

# Relative permeabilities for two-phase flow through wellbore cement fractures

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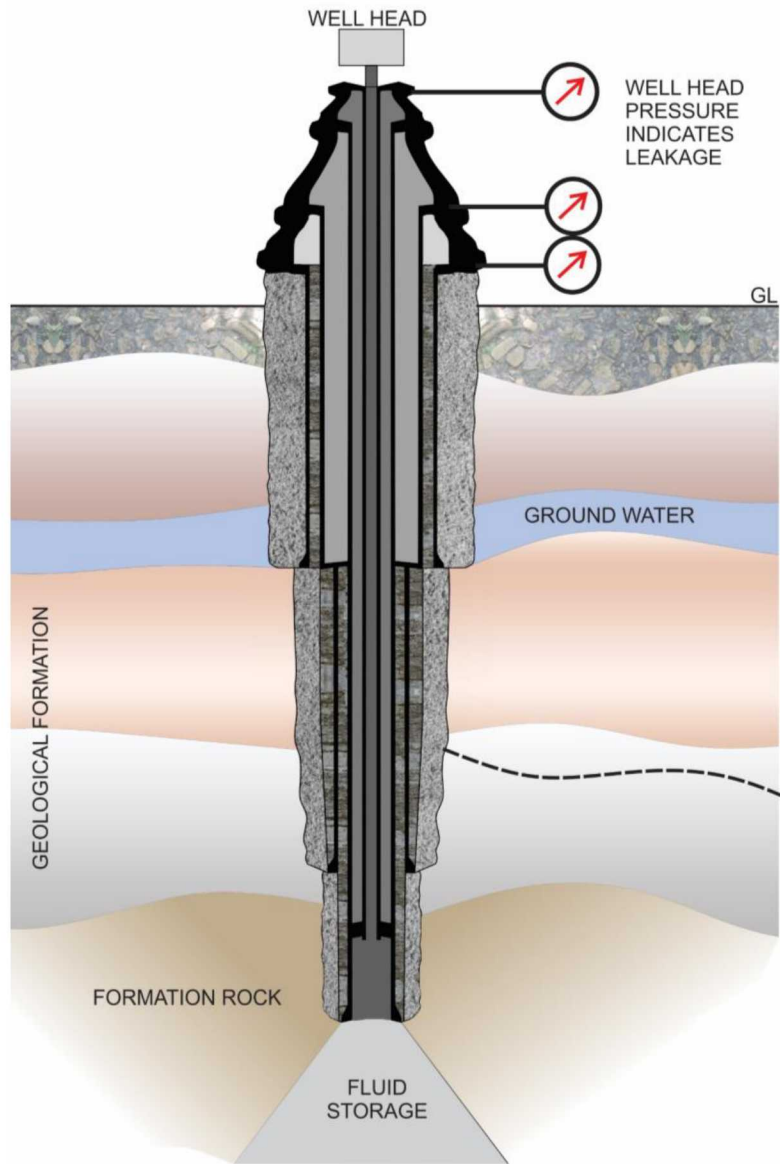
**Presented by Ishtiaque Anwar**

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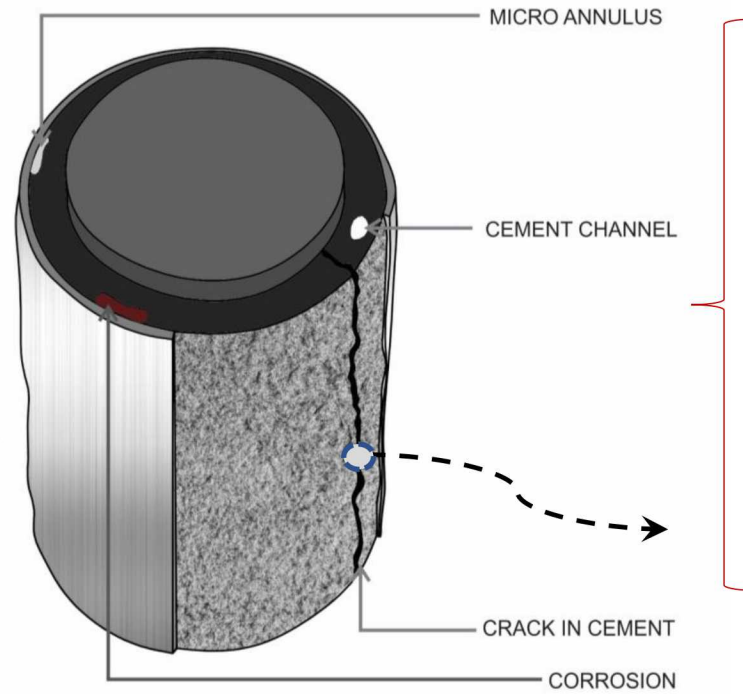
# Relative permeabilities for two-phase flow through wellbore cement fractures

Objective: to obtain gas-oil relative permeabilities from simultaneous gas-oil flow tests on fractured cement specimens.

***Leakage rates through wellbore flaws are affected by the presence of multiple fluids in fracture.***



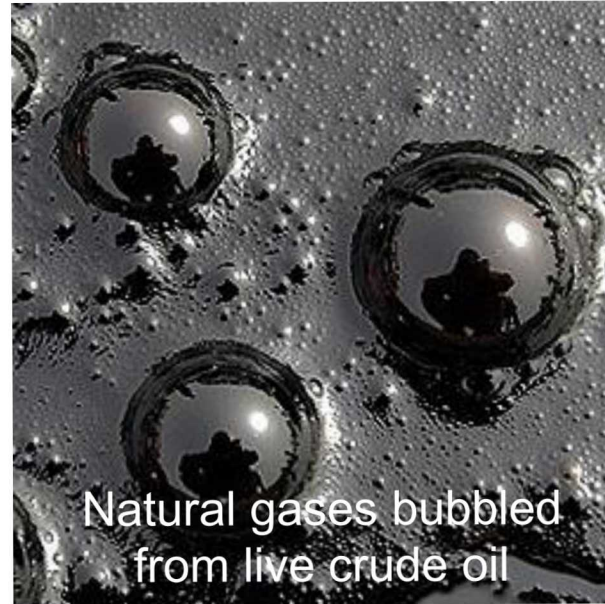
Upward leakage of fluid, through wellbore flaws.



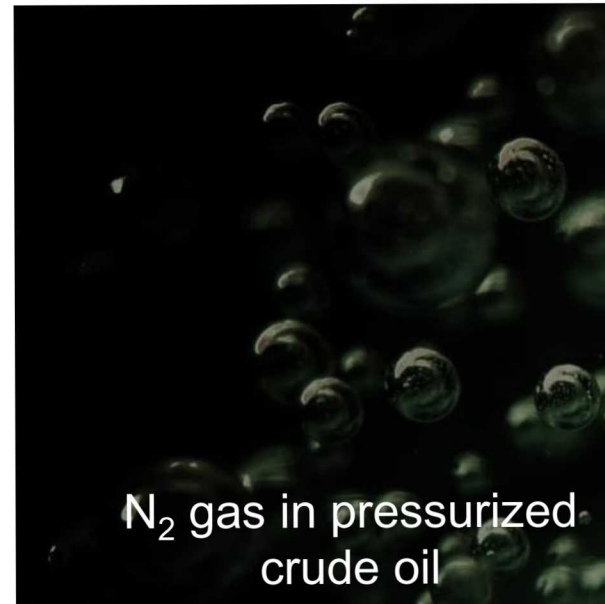




Source: Geomechanics Lab, UNM



Source: neftegaz.ru/en/news/oil/



Source: Geomechanics Lab, UNM



Source: depositphotos.com/178436602/

Multiple fluids are likely to exist in wellbore flows depending on the facility the wellbore is associated with.

# Materials and methods

## Specimen preparation



Tensile splitting (Brazilian test) equipment. Cylindrical cement sample is in load frame on left, control system is on right.

Prepared in accordance with ASTM C305-14



Curing of various cement cylinders in water tank



Sample after tensile splitting

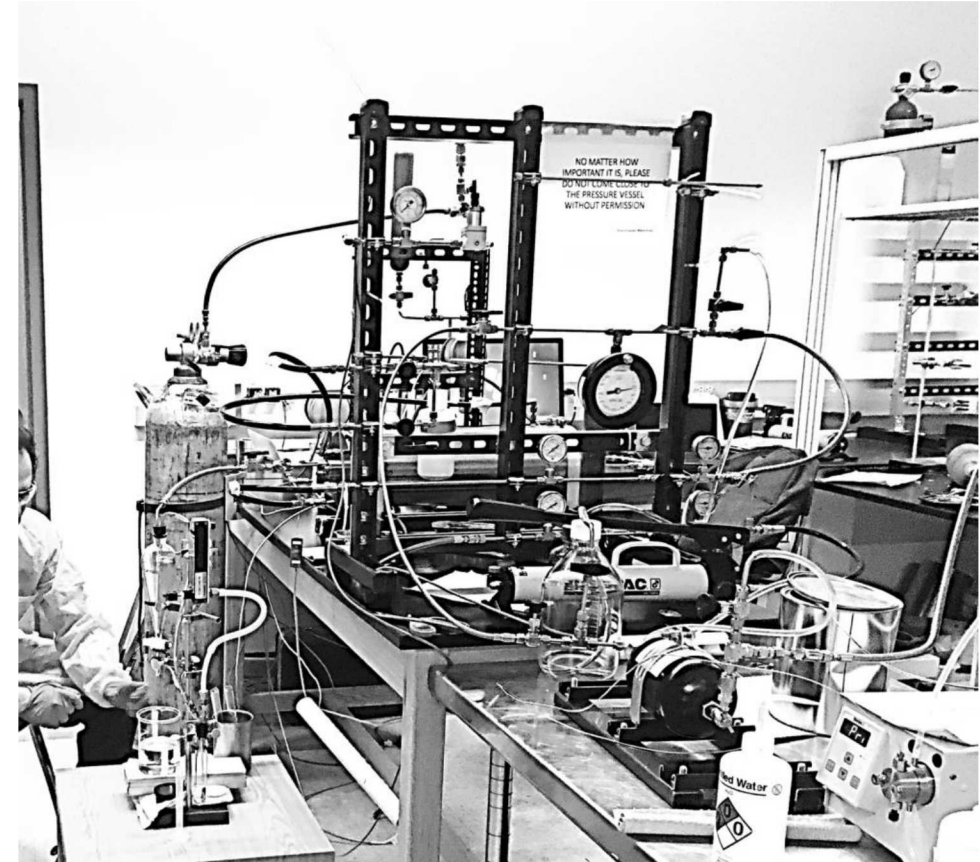


## Simultaneous two-phase flow test

The simultaneous steady-state gas and oil flow through the fracture is used to find both oil and gas relative permeabilities under the same conditions.

$$\text{Relative permeability, } K_{ri} = K_i / K$$

Where  $K$  is the permeability of fracture in single phase flow (absolute permeability) and  $K_i$  is the effective permeability of an individual phase (phase permeability)



**Laboratory setup for two-phase flow test**

## Relative permeability models

- ➔ The sum of relative permeabilities is equal to one, - **absence of phase interference** during the flow
- ➔ **Porous media approach**, where the pore space occupied by an individual phase is not available to the other phase.
- ➔ **Viscous coupling model**, where both phases of fluid interacts with each other similar to two-phase flow in pipes.



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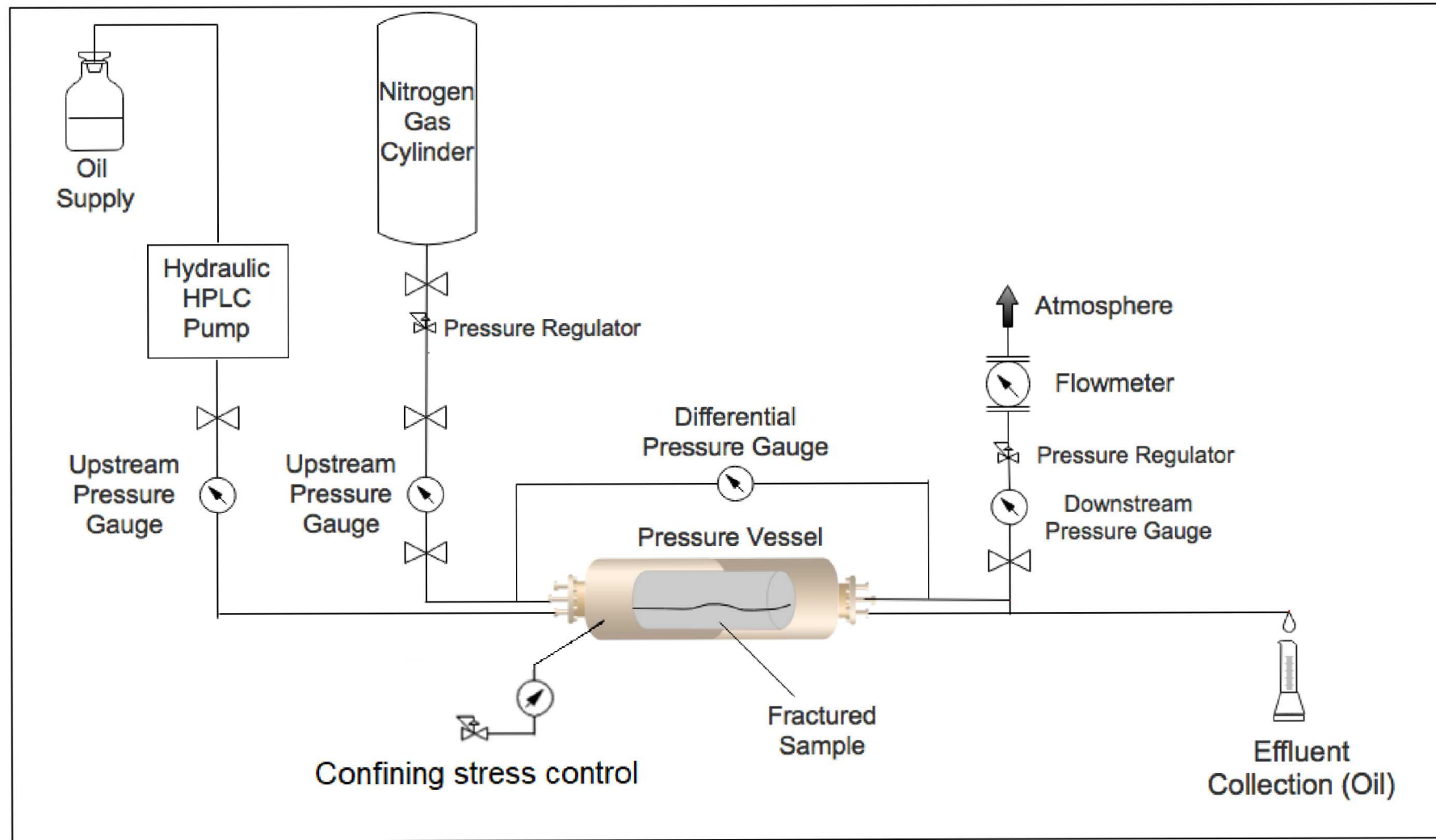
## Relative permeability models

Relative permeability model	Most commonly used model	Most commonly used mathematical expression*
Absence of phase interference	X - curve	$K_{rl} = 1 - K_{rg}$
Porous media approach	Corey's model (Power law)	$K_{rg} = (1 - \sqrt[4]{K_{rl}})^2 (1 - \sqrt[2]{K_{rl}})$
Viscous coupling model	Pipe flow model	$K_{rl} = \frac{1}{2} (1 - \sqrt[3]{K_{rg}})^2 (2 + \sqrt[3]{K_{rg}})$

\*Note:  $K_{rl}$  is the relative permeability of liquid, and  $K_{rg}$  is the relative permeability of gas.

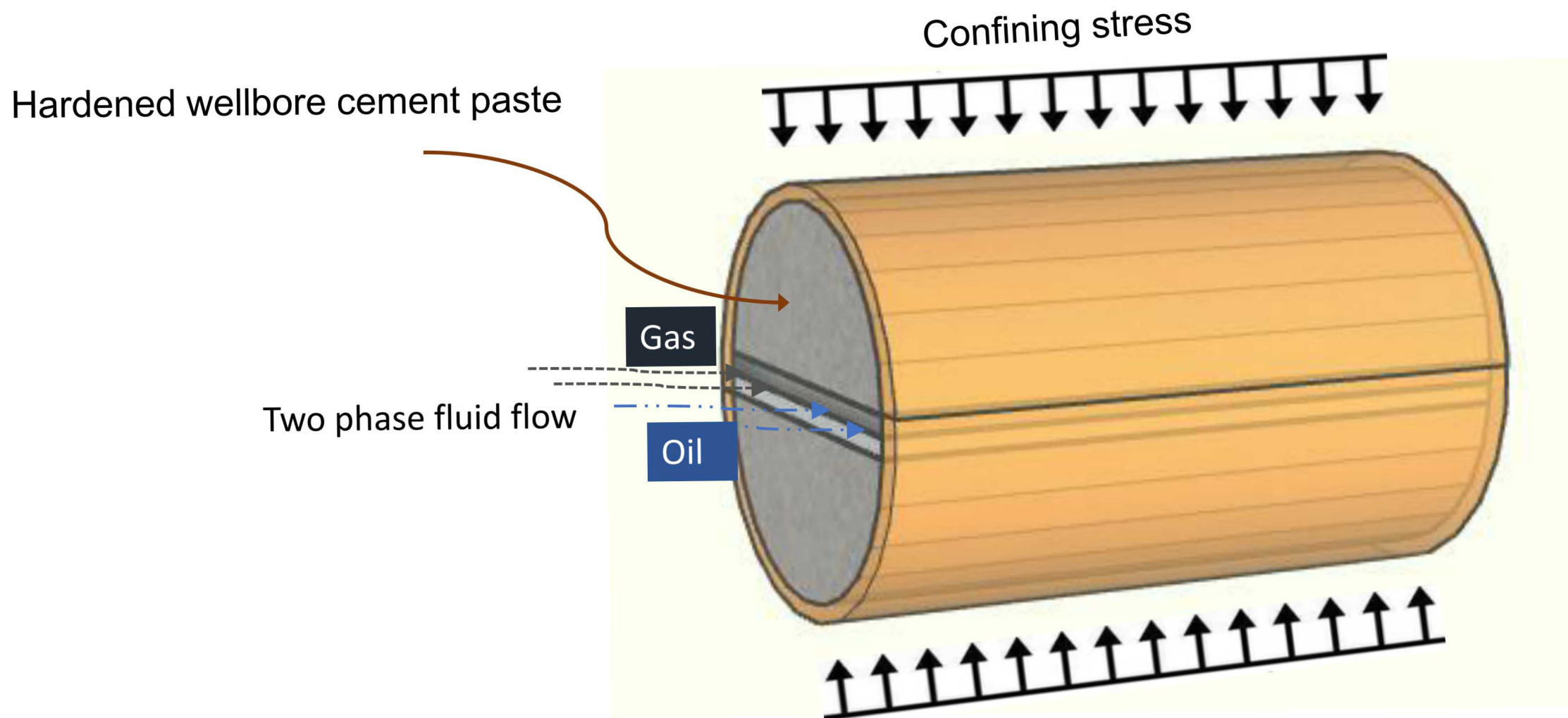


## Simultaneous two-phase flow test



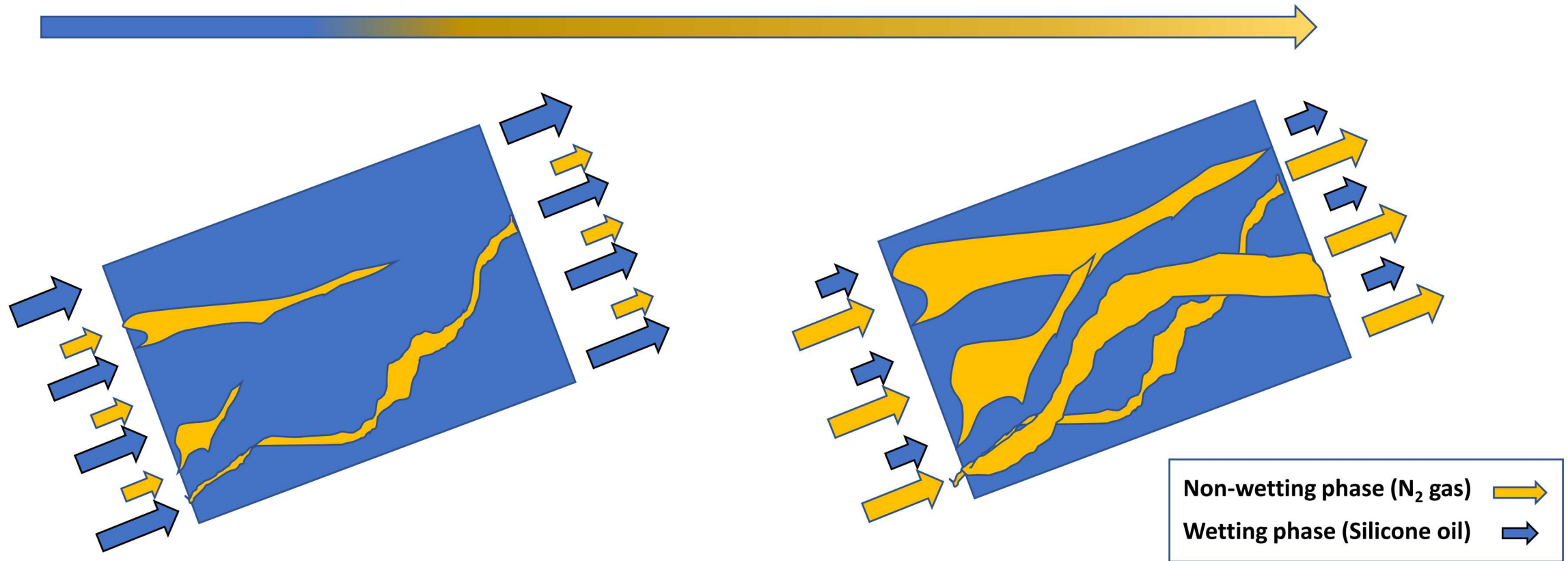
Simplified schematic of the two-phase flow test configuration

## Simultaneous two-phase flow test



# Simultaneous two-phase flow test

Increasing gas flow and decreasing oil flow.



Plan view of fracture face (for illustration purpose only)



## Simultaneous two-phase flow test

Evaluate the role of aperture  
size and nature of fracture

Wetting fluid	Non-wetting fluid	Confining stress (MPa)
Silicone oil (Viscosity 10 cSt)	Nitrogen gas	3.45
Silicone oil (Viscosity 10 cSt)		13.80
Silicone oil (Viscosity 20 cSt)		3.45

### Absolute permeability measurements of the fracture

Confining stress (MPa)	Permeability (m <sup>2</sup> )	Mean hydraulic aperture (μm)
3.45	$7.08 \times 10^{-14}$	40
13.80	$2.26 \times 10^{-14}$	27

# Simultaneous two-phase flow test

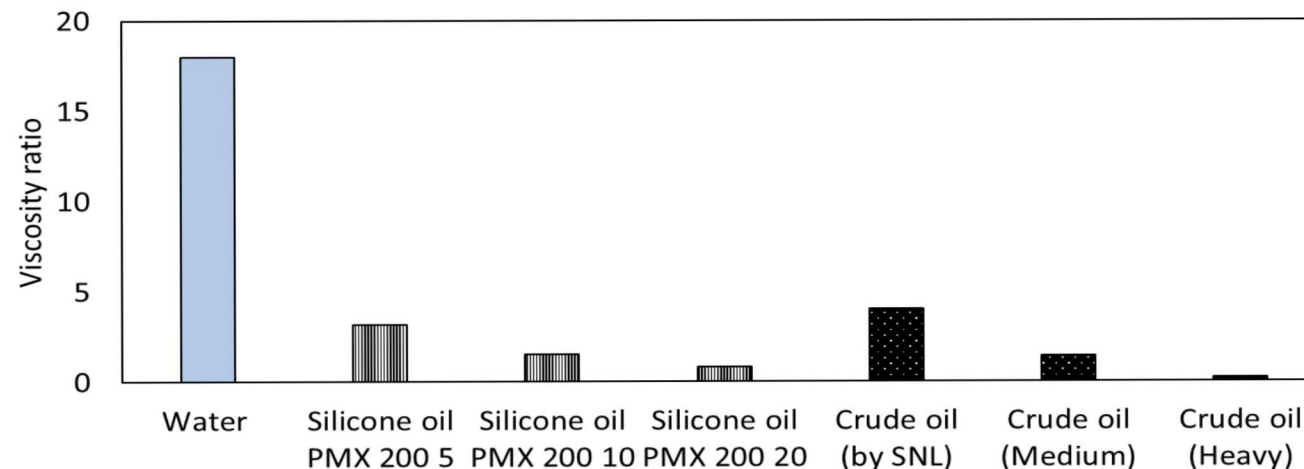
Evaluate the role of viscosity ratio

Wetting fluid	Non-wetting fluid	Confining stress (MPa)
Silicone oil (Viscosity 10 cSt)		3.45
Silicone oil (Viscosity 10 cSt)	Nitrogen gas	13.80
Silicone oil (Viscosity 20 cSt)		3.45

Brookfield RST-CC Rheometer

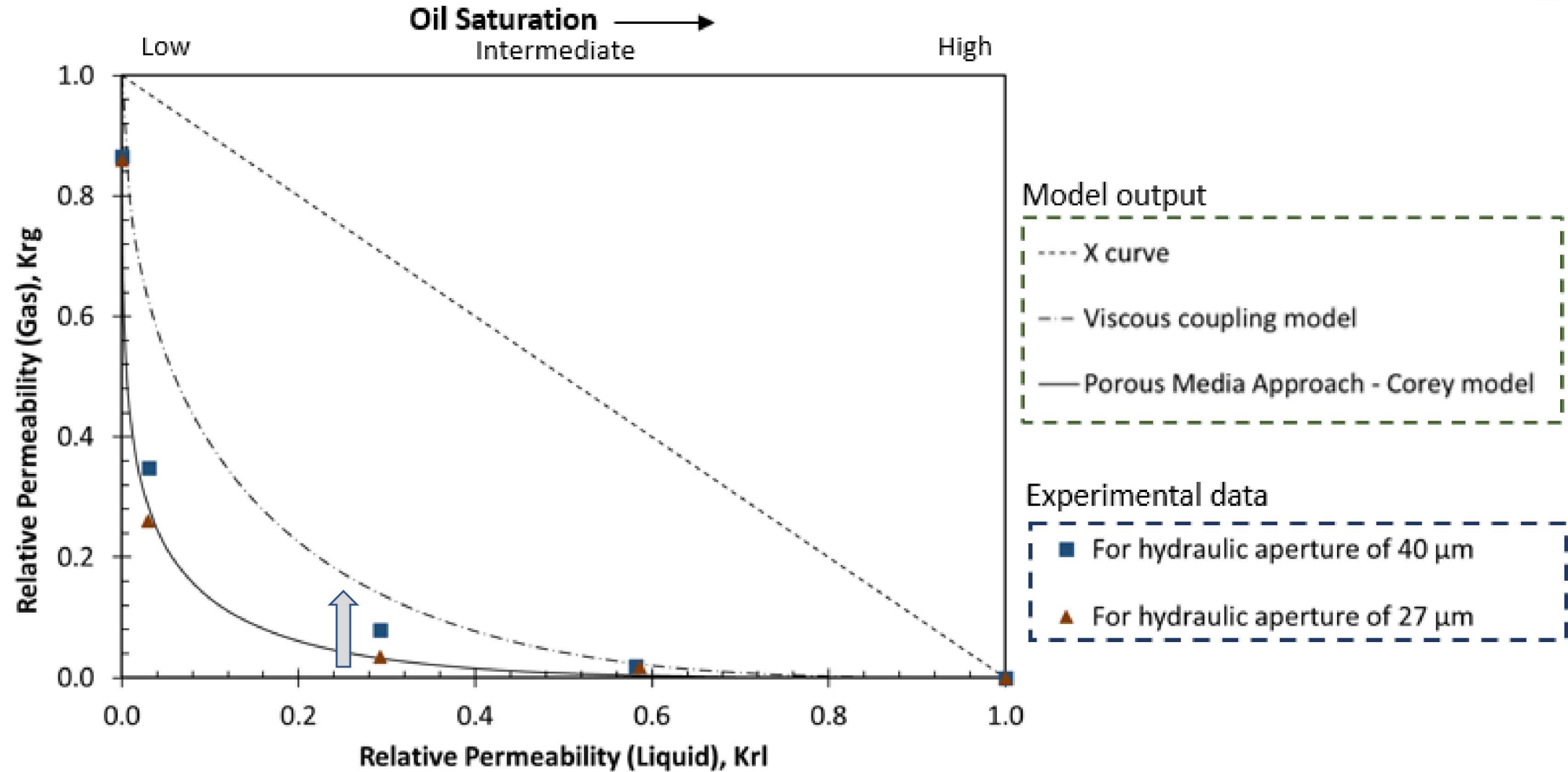


Comparison of viscosity Ratio ( $\mu_{\text{nitrogen}}/\mu_{\text{liquid}}$ )



# Results





The relationship between wetting (l) and non-wetting (g) relative permeabilities ( $K_r$ ) for different fracture apertures (experimental data and model output).

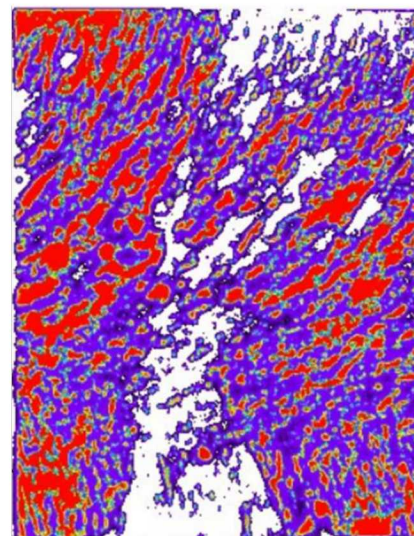
## Pressure sensitive film

Change in contact area with  
confining stress observed using  
pressure sensitive film

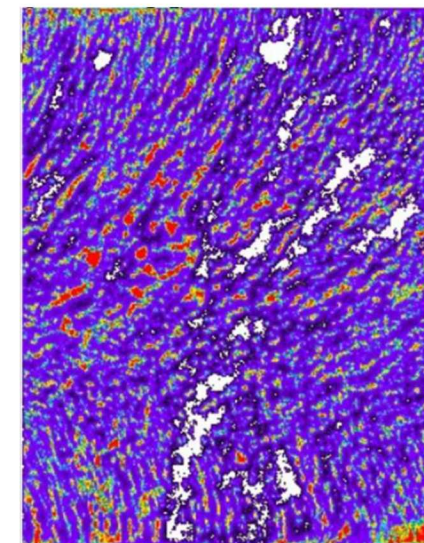


## Pseudo color representation of the specimens

The contact area increased  
about 12% due to the  
increase in applied  
confining stress.

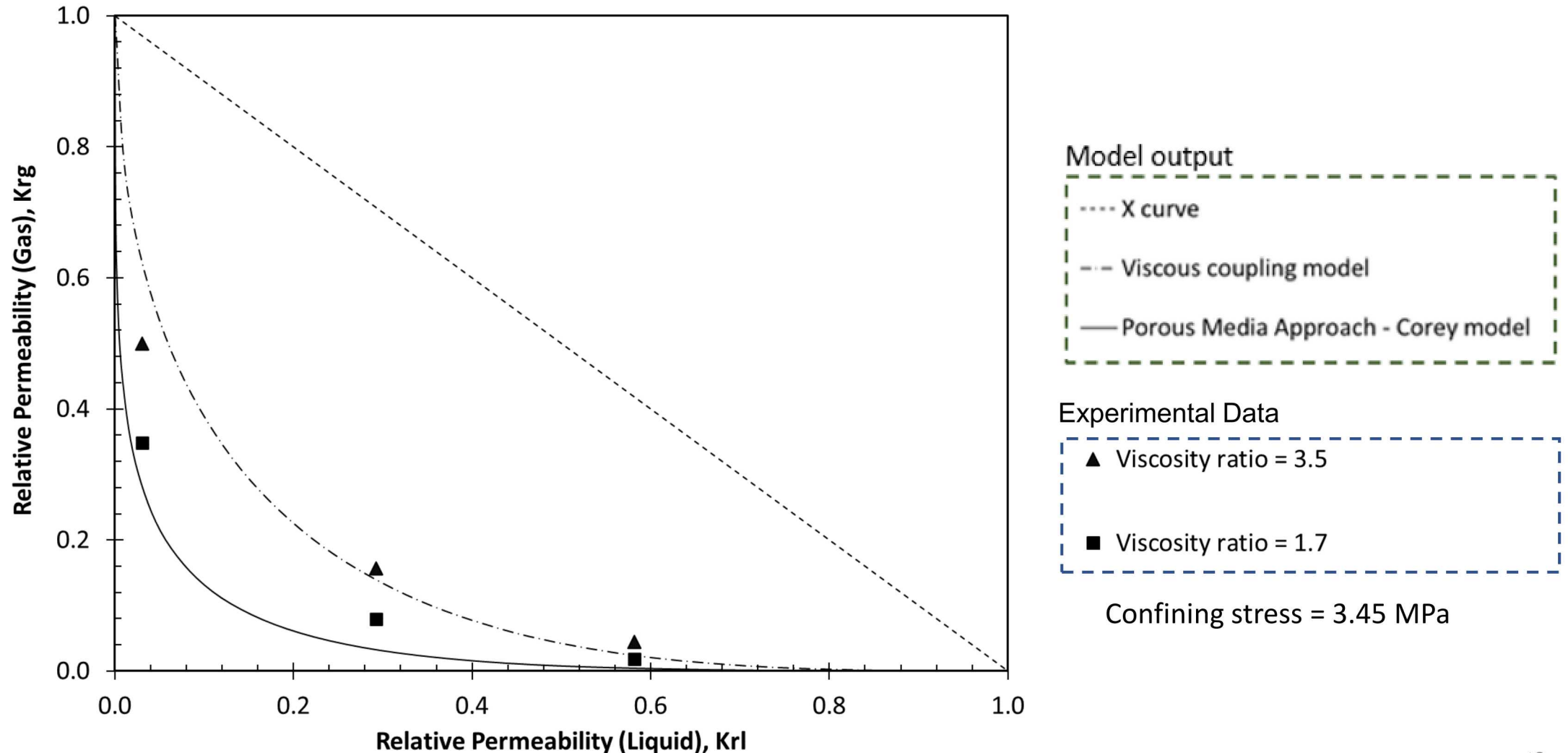


At 3.45 Mpa (500 psig) confining stress



At 13.8 Mpa (2000 psig) confining stress

## Relative permeabilities (for two different values of $M$ ) obtained from experimental studies and conceptual models often used by industry





# Conclusions

- The two-phase flow relative permeability is not solely a function of saturation.
- The sum of wetting and non-wetting phase permeabilities is smaller than one.

**There is very significant phase interference. Therefore, the simplest models for relative permeability are not applicable.**

- Relative permeability varies with fracture aperture, which controls the amount of fluid flow, flow path geometry and tortuosity.
- The relative permeability of the non-wetting phase varies with the viscosity ratio.

**The measured relative permeabilities mostly fall between the porous media and viscous coupling models, depending on viscosities of the fluids and the geometric character of the fracture.**

## **Acknowledgments**

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# Thank you

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