk W

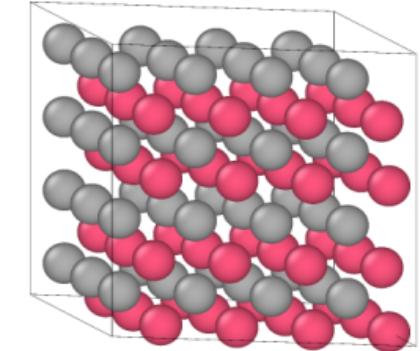
W-N Data

- N adsorption and surface diffusion on (100), (110), (111) surfaces
- N_2 dissociation on (100), (110), (111) surfaces
- NEB of N into bulk W for (100) and (110) surface
- N defects in bulk W
- W_xN_x bulk structures
- W_xN_x sheared/strained structures

H_2 Adsorption



WN NiAs Structure



Objective Functions

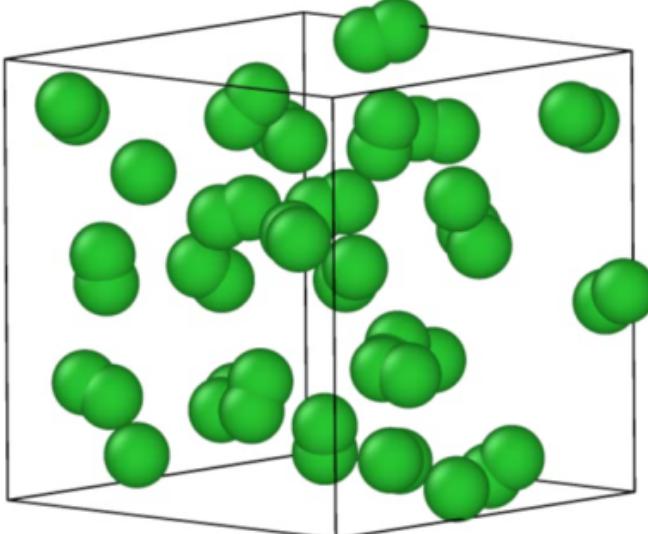
- Energy/force errors on training data
- W or W_xN_x cohesive energies
- W and W-H or W-N defect formation energies
- H/N dimer and trimer binding energies
- H/N atom and molecular surface binding energies

Challenges in Developing W-H and W-N SNAP Potentials

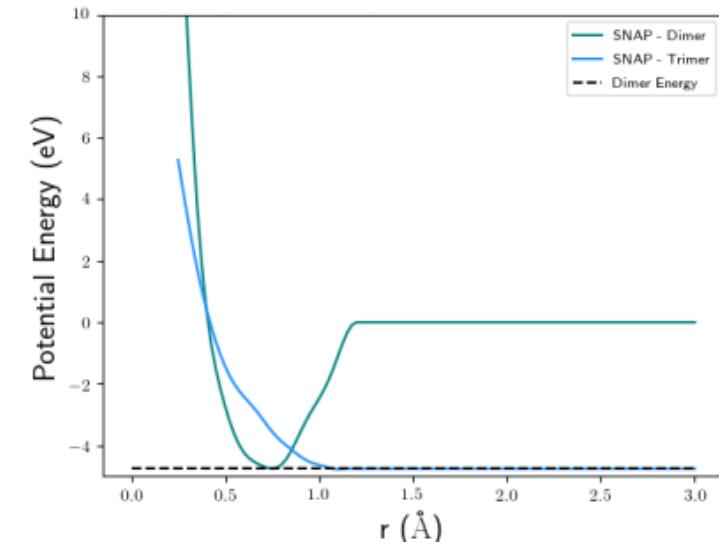


- Have never used SNAP for gaseous species before
- Hydrogen and nitrogen raining data is also more sparse compared to crystalline structures i.e. tungsten
- Difficult resides in how to get correct gas behavior (like forming dimers but not trimers) without inherent physics built-in to potential form

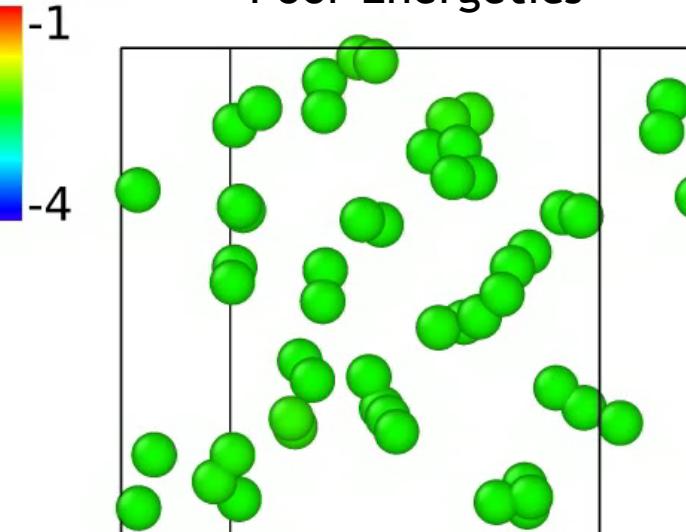
Poor Clustering Behavior



Hydrogen Binding Curves



c_peatom Poor Energetics



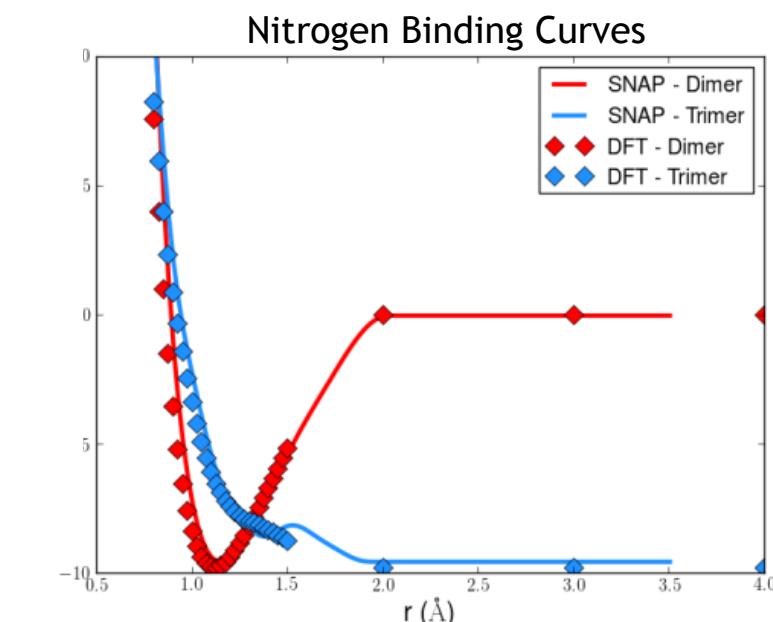
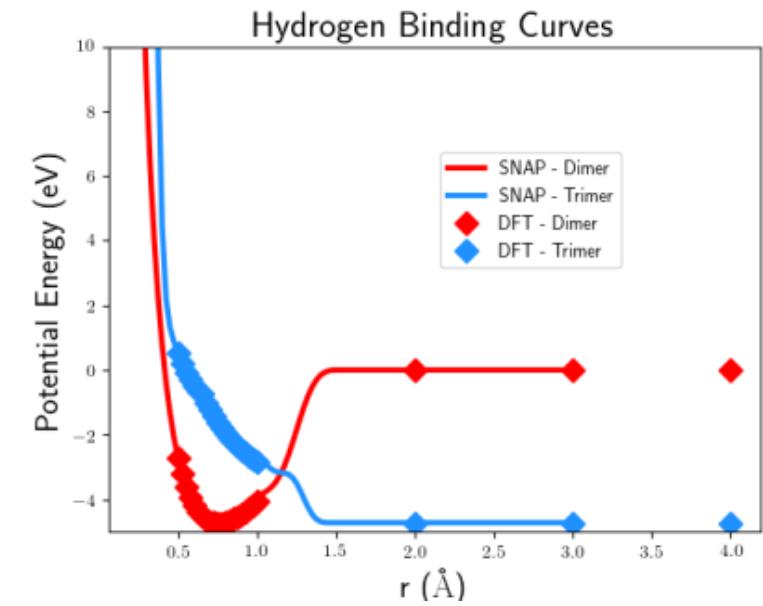
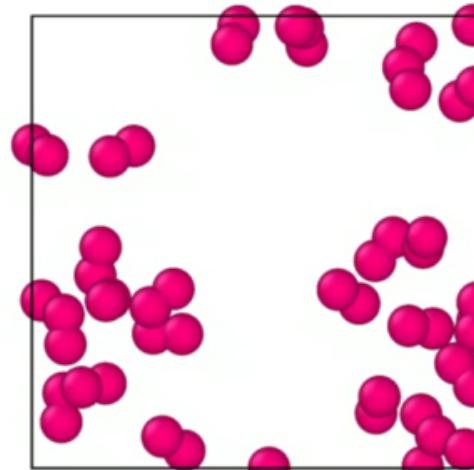
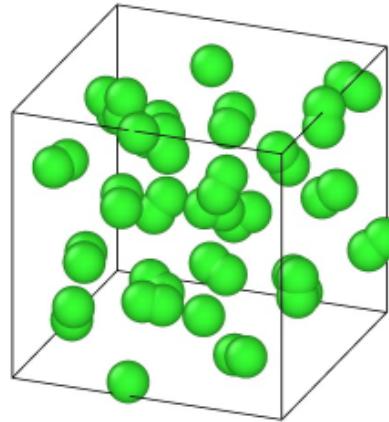
Movie colored by PE/atom

- Green is nominal H₂ energy
- Reproduces correct binding curves

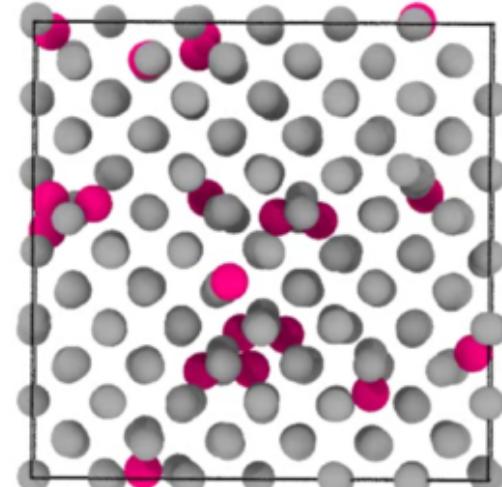
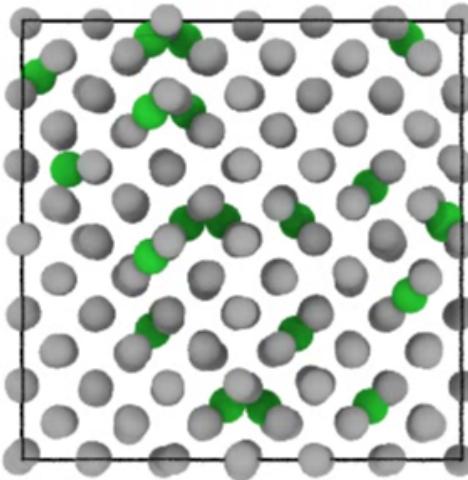
Changes to Fitting Results in Better Hydrogen and Nitrogen Potentials



- Modifications to fitting workflow yielded better results in reproducing correct gas species behavior
- Adjustments included:
 - Only including training data near potential energy well
 - Making radial cutoff much shorter (1.5 Å for H and 2.0 Å for N)
 - Adding extra objective function for dynamics behavior
 - Adjusted ZBL cutoff
 - Adjusted objective function for binding curves



Preliminary Results for W-H and W-N SNAP Bulk Properties



W_xN_x Cohesive Energies

	DFT	SNAP
P62mmc (WN_2) (eV)	-1.84	-2.64
P6m2 (WN_2) (eV)	-0.92	-2.63
NiAs (WN) (eV)	-0.83	-1.35
WC (WN) (eV)	-0.24	-1.00
$MoSi_2$ (W_2N) (eV)	-0.07	-0.06

W-H Bulk Properties

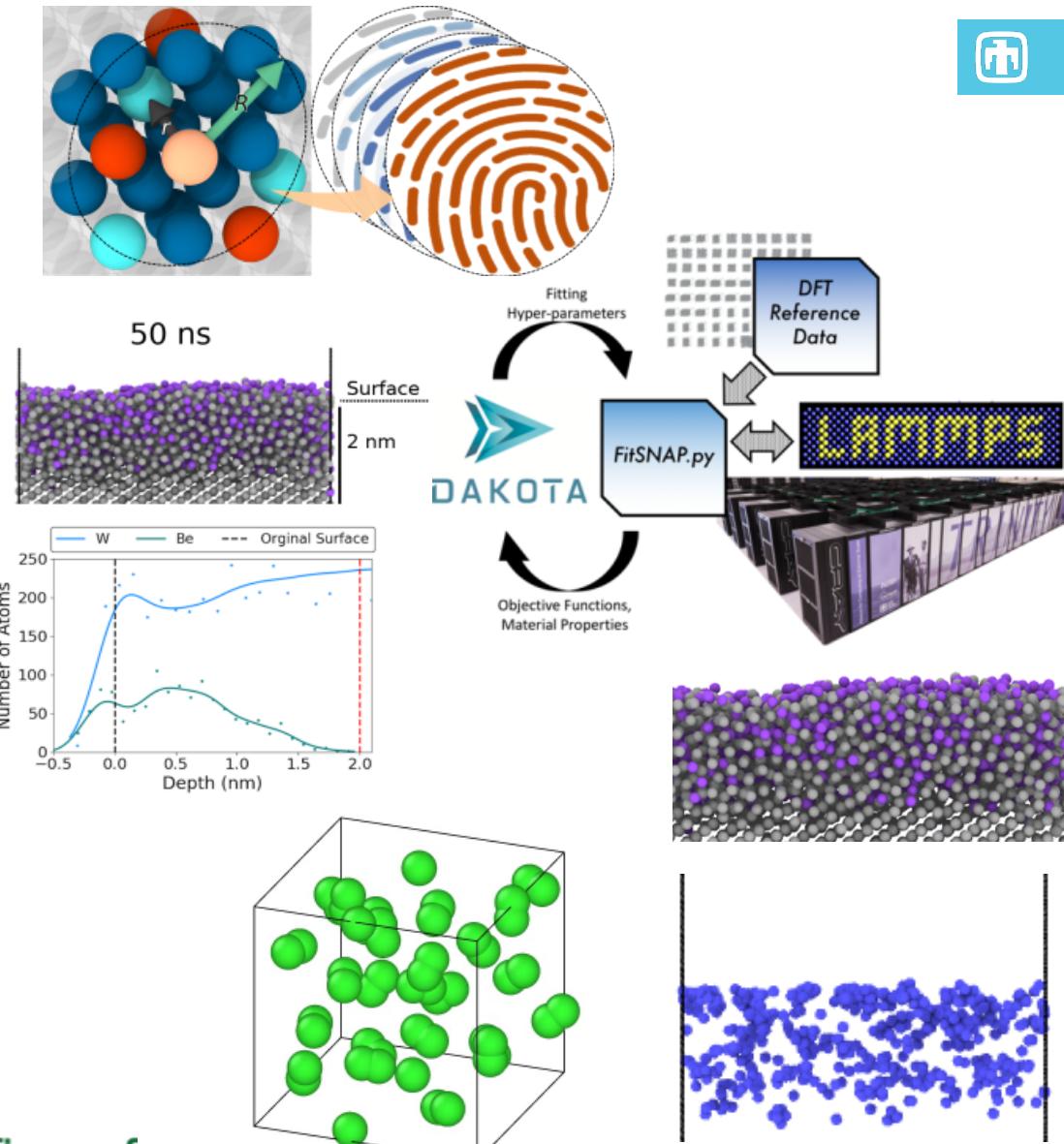
	DFT	SNAP
E_f^{H2} (eV)	-4.75	-4.74
E_f^{Tet} (eV)	0.88	0.85
E_f^{Oct} (eV)	1.26	1.17
E_f^{Sub} (eV)	4.08	4.25
E_f^V (eV)	3.27	3.30

W-N Bulk Properties

	DFT	SNAP
E_f^{H2} (eV)	-9.79	-9.71
E_f^{Tet} (eV)	1.26	1.45
E_f^{Oct} (eV)	0.53	0.56
E_f^{Sub} (eV)	4.15	1.23
E_f^V (eV)	3.27	2.95

Summary

- SNAP is a versatile ML interatomic potential that has been applied to a variety of materials including materials for fusion energy
- A W-Be SNAP potential has been developed and used to study Be implantation in W and extended to simulation He implantation W-Be materials
- The current SNAP potential is being extended for W-H and W-N and SNAP can reproduce gas species behavior both in vacuum and in metals
- Future work entails the development of one W-Be-H-He-N potential for studying fusion energy materials



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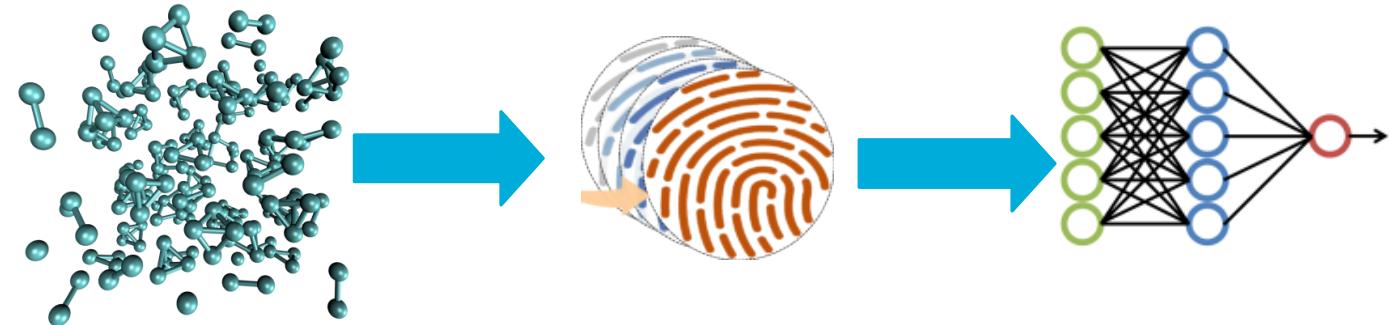
Variations of SNAP



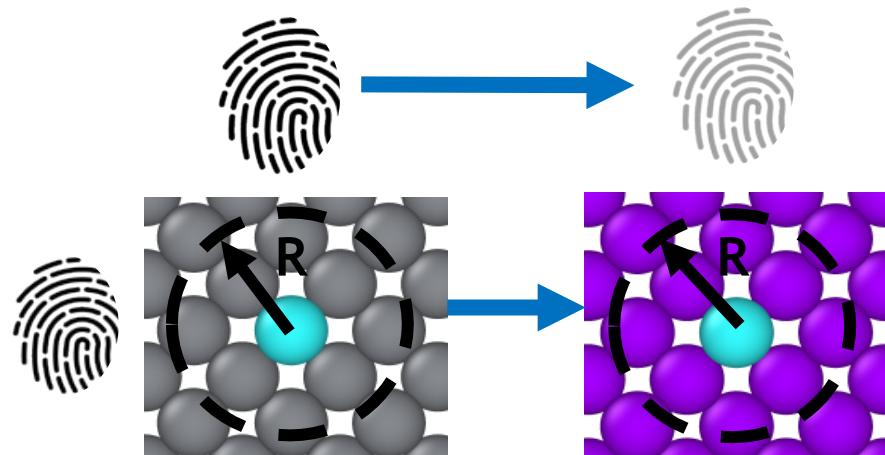
Quadratic SNAP

$$E_{SNAP}^i = \beta \cdot \mathbf{B}^i + \frac{1}{2}(\mathbf{B}^i)^T \cdot \alpha \cdot \mathbf{B}^i$$

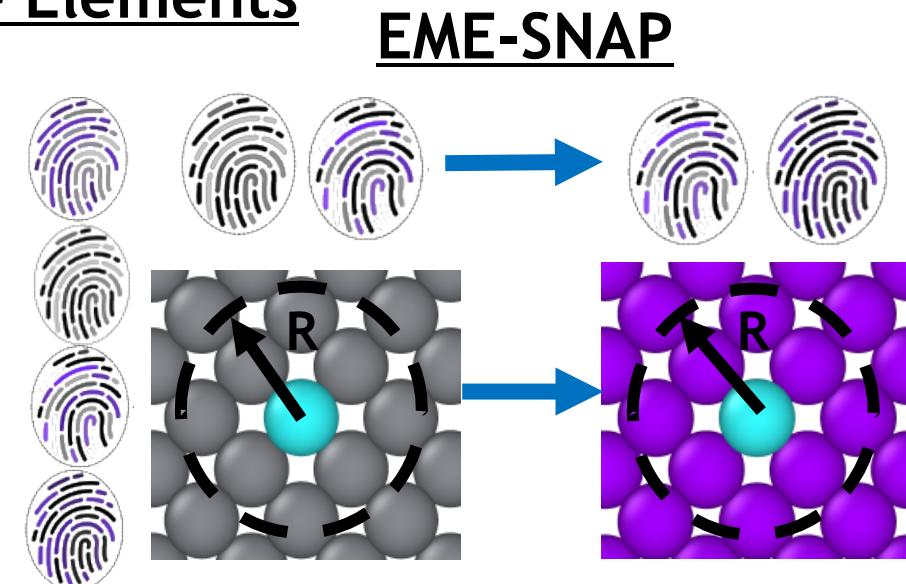
- Linear terms are 4-body
- Quadratic terms are 7-body
- Number of linear coefficients grows as $O(J^3)$
- Number of quadratic coefficients grows as $= O(J^6)$



WD-SNAP



SNAP for Multiple Elements



EME-SNAP