

Estimating electron density, electron temperature, and signal-to-noise ratio from laser-collision induced fluorescence data by treating the measurement as a stochastic process

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I. Abstract

Diagnostic measurements are inherently stochastic. Using Gaussian statistics, we demonstrate estimation of electron density (n_e), temperature (T_e), and the signal-to-noise ratio (SNR) in 2-D in a cathodic arc (30 mTorr He) and the positive column of a DC discharge (500 mTorr He) using Laser-collision induced fluorescence (LCIF) data.

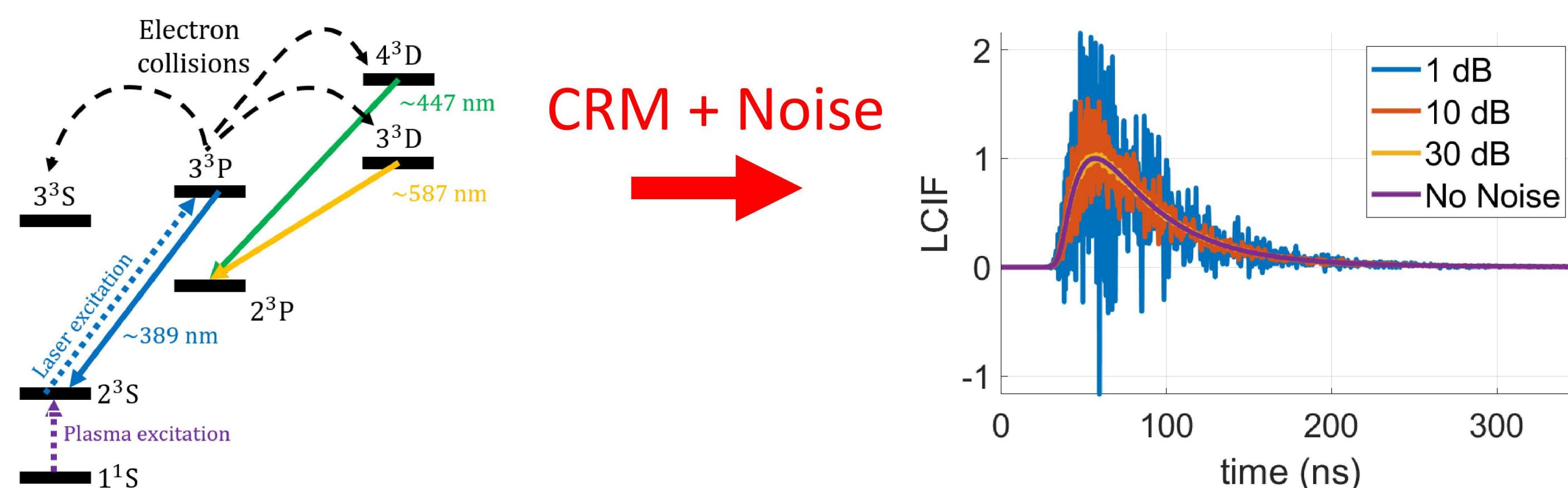
II. LCIF Diagnostic Measurement Model

- He atomic system described by collisional radiative model (CRM), $\mathbf{f}(n_e, T_e)$ [1]
- Shot noise for measured photodetector current, \mathbf{y} , is described by Gaussian statistics [2]

$$p(\mathbf{y}) = \frac{1}{[(2\pi)^P |\mathbf{Y}|]^{1/2}} \exp \left[-\frac{1}{2} \|\mathbf{y} - w\mathbf{f}(n_e, T_e)\|_{\mathbf{Y}^{-1}}^2 \right]$$

- Noisy measurements can be simulated from covariance, $\mathbf{Y}_{ii} = \sigma^2$, and SNR

$$\mathbf{y} = \mathbf{y} + \sigma N(0, 1) \quad \text{SNR} = \frac{[\mathbf{f}(n_e, T_e)]^2}{\sigma^2}$$



III. Parameter Estimation and Simulated Detection Limits

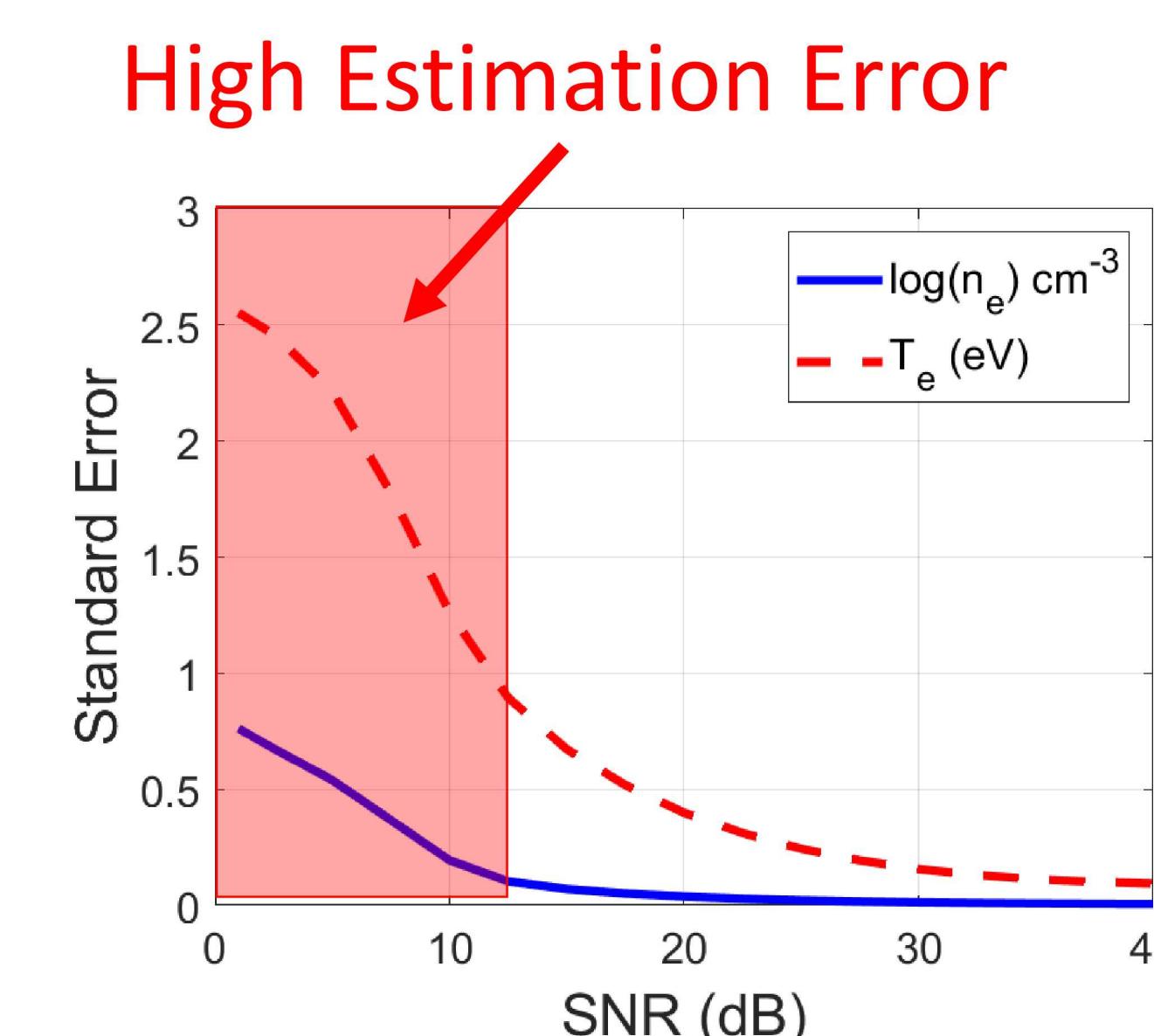
- Model enables estimation of $\mathbf{x} = [n_e, T_e]$ [3]

$$c(\mathbf{x}) = \|\mathbf{y} - \tilde{w}\mathbf{f}(\mathbf{x})\|_{\mathbf{Y}^{-1}}^2 \quad \tilde{w} = \frac{\mathbf{f}^T(\mathbf{x})\mathbf{Y}^{-1}\mathbf{y}}{\mathbf{f}^T(\mathbf{x})\mathbf{Y}^{-1}\mathbf{f}(\mathbf{x})}$$

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} c(\mathbf{x}) \quad \hat{w} = \tilde{w}(\hat{\mathbf{x}})$$

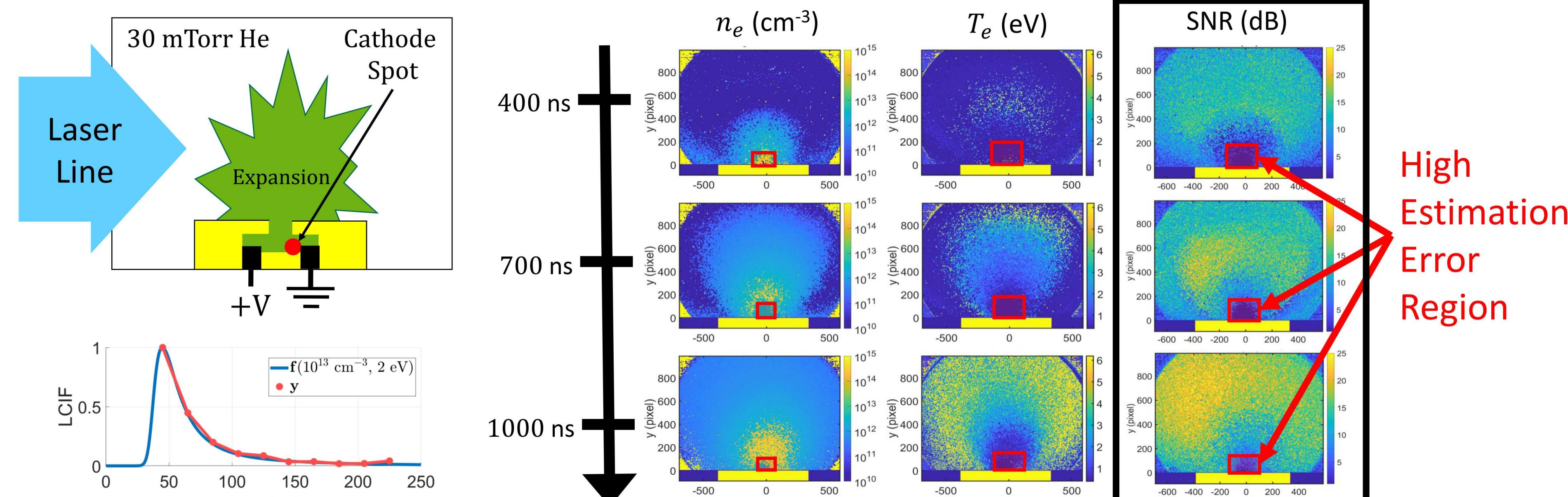
- SNR determined by estimating σ^2

$$\text{SNR} = \frac{\mathbf{f}(\mathbf{x})}{\left[\frac{1}{N} \|\mathbf{y} - \hat{w}\mathbf{f}(\hat{\mathbf{x}})\|_{\mathbf{Y}^{-1}}^2 \right]}$$

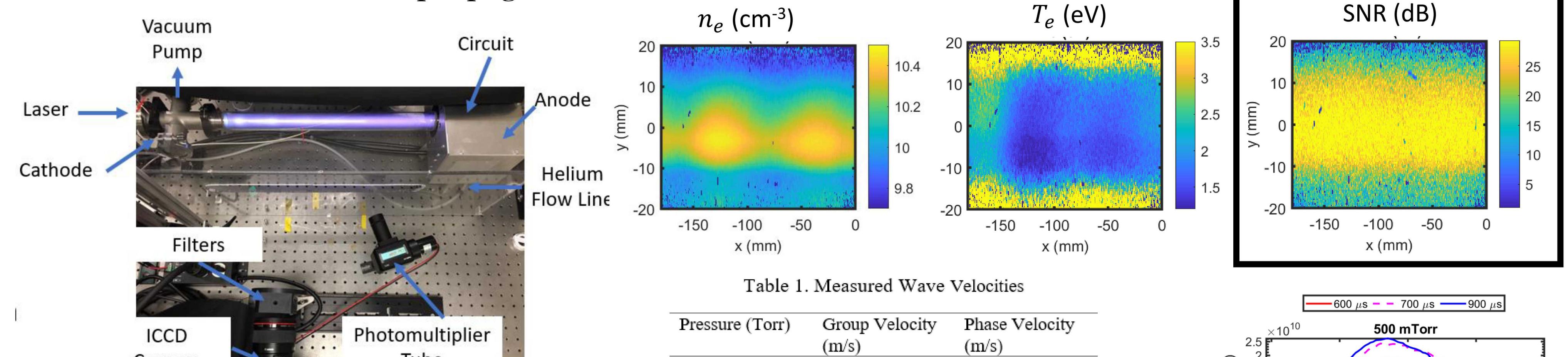


IV. Results

- Localized estimation of n_e and T_e in a cathodic arc expanding into 30 mTorr of He
- Fast electrons at expansion front and cooler high density core observed



- Estimation of n_e and T_e in the positive column of a DC discharge (500 mTorr He)
- Ionization wave propagation and radial expansion observed



V. Conclusions

Maximum likelihood estimation of n_e , T_e , and SNR in 2-D is possible using a CRM and Gaussian statistics. The SNR provides a useful metric for establishing regions of diagnostic validity.

References

- [1] E. V. Barnat and K. Frederickson, *Plasma Sources Sci. Technol.* 19(5), 055015 (2010)
- [2] J.-C. Ye, K. J. Webb, C. A. Bouman, and R. P. Millane, *J. Opt. Soc. Am. A* 16(10), 2400 (1999)
- [3] B. Z. Bentz, D. Lin, and K. J. Webb, *Phys. Rev. Appl.* 10(3), 034021 (2018)

