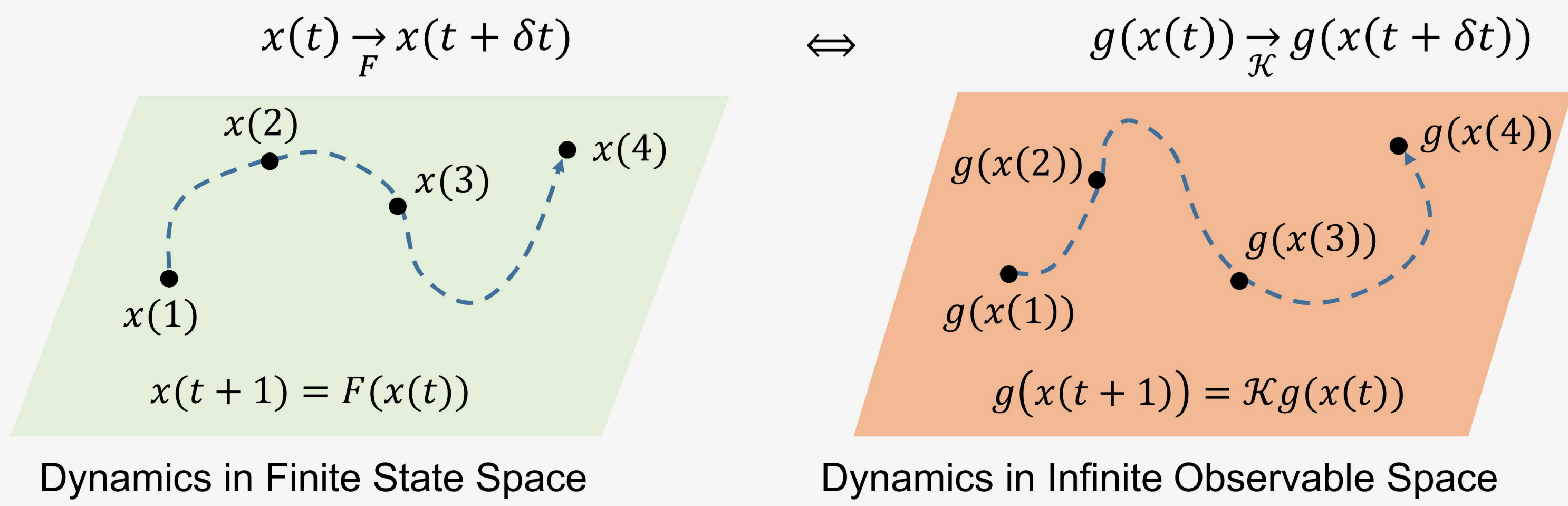


## Introduction

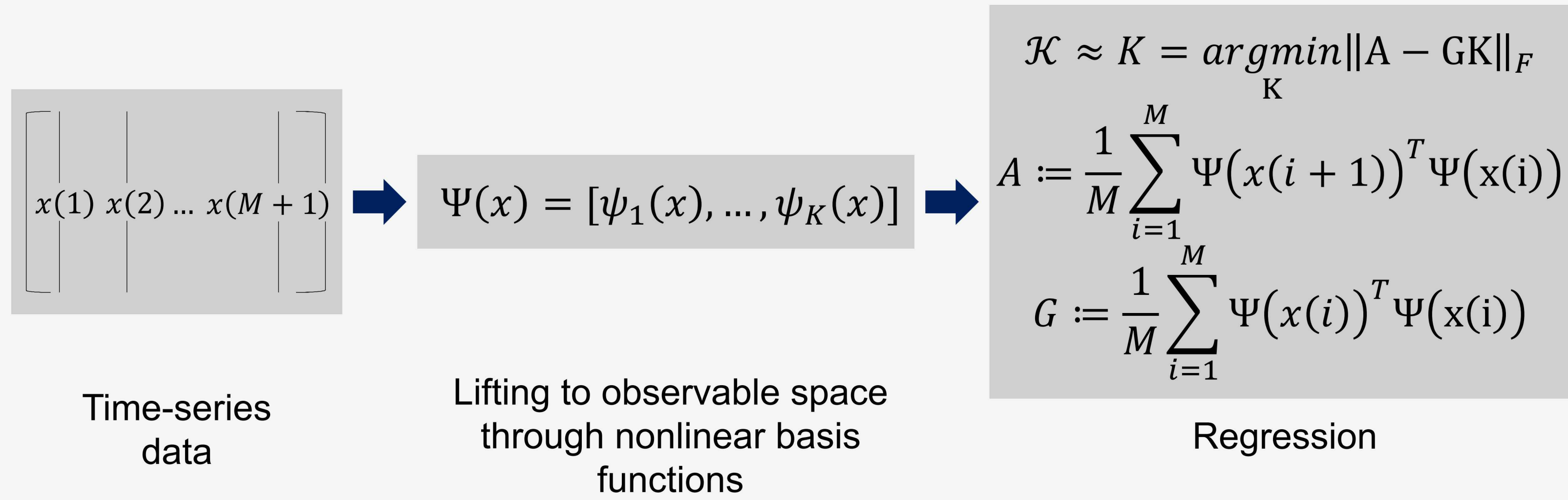
- Classical approaches for incident detection rely on some **knowledge of the system topology**, such as in graph-based techniques and methods based on traveling waves.
- With the introduction of PMUs, **data-driven techniques** started receiving more attention, as in the case with SVD-based approaches [1].
- Our proposed approach draws on Koopman operator theory, which accounts for the **causal relationship** among multiple sensor data streams **without prior knowledge of the dynamic model**.

## Koopman Operator Theory

- The Koopman operator  $\mathcal{K}$  is a linear operator for the dynamics of  $x(t)$  in the observable space.



- The Koopman operator is infinite-dimensional, making computation impractical.
- Extended Dynamic Mode Decomposition (EDMD) overcomes this issue by providing a finite-dimensional approximation of Koopman operator.
- EDMD uses time-series data and hence it is suitable for data-driven frameworks.
- Incident detection method is formulated as a sparsity-promoting variant of EDMD.

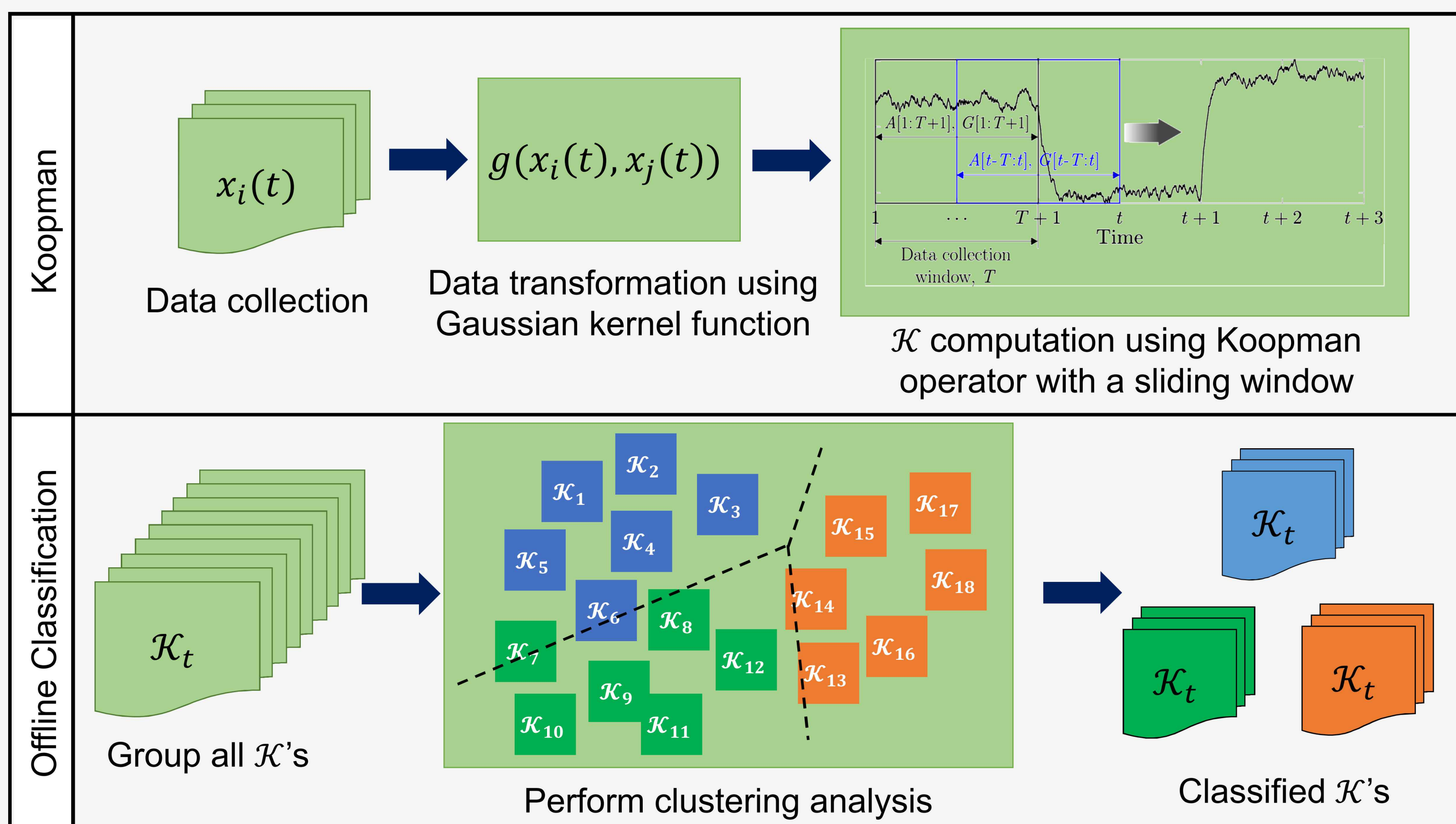


## Methodology for Incident Detection

- We hypothesize that the relationship between different time-series data carries more information than individual data streams.
- Instead of using raw data for the incident detection via Koopman operators, we augment the data with the use of the Gaussian kernel function.

$$g(x_i, x_j) = \exp\left(-\frac{\|x_i - x_j\|^2}{2\sigma}\right)$$

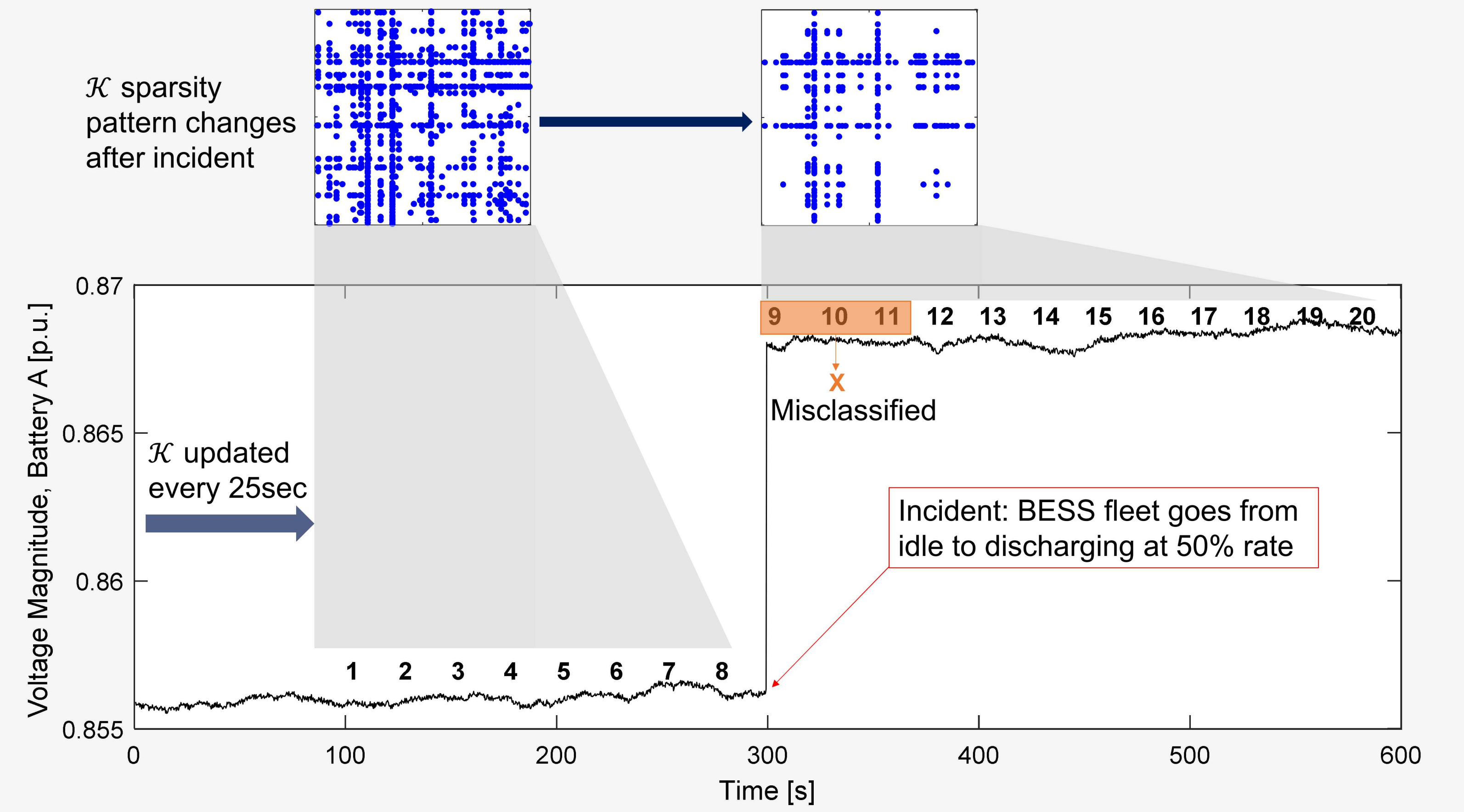
- This nonlinear transformation lifts the data into a higher dimensional space by giving a measure of similarity between states  $x_i$ .
- The transformed data is used to compute a sequence of  $\mathcal{K}$  matrices through a sliding window, and significant changes in  $\mathcal{K}$  indicates altered causality in states (i.e., occurrence of incidents).



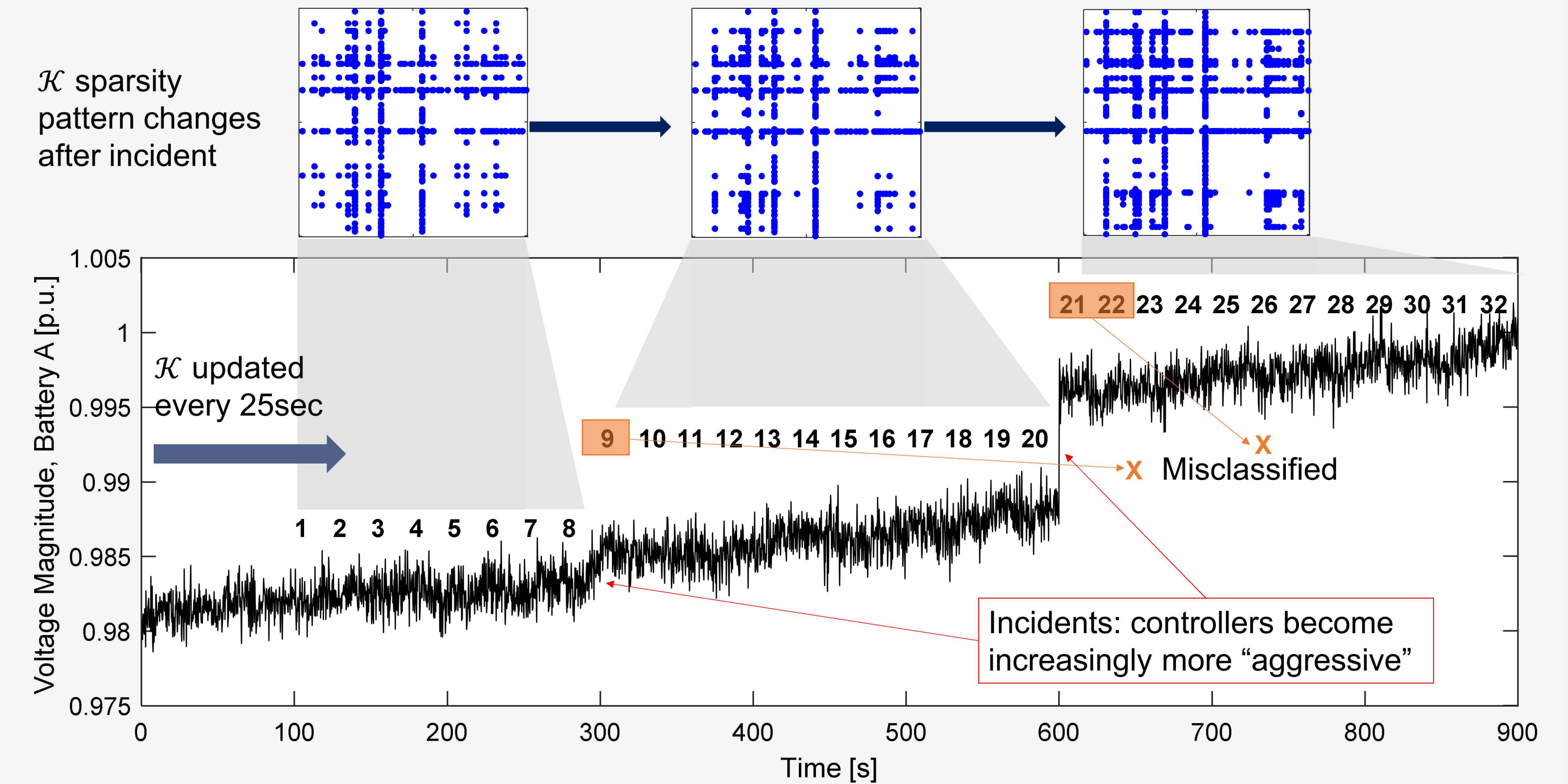
## Case Studies

- We considered the IEEE 8500-node Test feeder unbalanced radial network with 7 grid battery energy storage systems (BESS) added.
- BESS can perform Volt/VAR control and take real power dispatch commands.
- The data was generated in OpenDSS, assuming voltage magnitude and phase measurements from PMUs were available at the nodes of 3 of these BESS.
- Gaussian noise was added to the voltage magnitude ( $\pm 0.01\%$ ) and voltage angle ( $\pm 0.01^\circ$ ) measurements.
- Fluctuations in load real and reactive power were considered in the feeder model.
- Changes in the sparsity pattern of the  $\mathcal{K}$  matrices indicated the occurrence of an incident.
- To confirm the  $\mathcal{K}$  matrices had unique sparsity patterns for each scenario in which the causality of the model was maintained, an offline analysis was performed using k-means clustering to classify these matrices.
- Typical results showed misclassifications immediately after incidents occurred, while remaining  $\mathcal{K}$ 's were correctly classified.

### 1) Detecting changes in battery discharge rate



### 2) Detecting changes in battery controller parameters



## Conclusion

- In a distribution network with energy storage systems and advanced controls, traditional monitoring and protection schemes are not well suited for detecting anomalies such as malfunction of controllable devices.
- We propose a data-driven method that requires no prior knowledge of the network dynamic model for the detection of these anomalies.
- The algorithm proposed is robust to load variations and noise measurements.

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## References

- [1] J. M. Lim and C. L. DeMarco, "Svd-based voltage stability assessment from phasor measurement unit data," IEEE Transactions on Power Systems, vol. 31, no. 4, pp. 2557–2565, 2016.