

# Using Machine Learning to Predict Self-Diffusion in Lennard Jones Fluids

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Division/Committee: Chemical Information

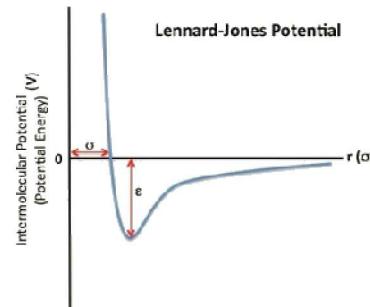
*\*Due to the COVID-19 pandemic this presentation was pre-recorded and will be broadcast*

PRESENTED BY

**Joshua P. Allers**

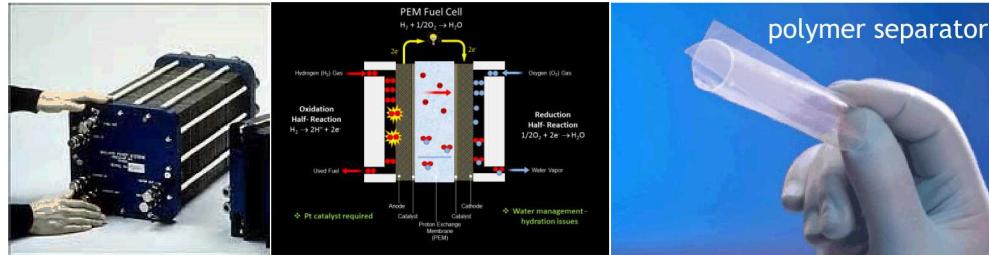
Organic Materials Science Department  
Sandia National Laboratories  
Albuquerque, NM

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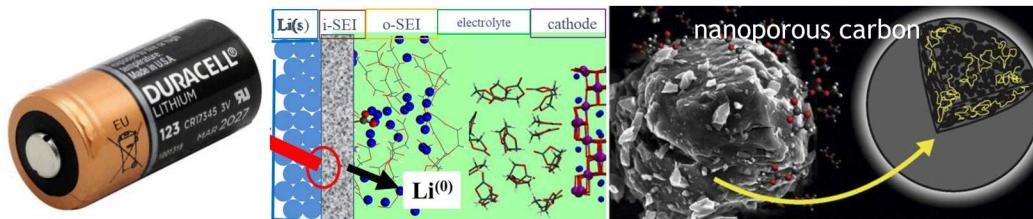


# Diffusion of Mixtures Absorbed into Materials: Interest at Sandia National Laboratories

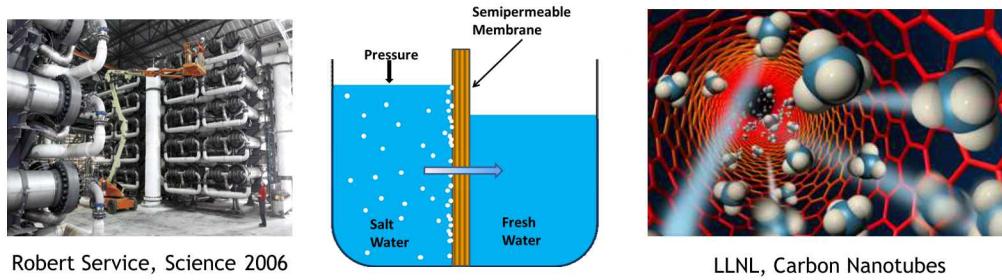
## H<sub>2</sub>O/MeOH Fuel Cells



## Batteries



## Separation Membranes



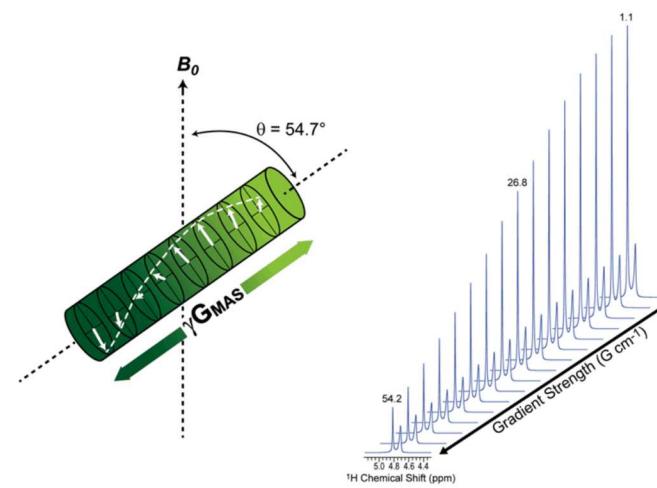
- Understanding the diffusion of chemical species in porous materials critical for the design and performance optimization for different materials.



# Current Methods for Calculating Diffusion

## Calculating diffusion experimentally

- **NMR diffusometry**, absorption, CT, etc.
- expensive and time-consuming



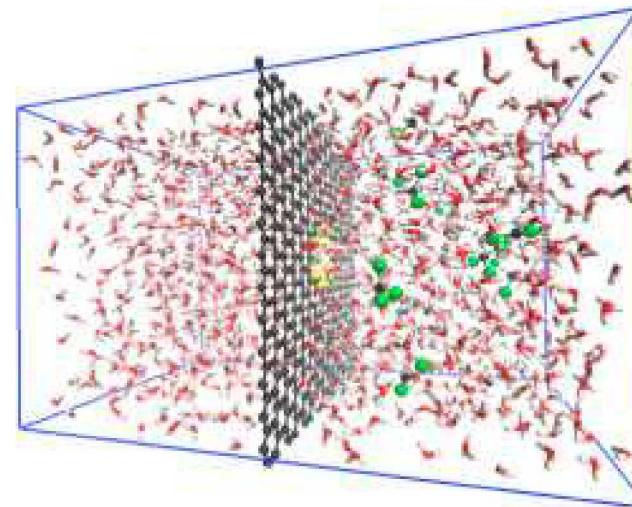
Todd Alam and Janelle Jenkins. Advanced Aspects of Spectroscopy. 2012.

## Calculating diffusion computationally

- **Molecular dynamics** and DFT
- Accurate, but time-consuming
- Require large amounts of computation

## Consider studying 10 different compounds

- Forming all possible binary mixtures
- Testing 10 different compositions
- 450 experiments or simulations



Jafar Azamat *et. al.* Chemical Engineering Science. 2015.



# Challenge - Universal Model for Diffusion

**Maxwell Stephen (MS) Model**  
(dominant diffusion model)

$$\frac{1}{D_{i,\text{self,s}}} = \frac{1}{D_{i,s}} + \frac{x_i}{D_{ii}} + \frac{x_j}{D_{ij}}$$

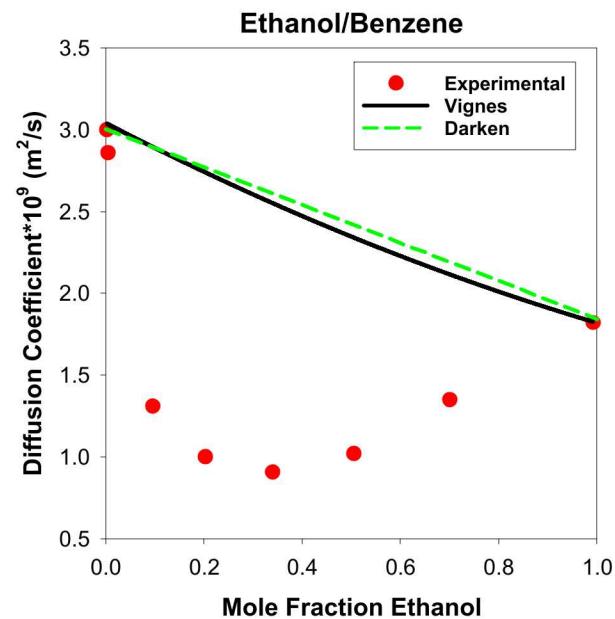
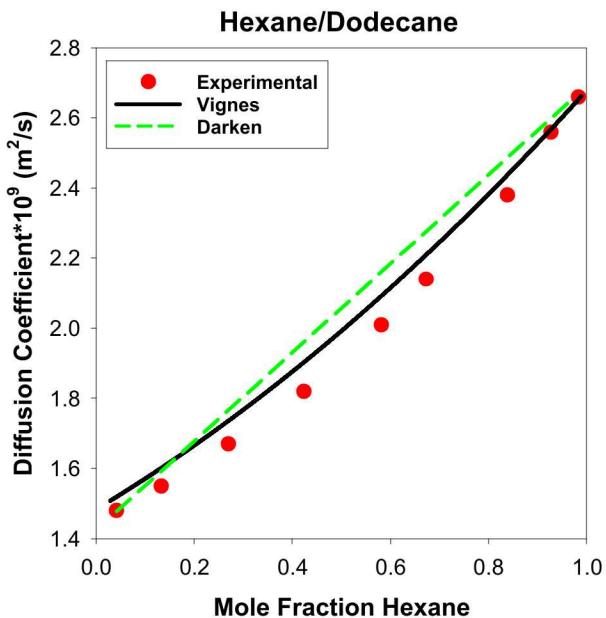
surface    self    exchange

**Darken Relationship**  
(semi-empirical - linear)

$$D_{ij} = D_i D_j \sum_{k=1}^N \frac{x_k}{D_k}$$

**Vignes Model**  
(semi-empirical- power law)

$$D_{ij} = \left( D_{ij}^{x_j \rightarrow 1} \right)^{x_i} \left( D_{ij}^{x_j \rightarrow 1} \right)^{x_j} \prod_{k, k \neq i, j}^{i=N} \left( D_{ij}^{x_k \rightarrow 1} \right)^{x_k}$$

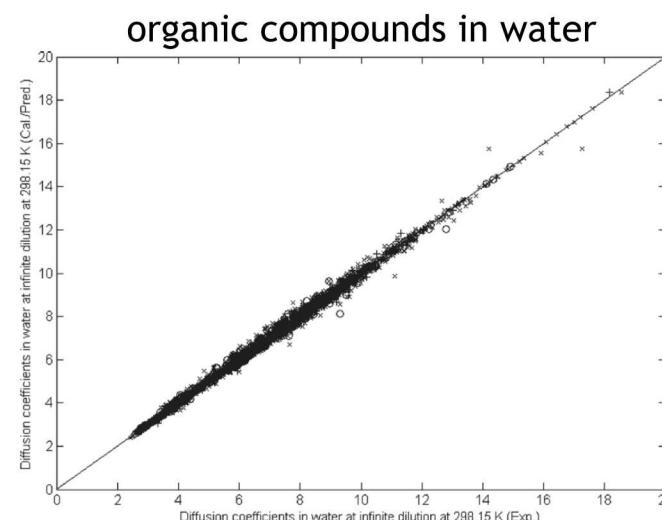
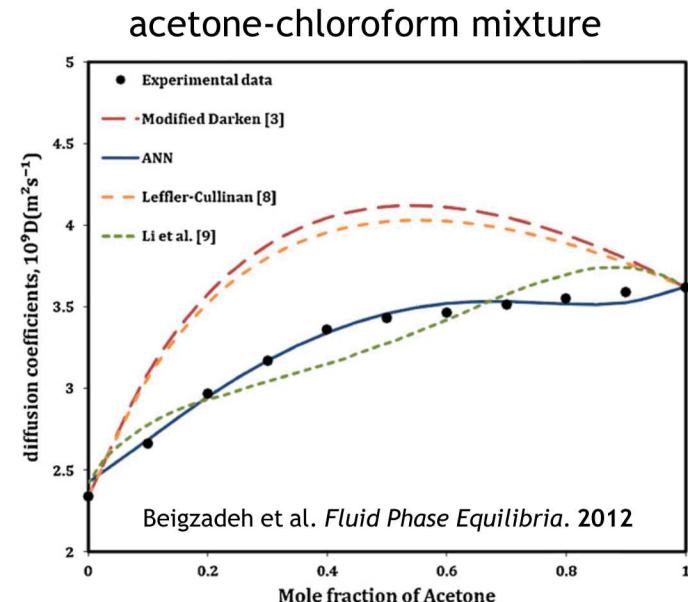


**Goal:** Develop a generalized model that can accurately predict diffusion in multi-component mixtures

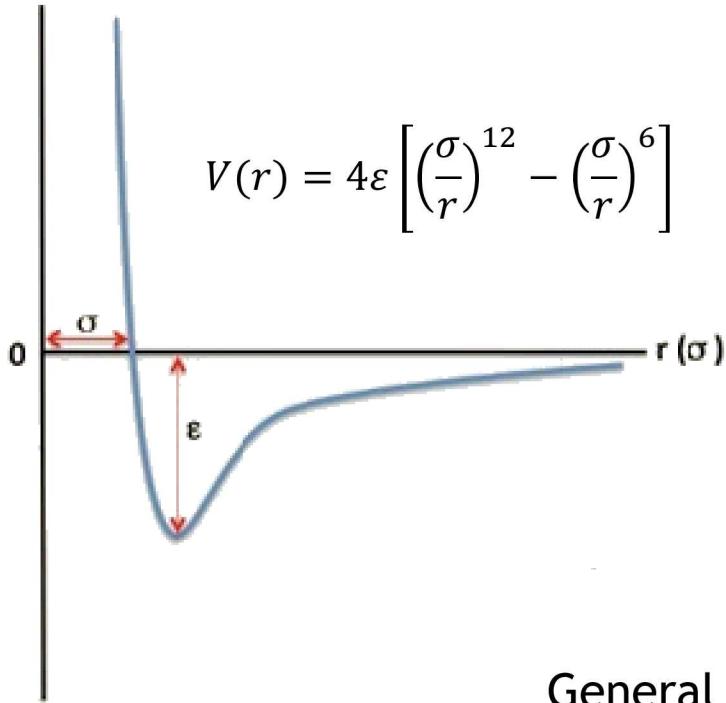


# Potential of Machine Learning

- Rapidly growing field in materials science
- Powerful tools for prediction
  - Random Forests
  - Artificial Neural Networks (ANN)
  - Symbolic Regression
  - Genetic Engineering
- Already showing promise in literature



# Start Simple – Lennard Jones (LJ)

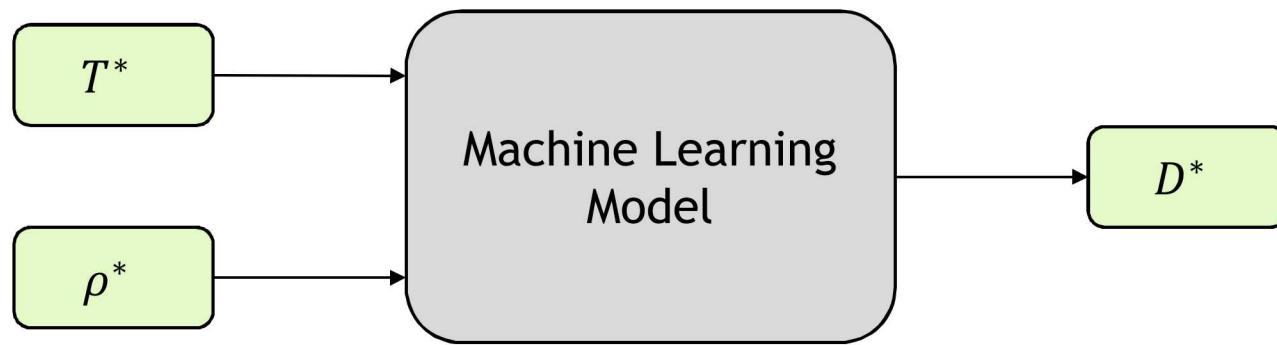


$$V(r) = 4\epsilon \left[ \left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6 \right]$$

$$T^* = \frac{Tk}{\epsilon} \quad \rho^* = \frac{N\sigma^3}{V} \quad D^* = D \sqrt{\frac{m}{\epsilon}}$$

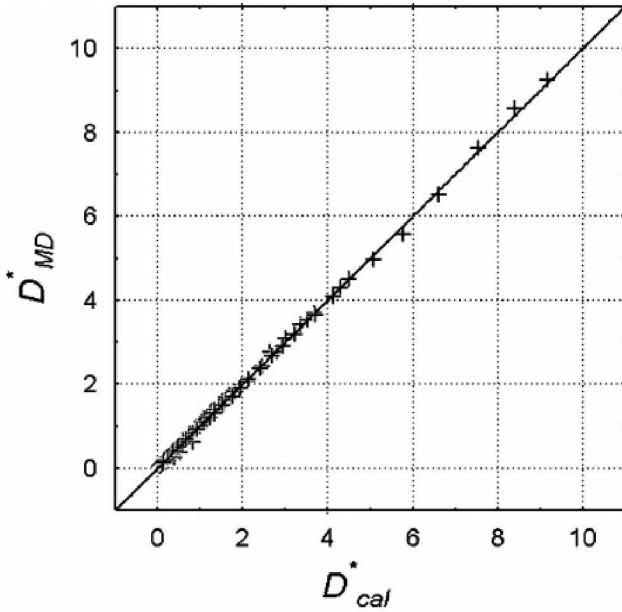
- Explained by two parameters
  - $\sigma$  - Distance where potential becomes zero
  - $\epsilon$  - Well depth and measure of attractive force
- Allows model development over multiple phases

## General Model Architecture



# Lennard Jones Molecular Dynamics (MD)

- Many MD simulations have been performed for LJ systems
- Zhu's empirical equation is one of the better models
  - Has 8 adjustable parameters
- Will act as the “gold standard” for comparison



$$D_{cal}^* = \frac{3\sqrt{T^*}}{8\rho^*\sqrt{\pi}} A \times B$$

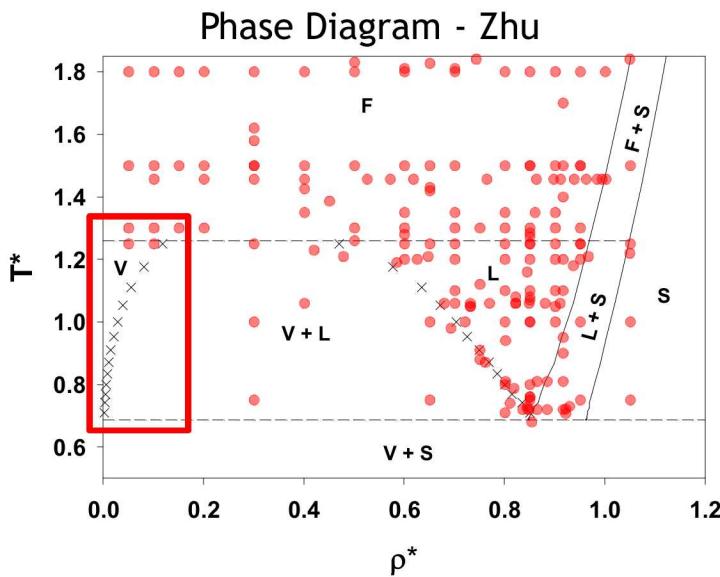
$$A = \left(1 - \frac{\rho^*}{a(T^*)^b}\right) \left[1 + (\rho^*)^c \left( \frac{P1(\rho^* - 1)}{P2(\rho^* - 1) + (T^*)^{(P3+P4\rho^*)}} + P5 \right)\right]$$

$$B = \exp\left(\frac{-\rho^*}{2T^*}\right)$$

Yu Zhu, Xiaohua Lu, Jian Zhou, Yanru Wang, Jun Shi, “Prediction of diffusion coefficients for gas, liquid and supercritical fluid: application to pure real fluids and infinite binary solutions based on the simulation of Lennard-Jones fluid”. *Fluid Phase Equilibria*. 2002. [https://doi.org/10.1016/S0378-3812\(01\)00669-0](https://doi.org/10.1016/S0378-3812(01)00669-0)

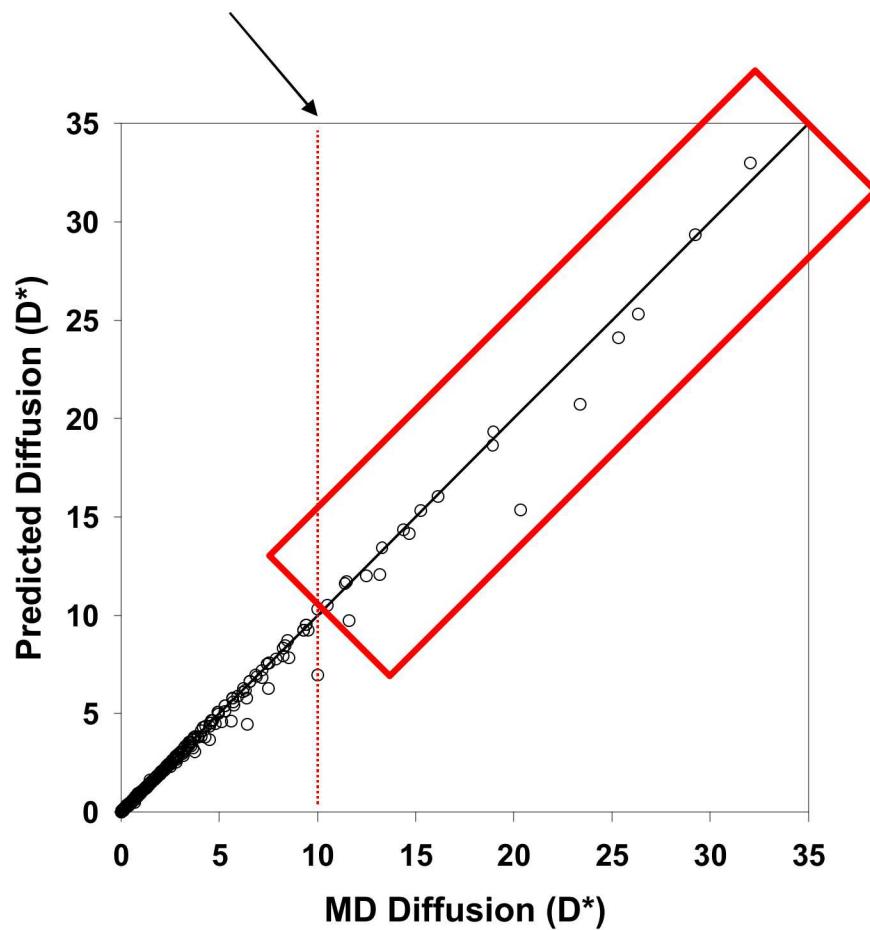


# Expanded Diffusion Dataset



V - vapor  
 L - liquid  
 F - supercritical  
 S - solid

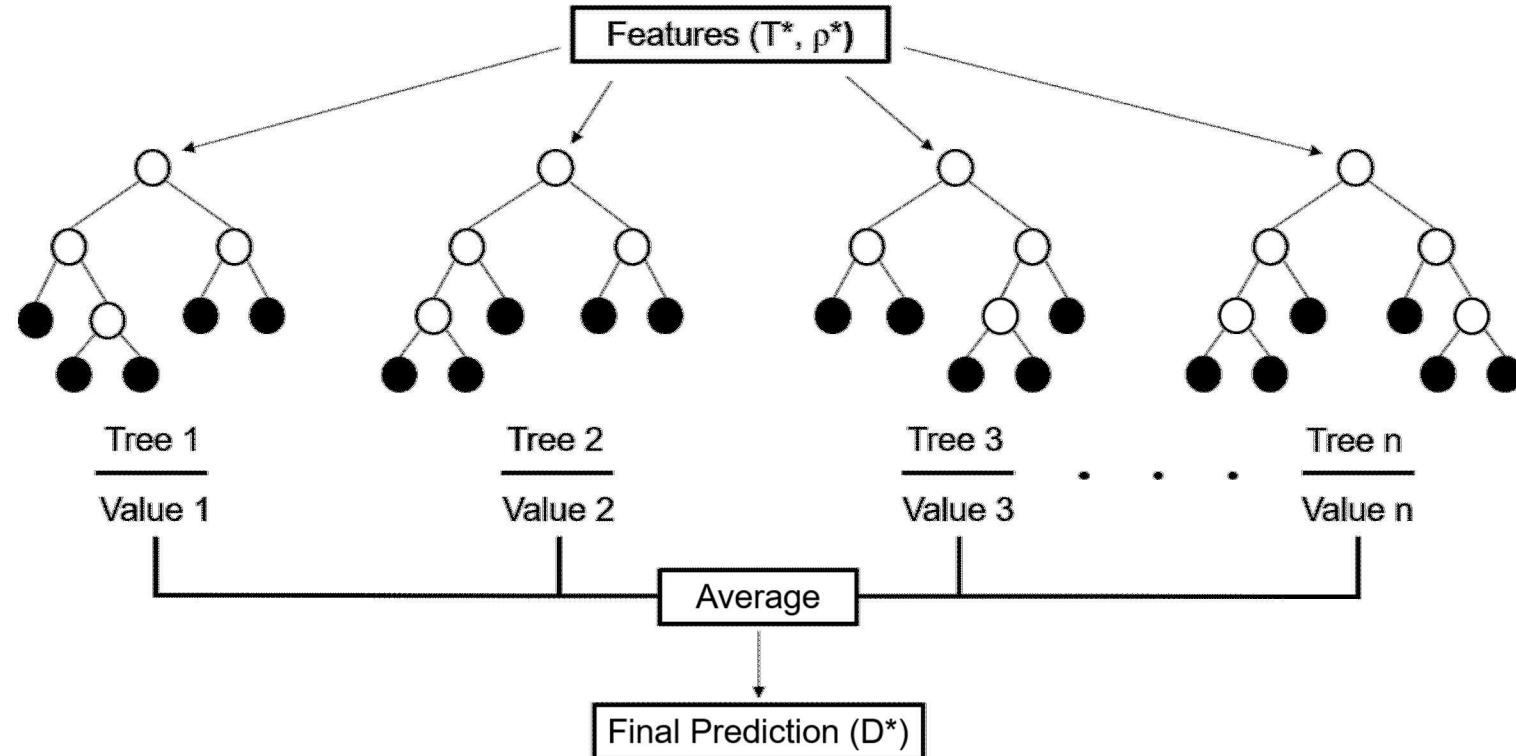
Upper limit of Zhu's Dataset



Joshua P. Allers, Jacob A. Harvey, Fernando H. Garzon, Todd M.  
 "Machine learning prediction of self-diffusion in Lennard Jones fl  
 Chem. Phys. 153, 034102 (2020).



# Random Forest Architecture

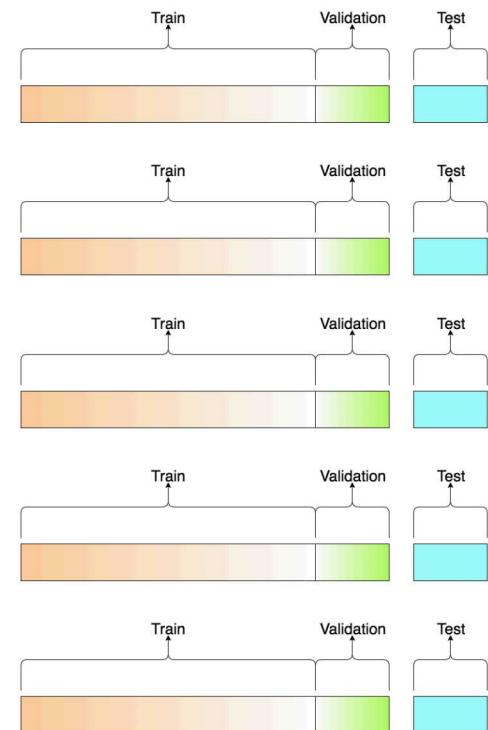
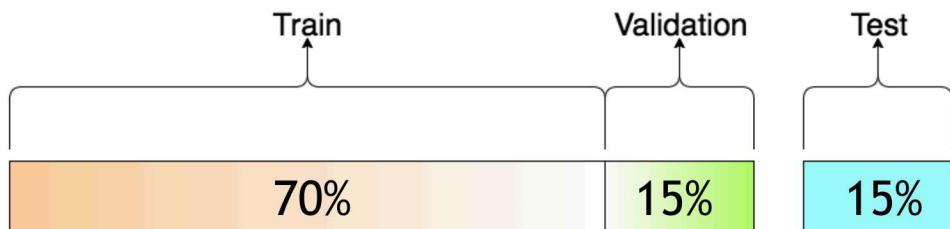


- Software: Python Scikit-Learn
- Optimal number of trees: 235



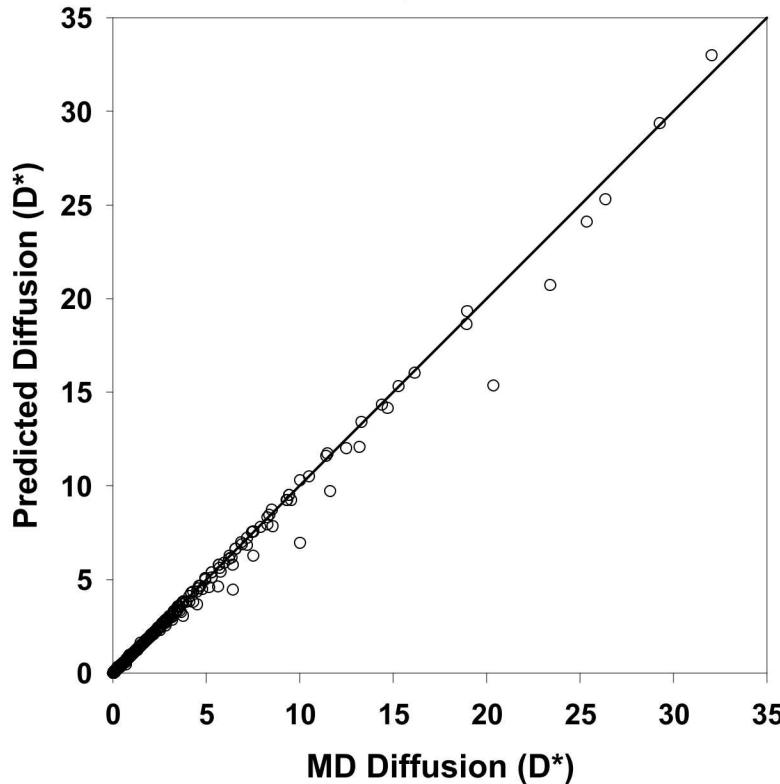
# Performance Assessed with Cross Validation (CV)

- Splits dataset in even train/validate/test sets
  - ML models train on the 70%
  - Validation set used to adjust hyperparameters (model parameters)
  - Test set gave final predictive power
- 5 different splits of the data
  - Randomly divided
- Performance metrics:
  - Mean Square Error (MSE)
  - Correlation Coefficient (R)

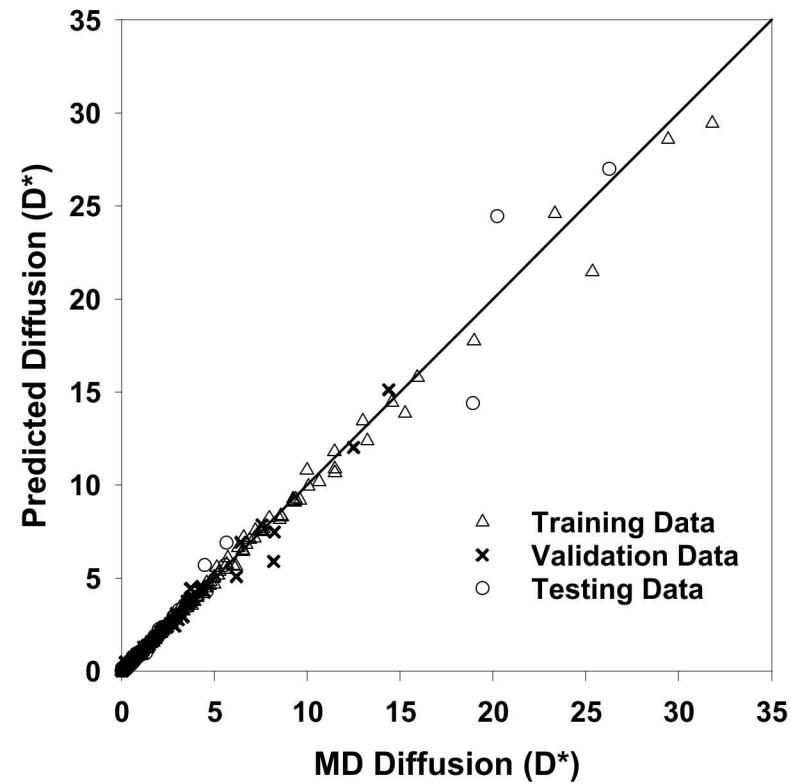


# Performance of Random Forest

Zhu's Empirical Model



Random Forest

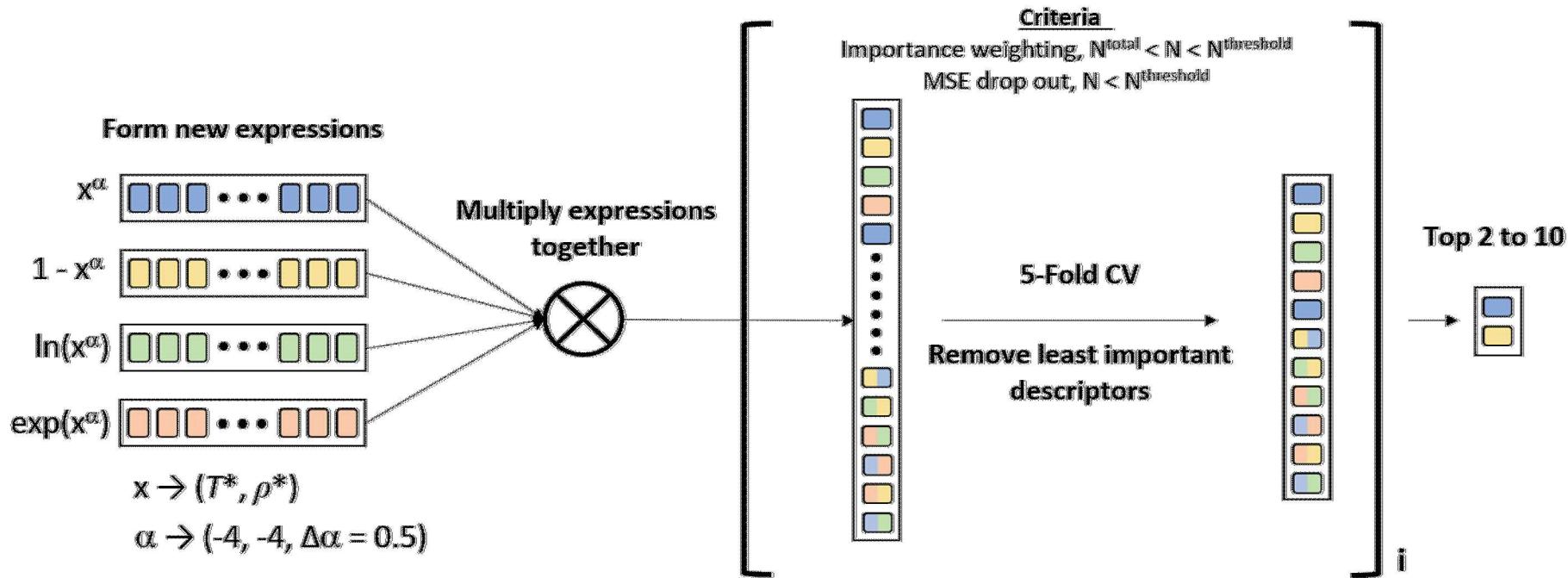


Model	Zhu	RF
Mean MSE	0.067	0.18
Std. Dev.	$\pm 0.077$	$\pm 0.21$
Mean R	0.99685	0.99624

Joshua P. Allers, Jacob A. Harvey, Fernando H. Garzon, Todd M. Alam. "Machine learning prediction of self-diffusion in Lennard Jones fluids." *J Chem. Phys.* 153, 034102 (2020).



# Feature Engineering Process



**Solo**  
 $f(T^*)$  or  $f(\rho^*)$   
128 Features

e.g.  $\ln(T^*)$

**Binary**  
 $f(T^*) * g(\rho^*)$   
4224 Features

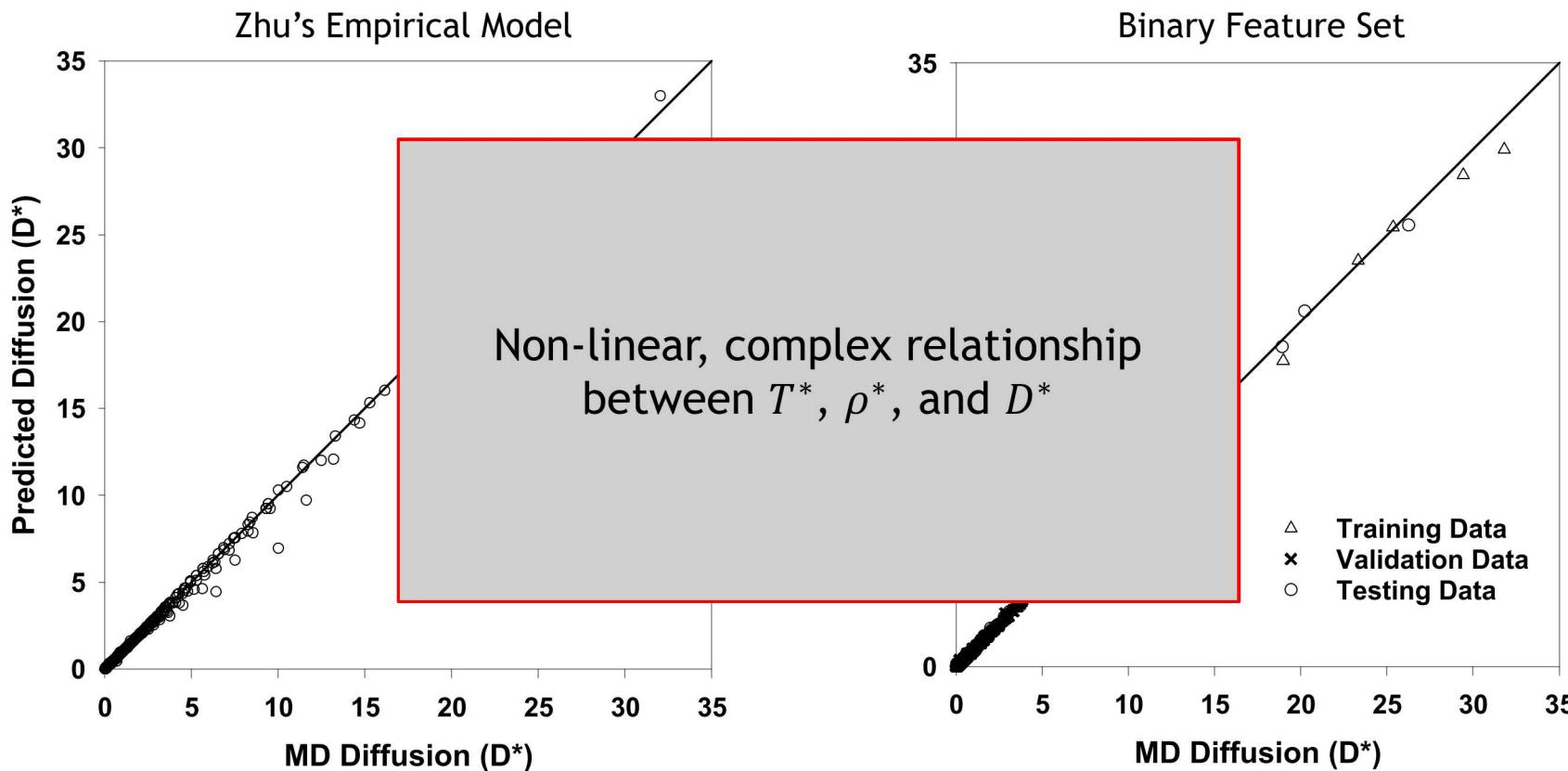
e.g.  $\ln(T^*) * \exp(\rho^*)$

**Self-Binary**  
 $f(T^*) * g(T^*)$   
7296 Features

e.g.  $\ln(T^*) * \exp(T^*)$



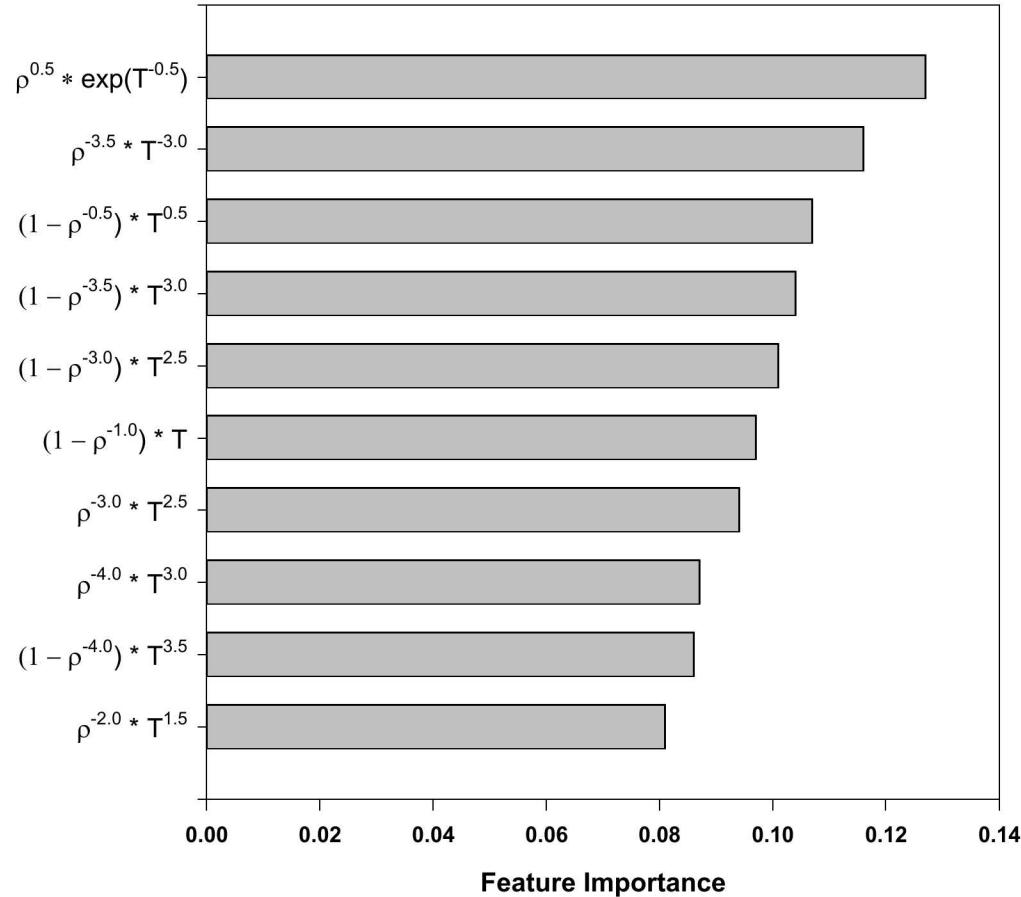
# Random Forest with Feature Engineering



Model	Zhu	RF	Solo	Binary	Self-Binary
Mean MSE	0.067	0.18	0.15	0.052	0.047
Std. Dev.	$\pm 0.077$	$\pm 0.21$	$\pm 0.18$	$\pm 0.047$	$\pm 0.072$
Mean R	0.99685	0.99624	0.99642	0.99913	0.99912



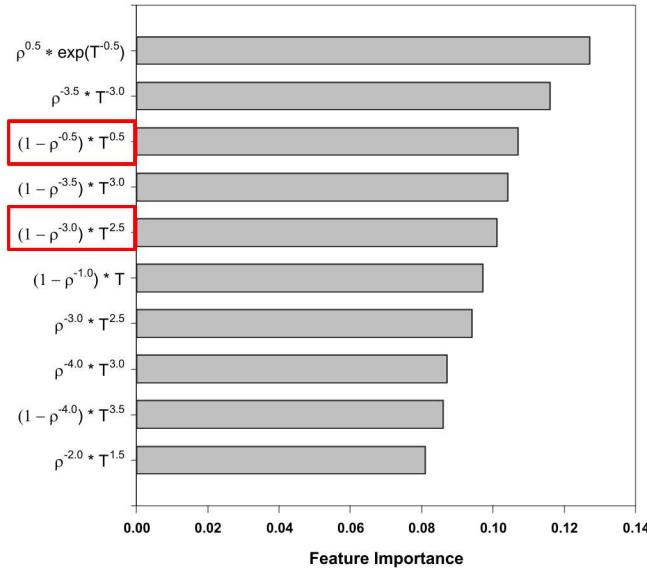
# Most Important Features – Binary Feature Set



**Observed trend:** non-linear functions of  $T^*$  and  $\rho^*$  consistently show up as the most important features



# Most Important Features – Binary Feature Set



Continued iteration →

Top 2 Features

$$(1 - \rho^{-0.5}) * T^{0.5}$$

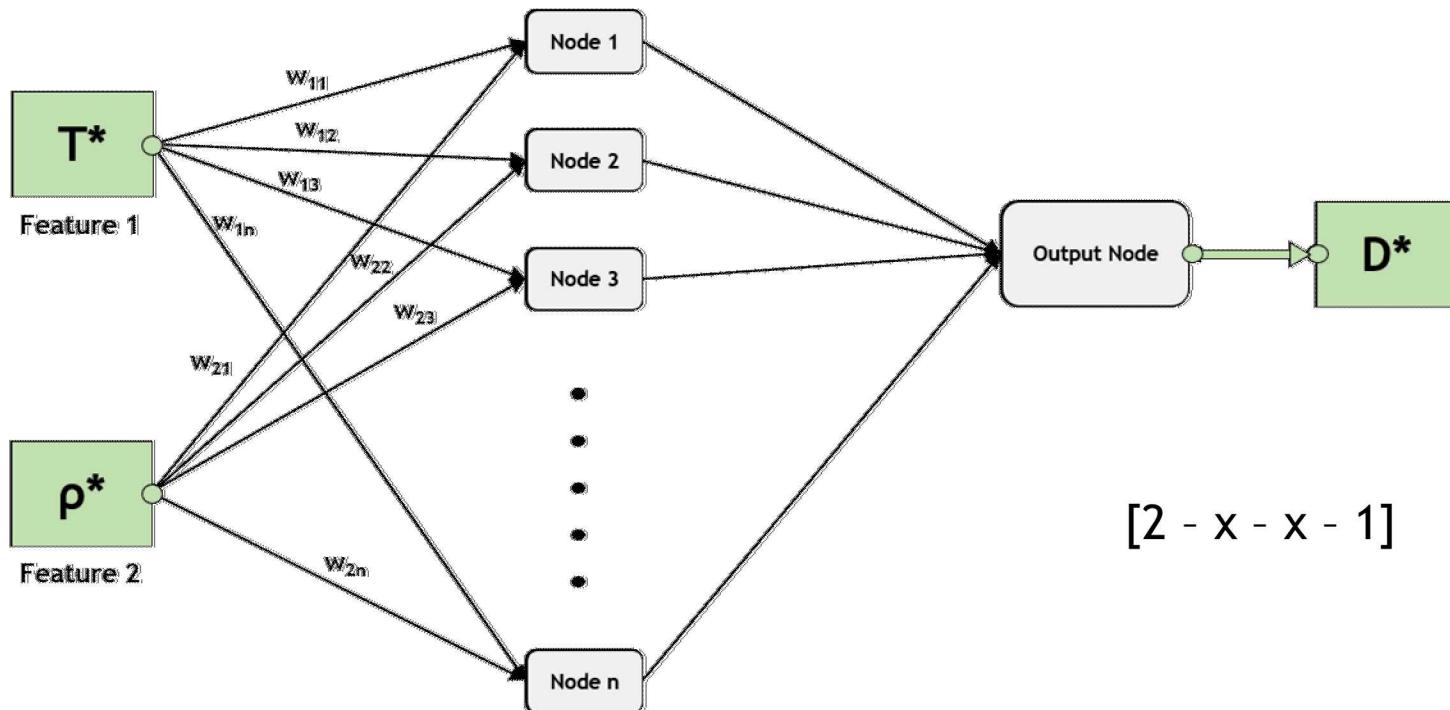
$$(1 - \rho^{-3.0}) * T^{2.5}$$

3<sup>rd</sup> and 5<sup>th</sup> ranked features become the top 2



# Artificial Neural Network (ANN) Architecture

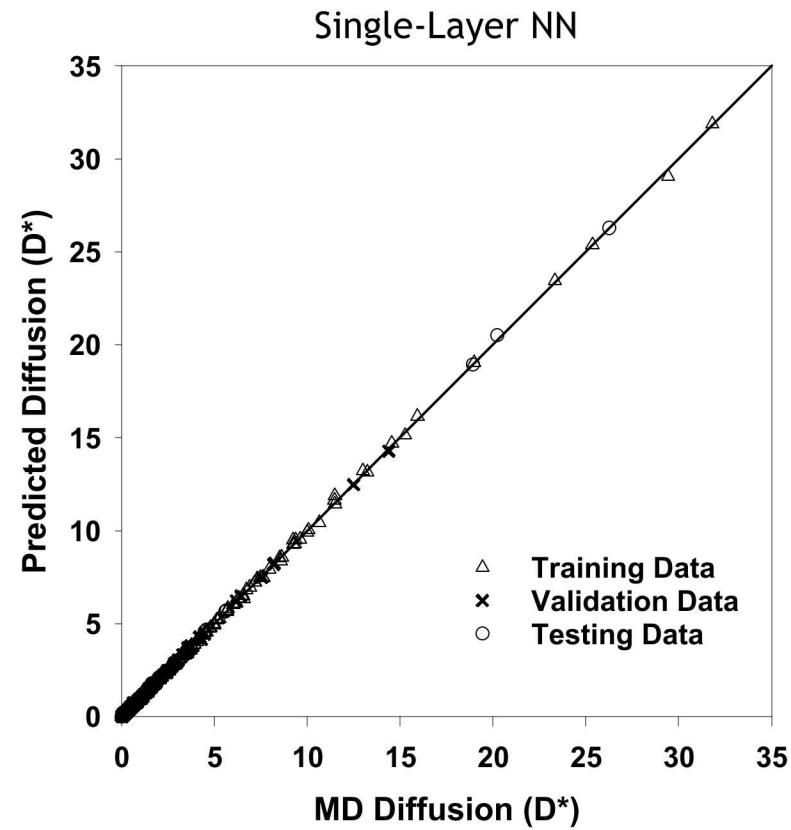
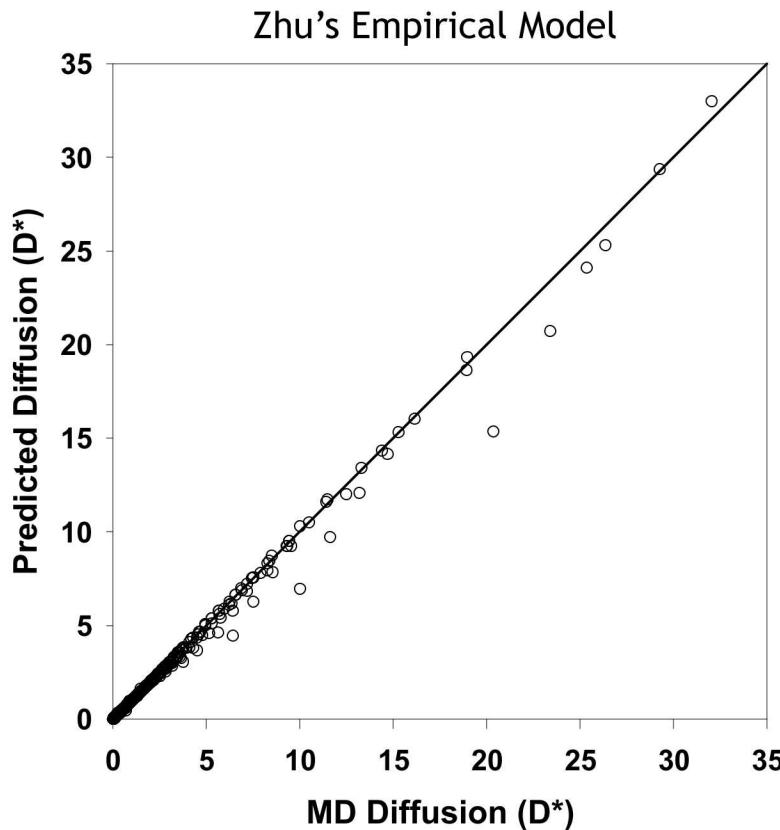
Input                      Hidden Layer                      Output Layer              Output



- Software: MATLAB Deep Learning Toolbox



# Neural Network Performance



Model	ANN(2-14-12-1)	ANN(2-14-1)	RF-FE	Zhu	RF
Mean MSE	0.00012	0.0016	0.052	0.067	0.18
Std. Dev.	$\pm 0.0009$	$\pm 0.001$	0.047	$\pm 0.077$	$\pm 0.21$
Mean R	0.99994	0.99991	0.99913	0.99685	0.99624



# Conclusions

- Machine learning improved upon existing empirical relationships in LJ system
- Random Forest with  $T^*$  and  $\rho^*$  performed worse than Zhu's equation
- Employed feature engineering, which improved predictions
  - On par with Zhu's equation
  - Pointed to non-linear, complex relationships
- Artificial Neural Networks provide the best predictions
  - Will be used going forward with real systems

## Ongoing Work

- Machine Learning extended to sets of binary LJ fluids
- Artificial Neural Networks assessed on a dataset of pure solutions
  - Shows excellent performance over multiple compounds and phases



# Acknowledgements



**Todd Alam (SNL Advisor)**

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**Calen Leverant (SNL)**

**Thank you for your attention - Questions?**

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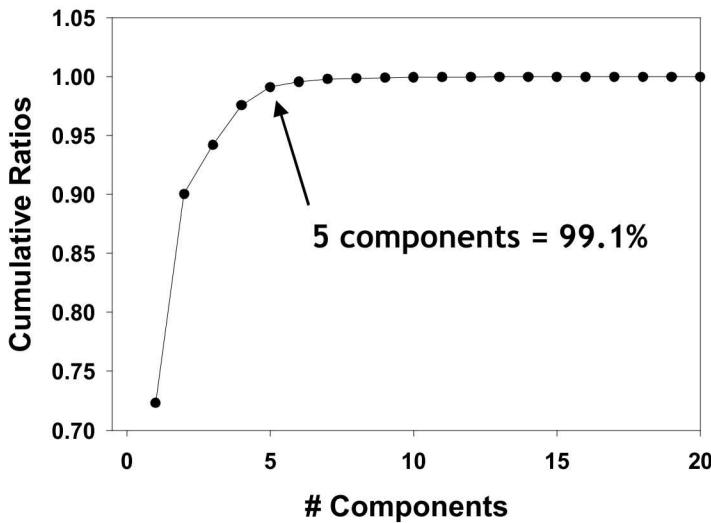
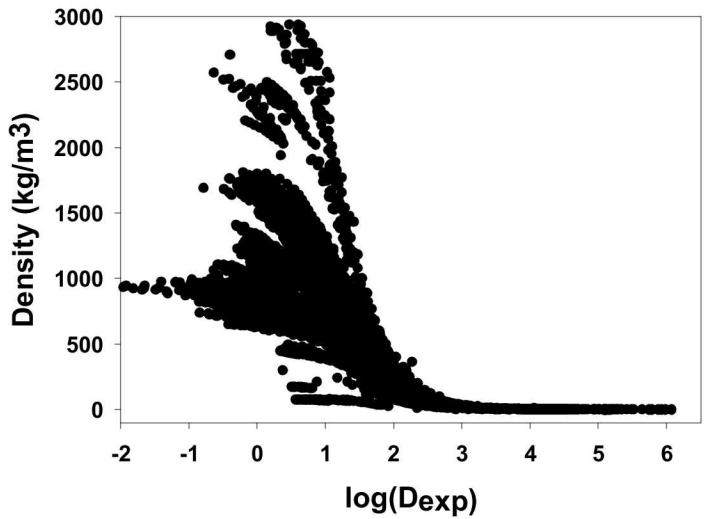
*Project funding through the Sandia LDRD program*



# Additional Slides

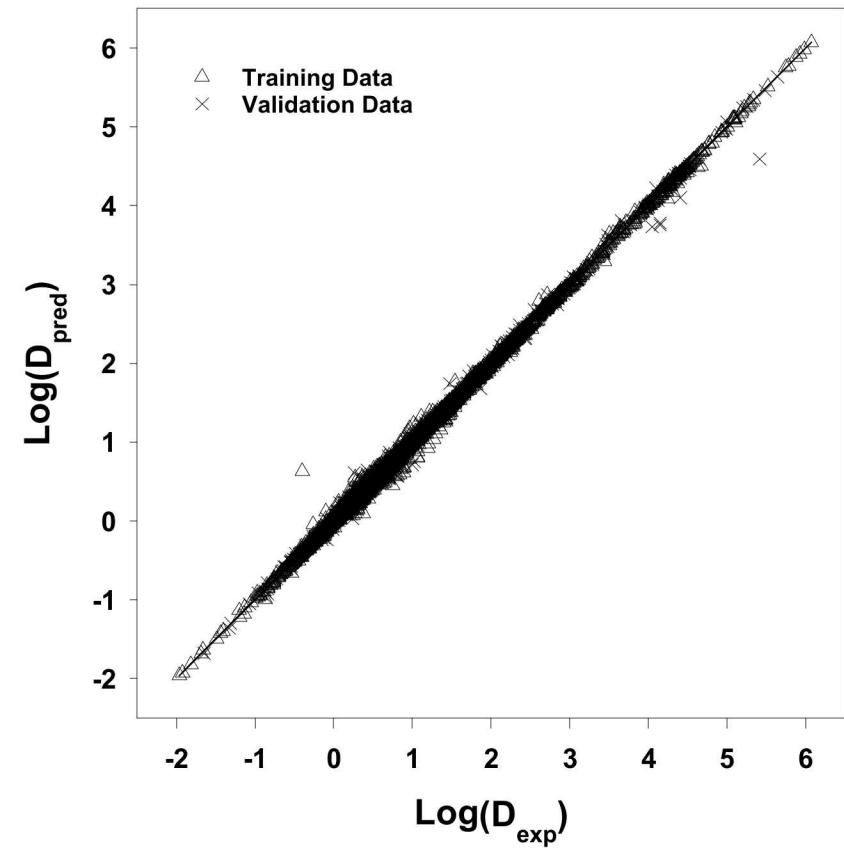


# Current Work – Pure Solutions Diffusion



- 6252 points from a wide range of compounds
  - Multiple phases present
- 24 features were collected including:
  - Critical properties
  - Experimental properties
  - Phase information
  - Structural information
- Principal Component Analysis (PCA) used to reduce the dimensionality

# Current Work – Pure Solution Diffusion



- Models are robust and generalized over a 5-fold cross-validation
- Shows good predictions over multiple phases