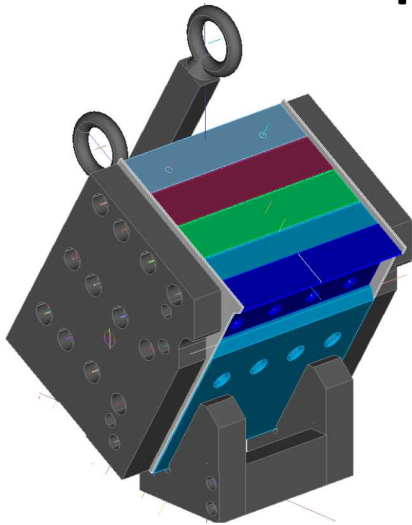


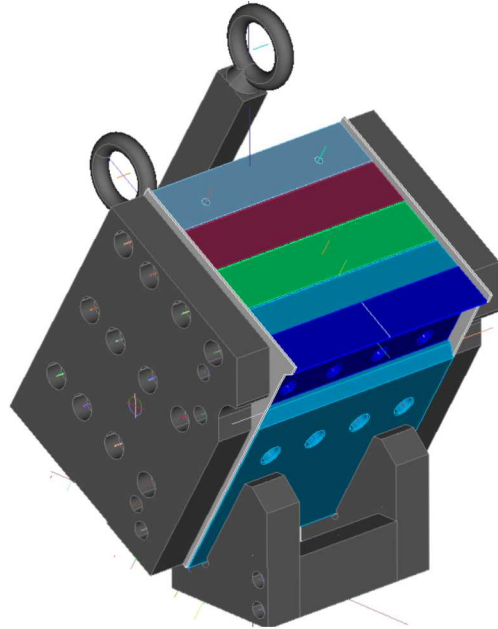
Multilayer Slide Coating Model for Manufacturing of PEMFC

**Kristianto Tjiptowidjojo[†], Janghoon Park[§], Scott A. Mauger[§],
Michael Ulsh[§], P. Randall Schunk^{†,*}**

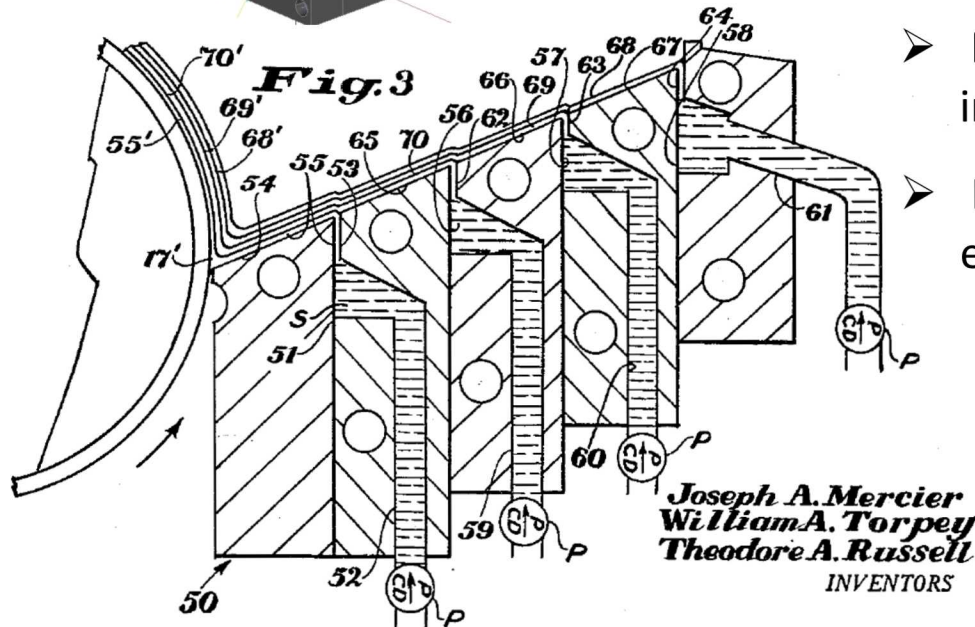


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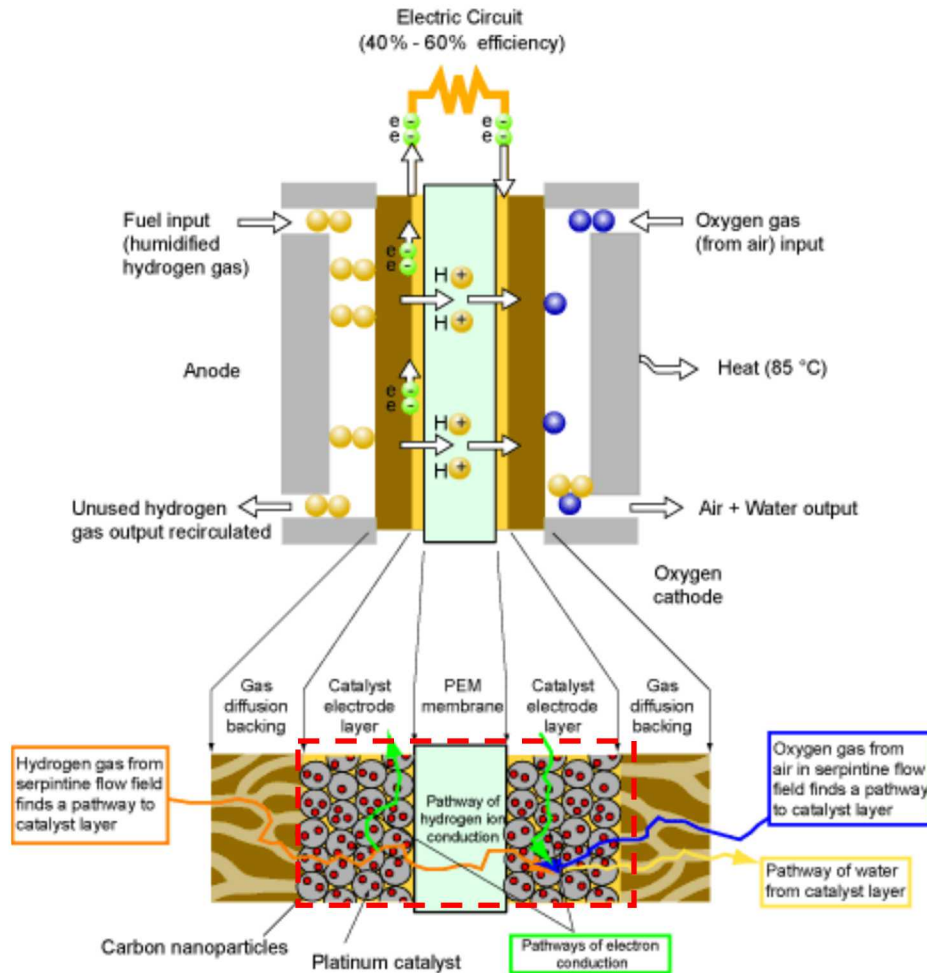
Slide Coating



- A method ideal for **precisely coating multiple layers** or more
- Stack multiple layers via **gravity driven flow** and coat them simultaneously on a moving substrate.
- **Premetered method** → thickness is set by flow rate and coating speed
- Developed originally by photographic film industries
- Emerging application: Multilayer structures for energy -> **polymer membrane fuel cell (PEMFC)**



Polymer Electrolyte Membrane Fuel Cells (PEMFC)



<https://www.physics.nist.gov/MajResFac/NIF/pemFuelCells.html>

Anode Reaction

Convert hydrogen gas into **protons** and **electrons**



Ions Transport

- Transport **protons** *through the membrane*
- Transport **electrons** *around the membrane* through external circuit → electricity

Cathode Reaction

Combine protons, electrons, and oxygen to form water and heat



- Use slide coating to manufacture **membrane-electrode-assembly (MEA)**
- Target speed: **1- 10 min/min**
- Target wet thicknesses:
 - Anode/cathode: **60 – 150 μm**.
 - Membrane: **250 μm**

Slide Coating Model

Cauchy momentum
Continuity

$$\begin{aligned}\rho \mathbf{u} \cdot \nabla \mathbf{u} - \nabla \cdot \underline{\underline{\mathbf{T}}} - \rho \mathbf{g} &= \mathbf{0} \\ \nabla \cdot \mathbf{u} &= 0\end{aligned}$$

Die Surface

$$\mathbf{u} = 0$$

Inflow

Specify velocity profile,
(flow rate)

Downstream Meniscus

$$\mathbf{n} \cdot \underline{\underline{\mathbf{T}}} = 2H\sigma\mathbf{n} + p_{atm}\mathbf{n}$$

Outflow

"Open" or "Free"

- Two-dimensional **steady state** model
- **Free surface shape is not known a priori** → need to be solved as well
- **Arbitrary Lagrangian Eulerian (ALE)** method
 - pseudo solid elasticity
- Solved with Galerkin finite element method
 - **G/FEM**

Dynamic Contact Line

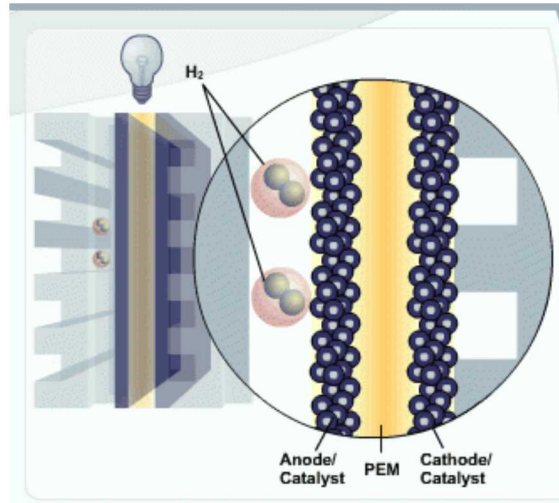
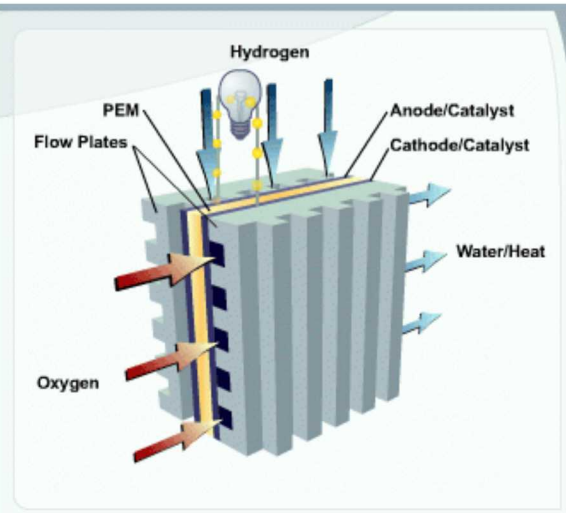
$$\mathbf{t}\mathbf{n} : \underline{\underline{\mathbf{T}}} = \frac{1}{\beta} \mathbf{t} \cdot (\mathbf{u} - \mathbf{U}_w)$$

Web Surface
 $\mathbf{u} = \mathbf{U}_w$

Upstream Meniscus

$$\mathbf{n} \cdot \underline{\underline{\mathbf{T}}} = 2H\sigma\mathbf{n} + p_{vac}\mathbf{n}$$

Coating Materials



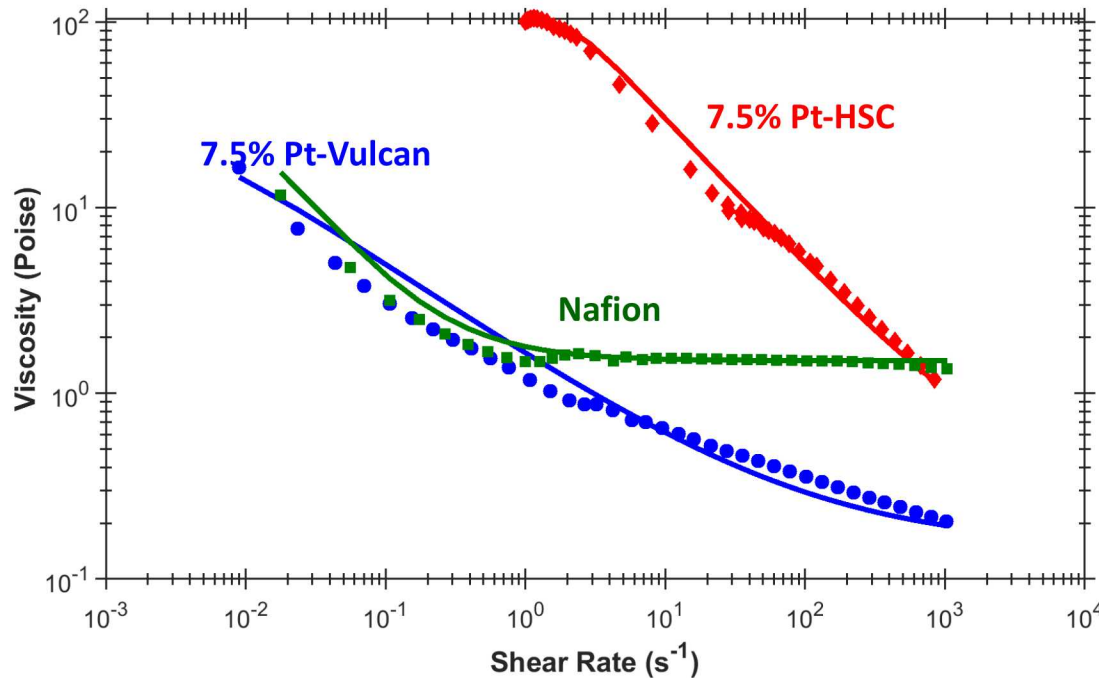
Anode/Cathode:

- Platinum – Vulcan 3% or 7.5%, 1-propanol 10%, I/C 1.05
- Platinum – High Surface Carbon (HSC) 3% or 7.5%, 1-propanol 10%, I/C 1.05

Membrane:

- Nafion™ D2020 – Ionomer 20%, Water 34%, 1 Propanol 46%

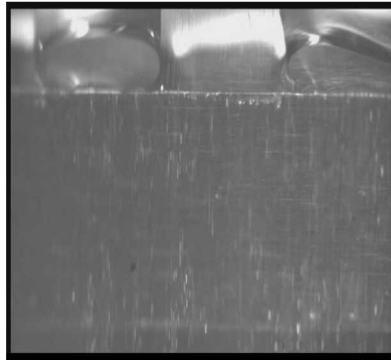
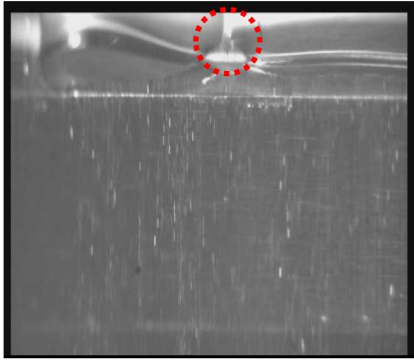
<https://www.energy.gov/eere/fuelcells/fuel-cell-animation-text-version>



- Particles-laden ink system – highly **shear thinning**
- All layers are miscible → **no interfacial tension**
- Wide ranges of viscosity values → **tailor ink rheology** to improve coatability

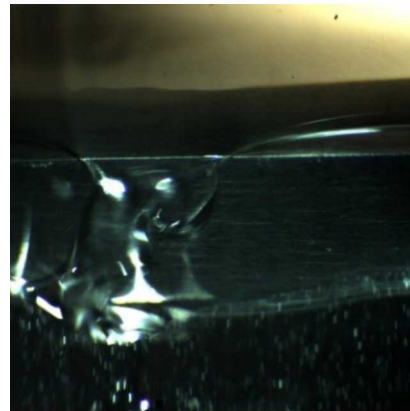
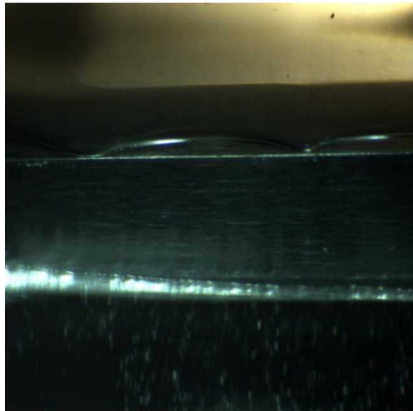
Mapping Vacuum Limits

Front View of Bead – Low Vacuum Limits



- Typically a “vacuum” pressure is applied on upstream meniscus to **stabilize the bead**
- Too little vacuum → **rivulets – low vacuum limit**
- Too high vacuum → **weeping, leakage – high vacuum limit**

Front View of Bead – High Vacuum Limits



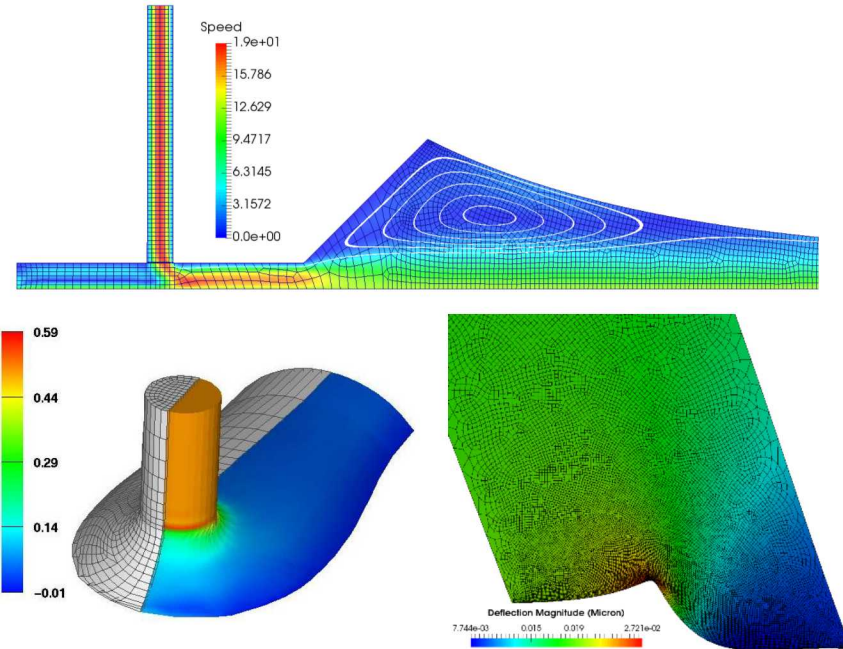
- Strongly correlates with **upstream meniscus** (contact lines) **location**
- Solve **an augmenting condition** for vacuum pressure needed to place upstream contact line in either edge of die face → **solve for vacuum limits**.

Tjiptowidjojo, K., & Carvalho, M. S. (2011). Operability limits of slide coating. *Chemical Engineering Science*, 66(21), 5077-5083.

Simulation Tool: Goma 6.0



2014 R&D 100 Award Winner

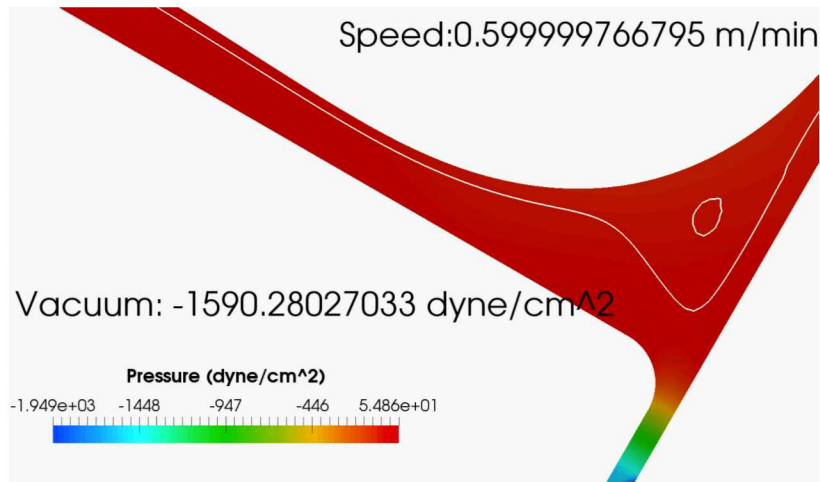


- Multiphysics *finite element* code, suitable for both *research* and *production*
- Fully-coupled and segregated *free* and moving *boundary* parameterization – ALE, Level Set, etc.
- Modular code; *easy to add equations* – currently has 200+ differential equations
- *Open source*! Available at <http://goma.github.io>
- *Goma 6.0. training* is available!

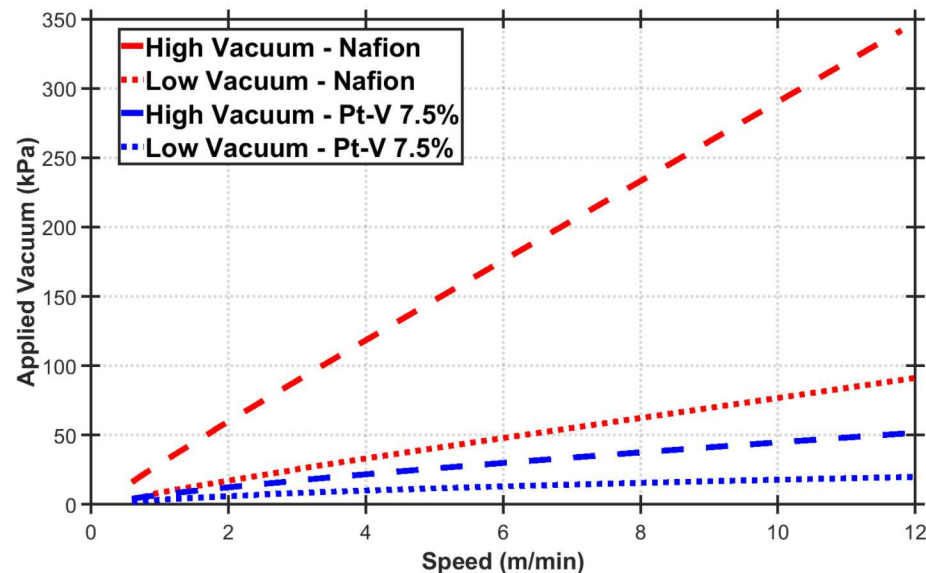
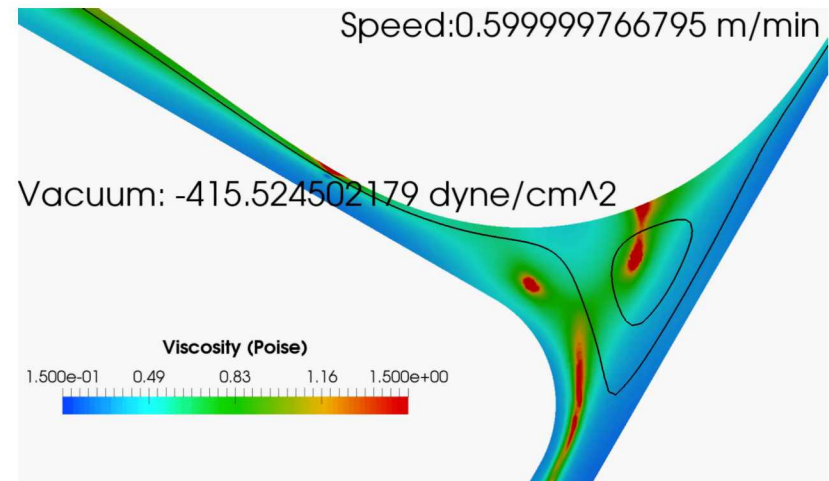
Goma has been used successfully in coating manufacturing for 3 decades!

Single Layer – Vacuum Limits

Nafion – $h_{\text{wet}} = 250 \mu\text{m}$

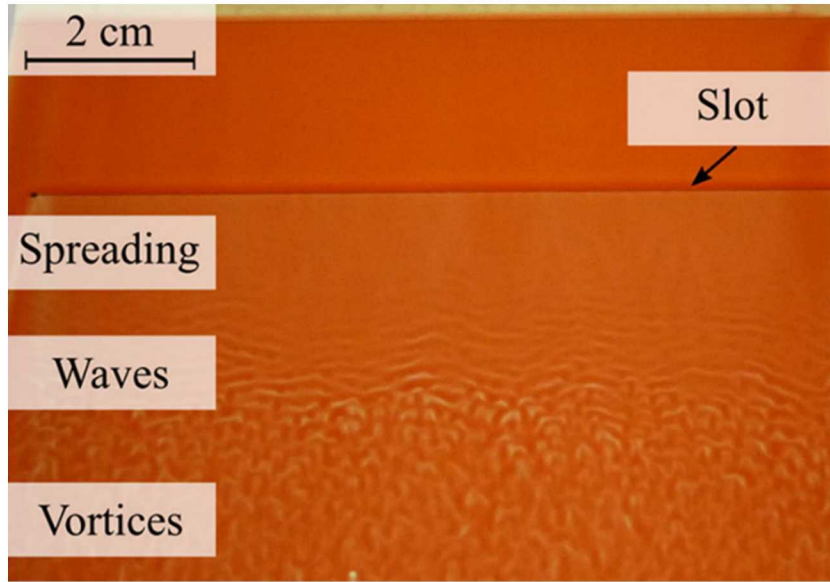


Pt-V 7.5% – $h_{\text{wet}} = 64 \mu\text{m}$



- Increase speed with constant h_{wet} → **calculate flow field and required applied vacuum** to keep upstream static contact line at either die face edge
- Downstream vortex disappear at higher speed (and vacuum)
- Nafion vacuum limits are higher than Pt-V 7.5% due to **shear thinning** of catalyst ink

Stability of Flow



Buerkin, Cornelia K., et al. "Investigation of interfacial instabilities with a two-layer slide coating process." *Journal of Coatings Technology and Research* 14.5 (2017): 991-1001.

- Predict vacuum limits – **onset of 3-D flow instabilities** with **heuristics** from visualization
- Enable **prediction** of vacuum limits with a **2-D model**.
- Other defects commonly found in multilayer slide coating: **Interfacial instabilities**.
Manifestation: Dewetting, waves, vortices
- No known heuristics to predict onset, some rules of thumbs available → Buerkin et al. (2017).

Predict stability of flow with 2-D base flow model → linear stability analysis

Linear Stability Analysis

Examining flow behavior due to *infinitesimally small* disturbances

Governing equations:

$$\rho \left[\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right] - \nabla \cdot \underline{\underline{\mathbf{T}}} - \rho \mathbf{g} = \mathbf{0} \quad ; \quad \mathbf{T} = -p \mathbf{I} + \mu [\nabla \mathbf{u} + \nabla \mathbf{u}^T]$$

$$\nabla \cdot \mathbf{u} = 0$$

Express solution in terms of **base (steady state)** solution and **small disturbance**:

$$\begin{aligned} \mathbf{u} &= \mathbf{u}_0 + \varepsilon \mathbf{u}_1 \\ p &= p_0 + \varepsilon p_1 \end{aligned}$$

Base Disturbance
(steady)

Substitute into PDE, eliminate $o(\varepsilon^2)$ and higher order terms, discretize with G/FEM:

$$\underline{\underline{\mathbf{M}}} \frac{d}{dt} \begin{bmatrix} \mathbf{u} \\ p \end{bmatrix} = \underline{\underline{\mathbf{J}}} \begin{bmatrix} \mathbf{u} \\ p \end{bmatrix}$$

Express solution in terms of eigenmodes: $\begin{bmatrix} \mathbf{u} \\ p \end{bmatrix} = \sum_{i=1}^N \mathbf{x}_i \exp(\lambda_i t)$

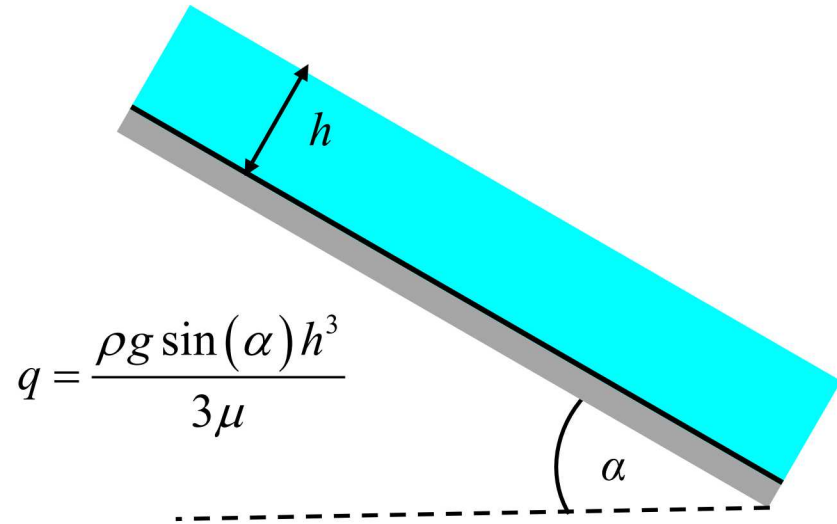
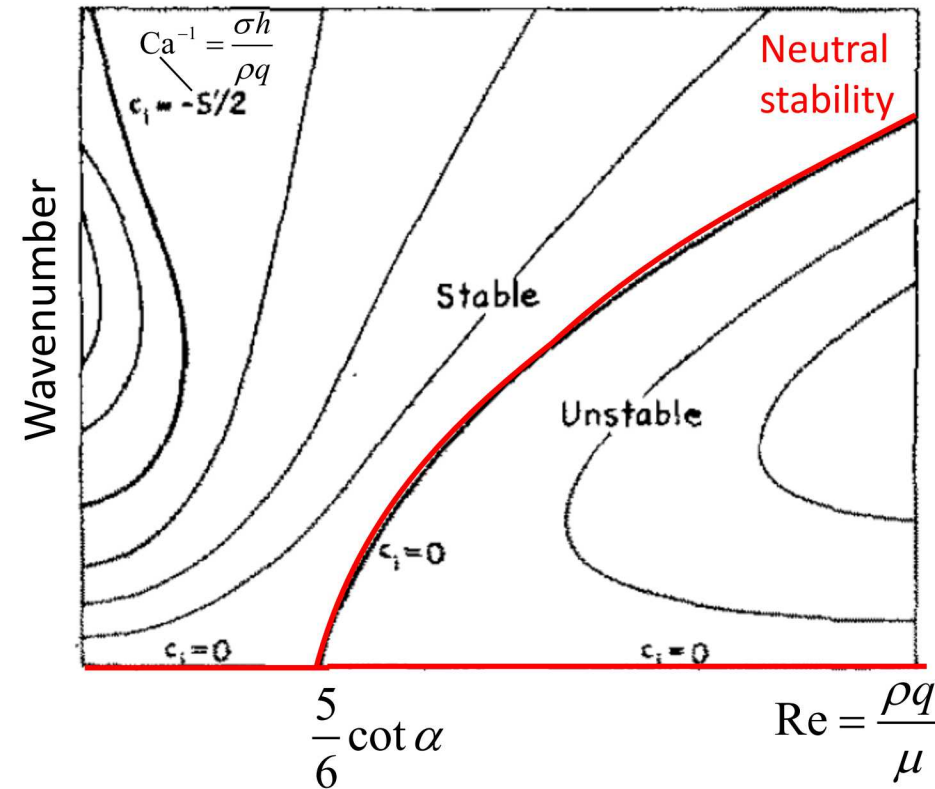
Generalized eigenvalue problem:

$$\lambda_i \underline{\underline{\mathbf{M}}} \mathbf{x}_i = \underline{\underline{\mathbf{J}}} \mathbf{x}_i$$

$\text{Re}(\lambda) > 0 \rightarrow \text{unstable mode}$

$\text{Re}(\lambda) < 0 \rightarrow \text{stable mode}$

Previous Work – Single Layer



Yih, C.S. (1963) "Stability of liquid flow down an inclined plane." *The Physics of Fluids* 6(3): 321-334.

- Fully developed Newtonian flow down an inclined plane – **2-D linear stability of 1-D flow**
- Neutral stability curve ($Re(\lambda) = 0$) **depends on plane inclination** α .
- Small wavenumber (**long wavelength**) modes are **most unstable**. Smaller wavelength modes are dampened with surface tension
- For inclination of 30° , critical $Re = 1.44$

Linear Stability Analysis of Slide Flow

Cauchy momentum $\rho \mathbf{u} \cdot \nabla \mathbf{u} - \nabla \cdot \underline{\underline{\mathbf{T}}} - \rho \mathbf{g} = \mathbf{0}$

Continuity $\nabla \cdot \mathbf{u} = 0$

Die Surface
 $\mathbf{u} = 0$

Downstream Meniscus

$$\mathbf{n} \cdot \underline{\underline{\mathbf{T}}} = 2H\sigma\mathbf{n} + p_{atm}\mathbf{n}$$

Outflow
"Open" or "Free"

- Two-dimensional **2-D stability analysis**
- Use **rheological properties** of **nafion**
- Solve generalized eigenvalue system with **varied Re** (density) – we use dimensional formulation in Goma.

Conclusions

- Complete single layer and two-layer slide coating flow model
- Augment the flow model to solve for applied vacuum pressure needed to locate upstream contact line at either die face edge → expedite vacuum limits mapping by continuing in speed and vacuum simultaneously
- Verify linear stability analysis implementation with single-layer slide flow study

Research Plans

- Complete three-layer slide coating flow model
- Complete stability analysis of two-layer and three-layer slide flow
- Use the model and stability analysis to guide ink and process condition selections

References

Funding Support



Back Up Slides

Linear Stability Analysis

Examining flow behavior due to *infinitesimally small* disturbances

Governing equations:

$$\rho \left[\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right] - \nabla \cdot \underline{\underline{\mathbf{T}}} - \rho \mathbf{g} = \mathbf{0} \quad ; \quad \mathbf{T} = -p\mathbf{I} + \mu [\nabla \mathbf{u} + \nabla \mathbf{u}^T]$$

$$\nabla \cdot \mathbf{u} = 0$$

Express solution in terms of **base (steady state)** solution and **small disturbance**:

$$\mathbf{u} = \mathbf{u}_0 + \varepsilon \mathbf{u}_1$$

$$p = p_0 + \varepsilon p_1$$

Base Disturbance
(steady)

Substitute into PDE and eliminate $o(\varepsilon^2)$ or higher order terms

$o(1)$ term:

$$\rho \mathbf{u}_0 \cdot \nabla \mathbf{u}_0 - \nabla \cdot \underline{\underline{\mathbf{T}}}_0 - \rho \mathbf{g} = \mathbf{0}$$

$$\nabla \cdot \mathbf{u}_0 = 0$$

Solve base flow fields \mathbf{u}_0 and p_0 with finite element method

$o(\varepsilon)$ term:

$$\rho \left[\frac{\partial \mathbf{u}_1}{\partial t} + \mathbf{u}_0 \cdot \nabla \mathbf{u}_1 + \mathbf{u}_1 \cdot \nabla \mathbf{u}_0 \right] - \nabla \cdot \mathbf{T}_1 = \mathbf{0}$$

$$\nabla \cdot \mathbf{u}_1 = 0$$

Use base flow solution to solve for disturbance flow fields.

Generalized Eigenvalue Problem

Finite element method transforms the PDEs into a system of differential algebraic equations

$$\underline{\underline{\mathbf{M}}} \frac{d}{dt} \begin{bmatrix} \mathbf{u} \\ p \end{bmatrix} = \underline{\underline{\mathbf{J}}} \begin{bmatrix} \mathbf{u} \\ p \end{bmatrix}$$

Express solution in terms of eigenmodes: $\begin{bmatrix} \mathbf{u} \\ p \end{bmatrix} = \sum_{i=1}^N \mathbf{x}_i \exp(\lambda_i t)$

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$\text{Re}(\lambda) > 0 \rightarrow \text{unstable mode}$

$\text{Re}(\lambda) < 0 \rightarrow \text{stable mode}$