SAND2020-13472C

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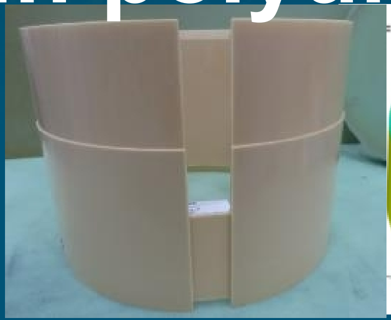
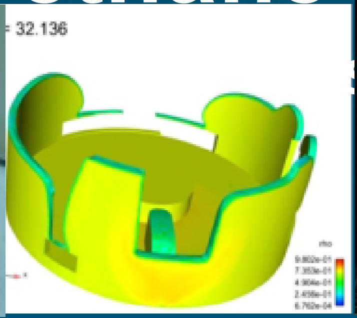
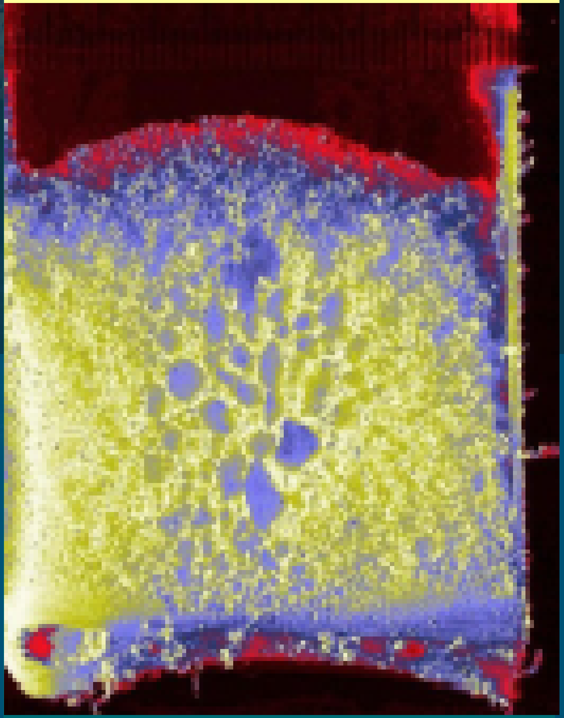
Multiphysics modeling of long-term aging and deformation mechanisms in polyurethane foams


January 11-15, 2021



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Introduction to Polyurethane Foams

- Polyurethane foams are widely used in manufacturing due to ease of production and varied material properties




We are developing models that can predict foam mold filling, void location, and final properties including density and modulus for structural foams and thermal conductivity for insulating material.

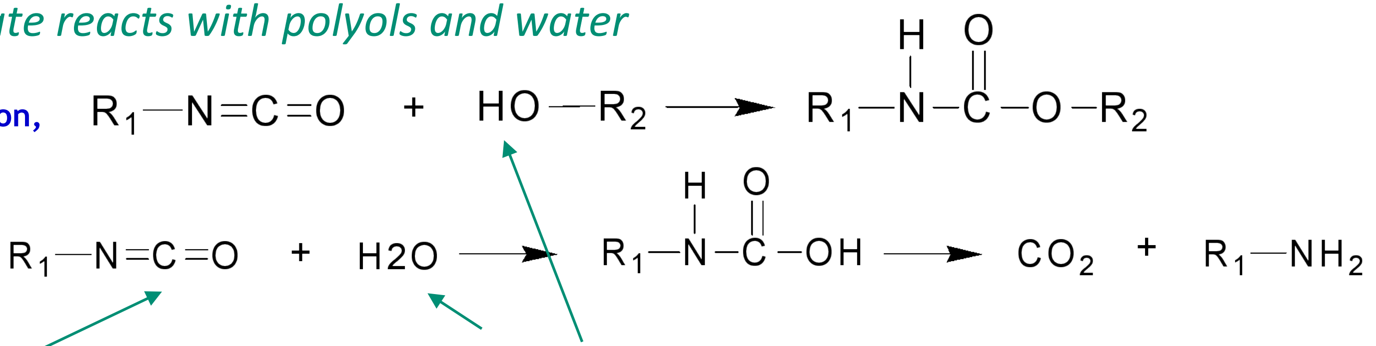
PMDI Foams Are Not Dimensionally Stable

<u>What are PMDI Foams?</u> *Polyurethane foams are used as an **encapsulant** and a **structural** material to provide voltage isolation and mitigate against shock and vibration*

<u>How are they made?</u> *Chemically blown manufacturing process with Two key reactions: Isocyanate reacts with polyols and water*

Urethane formation, crosslinking

Foaming reaction yields CO_2 and amine

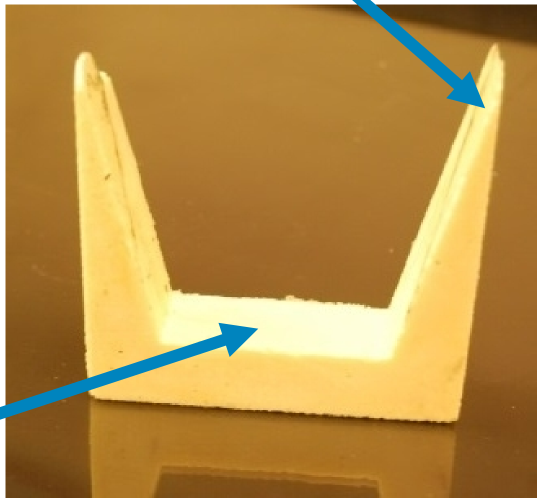


Isocyanate is in excess

Water and polyol are limiting/exhausted

<u>Shape stability over weeks, months, years is problematic</u>

- Tight tolerances (microns) lead to low part yields
- Expensive molds currently designed based on average shrinkage amounts, institutional knowledge, trial-and-error
- Dimensional changes are often not spatially uniform
- Many mechanisms for shrinkage identified



Small dimensional changes in foam translate to significant displacements in parts depending on geometries

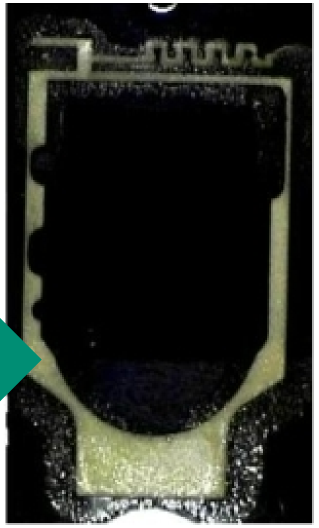
Foam Part Life Cycle Process

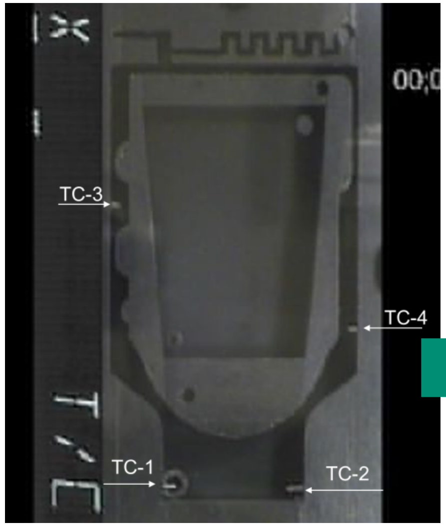
Overarching Goal: **Life cycle models for foaming, vitrification, cure, aging for Structural Foam Parts**

Focus on moderate density PMDI foams

Injection, foaming and initial curing at lower T

Oven time at higher T to make sure it is fully cured



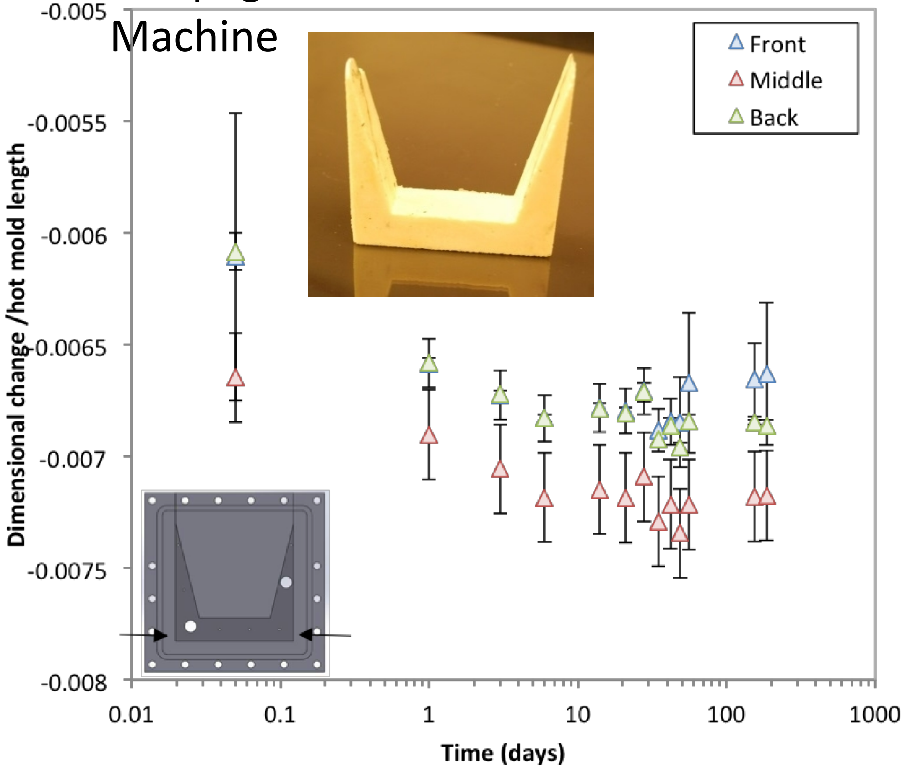


Remove from mold – predict cure and thermal stresses

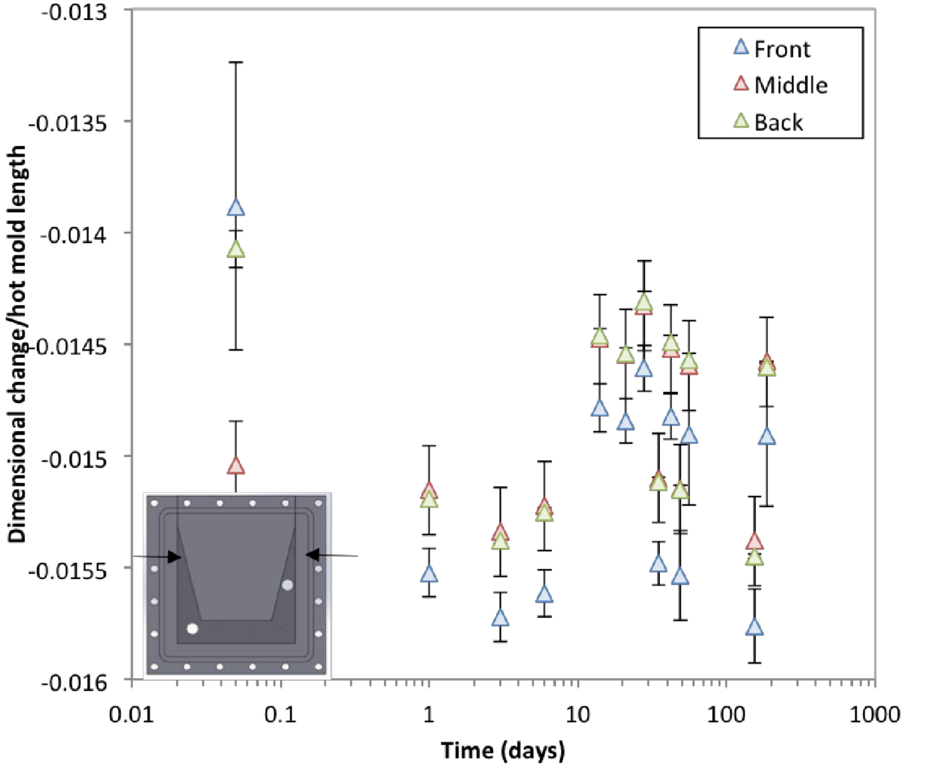
Predict shape and size over years

Motivation: Warpage and Aging Demonstration on Staple

- PMDI 10 S packed to 12.5 PCF
- Cure Schedule: 30 C for 10 minutes, 4 hours at 120 C
- Warpage measurements with a Zeiss® Coordinate Measurement (CMM) Machine



Monotonic and Consistent Warpage Trend in Thick Regions

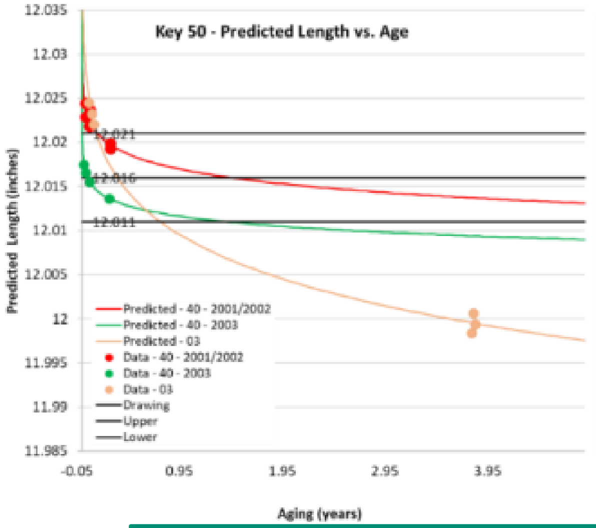


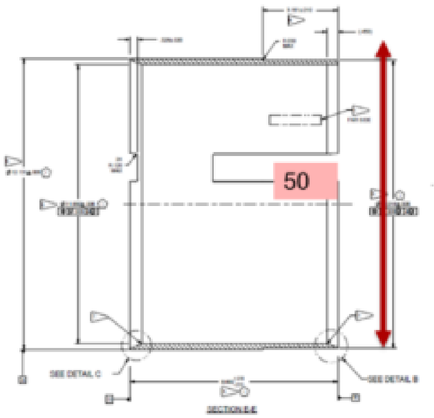
Non-Monotonic and Complex Warpage Trend On Thin Staple Arms

What are the key factors that make complex warpage behavior at the ”staple arms”?

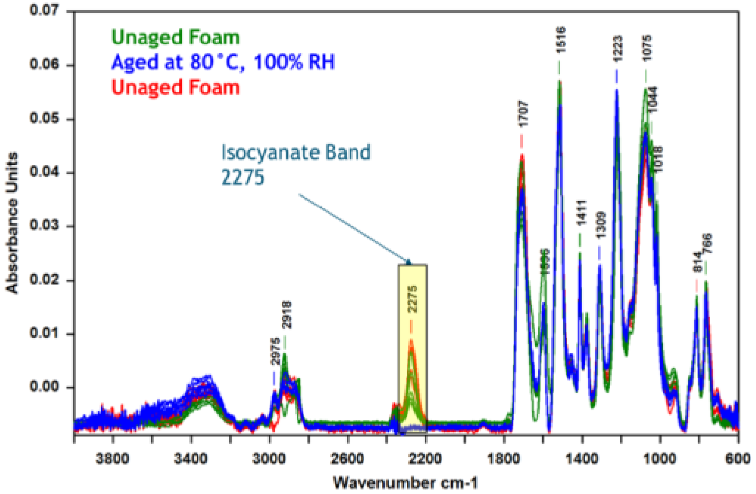
Foam Structural Support Shrinkage Models

- Manufacturing stresses and CO_2 loss cannot explain all of the experimentally observed deformation in PMDI support parts.
- Previous work shows water can react with isocyanate in PMDI foams to form CO_2 even below the T_g of the material. This causes shrinkage because new crosslinks are formed and the reaction off gases carbon dioxide.





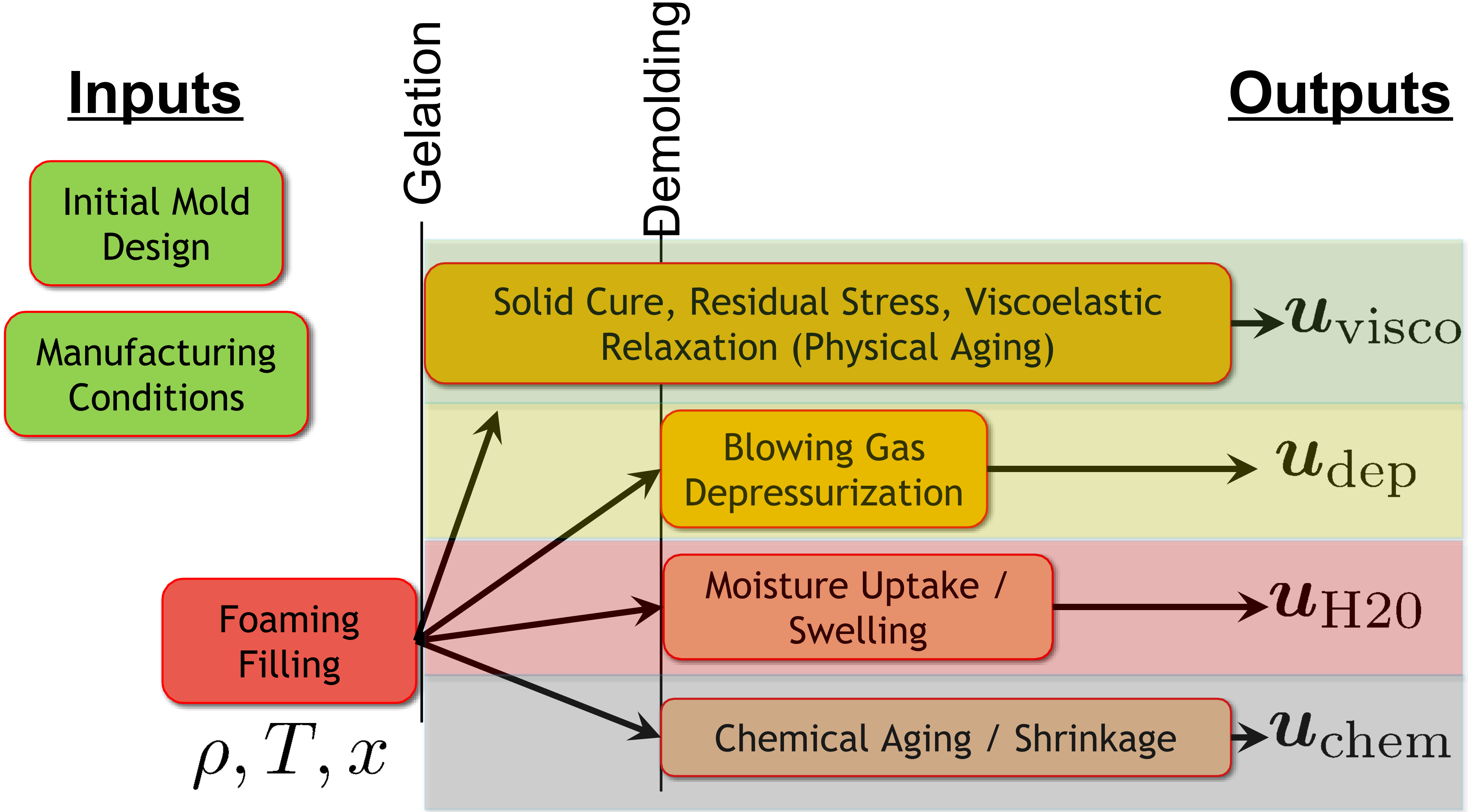
Surveillance data show foam structural parts change shape over time in storage



FTIR data show that the residual isocyanate exists post-manufacture and will be consumed in humid environments

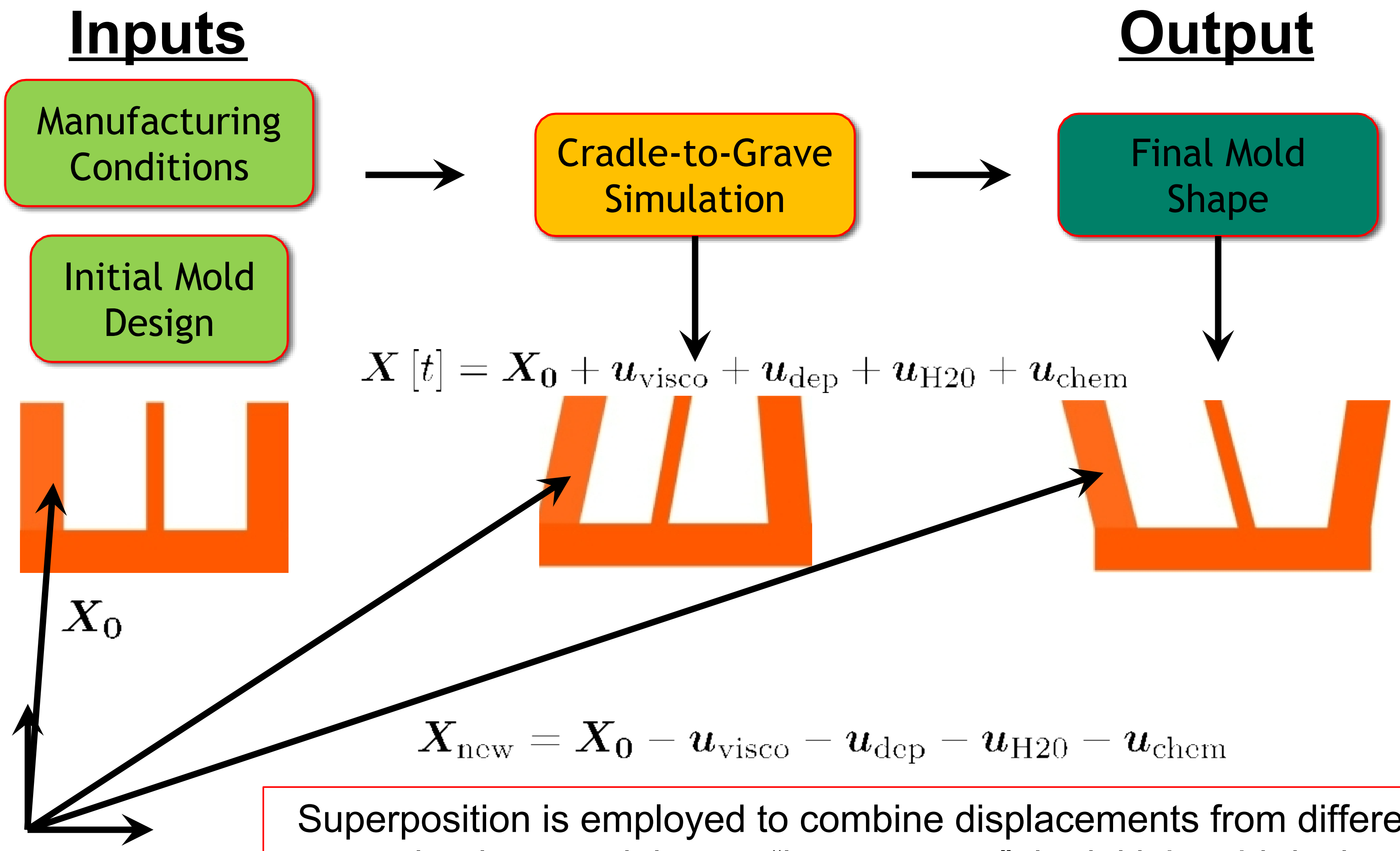
	Occurs over	Strain (%)
Thermal contraction/Manufacturing stress	Hours	~0.1% from 120 C to RT depending on density
CO_2 loss, bubble depressurization	Days/Weeks	~0.02% depending on density
Post-cure Isocyanate reaction	Months? Years? Depends on humidity	~0.05% depending on density
Viscoelastic relaxation (Physical aging)	Decades	Very small

Engineering-scale model framework for manufacturing and in-service aging for Rigid PMDI Foams



$$\boldsymbol{u} = \boldsymbol{u}_{\mathrm{visco}} + \boldsymbol{u}_{\mathrm{dep}} + \boldsymbol{u}_{\mathrm{H20}} + \boldsymbol{u}_{\mathrm{chem}}$$

A Key Model Target: Inverse mold design for manufacturing/age aware shrinkage mitigation



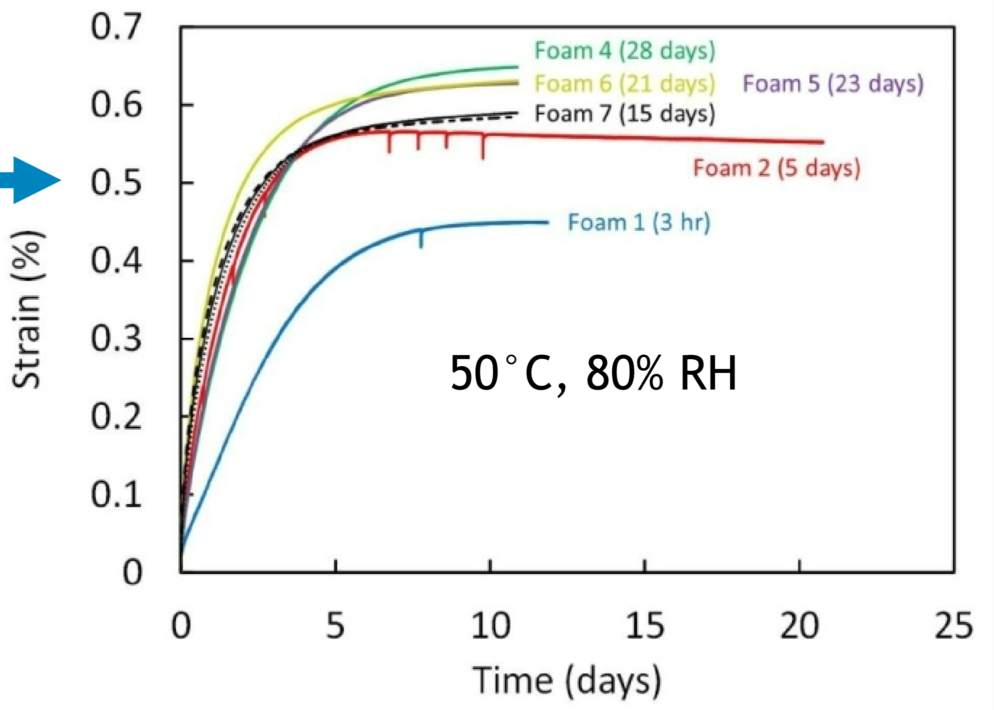
Superposition is employed to combine displacements from different mechanisms and then to “inverse warp” the initial mold design

Review of the Theory

- We consider that water concentration infiltrates and diffuses into foam components post manufacture
  - Water infiltration is associated with Swelling and Tg depression

- Water reacts with residual isocyanate to shrink the foam and elevate the glass transition (anti-plasticization)

- The stress response considers:
  - Primary cross-linking (degree of cure, x)
  - Secondary cross-linking, NCO consumption (degree of cur
  - Moisture Uptake via a water concentration, (CH20)
  - Thermal Expansion
  - Shear and Bulk Responses



FBG-derived strain profiles during equilibration of PMDI foam cylinders at 50 °C, 80% RH. The duration for which each foam cylinder was initially equilibrated at 50 °C, 0% RH is indicated in parentheses

Equations of motion and Constitutive Models for the Solid Foam

Displacement as a function of water concentration, and secondary cure

Equations of Motion

Spatial Quasi-static Linear Momentum Balance (u)

$$\nabla \cdot \boldsymbol{\sigma} + \boldsymbol{b} = \boldsymbol{0},$$

Constitutive Law for the Cauchy Stress

$$\begin{aligned}
\boldsymbol{S}_{\boldsymbol{\varepsilon}} &= \frac{\partial \psi}{\partial \boldsymbol{\varepsilon}} = \boldsymbol{S}_{\boldsymbol{\varepsilon}}{}^{\text{mech}} - \delta^{\infty} K^{\infty} \left(C_{H_2O} - C_{H_2O}^{\text{ref}} \right) \mathbf{1} \\
\boldsymbol{S}_E &= \frac{1}{2} \frac{\partial \psi}{\partial \boldsymbol{\varepsilon}} : \frac{\partial \boldsymbol{\varepsilon}}{\partial \boldsymbol{C}} \\
\boldsymbol{\sigma} &= J^{-1} \boldsymbol{F} \boldsymbol{S}_{\boldsymbol{E}} \boldsymbol{F}^T
\end{aligned}$$

Lagrangian Species Balances for Isocyanate, Water, and dissolved Carbon Dioxide in the Foam

$$\frac{dC_{NCO}}{dt} = -k_{NCO} C_{NCO}^2 C_{H_2O}^2$$

$$\frac{dC_{H_2O}}{dt} = -k_{NCO} C_{NCO}^2 C_{H_2O}^2$$

$$\frac{dC_{CO_2}}{dt} = +k_{NCO} C_{NCO}^2 C_{H_2O}^2$$

Rubbery Response

$$\begin{aligned}
S_{ij}^{\varepsilon\infty} = \frac{\partial \Psi^{\infty}}{\partial \varepsilon_{ij}} &= 2G^{\infty}(\varepsilon_{ij}^{dev} - \xi_{ij}^{dev}) \\
&+ (P_{ref} - K^{\infty}\alpha^{\infty}(\Theta - \Theta_{ref}) - K^{\infty} I_{1\varepsilon})\,\delta_{ij} \\
&- (K^{\infty}\beta^{\infty}(x - x_{ref}) - K^{\infty}\gamma^{\infty}(y - y_{ref}))\,\delta_{ij} \\
&- K^{\infty}\delta^{\infty}\left(C_{H_2O} - C_{H_2O}^{\text{ref}}\right)\delta_{ij}
\end{aligned}$$

Combined (Glassy + Rubbery) Response

$$\begin{aligned}
S_{ij}^{\varepsilon} = \frac{\partial \Psi}{\partial \varepsilon_{ij}} = S_{ij}^{\varepsilon\infty} &+ (K^G - K^{\infty}) \int_0^t ds\, f^v(t' - s', 0) \frac{dI_{1\varepsilon}}{ds} \delta_{ij} \\
&+ 2(G^G - G^{\infty}) \int_0^t ds\, f^s(t' - s', 0) \frac{d(\varepsilon_{ij}^{dev} - \xi_{ij}^{dev})}{ds} \\
&- (K^G\alpha^G - K^{\infty}\alpha^{\infty}) \int_0^t ds\, f^v(t' - s', 0) \frac{d\Theta}{ds} \delta_{ij} \\
&- (K^G\beta^G - K^{\infty}\beta^{\infty}) \int_0^t ds\, f^v(t' - s', 0) \frac{dx}{ds} \delta_{ij} \\
&- (K^G\gamma^G - K^{\infty}\gamma^{\infty}) \int_0^t ds\, f^v(t' - s', 0) \frac{dy}{ds} \delta_{ij} \\
&- (K^G\delta^G - K^{\infty}\delta^{\infty}) \int_0^t ds\, f^v(t' - s', 0) \frac{dC_{H_2O}}{ds} \delta_{ij}
\end{aligned}$$

Constitutive Models for the Solid Foam

Prony Series (Viscoelastic Relaxation Functions)

$$f^k\left(t'-s',t'-u'\right) = \sum_{j=1}^{m} A^j \exp\left(\frac{-\left(t'-s'\right)}{\tau_j}\right)\exp\left(\frac{-\left(t'-u'\right)}{\tau_j}\right)$$

Relation between material and laboratory time

$$t'-s' = \int_s^t \frac{dz}{a(z)}dz. \qquad \log a = \frac{-C_1 N}{C_2+N}$$

Determination of time-history superposition

$$\begin{aligned} N = & \left(\Theta-\Theta_{glass}-\int_0^t ds f^v\left(t'-s',0\right)\frac{d\Theta}{ds}\right) \\ & +C_3\left(I_{1\varepsilon}-\int_0^t ds f^v\left(t'-s',0\right)\frac{dI_{1\varepsilon}}{ds}\right) \\ & +C_4\int_0^t ds\int_0^t du f^s\left(t'-s',t'-u'\right)\frac{d(\varepsilon_{ij}^{dev}-\xi_{ij}^{dev})}{ds}\frac{d(\varepsilon_{ij}^{dev}-\xi_{ij}^{dev})}{du} \\ & +C_5\left(x-x_{ref}-\int_0^t ds f^v\left(t'-s',0\right)\frac{dx}{ds}\right) \\ & +C_6\left(y-y_{ref}-\int_0^t ds f^v\left(t'-s',0\right)\frac{dy}{ds}\right). \\ & +C_7\left(C_{H_2O}-C_{H_2O}^{\mathrm{ref}}-\int_0^t ds f^v\left(t'-s',0\right)\frac{dC_{H_2O}}{ds}\right). \end{aligned}$$

Change in the glass transition from curing and swelling

$$\Theta_{ref}\left(x,y\right) = -\frac{\left(C_3\beta_\infty+C_5\right)\left(x-x_{ref}\right)+\left(C_3\gamma_\infty+C_6\right)\left(y-y_{ref}\right)+\left(C_3\delta_\infty+C_7\right)\left(C_{H_2O}-C_{H_2O}^{ref}\right)}{1+C_3\alpha_\infty}$$

Total Helmholtz FE per unit undeformed volume

Chemical Potential of Water Uptake

$$\mu = \frac{\partial\psi}{\partial C_{H_2O}} = A\left(C_{H_2O}-C_{H_2O}^{\mathrm{ref}}\right)-\delta^\infty K^\infty \mathrm{tr}\boldsymbol{\varepsilon}-\mu_{\mathrm{ref}}.$$

Assumption of Water Transport Kinetics

$$\boldsymbol{j} = -m\nabla\mu = -m\left(A\nabla C_{H_2O}-\delta^\infty K^\infty\nabla\left(\mathrm{tr}\boldsymbol{\varepsilon}\right)\right)$$

Ultimately, we simplified transport kinetics:

$$D_{H_2O}^{eff} = D_{H_2O}e^{-E_{H_2O}/RT}$$

$$D_{CO_2}^{eff} = D_{CO_2}e^{-E_{CO_2}/RT}$$

Cradle-to-Grave Modeling of Foam Parts

Sierra Mechanics FEA Code Suite

Kinetics and species balances for CH20 and YRCT were developed and coupled to the solid mechanics FE code through an ALE formulation in the thermal-fluid FE code

Thermal-Fluid

Pre-Gel
($0\text{-}10^{3}$ seconds)

Chemistry results in both gas production (foaming) and matrix polymerization (curing)

Foaming liquid rises to fill the mold until polymer matrix gelation

Thermal-Fluid/Solid Mechanics

Post-Gel Cure
(10^{3}– 10^{4} seconds)

Variations in temperature cause variations in density and extent of cure

Solid polymer matrix locks in density gradients

Once the polymer vitrifies, further gas production causes bubble pressurization without volume increase

Thermal-Fluid/Solid Mechanics

Vitrified and Released
(10^{4} + seconds)

Residual stresses, density, and properties vary spatially

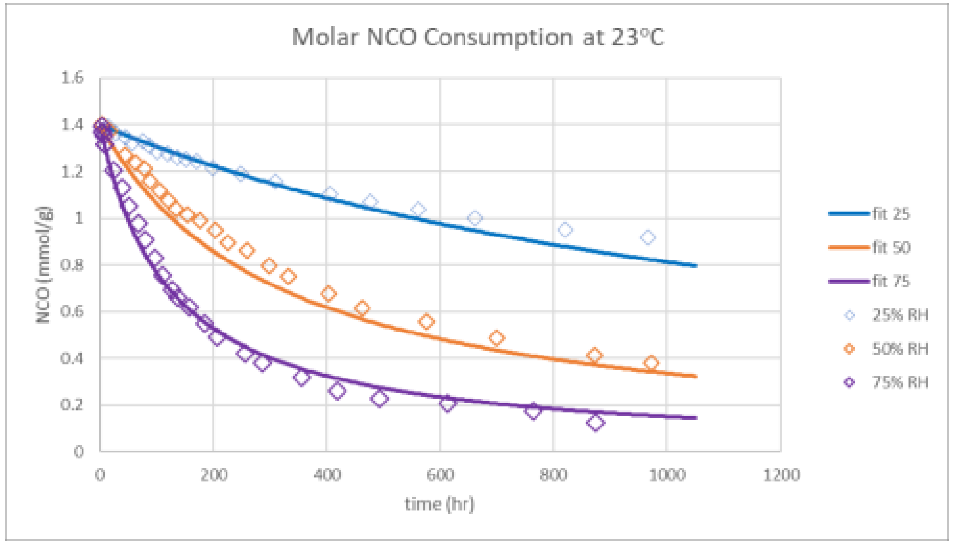
Water uptake/swelling and post-cure shrinkage reactions

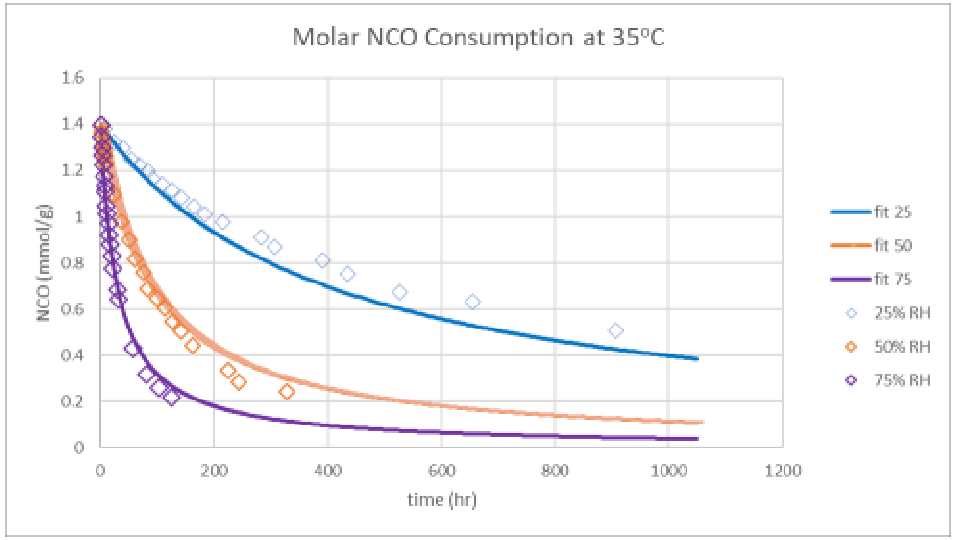
Both long and short term shape change is possible as different parts of the foam relax at different rates

t = 1 - 15 minutes | t = 3 hours | t = 1- 30 years

Manufacturing | Service Life

NCO Kinetics as a Function of Temperature and Humidity





k=$k_o$exp(-E_a/RT)*exp(-a*C/RT)

$$k_{NCO} = k_o \exp(-E_{NCO}/RT)$$

$$E_{NCO} = E_a + a(T)C_{H_2O}$$

$$\frac{dC_{NCO}}{dt} = -k_{NCO}C_{NCO}^2C_{H_2O}^2$$

$$\frac{dC_{H_2O}}{dt} = -k_{NCO}C_{NCO}^2C_{H_2O}^2$$

$$\frac{dC_{CO_2}}{dt} = +k_{NCO}C_{NCO}^2C_{H_2O}^2$$

Temperature (K)	296.15	308.15	323.15
a(T)	-800	-2400	-4100

Parameter	Value
Ea (J/mol)	39500
k0(ml^3/hr mmol^3	1.05E+04

- New model with water concentration accelerating the reactions and modifying the activation energy of NCO post-cure reactions

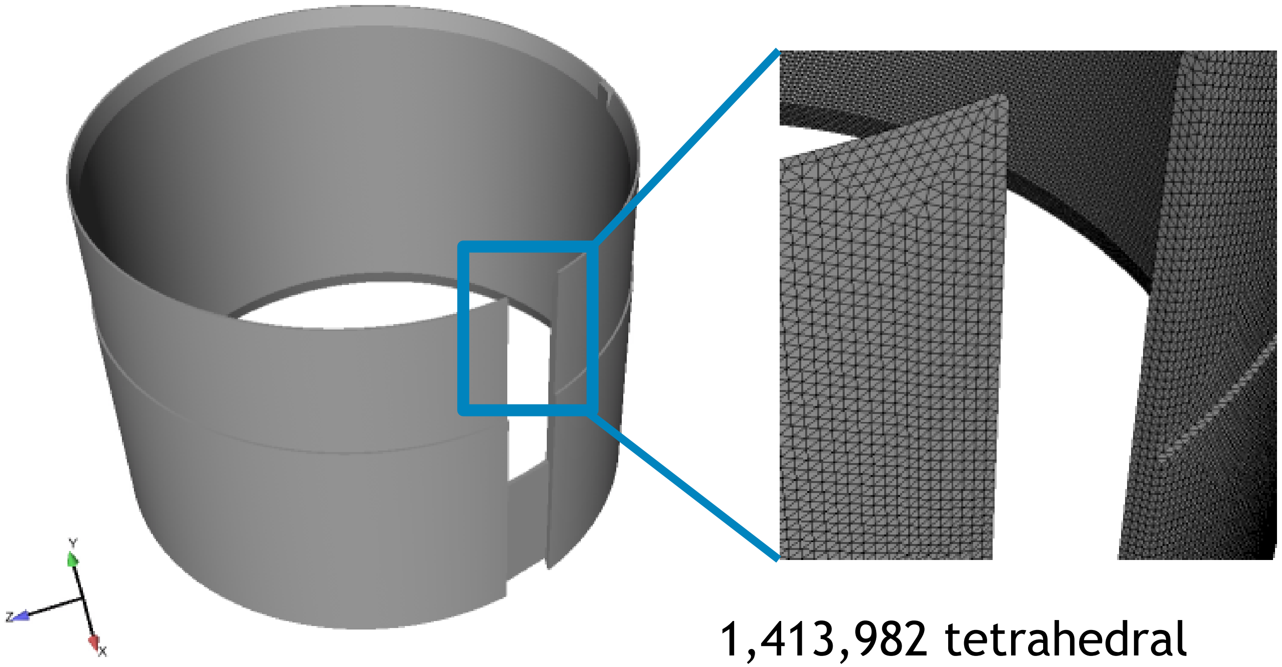
Example: Structural Foam Cylinder

❖ Thin-walled cylinder with notch cut-out to test behavior of thin sections and tight dimensional tolerances

Experiments: Manufacture + Aging

Manufacturing Parameters	Test Number					
Serial Numbers	X112	X117	X120	2001	2002	2003
Mold Pre-Heat (°F)	95 ± 5			95 ± 5		
Pour Wt. (g)	810.3	810.0	809.7	830.0		
Cure Temp (°F)	250			250		
Cure Time (hrs)	4			4		
Mold Strip Temp (°F)	<200			<200		
Inspection Timing (days)	42 1399	35 1392	26 1386	7,14,28,90+		
Inspection	CMM Zeiss/ Weight			CMM Zeiss/ Weight		

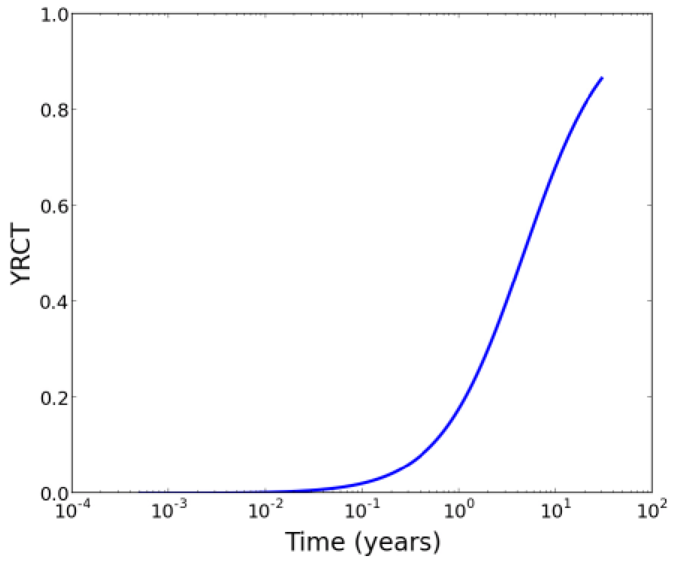
3-D Finite Element Model



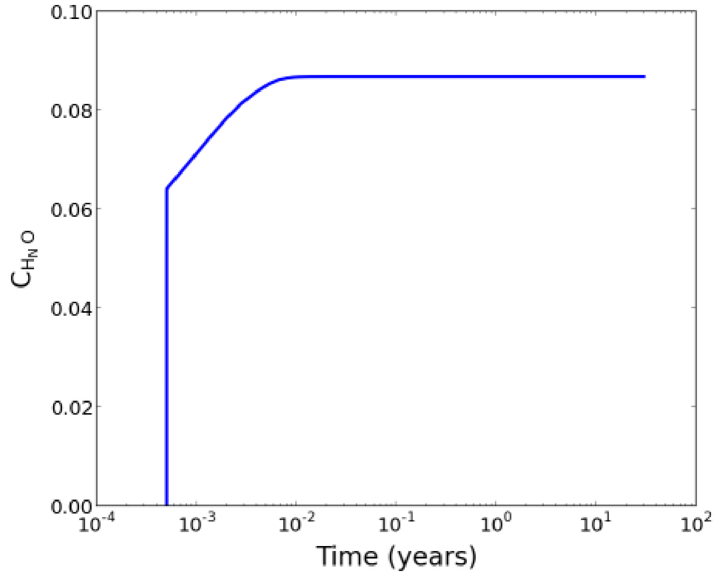
1,413,982 tetrahedral elements

Chemistry Evolution Over 30-Year Lifespan

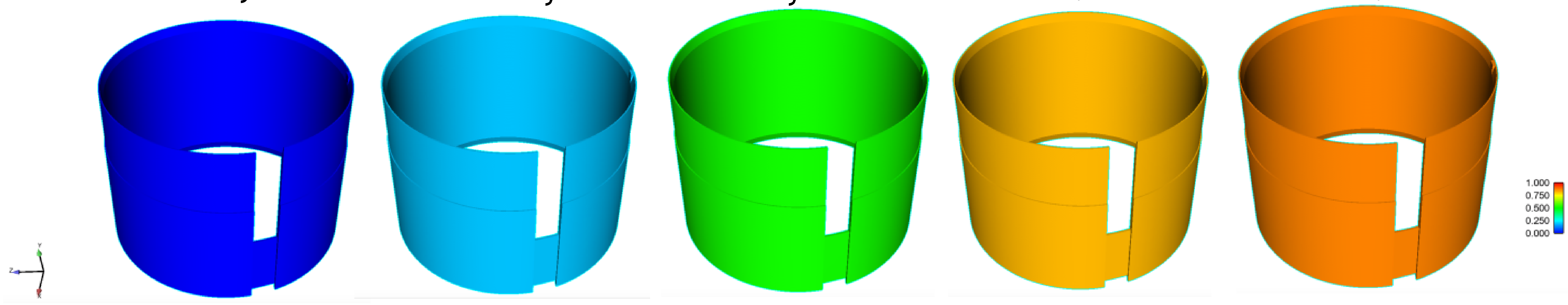
Secondary Cure Reaction Progress



Water Concentration

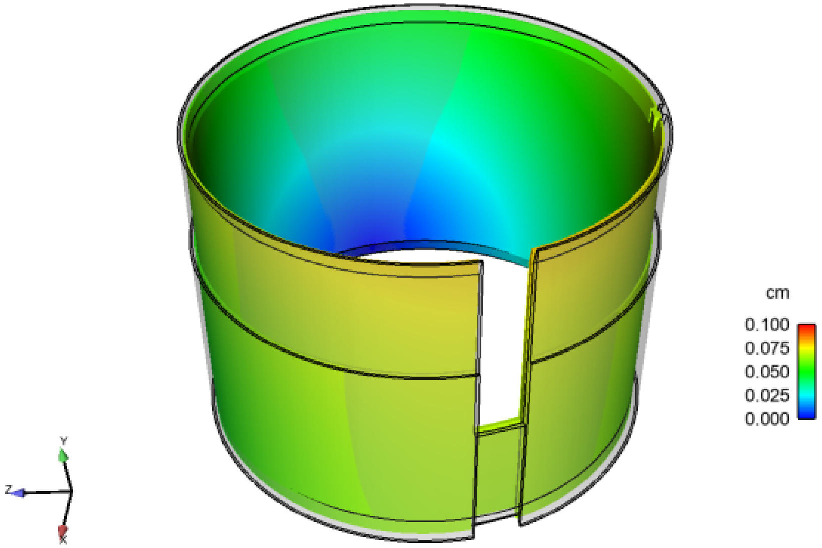


t = 0 years | t = 1.1 years | t = 5 years | t = 20 years | t = 30 years

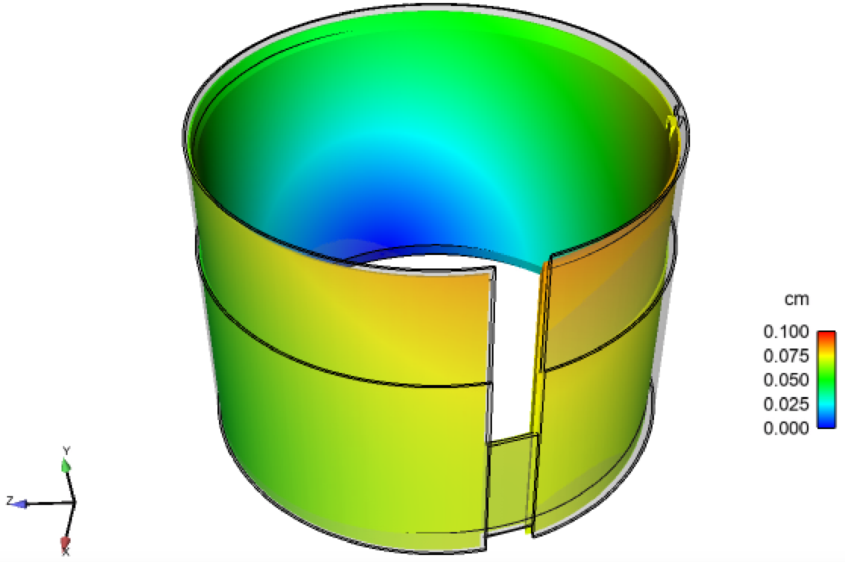


Model Predicts Part Shrinkage Over Time

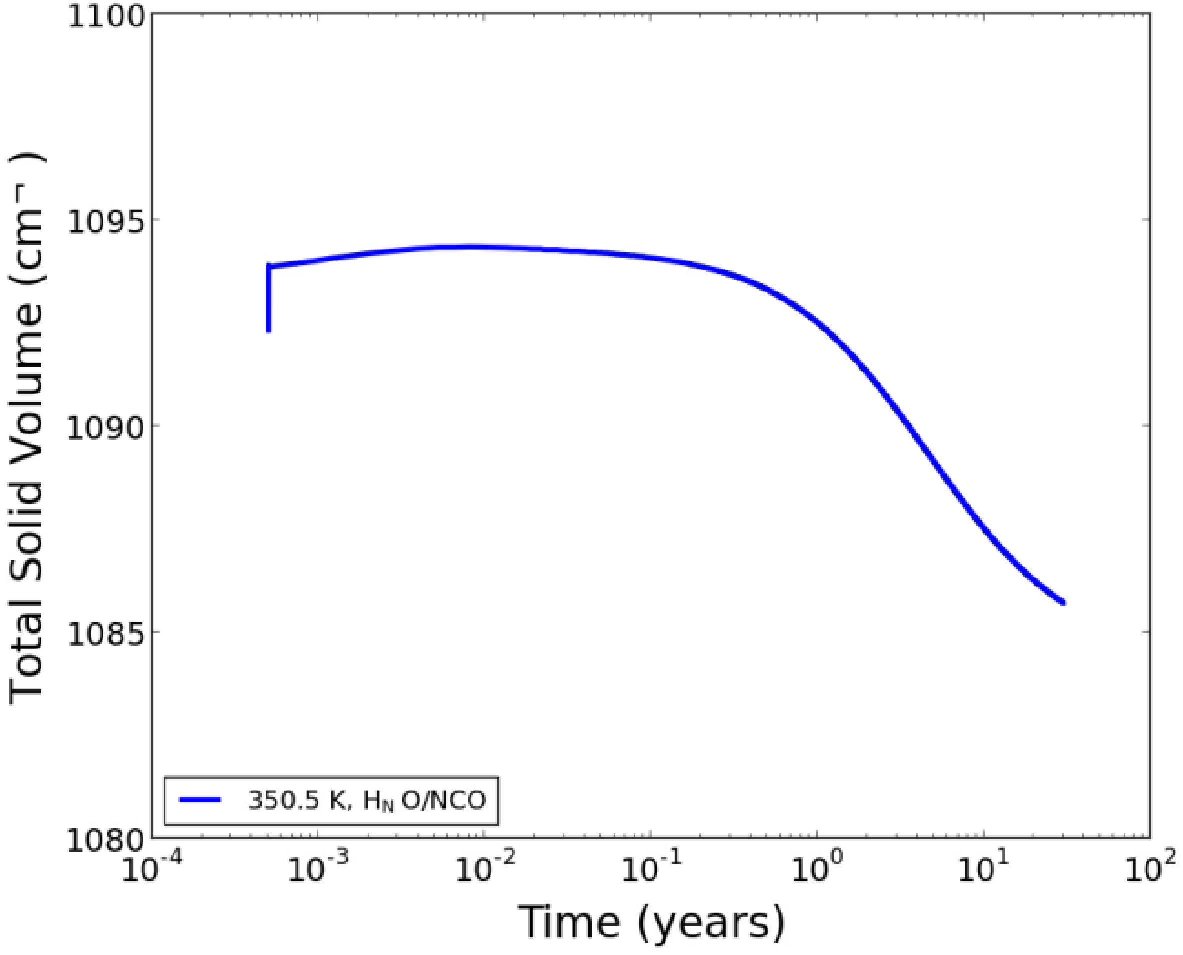
Manufacturing
+
Viscoelasticity



Moisture Uptake + Secondary Cure

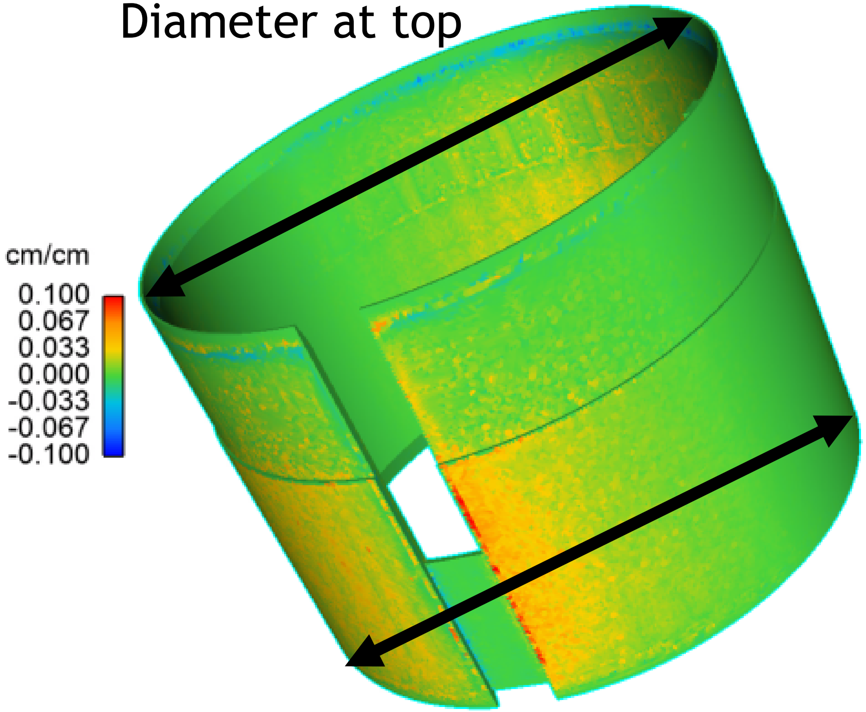


Volume Change from All Mechanisms Combined



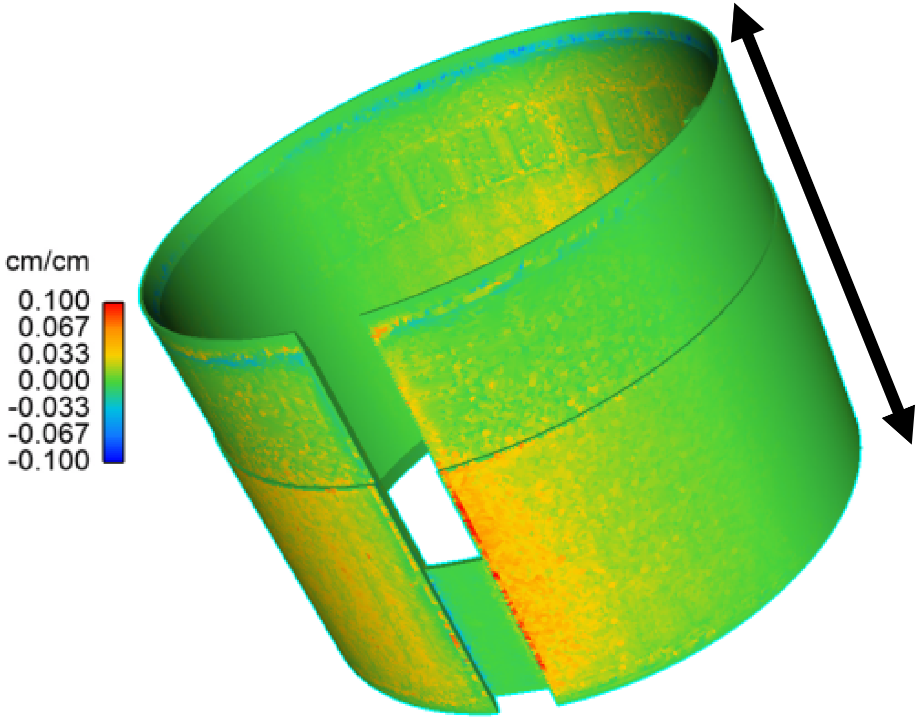
Comparison Metrics with Experimental Measurements

Key 50 = Outer Diameter at top

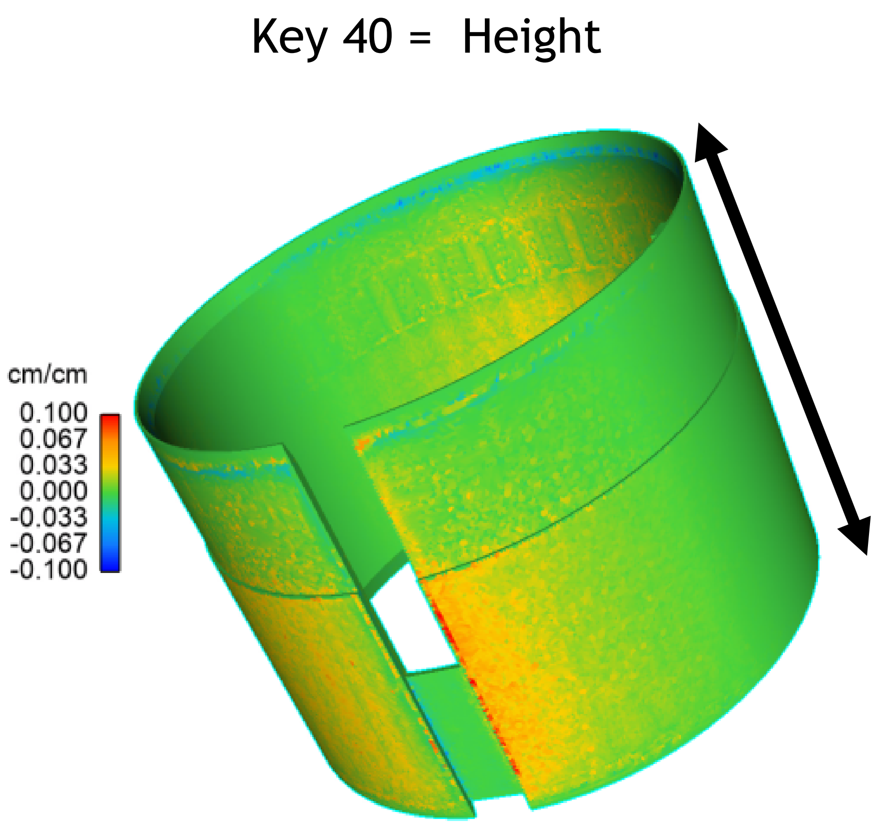


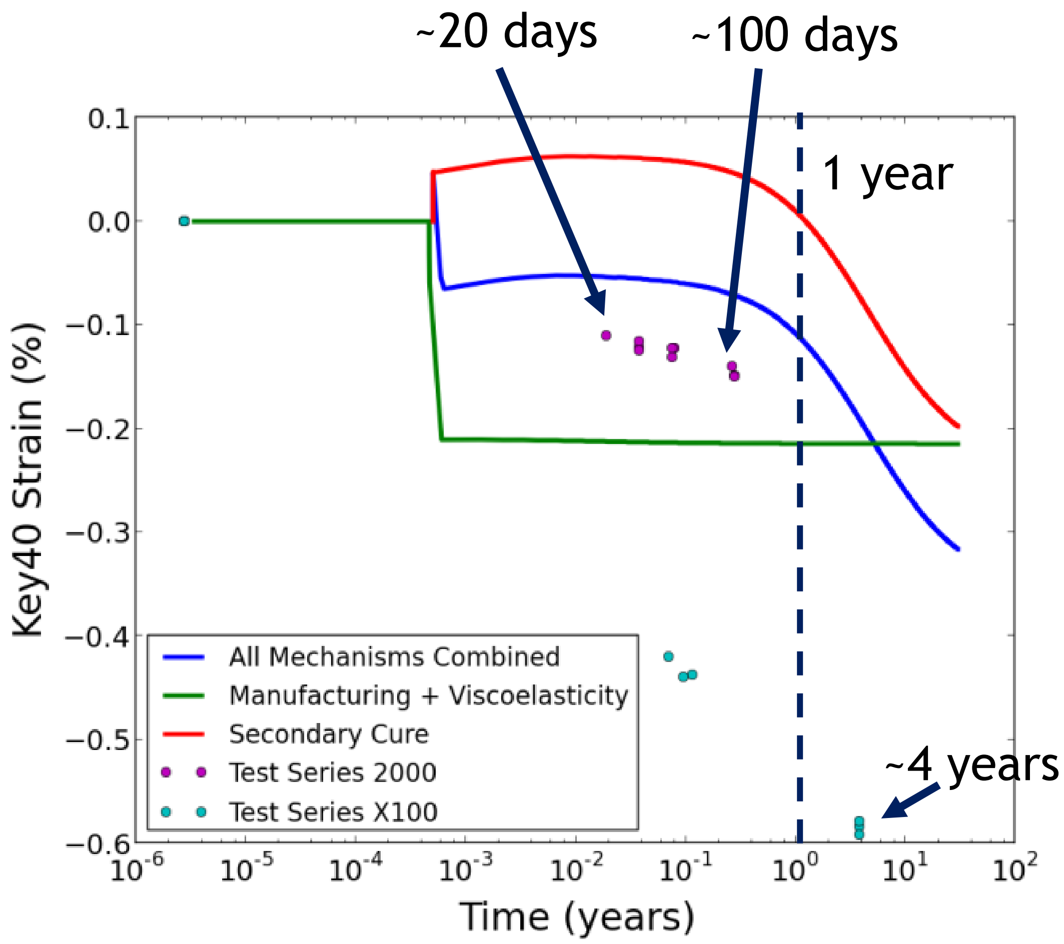
Key 10 = Outer Diameter at bottom

Key 40 = Height (distance between top surface and bottom surface)

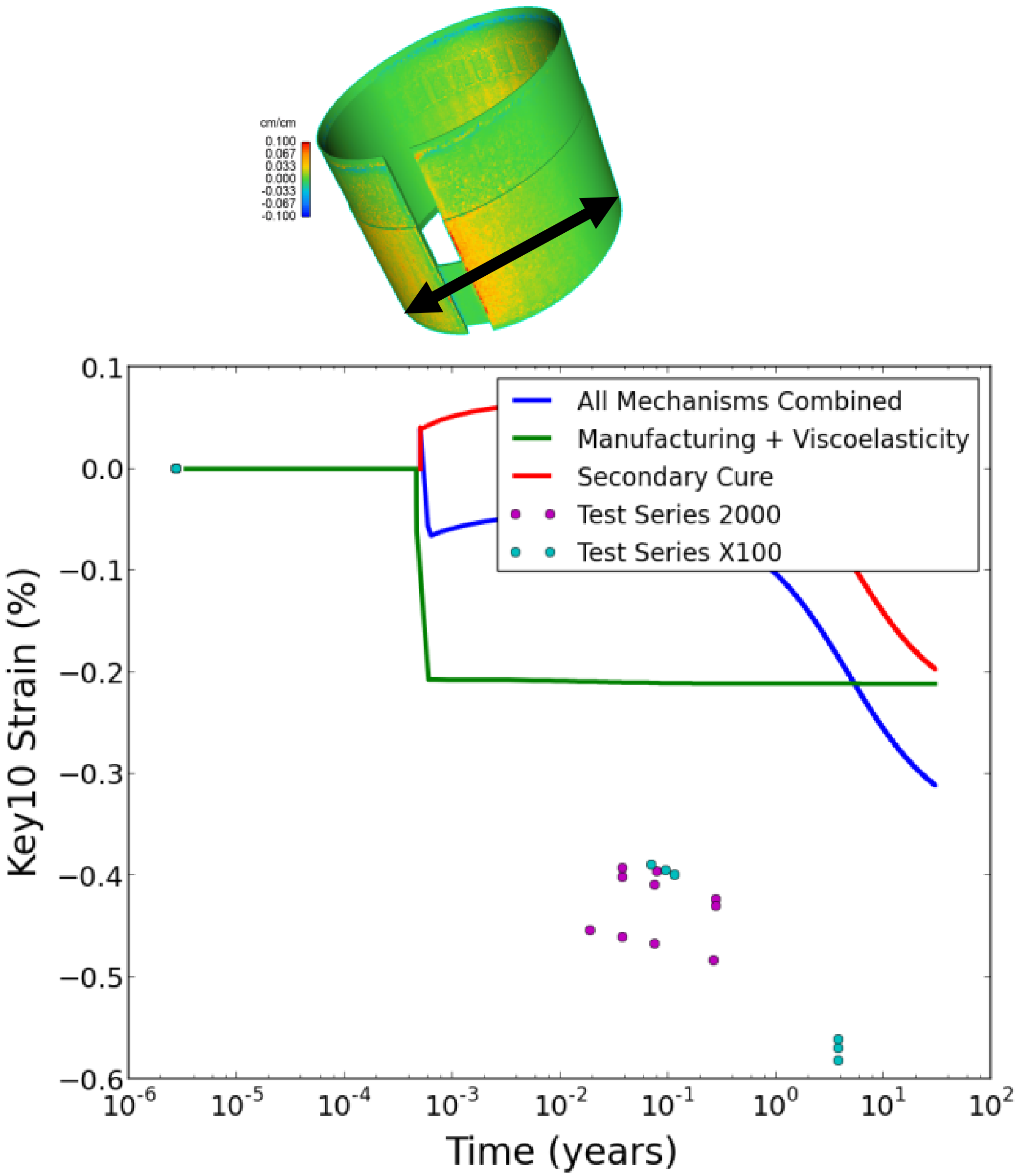


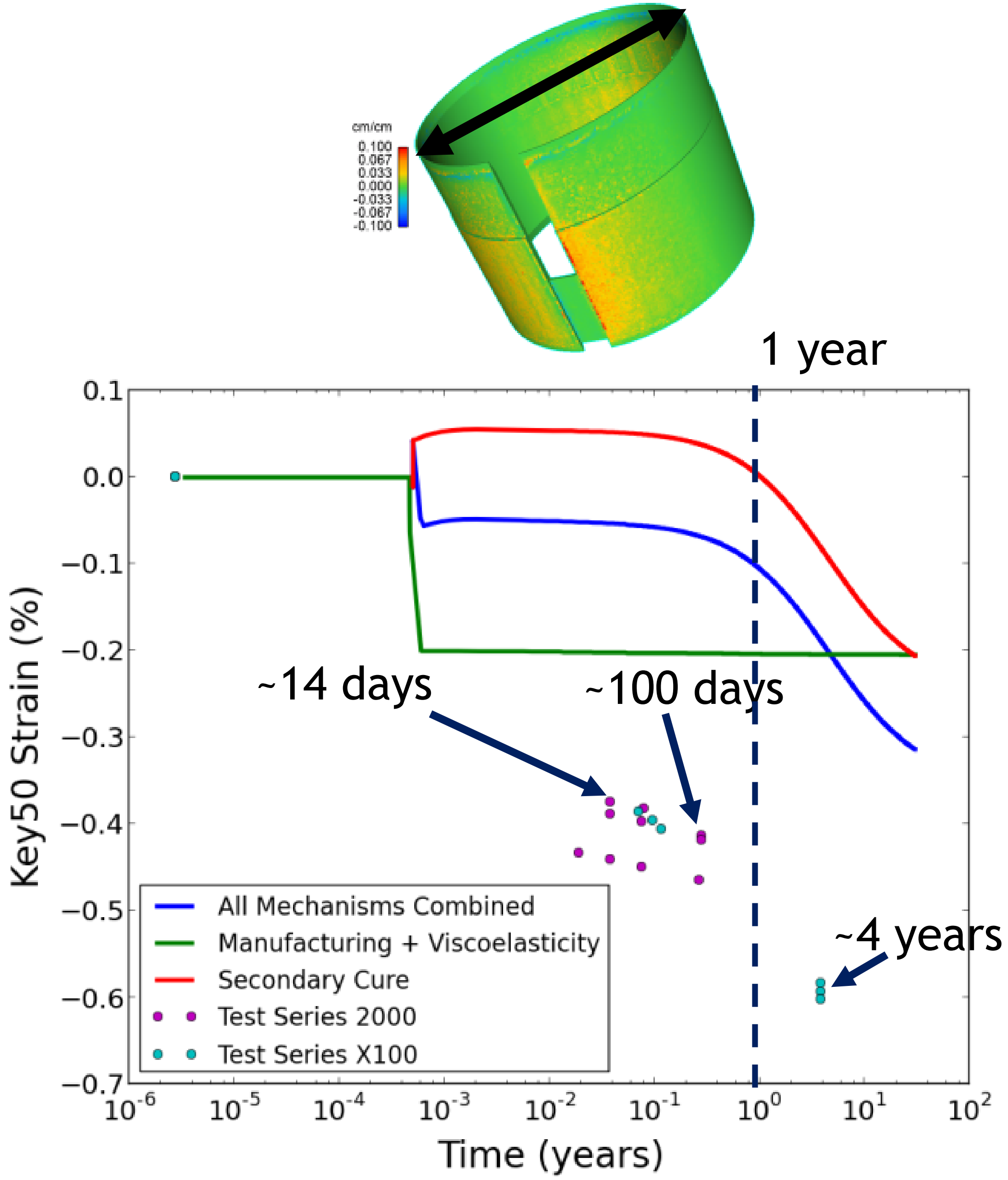
Structural Foam Part Predictions: Height





Structural Foam Part Predictions: Diameter





Conclusions

- Multiple sources contribute to shrinkage of PMDI foams
- Long-term (months) dimensional changes are due to isocyanate reacting with water.
- Pre-aging foamed parts with a humidity treatment could remove excess isocyanate and make them dimensionally stable against additional chemical shrinkage
- However, water swelling, though reversible, can be significant

Phenomenon	Time Scale	Strain (%)
Thermal contraction	Hours	~0.1% from 120 C to RT depending on density
Water Swelling	Hours	~2.1%
Depressurization	Days/Weeks	~0.02% depending on density
Isocyanate reaction	Weeks/years	~0.05% depending on density
Viscoelastic relaxation (Physical aging)	Decades	Very small

Conclusions

- A new kinetic model of post-cure reactions was developed (second order in NCO and water concentration with plasticization from water)
- The time scale for cure shrinkage is highly dependent on the water environment and temperature seen by the part.
- For our dry oven and 10% RH boundary conditions, we see shape change continuously for 30 years, though it slows after about 12 years.

Thank you for your attention!