



The modelling and 3D printing of functionally graded foams for tunable crushing performance

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Outline

- **Background/Motivation**
- **Goals**
- **Results**
 - Numerical/experimental approach
 - Model fitting and comparisons
 - Design space exploration
- **Conclusions**

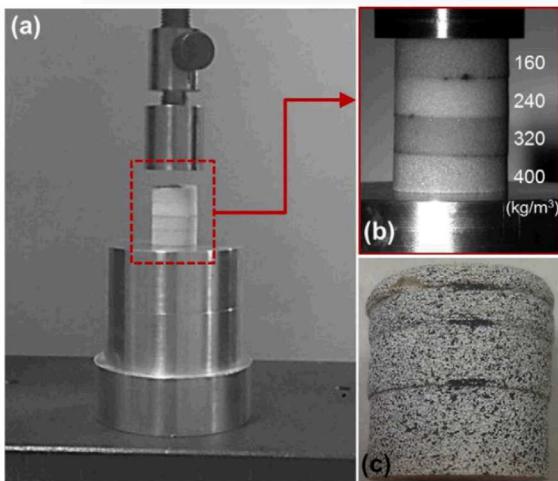
Acknowledgements

- **Sandia National Labs**
- **AFOSR, FA-20-1-0306, FA9550-19-1-0151.**

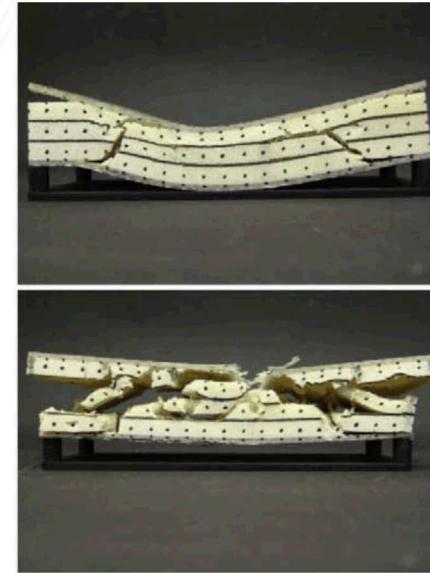
- This work was partially supported by the Laboratory Directed Research and Development program at Sandia National Laboratories. Sandia National Laboratories, a multimission laboratory managed and operated by National Technology and Engineering Solutions of Sandia LLC, a wholly owned subsidiary of Honeywell International Inc. for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.
- We also thank the Air Force Office of Scientific Research for Grant AFOSR, FA-20-1-0306, FA9550-19-1-0151.

Motivation

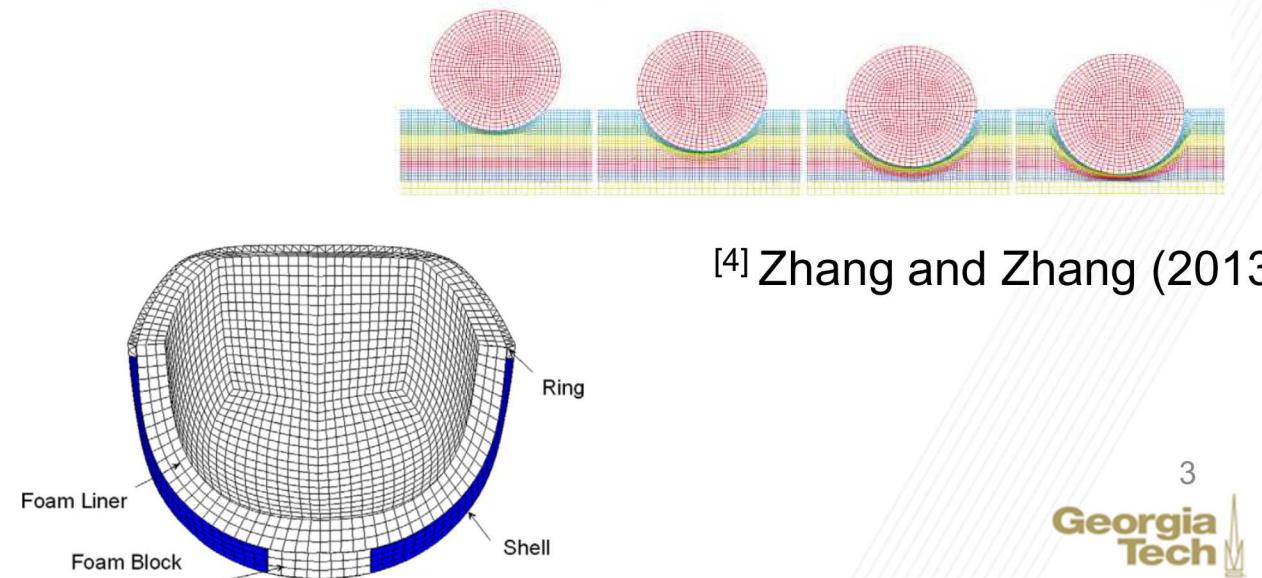
- **Most safety/packaging applications require designing for a variety of impact scenarios**
- **FGFs are introduced to overcome limitations of uniform foams**
- **FGFs have their own limitations**
 - **Little microstructural control, limited to simple gradients, large design space, hard to model accurately**



[1] Koohbor and Kidane (2016)



[2] Wang *et al.* (2009)

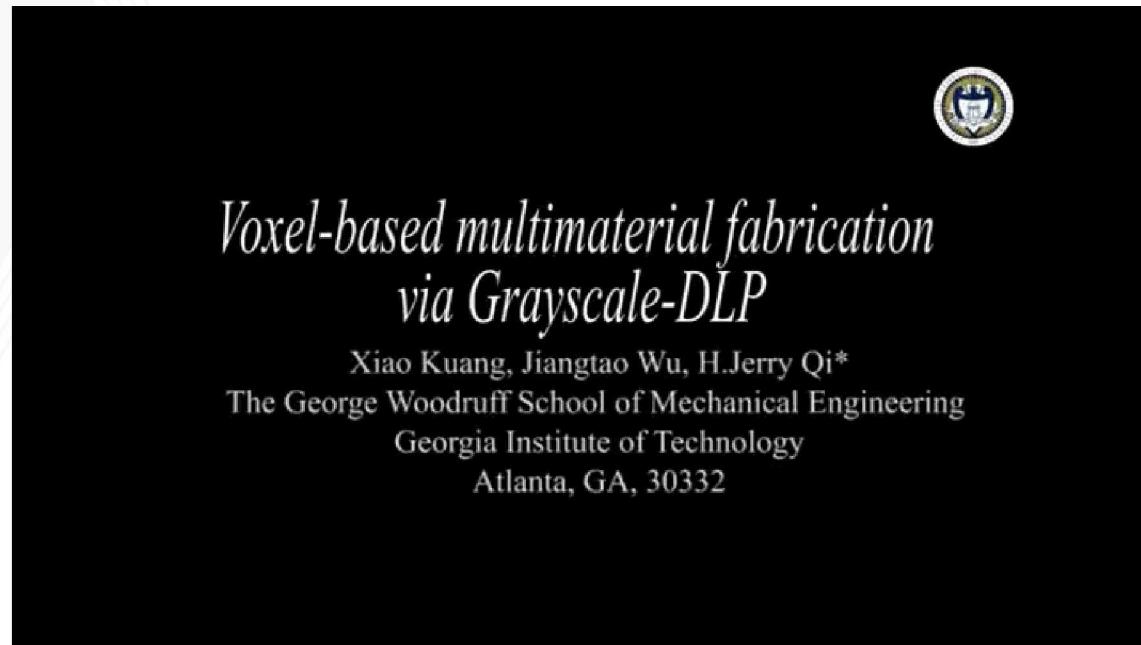


[3] Cui *et al.* (2009)

[4] Zhang and Zhang (2013)

Grayscale Digital Light Processing (g-DLP)

- In DLP, a projector shines light onto a build platform submerged in resin
- Build platform is slowly lowered into the resin, building the final part layer-by-layer
- The brightness of each image will determine the material properties



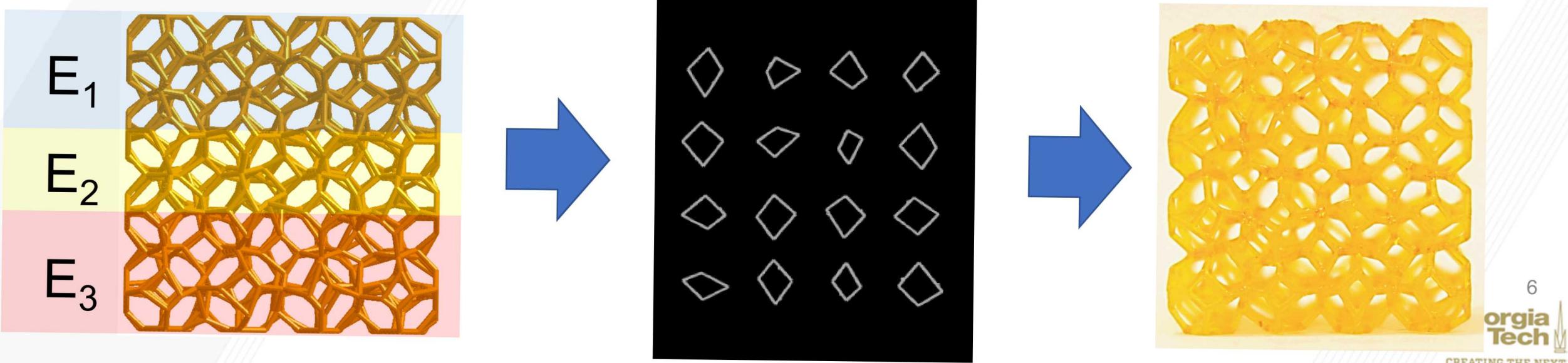
[5] Kuang *et al.* (2019)

Goals

- **Develop a numerical model that can accurately predict the response of 3D-printed viscoelastic foams**
- **Use this model to better understand the benefits of FGFs**
- **Use this model to explore the graded foam design space**
- **Display its usefulness as a design guide to select the right foam for a certain use case**

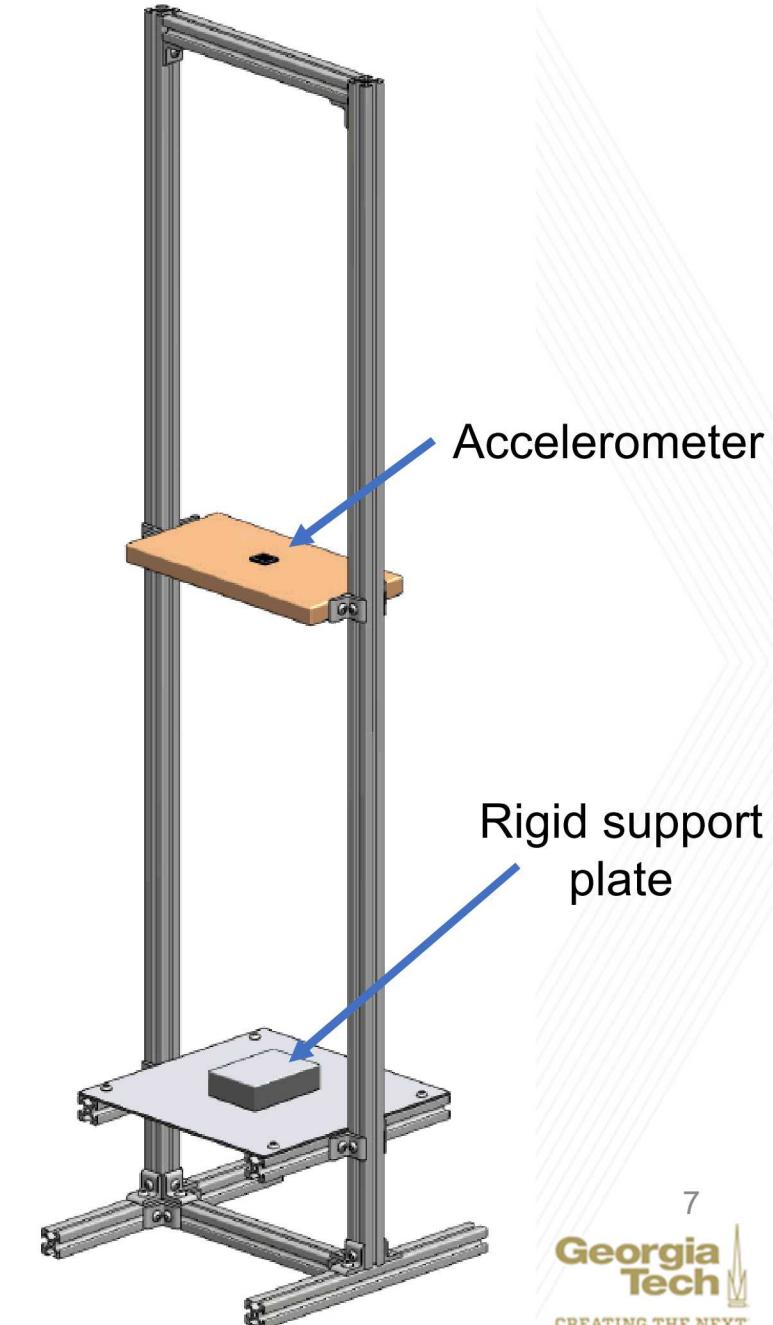
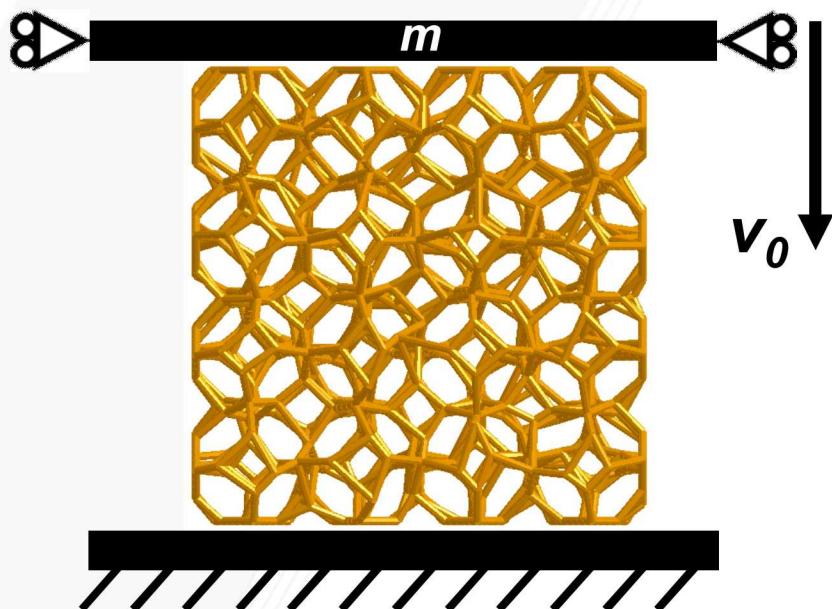
Grayscale Foam Structure

- Modeled as Kelvin cells with uniform circular beam cross-sections
- Arranged as 4x4x4 cell RVEs
- Cell vertices are randomly perturbed
- Graded foams are assigned 3 properties



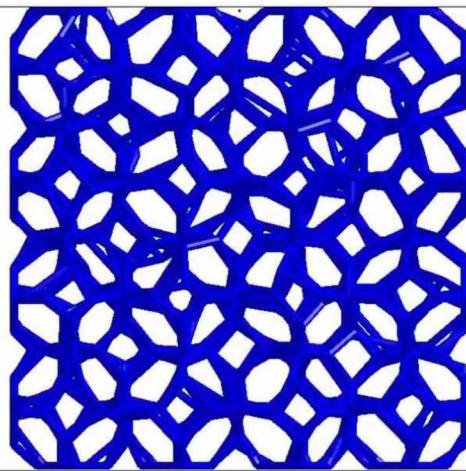
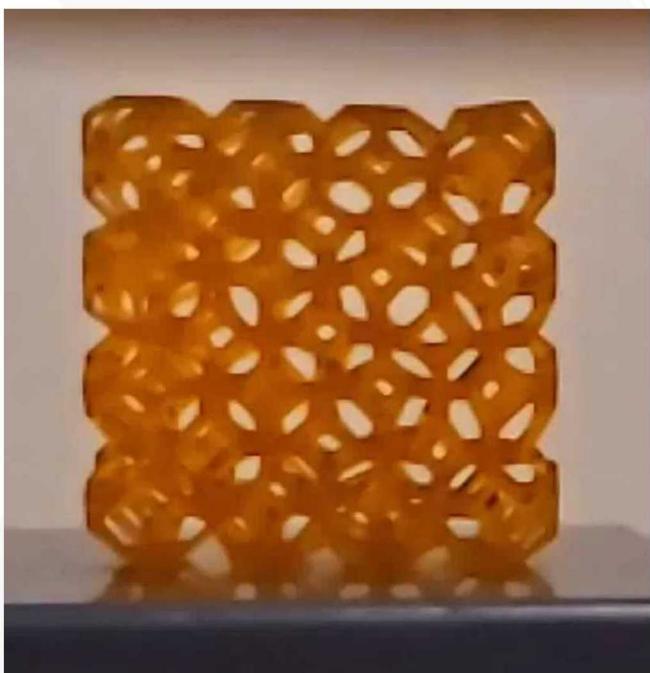
Testing Configuration

- A plate of prescribed mass m and initial velocity v_0 is dropped onto a foam
- Bottom plate has a rigid boundary
- In the experimental setup, the mass is fixed, and the velocities represent a height of 1ft or 3ft

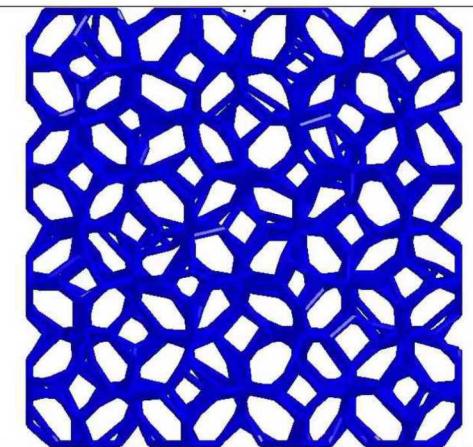
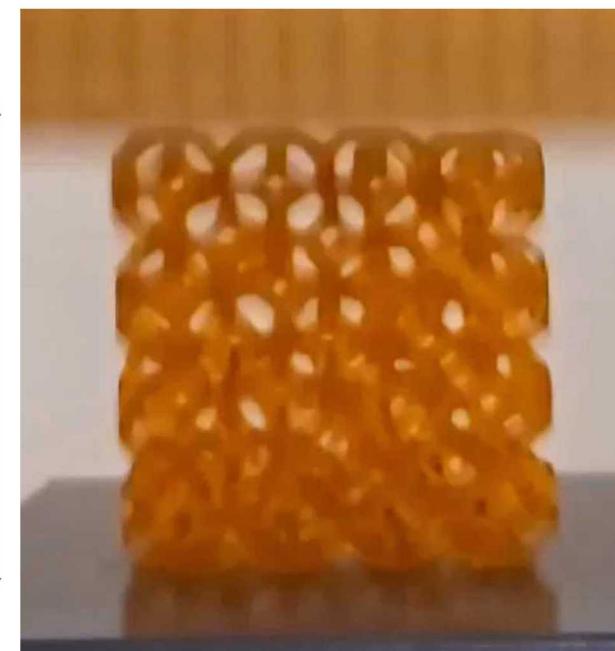


Model Qualitative Comparisons

4.23m/s

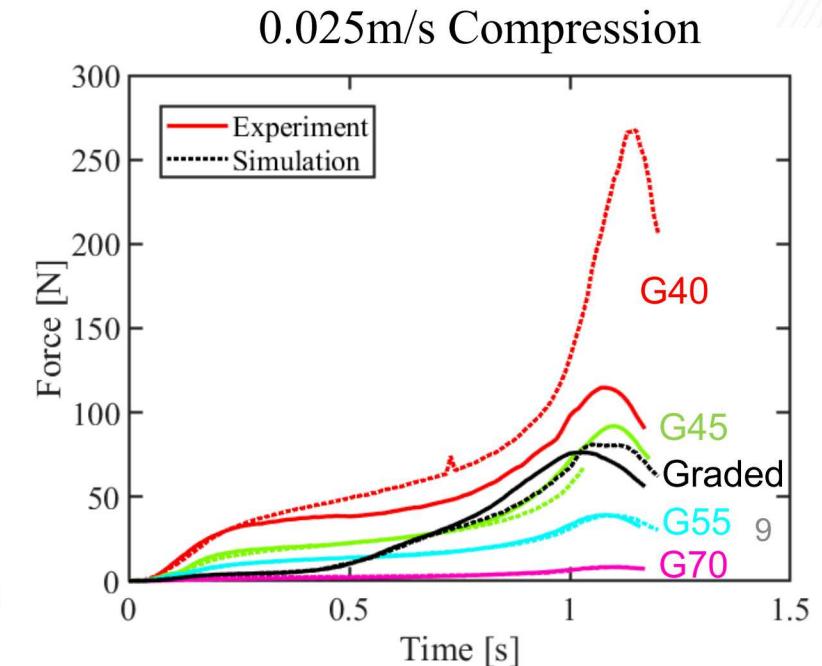
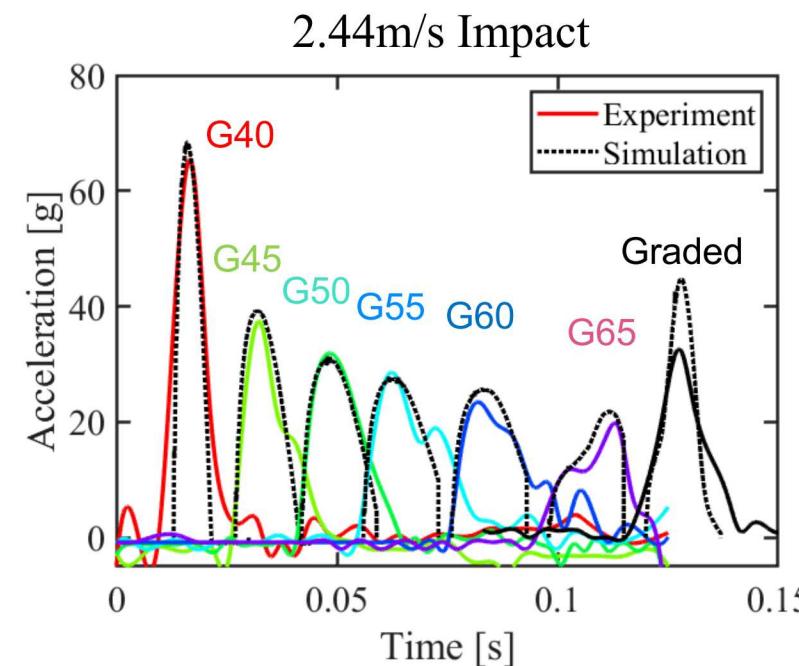
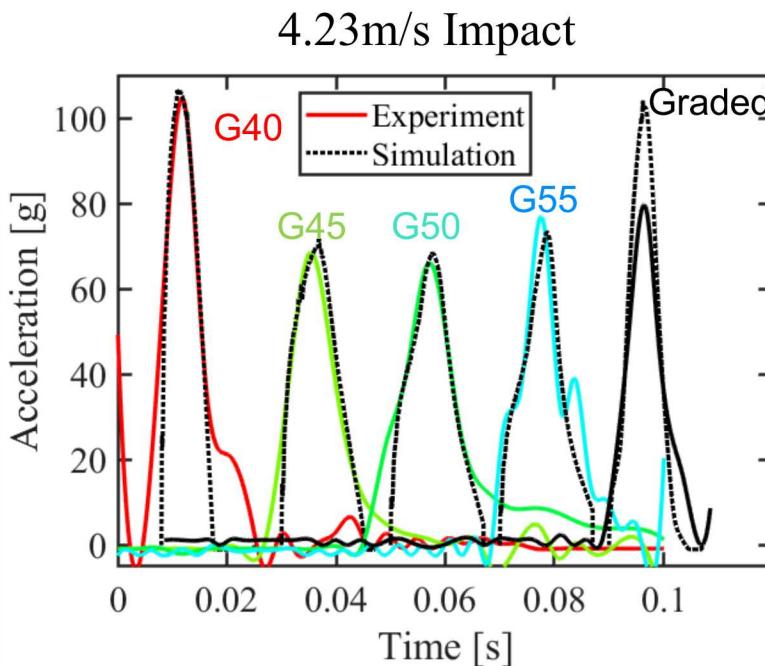


2.44m/s



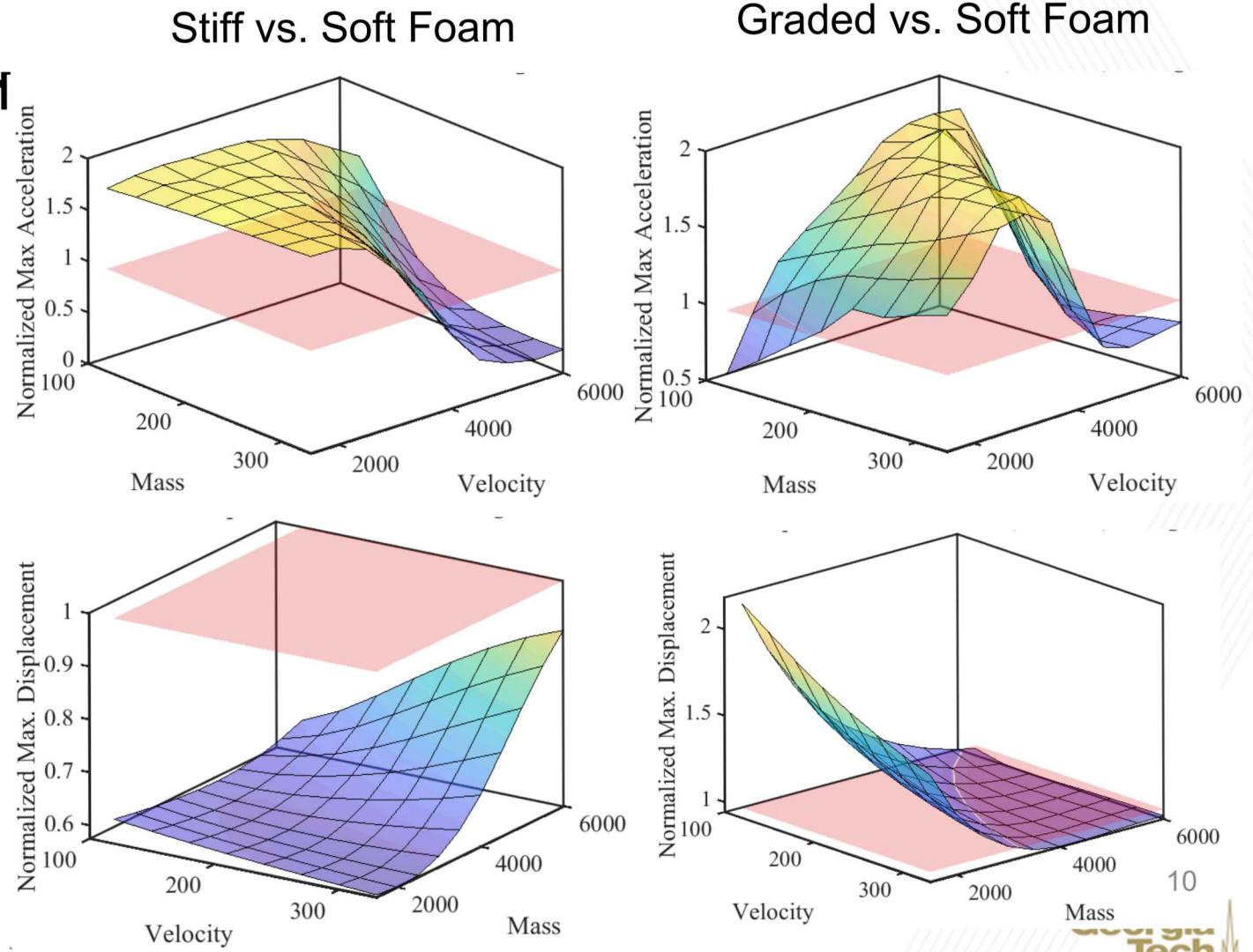
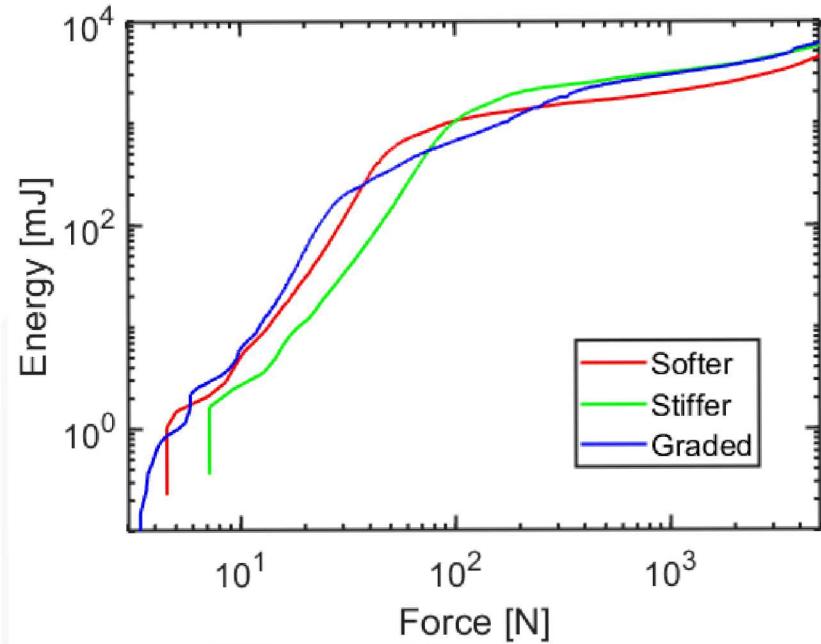
Model Quantitative Comparisons

- The viscoelastic data is fit to the model at multiple strain rates
 - 170x difference in fastest and slowest rates
- This strong agreement gives us confidence in our properties



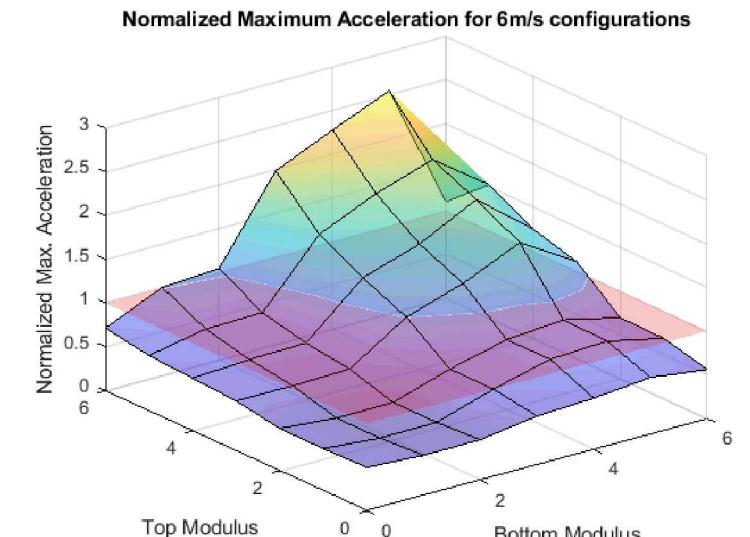
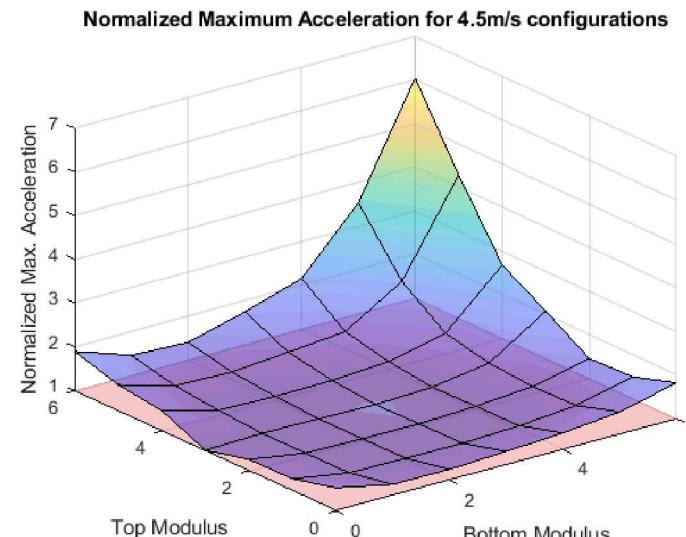
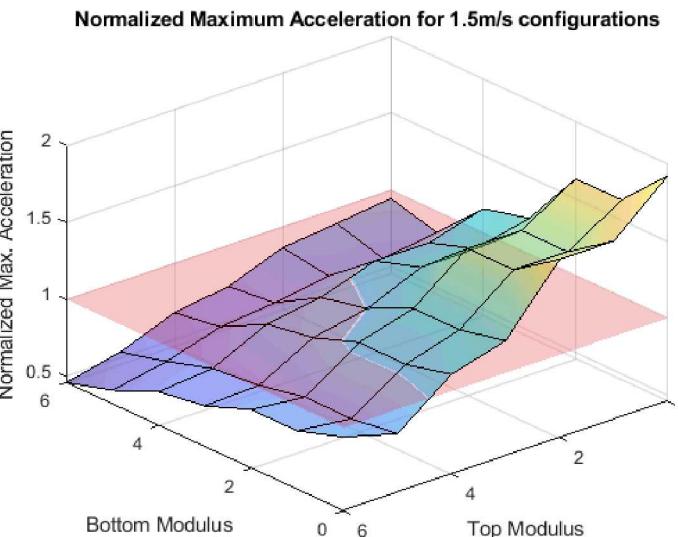
Exploring the Design Space

- This accurate model give us insight the performance of graded foams



Design Application

- The accurate model allows us to also explore graded configurations we have not printed and compare them

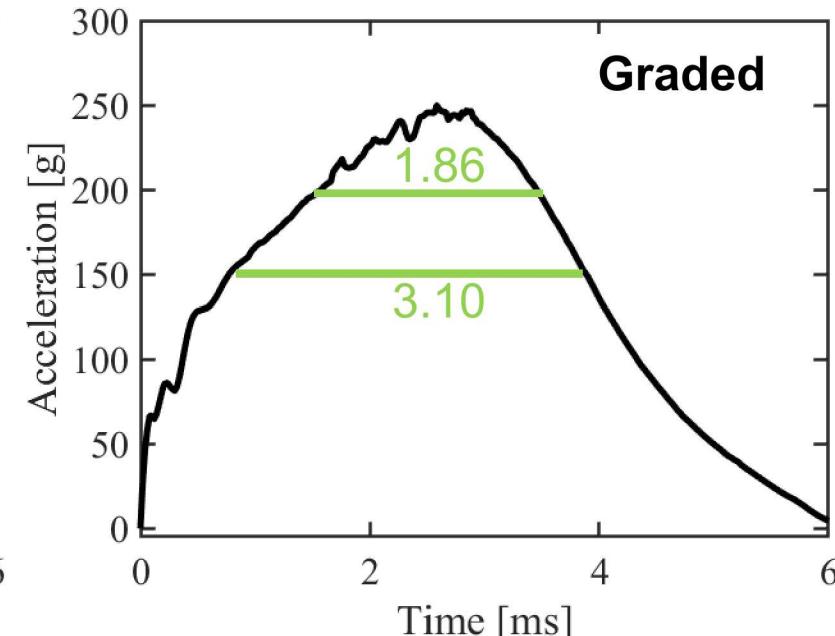
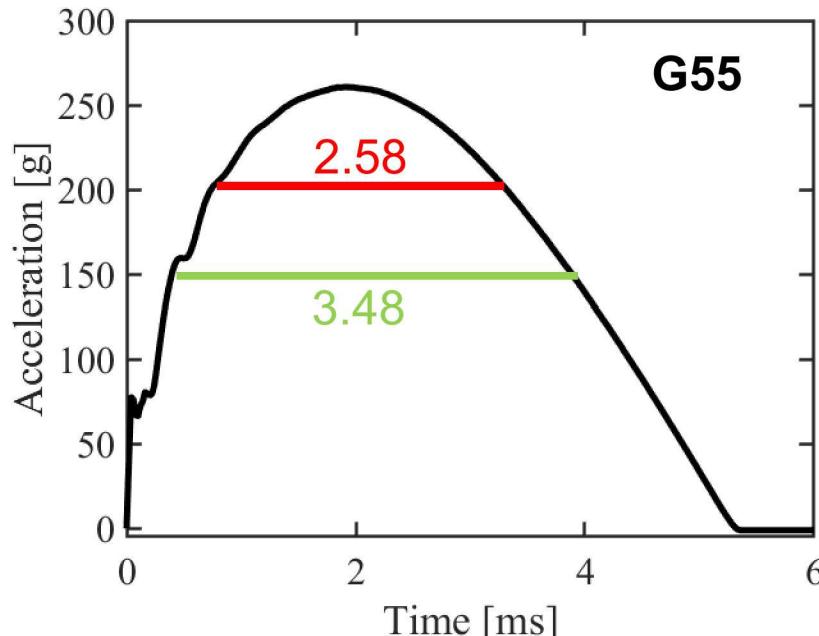
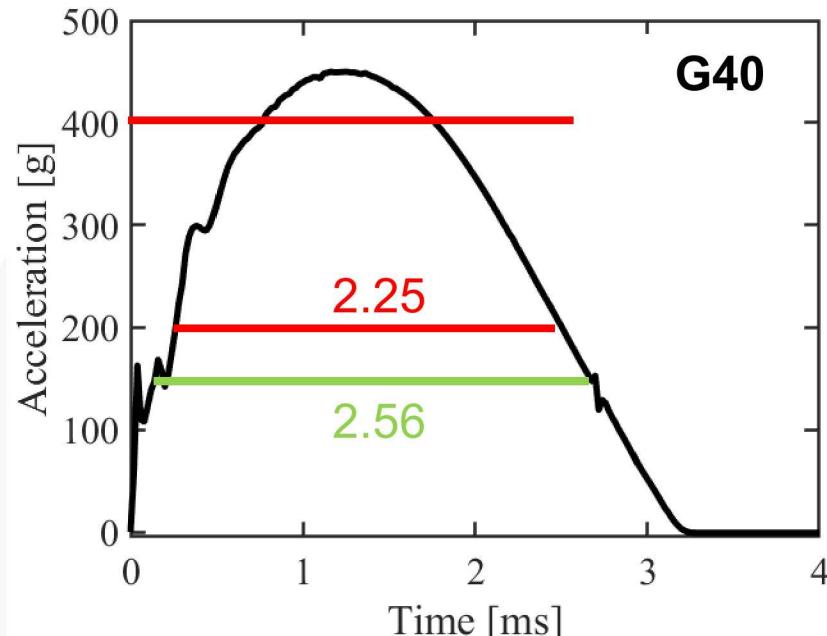


Helmet Design Scenario

- Simulations Performed in accordance with National Highway Traffic Safety Administration (NHTSA) Test Procedure TP-218-07

Test Parameters	
Mass	4.9 – 5.1kg
Velocity	5.8 – 6.2m/s
400g Limit	0ms
200g Limit	< 2ms
150g Limit	< 4m/s

[6] TP-218-07 (2011)



Conclusions

- A beam element model can be used to accurately predict highly viscoelastic foam responses across wide range of strain rates
- Property gradients decrease the maximum efficiency but extend the effective range of foams
- This model can be used to explore the design space to predict relative performance like a design guide

Citations

1. Koohbor, B. and A. Kidane (2016). "Design optimization of continuously and discretely graded foam materials for efficient energy absorption." Materials & Design 102: 151-161.
2. Wang, E., et al. (2009). "The blast resistance of sandwich composites with stepwise graded cores." International Journal of Solids and Structures 46(18): 3492-3502.
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4. Zhang, X. and H. Zhang (2013). "Optimal design of functionally graded foam material under impact loading." International Journal of Mechanical Sciences 68: 199-211.
5. Kuang, X., et al. (2019). "Grayscale digital light processing 3D printing for highly functionally graded materials." Science Advances 5(5): eaav5790.
6. (2011). **LABORATORY TEST PROCEDURE FOR FMVSS No. 218 Motorcycle Helmets.** D. o. Transportation, Office of Vehicle Safety Compliance

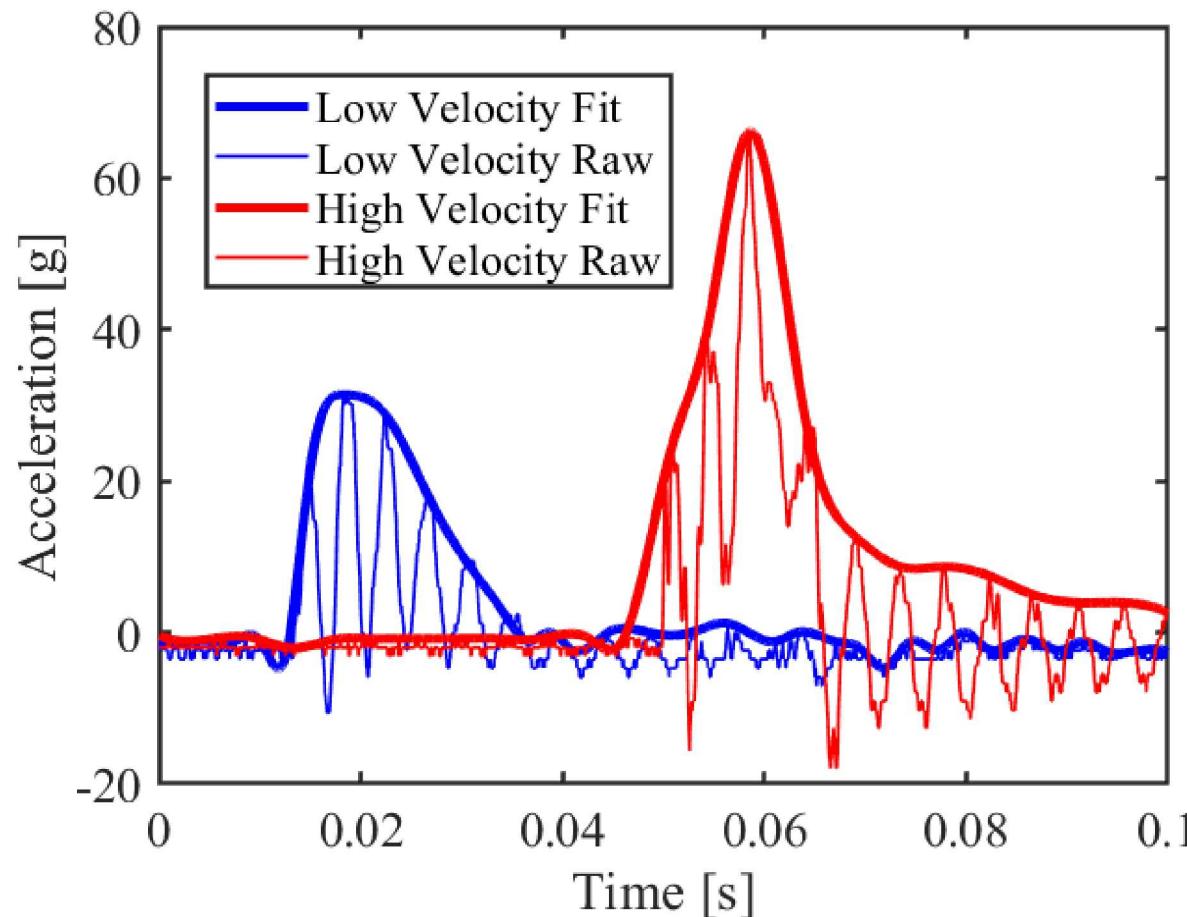
Thank you!

Questions?

Appendix

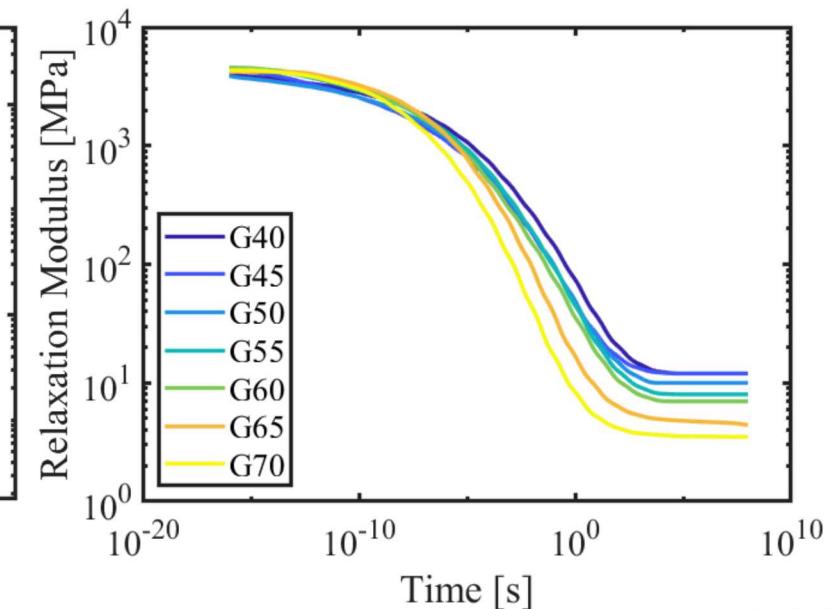
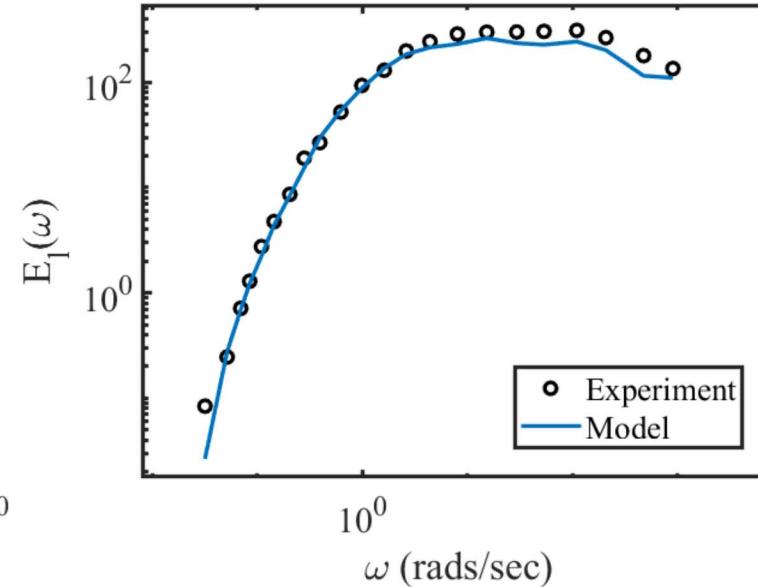
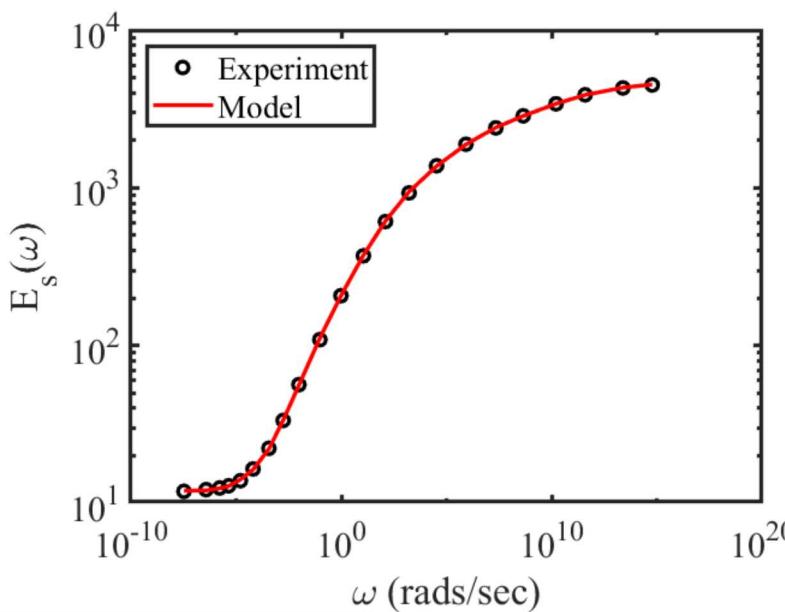
Acceleration Data Fitting

- Envelope function in MATLAB with window of 30 points



Material Property Characterization

- Individual grayscale materials analyzed under frequency sweep
- The Prony series branch moduli were determined by fitting the frequency-dependent storage and loss moduli



Headform size calculations

- **Top area is calculated as the area of the headform at the reference plane**
- **Side area is calculated as the profile area above the reference plane**

