



Finite Element Modeling of SS316 Pit Stability, with respect to Geometry Parameters, Under Atmospheric Conditions

R. Skelton Marshall,¹ R. M. Katona,^{1,2} M. A. Melia,² R. G. Kelly¹

¹ University of Virginia, Department of Material Science and Engineering

² Sandia National Laboratories

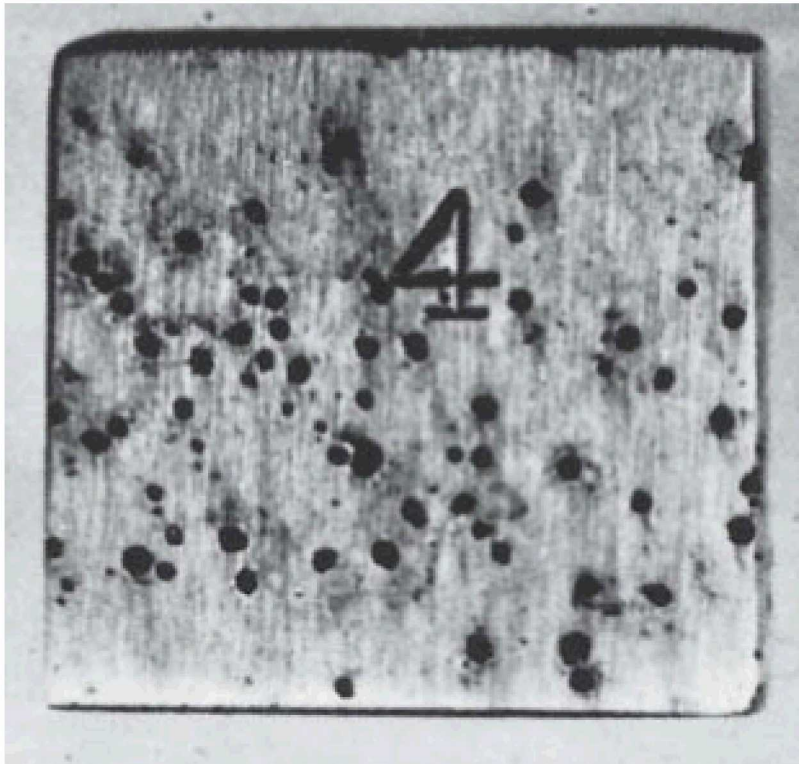
C06-1306: Atmospheric and Marine Corrosion, PRIME ECS 2020, Virtual, 10/5/2020 from 10:40 to 11am HST

Presenter email: rjs2wu@virginia.edu

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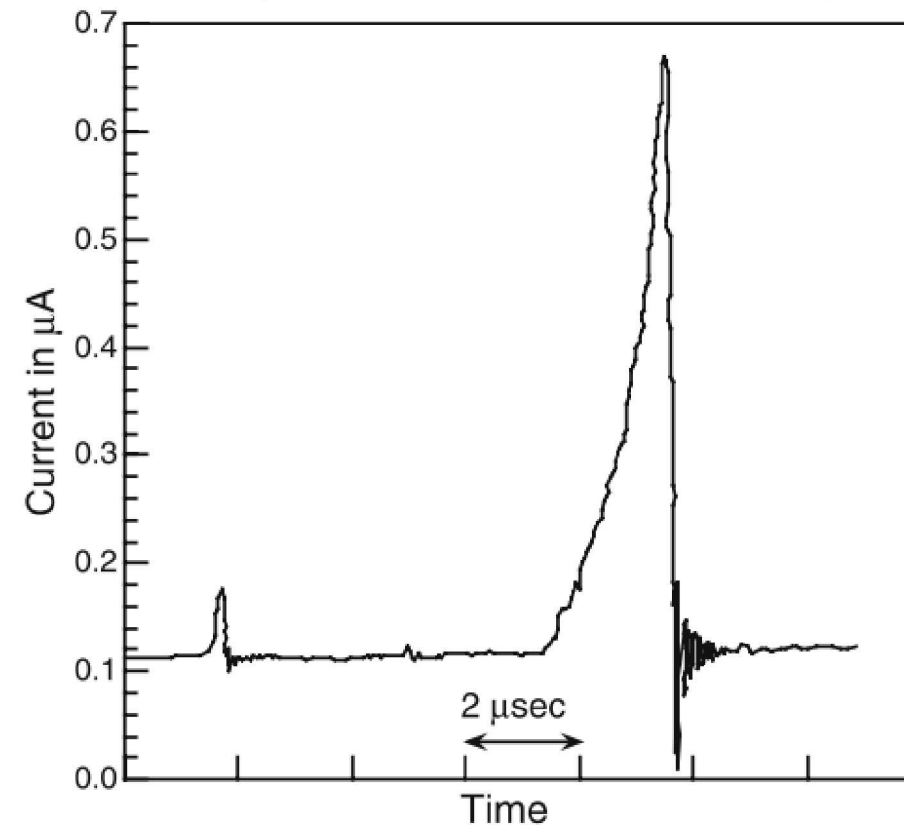
Pitting on Stainless Steels

Pitting on SS304



M. G. Fontana, Corrosion Engineering, 3rd edition.
1986 by McGraw-Hill Book Company

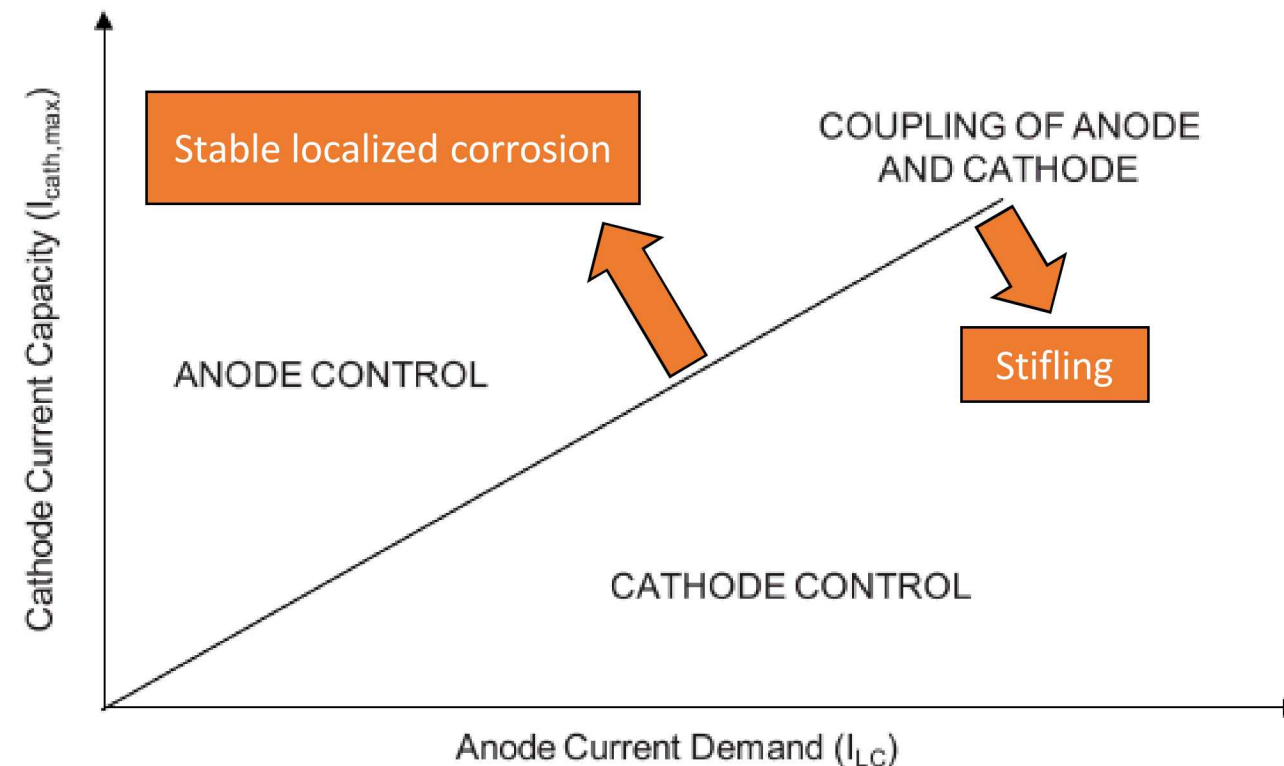
Pit Repassivation on SS302



E. McCafferty, Introduction to corrosion
science, Springer, 2010.

Pit Stability Background

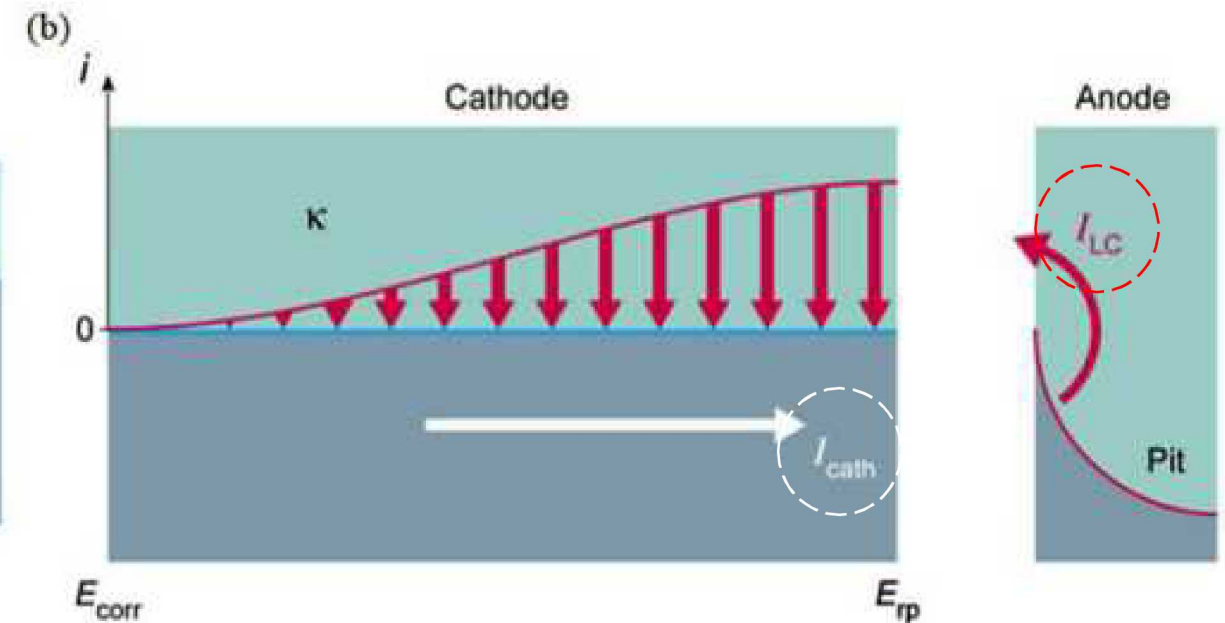
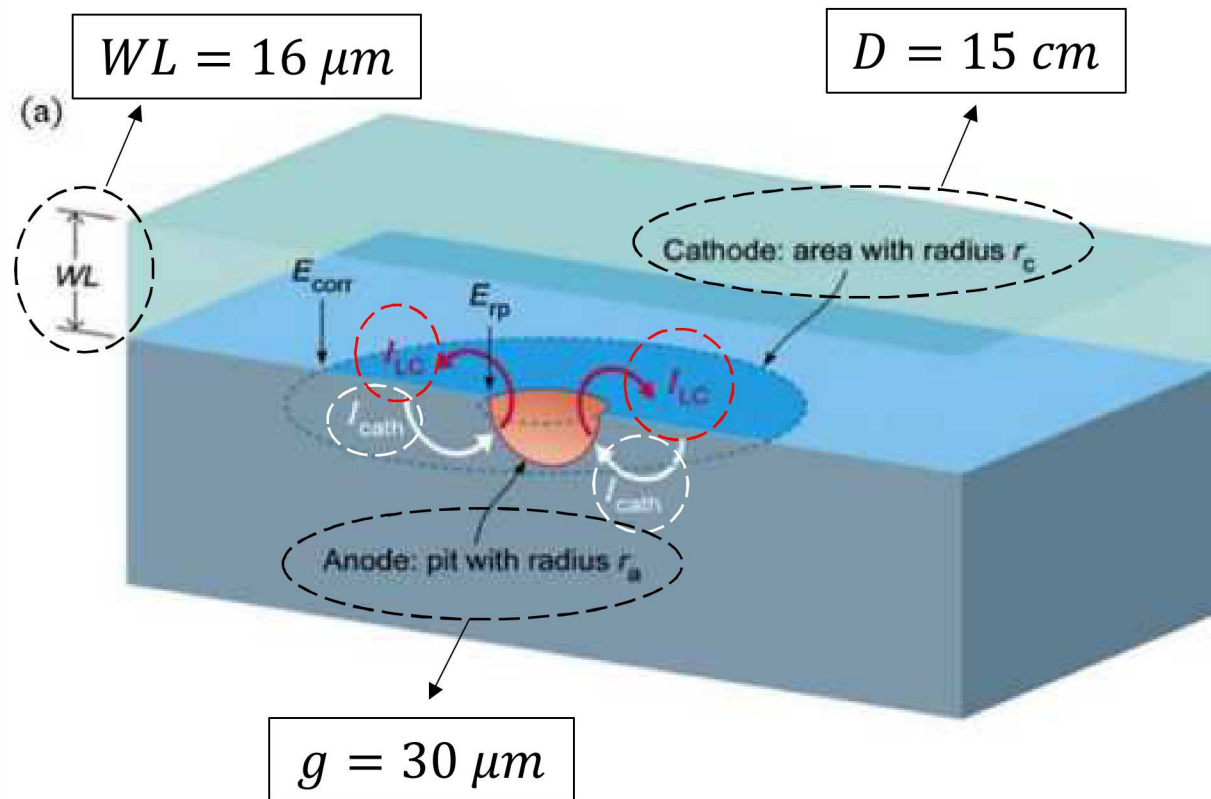
$$I_c = I_a$$



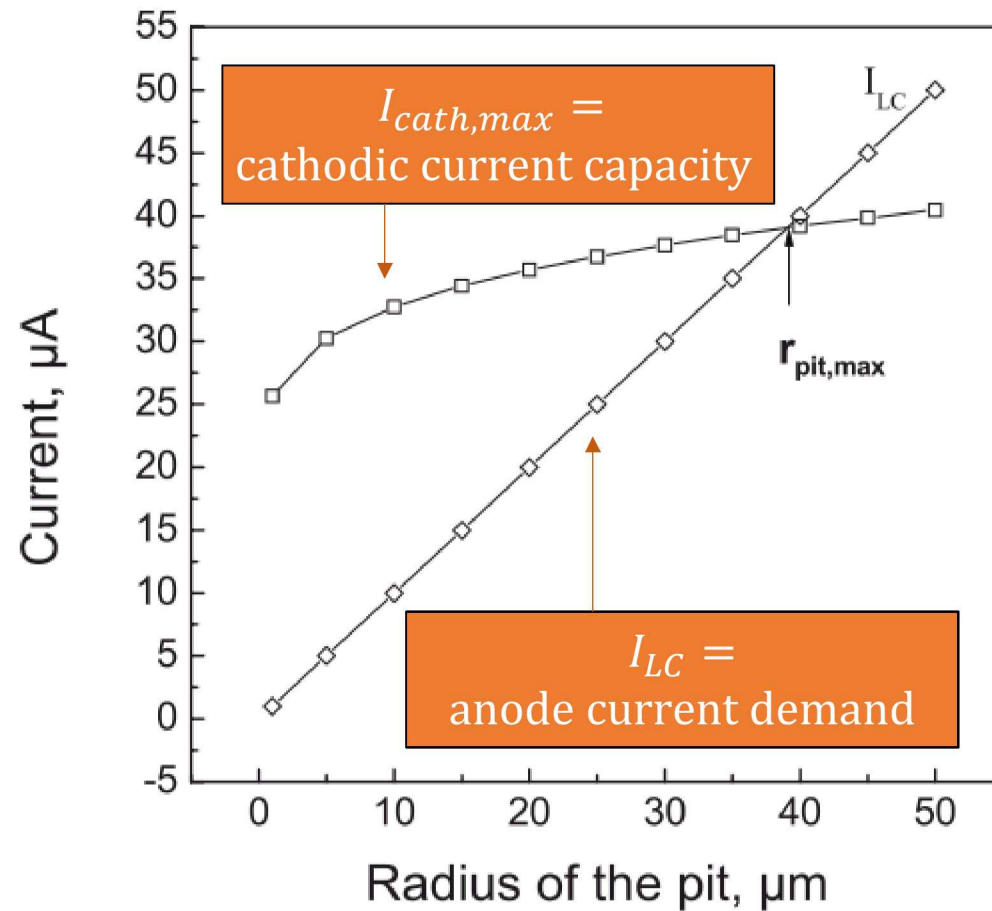
Determined through cathode kinetics and environmental factors

Determined through size of the pit, and pit stability product

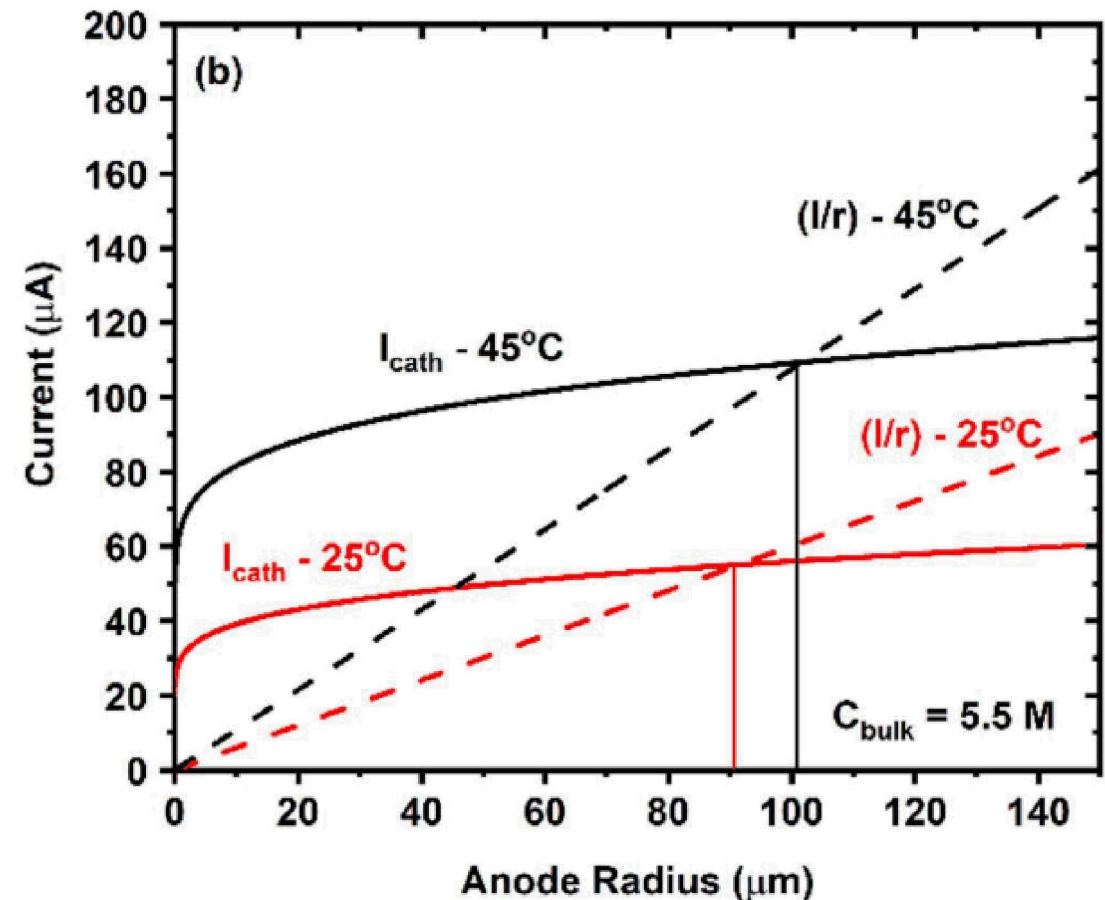
Pit Stability Background



Pit Stability Background



Z.Y. Chen, R.G. Kelly (2009)



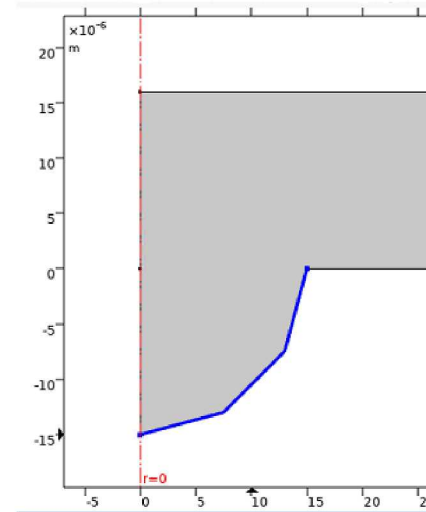
R.M. Katona, J. Carpenter, E.J. Schindelholz, R.G. Kelly (2019)

Motivation and Goals

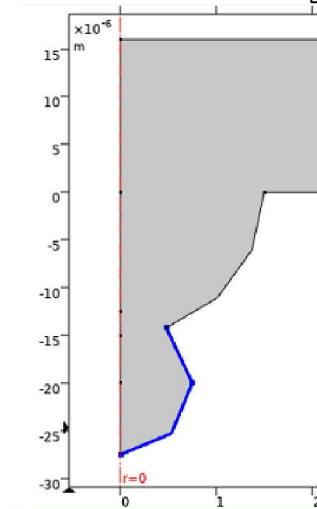
- Maximum pit model provides size bound, but
 - No time dependence
 - No pit geometry dependence
 - No insights into effects of cathodes smaller than maximum cathode
- Next step is time dependence of chemistry in a pitting system
 - Still must couple pit with external cathode
 - Apply pit stability criteria
 - Must implement potential-dependent pit kinetics and transport of species
- Current presentation
 - Initial development of modeling framework and application to a range of pit geometries and WL

Different Pit Geometries

- Consider three pit shapes:
 - Hemisphere (simple)
 - Double and undercutting pits (complex)
 - Under what conditions will these pits grow or repassivate?*
- $I_{cath,max}$ impact on stability
 - Water layer thickness change
- I_{LC} impact on stability
 - Pit geometry/size

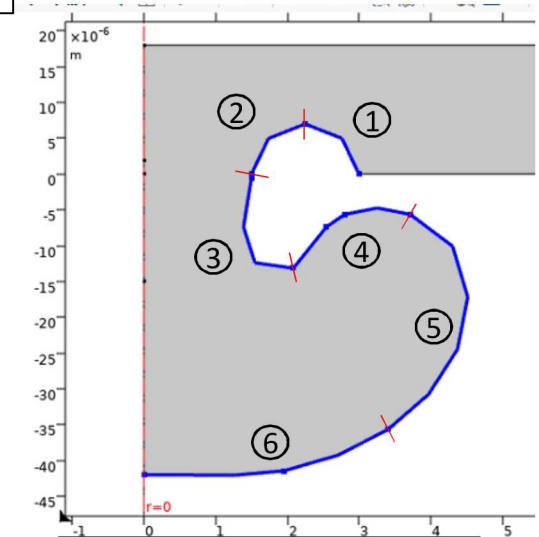


Hemispherical Pit



Double Pit

Represents active pit growing on "old" repassivated pit



Undercutting Pit

Represents undercut pit with corrosion product built up at pit mouth

Pit Stability Criteria

If Inequality is True, Then Pit Will Grow

1. $E_{\text{mouth}} > E_{\text{rp}}$

Criteria for all pits

2. $\left(\frac{i}{r}\right)_{\text{FEM, anode}} > \left(\frac{i}{r}\right)_{\text{max pit model}}$

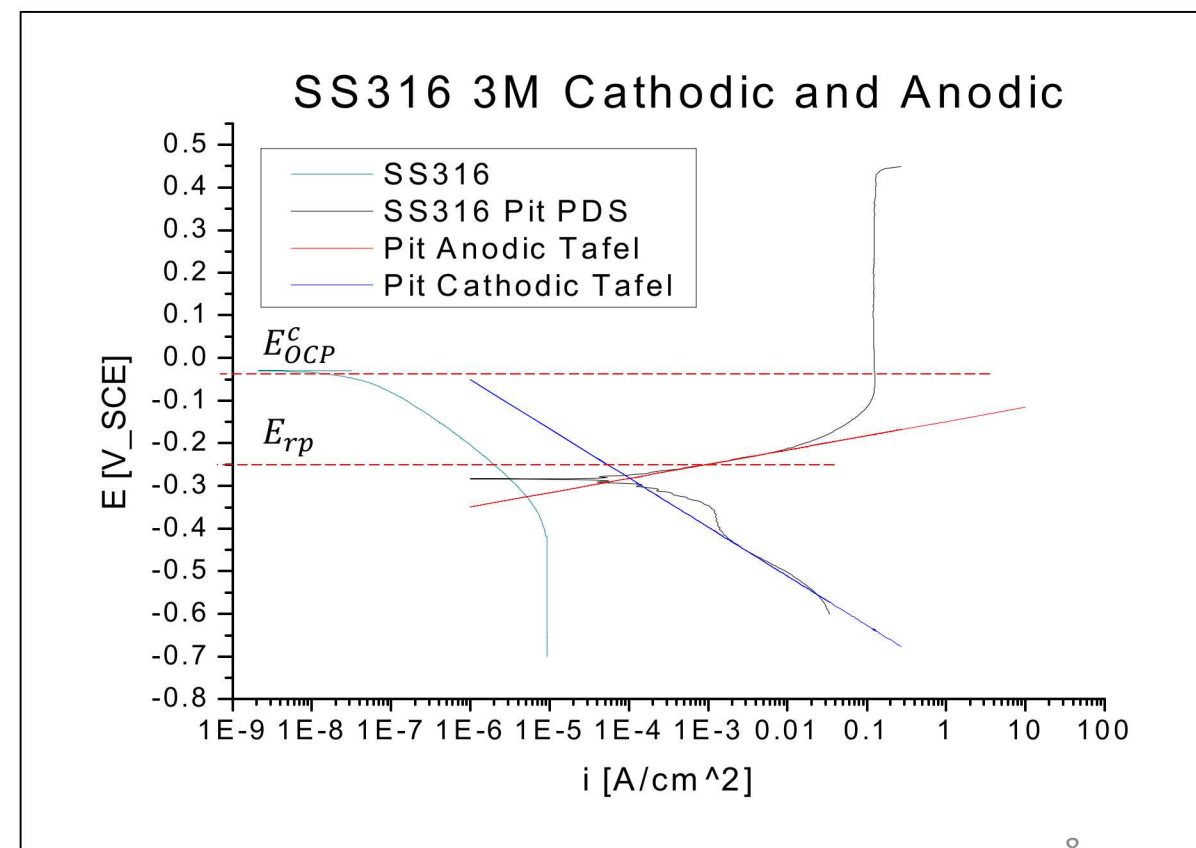
- $\left(\frac{i}{r}\right)_{\text{max pit model}}^{3M} = 0.8 \frac{\text{A}}{\text{m}}$

3. $[M^+]_{\text{FEM}} > [M^+]_{\text{critical}}$

- $[Ni^{2+}]_{\text{critical}} = 2048.84 \left[\frac{\text{mol}}{\text{m}^3} \right]$

- $[Cr^{3+}]_{\text{critical}} = 3213 \left[\frac{\text{mol}}{\text{m}^3} \right]$

- $[Fe^{2+}]_{\text{critical}} = 13,622.02 \left[\frac{\text{mol}}{\text{m}^3} \right]$



Pit Stability Criteria

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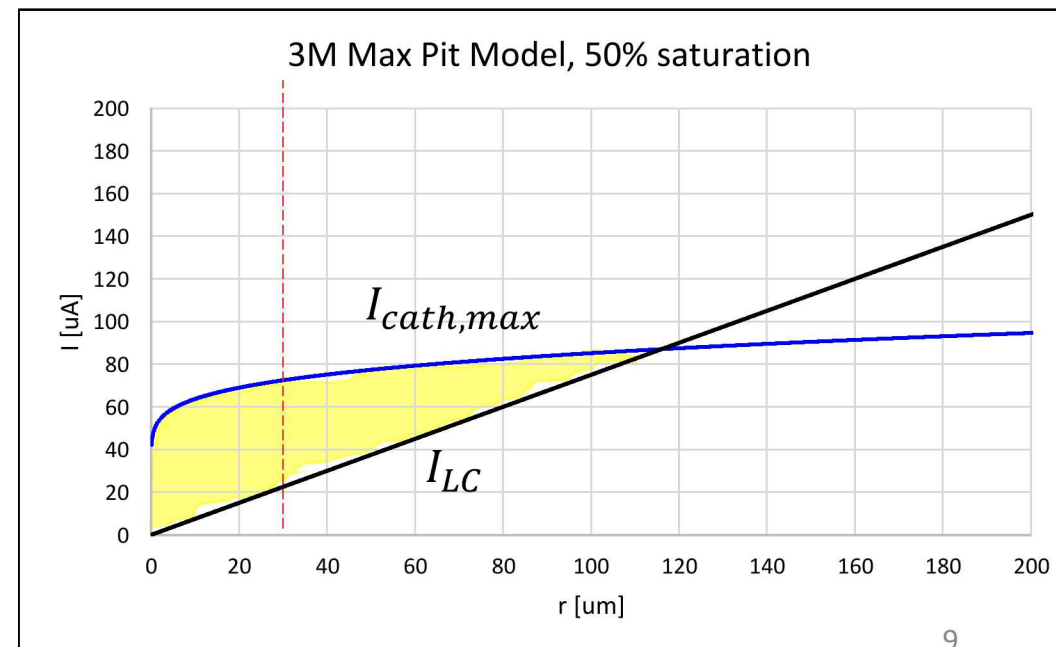
$$\bullet [Ni^{2+}]_{\text{critical}} = 2048.84 \left[\frac{\text{mol}}{\text{m}^3}\right]$$

$$\bullet [Cr^{3+}]_{\text{critical}} = 3213 \left[\frac{\text{mol}}{\text{m}^3}\right]$$

$$\bullet [Fe^{2+}]_{\text{critical}} = 13,622.02 \left[\frac{\text{mol}}{\text{m}^3}\right]$$

- Dashed lines represent constant pit size, $g = 30\mu\text{m}$
- Highlighted region represents satisfied pit stability

Criteria for hemisphere-like pits



Pit Stability Criteria

If Inequality is True, Then Pit Will Grow

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Criteria for time-dependent pits

Stationary Pit Stability Criterion

Summary: No differences between pits are seen in $E > E_{rp}$ criteria; always satisfied. Minimal differences between pits are seen in $\frac{I}{r}$ criterion

Finite Element Modeling Setup

Input Parameters:

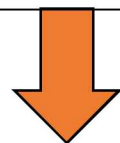
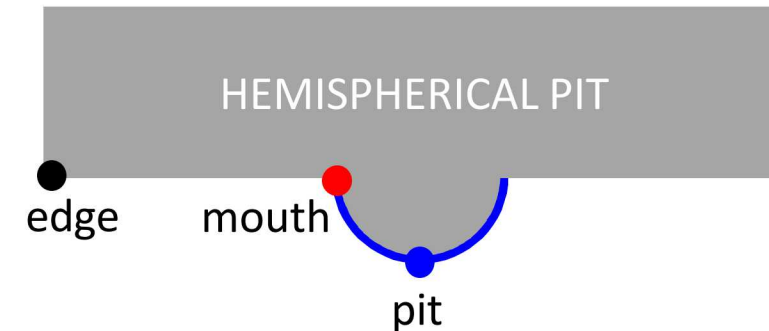
Concentration NaCl = 3M (RH = 88.321)
 WL = 10 – 1000 μm (for LD = 1.8 – 180 g/m²)
 $g = 30 \mu\text{m}$; $D = 15 \text{ cm}$

$$\kappa = 19.7 \left[\frac{\text{S}}{\text{m}} \right]$$

Assumptions:

Laplace as governing equation (constant conductivity)

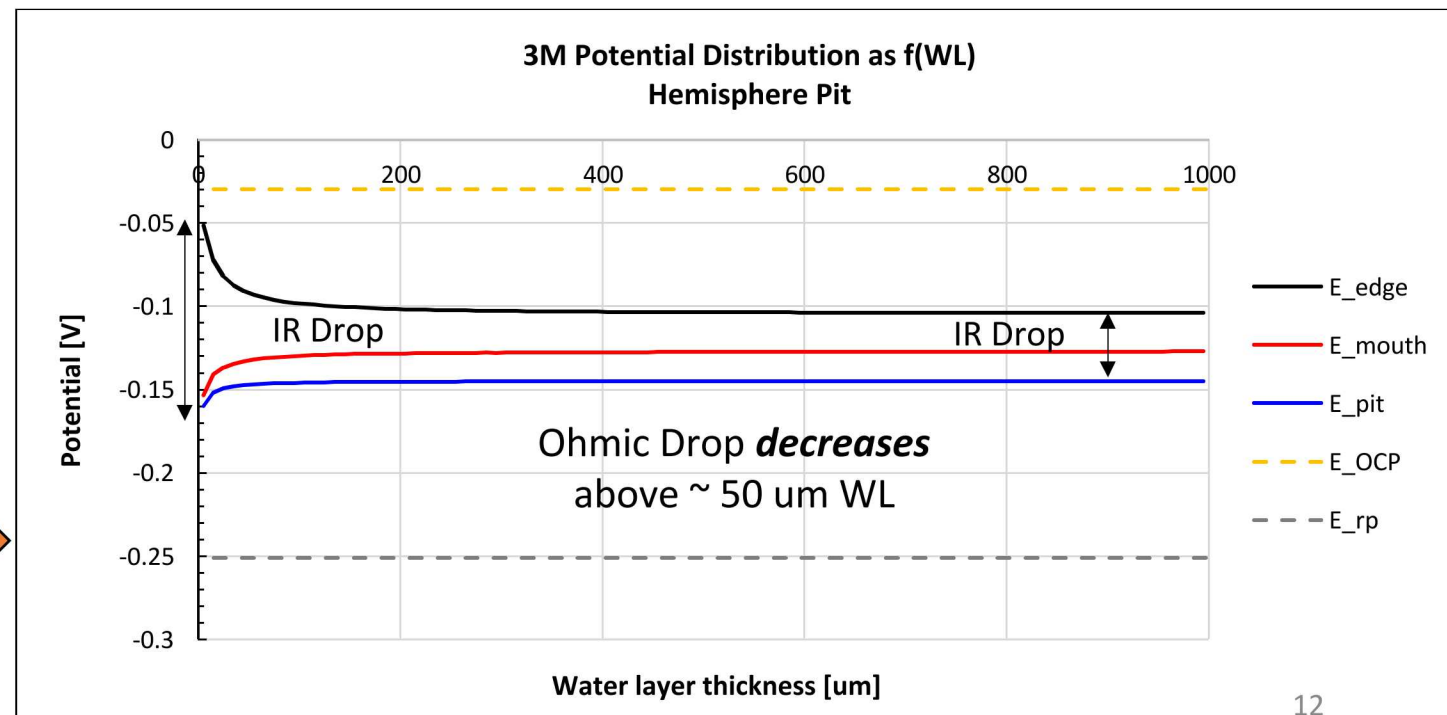
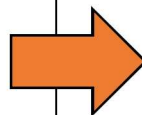
WL = water layer thickness
 g = pit diameter
 D = cathode diameter



Comparison of stability criterion:

$$E_{FEM} > E_{rp}$$

$$\left(\frac{I}{r} \right)_{FEM} > \left(\frac{I}{r} \right)_{max \text{ pit}}$$



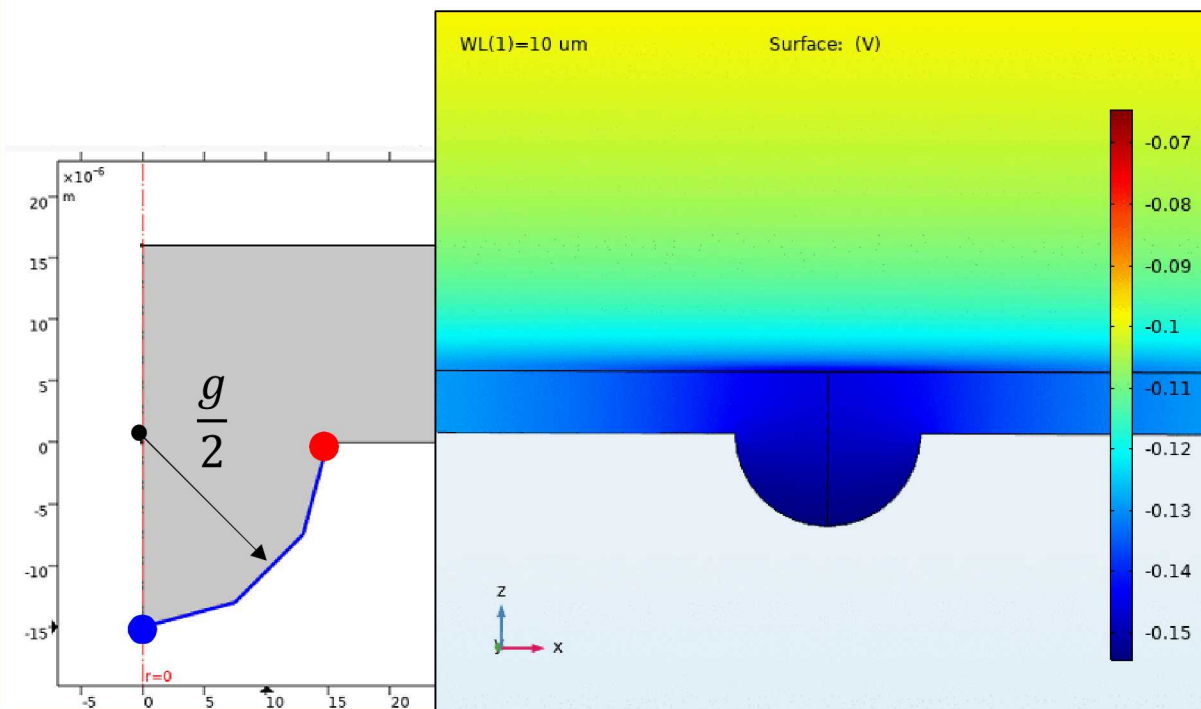
Hemisphere Pit

Geometric Parameters:

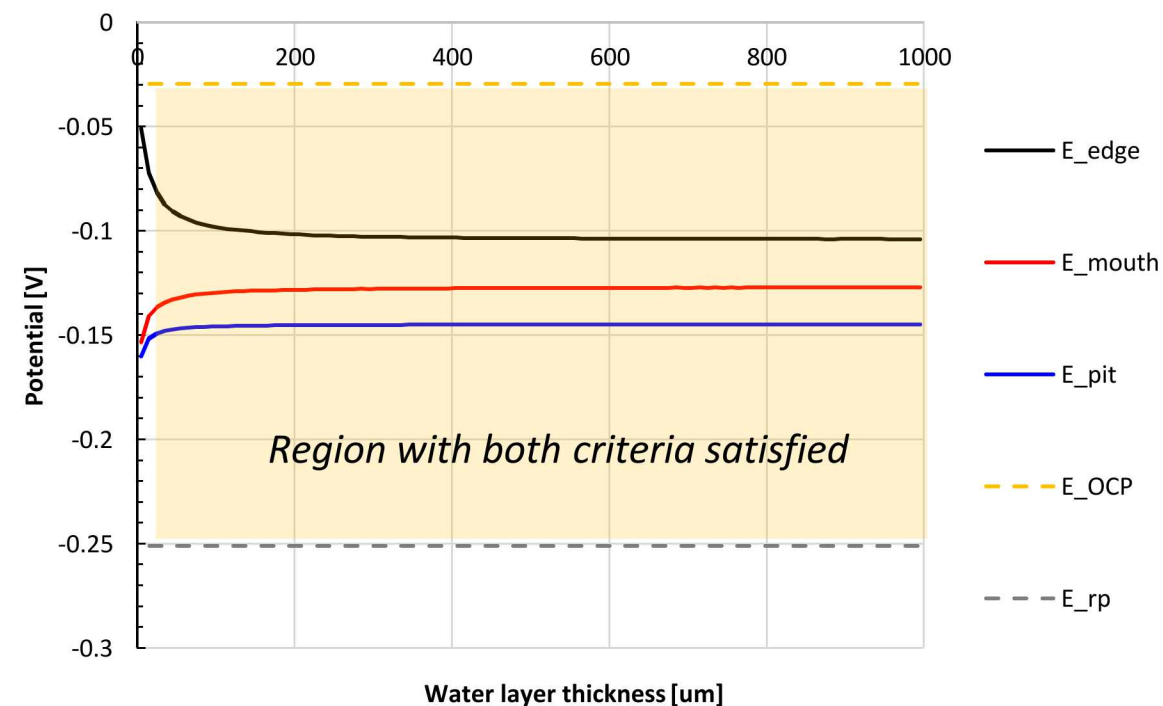
water layer varied

WL = 10–1000 μm , $g = 30 \mu\text{m}$, $D = 15 \text{ cm}$

- $\frac{I}{r}$ satisfied for $WL > 10.5 \mu\text{m}$
- $E_{\text{pit}} > E_{\text{rp}}$ for ALL WL's



3M Potential Distribution as f(WL)
Hemisphere Pit



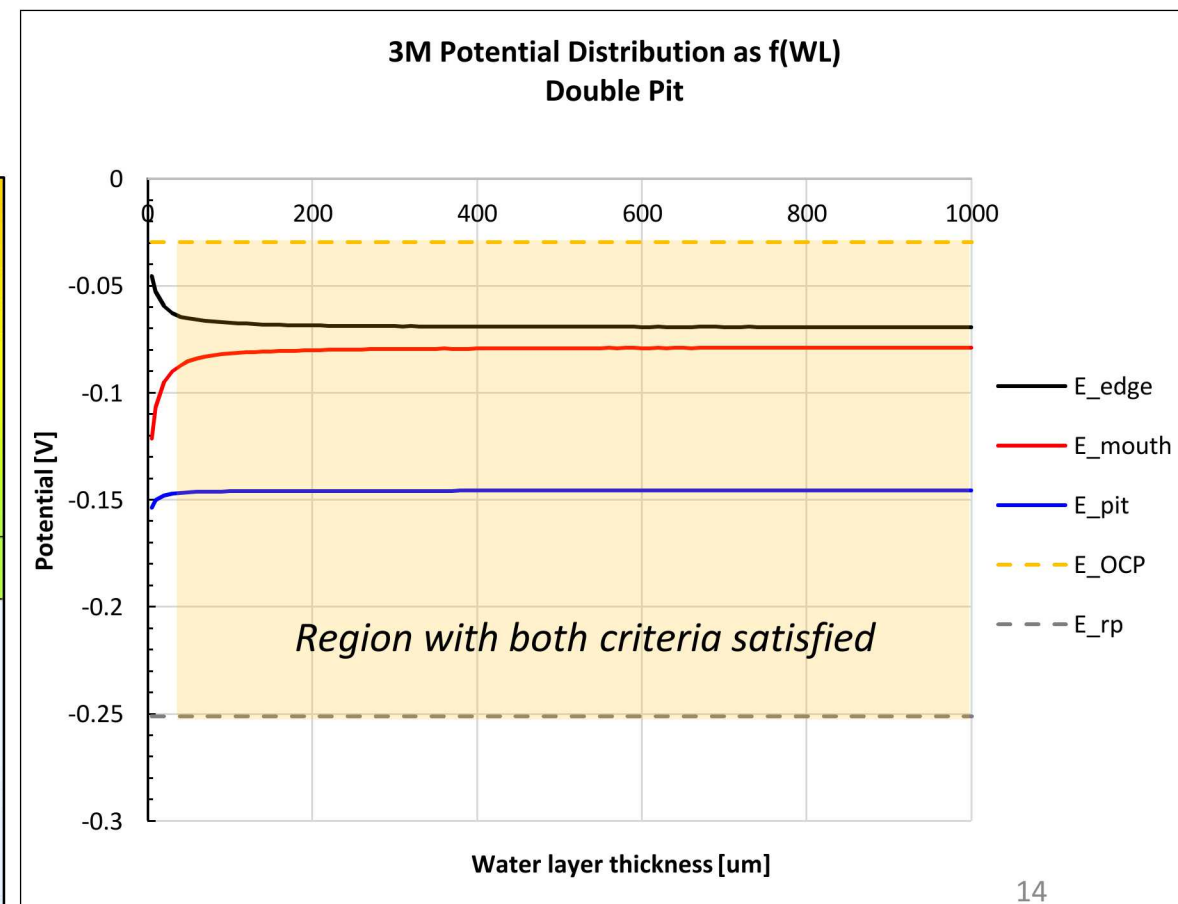
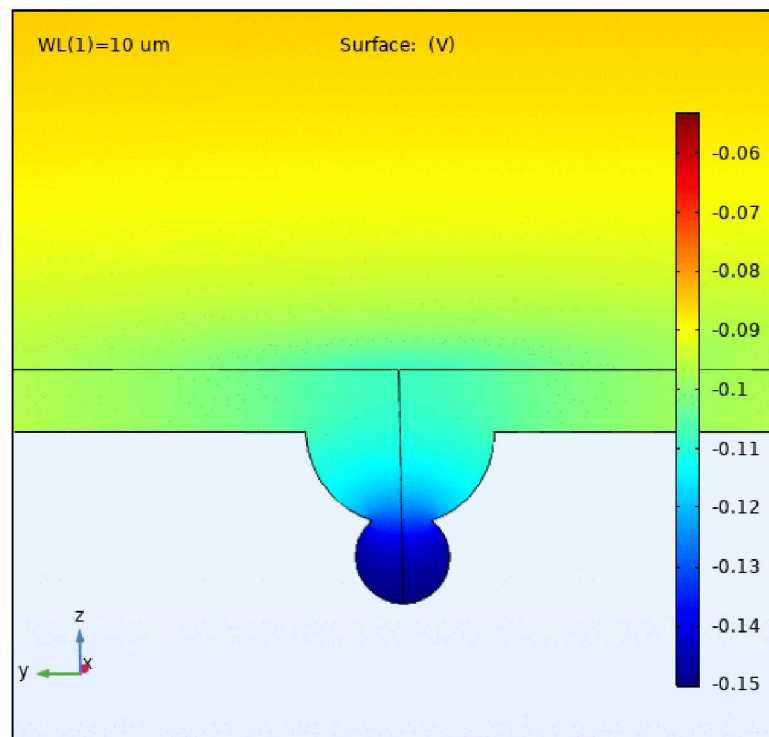
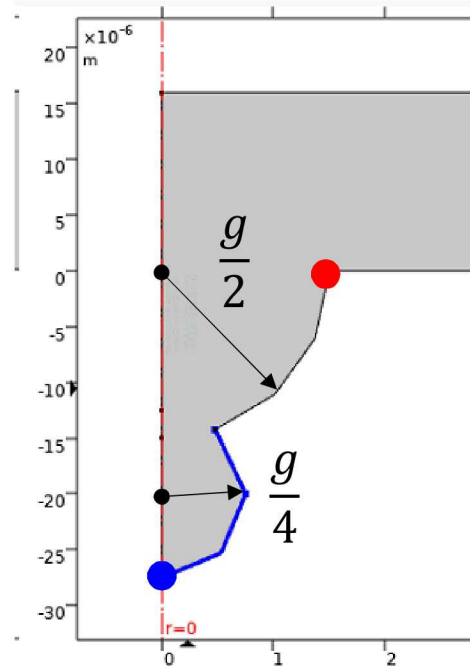
Double Pit

Geometric Parameters:

water layer varied

WL = 10– 1000 μm , $g = 30 \mu\text{m}$, $D = 15 \text{ cm}$

- $\frac{I}{r}$ satisfied for $WL > 50 \mu\text{m}$
- $E_{pit} > E_{rp}$ for ALL WL's



Undercut Pit

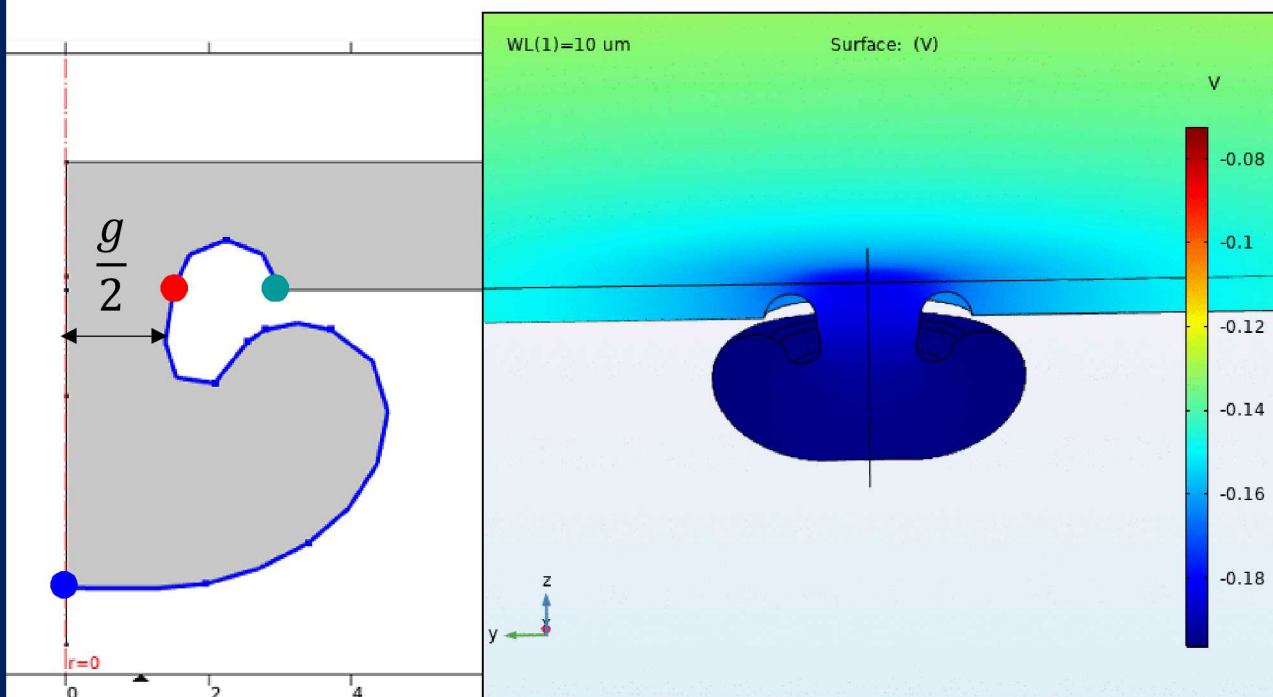
Geometric Parameters:

water layer varied

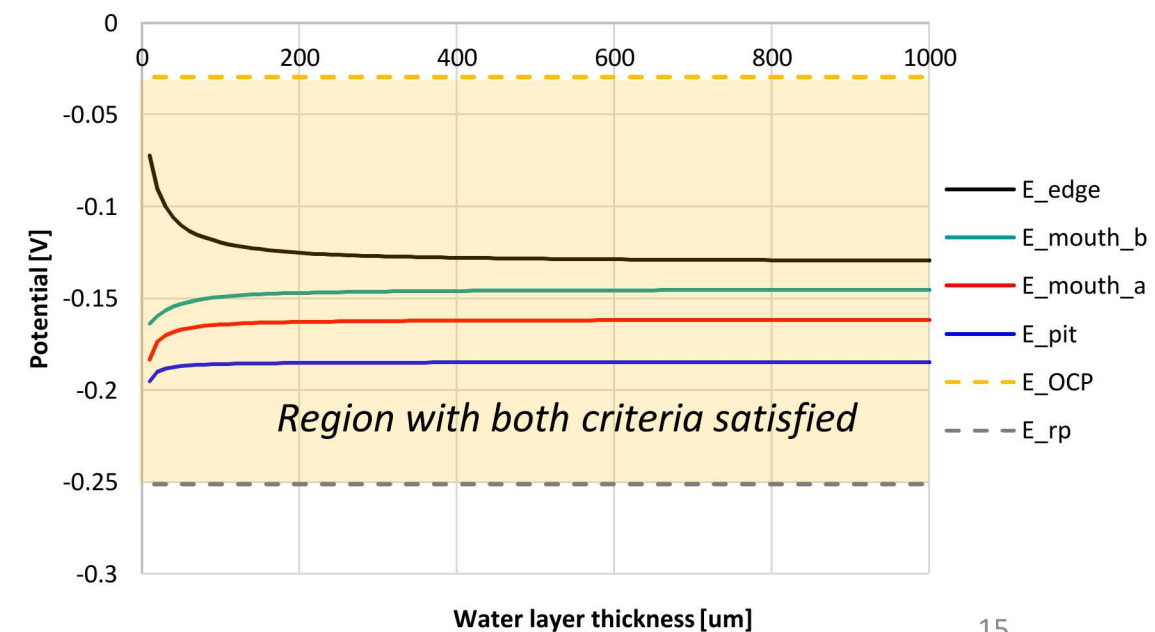
WL = 10– 1000 μm , $g = 30 \mu\text{m}$, $D = 15 \text{ cm}$

All Regions Active

- $\frac{I}{r}$ satisfied for *ALL WL's*
- $E_{pit} > E_{rp}$ for *ALL WL's*

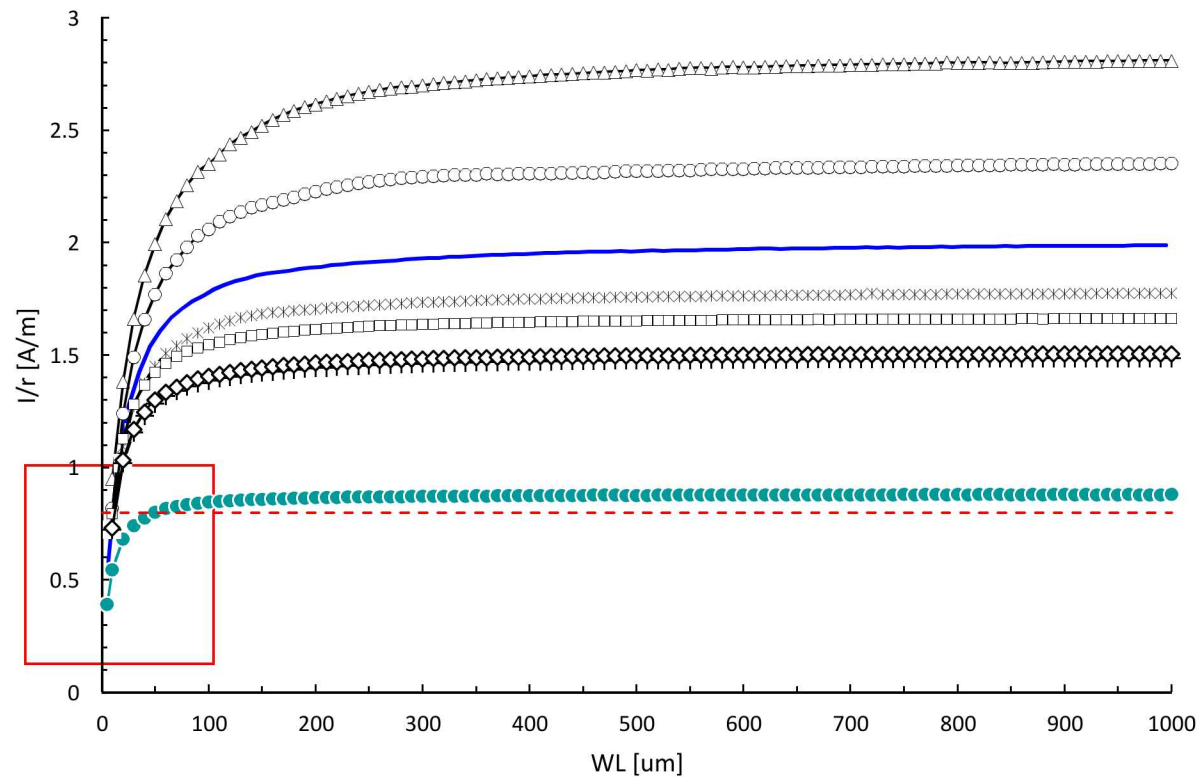


3M Potential Distribution as $f(WL)$
Undercut Pit, All Regions Active



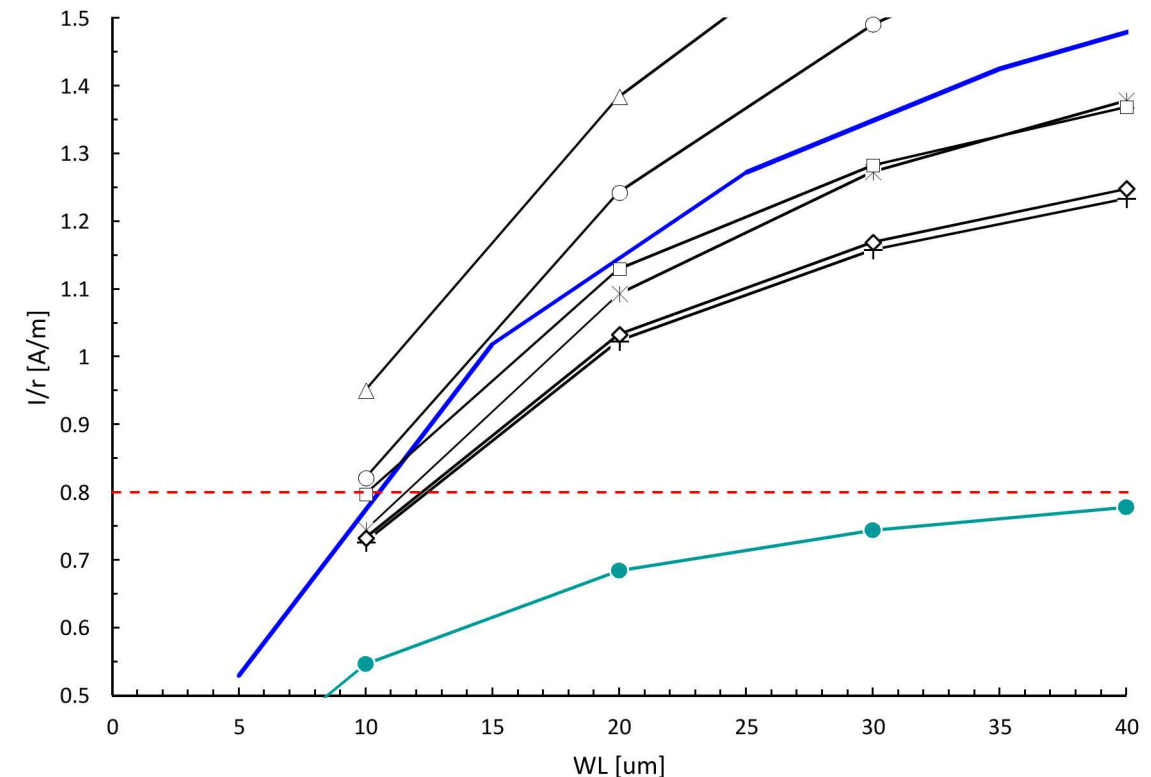
Plotting I/r Stability Criterion for Hemisphere-Based Pits

I/r Stability Criterion



- | | | |
|-----------------------|-----------------------|-----------------------|
| —●— Hemisphere | —●— Double Pit | —●— Region 1 Undercut |
| —○— Region 2 Undercut | —×— Region 3 Undercut | —+— Region 4 Undercut |
| —□— Region 5 Undercut | —◇— Region 6 Undercut | --- Max Pit Criterion |

I/r Stability Criterion



- | | | |
|-----------------------|-----------------------|-----------------------|
| —●— Hemisphere | —●— Double Pit | —●— Region 1 Undercut |
| —○— Region 2 Undercut | —×— Region 3 Undercut | —+— Region 4 Undercut |
| —□— Region 5 Undercut | —◇— Region 6 Undercut | --- Max Pit Criterion |

Conclusions for Steady-State Modeling

- All pits satisfy $E_{FEM} > E_{rp}$ criteria for geometries and environmental factors considered
- Water layer changes $> 100 \mu m$ do not have a large impact on stability, indicating that pit size/geometry (*i.e.* I_{LC}) is *more important* to stability than environmental factors (*i.e.* $I_{cath,max}$)
- Complex hemisphere-like pits behave *similarly to a hemisphere pit* in both $E_{FEM} > E_{rp}$ and $\left(\frac{I}{r}\right)_{FEM} > \left(\frac{I}{r}\right)_{max\ pit}$ criteria
 - Indicates that using “hemispherical pit” for simplicity is not a bad assumption
- “Double Pit” is less stable than hemisphere and undercutting pit

Does the concentration profile of metal ions agree with these statements?

Time-Dependent Pit Stability Criterion

Summary: Concentrations of Ni^{2+} , Cr^{3+} , and Fe^{2+} all increase with time, and all satisfy critical concentration criteria before reaching steady-state

Time-Dependent FEM Setup

Input Parameters:

Concentration NaCl = 3M (RH = 88.321)

$$D_{Ni} = 4.01 \times 10^{-10} \left[\frac{m^2}{s} \right]$$

$$D_{Fe} = 4.03 \times 10^{-10} \left[\frac{m^2}{s} \right]$$

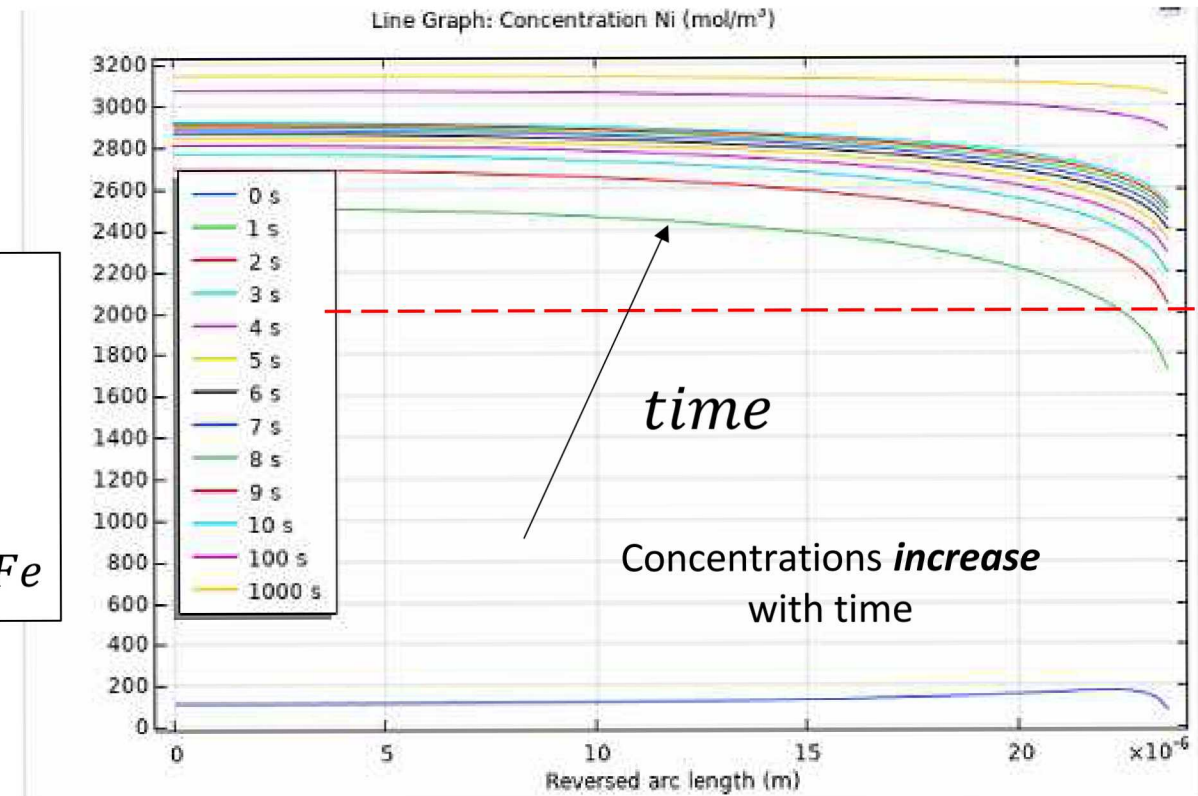
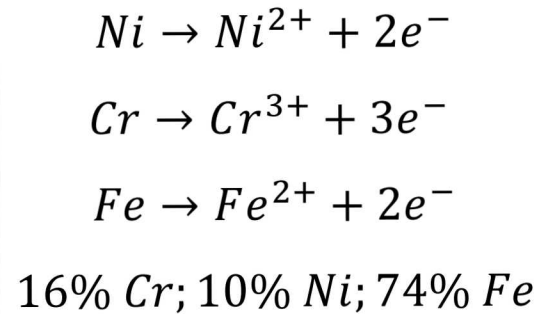
$$D_{Cr} = 3.23 \times 10^{-10} \left[\frac{m^2}{s} \right]$$

$$\kappa = 19.7 \left[\frac{S}{m} \right]$$

Assumptions:

Laplace as governing equation (constant conductivity)

Dilute solution (Nernst-Einstein equation)



Comparison of stability criterion:

$$[M^+]_{FEM} > [M^+]_{critical}$$

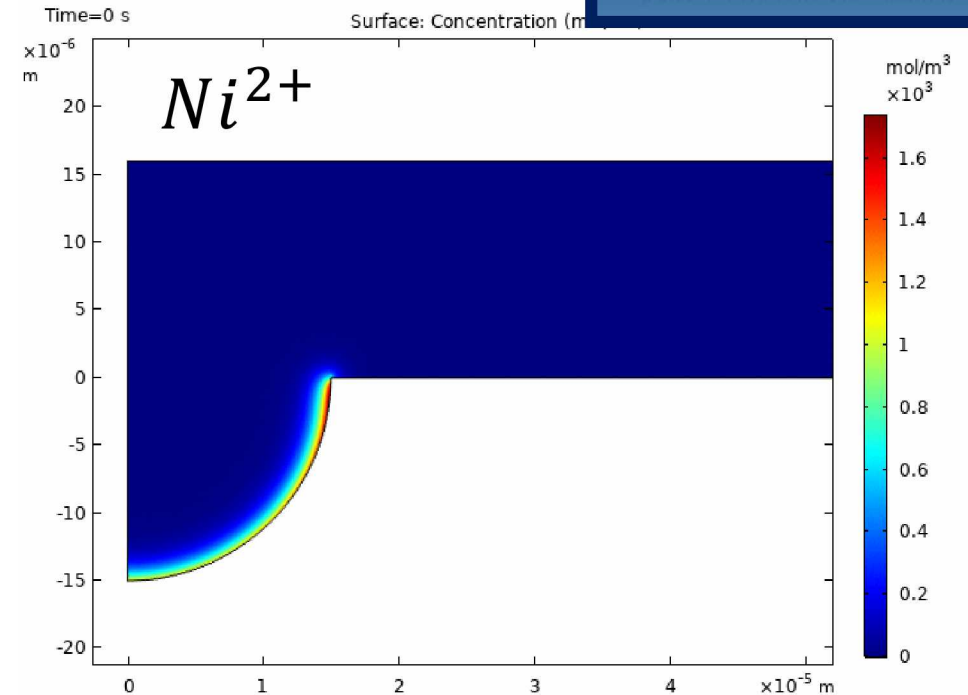
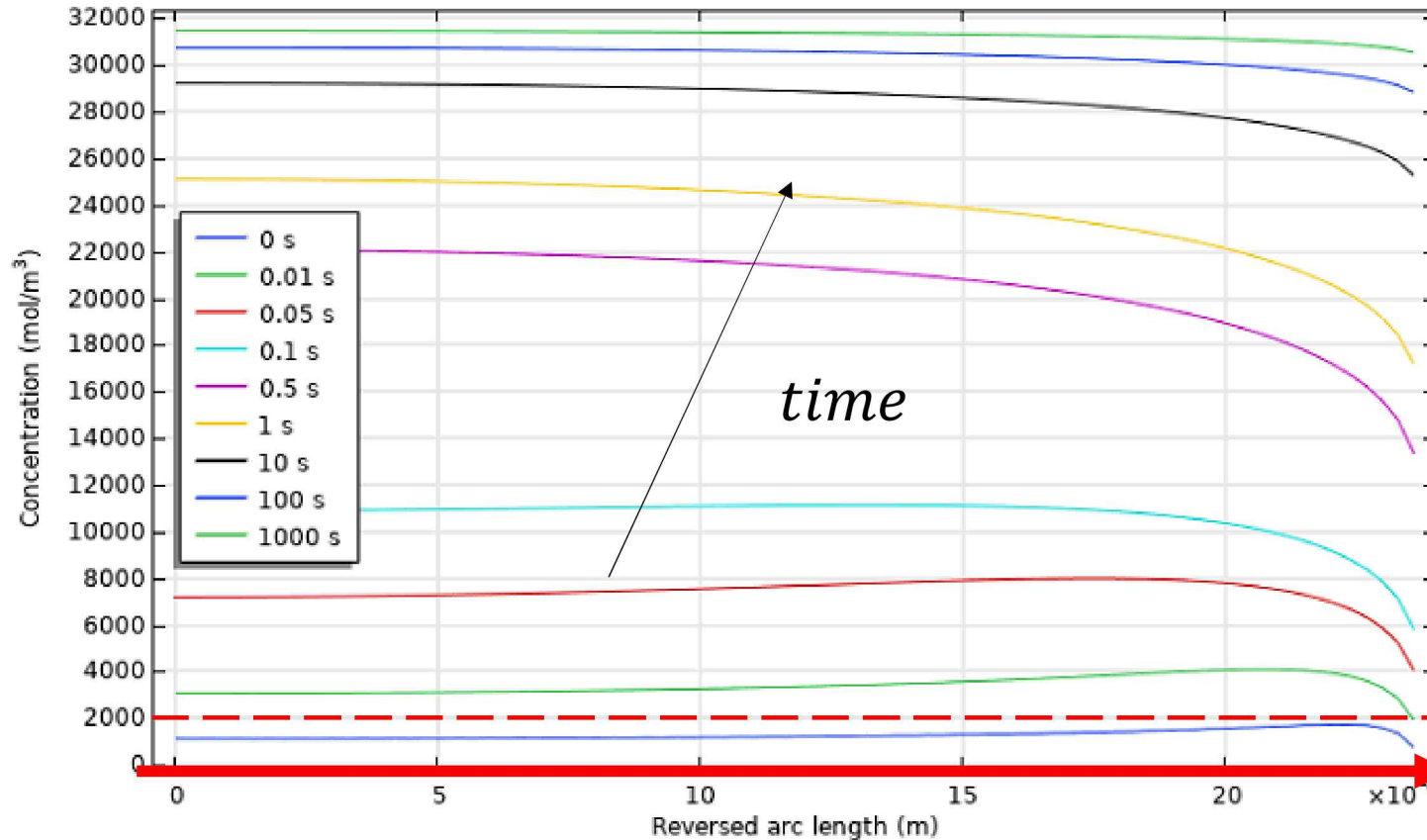
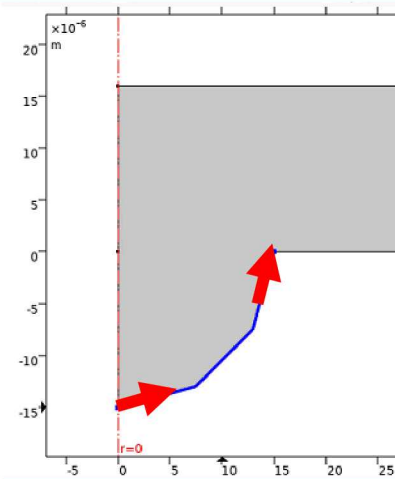
Hemisphere Pit

Geometric Parameters:

Time varied

$t = 0 - 1000$ s, WL = 16 μm ,
 $g = 30$ μm , $D = 15$ cm

(mol/m³)



Critical concentration $\left[\frac{\text{mol}}{\text{m}^3}\right]$
at BASE of pit satisfied for:

$[Ni^{2+}] > 2048.84$ after $0 < t < 0.01$ seconds

$[Cr^{3+}] > 3213$ after $0 < t < 0.01$ seconds

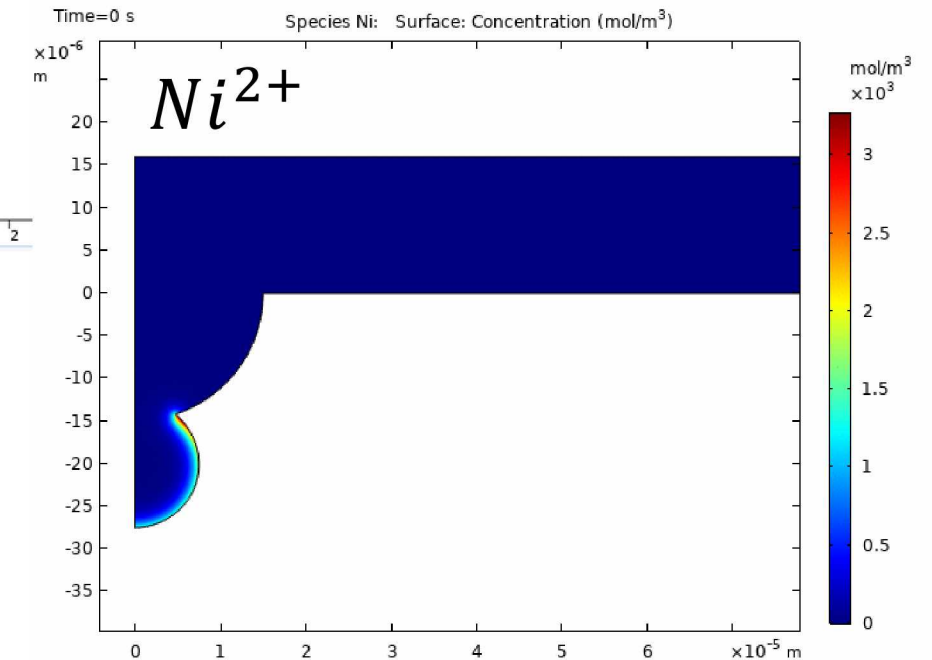
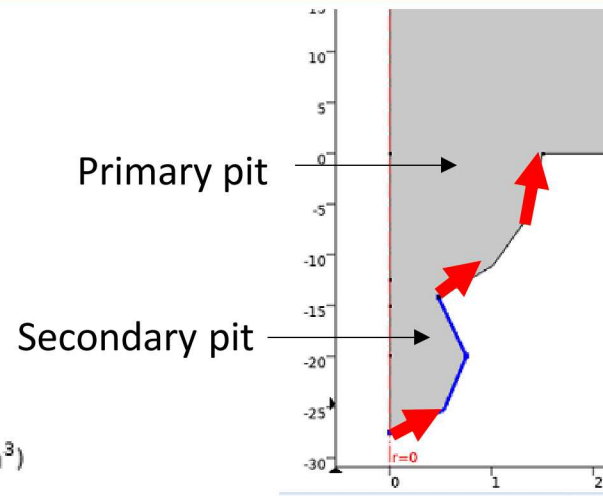
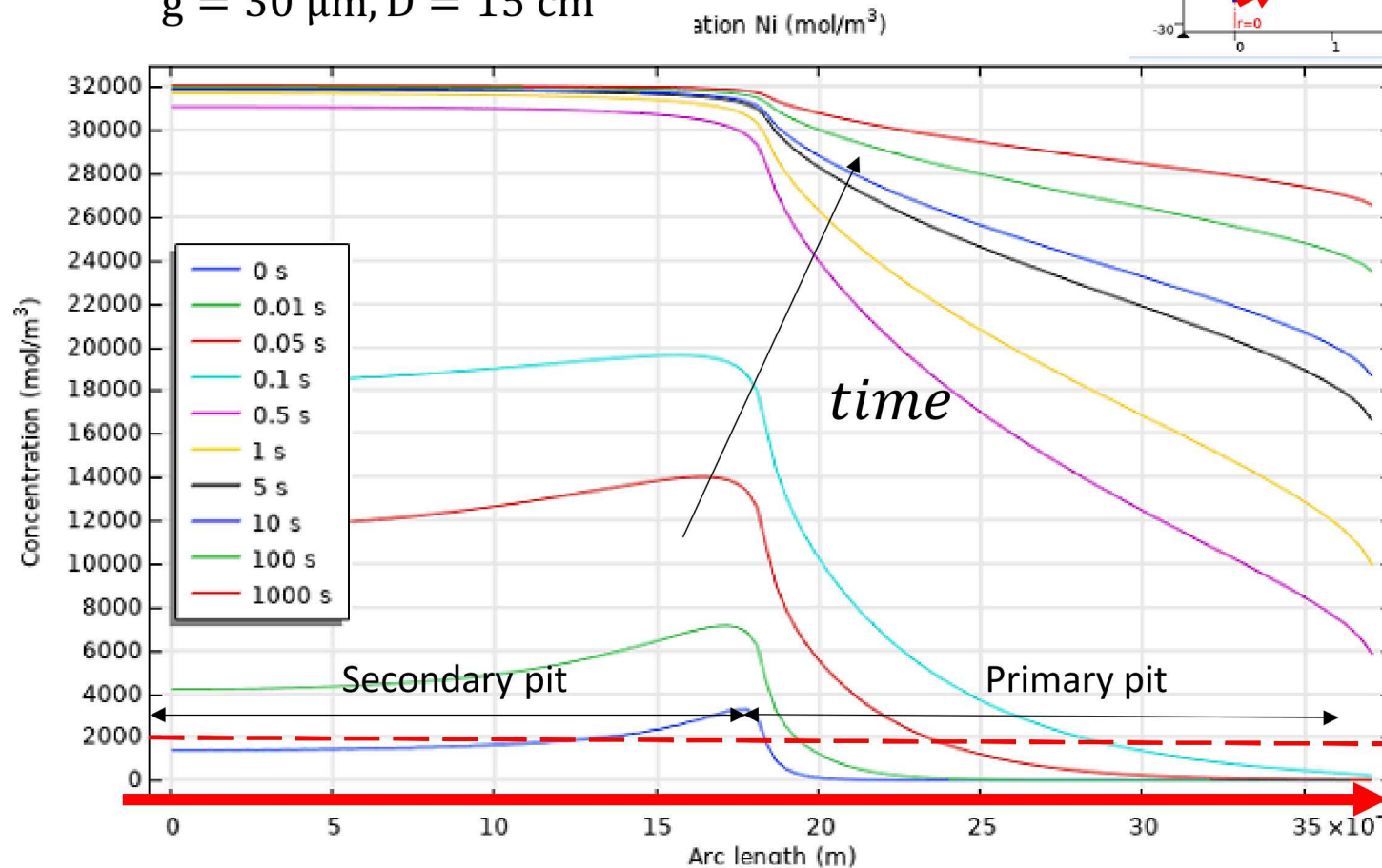
$[Fe^{2+}] > 13,622.02$ after $0 < t < 0.01$ seconds

Double Pit

Geometric Parameters:

Time varied

$t = 0 - 1000 \text{ s}$, $WL = 16 \mu\text{m}$,
 $g = 30 \mu\text{m}$, $D = 15 \text{ cm}$



Critical concentration $\left[\frac{\text{mol}}{\text{m}^3}\right]$
 at BASE of pit satisfied for:

$[Ni^{2+}] > 2048.84$ after $0 < t < 0.01 \text{ seconds}$

$[Cr^{3+}] > 3213$ after $0 < t < 0.01 \text{ seconds}$

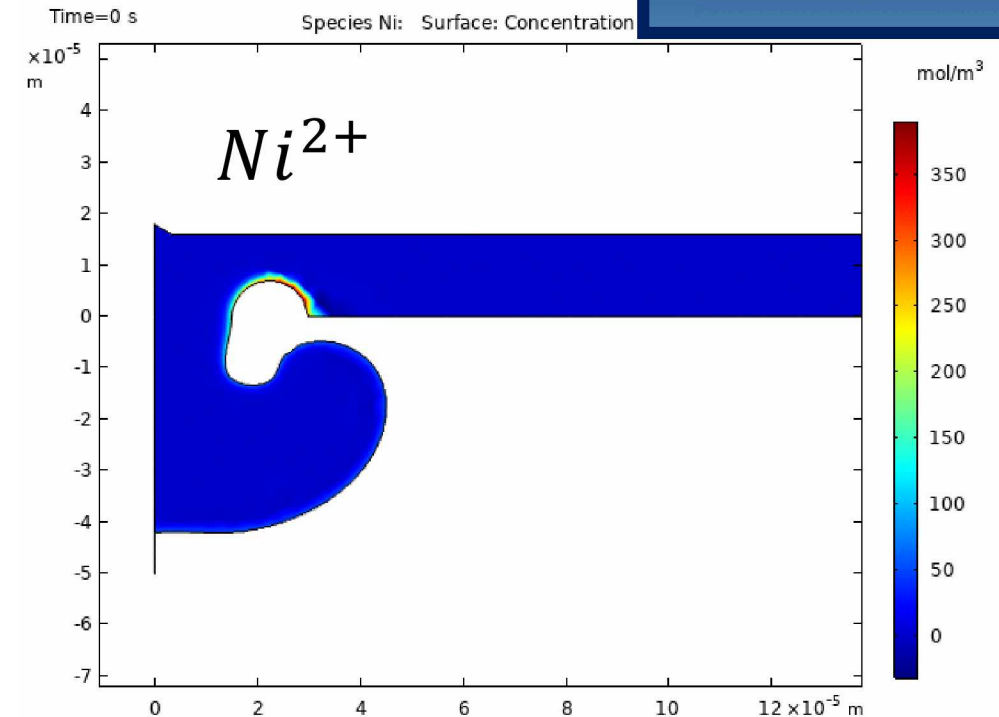
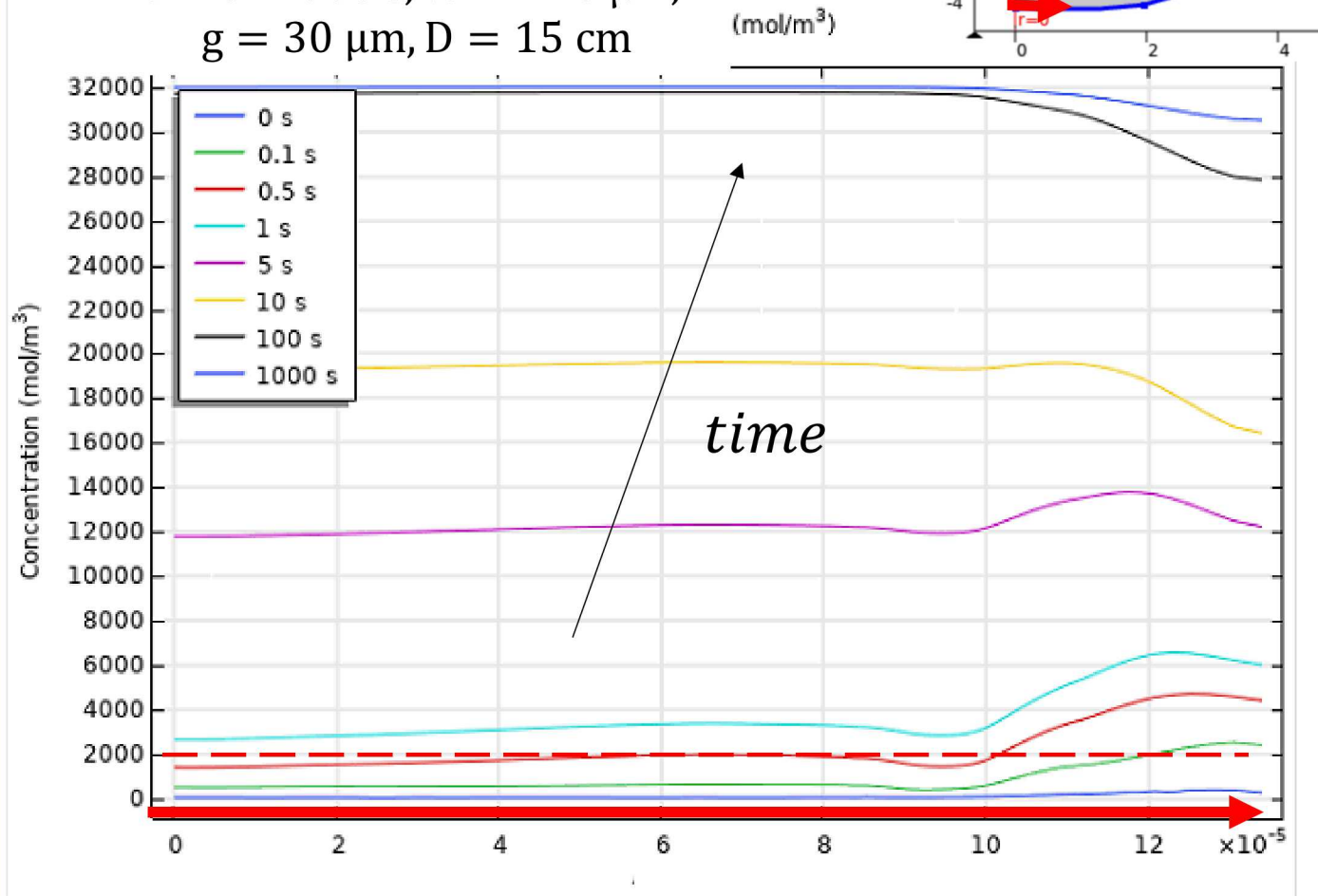
$[Fe^{2+}] < 13,622.02$ after $0 < t < 0.01 \text{ seconds}$

Undercut Pit

Geometric Parameters:

Time varied

$t = 0 - 1000$ s, $WL = 16$ μm ,
 $g = 30$ μm , $D = 15$ cm



Critical concentration $\left[\frac{\text{mol}}{\text{m}^3}\right]$
at BASE of pit satisfied for:

$[Ni^{2+}] > 2048.84$ after $0.5 < t < 1$ seconds

$[Cr^{3+}] > 3213$ after 1 second

$[Fe^{2+}] > 13,622.02$ after 0.5 seconds

Conclusions for Time-Dependent Modeling

- At the edge of the pit, it is more difficult to satisfy the critical concentration criteria (due to easier diffusion)
- In all pit geometries, all metal ions satisfy the critical concentration criteria *before reaching steady state*
- The Double Pit reached stability the *quickest*, but was also the quickest to *lose stability* via easy diffusion out of the pit
- Both steady-state and time-dependent results indicate that with the current set of pit geometries, all pits will actively corrode
 - Note that these pits are all fairly small, so it is not surprising that they are stable.
 - In the future we will explore pit size to find size at which external cathode cannot support pit growth

Disclaimer and Acknowledgements

- Any opinions, findings and conclusions or recommendations expressed in this material are those of the author(s) and do not necessarily reflect the views of Sandia National Laboratory
- Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525
- This work was supported through a DOE funded ACT program
- Discussions with other members of CESE at the University of Virginia are gratefully acknowledged



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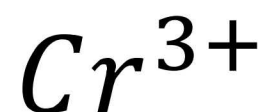
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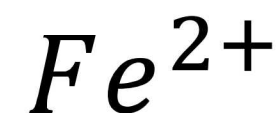
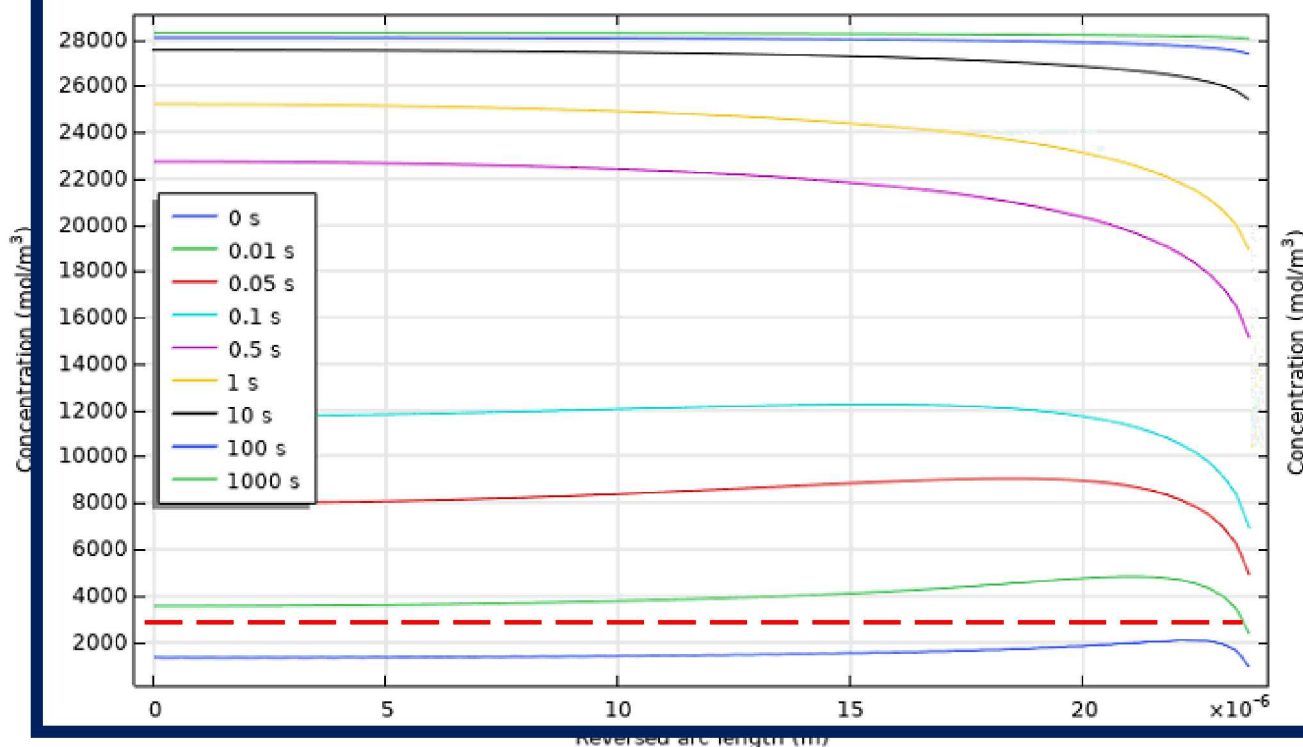
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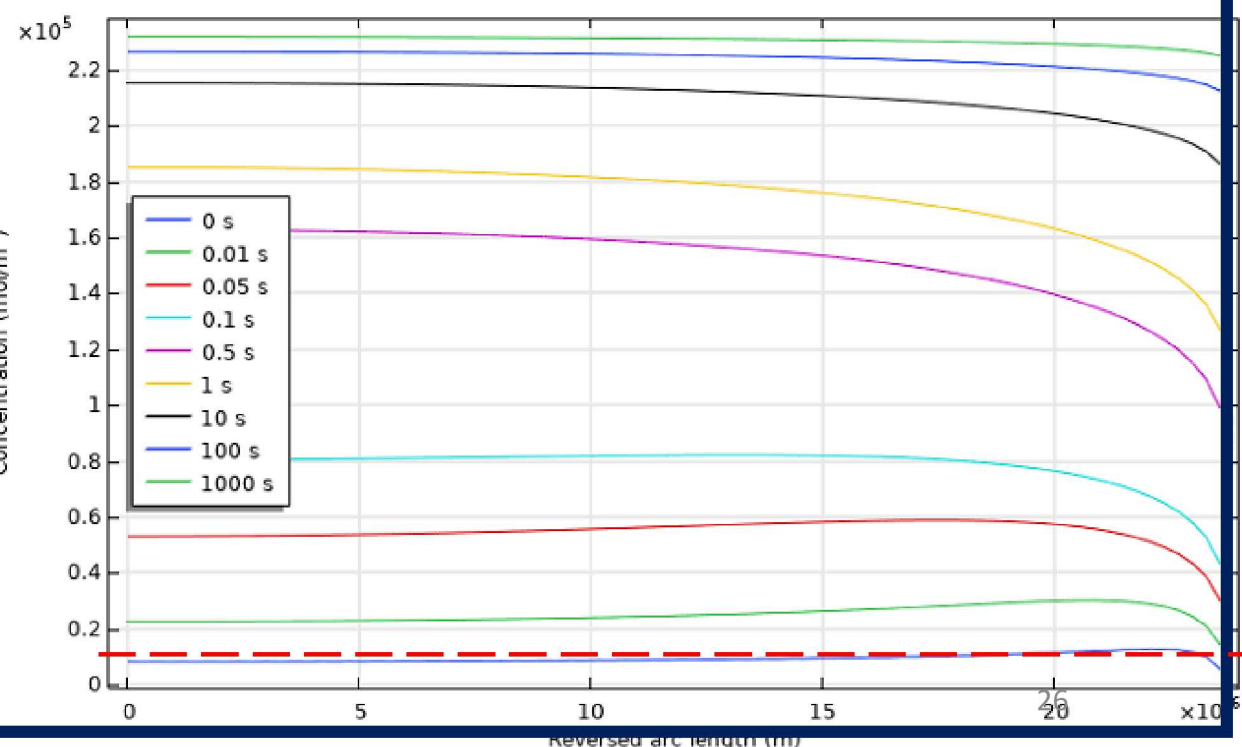
Hemisphere Pit

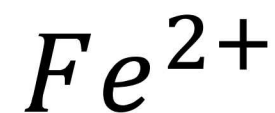


Line Graph: Concentration Cr (mol/m³)

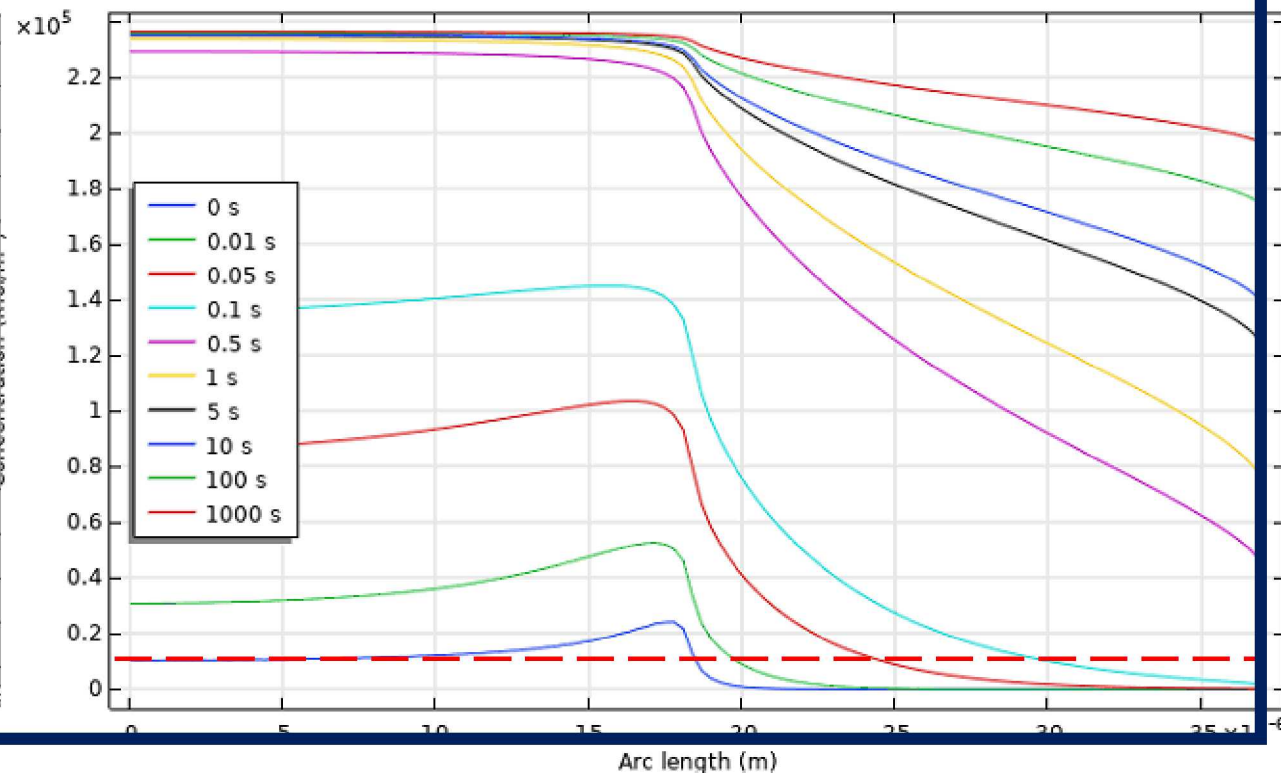


Line Graph: Concentration Fe (mol/m³)

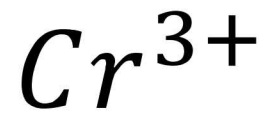




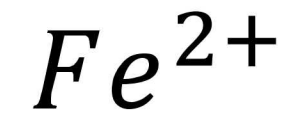
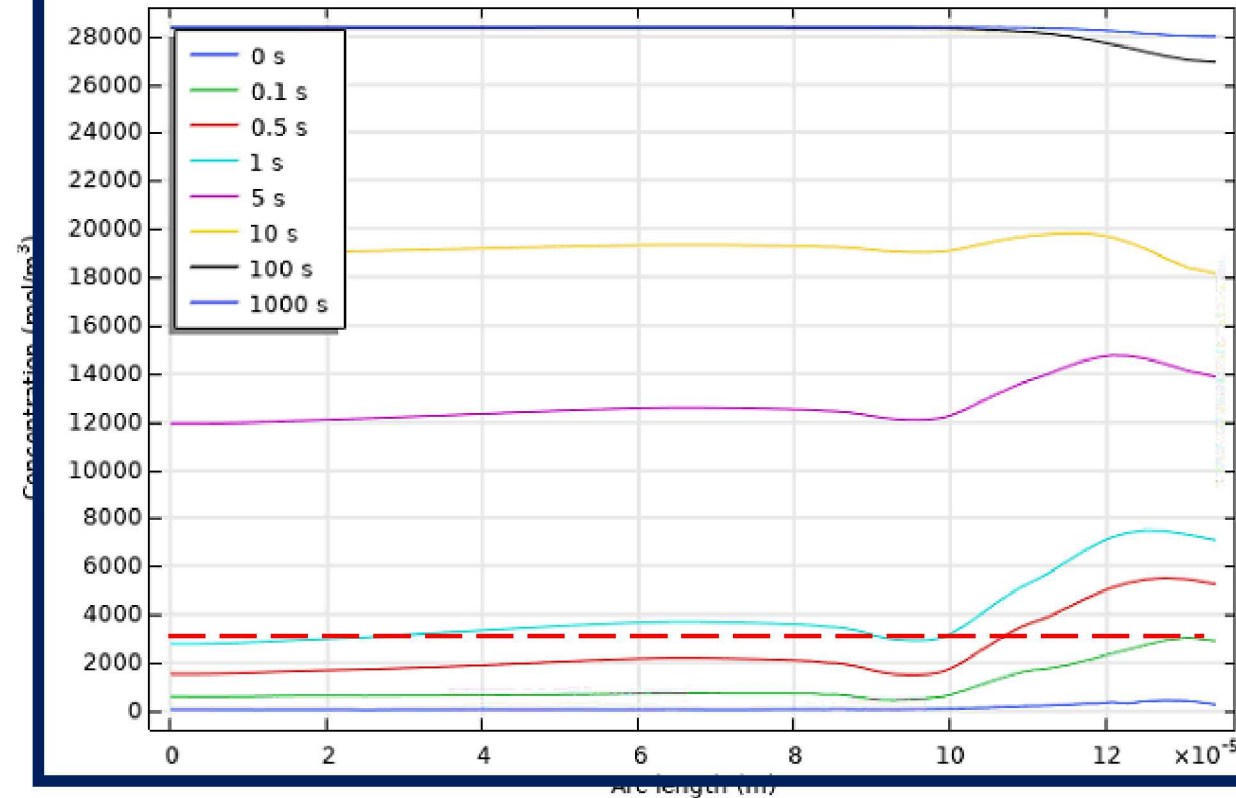
Line Graph: Concentration Fe (mol/m³)



Undercut Pit



Line Graph: Concentration Cr (mol/m³)



Line Graph: Concentration Fe (mol/m³)

