

ACCELERATING

SAND2021-0926C

PHASE-FIELD BASED PREDICTIONS

VIA

SURROGATE MODELS

TRAINED BY

MACHINE LEARNING METHODS

PRESENTED BY

RÉMI DINGREVILLE
(rdingre@sandia.gov)

New Mexico Machine Learning Symposium

40,000 FASTER...



3 mins



0.5 s

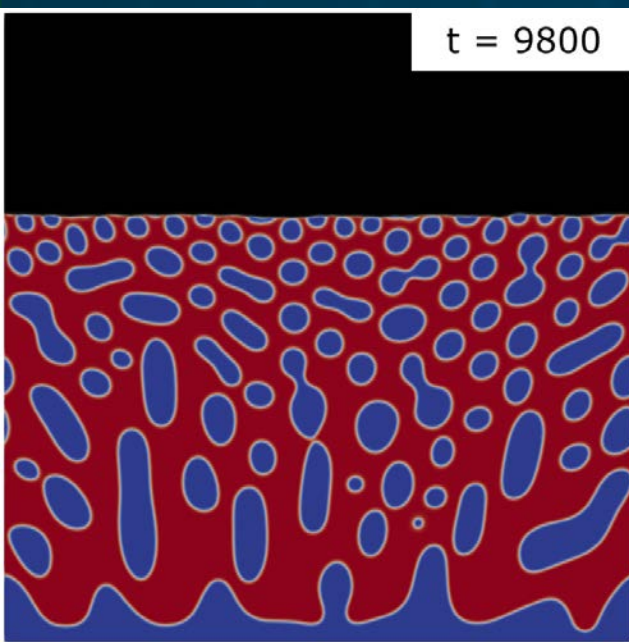


50 mins

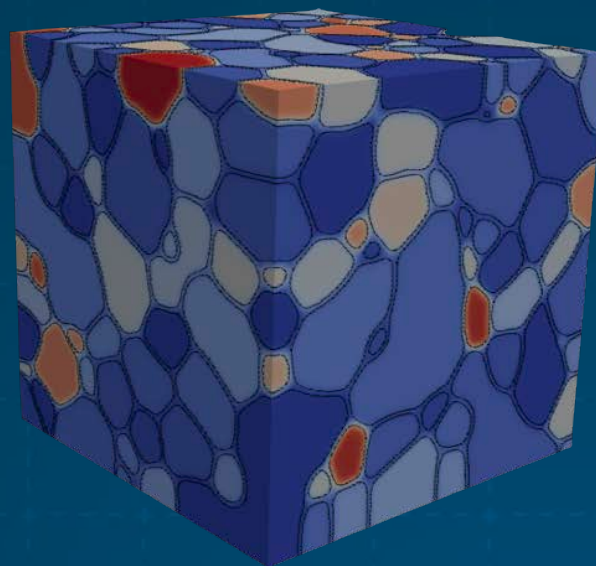
PREDICTING THE EVOLUTION OF MICROSTRUCTURES



Thin-film deposition



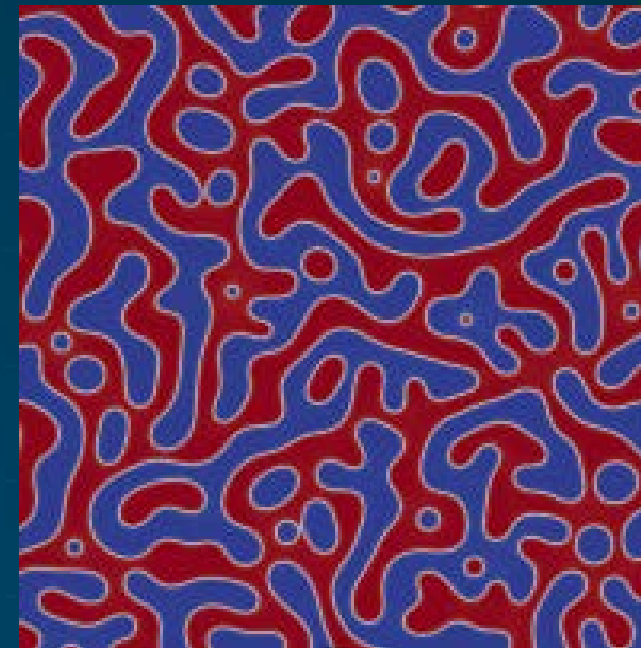
Grain growth



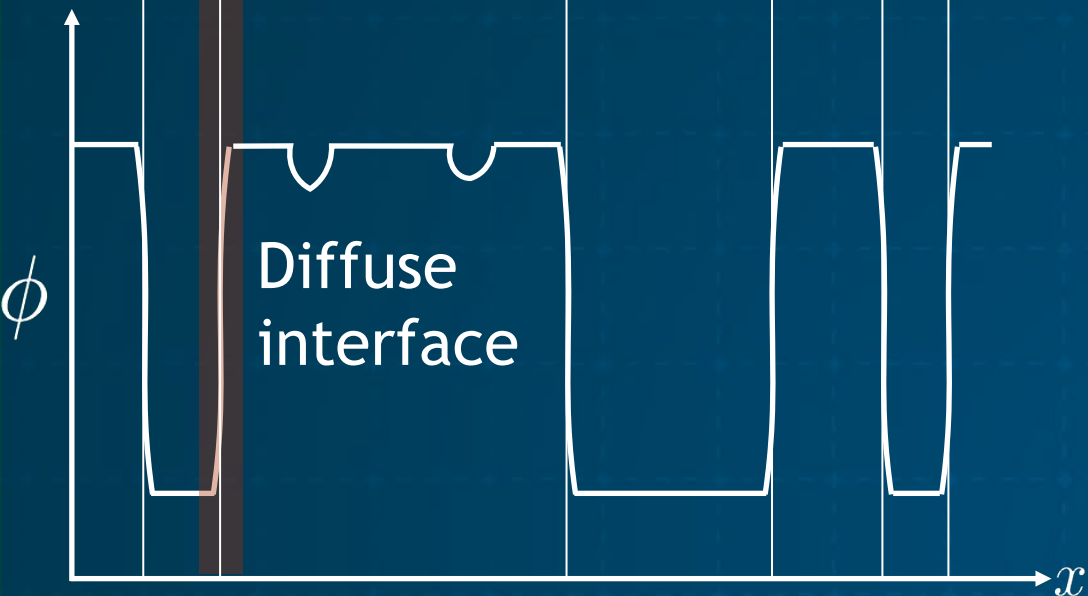
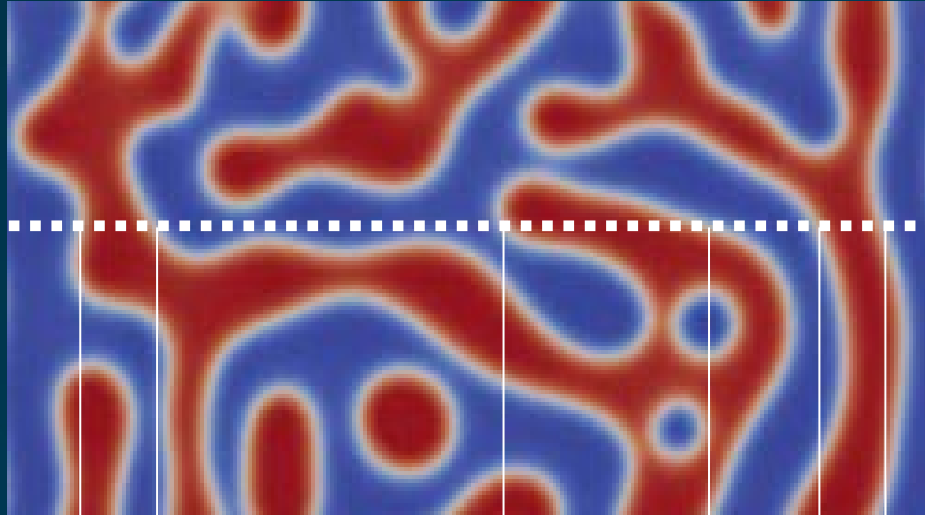
Solidification



Phase separation



PHASE FIELD I01



$$F = \int \left[f(\eta_1, \dots, \eta_p, c_1, \dots, c_p) + \sum_{i=1}^n \alpha_i (\nabla c_i)^2 + \sum_{i,j=1}^3 \sum_{k=1}^p \beta_{ij} \nabla_i \eta_k \nabla_j \eta_k \right] d\Omega$$

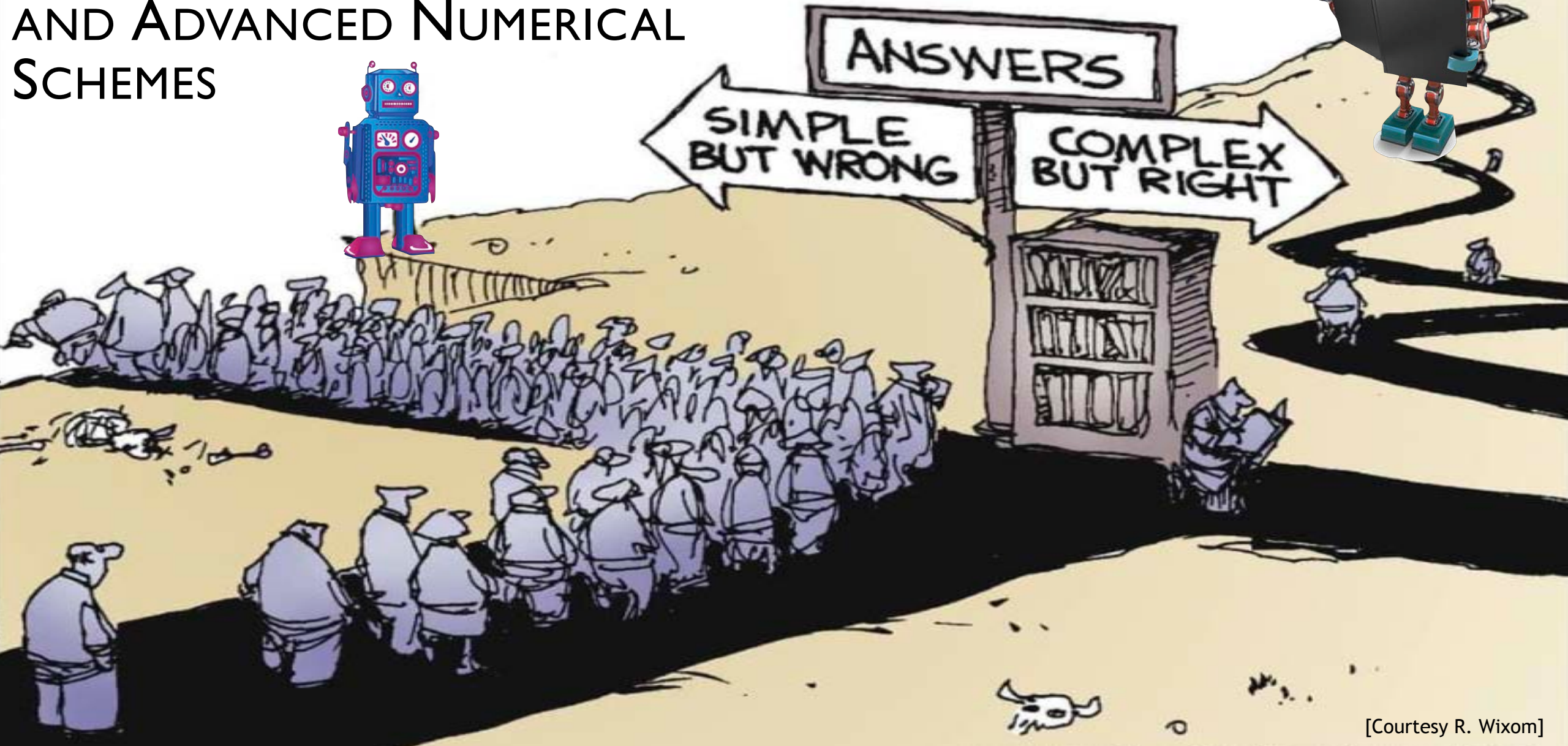
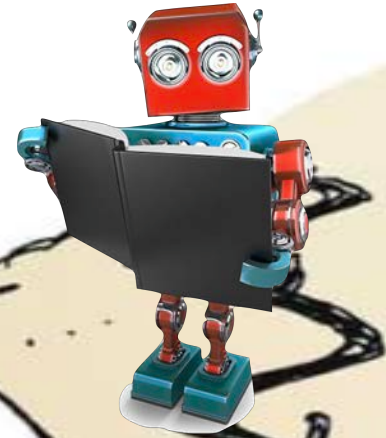
Allen-Cahn:
Non-conserved

$$\frac{\partial \eta_p}{\partial t} = -M_{pq} \frac{\delta F}{\delta \eta_q}$$

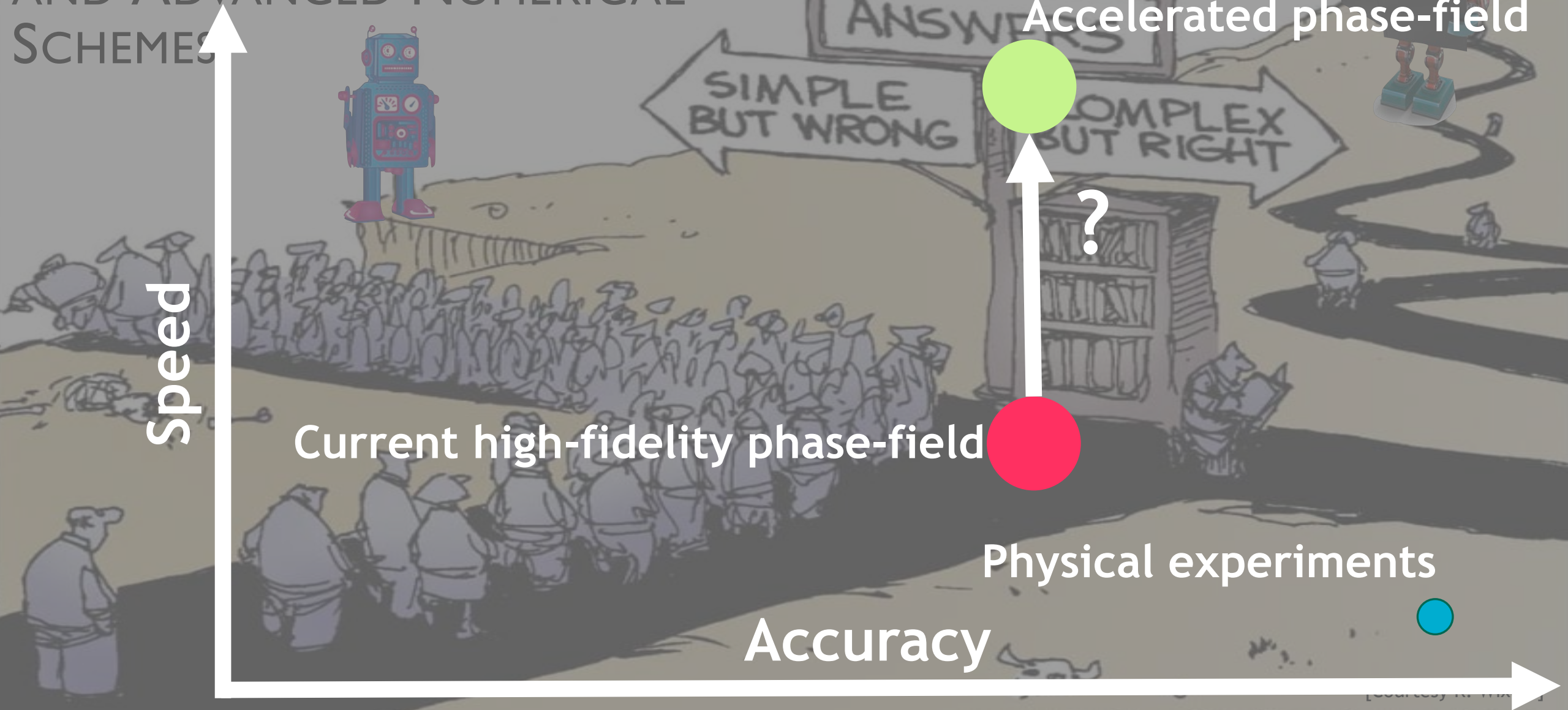
Cahn-Hilliard:
Conserved

$$\frac{\partial c_i}{\partial t} = \nabla \cdot \left(M_{ij} \nabla \frac{\delta F}{\delta c_j} \right)$$

CURRENT EFFORTS FOCUS ON LEVERAGING HIGH-PERFORMANCE COMPUTING ARCHITECTURES AND ADVANCED NUMERICAL SCHEMES



CURRENT EFFORTS FOCUS ON LEVERAGING
HIGH-PERFORMANCE COMPUTING ARCHITECTURES
AND ADVANCED NUMERICAL
SCHEMES

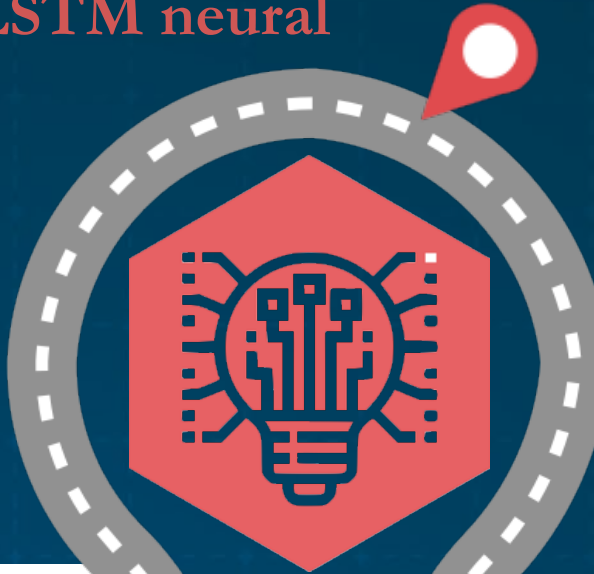


REFRAMING THE MICROSTRUCTURE EVOLUTION AS A MULTIVARIATE TIME-SERIES PROBLEM

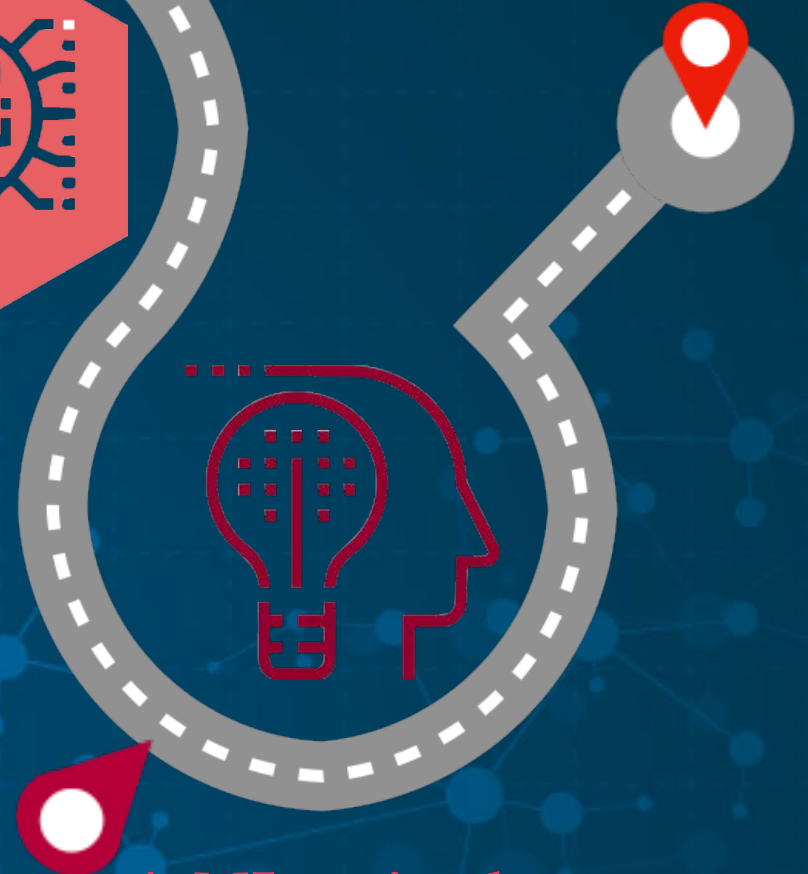
1. Data preparation



3. LSTM neural



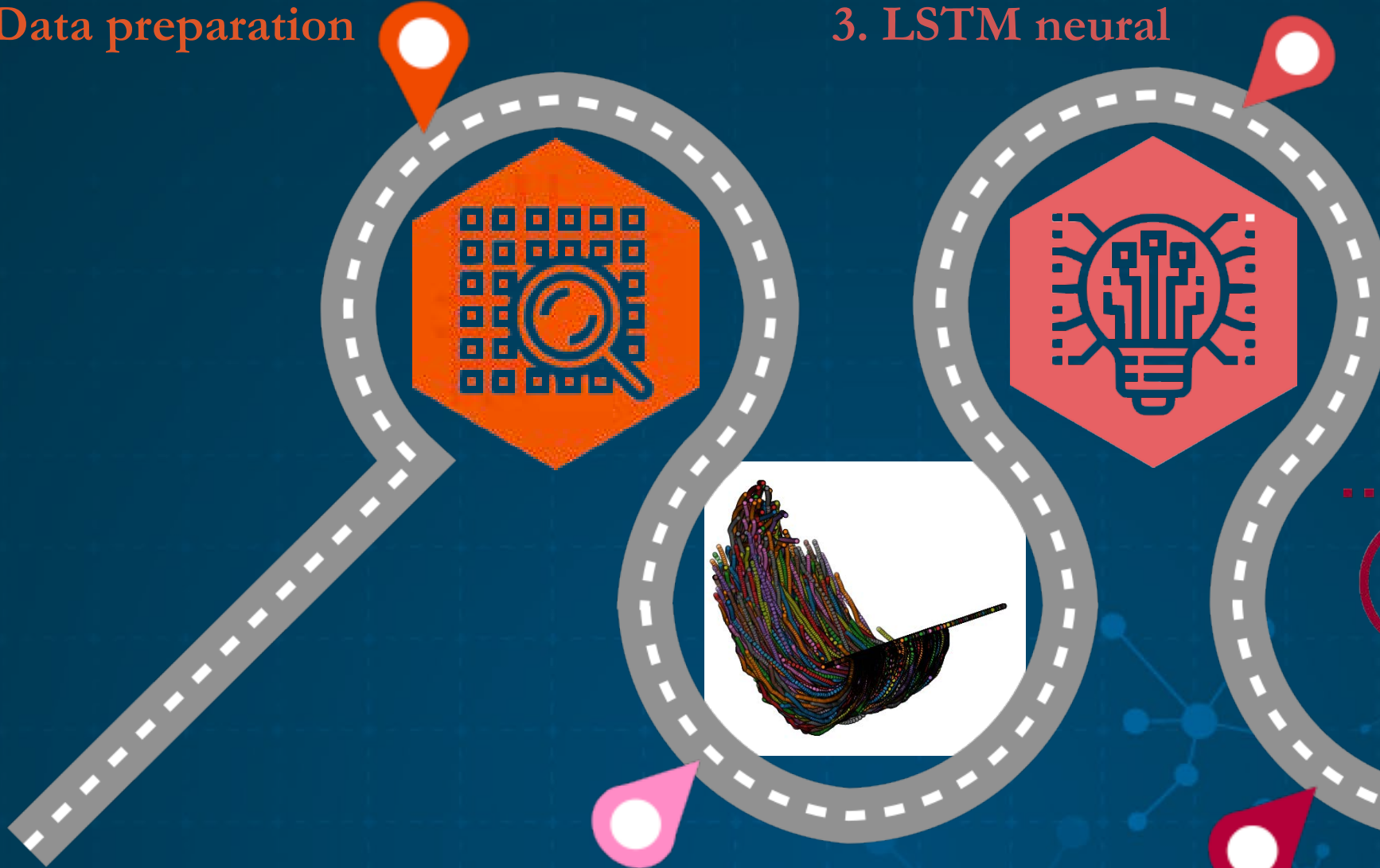
5. Accelerated PF



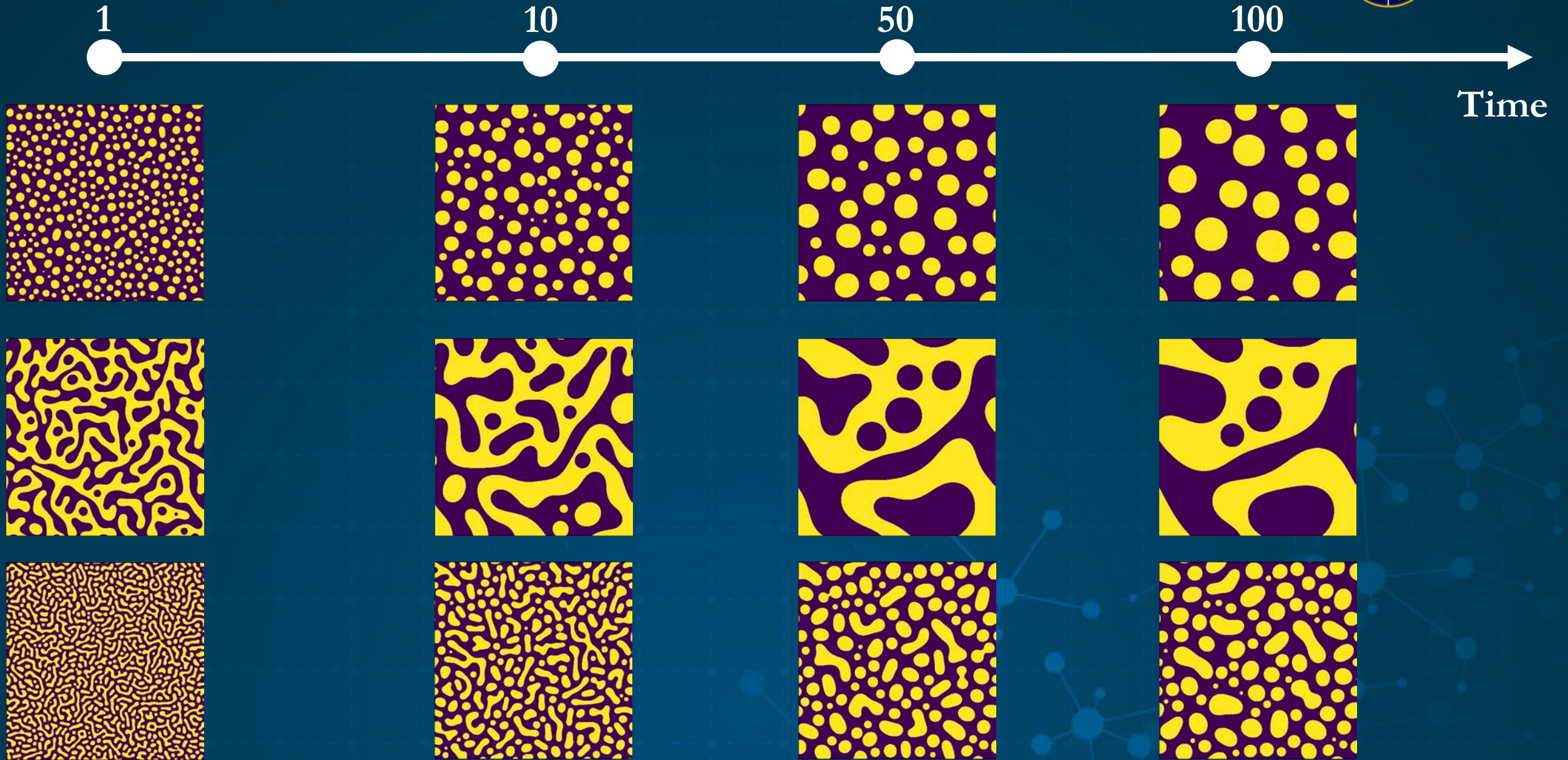
2. Low-Dimensional representation



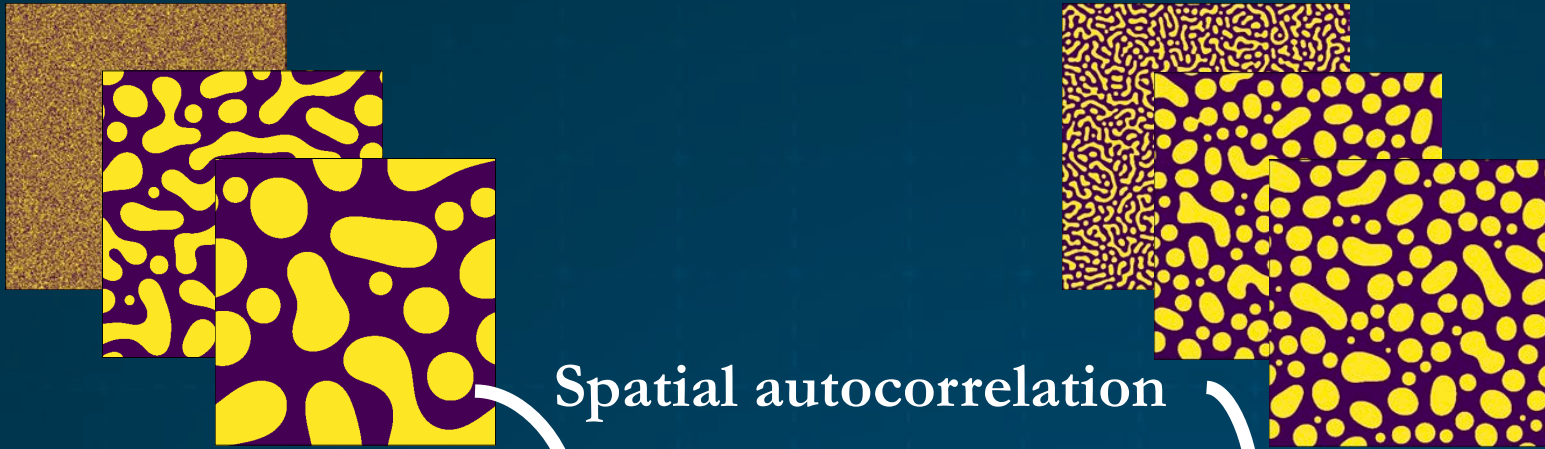
4. ML-trained surrogate



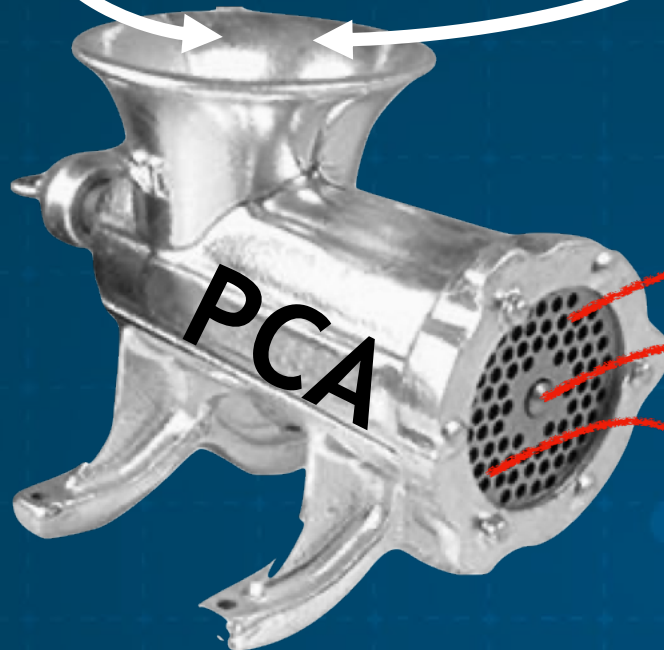
STEP I: DATA, DATA, AND MORE DATA



STEP 2: DIMENSIONALITY REDUCTION

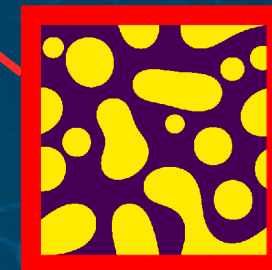
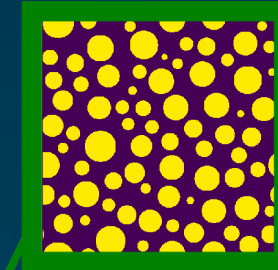
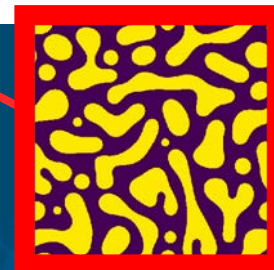
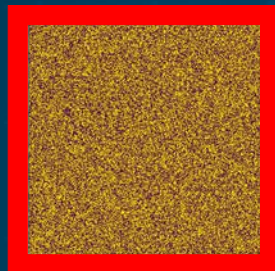
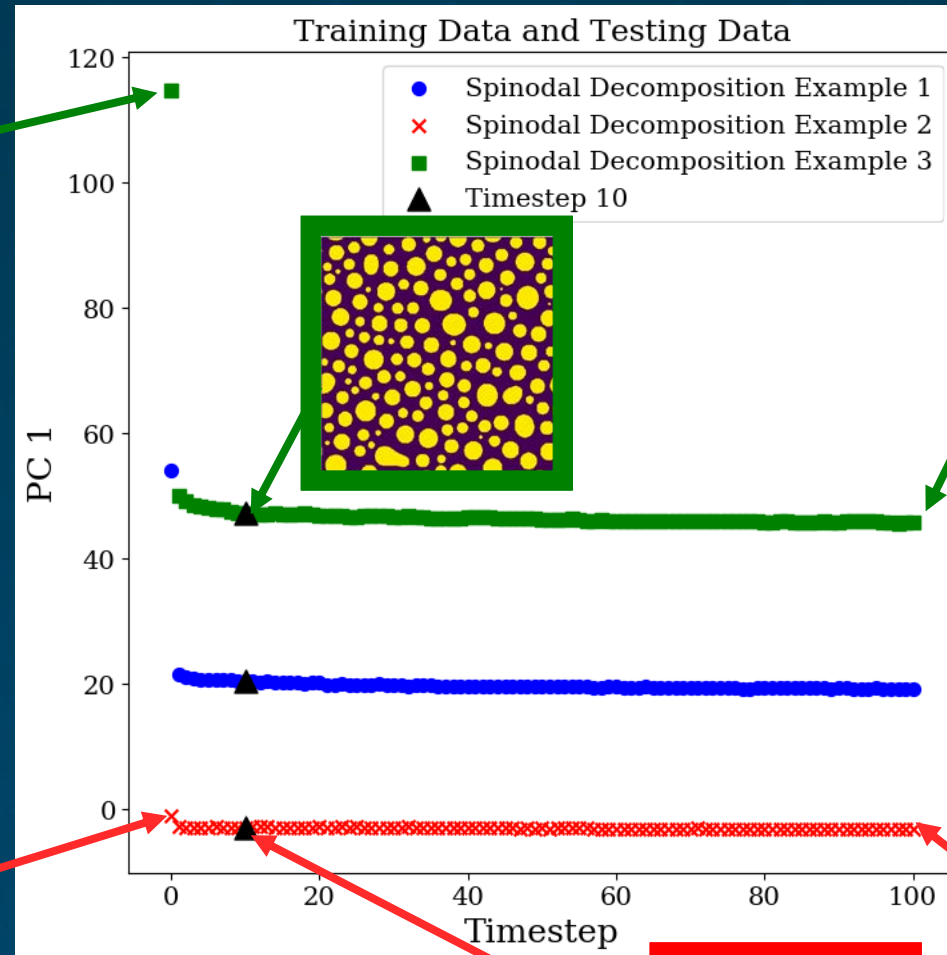
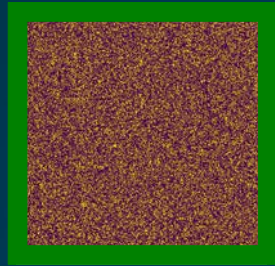


Spatial autocorrelation



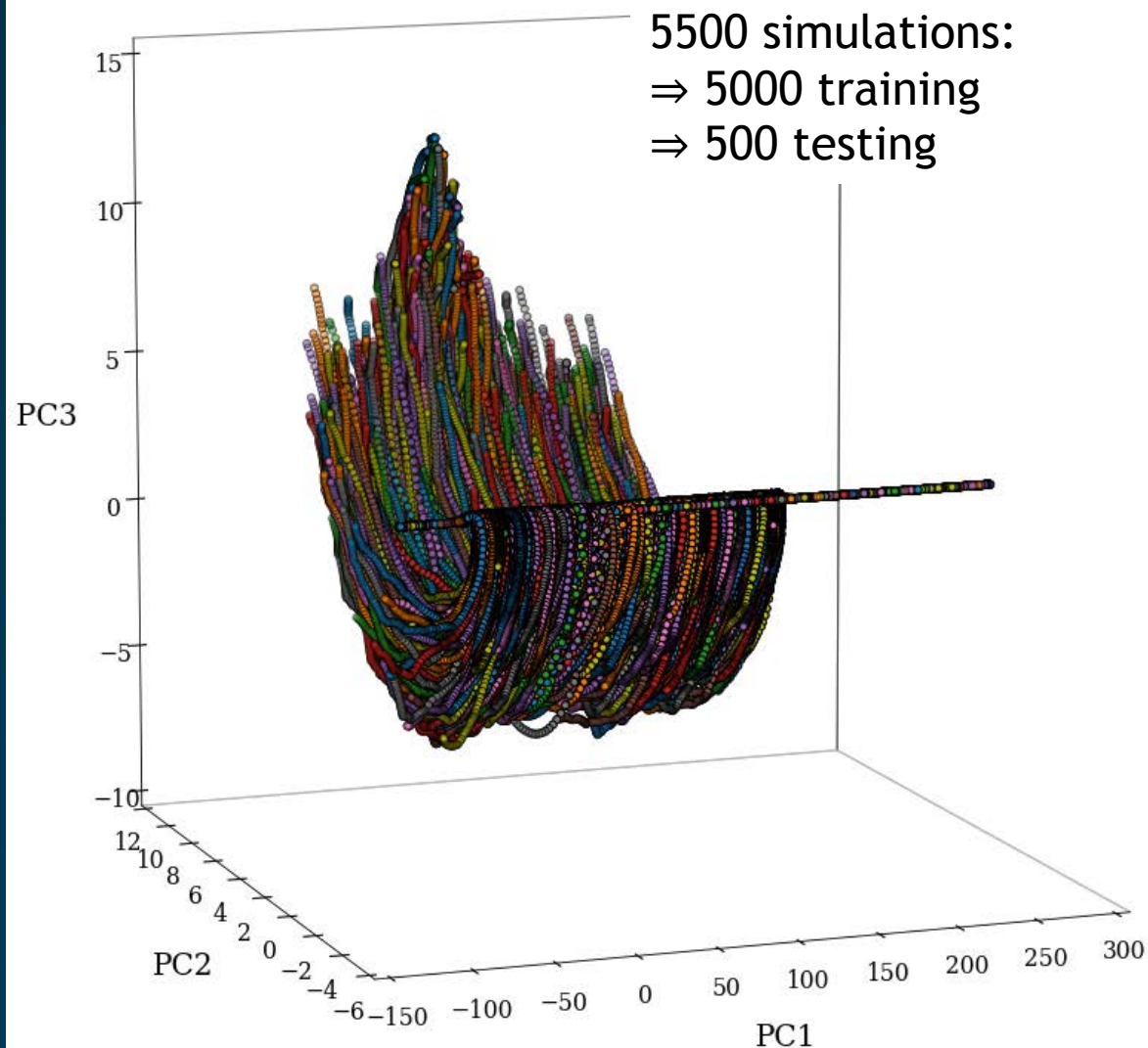
$$\mathbf{s}_{\text{pca}}^{(k)} = \sum_{j=1}^Q \alpha_j^{(k)}(t_i) \varphi_j + \bar{\mathbf{S}}$$

MICROSTRUCTURE TRAJECTORY IN REDUCED SPACE

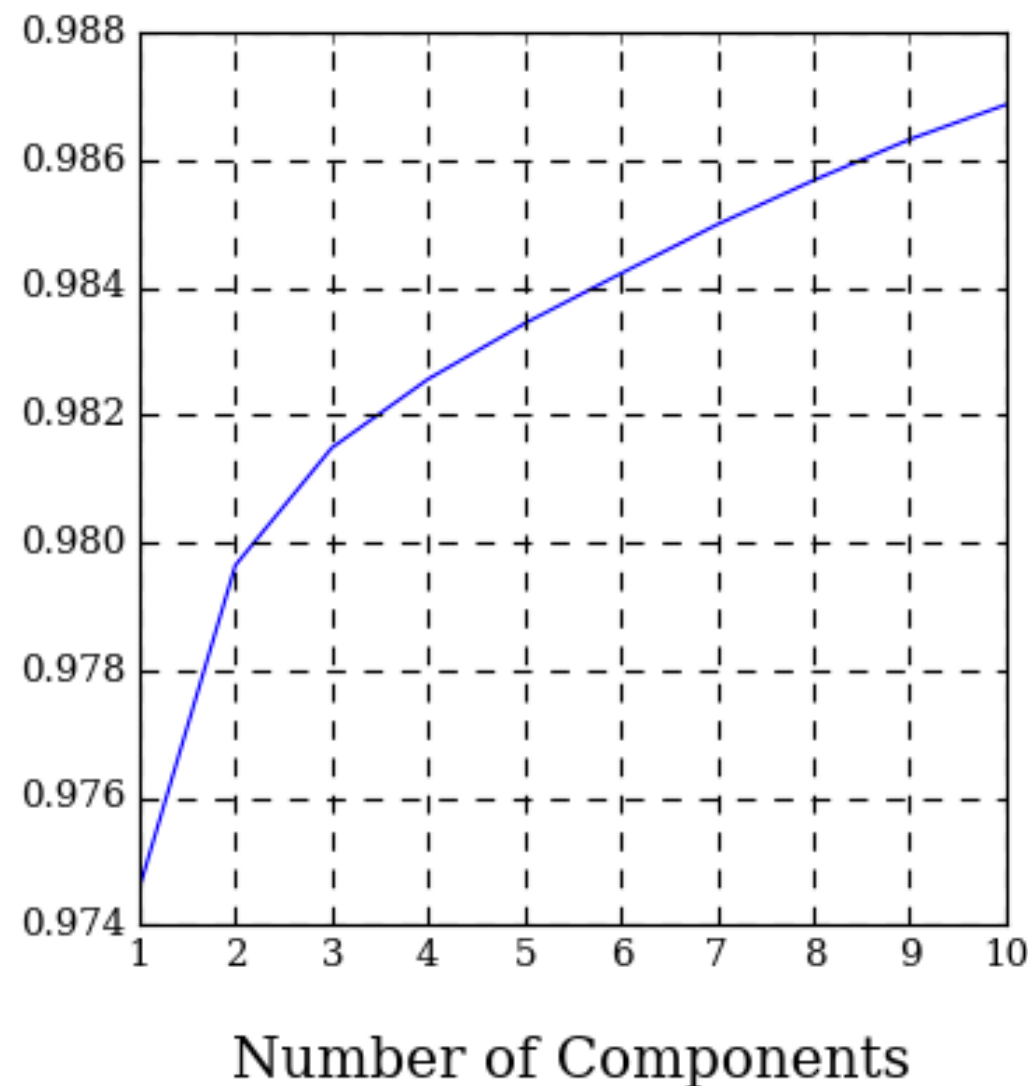


MICROSTRUCTURE TRAJECTORY IN REDUCED SPACE

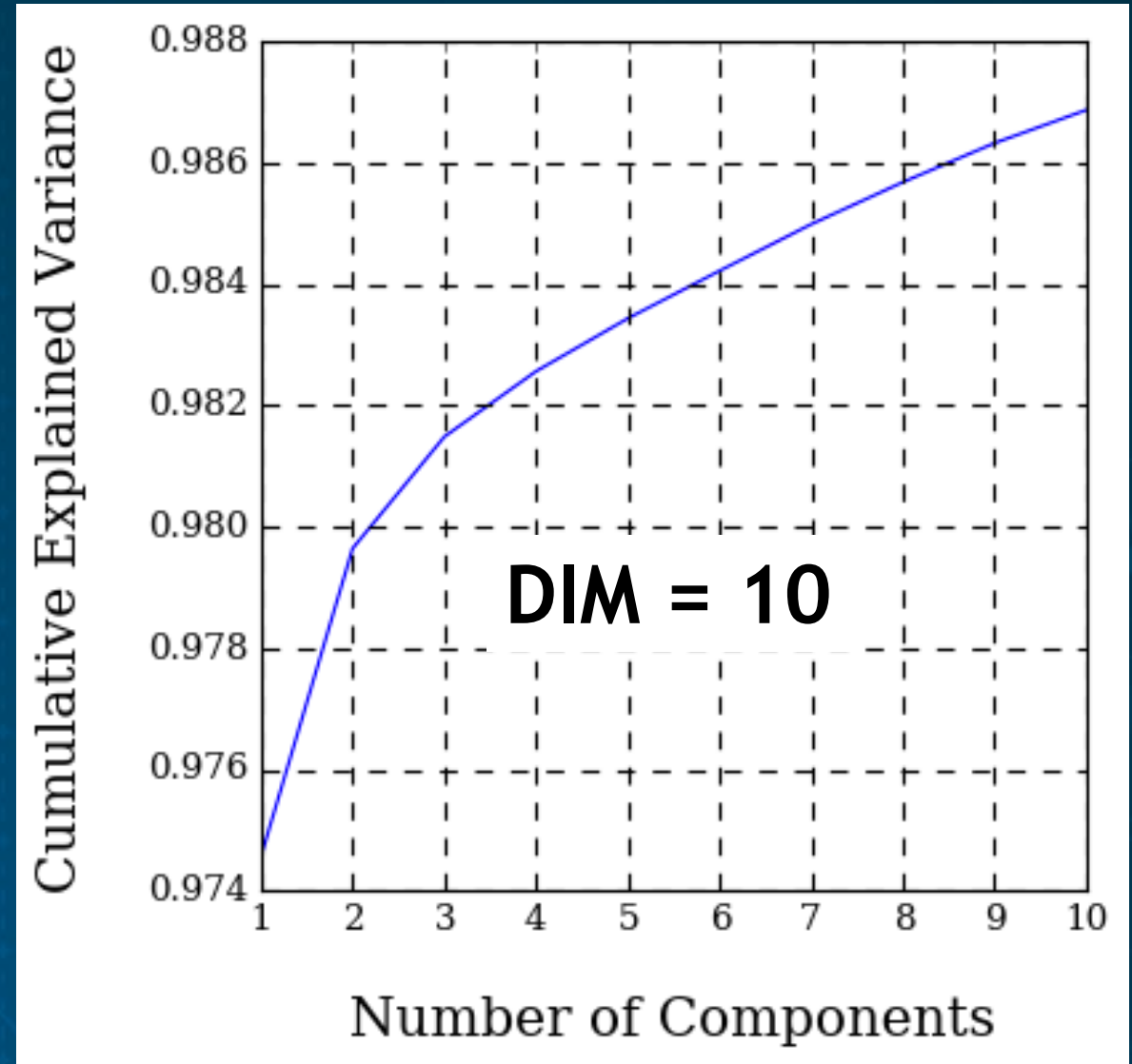
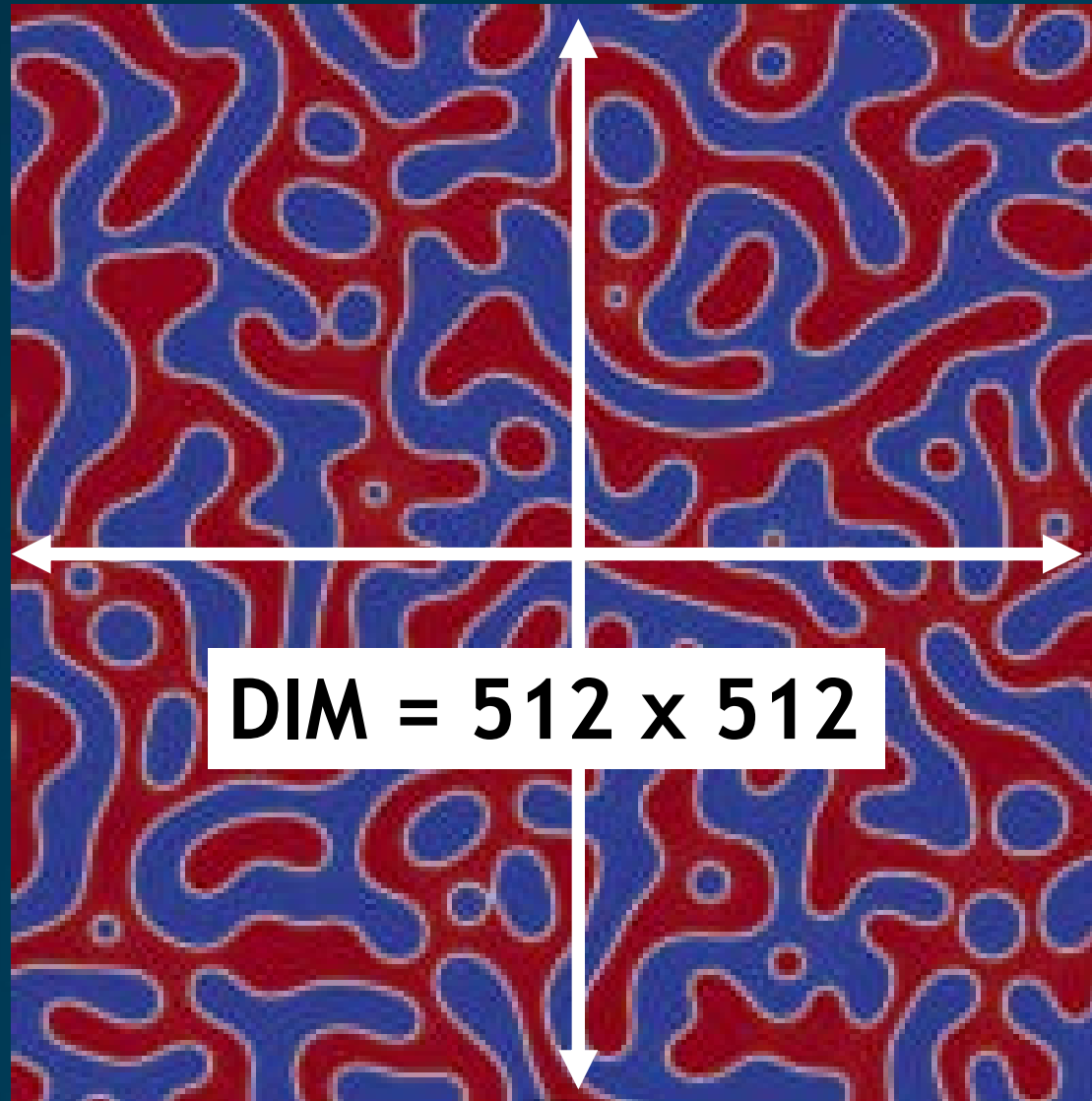
5500 simulations:
⇒ 5000 training
⇒ 500 testing



Cumulative Explained Variance

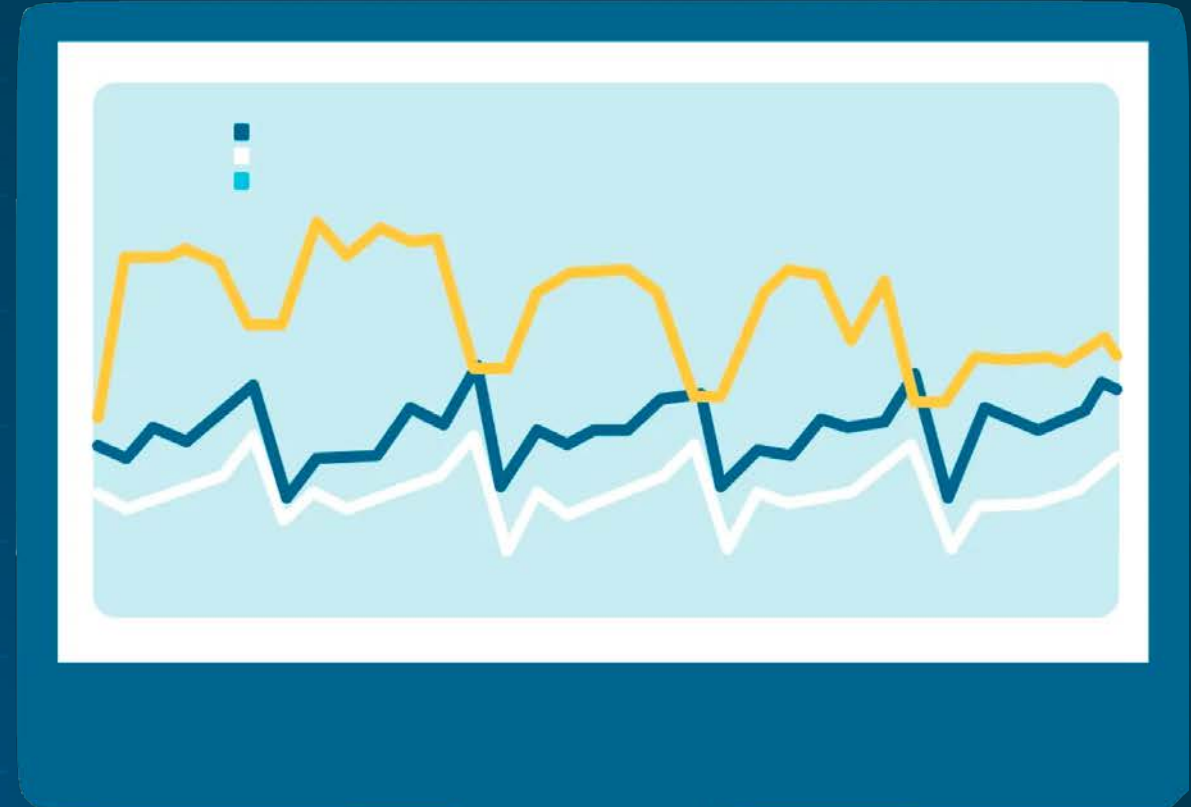


REDUCING THE DIMENSIONALITY BY A FACTOR OF 26,000

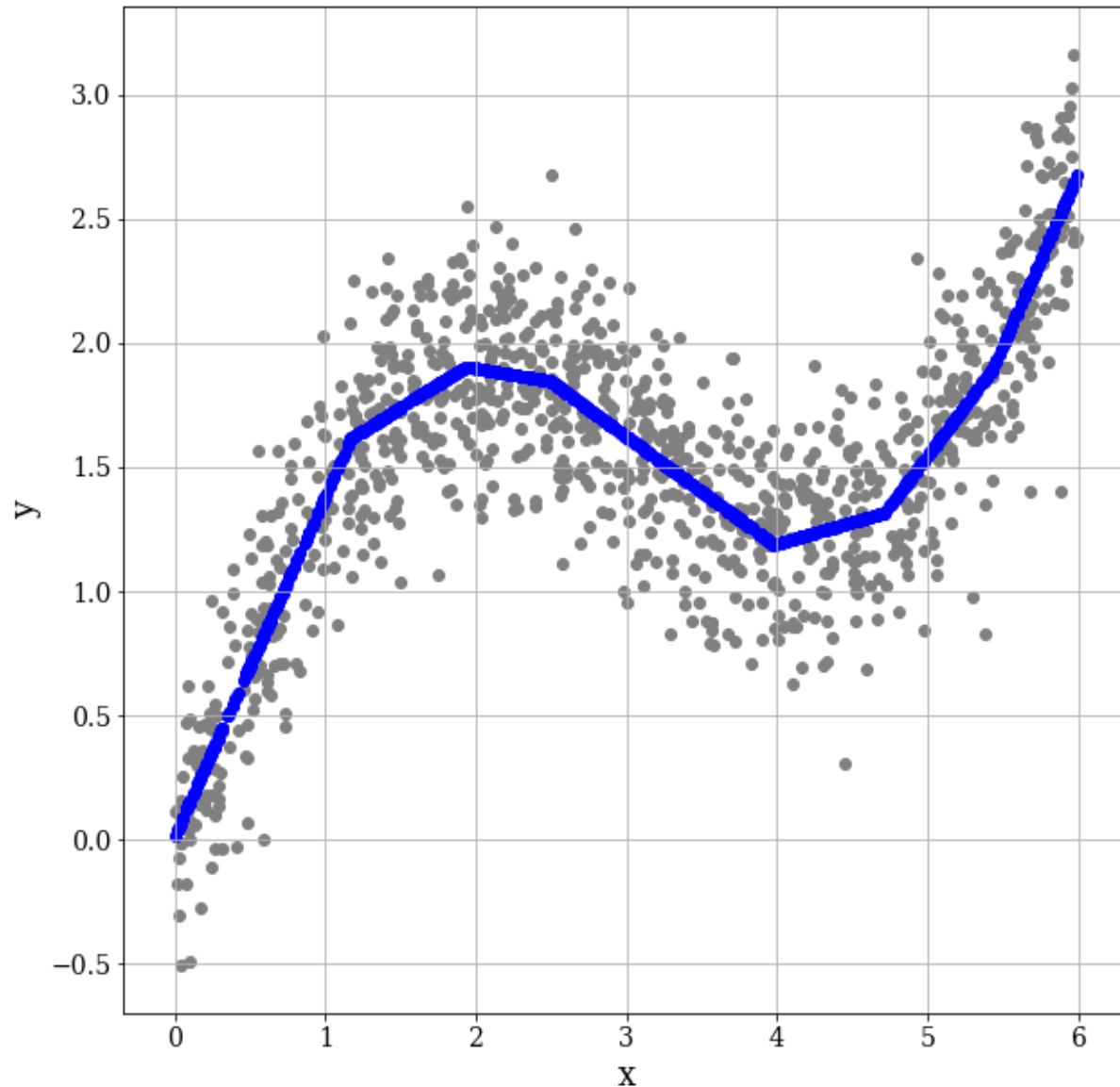


STEP 3: TIME-SERIES FORECASTING

Now the problem reduces to predicting the microstructure evolution in reduced space



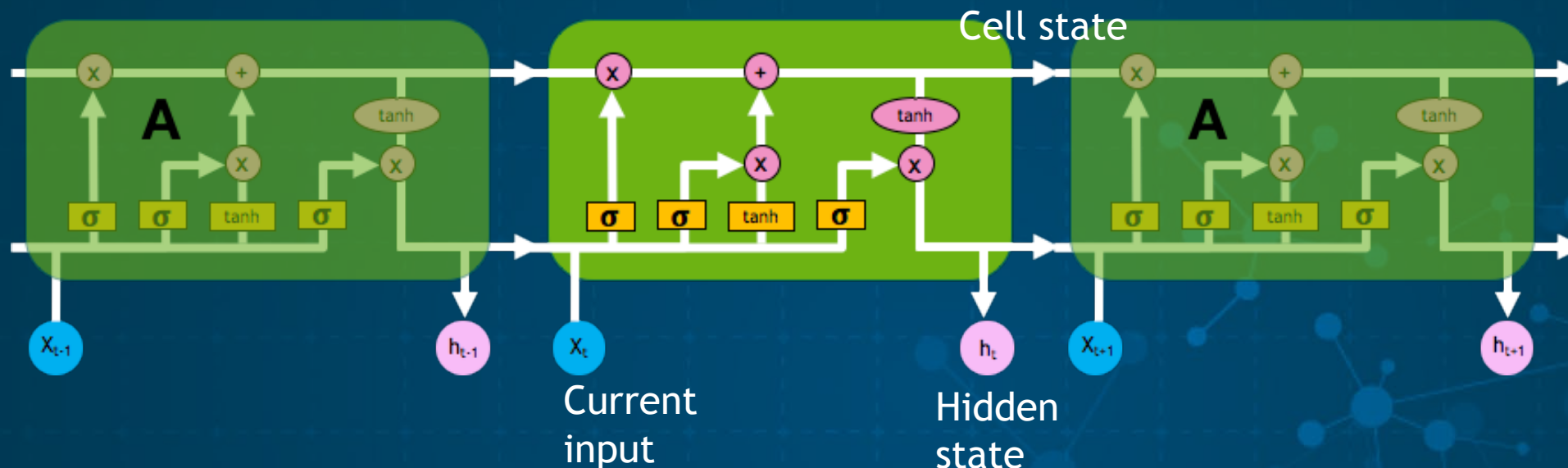
TIME-SERIES MULTIVARIATE ADAPTIVE REGRESSION SPLINES



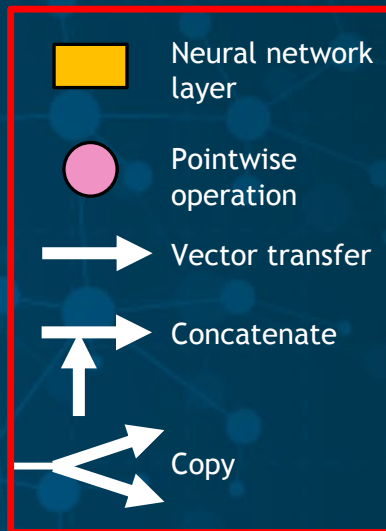
1. Useful for identifying nonlinear structure in time series
2. Non-parametric
3. Autoregressive: divide time-series into optimal subdomains to fit splines
4. Predicting microstructure evolution trajectories in PC space
5. Use m most recent time steps to predict $N+1$, $N+2, \dots$

LONG SHORT-TERM MEMORY NETWORK

1. LSTM is a special kind of a recurrent neural net (RNN):
Network with loops in them allowing information to persist (i.e., memory)
2. Looping connect previous information to current: **TIME HISTORY!**
3. Uses previous states, and current input
4. Learn/forget gate (internal structure) used to form long-term memory (known as cell state) and short-term memory (hidden state)
5. Predicting microstructure evolution trajectories in PC space
6. Use entire history to predict $N+1, N+2, \dots$

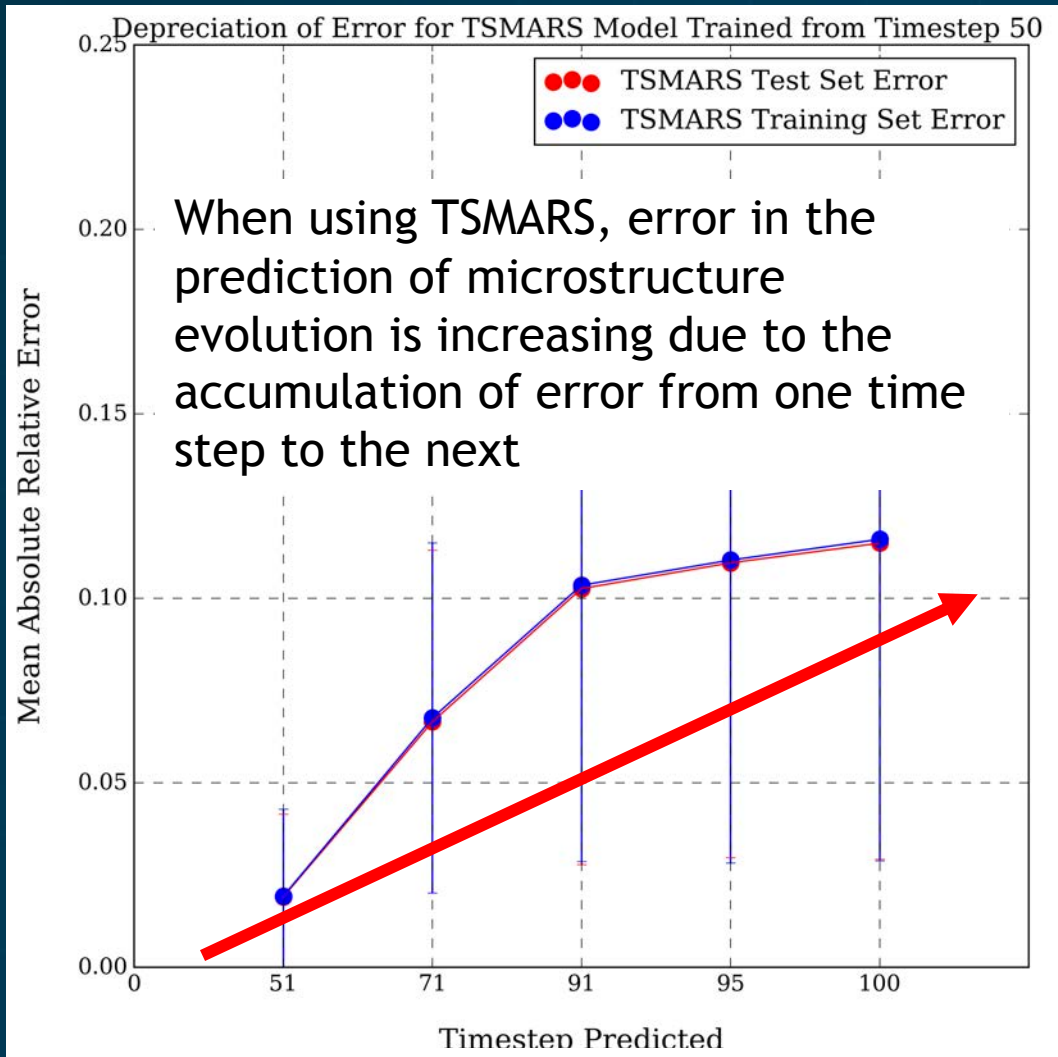


Nomenclature



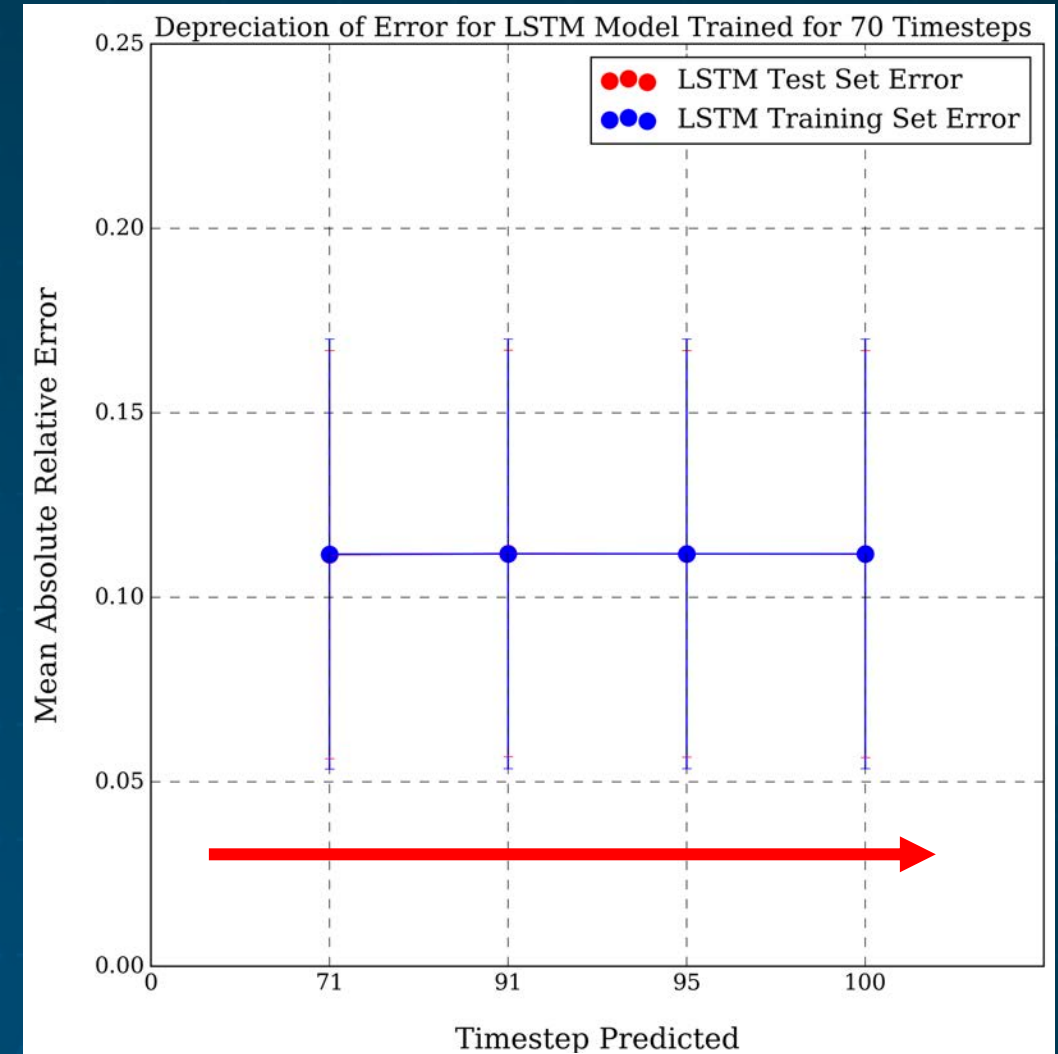
WHY DO WE NEED A DEEP LEARNING STRATEGY?

TSMARS



TSMARS for data augmentation?

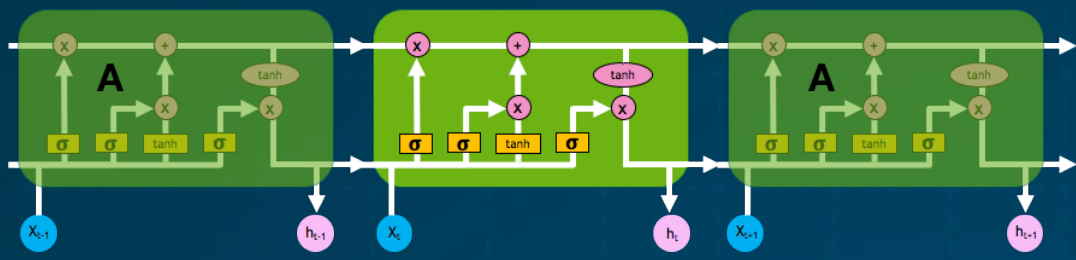
LSTM



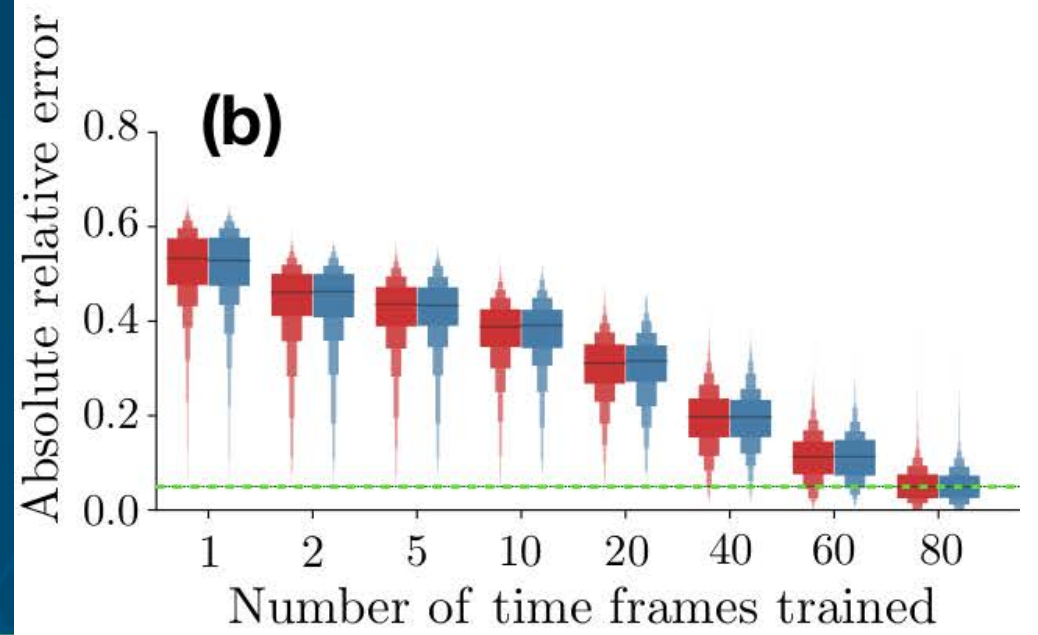
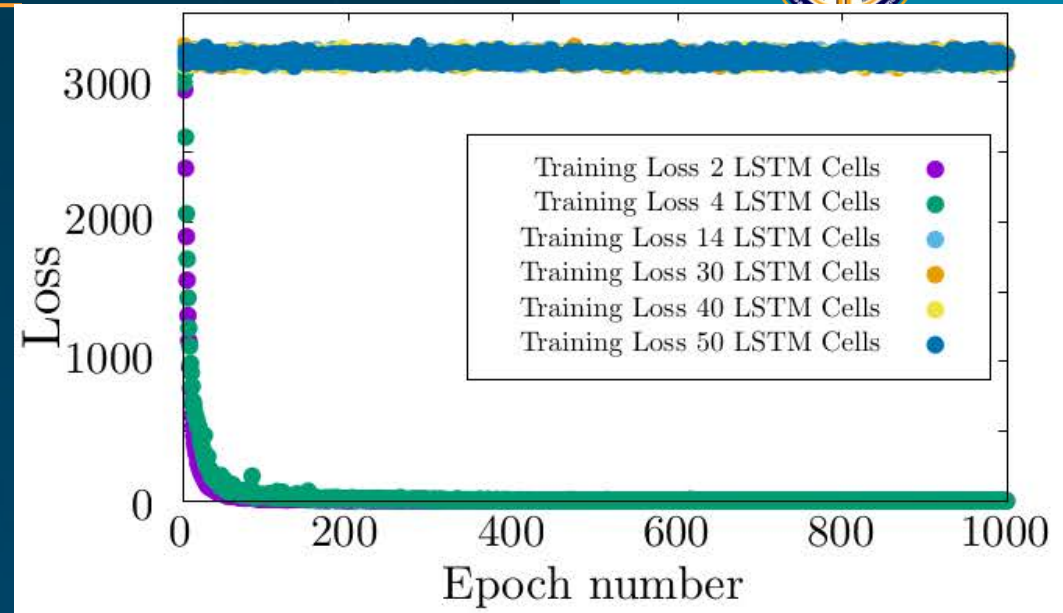
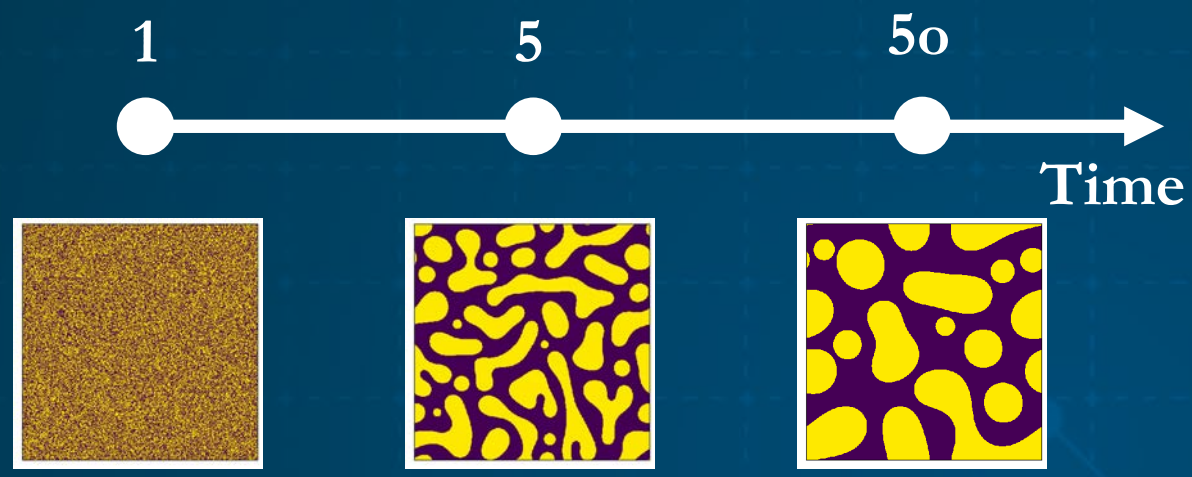
LSTM for PF acceleration?

OPTIMUM LSTM ARCHITECTURE

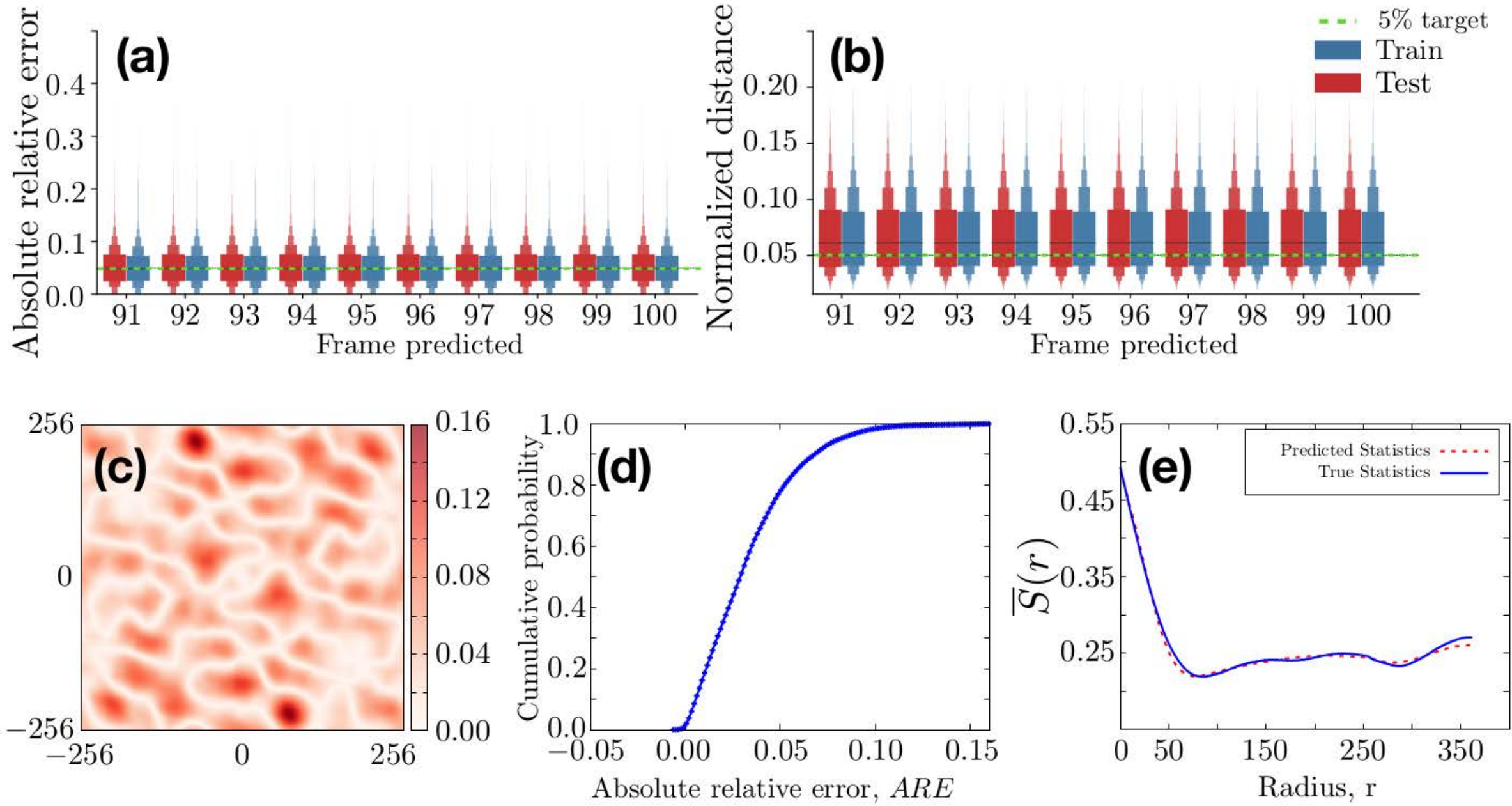
Number of LSTM cells:



Number of time frames needed for training:



PERFORMANCE OF LSTM-TRAINED MODEL



COMPUTATIONAL EFFICIENCY

	High-fidelity	LSTM-trained
1 simulation for 5M time steps	96 mins	0.06s
50,000 simulations	~9 year and 1 month	50 mins



Our LSTM-trained framework is more than 42,000 faster than the high-fidelity simulation with comparable accuracy!

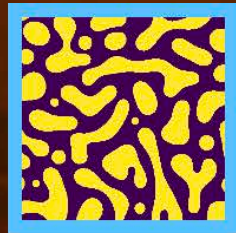
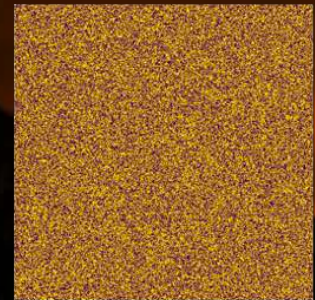
Opens a promising path forward for discovering, understanding and predicting evolutionary microstructural phenomena

ACCELERATING MICROSTRUCTURE EVOLUTION PREDICTIONS: STEP 4: LEAPING IN TIME USING MACHINE-LEARNED SURROGATE

● → High-fidelity phase field trajectory

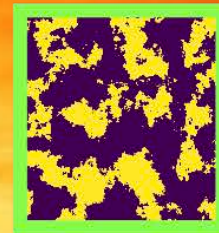
● → Accelerated trajectory

1. Phase field



2. Dimensionality reduction

3. LSTM



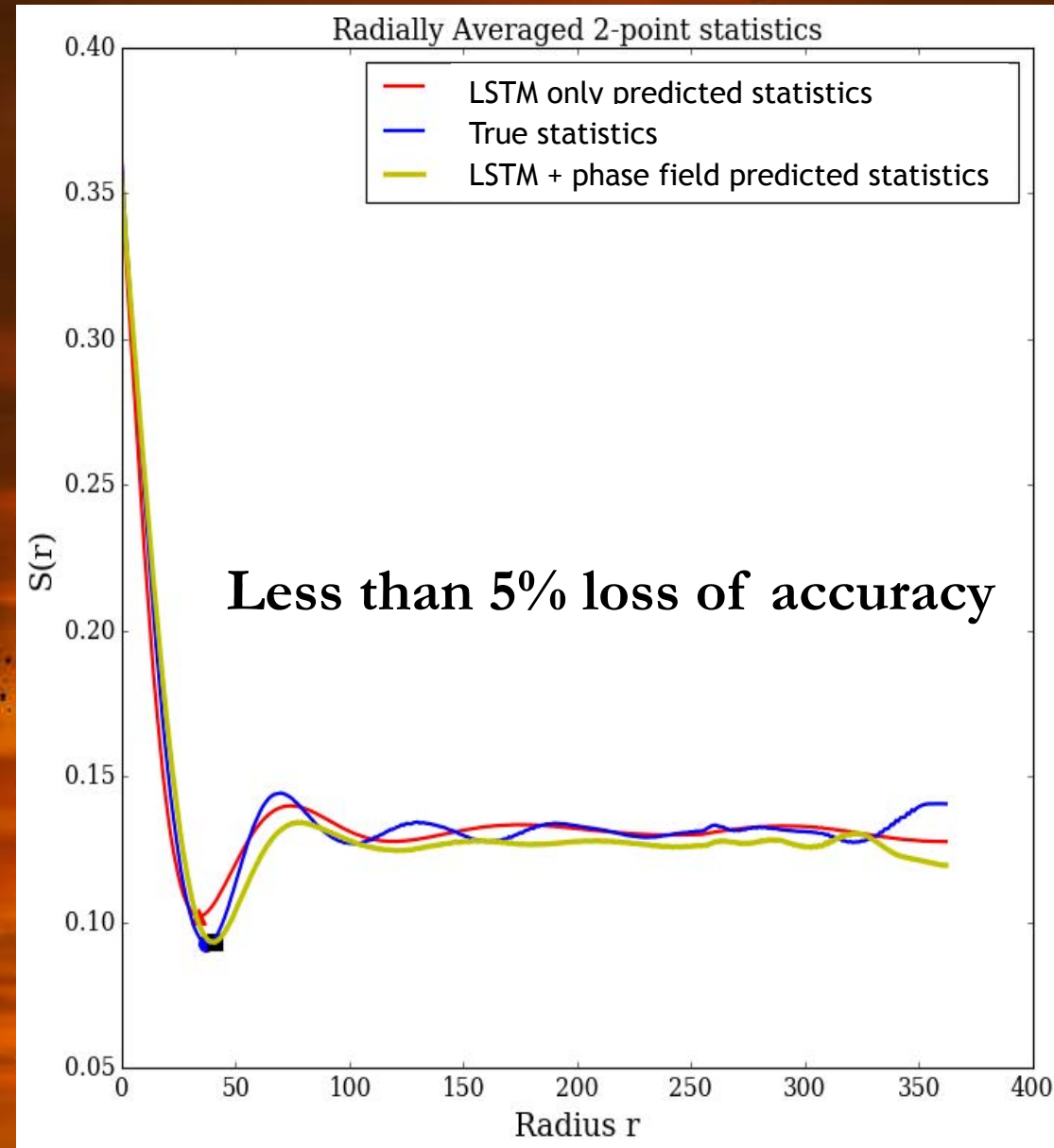
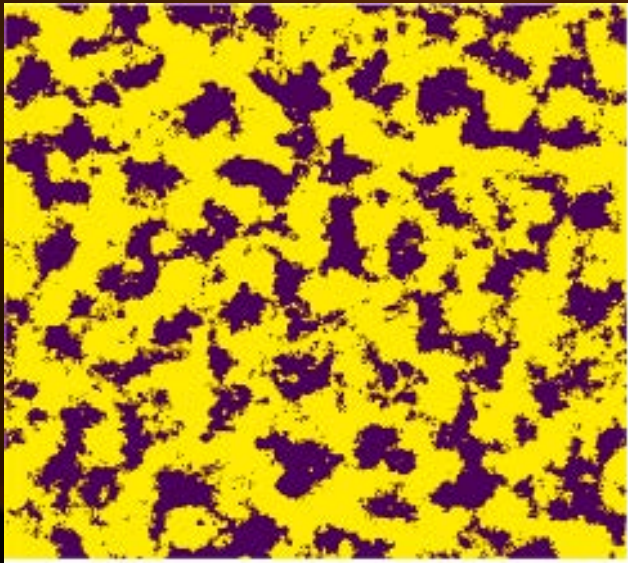
Reconstruction from low dimension

Accelerated

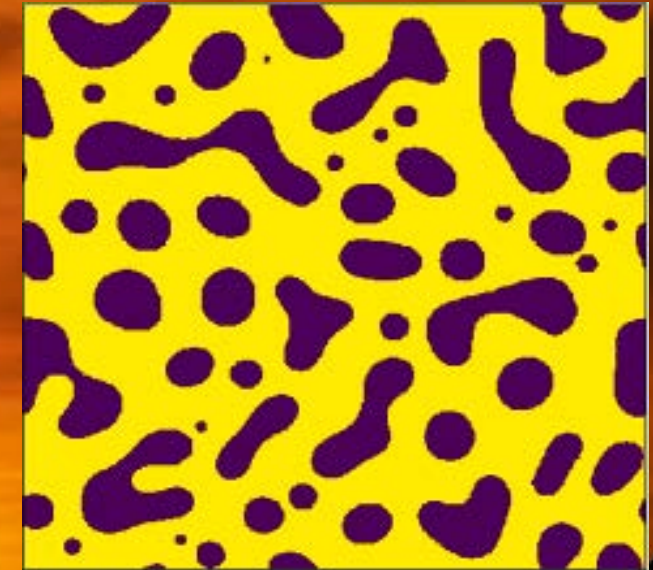


ACCELERATING MICROSTRUCTURE EVOLUTION PREDICTIONS: LEAPING IN TIME USING MACHINE-LEARNED MODEL

LSTM only

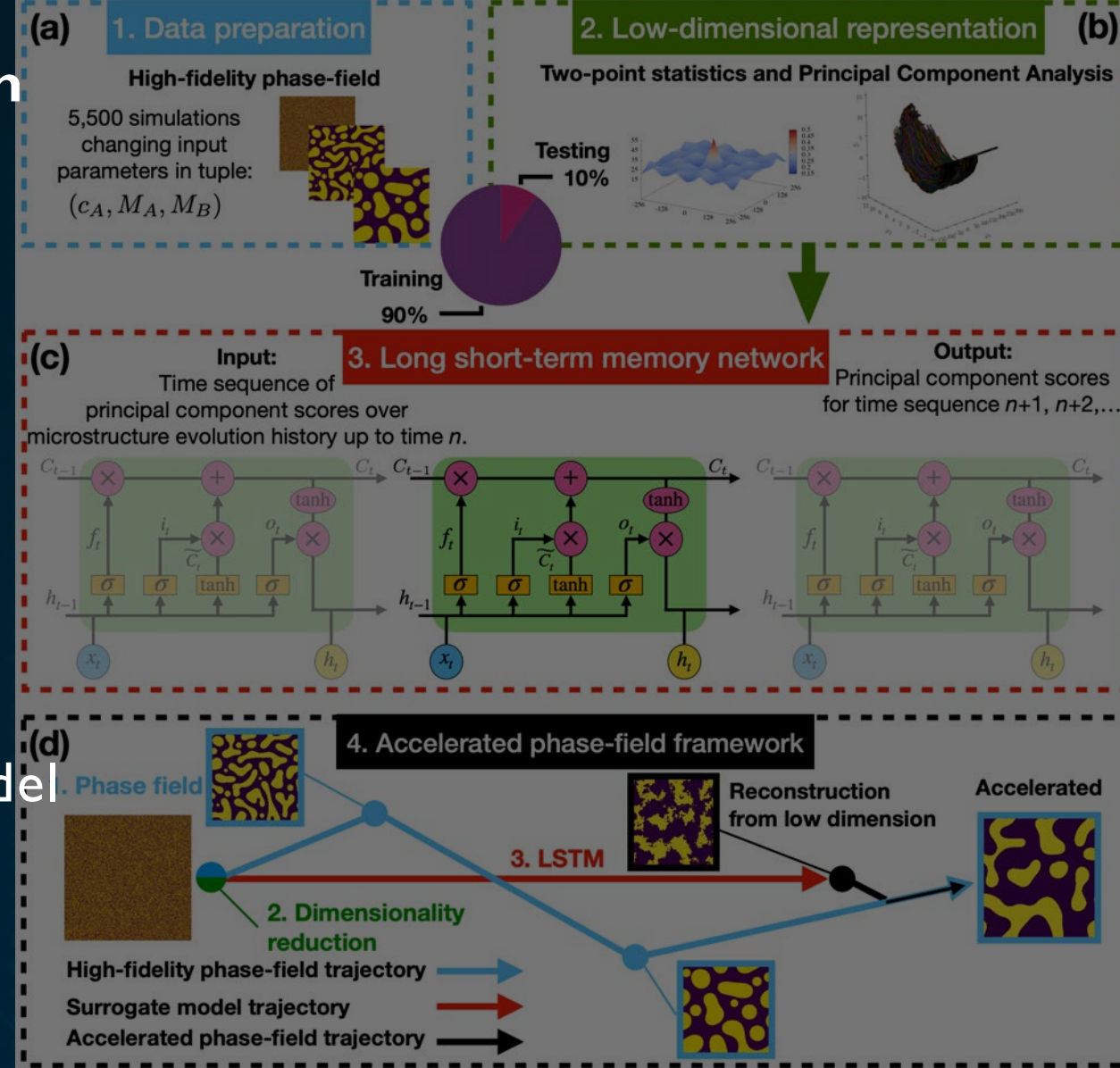


LSTM + phase-field



MOVING FORWARD

- Reframing microstructure evolution as a multivariate time-series problem
Using LSTM to learn long-term patterns in reduced space
- Performance comparable to high-fidelity PF capabilities
>42,000 faster
less than 5% loss in accuracy
- Automated workflow (with S. Martin)
- Alternatives to PCA:
Autoencoders, GP latent variable model
- Alternatives to ML engine:
GRU, Independently RNN, plastic NN





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