

Anomalous Shapiro steps in a Dirac semimetal Cd₃As₂-based SQUID

Joseph J. Cuozzo

Technical supervisor: Wei Pan

2020 Intern Symposium
August 7th, 2020

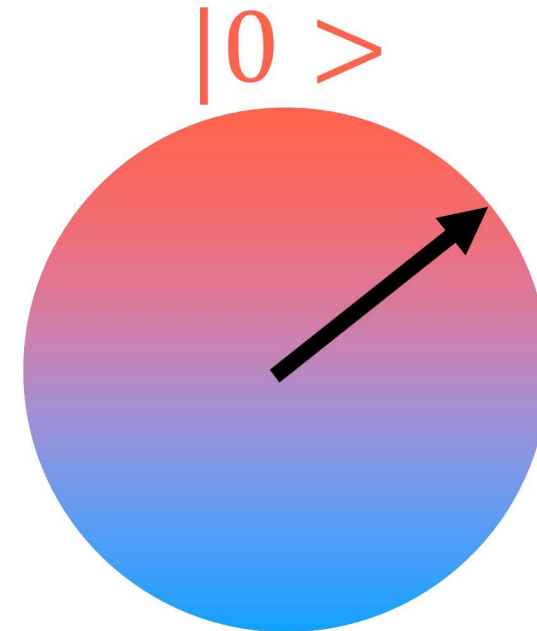
Quantum computing

0

Classical bit

1

Qubit



$$\alpha|0\rangle + \beta|1\rangle$$

Big issue: Decoherence

Can we protect our qubit from the environment?

PSPACE

Efficiently solved

Efficiently solved
by classical computers

ng
break
key cryptography
schemes!

Motivation

PHYSICAL REVIEW X **6**, 031016 (2016)

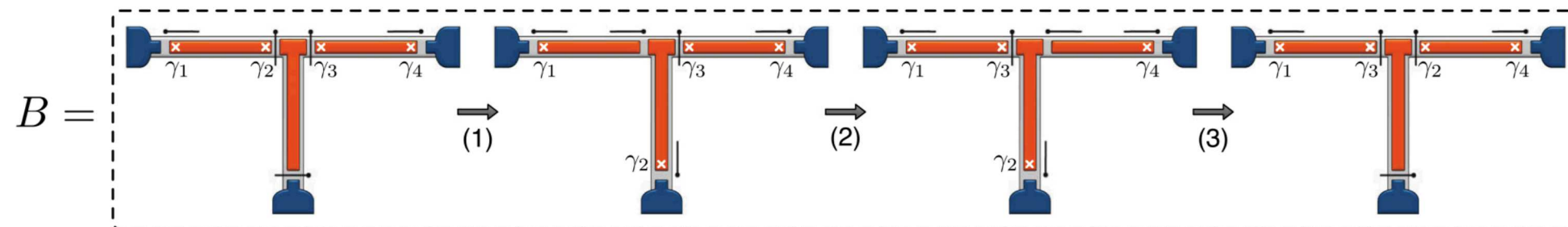
Milestones Toward Majorana-Based Quantum Computing

David Aasen,¹ Michael Hell,^{2,3} Ryan V. Mishmash,^{1,4} Andrew Higginbotham,^{5,3} Jeroen Danon,^{3,6} Martin Leijnse,^{2,3}
Thomas S. Jespersen,³ Joshua A. Folk,^{3,7,8} Charles M. Marcus,³ Karsten Flensberg,³ and Jason Alicea^{1,4}

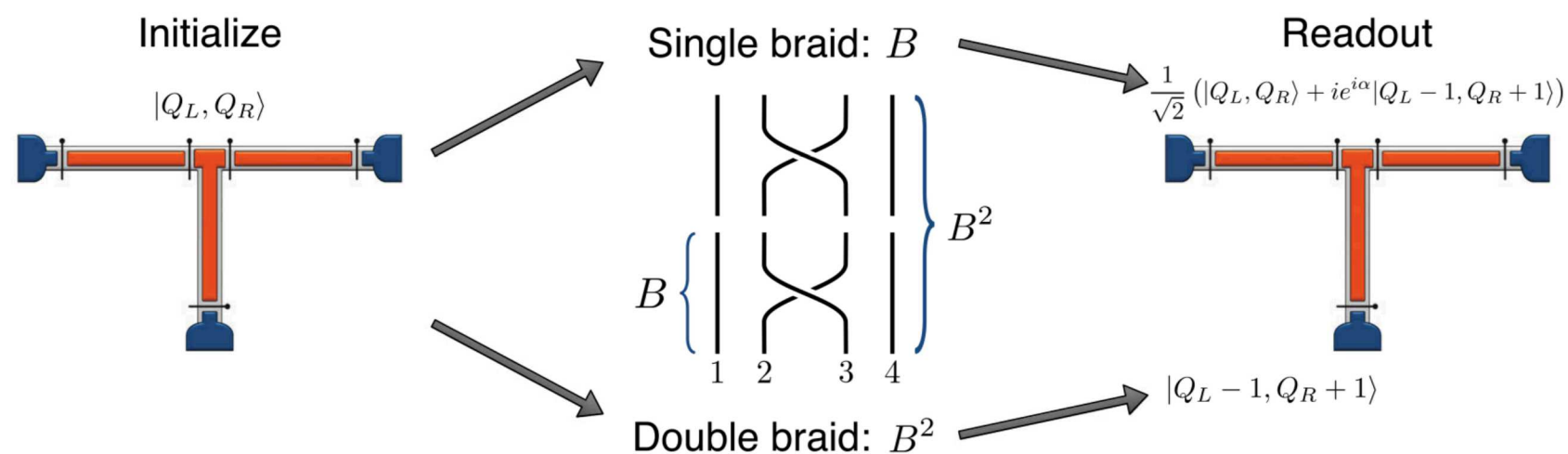
Non-Abelian anyons and topological quantum computation

Chetan Nayak, Steven H. Simon, Ady Stern, Michael Freedman, and Sankar Das Sarma
Rev. Mod. Phys. **80**, 1083 – Published 12 September 2008

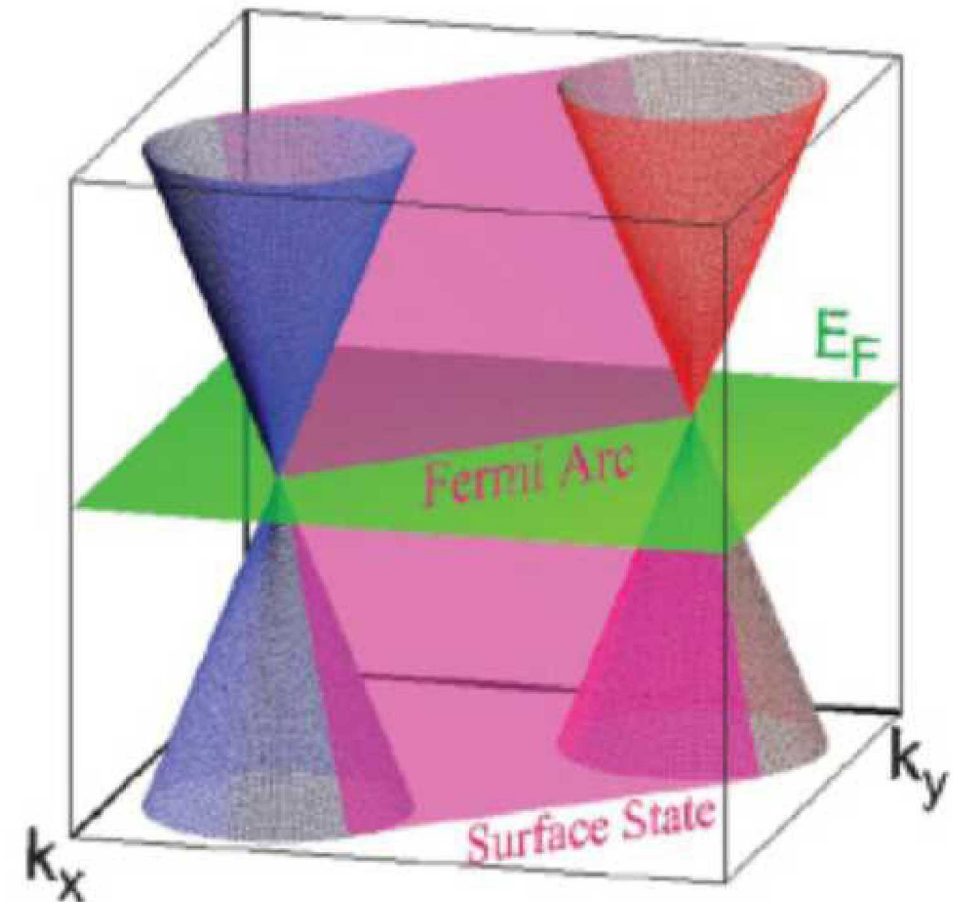
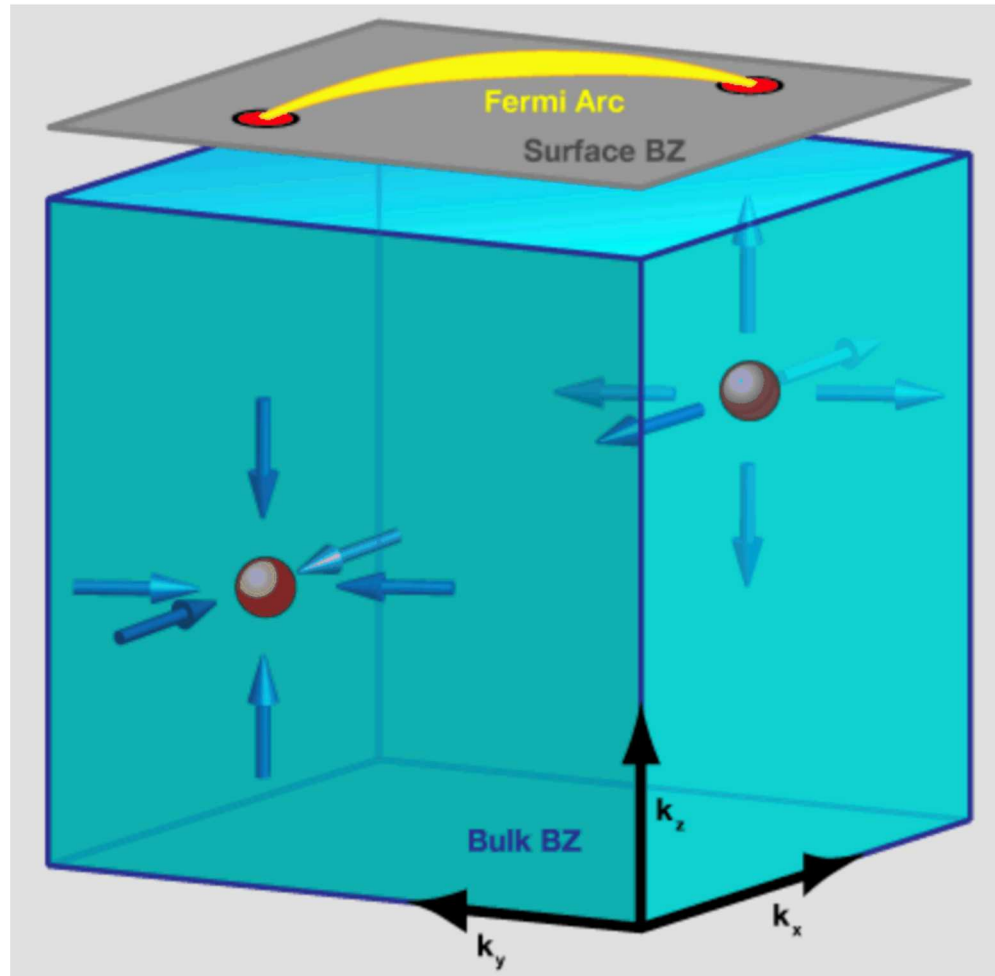
(a) Basic braiding operation



(b) Full protocols: Single and double braid



Dirac & Weyl Semimetals



PHYSICAL REVIEW B **95**, 174505 (2017)

Josephson current signatures of Majorana flat bands on the surface of time-reversal-invariant Weyl and Dirac semimetals

Anffany Chen,^{1,2} D. I. Pikulin,^{1,2,3} and M. Franz^{1,2}

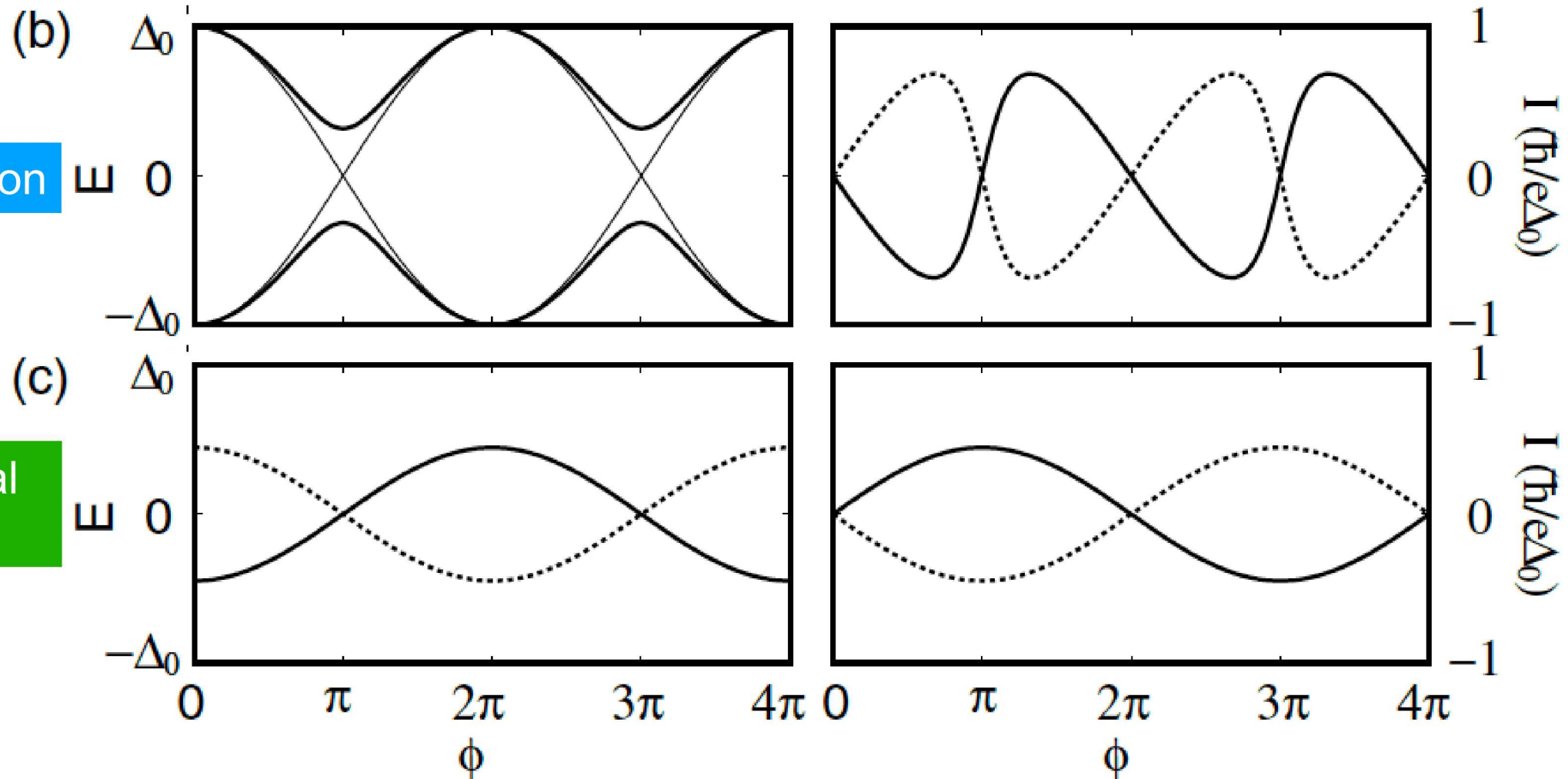
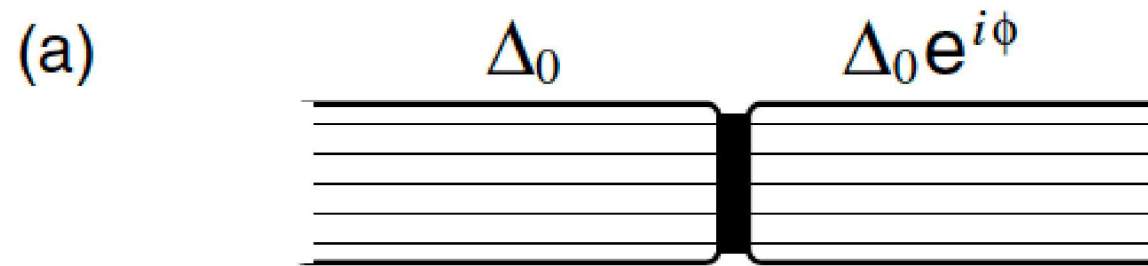
¹Department of Physics and Astronomy, University of British Columbia, Vancouver, BC, Canada V6T 1Z1

²Quantum Matter Institute, University of British Columbia, Vancouver, BC, Canada V6T 1Z4

³Station Q, Microsoft Research, Santa Barbara, California 93106-6105, USA

(Received 26 October 2016; revised manuscript received 13 March 2017; published 8 May 2017)

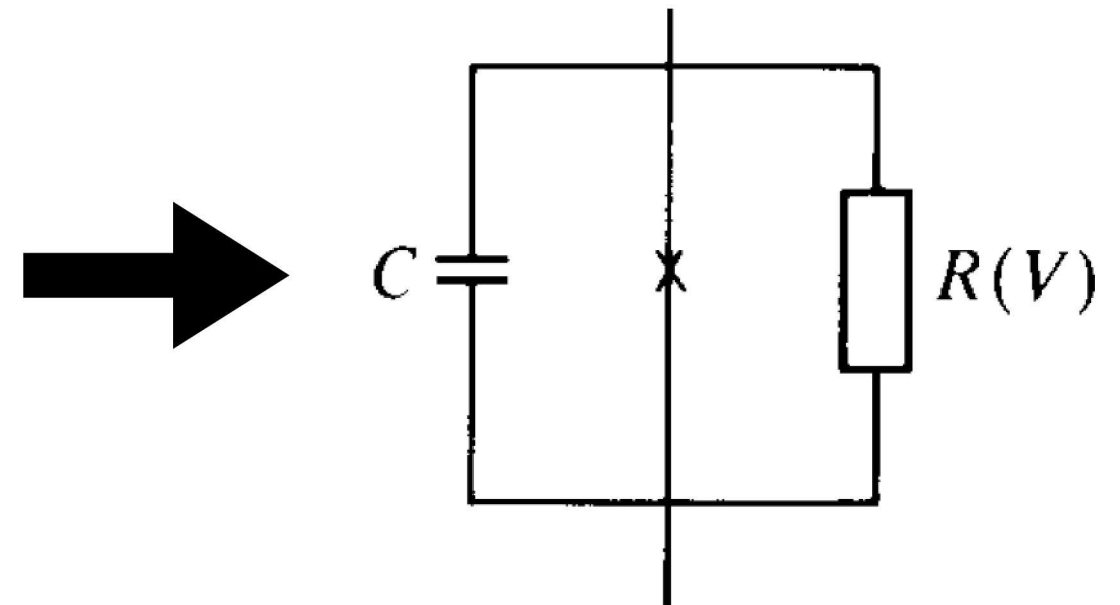
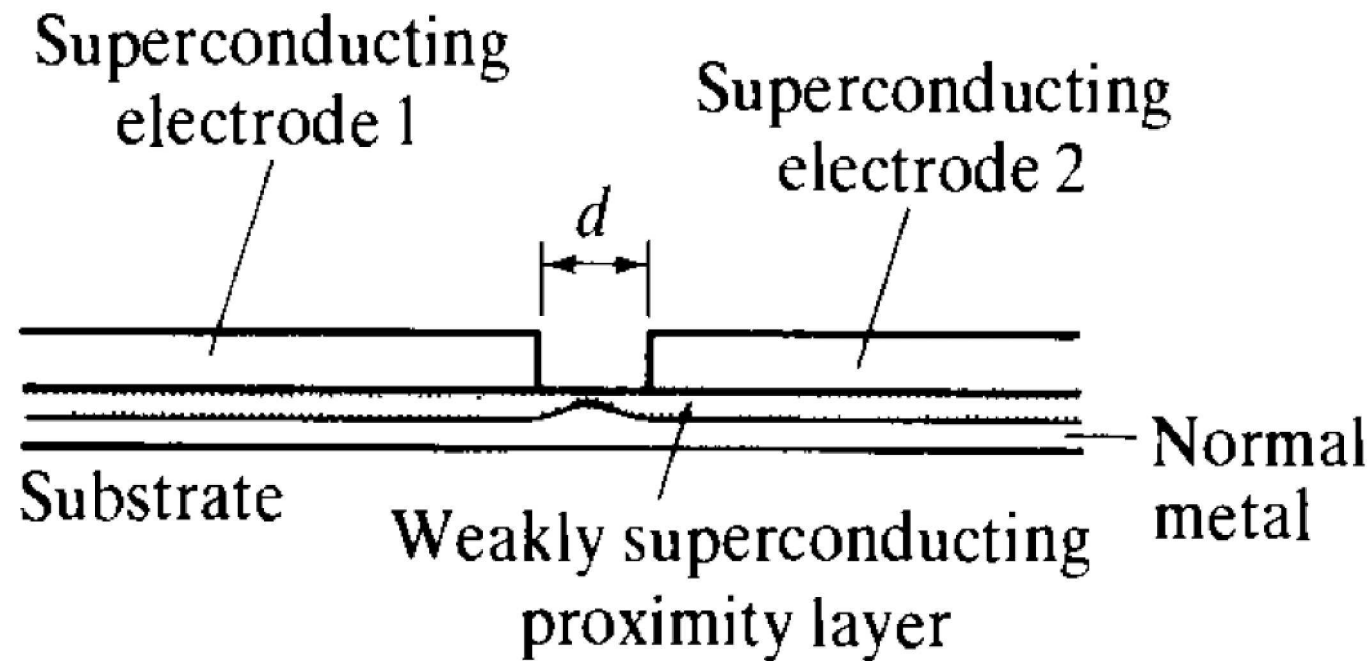
Josephson Effect



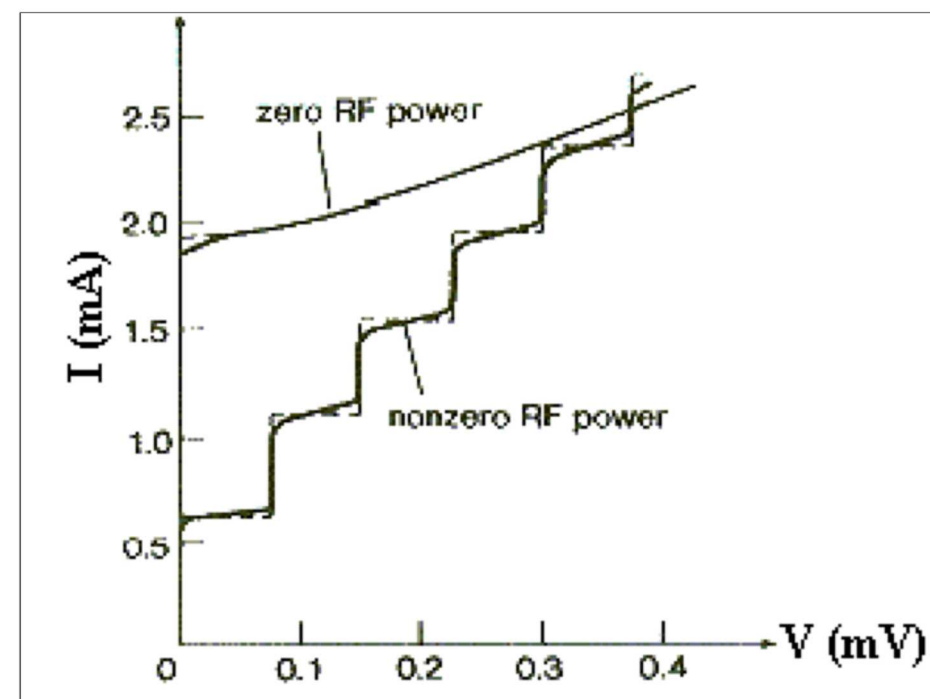
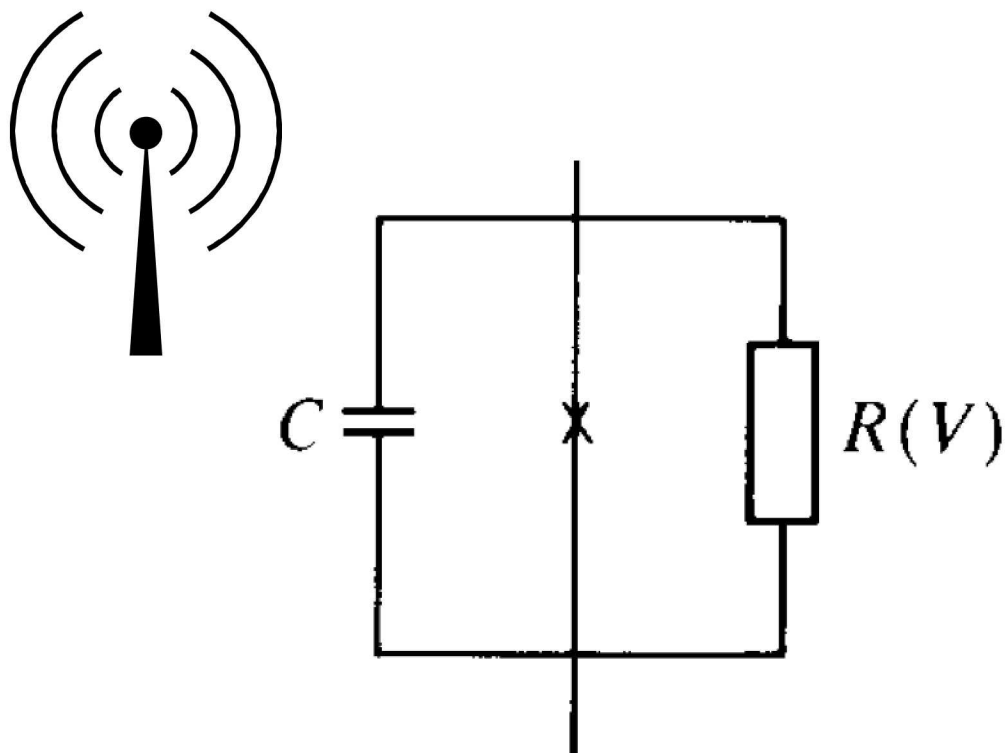
For a short junction and $T=0$:

$$I = \frac{2e}{\hbar} \sum_{mid-gap E_n} \frac{\partial E_n}{\partial \phi}$$

Shapiro Steps

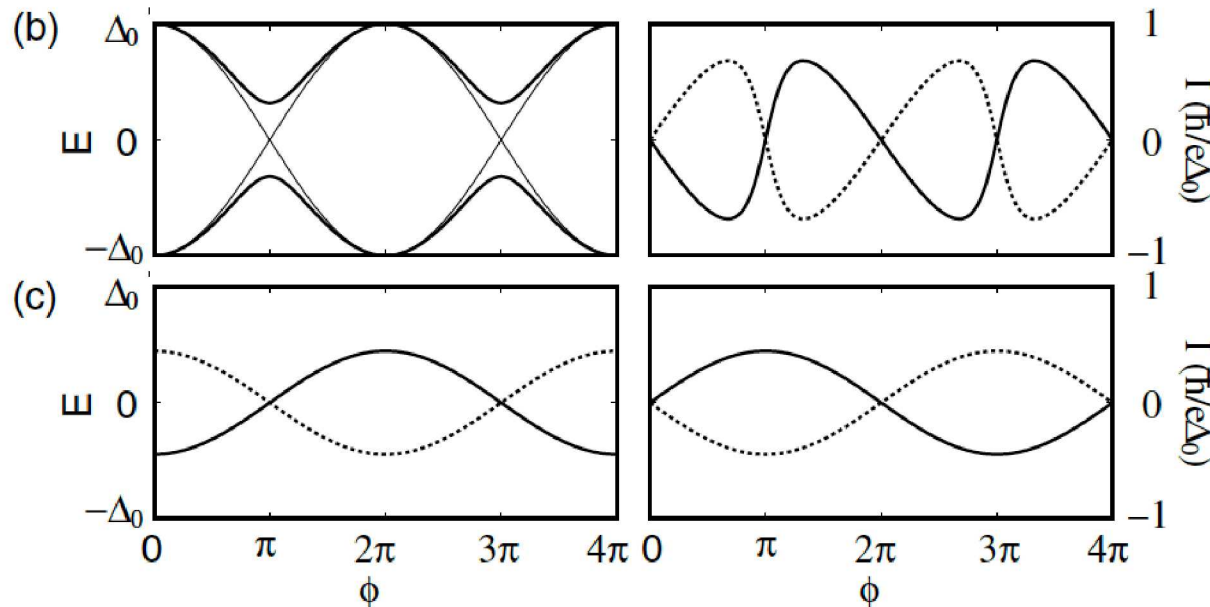
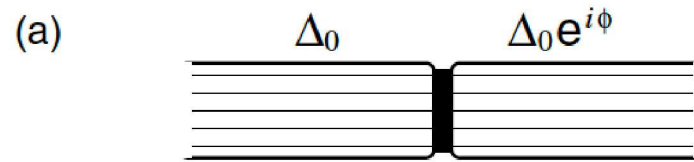
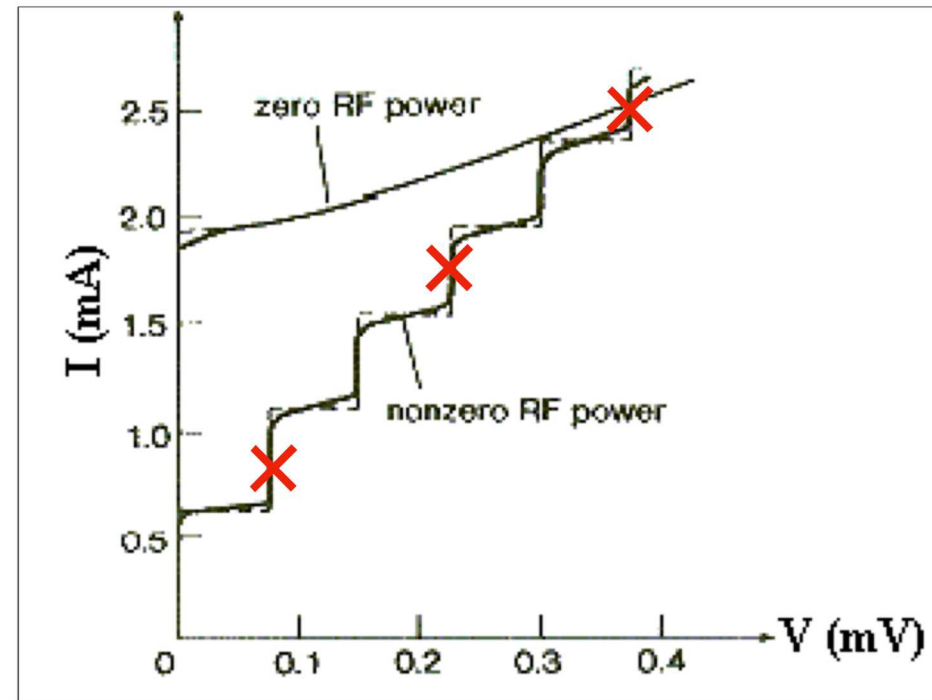
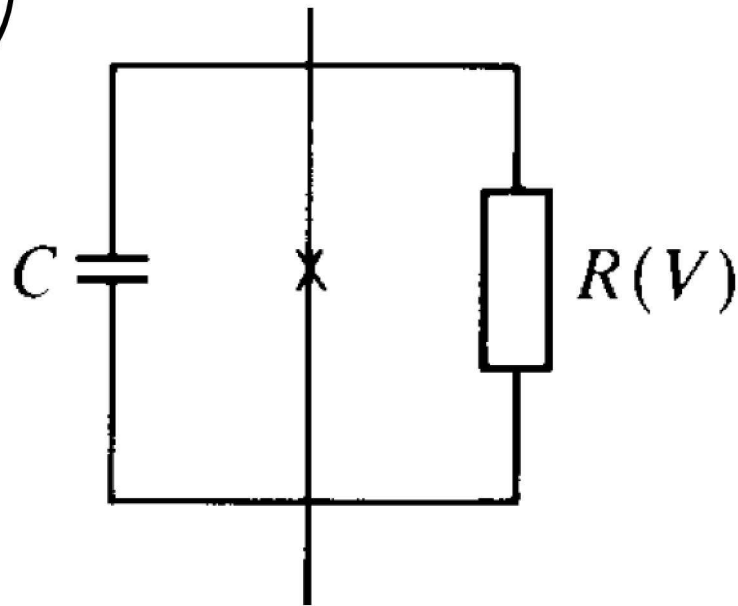


$$I_{bias} = I_s + \frac{V}{R} + C \frac{dV}{dt}$$



$$V_n = n \frac{\hbar \omega}{2e}$$

Topological Superconductivity



Trivial junction

Topological junction

$$V_n = n \frac{\hbar\omega}{2e} \quad \text{Supercurrent carried by a pair of electrons}$$

$$V_n = n \frac{\hbar\omega}{e} = (2n) \frac{\hbar\omega}{2e} \quad \text{Supercurrent carried by single electrons}$$

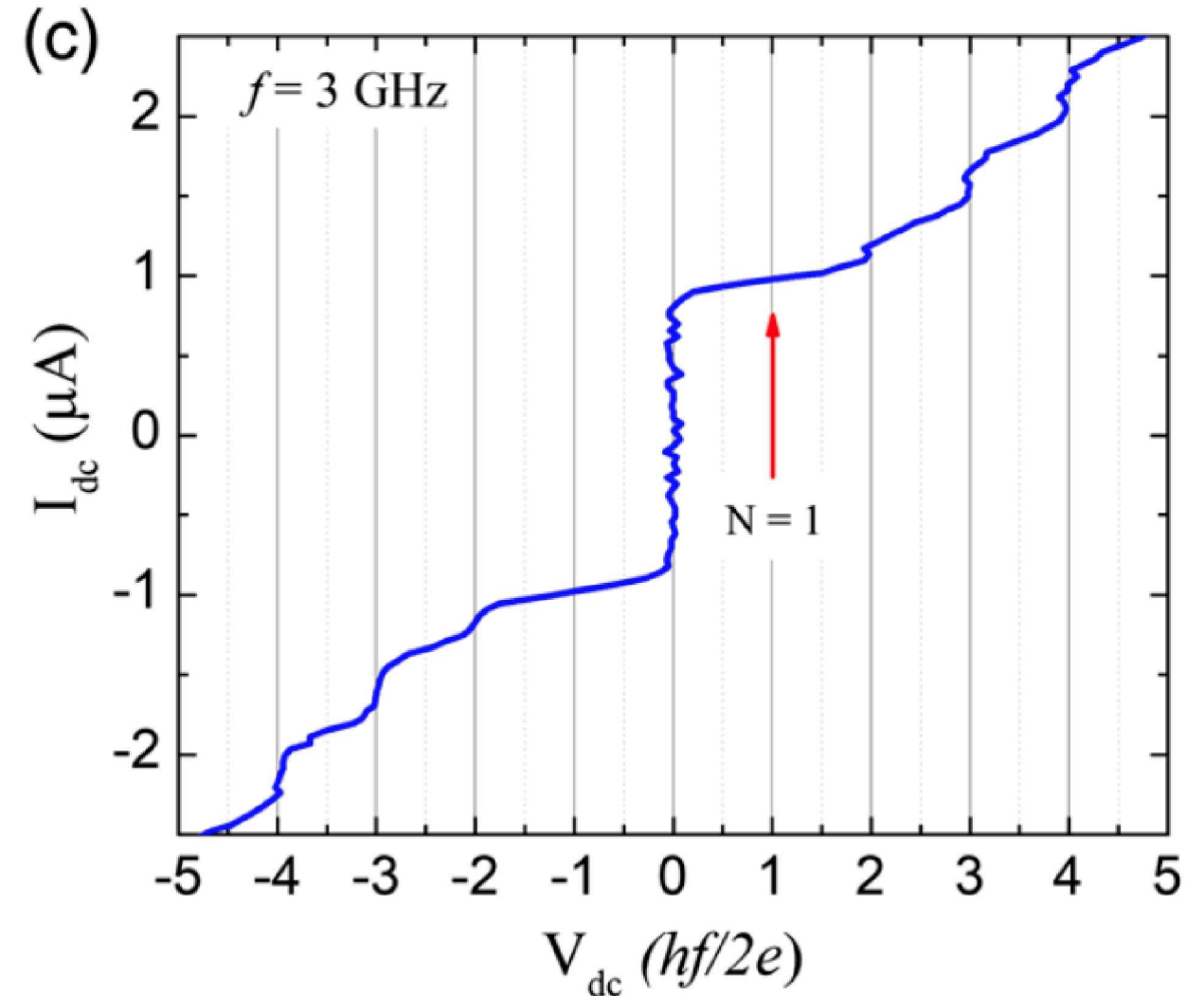
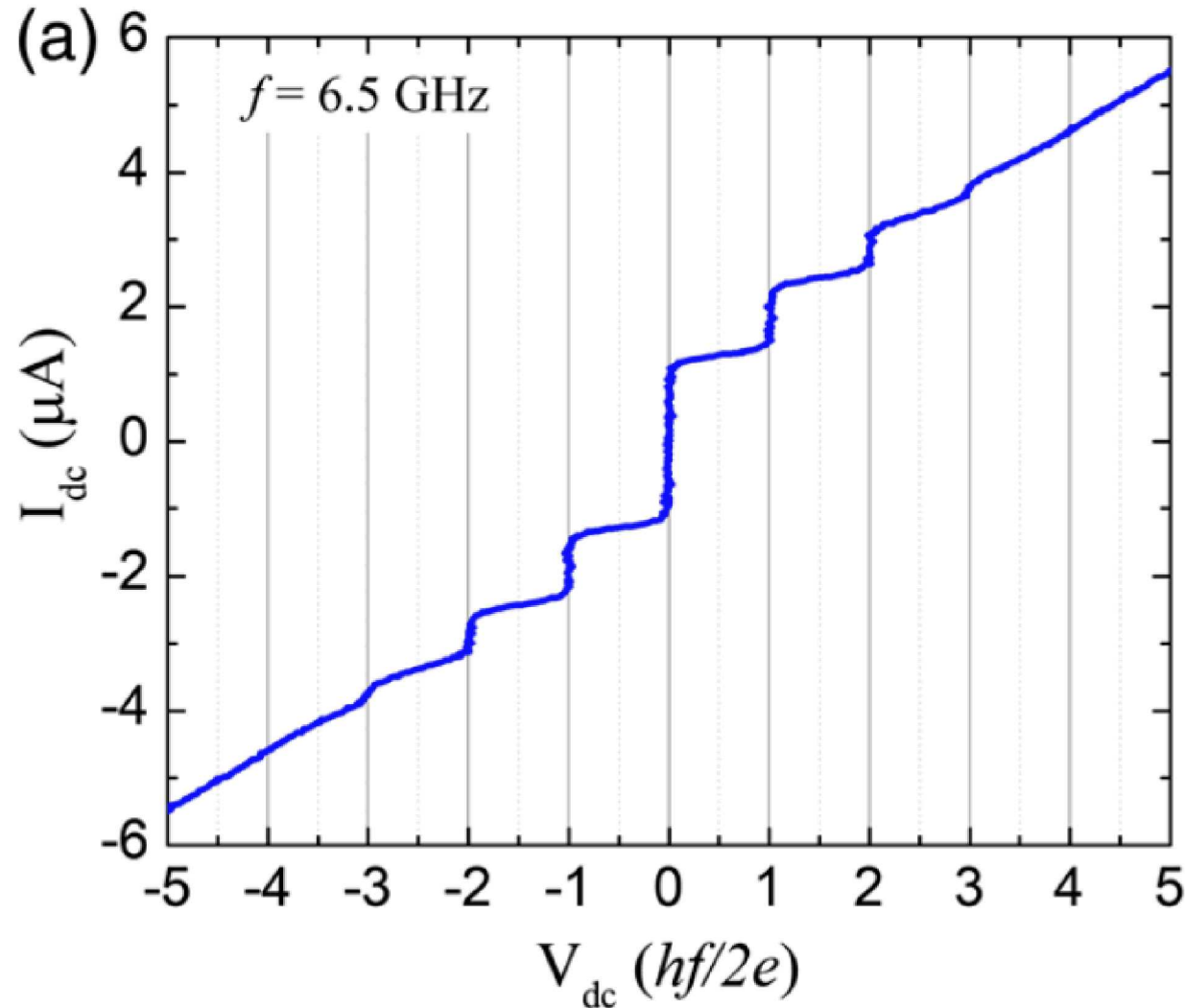
π and 4π Josephson Effects Mediated by a Dirac Semimetal

W. Yu,¹ W. Pan,¹ D. L. Medlin,² M. A. Rodriguez,¹ S. R. Lee,¹ Zhi-qiang Bao,³ and F. Zhang³

¹*Sandia National Laboratories, Albuquerque, New Mexico 87185, USA*

²*Sandia National Laboratories, Livermore, California 94551, USA*

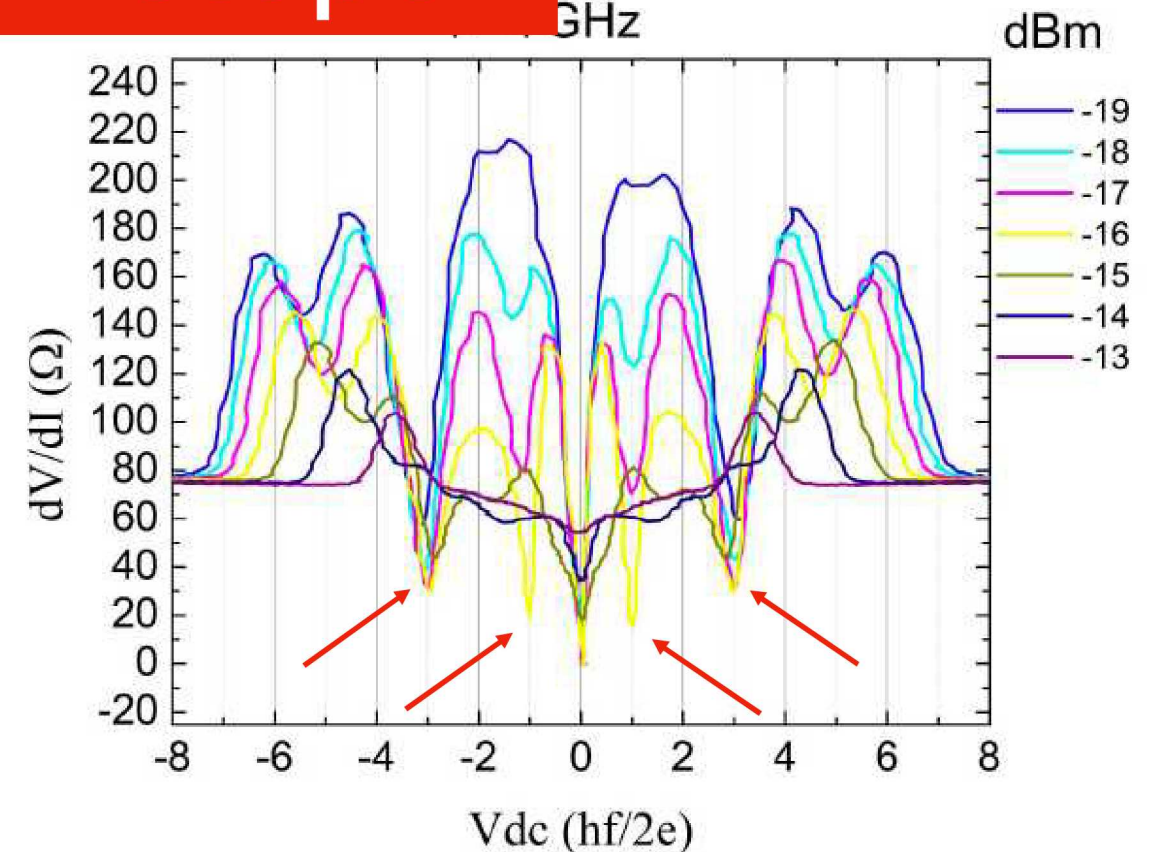
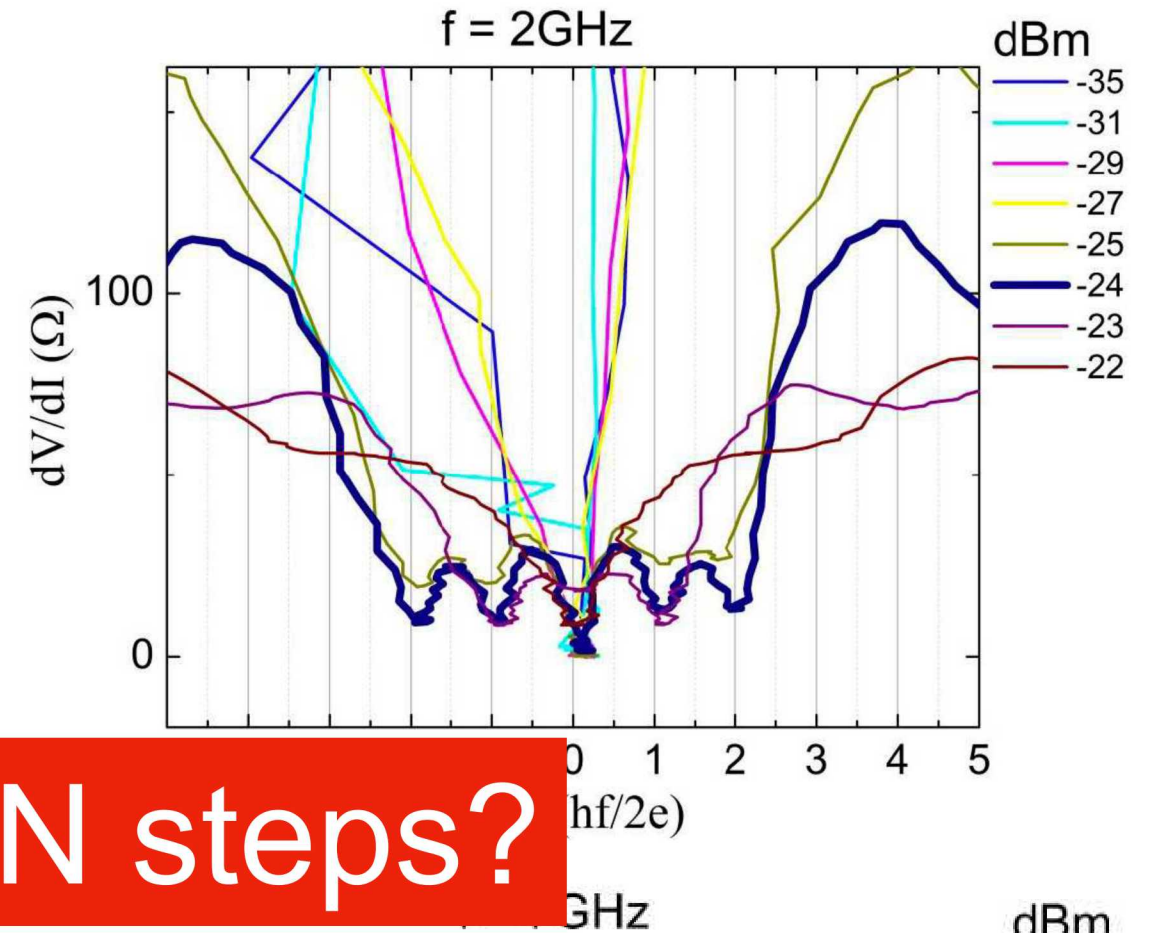
³*Department of Physics, University of Texas at Dallas, Dallas, Texas 75080, USA*



Anomalous Shapiro Steps

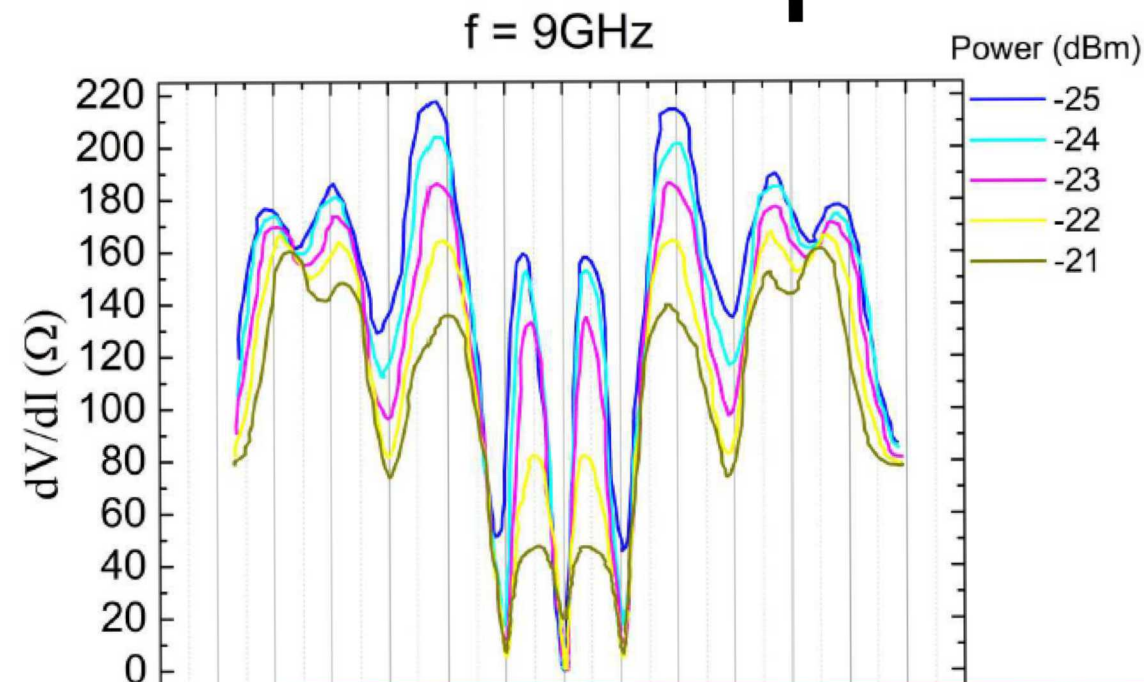


Missing EVEN steps?

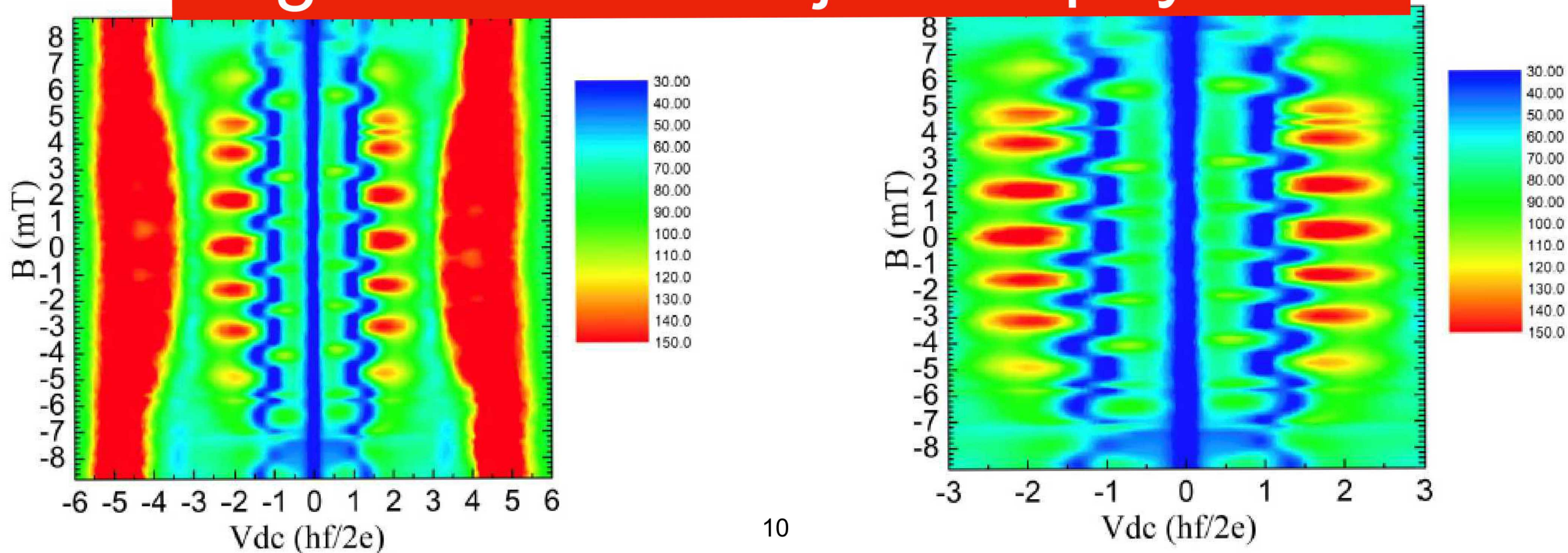


At a Shapiro step: $R = \frac{dV}{dI} = 0$

Anomalous Shapiro Steps



Signatures of Majorana physics?

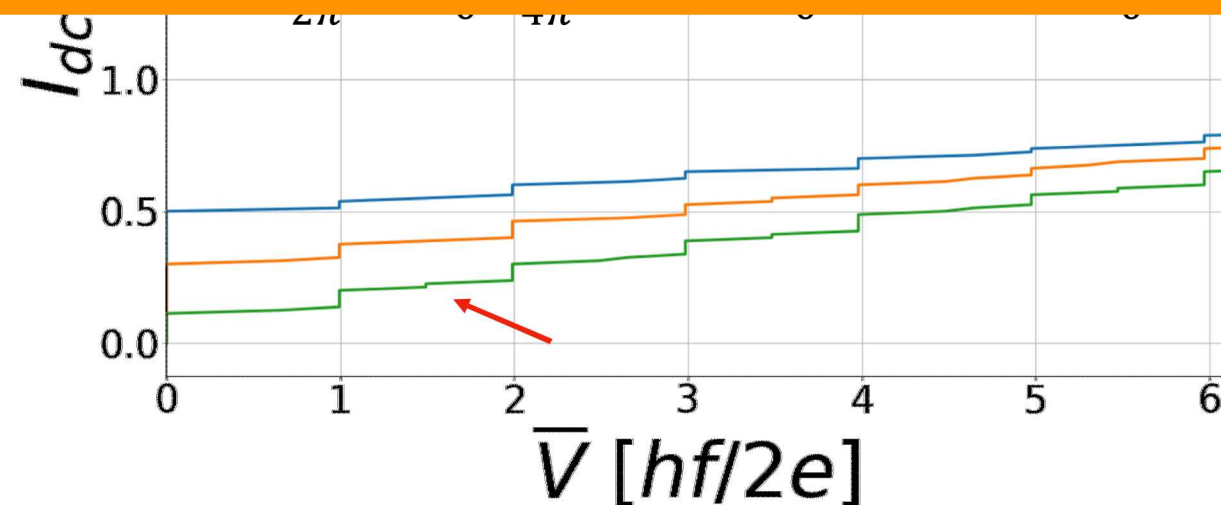


Shapiro Steps in Symmetric SQUID

Fail to observe suppressed even steps with most basic description of supercurrent channels

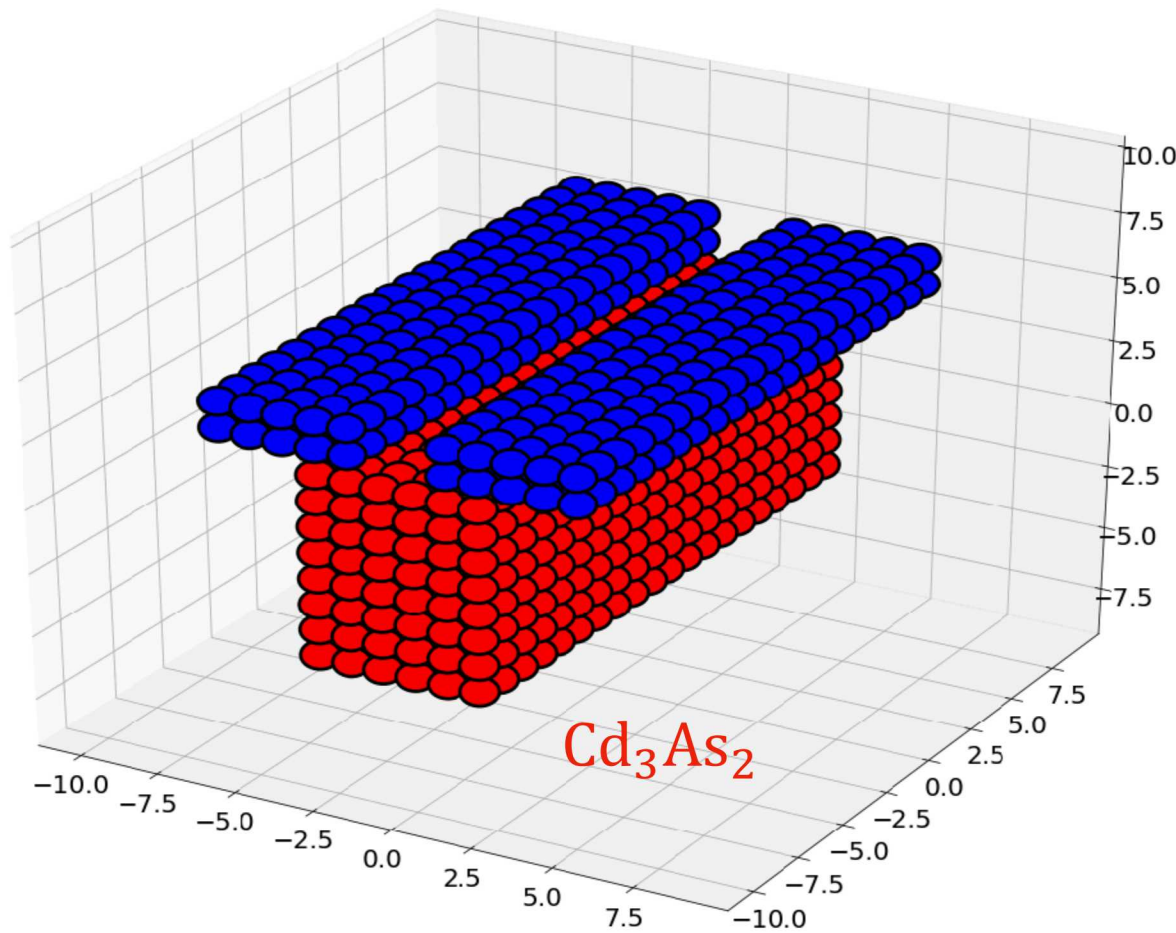


Let's take a step back and re-evaluate the model for the supercurrent channel

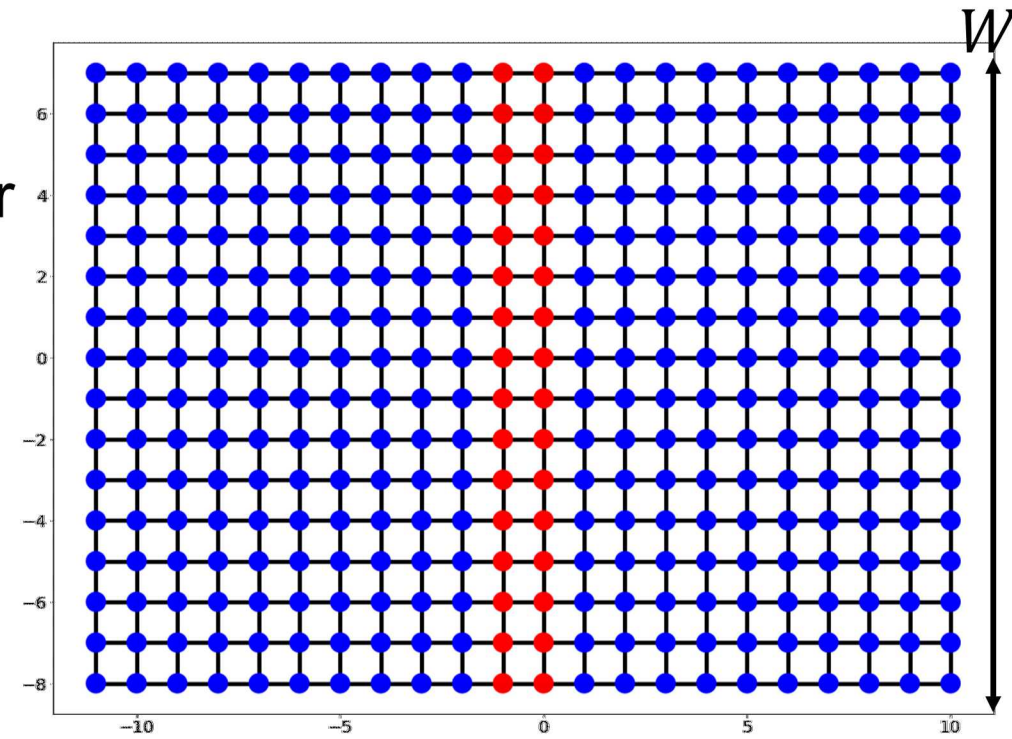
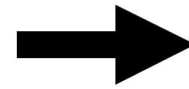


Observe 1/2 step and suppressed 1/2 step, as seen in experiment

Tight-binding Simulations



Reduce
dimensionality for
simplicity

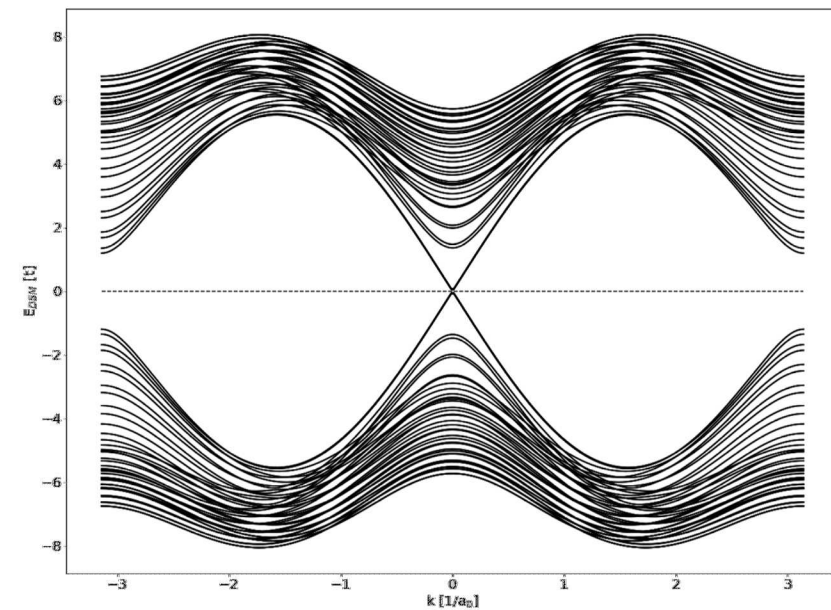


$$H_{dsm}(\vec{k}) = \epsilon(\vec{k})s_0 \otimes \sigma_0 + M(\vec{k})s_0 \otimes \sigma_z + A_0(k_x s_z \otimes \sigma_x - k_y s_0 \otimes \sigma_y)$$

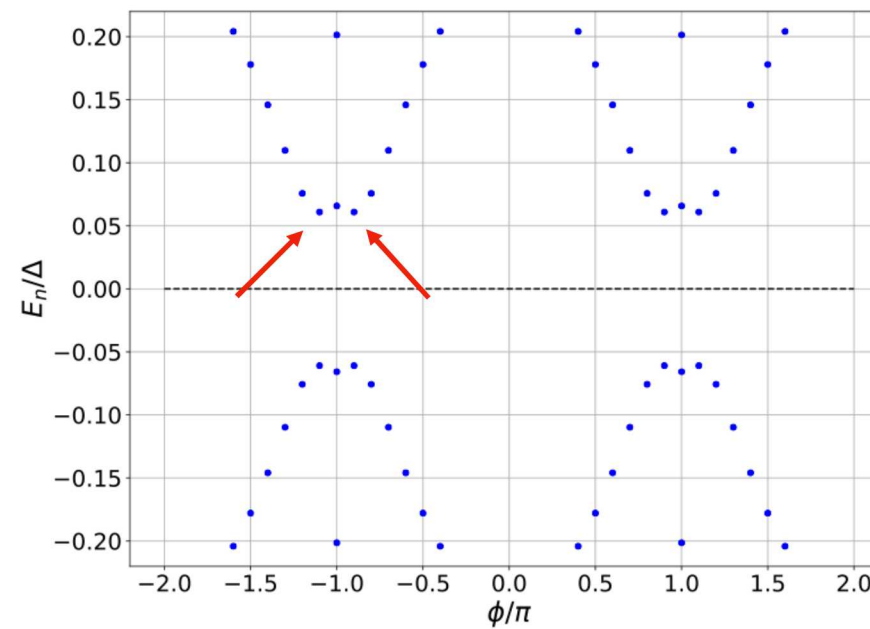
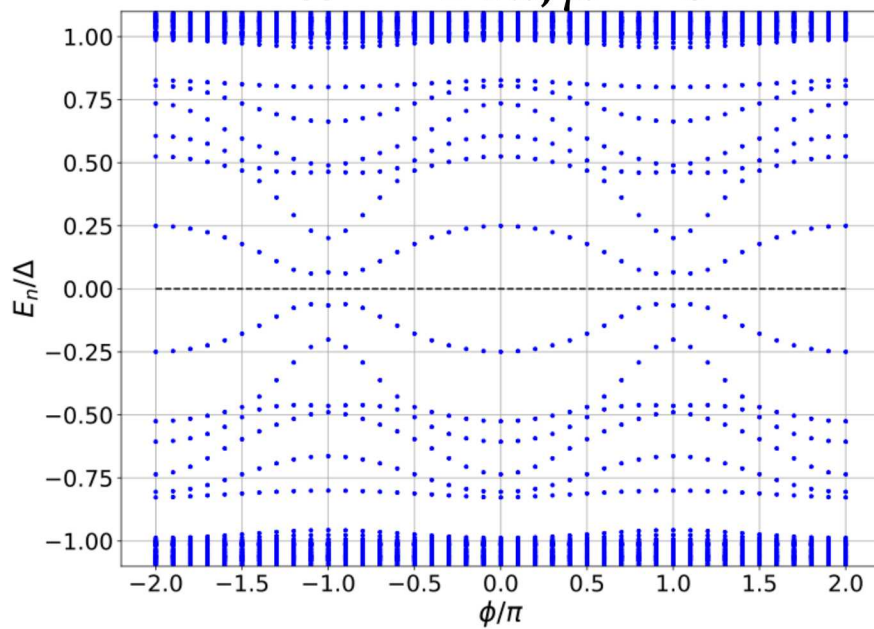
$$\epsilon(\vec{k}) = C_0 - \mu + 2C_1 k_z^2 + 2C_2(k_x^2 + k_y^2)$$

$$M(\vec{k}) = M_0 - 2M_1 k_z^2 - 2M_2(k_x^2 + k_y^2)$$

$$s_i \rightarrow \text{spin} \quad \sigma_i \rightarrow \text{orbital}$$

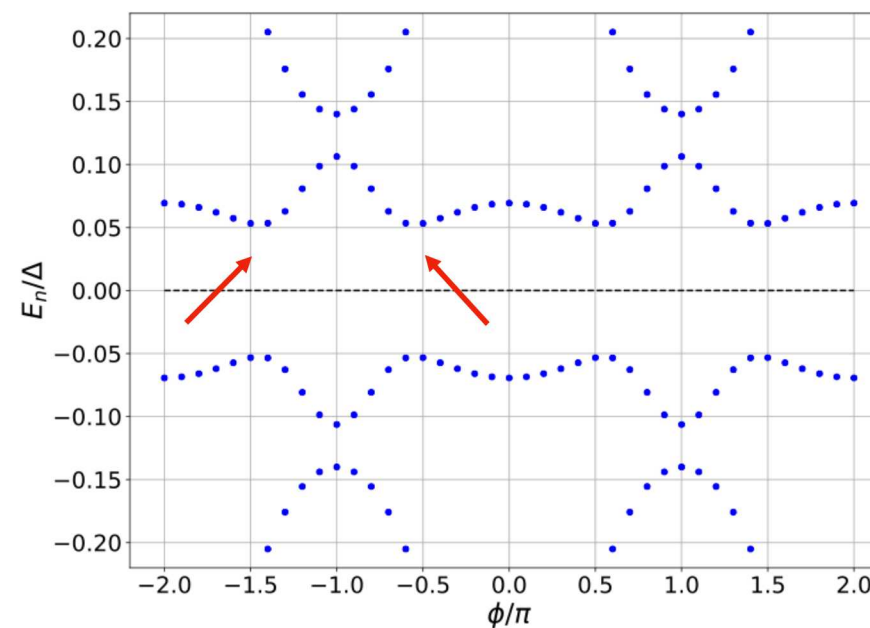
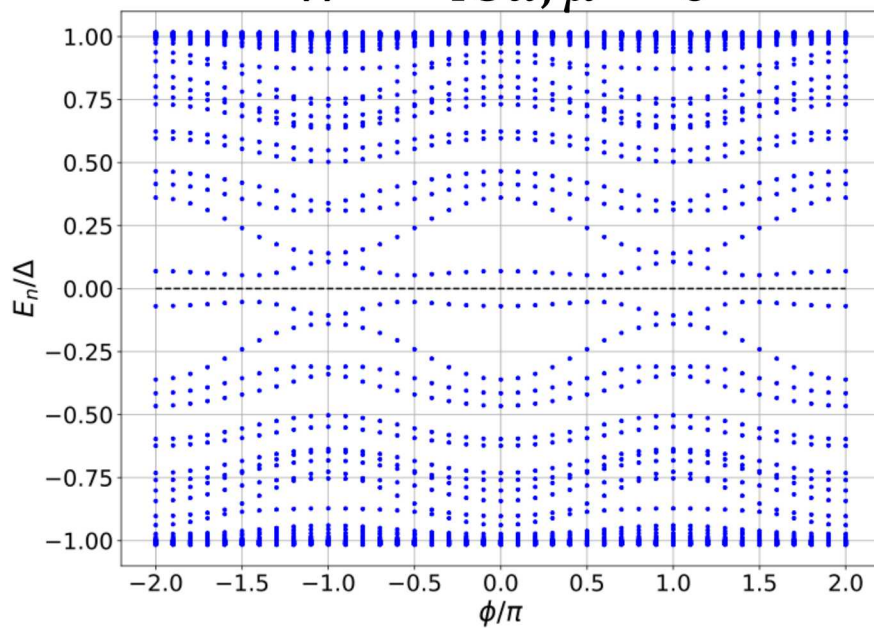


$$W = 24a, \mu = 0$$



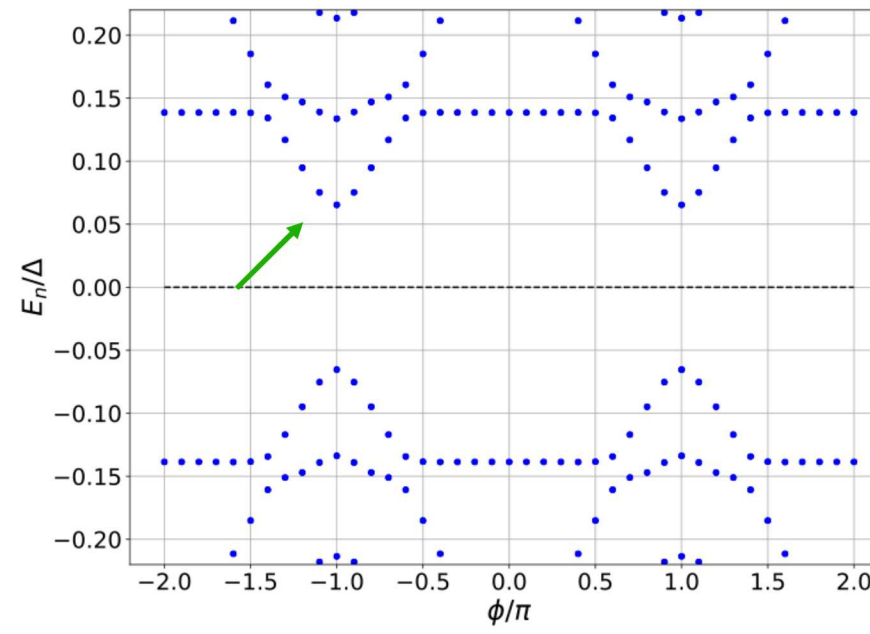
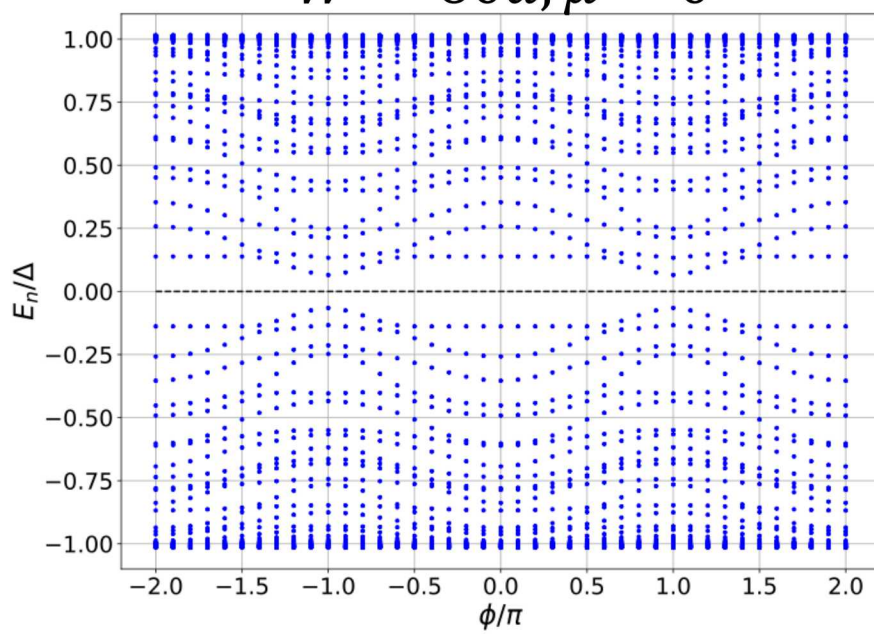
Two minima in excited ABS
split symmetrically about π
associated with spin-orbit
coupling

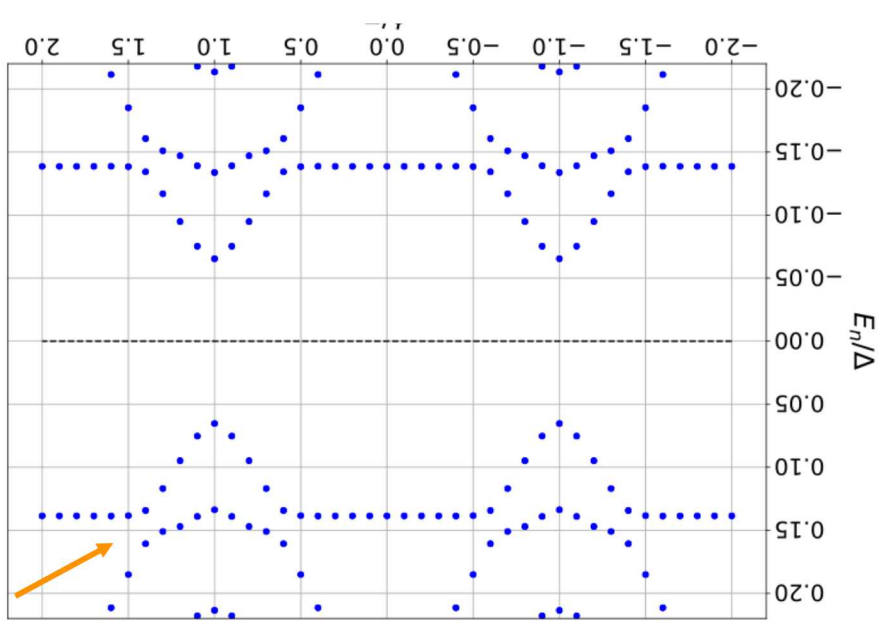
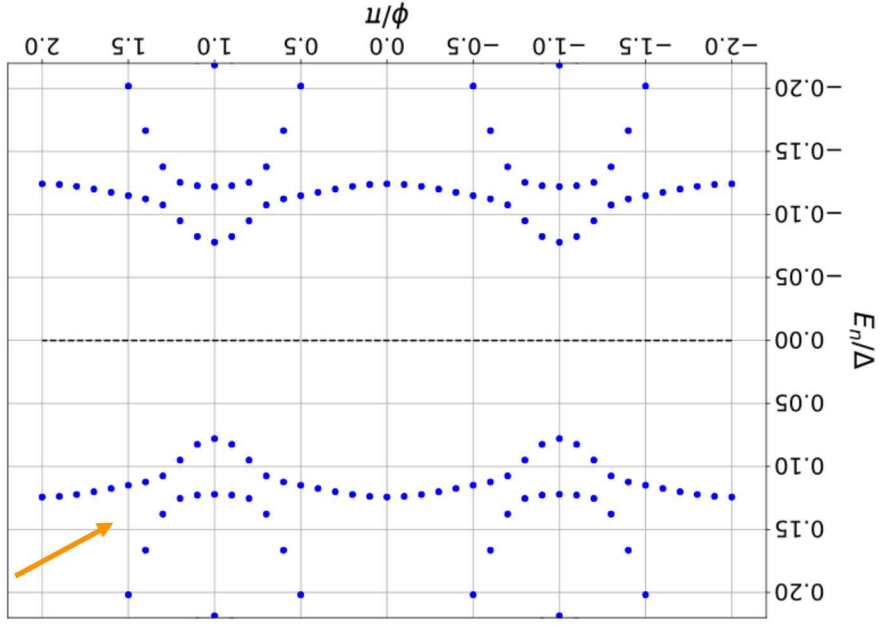
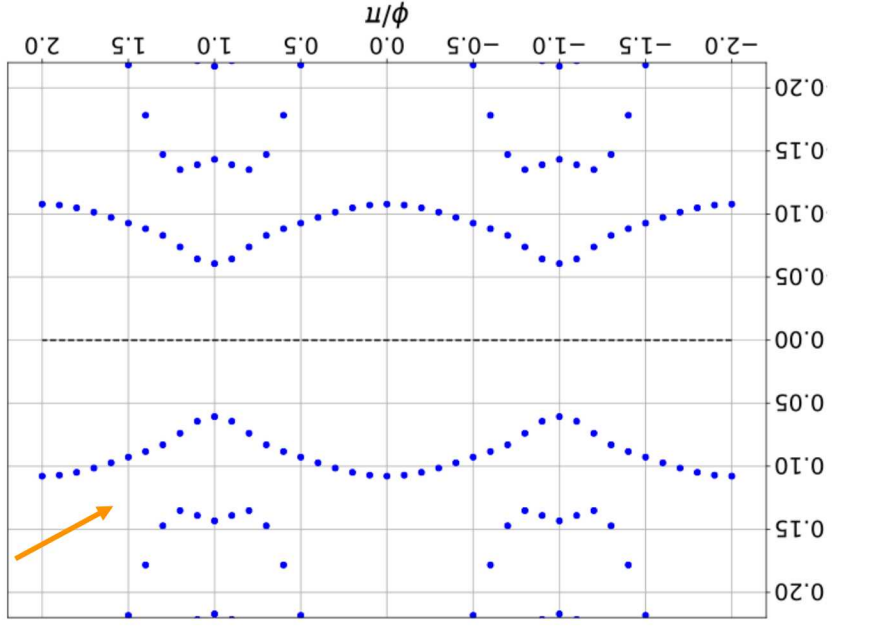
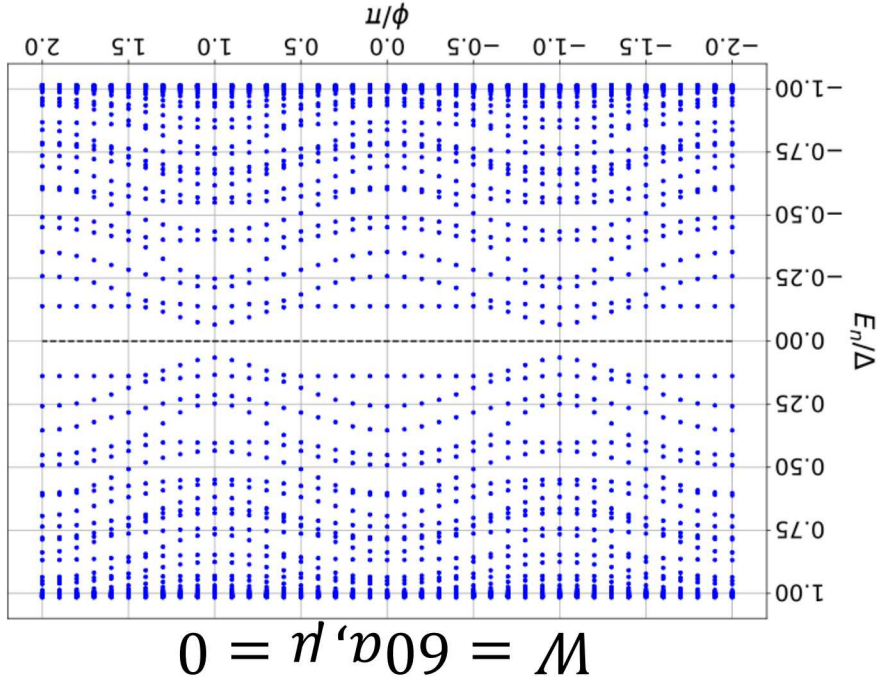
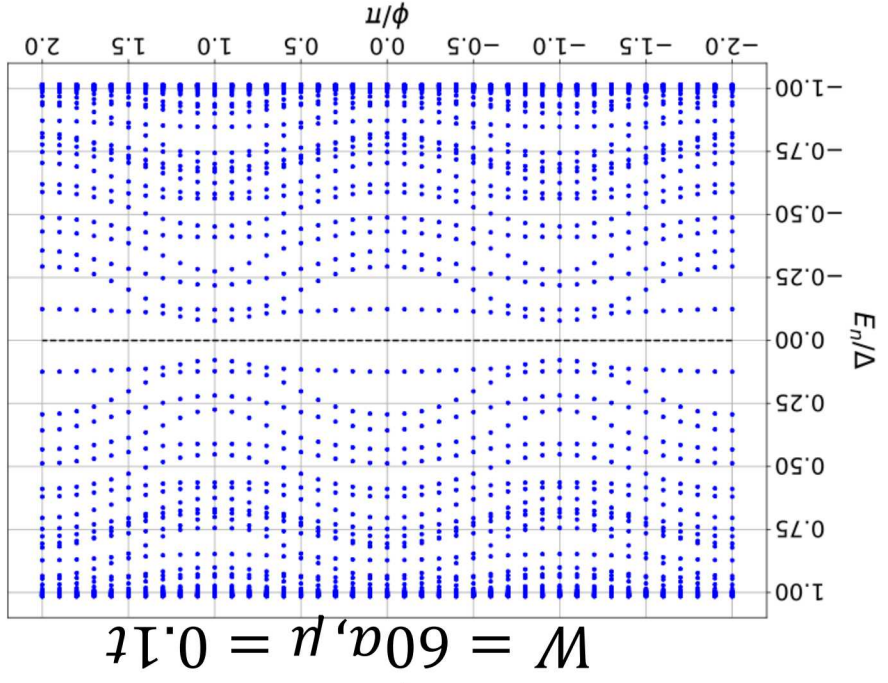
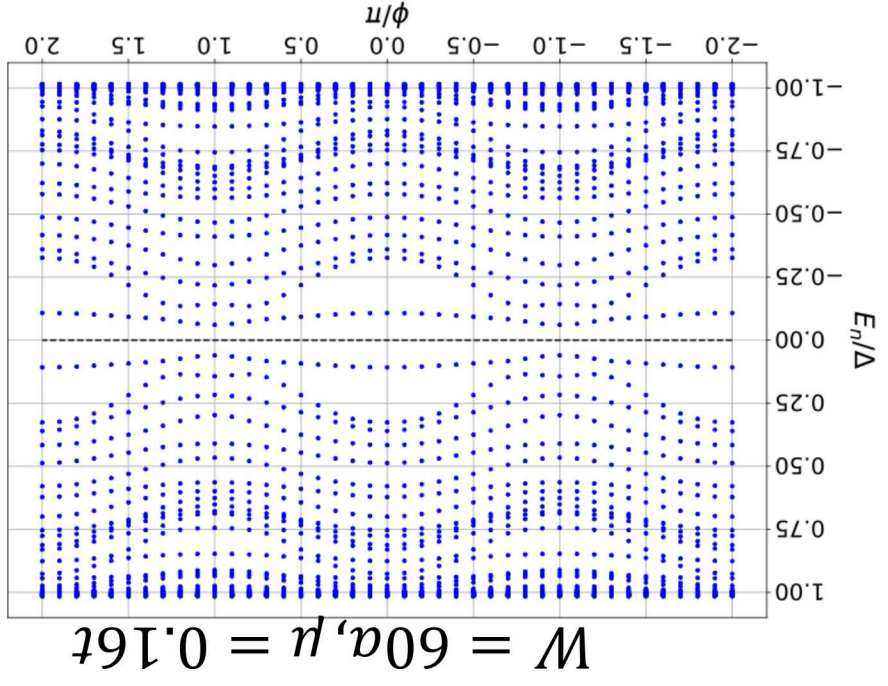
$$W = 48a, \mu = 0$$



Splitting is sensitive to
junction geometry

$$W = 60a, \mu = 0$$





Gap at π : sensitive to chemical potential

Splitting is insensitive to small deviations of the chemical potential away from the DP, but leads to avoided crossings due to backscattering

Summary

- No trivial mechanism identified to explain anomalous Shapiro steps
- Simplest description of a topological SQUID fails to agree with experiment
- Strong SOC in Cd₃As₂ affects ABS spectrum (directly related to supercurrent) significantly, even in the *absence* of Zeeman splitting
- Outlook:
 - Developing more detailed analytic model of CPR for Cd₃As₂ with and without magnetic field
 - Experimental signatures - potentially less ambiguous demonstration of Fermi-arc topological superconductivity