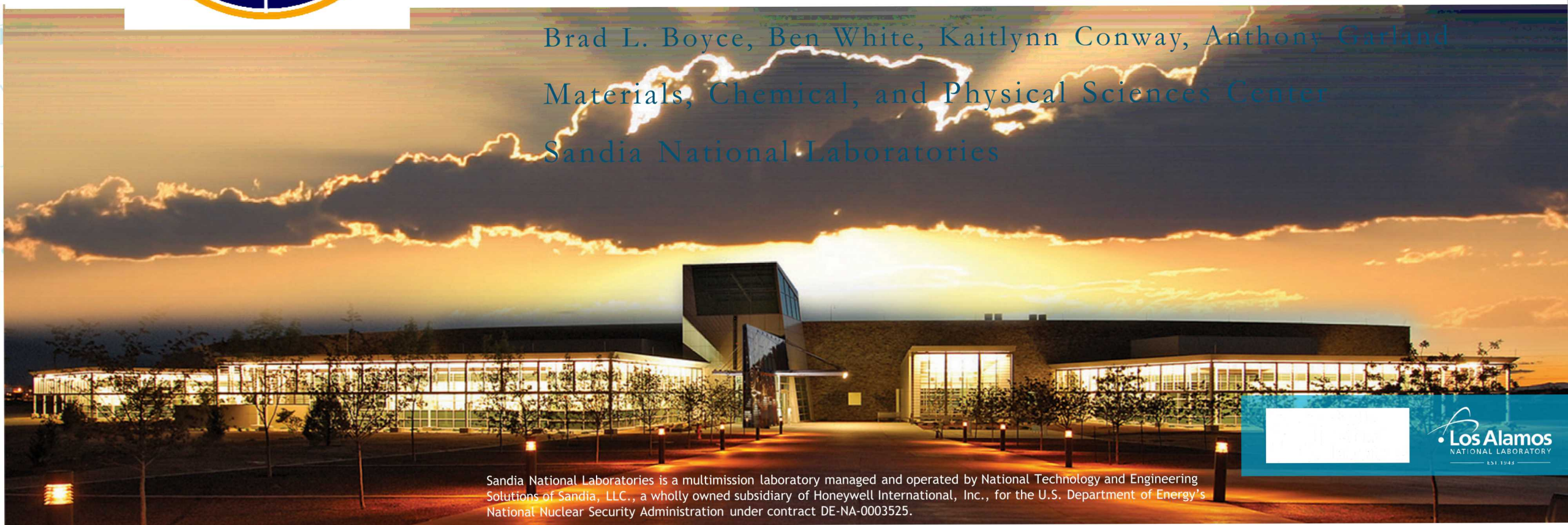


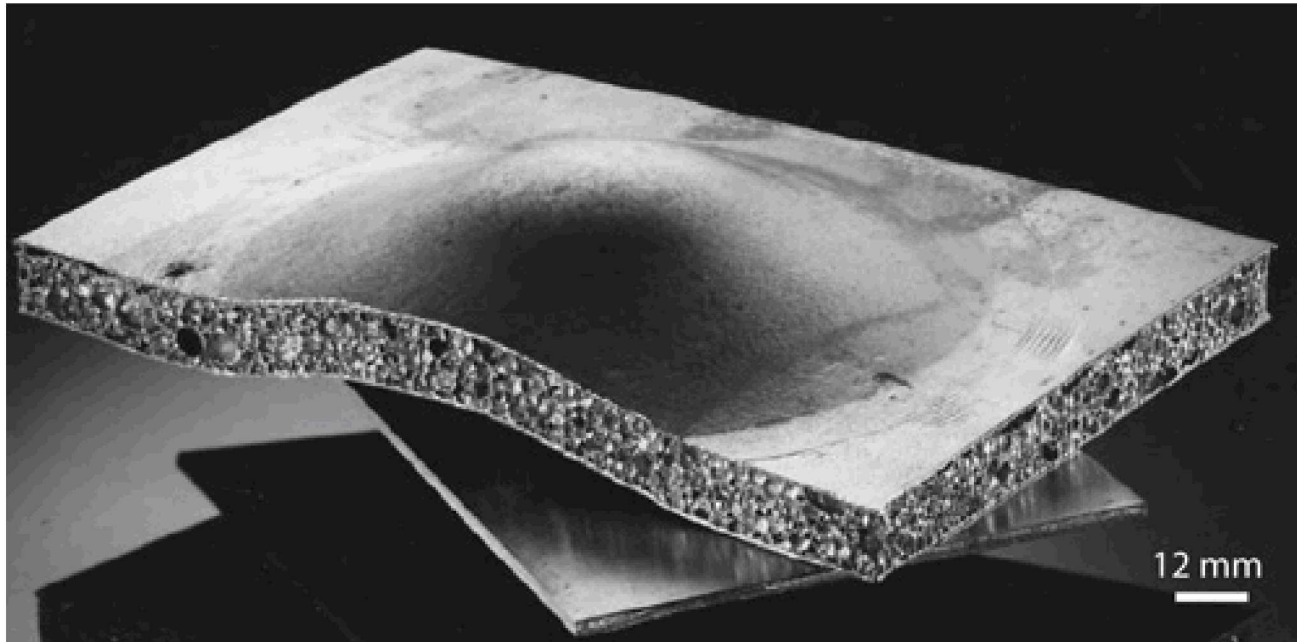


Toughening materials with air?

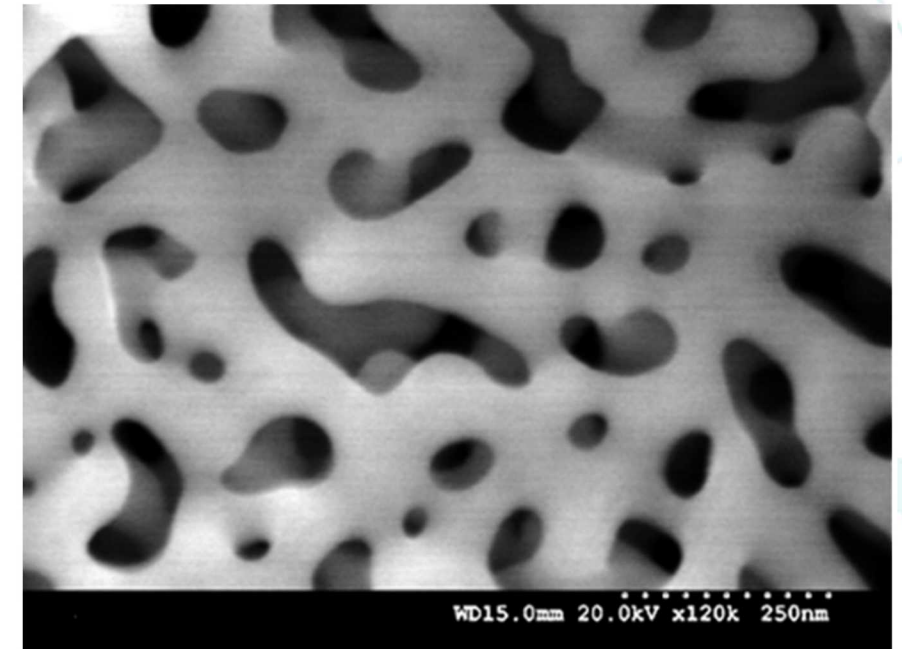
Brad L. Boyce, Ben White, Kaitlynn Conway, Anthony Garland
Materials, Chemical, and Physical Sciences Center
Sandia National Laboratories



Structural metal foams... aka cellular solids



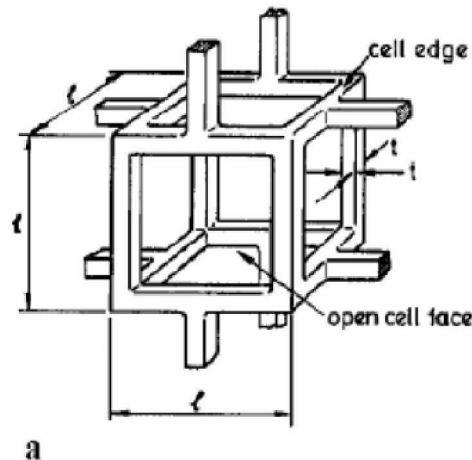
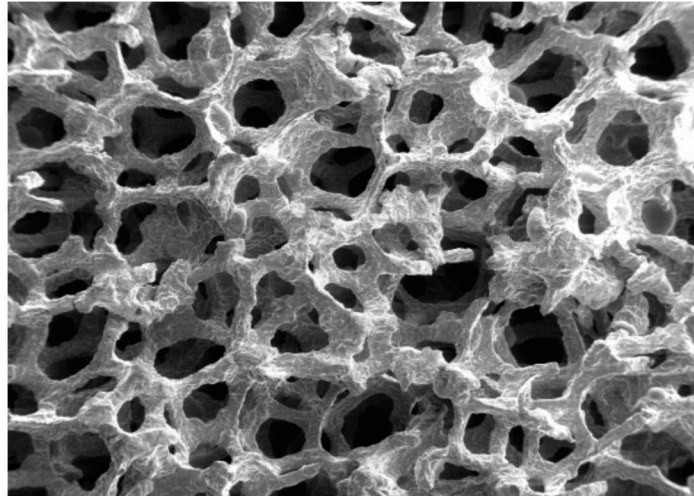
Aluminum Foam Sandwich (AFS) Panel



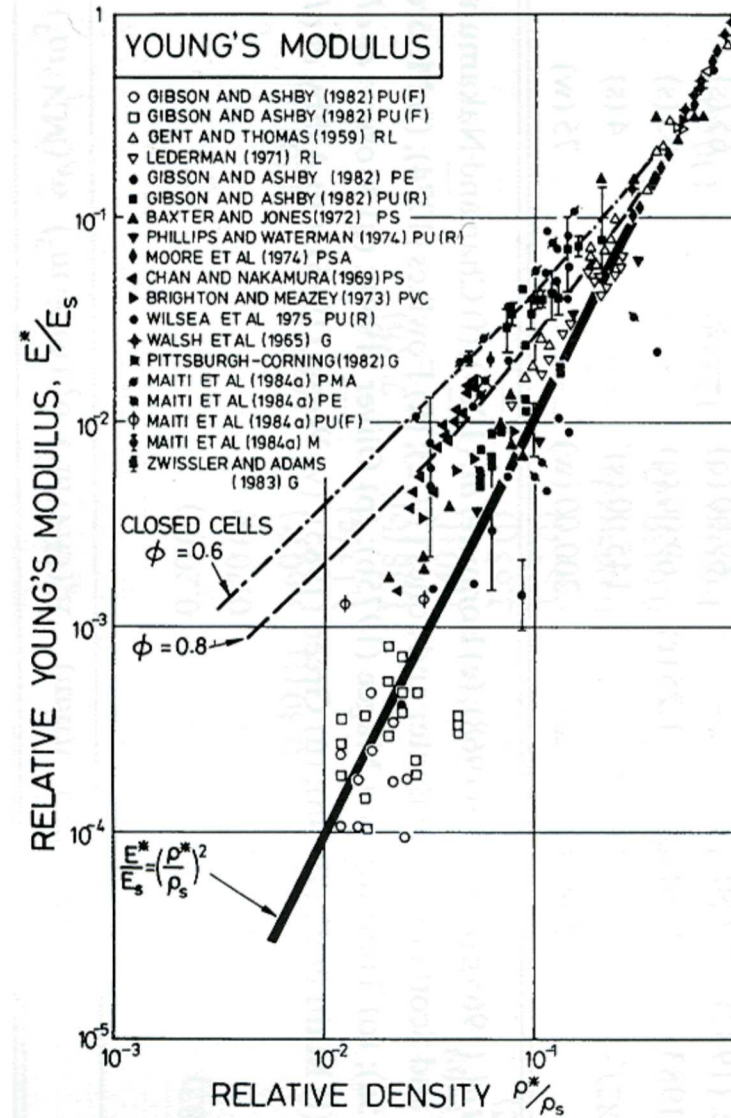
Nanoporous Au

**Gold with only one fourth the
fracture toughness of glass!**

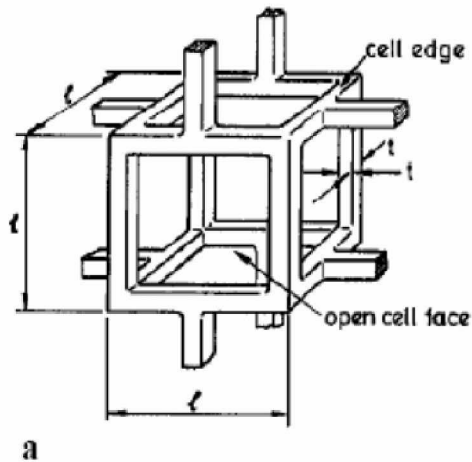
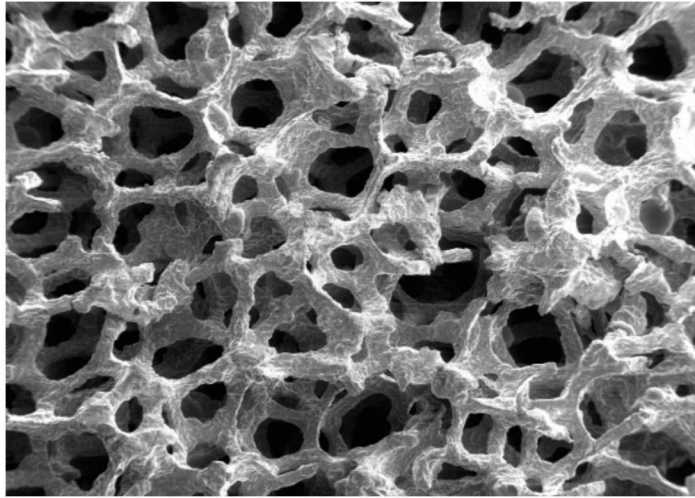
Modulus



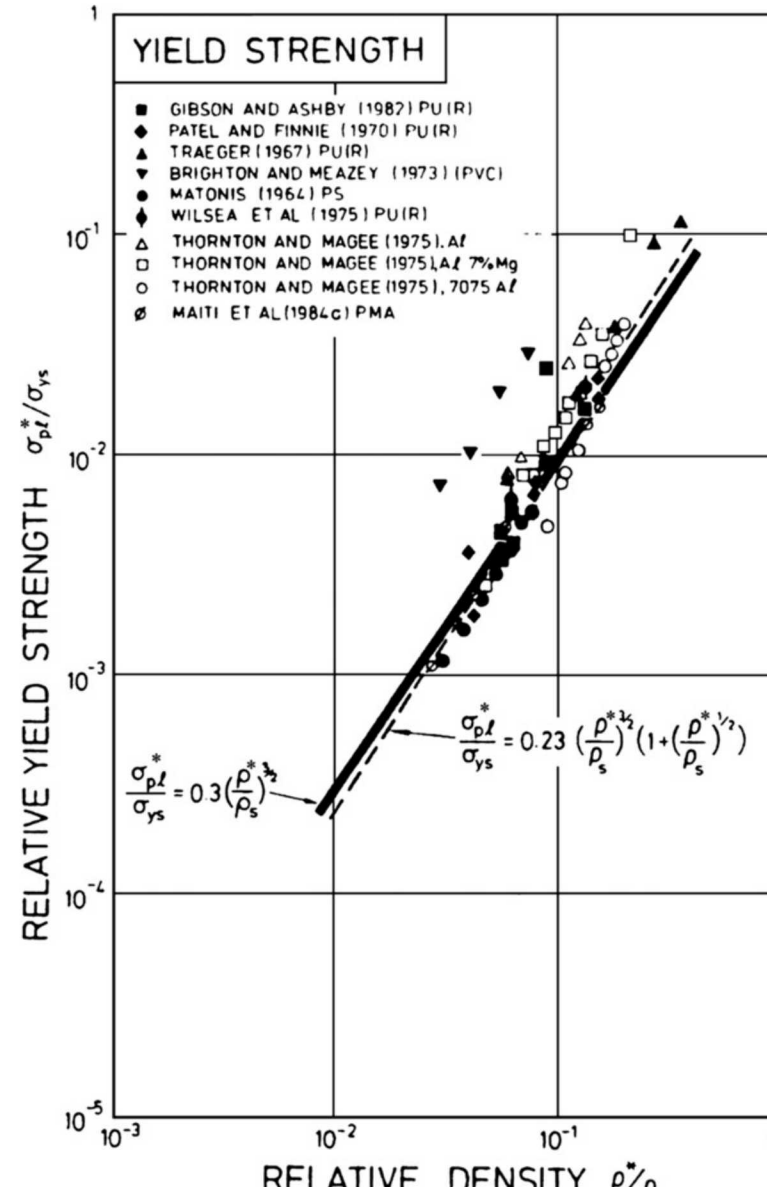
Gibson and Ashby, Cellular Solids, 1997



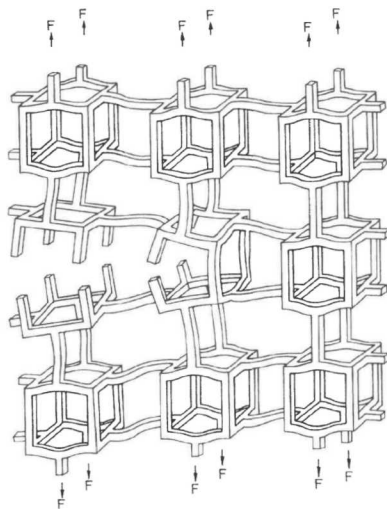
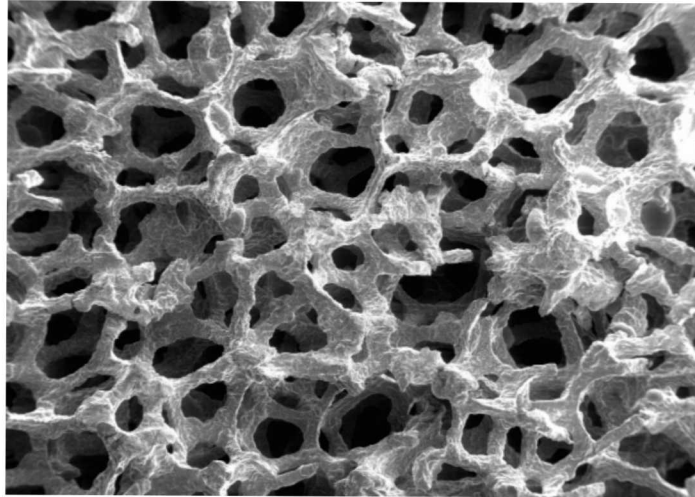
Strength



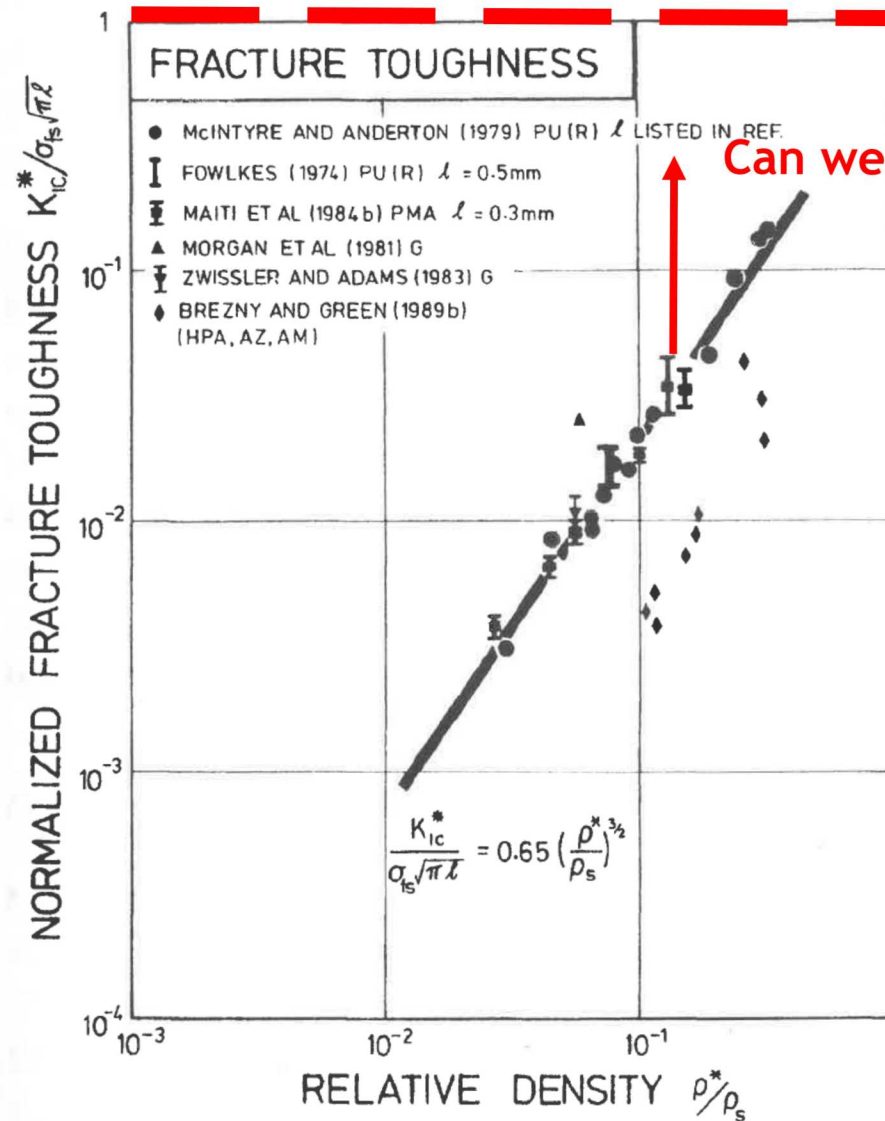
Gibson and Ashby, Cellular Solids, 1997



Foams are expected to lose toughness as density decreases



Gibson and Ashby, Cellular Solids, 1997



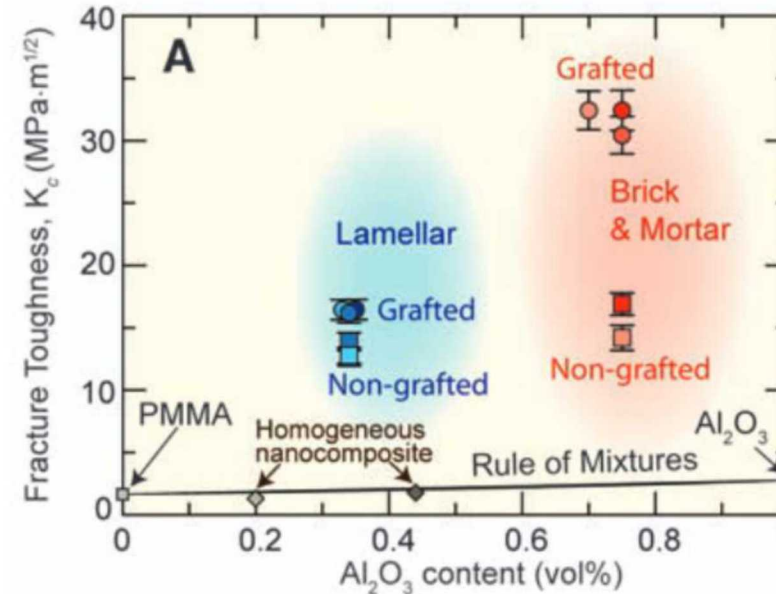
Is 1 an upper limit???

Can we architect?

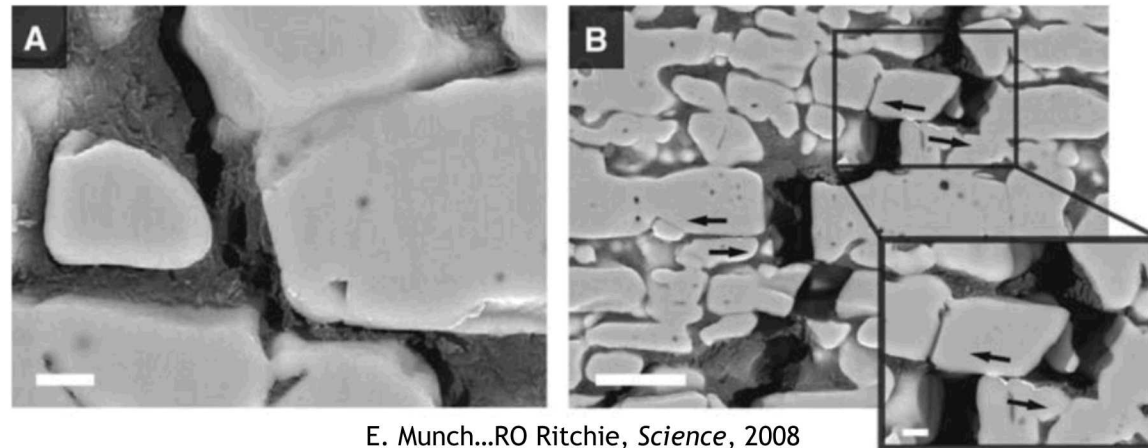
An inspiring example: synthetic nacre



Mother of pearl is mostly brittle calcium carbonate. How is it so tough???

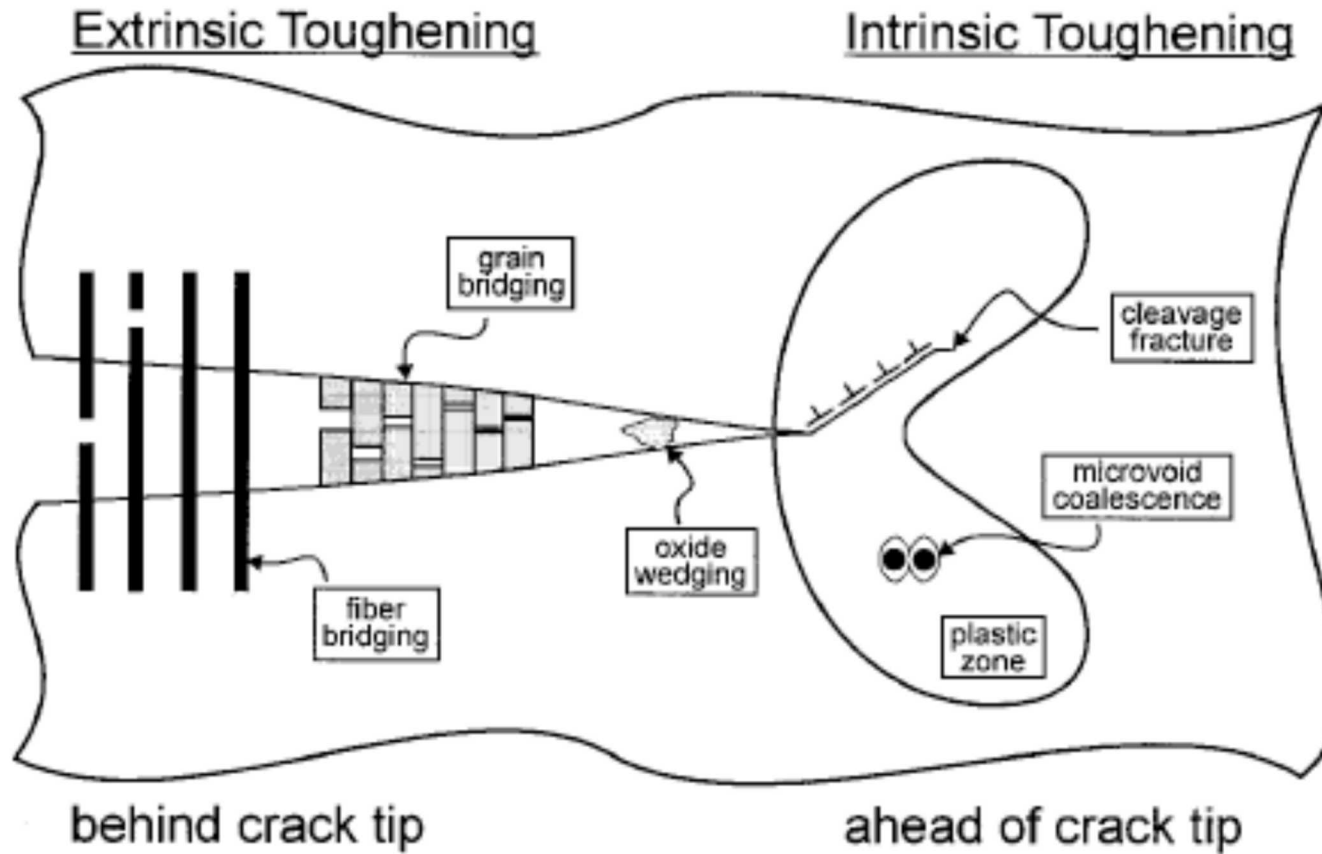


“Brick and Mortar” toughening in Synthetic Nacre



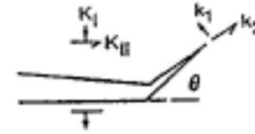
E. Munch...RO Ritchie, *Science*, 2008

How do we improve a materials resistance to crack propagation?



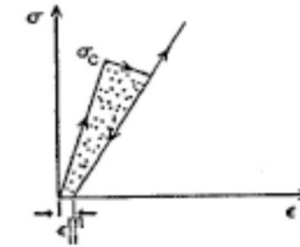
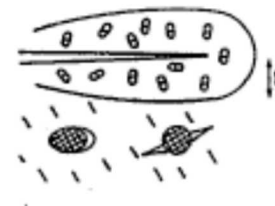
Extrinsic toughening mechanisms for brittle materials

- CRACK DEFLECTION



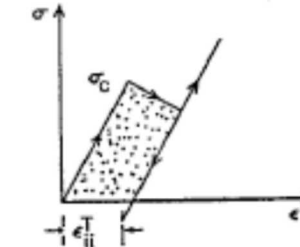
- MICROCRACK TOUGHENING:

$$\Delta(K) \sim E' f_v \varepsilon_s^m \sqrt{h}$$



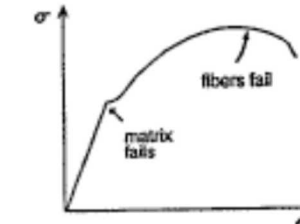
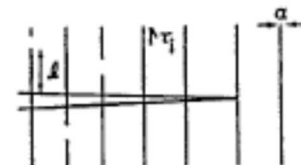
- TRANSFORMATION TOUGHENING:

$$\Delta(K) \sim E' f_v \varepsilon_s^T \sqrt{h}$$



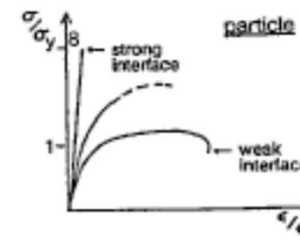
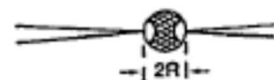
- BRITTLE FIBER/WHISKER TOUGHENING:
(crack bridging)

$$\Delta(K) \sim (2 f_v E' \tau_i \ell^2 / \alpha)^{1/2}$$

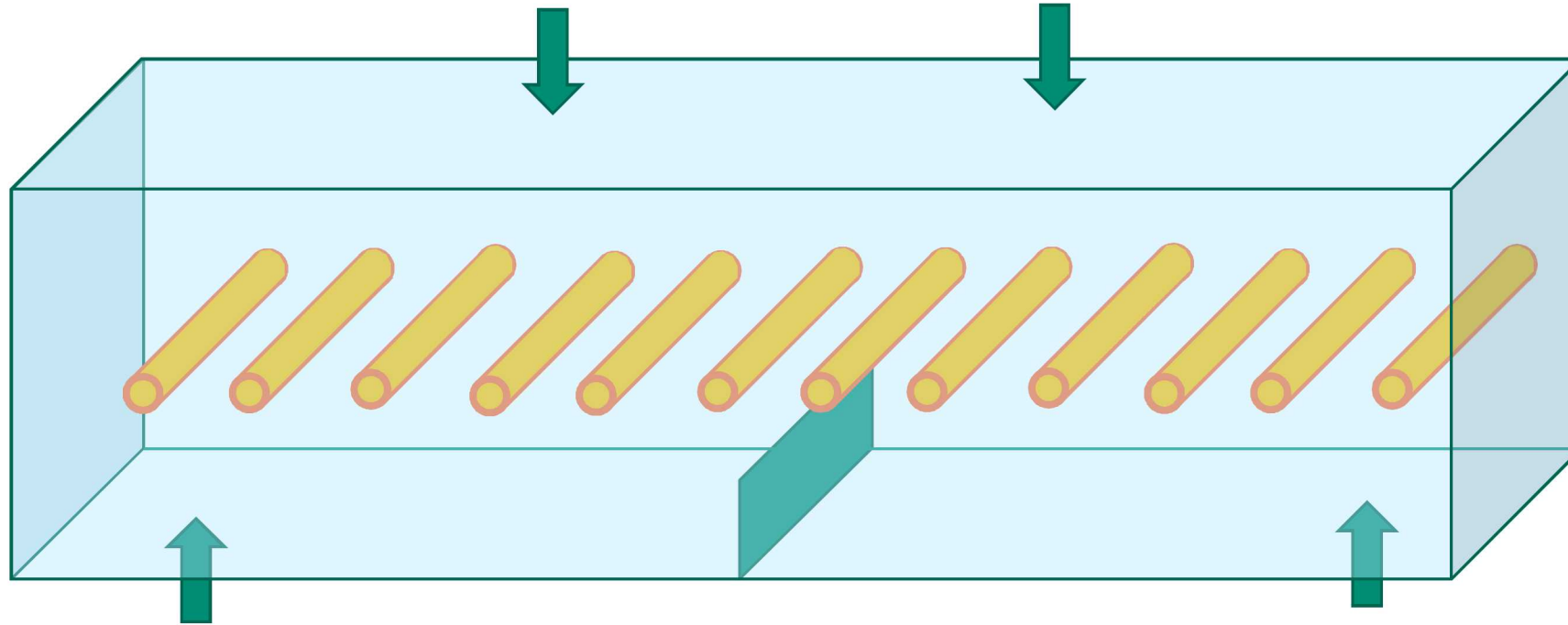


- DUCTILE PARTICLE TOUGHENING:

$$\Delta(K) \sim (C E' \sigma_y R f_v)^{1/2}$$



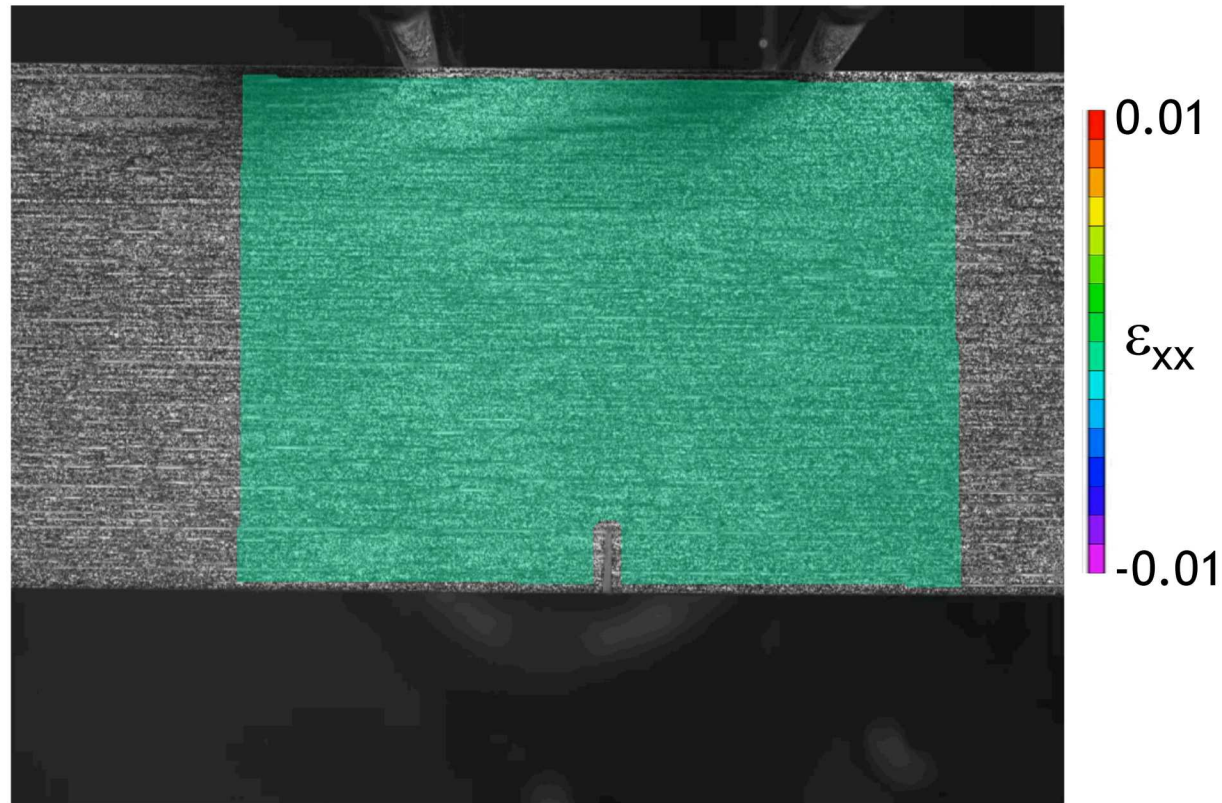
A simple proof of concept topology: Periodic array of cylindrical holes in an “arrestor” orientation



Limiting crack propagation in a brittle glassy polymer

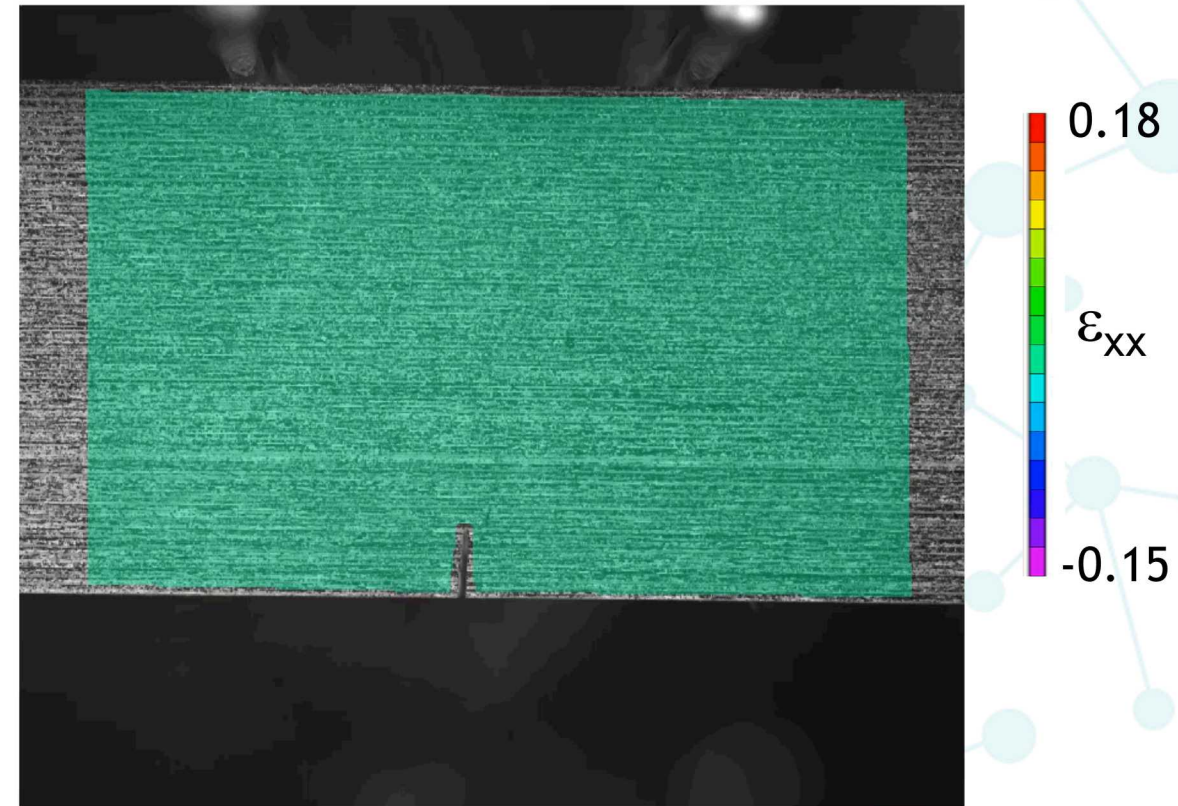
Unmodified

3 mm

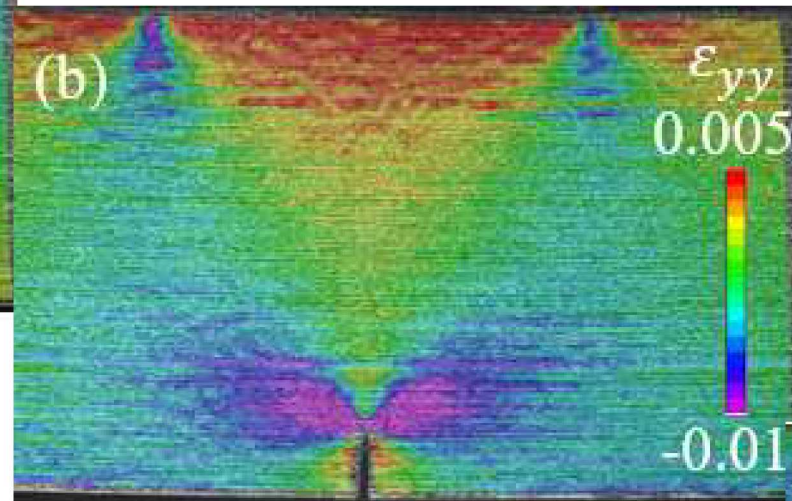
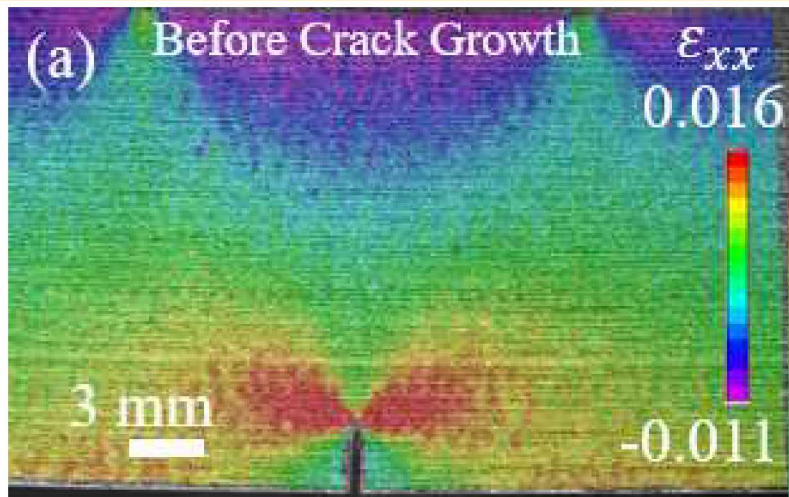


93% Dense... Four rows of cylindrical holes

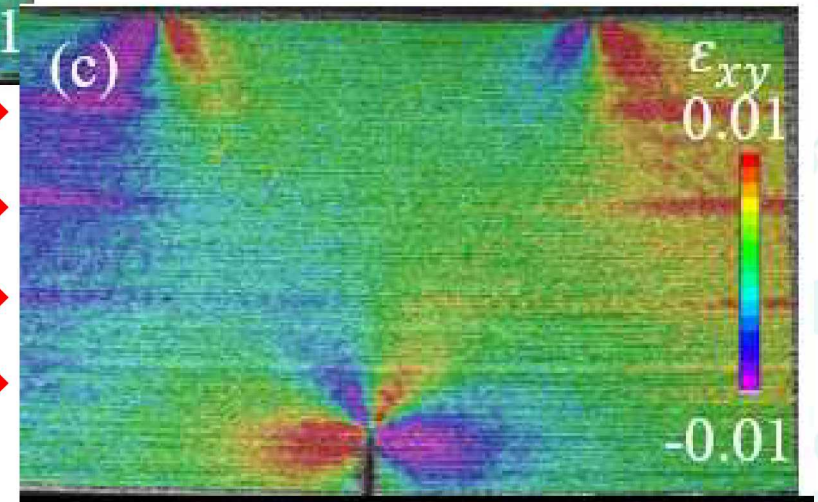
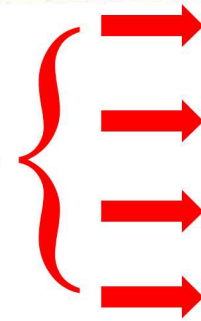
3 mm



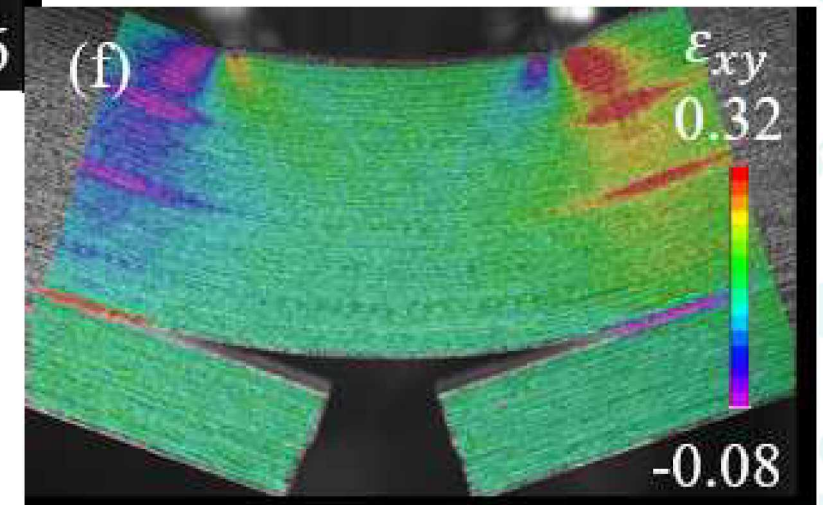
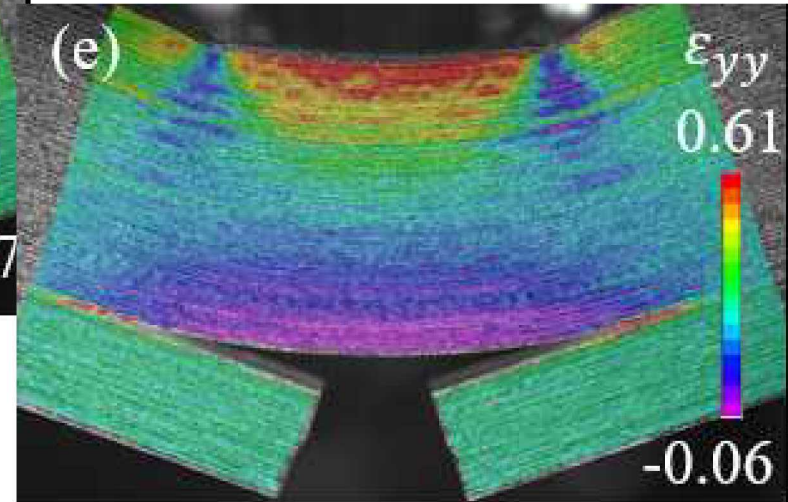
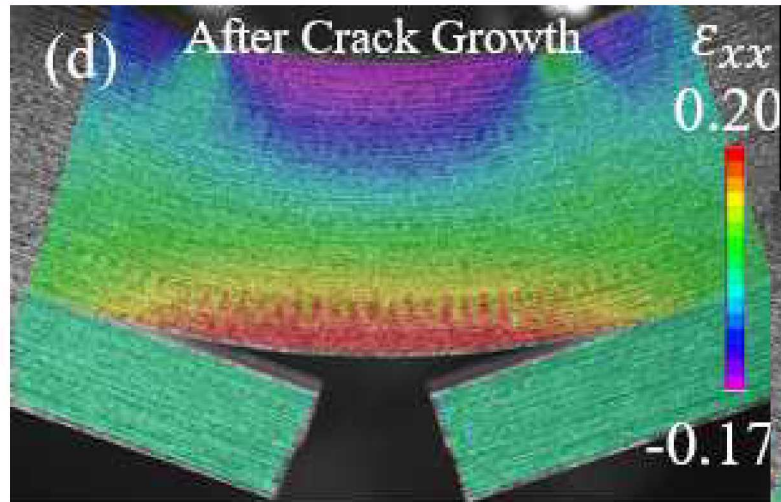
Material: Stratsys Durus, Polypropylene-like UV-Cured Glassy Polymer



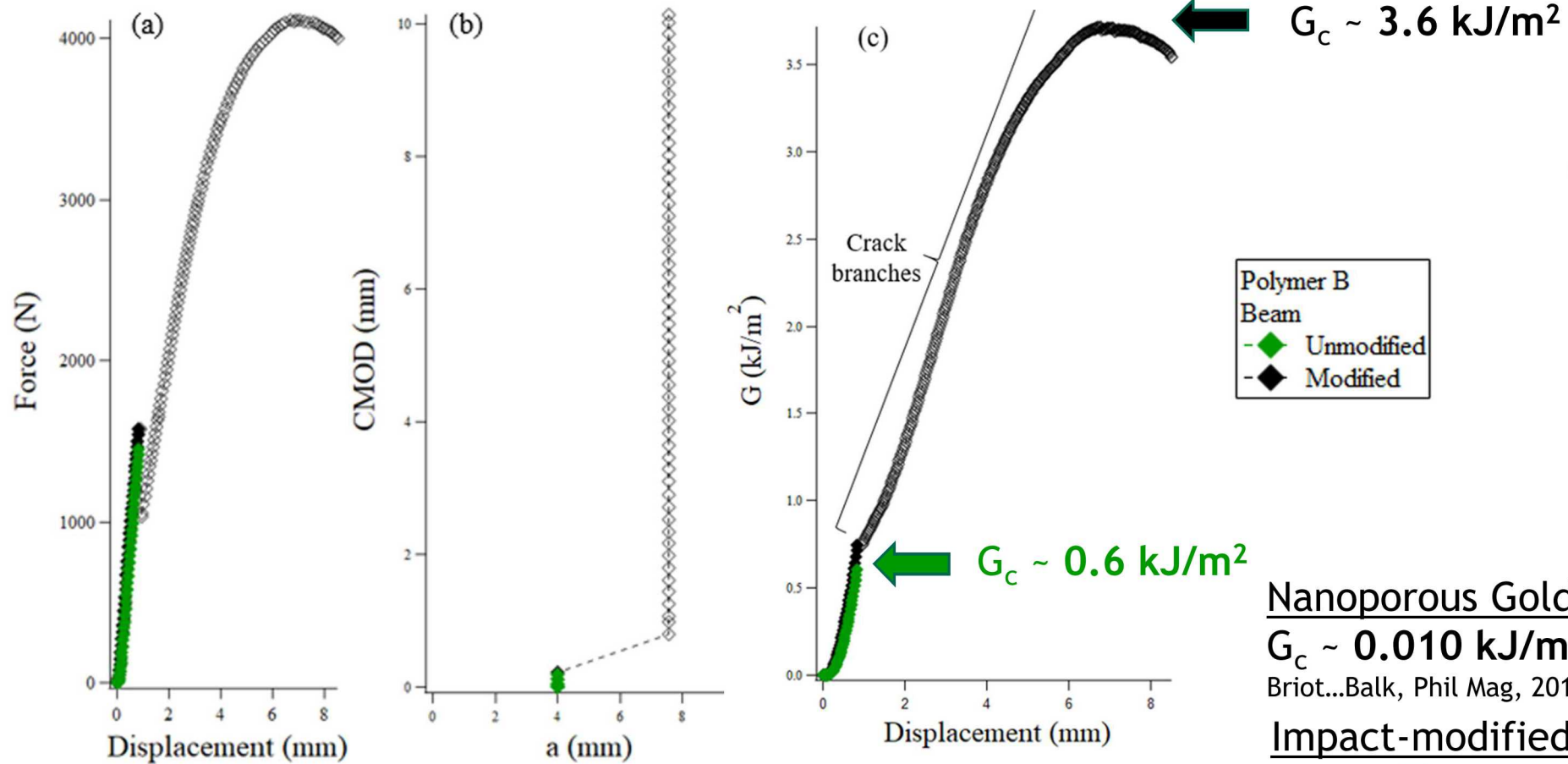
Planes of cylindrical perforations



Crack deflection, branching, pseudo-delamination along planes of cylindrical holes



600% improvement in fracture toughness over *base material* by adding air!



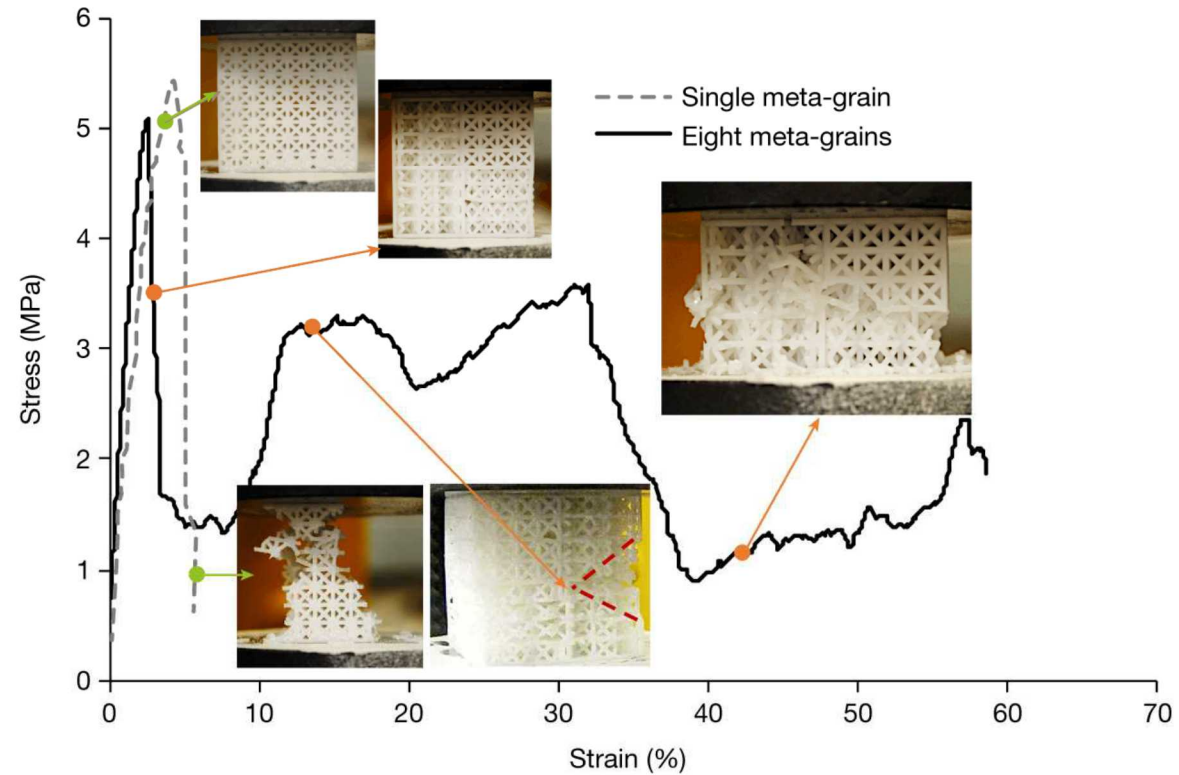
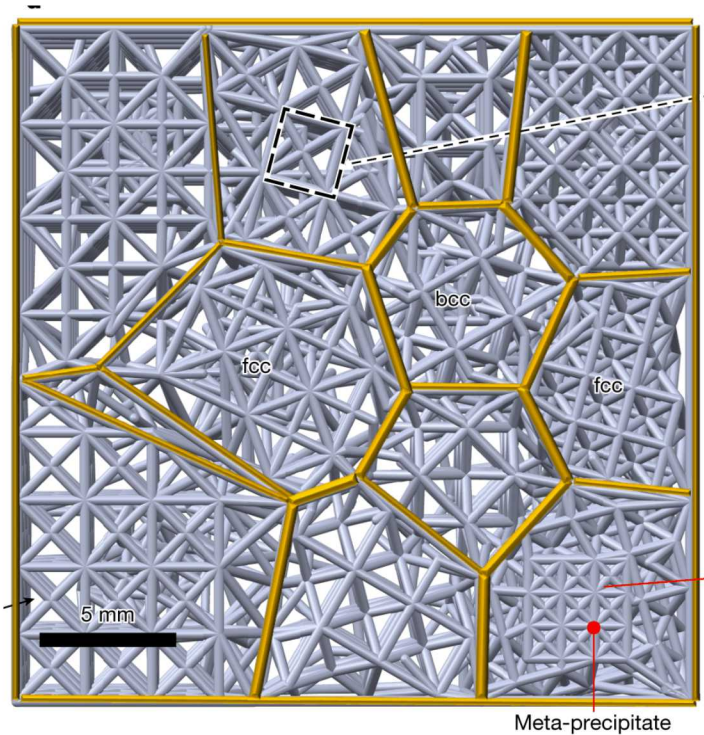
Nanoporous Gold,
 $G_c \sim 0.010$ kJ/m² density = 6.4 g/cm³
Briot...Balk, Phil Mag, 2014

Impact-modified Polypropylene

$G_c = 2-5$ kJ/m²
Li, Li, Tong, *Polymer Testing*, 1997

Are lattices tougher than foams?

Toughness vs Fracture Toughness

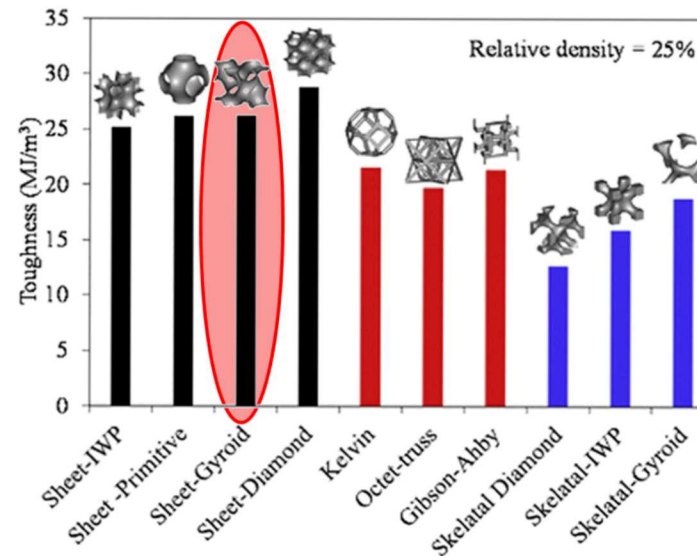
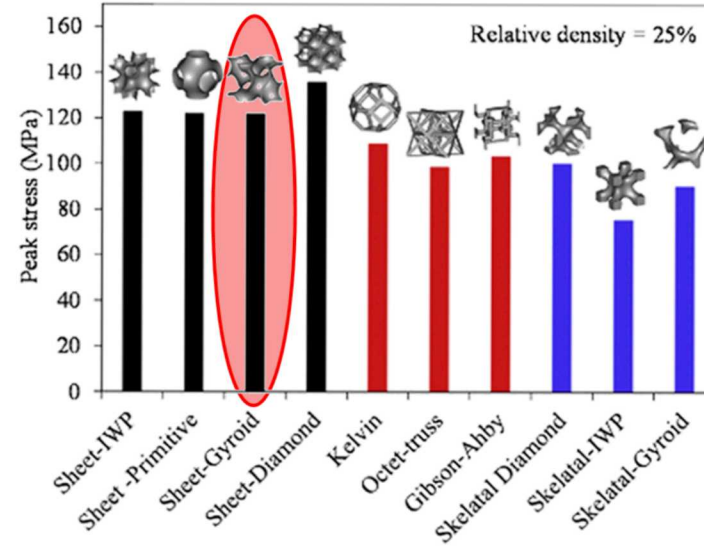
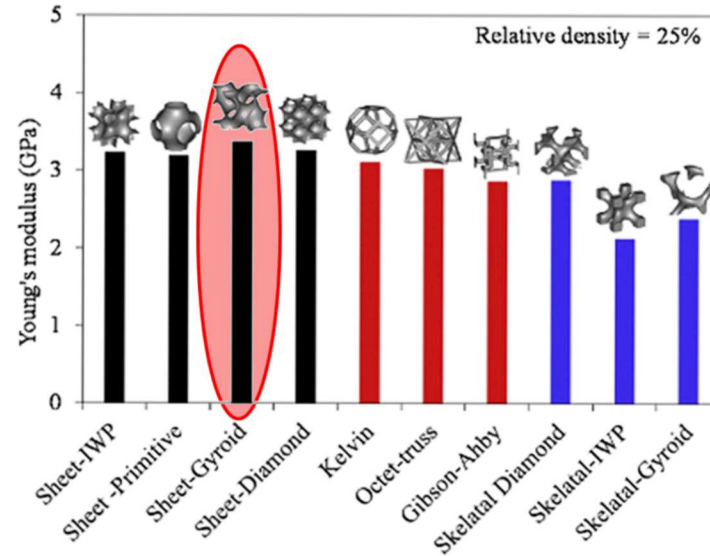


The gyroid lattice: a triply periodic minimum surface

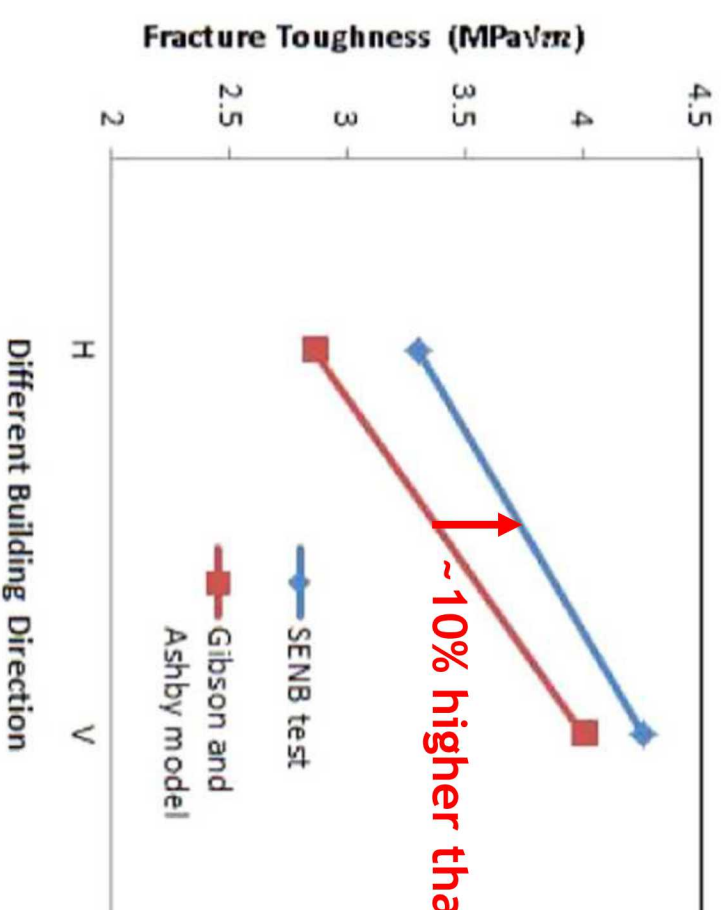
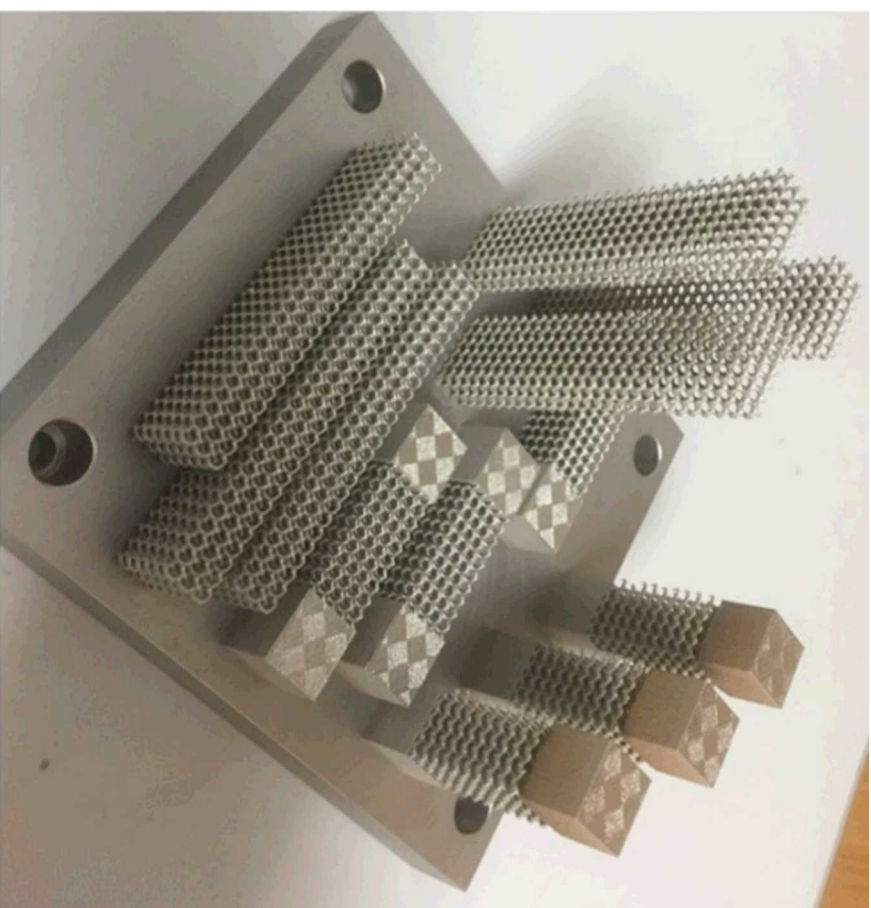


$$\sin x \cos y + \sin y \cos z + \sin z \cos x = 0$$

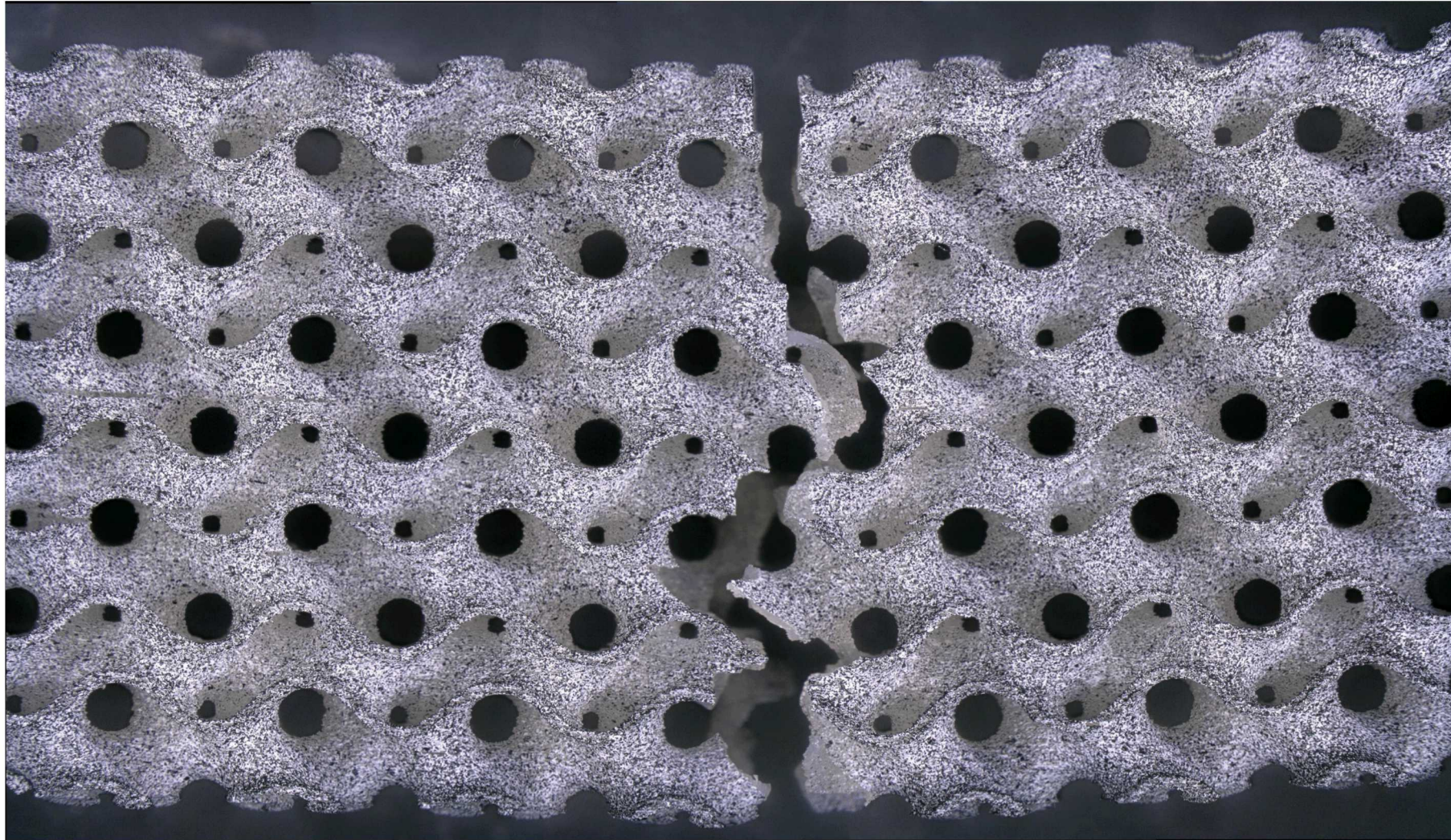
Why the gyroid?



15% dense 316L gyroid

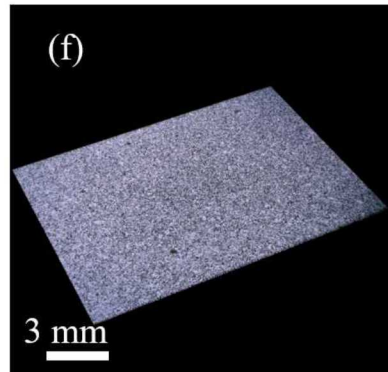
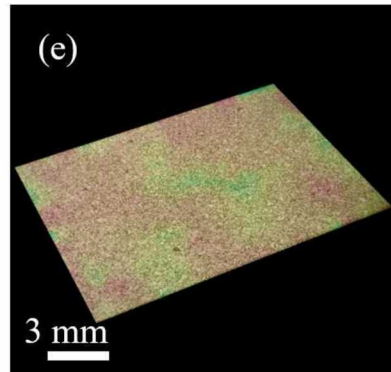
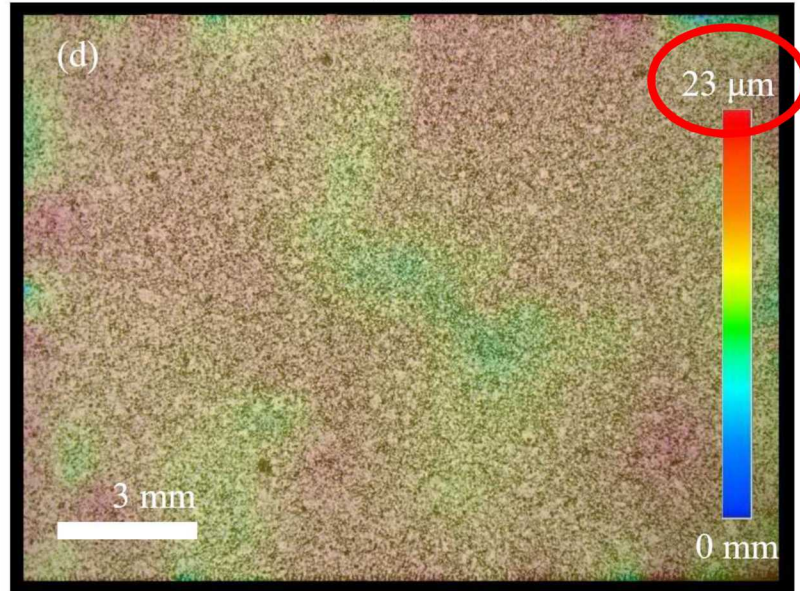


Crack deflection...

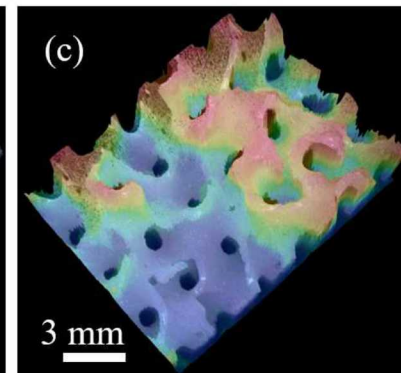
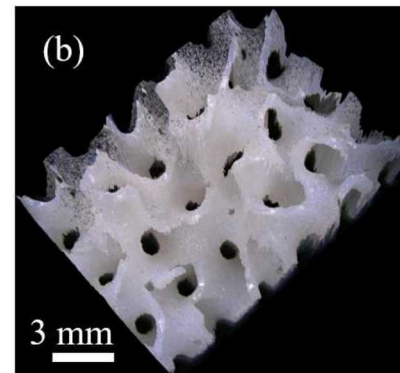
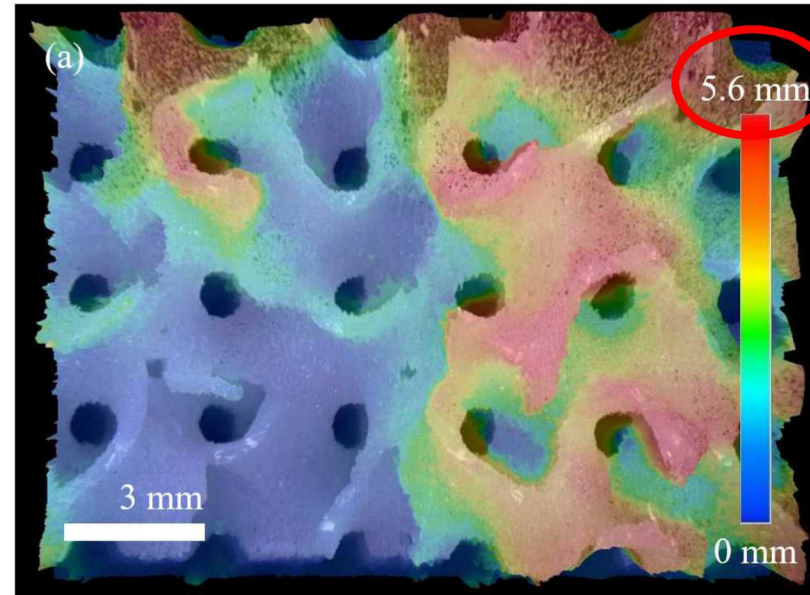


The Gyroid architecture toughens by crack deflection...

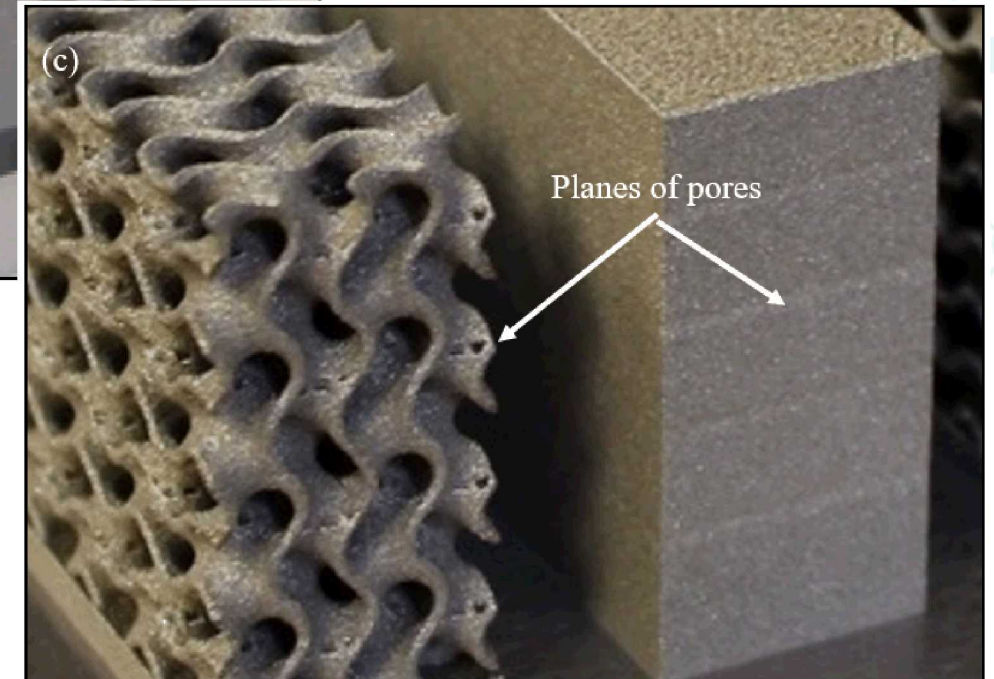
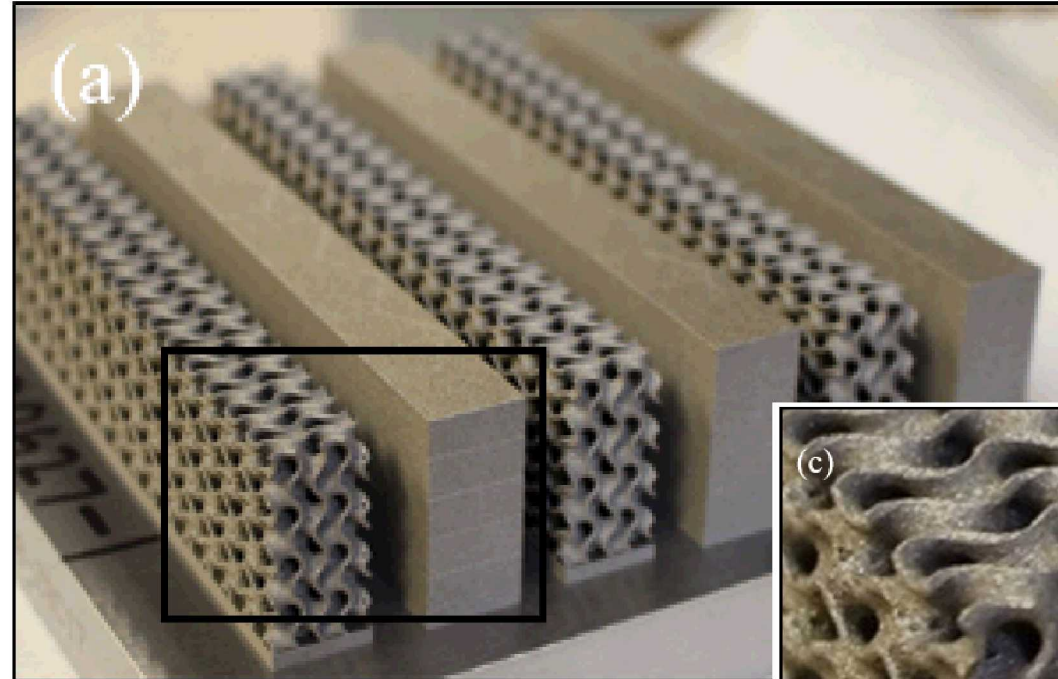
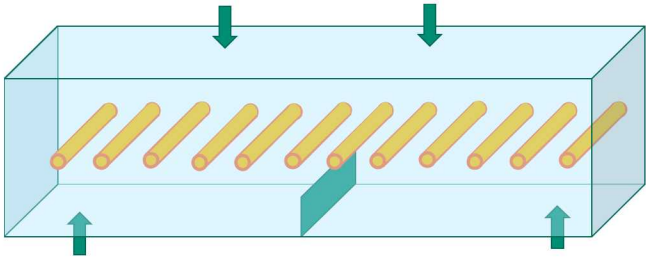
Fracture surface of solid material:
brittle UV-cured polymer, Verowhite



Fracture surface of gyroid architecture:
same brittle polymer, Verowhite

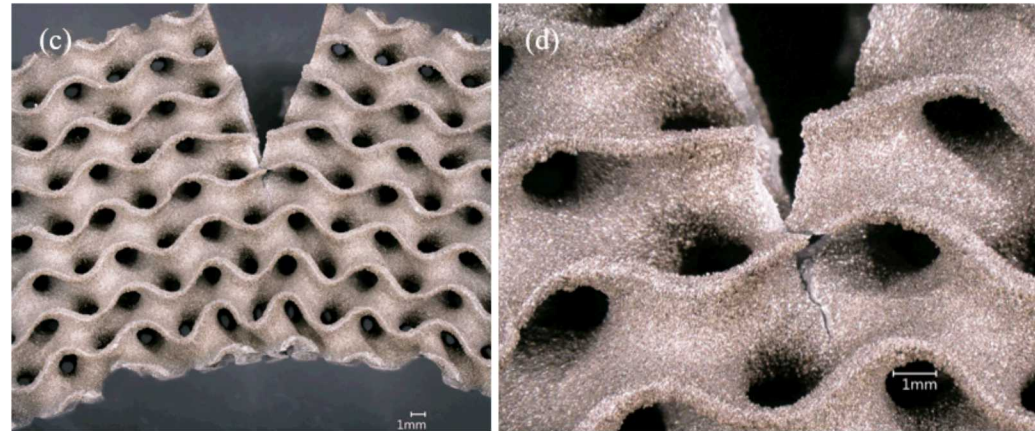


Can we further toughen a gyroid by adding hierarchical porosity?

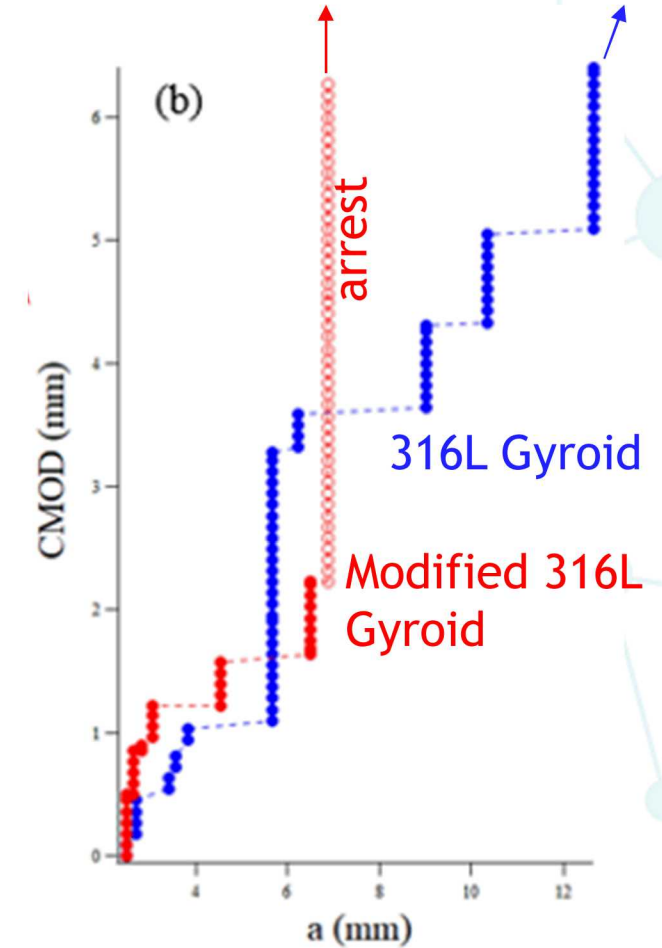
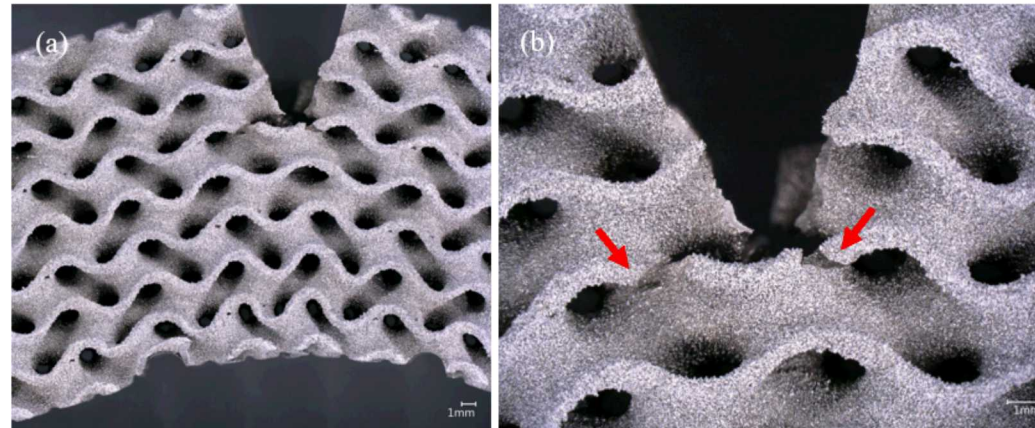


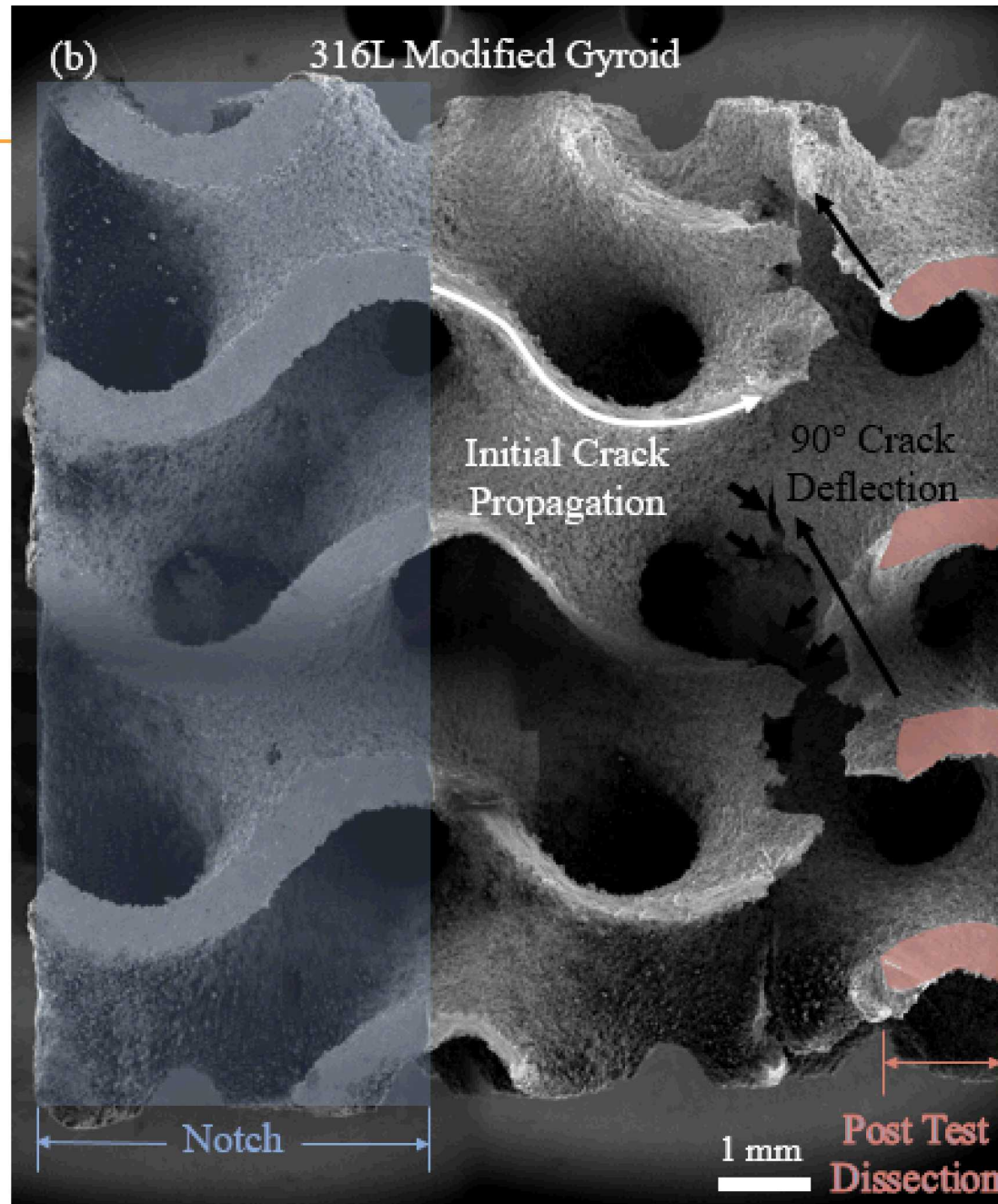
Crack deflection by additional porosity

Unmodified gyroid, 316L



Gyroid with additional cylindrical pores, 316L

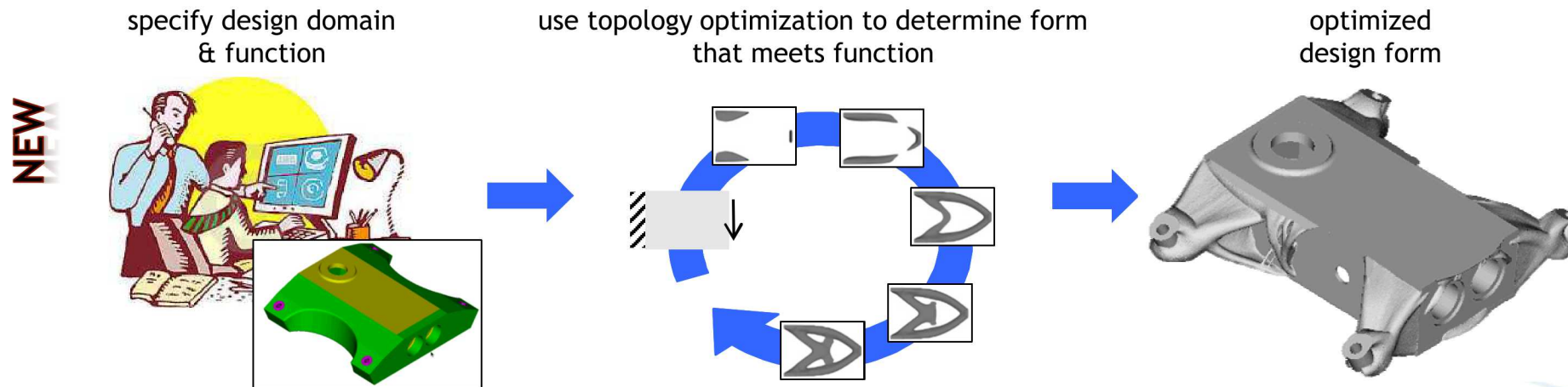
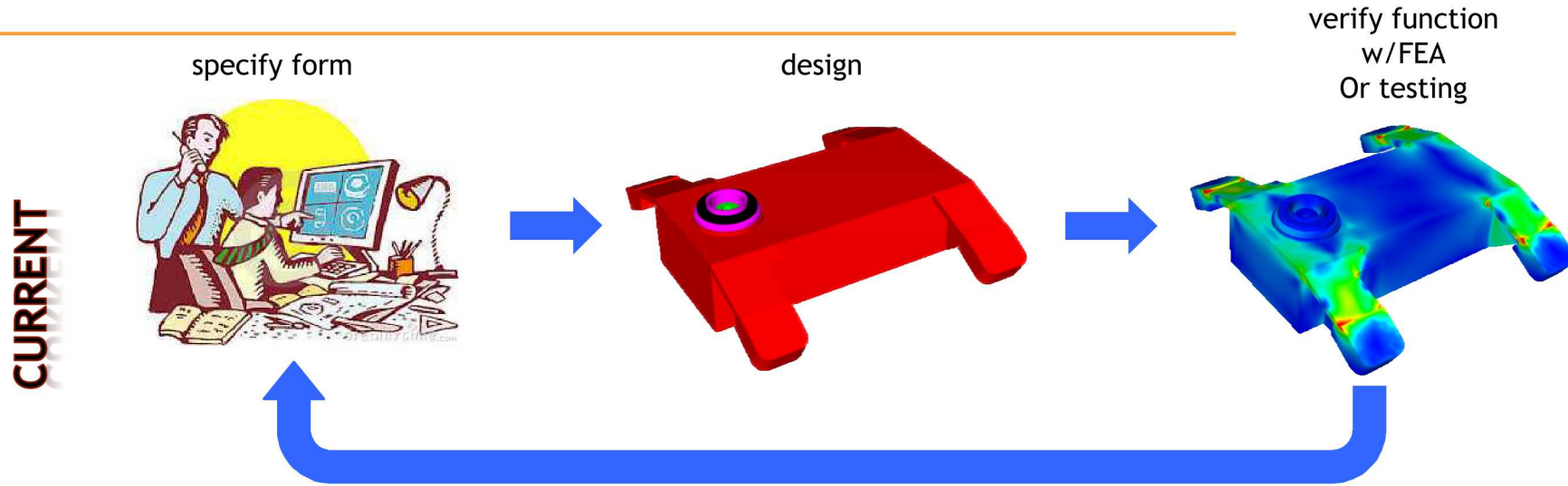




Additive manufacturing enables generative design...

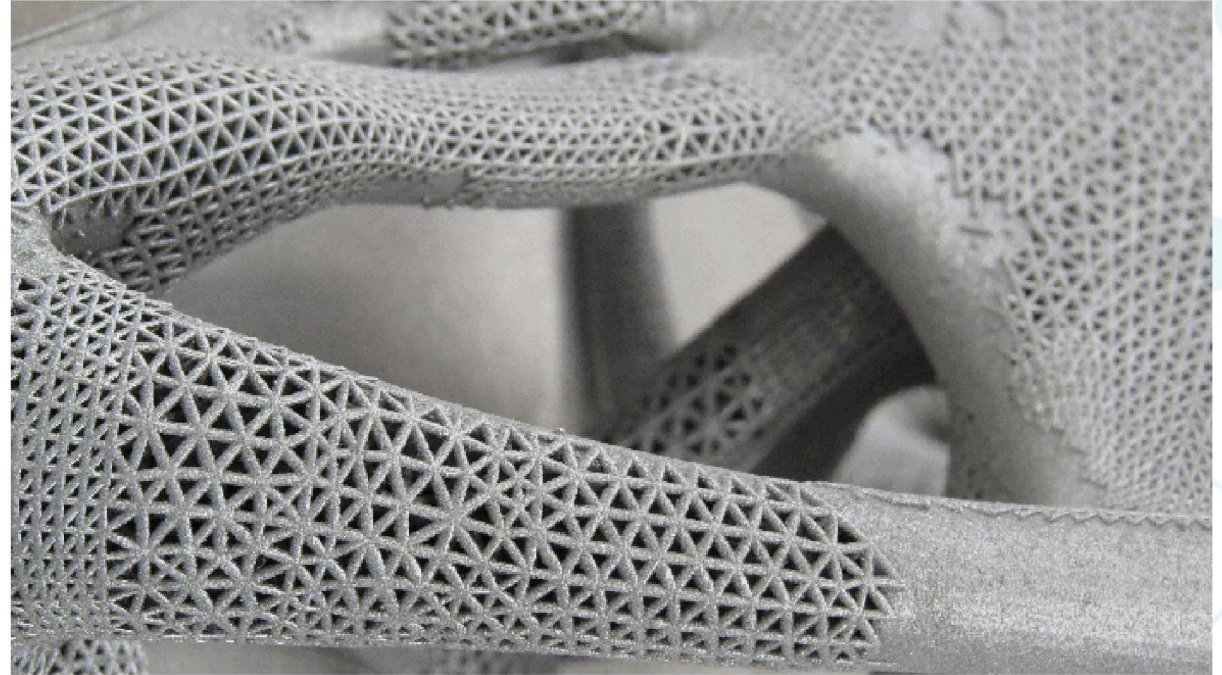
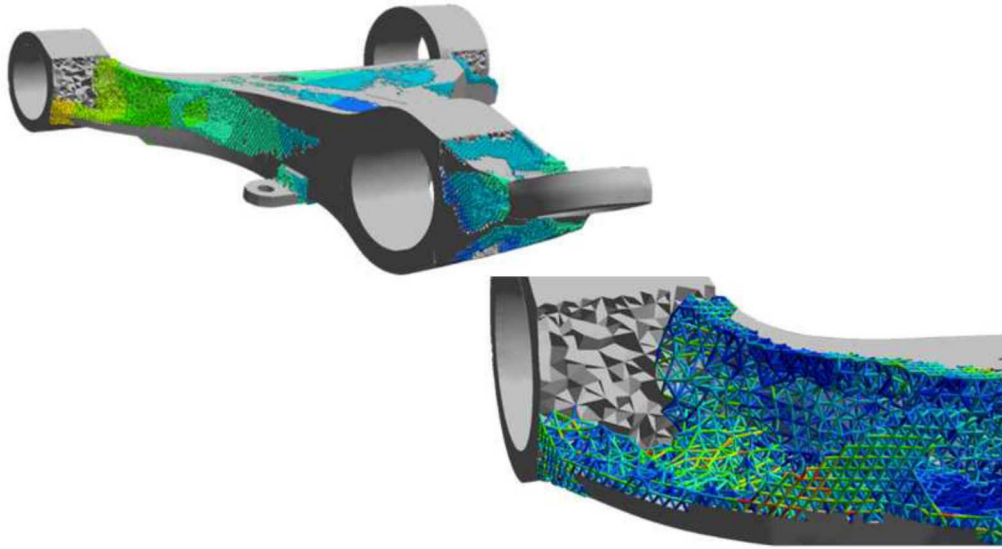


Topology optimization, a form of generative design



Galjaard, Hofman and Ren,
Biomimetic Lightweight..., 2015

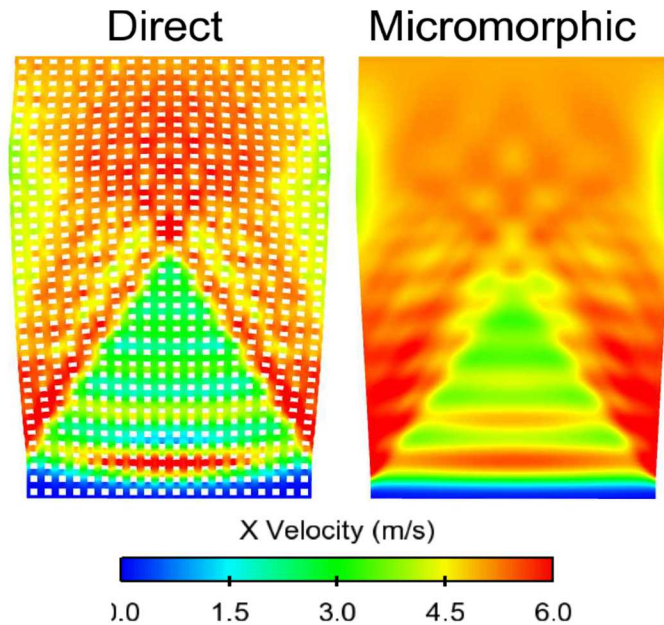
Two-scale topology optimization for fracture resistance?



Examples: nTopology, Altair hyperworks

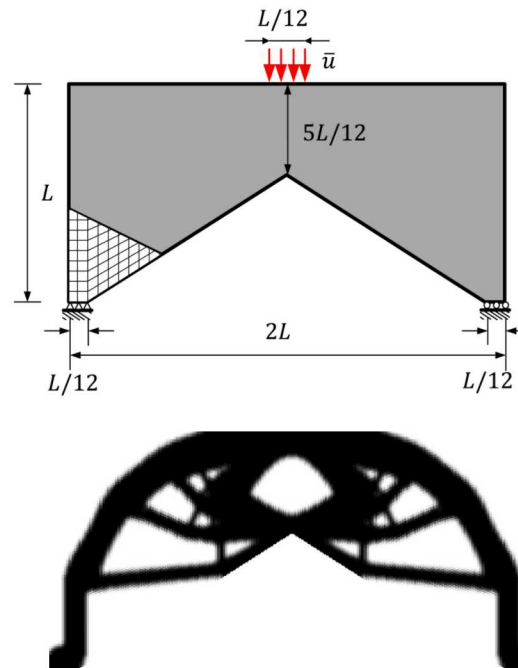
Three challenges for optimized design of fracture resistance

1. For computational tractability, you must employ **homogenization**



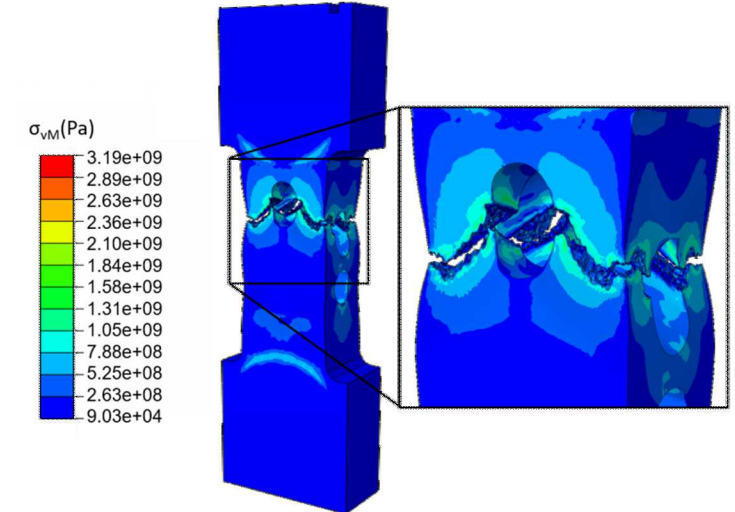
Dingreville, Robbins, Voth, *JOM*, 2013

2. **Nonlinear** elastoplastic response is path dependent: challenging for optimization



Alberdi, Zhang, Khandelwal, *Numerical Methods in Eng.*, 2018

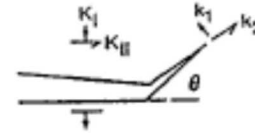
3. Predicting **ductile rupture** in FEA is challenging



Kramer...Boyce, *Int. J. Fracture*, 2019

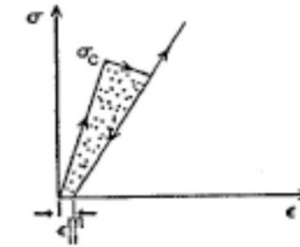
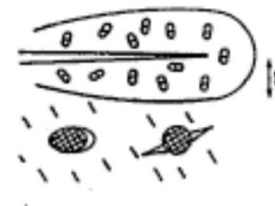
Extrinsic toughening mechanisms for brittle materials

- CRACK DEFLECTION



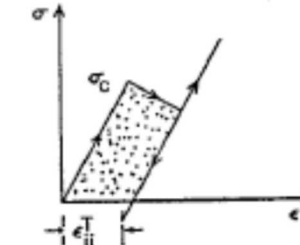
- MICROCRACK TOUGHENING:

$$\Delta(K) \sim E' f_v \varepsilon_m^m \sqrt{h}$$



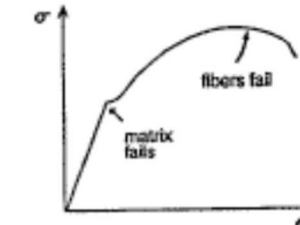
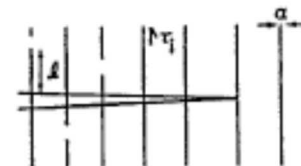
- TRANSFORMATION TOUGHENING:

$$\Delta(K) \sim E' f_v \varepsilon_t^T \sqrt{h}$$



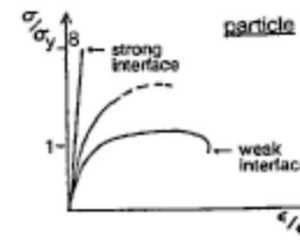
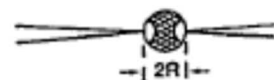
- BRITTLE FIBER/WHISKER TOUGHENING:
(crack bridging)

$$\Delta(K) \sim (2 f_v E' \tau_i \ell^2 / \alpha)^{1/2}$$

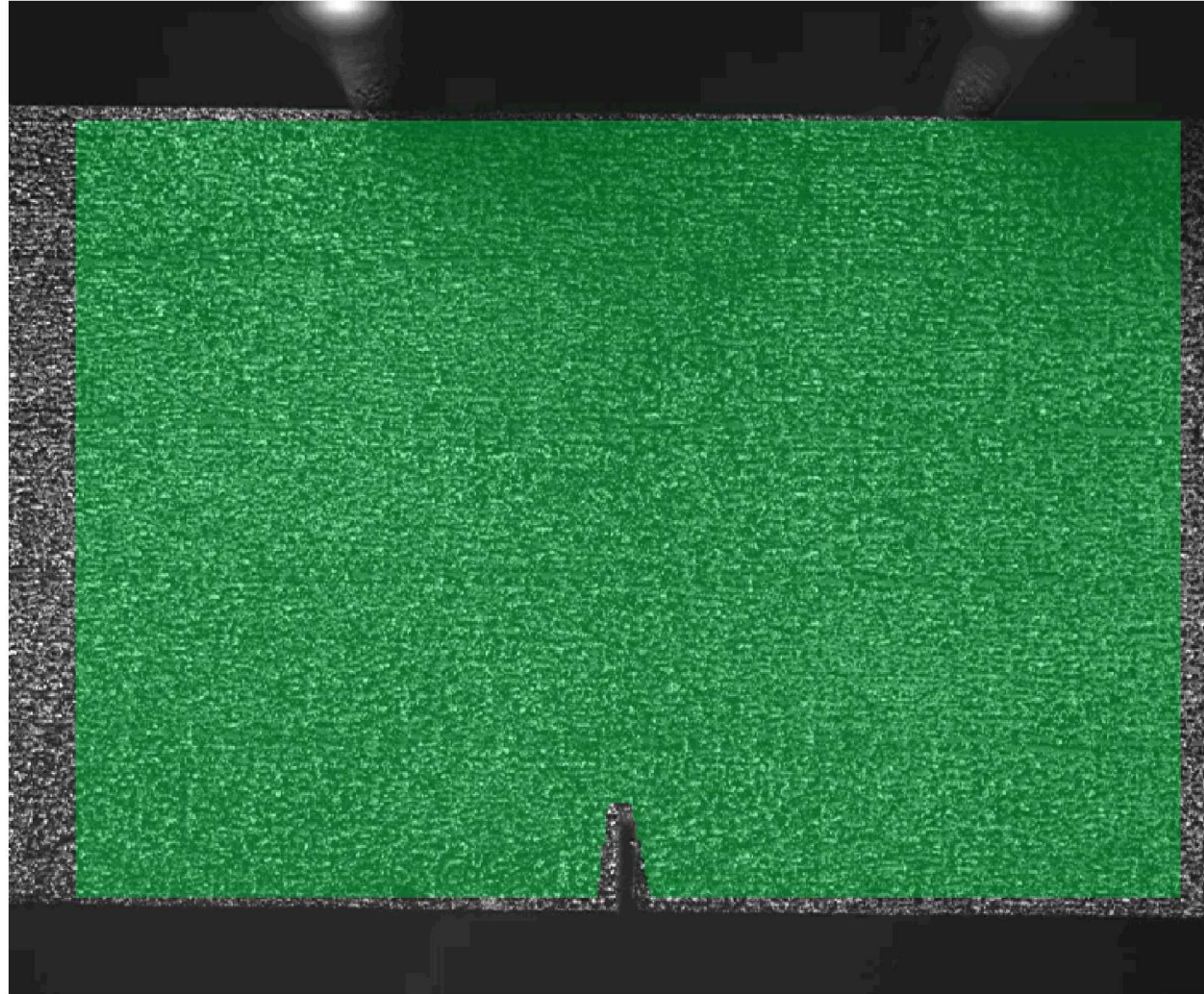
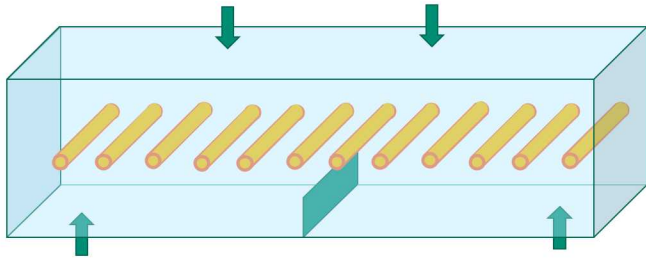


- DUCTILE PARTICLE TOUGHENING:

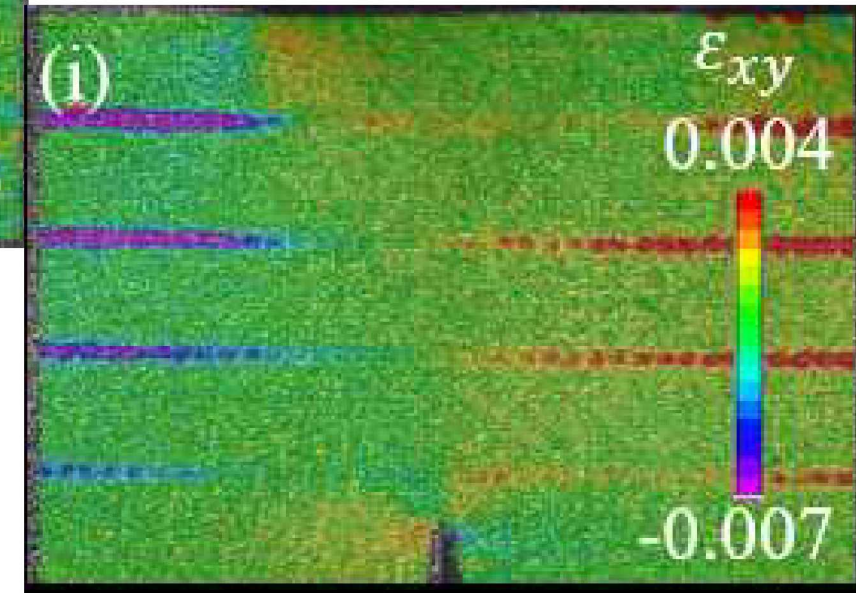
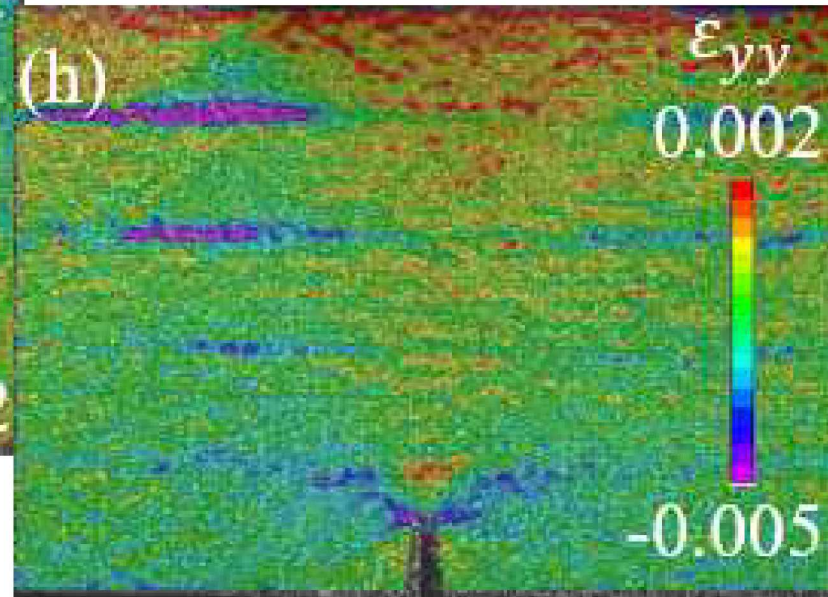
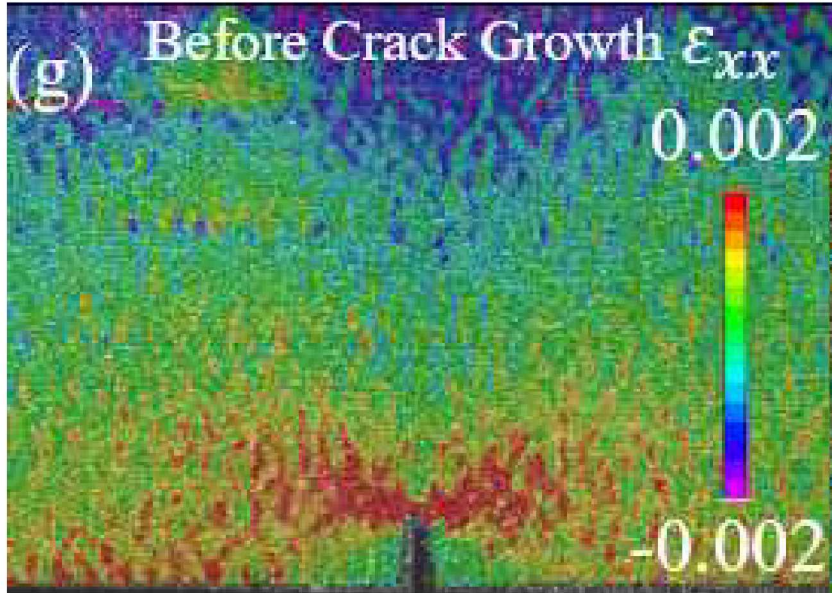
$$\Delta(K) \sim (C E' \sigma_y R f_v)^{1/2}$$



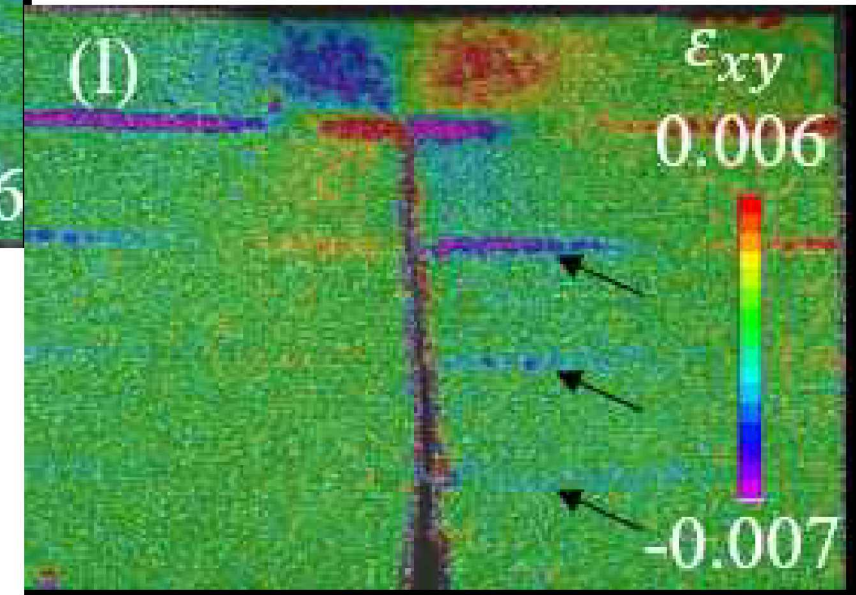
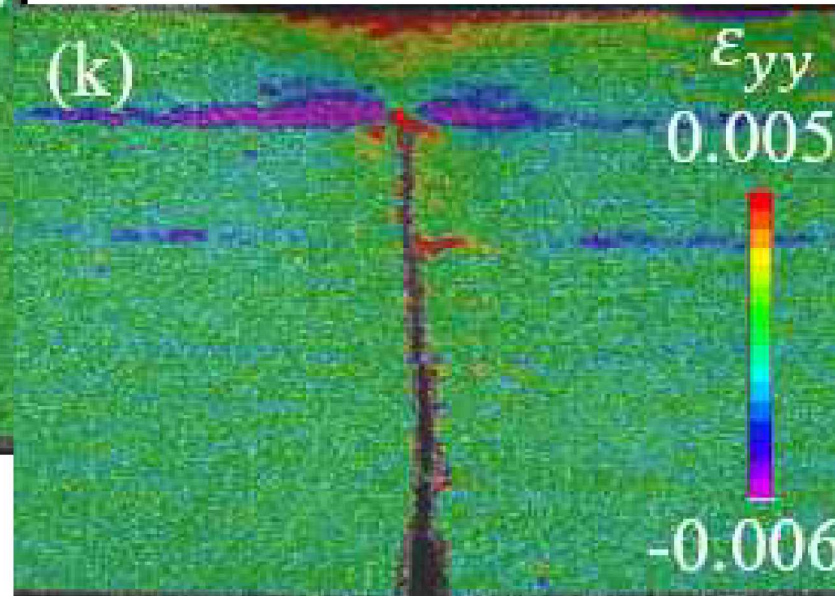
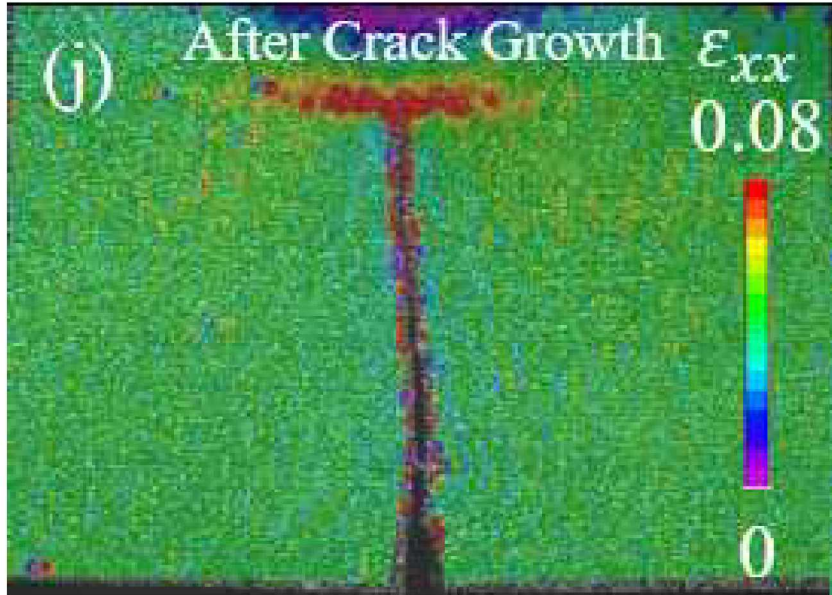
Another form of toughening: pseudo-blunting



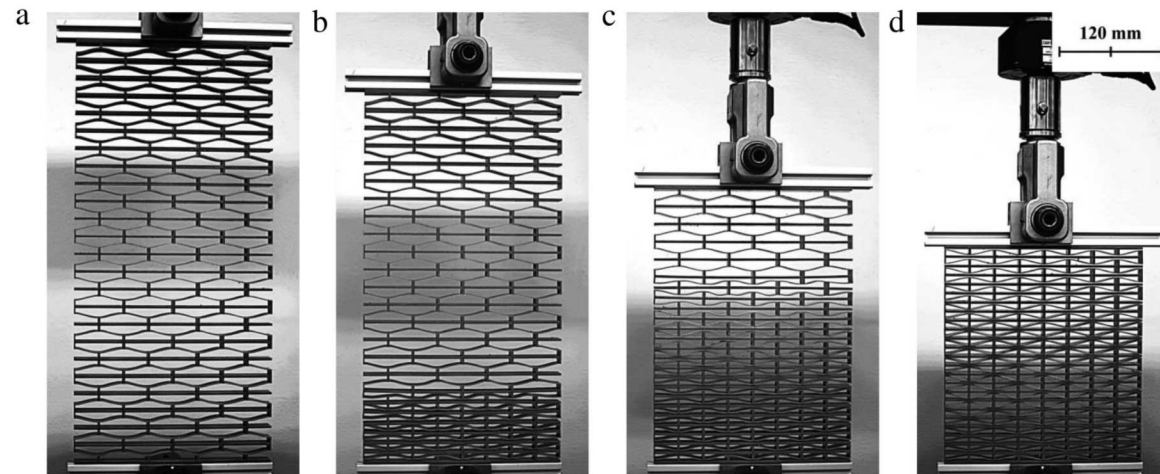
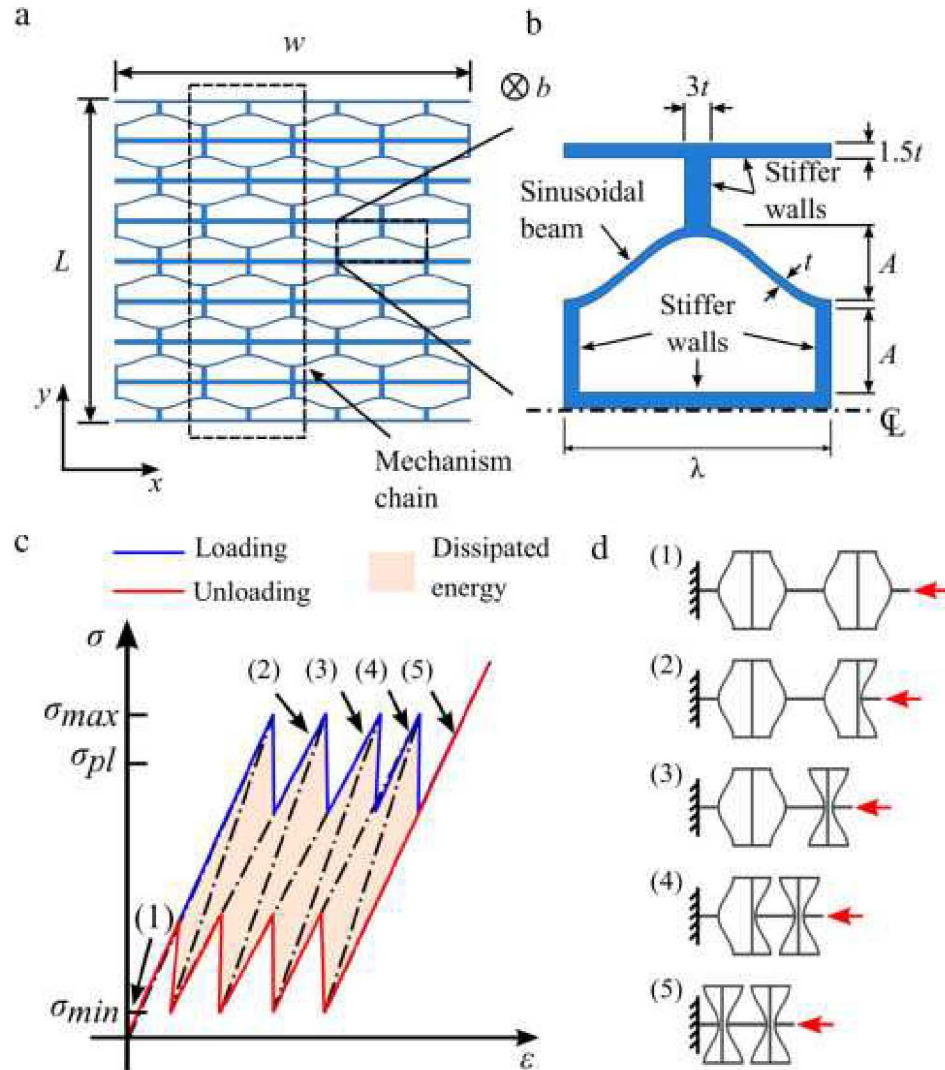
A second form of toughening: pseudo-blunting



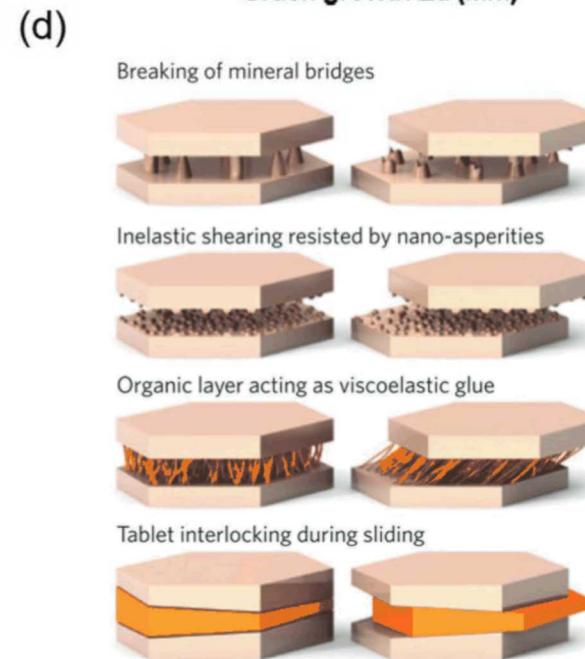
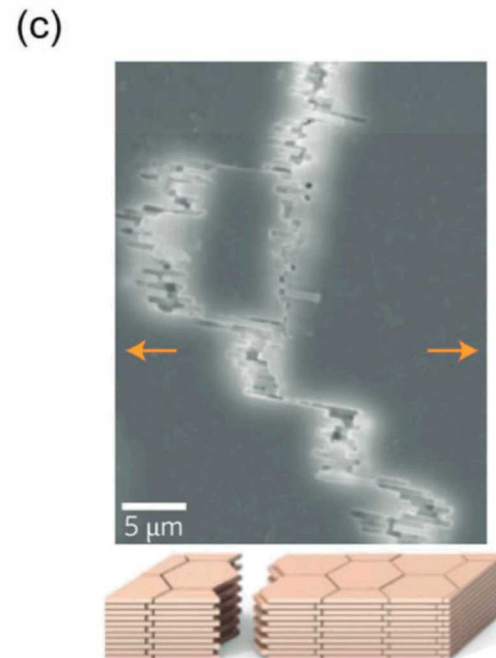
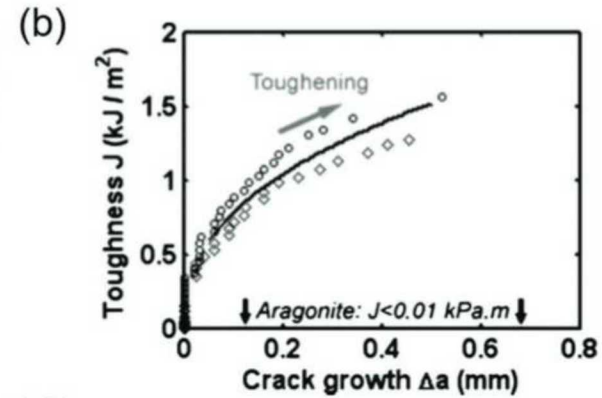
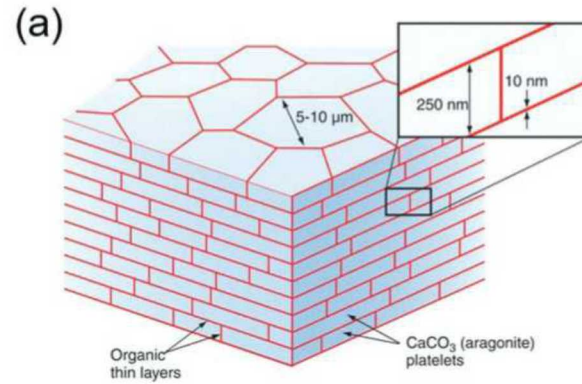
A second form of toughening: pseudo-blunting



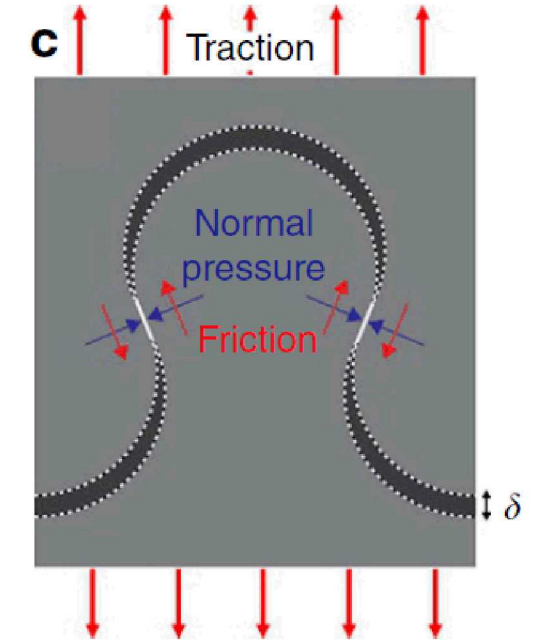
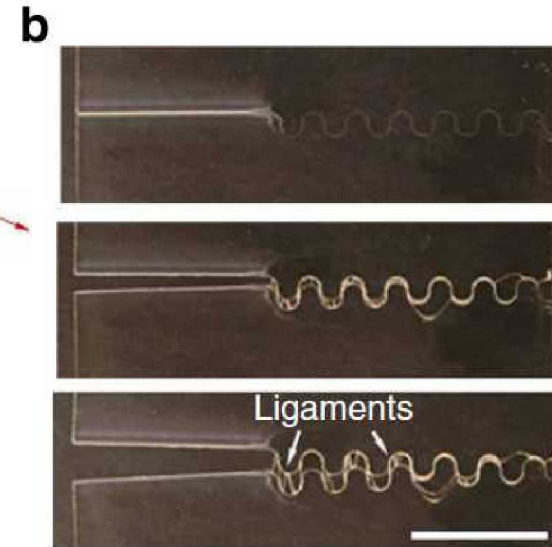
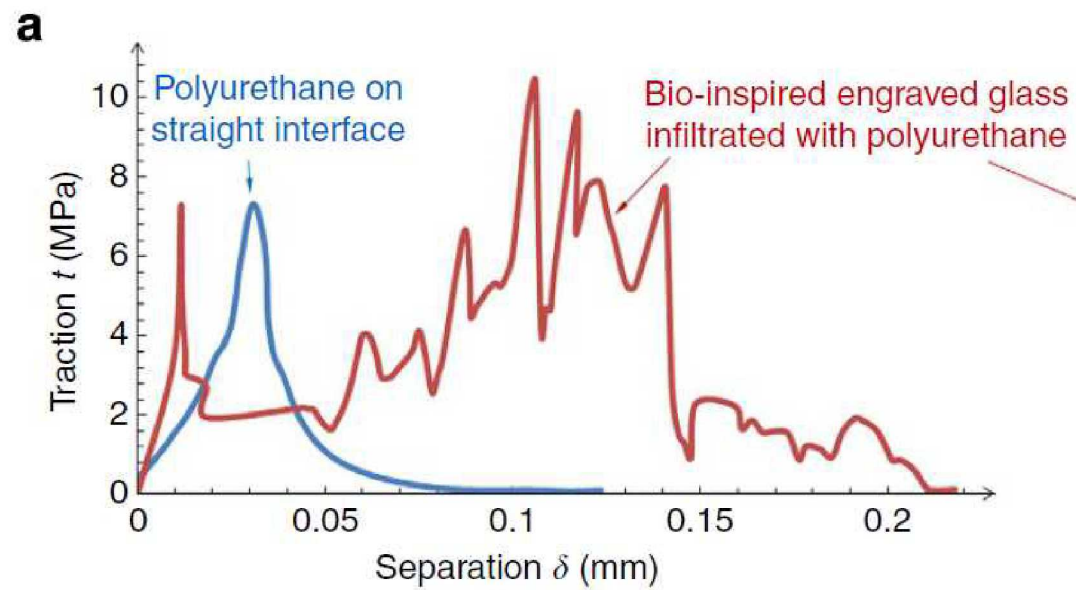
Any material can be a phase transforming material!



Localized shearing for toughening

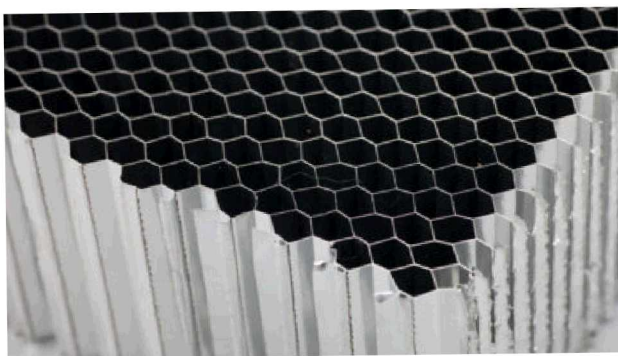


Etching a crack path on a brittle material...

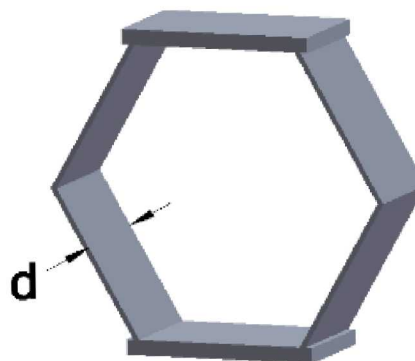
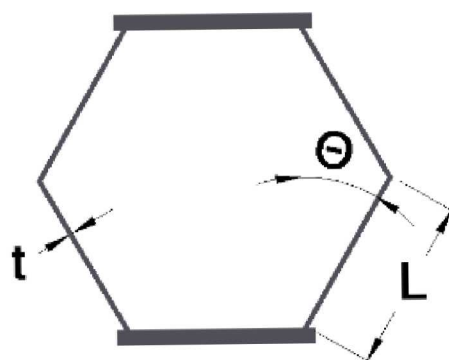


Mirkhalaf, Khayer Dastjerdi, Barthelat, *Nature Comm*, 2014

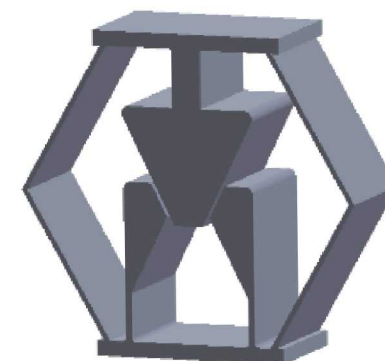
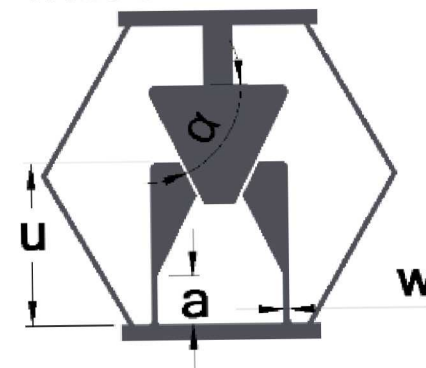
Adding friction to the honeycomb topology...



honeycomb

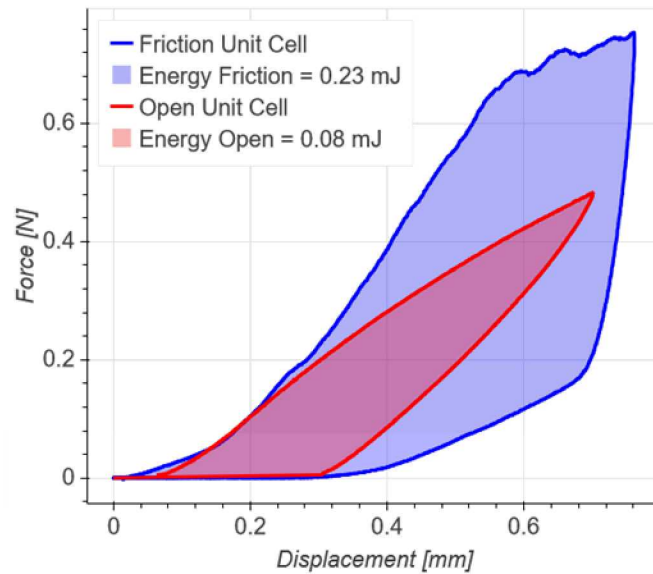
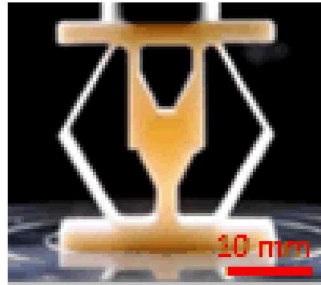


honeycomb with
friction elements

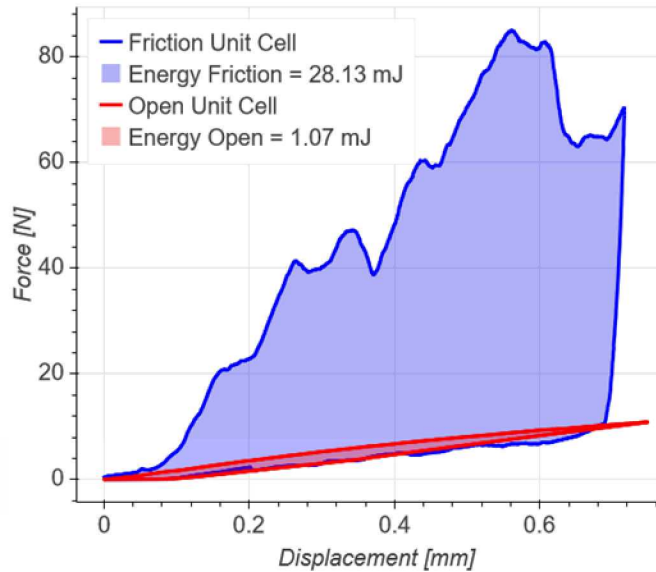
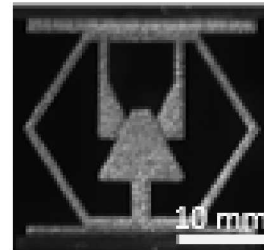


Architected energy dissipation

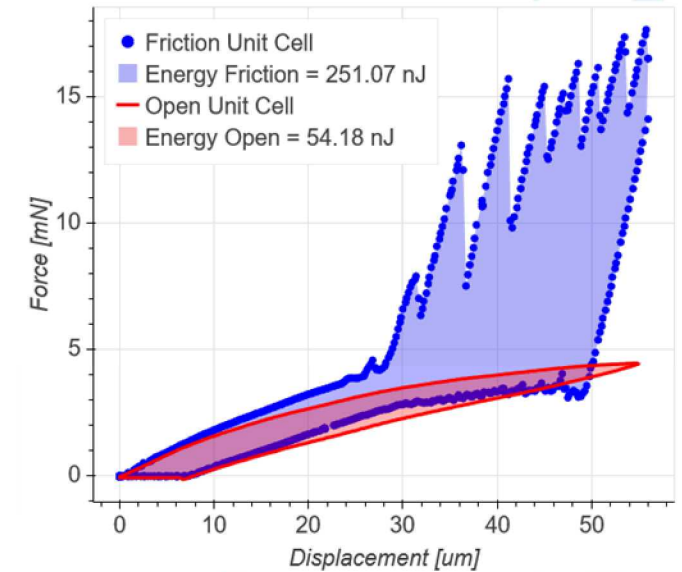
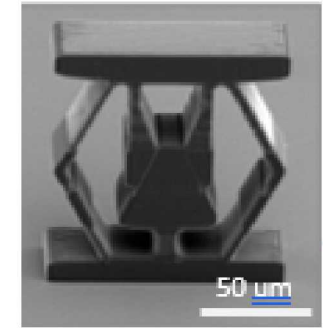
In a polymer



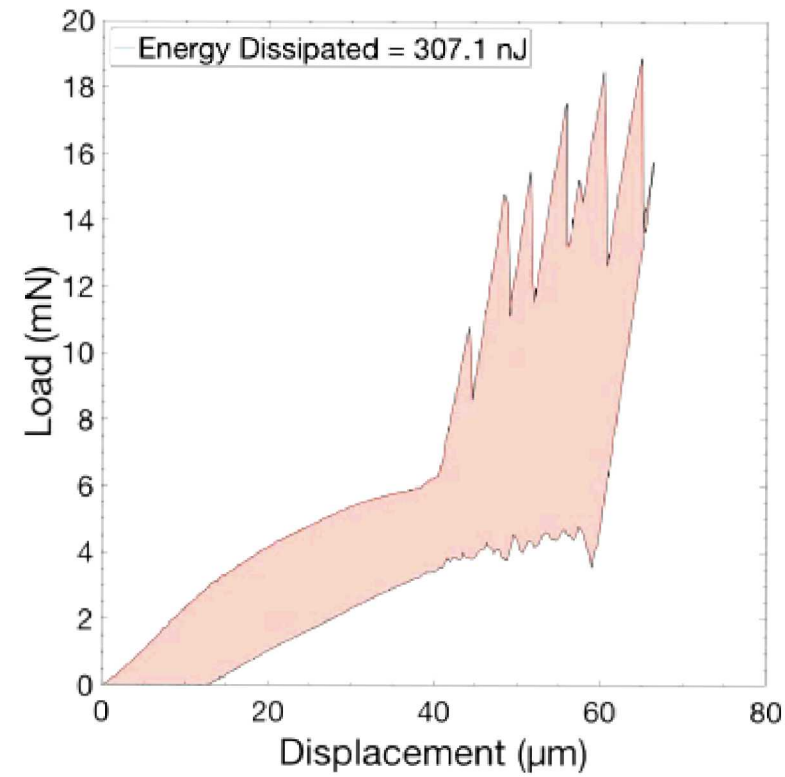
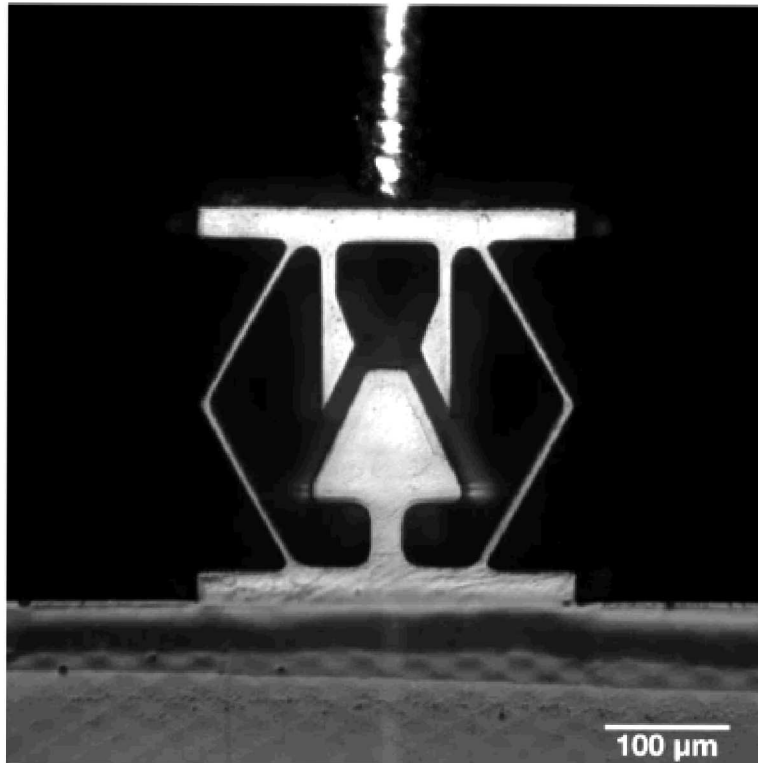
In a metal



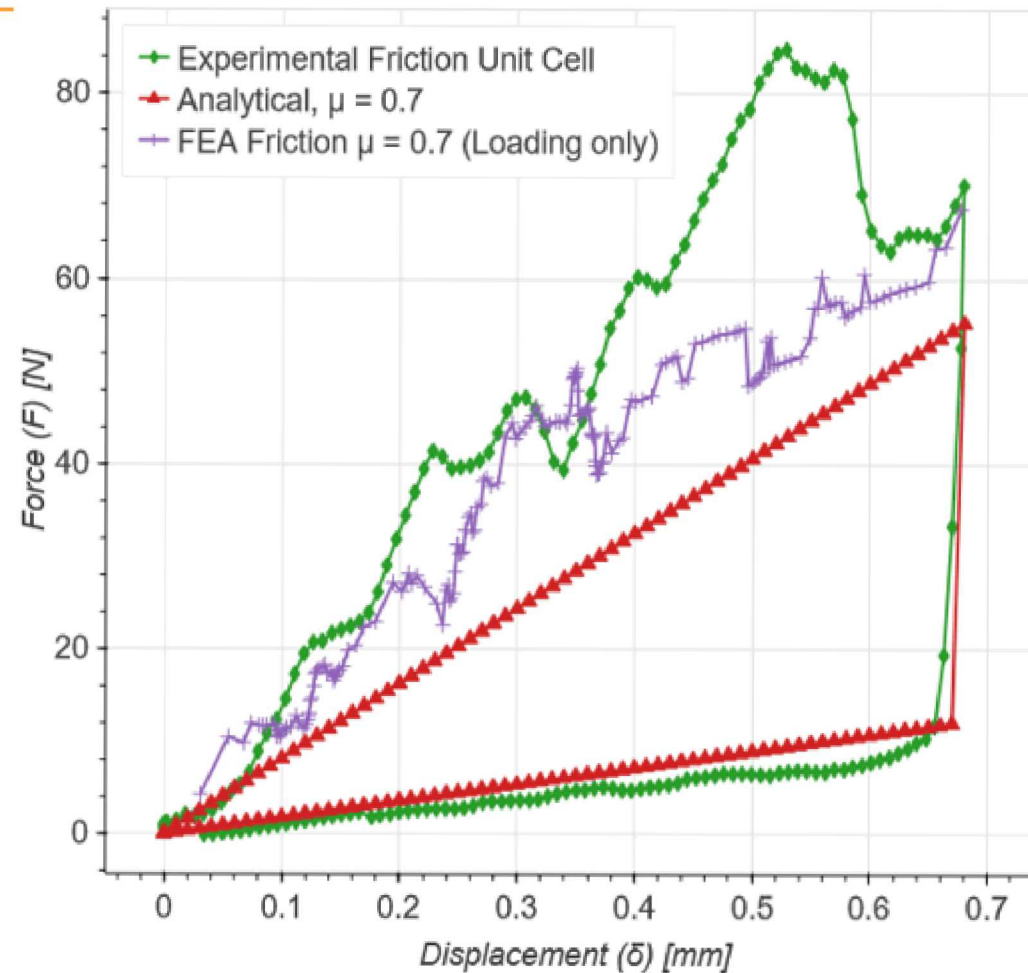
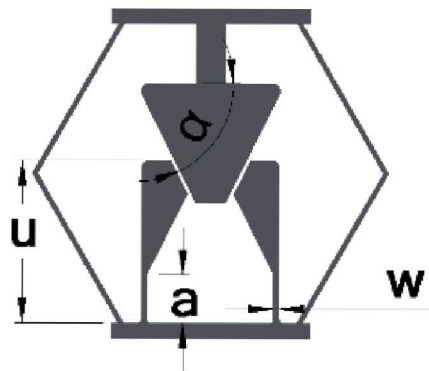
At the microscale



Architecting dissipation at the microscale...

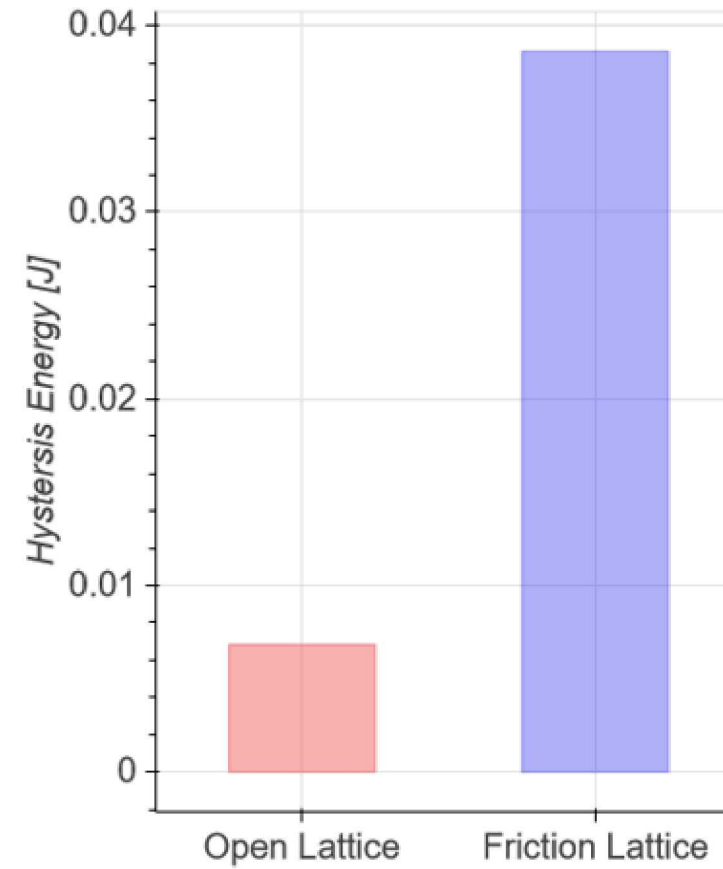
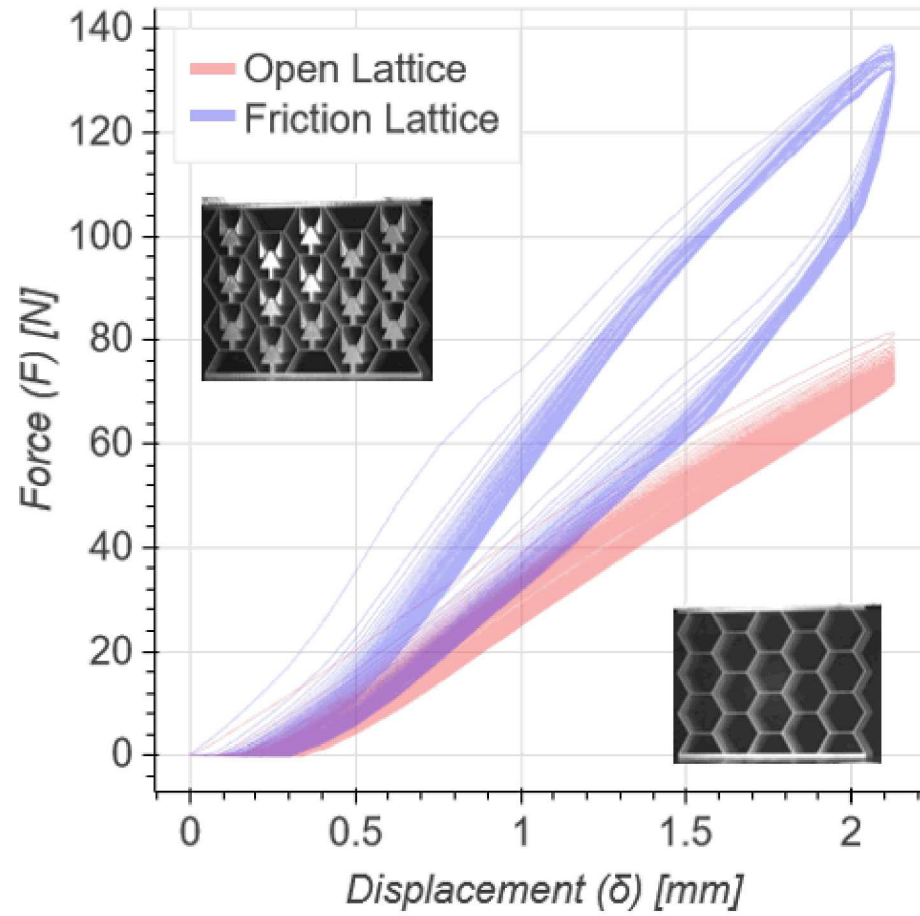


Behavior is predictable = “programmable”

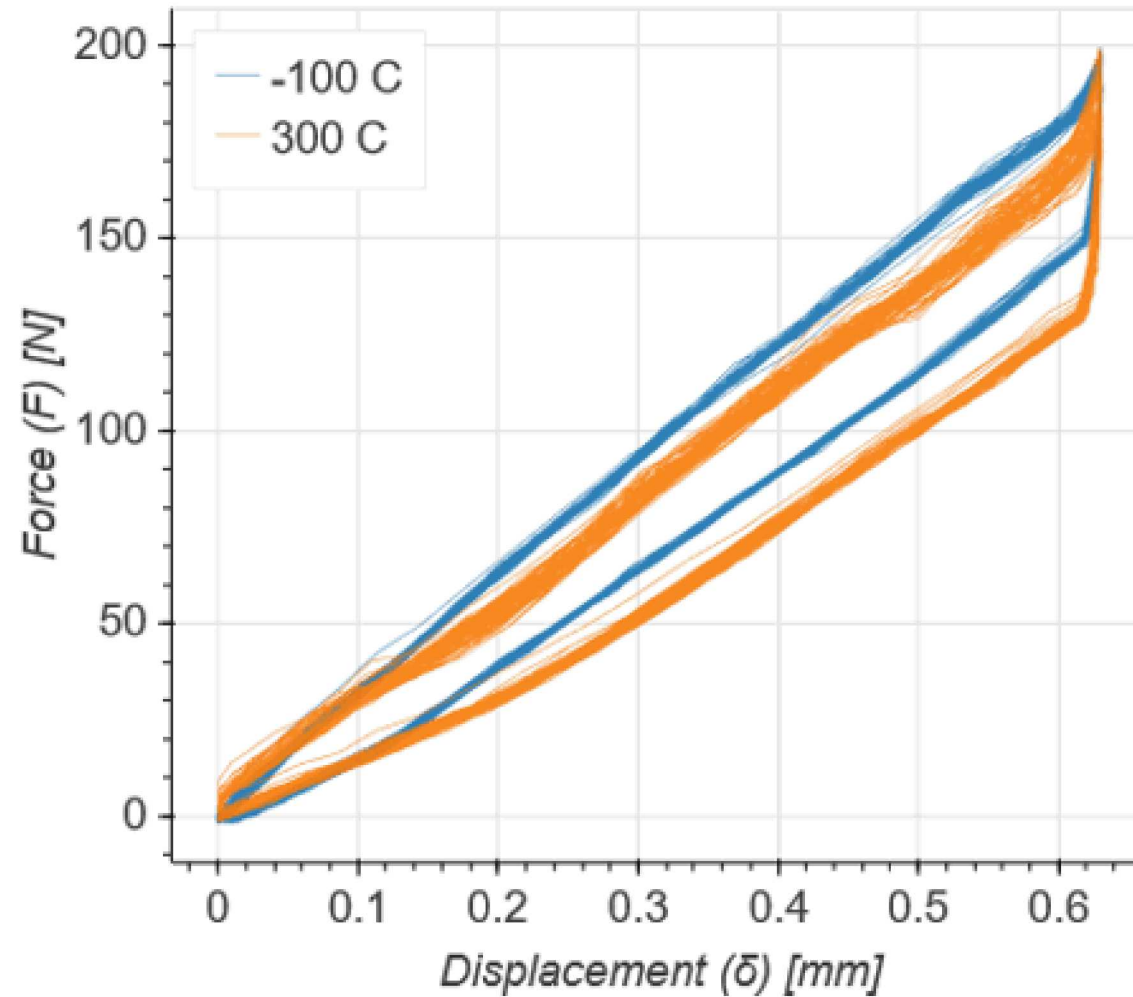


$$W_{FrictionCell} = \frac{EI_{mult}d\delta^2\mu w^3 \cot(\alpha) \csc(\alpha) \sec(\alpha)}{2(I_{mult}a^3 - a^3 + u^3)} + \frac{EI_{mult}d\delta^2w^3 \cot^2(\alpha)}{2(I_{mult}a^3 - a^3 + u^3)} + \frac{Ed\delta^2t^3}{L^3 \sin^2(\theta)}$$

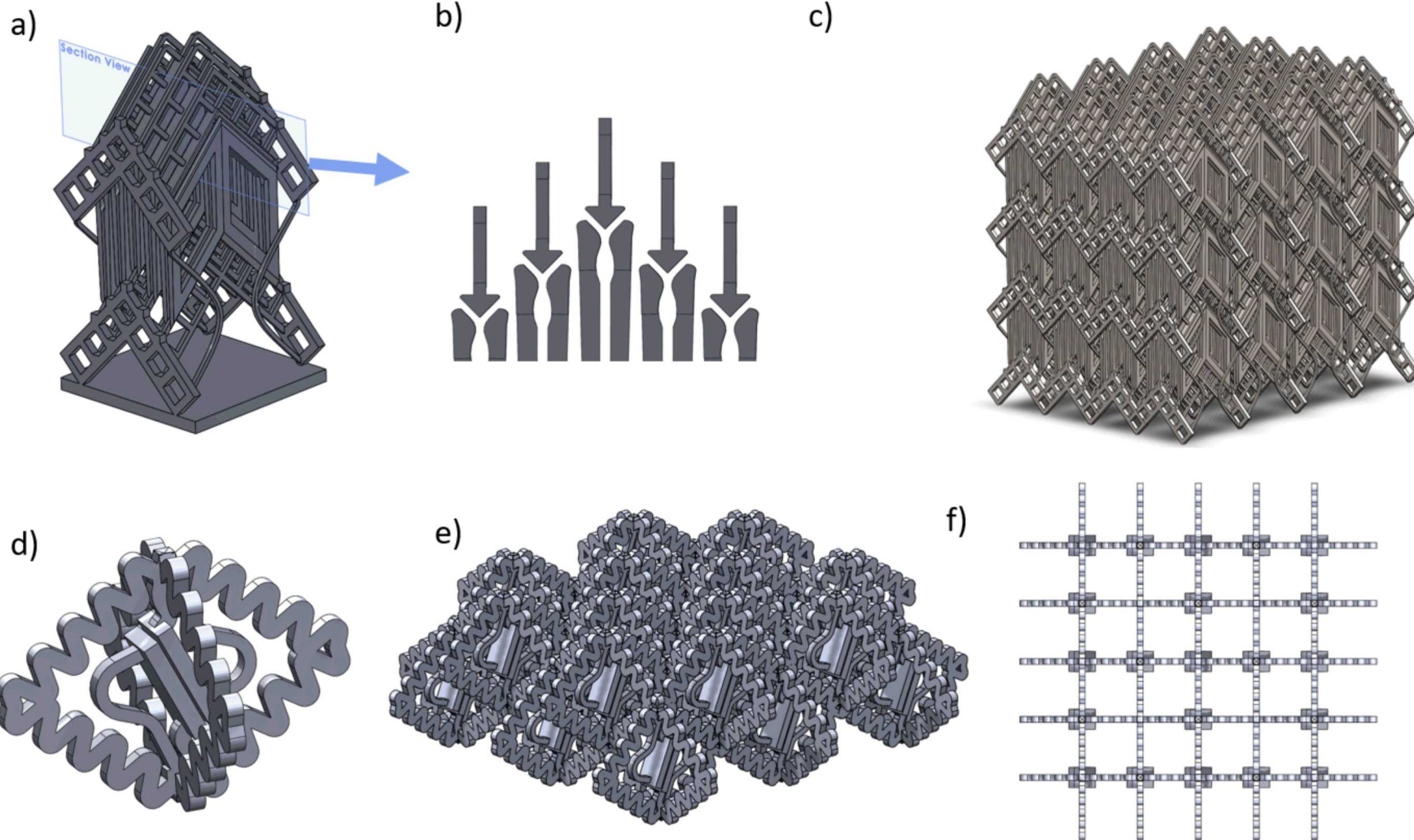
Reusable energy dissipation... like an elastomer



Dissipative properties like an elastomer... but thermally robust...



Complex, hierarchical friction lattices....



You can toughen materials with air, but its all about **the placement!**

All traditional toughening mechanisms: deflection, delamination, transformation, pull-out, etc. are possible, even with a single material!

These mechanisms can be enabled *topologically* in any material, albeit with reduced density.

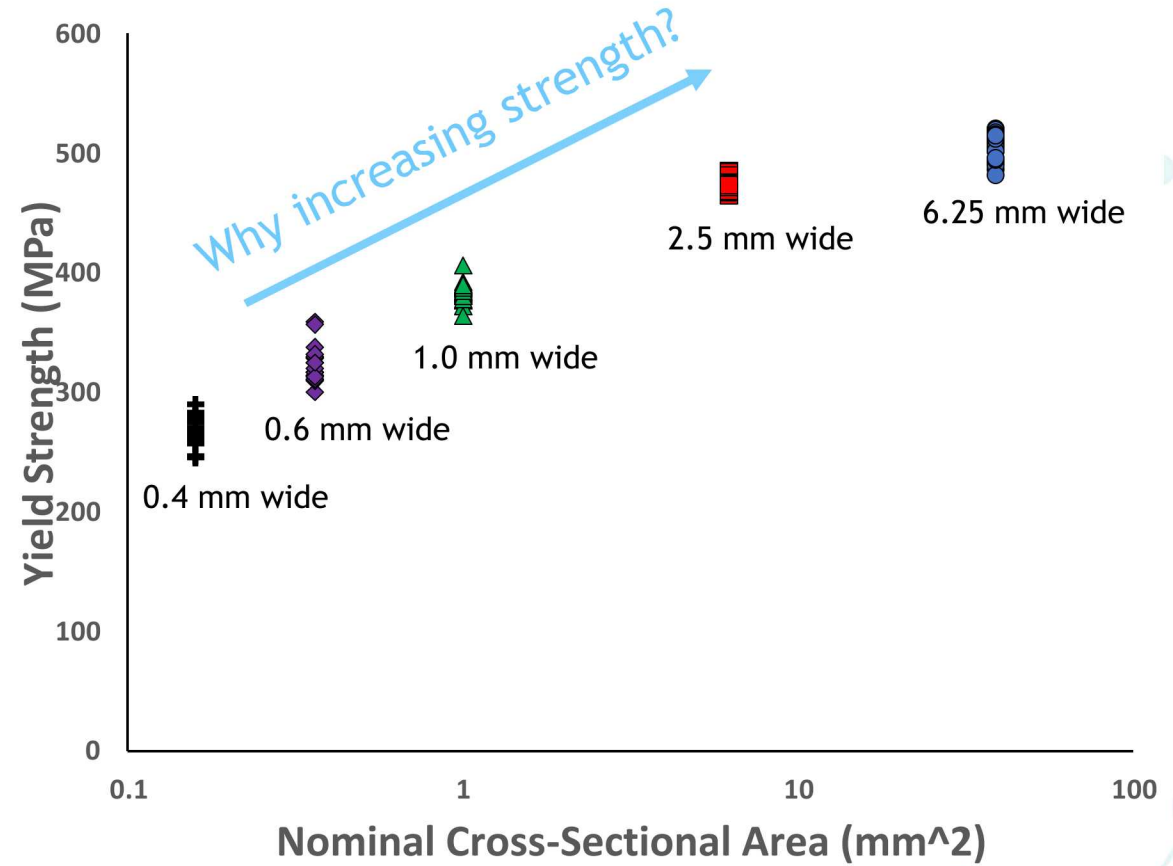
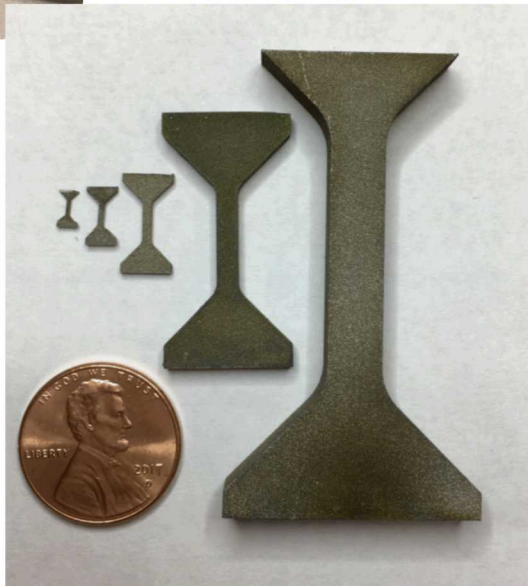
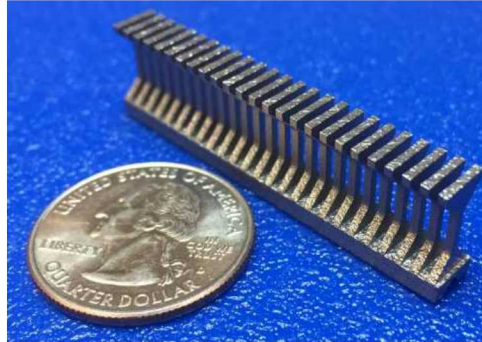
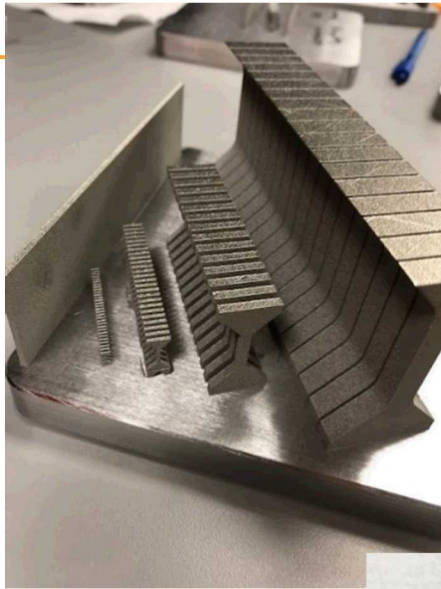
But optimized digital design of fracture resistance is challenging

Setting aside topology... how does it scale?

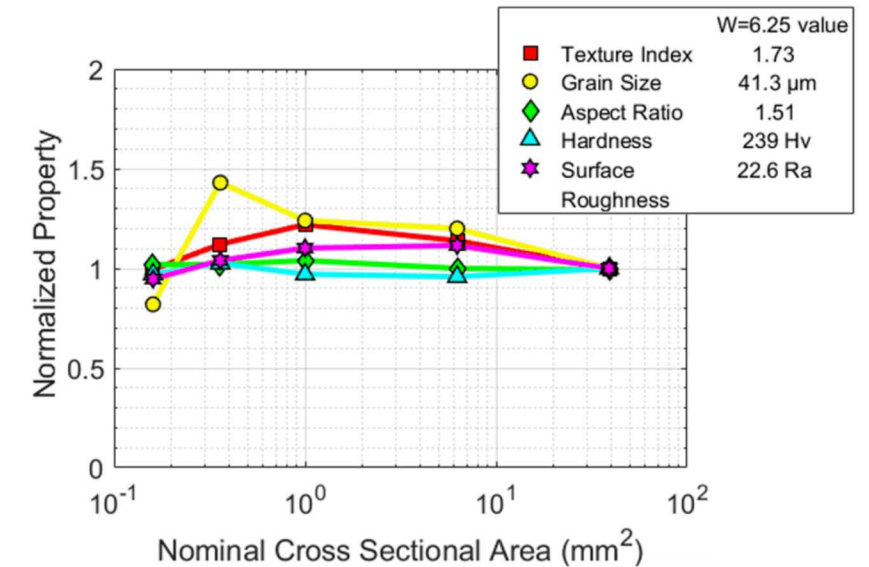
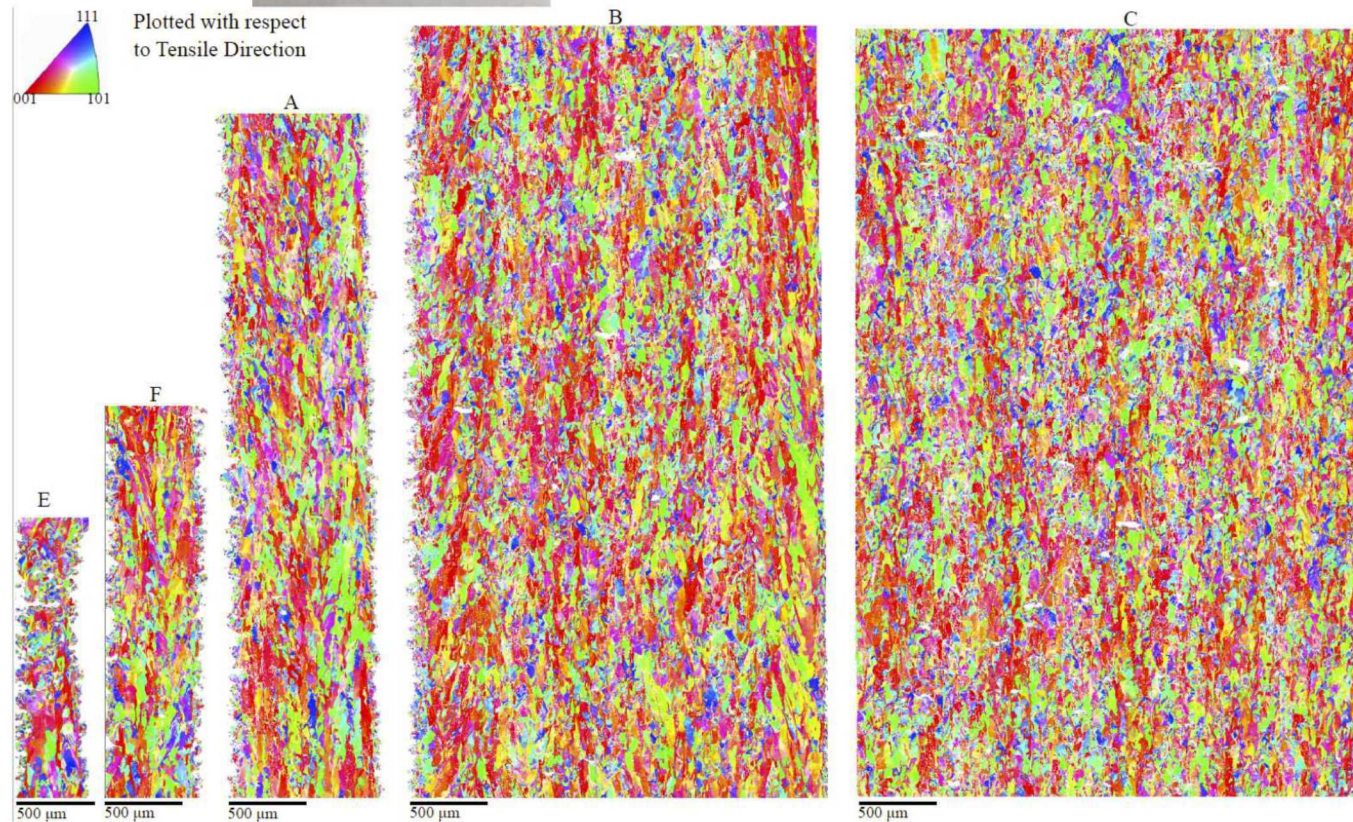
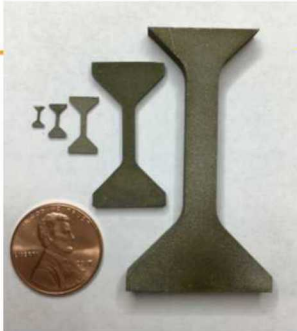


Representative volume consideration???

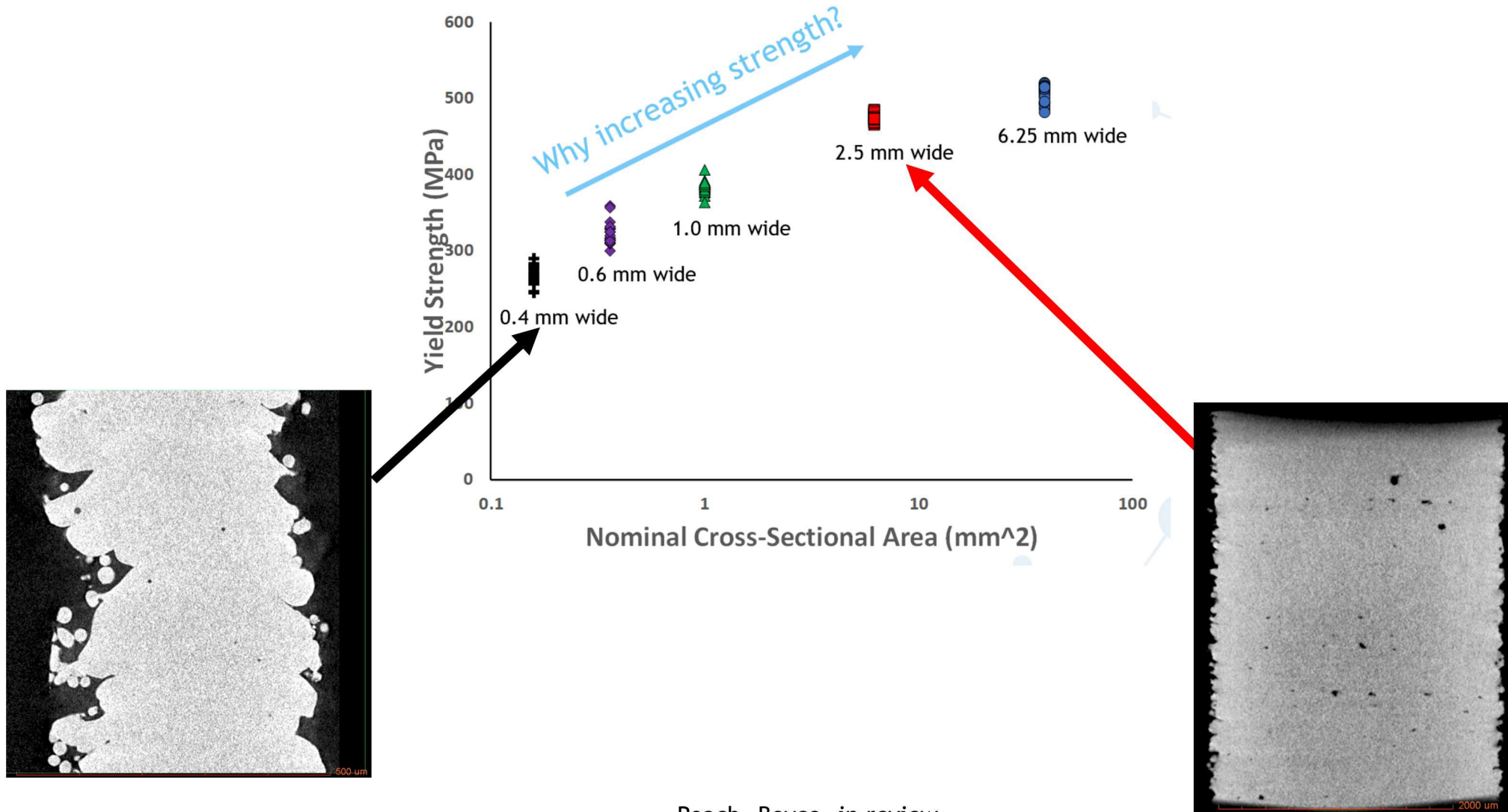
Size dependence of effective mechanical properties...



No microstructural source of size dependent properties...!

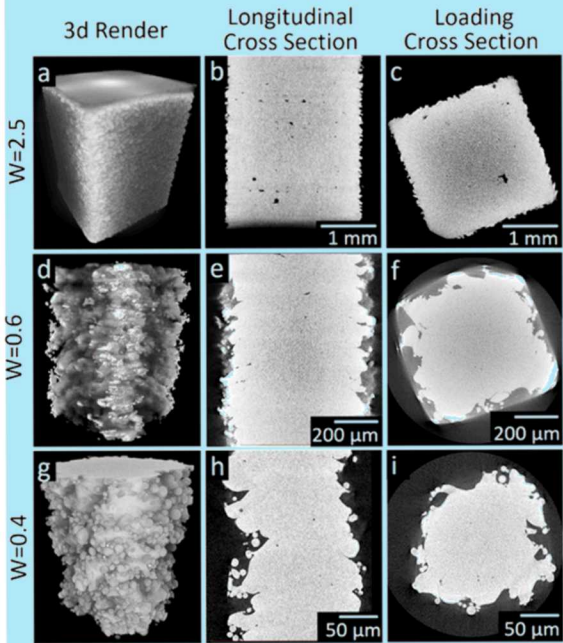


Surface topography dominates when features are <2.5 mm!

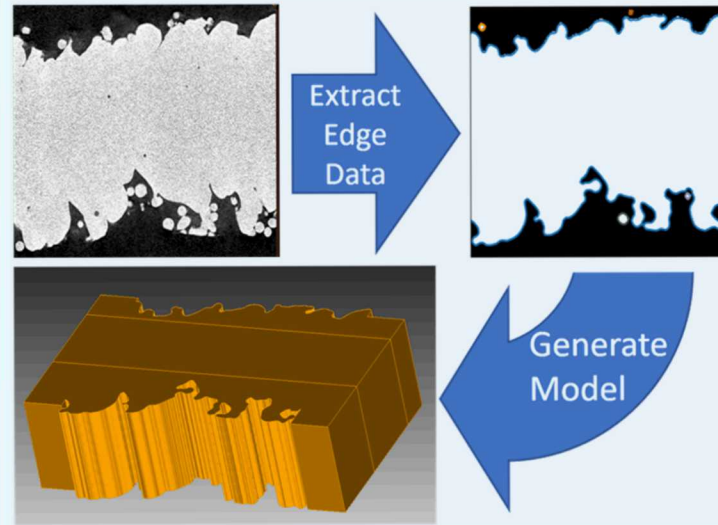


Finite element modeling of roughness effect

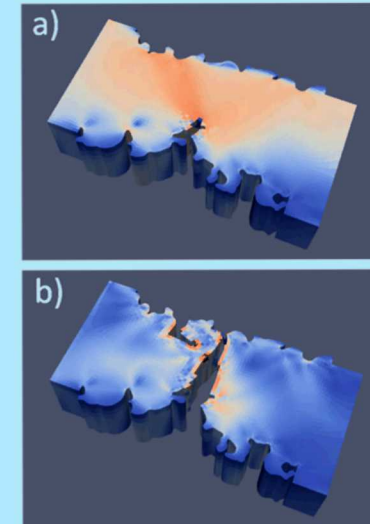
1) Collect CT scans



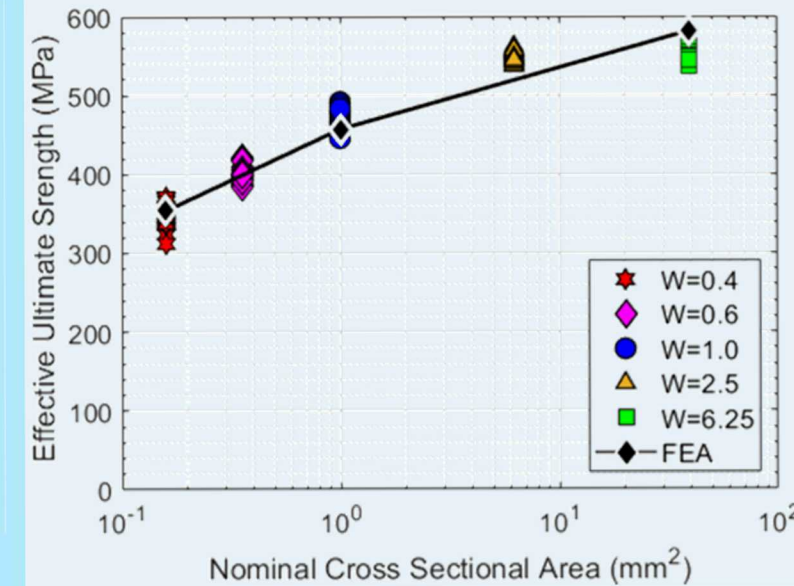
2) Digitize geometry

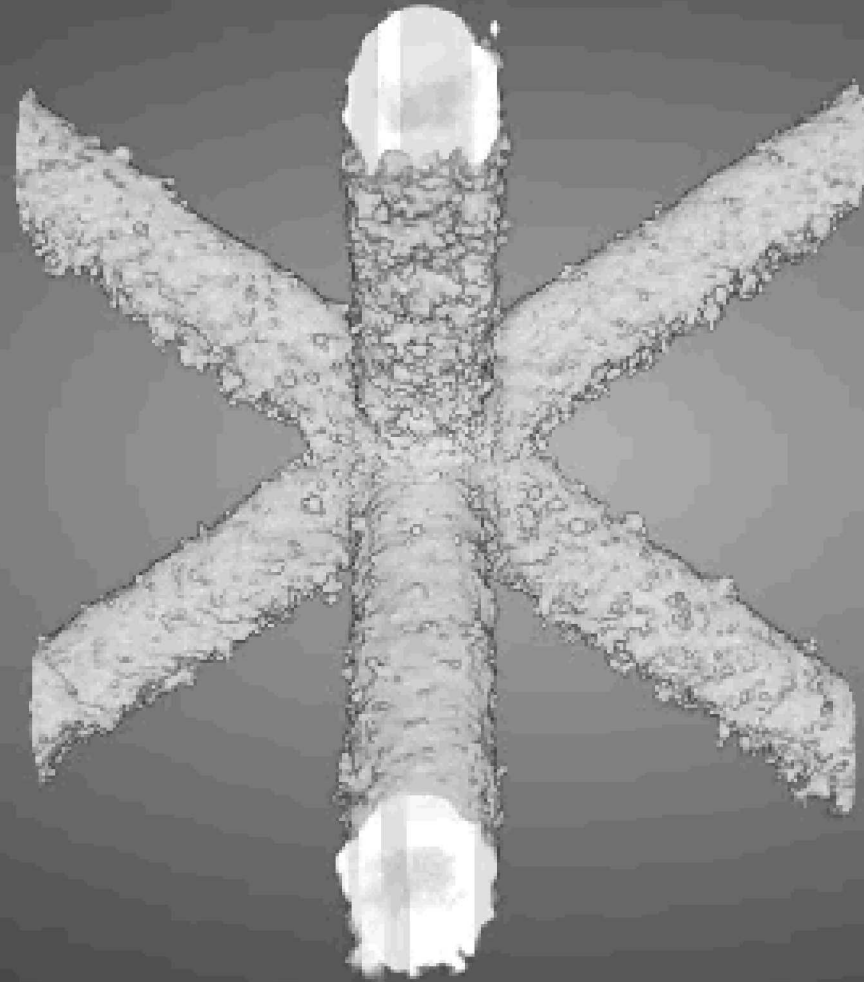


3) FEA

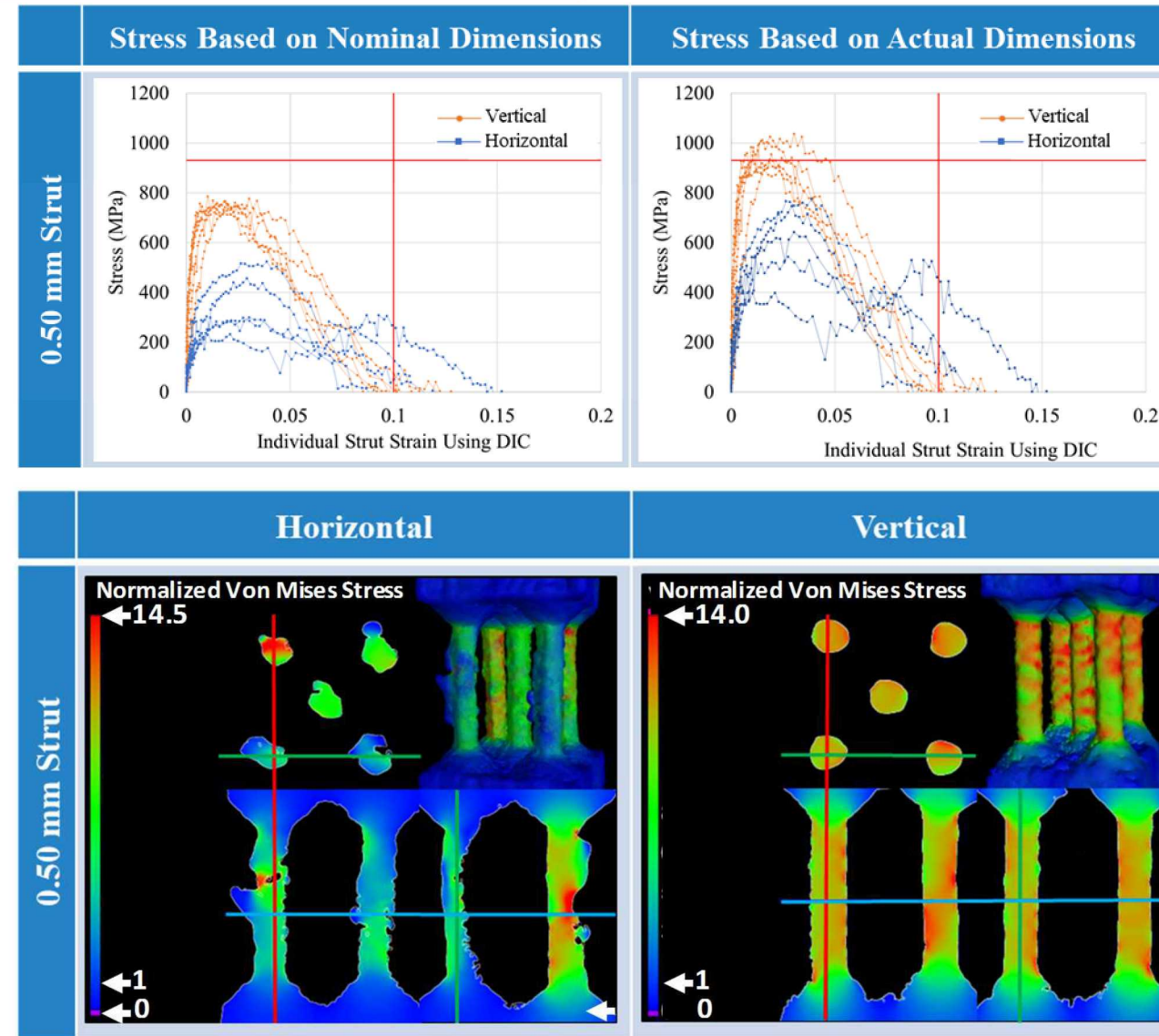
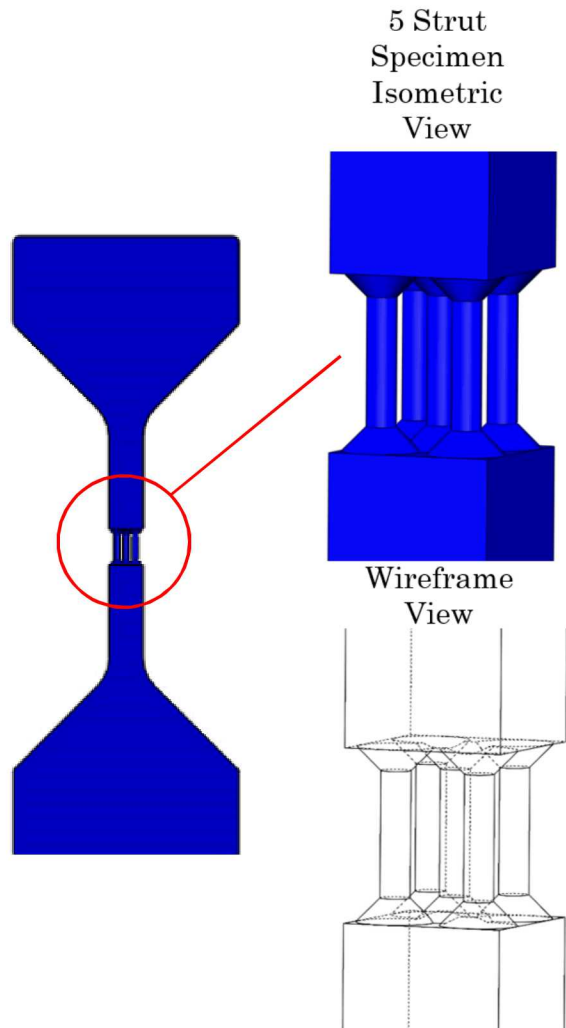


4) Confirm experimental trends



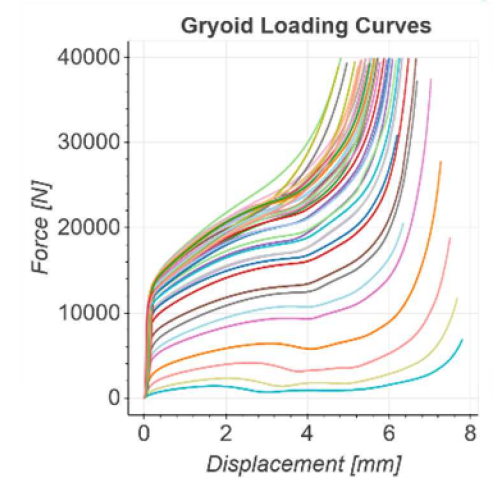
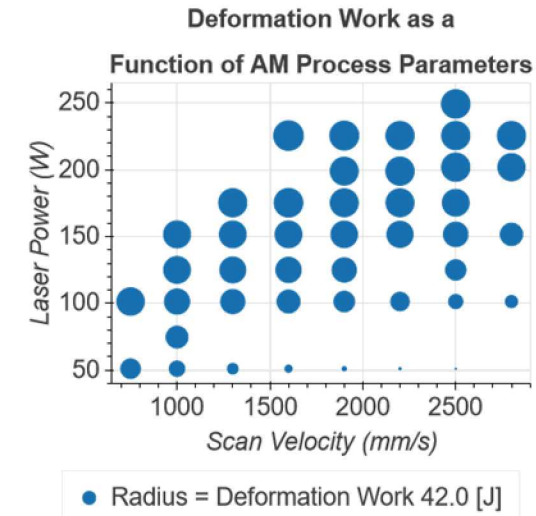
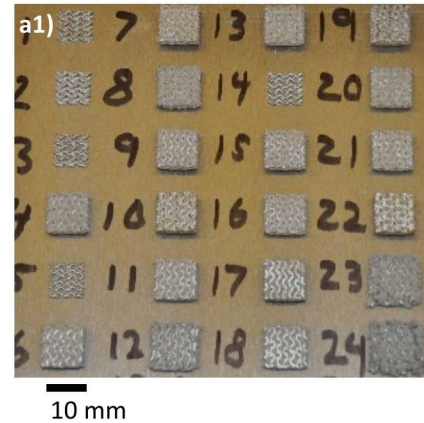
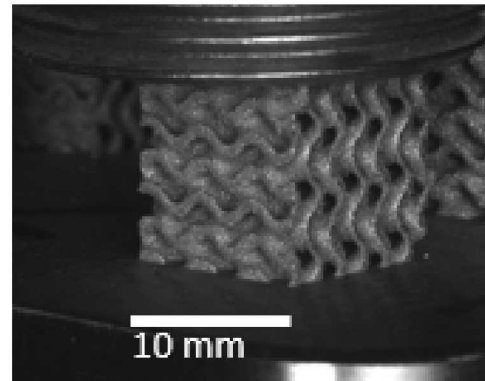


Indeed, the effective strength of struts can be $<50\%$ of the 'material' strength

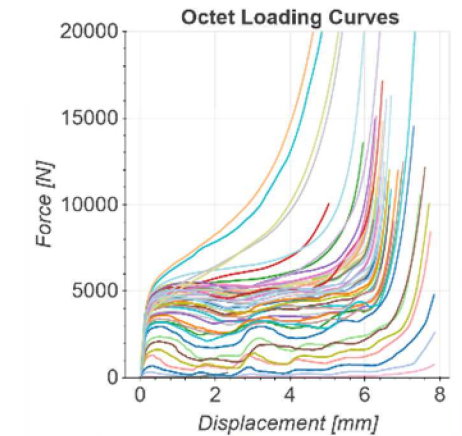
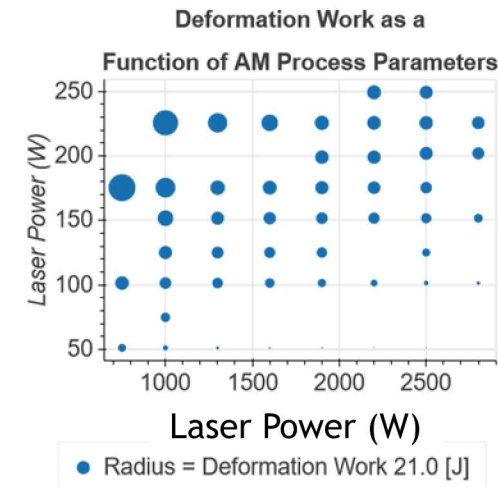
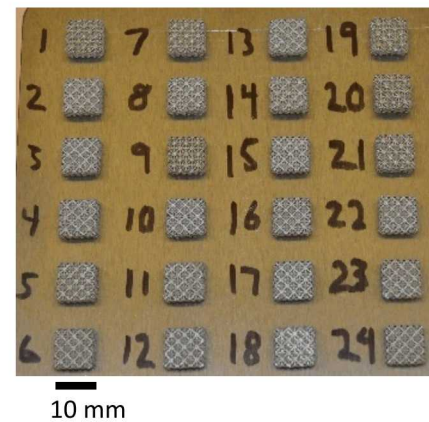
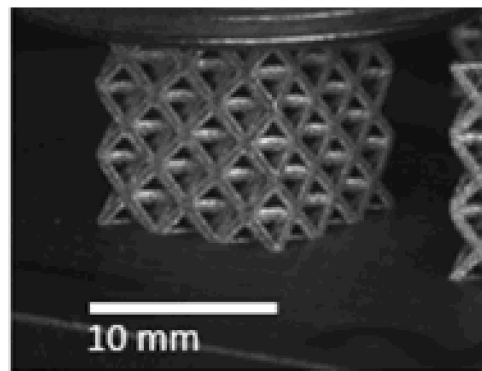


Process parameter study for a lattice...

gyroid

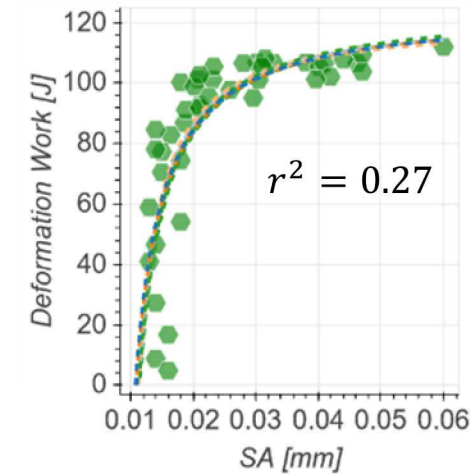
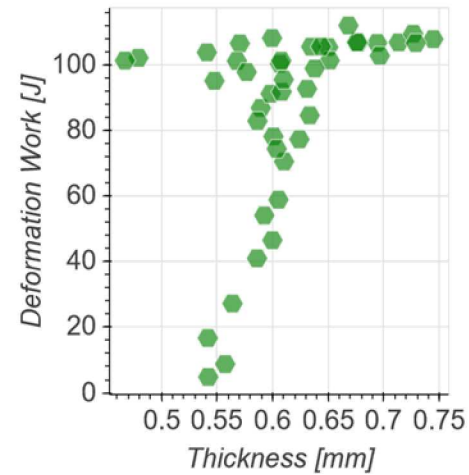
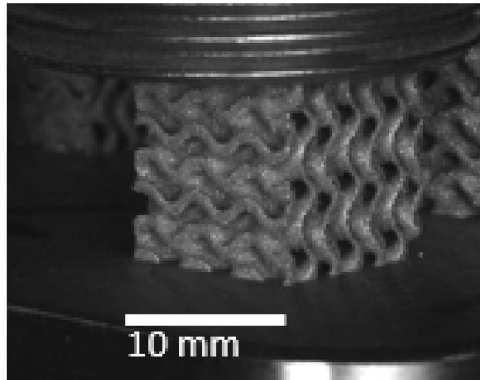


Octet truss

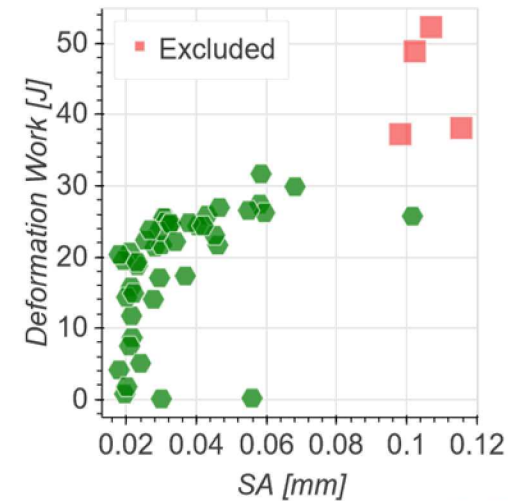
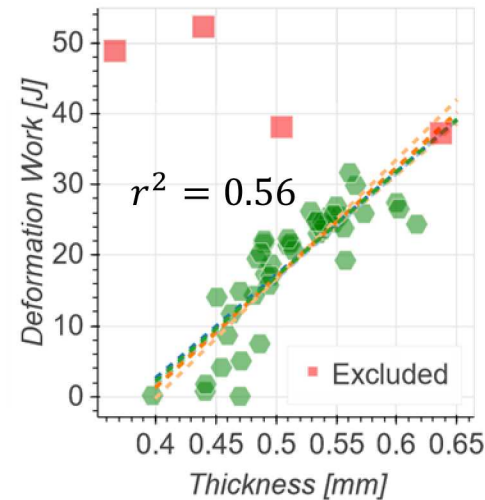
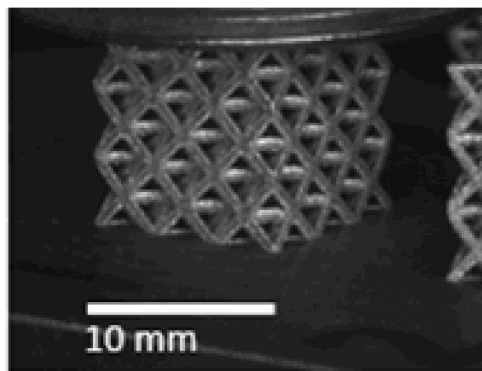


Can we 'predict' mechanical properties with just scalar measures

gyroid

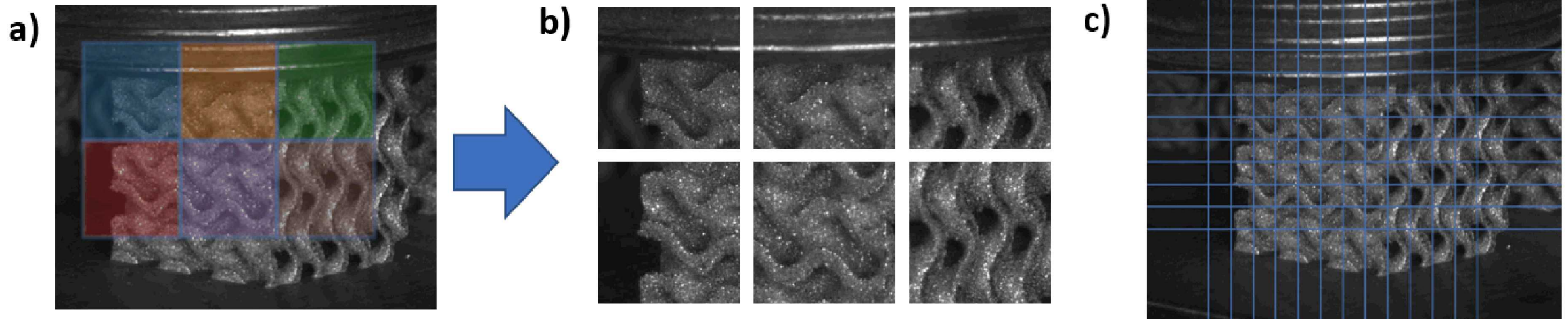


Octet truss



Can machine learning do any better?

Convolutional neural network; 16 layers (resnet16 in fastai library);
stratified k-fold training (8 folds / 11% of data held for testing); enriched data by subwindowing



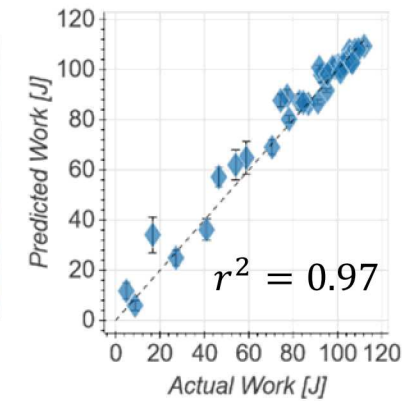
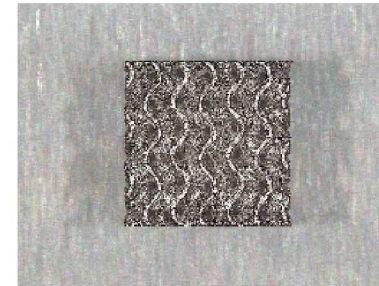
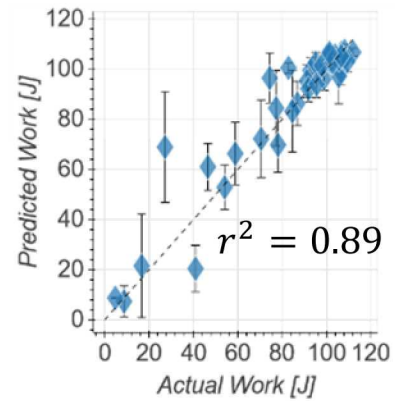
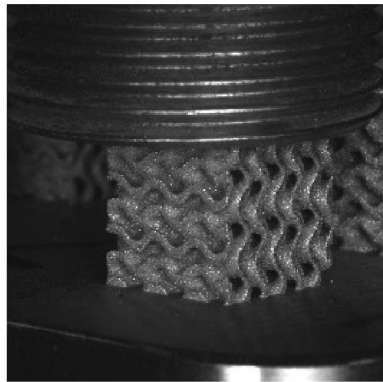
To ‘enrich’ the available data, rather than training on the entire image, we trained on 45 sub-images (windows) of each original image. This takes advantage of the repetitive nature of the lattice.

Can machine learning do any better?

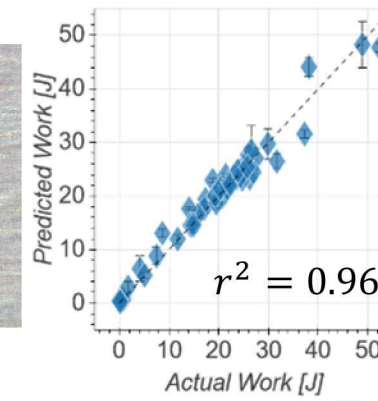
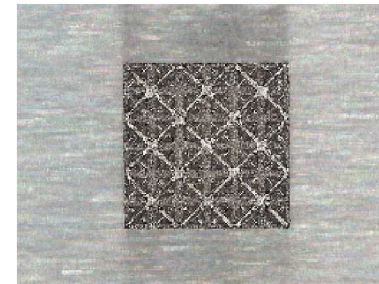
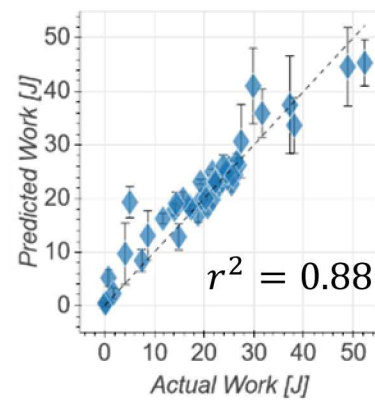
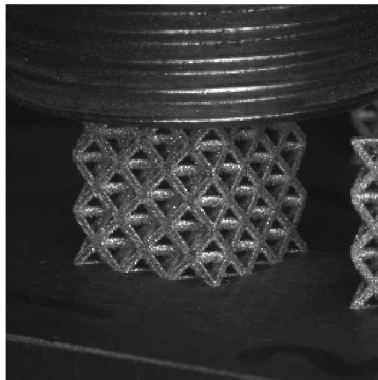
Oblique view

Top-down view

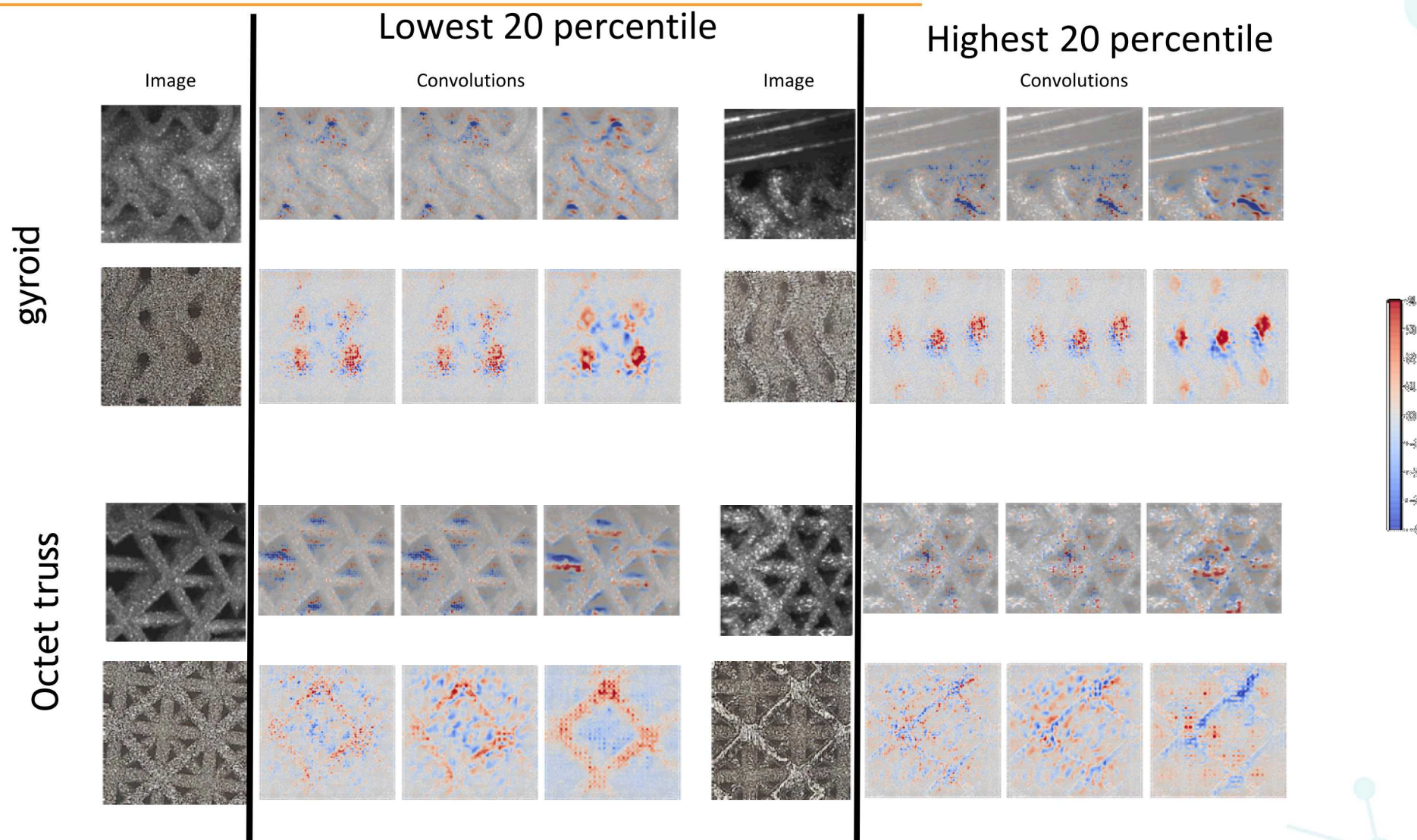
gyroid



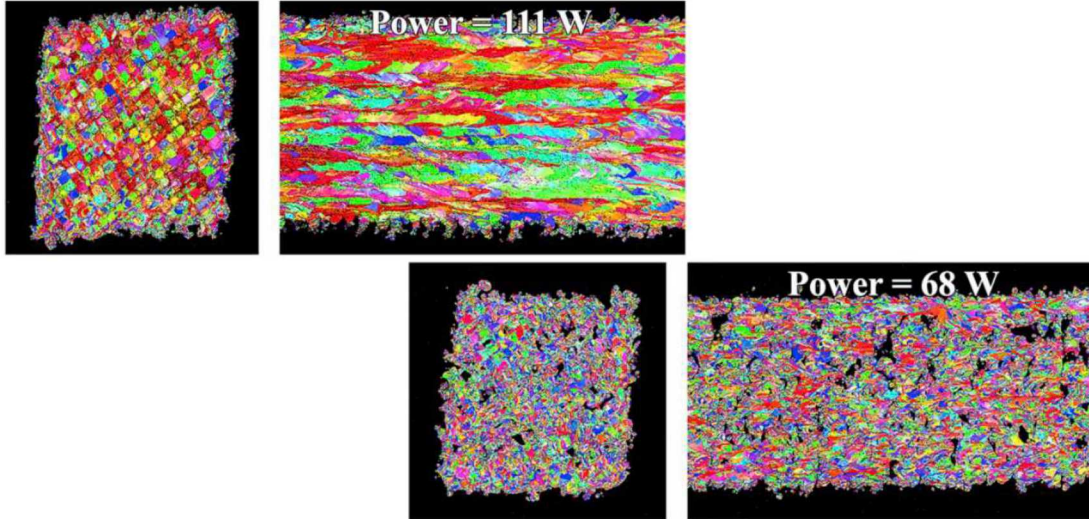
Octet truss



Machine learning's weakness: 'explainability' and extrapolation

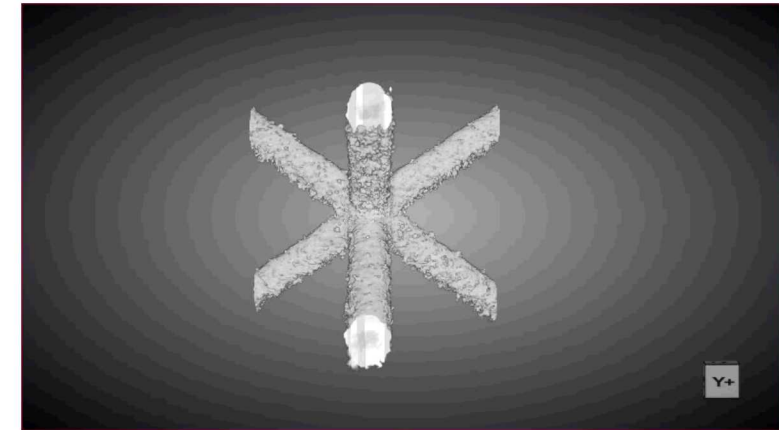


Monolithic AM



First order influence: microstructure & porosity
Complex pathway to prediction

Feature-rich AM



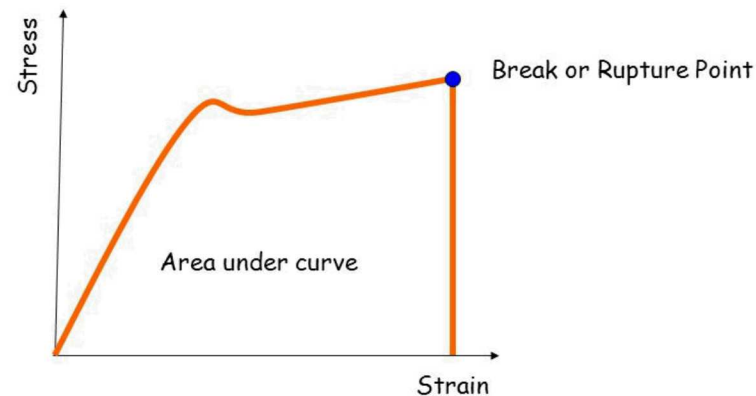
First order influence: dimensions & surface topography
Potentially easier to predict

In this presentation, I drew data from ~2000 mechanical tests. High-throughput testing and machine learning enable us to develop process-structure-property relationships that were otherwise elusive.

Toughness: two basic definitions

Toughness = work of fracture

Units of J or N-m

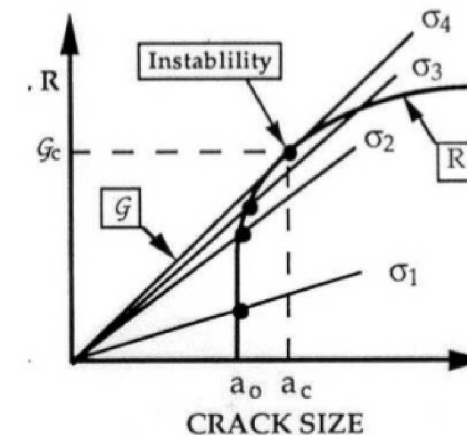


$$W = \int \mathbf{F} \cdot d\mathbf{x}$$

$$U = \int \boldsymbol{\sigma} : d\boldsymbol{\epsilon} V$$

Fracture toughness= work required advance a crack by a unit length

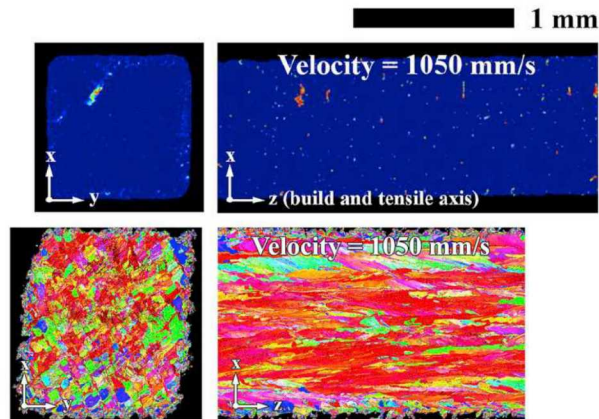
Units of MPa $\sqrt{\text{m}}$ (K) or J/m² (G)



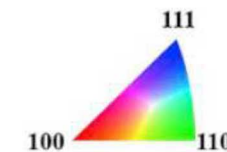
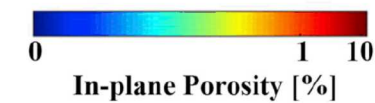
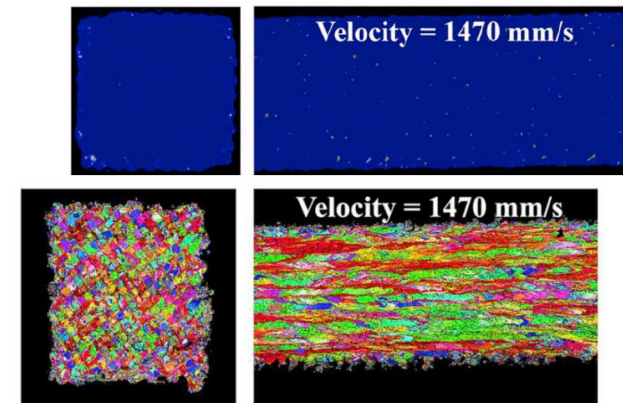
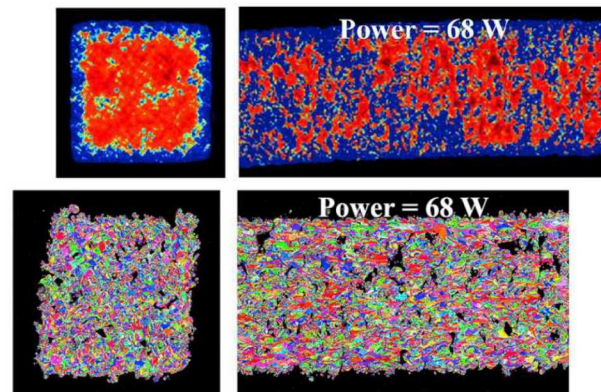
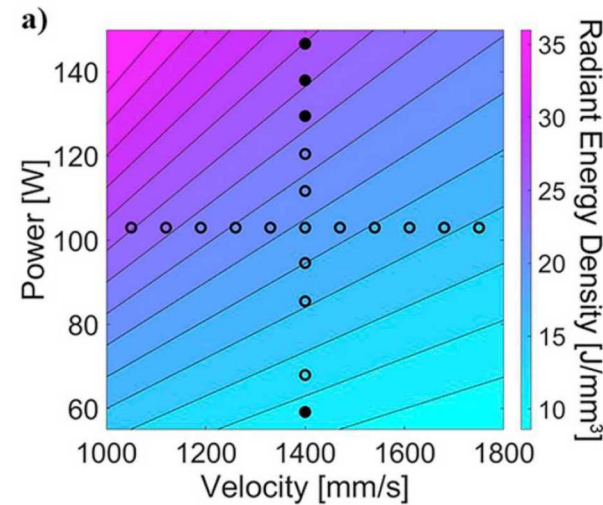
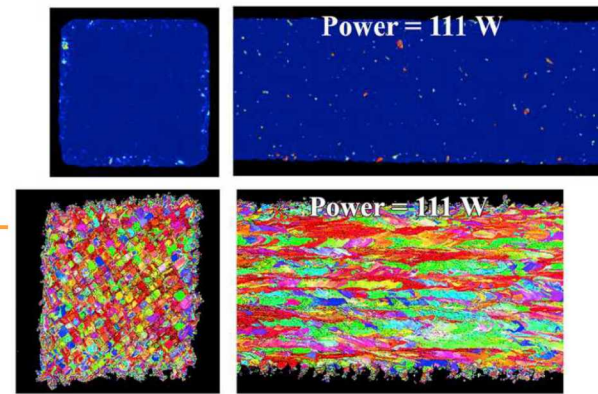
$$G = G_I = \begin{cases} \frac{K_I^2}{E} & \text{plane stress} \\ \frac{(1 - \nu^2)K_I^2}{E} & \text{plane strain} \end{cases}$$

Process parameter study

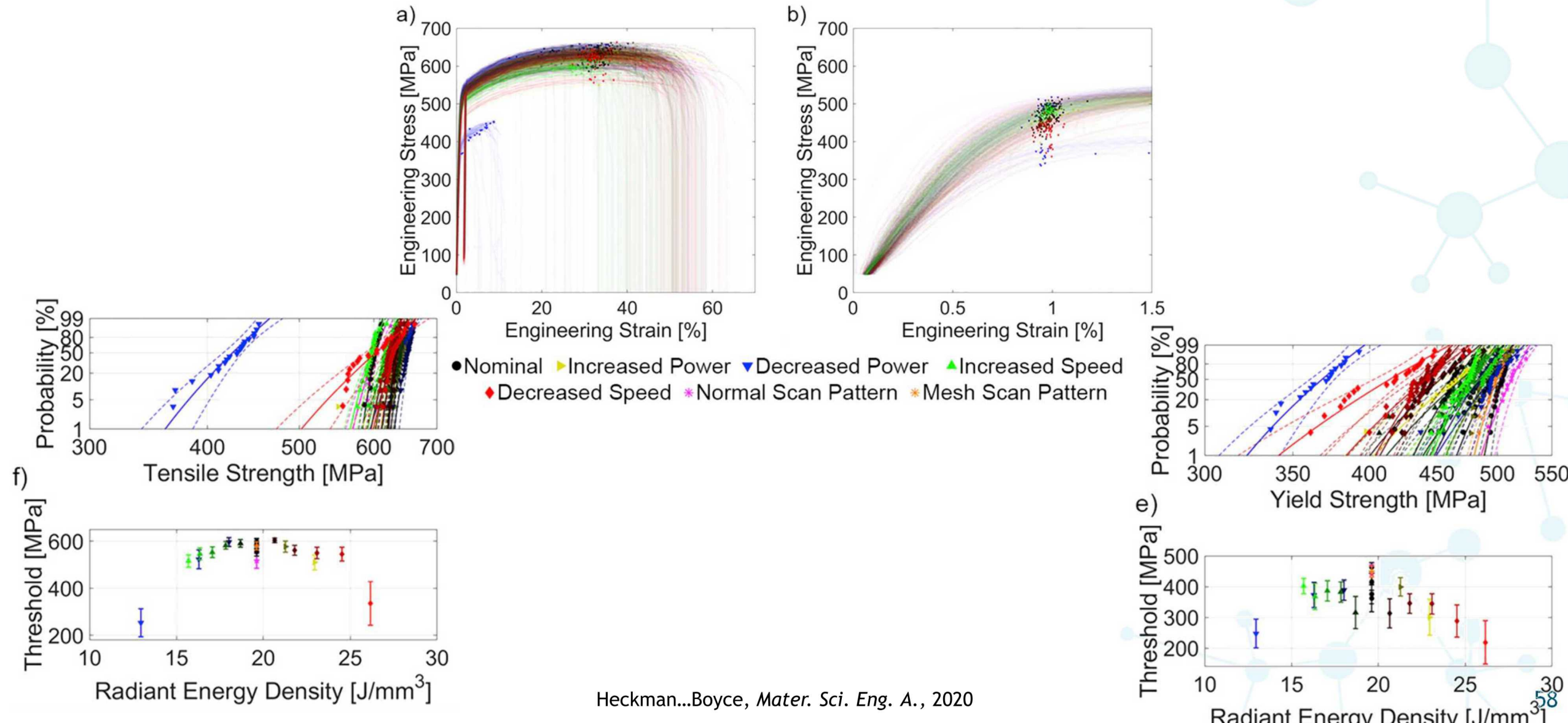
X-ray computed tomography



High-speed electron backscatter diffraction

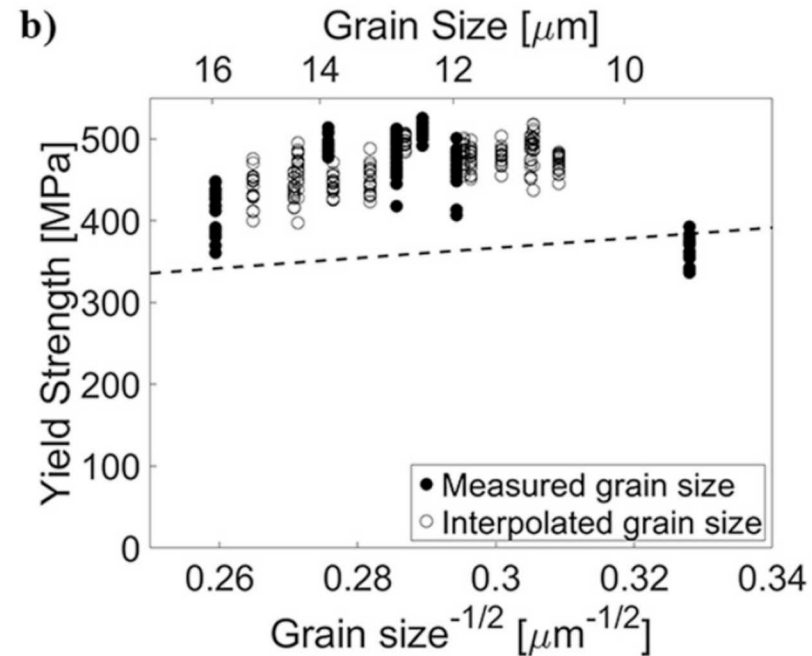
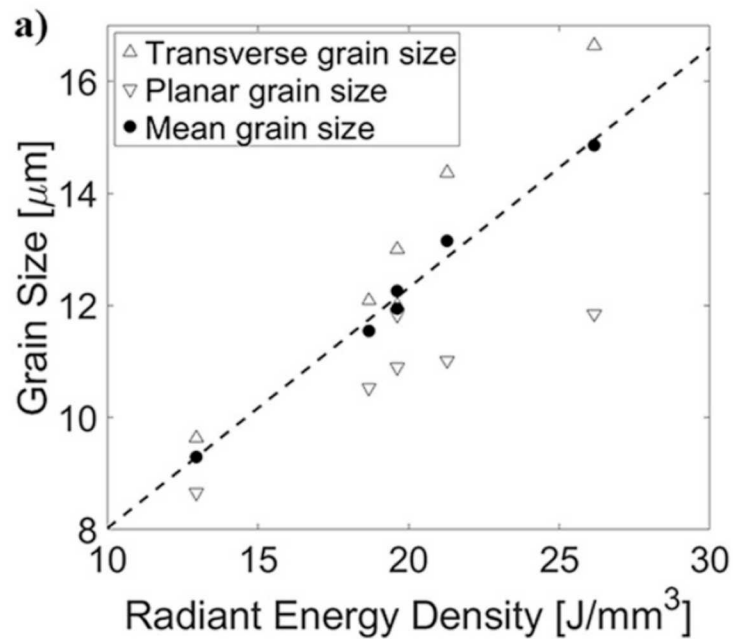
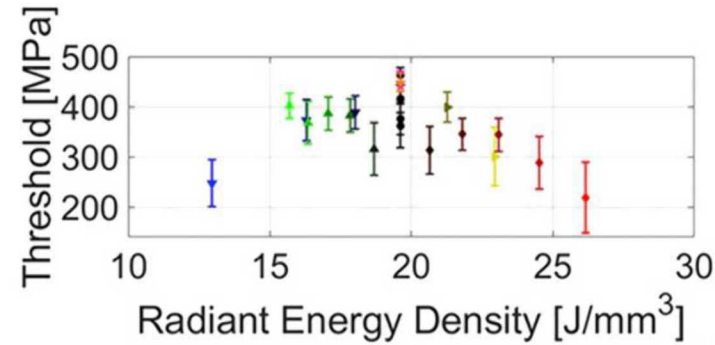


High-throughput data → a Weibull minimum allowable threshold

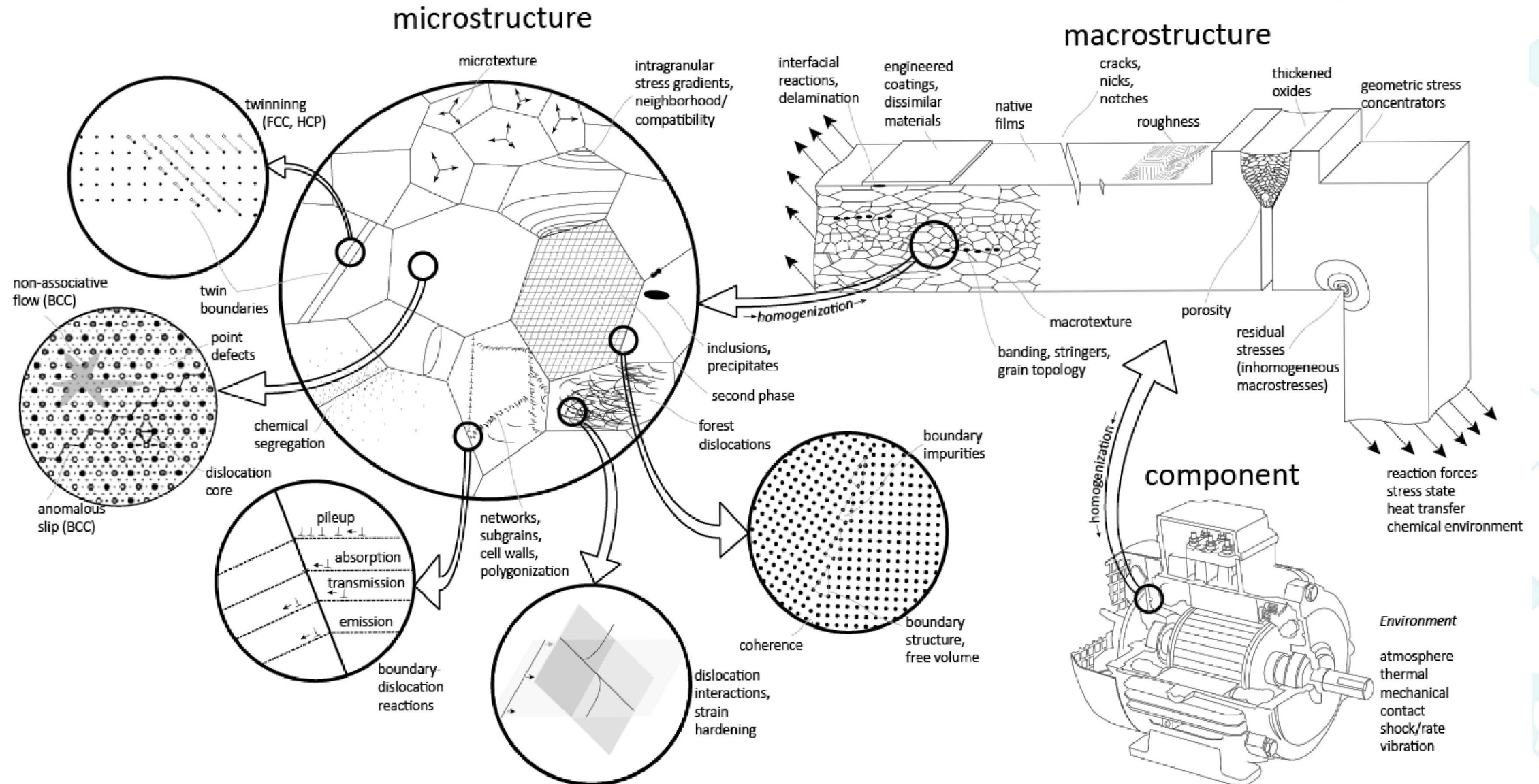


Connecting the dots... the old fashioned way...

Weibull threshold
Yield Strength (MPa)



Grain size is not the only factor affecting mechanical response...



Griffith fracture criterion (1921)²

Criterion: Crack growth will occur if the potential energy decrease produced by an increment of crack extension equals the energy needed to extend the crack that same increment.

$$\sigma = \sigma_f, \text{ if } \frac{\partial \Pi}{\partial a} = \frac{\partial W}{\partial a}$$

For the elliptical crack

$$\frac{\partial \Pi}{\partial a} = \frac{\pi a^2 \sigma_0^2}{E^*}, \quad E^* = \begin{cases} E, & \text{if plane stress} \\ \frac{E}{1-\nu^2}, & \text{if plane strain} \end{cases}$$
