



Sequential Tempered Markov Chain Monte Carlo:

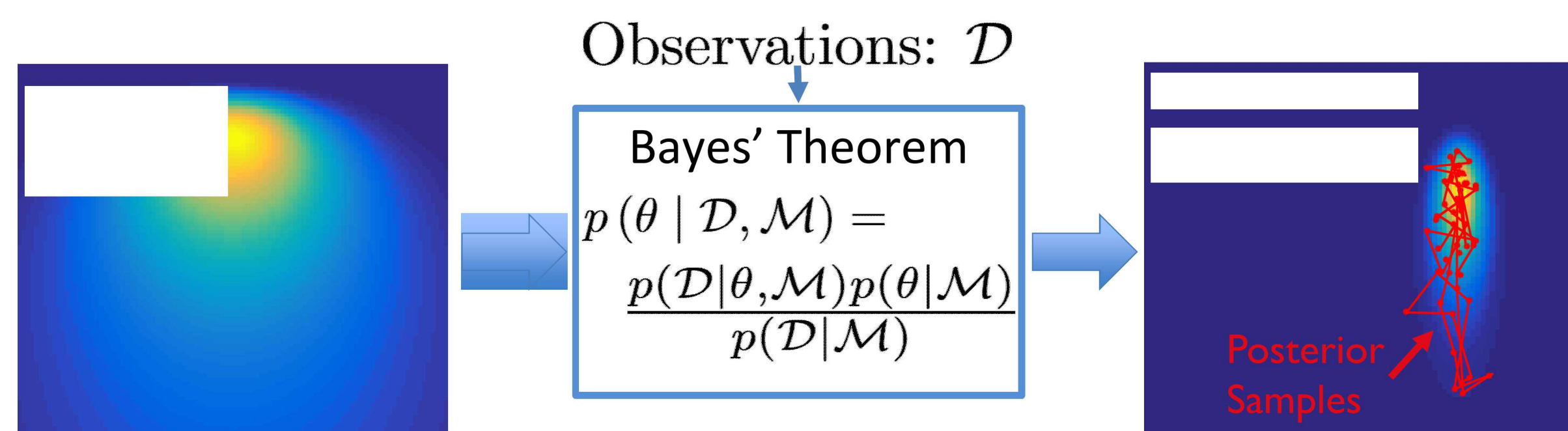
Accelerating Bayesian Inference, Model Selection, and Uncertainty Quantification

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Problem

The Bayesian Perspective:

We update uncertainty as information or observations (\mathcal{D}) are added (**Bayes' Theorem**)



Applications

- Calibrate model parameters $p(\theta|\mathcal{D})$
- Compare model structures $p(\mathcal{M}|\mathcal{D})$
- Predict failures from data $p(\mathcal{F}|\mathcal{D})$

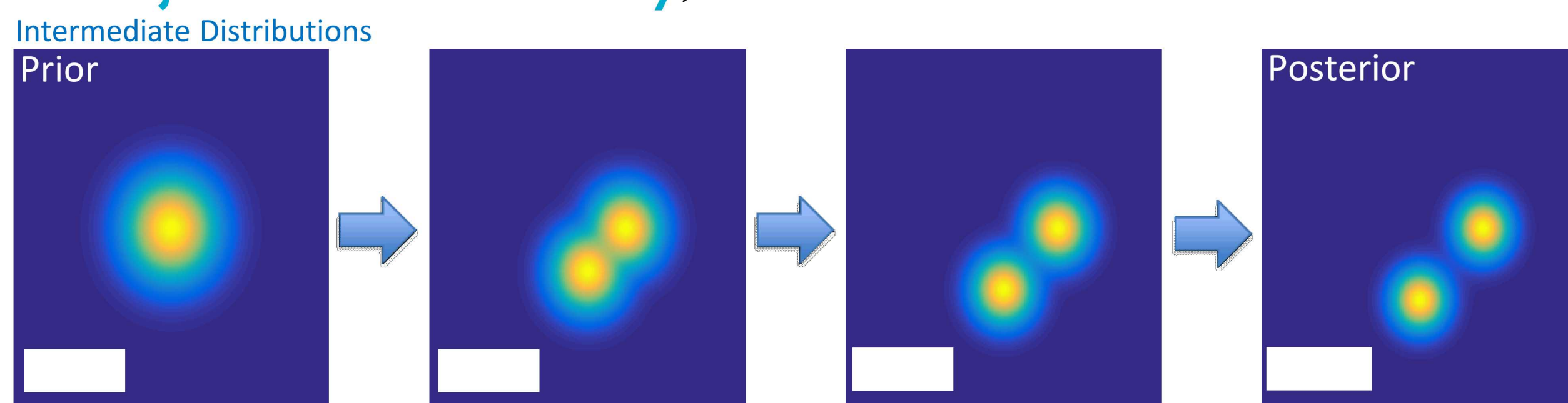
Challenges of Bayesian Methods:

- Markov Chain Monte Carlo (MCMC) is often used to sample the posterior in these applications
- We desire MCMC methods that quickly **explore** the posterior, require **little tuning**, can be **parallelized**, and leverage **multifidelity** models

Approach

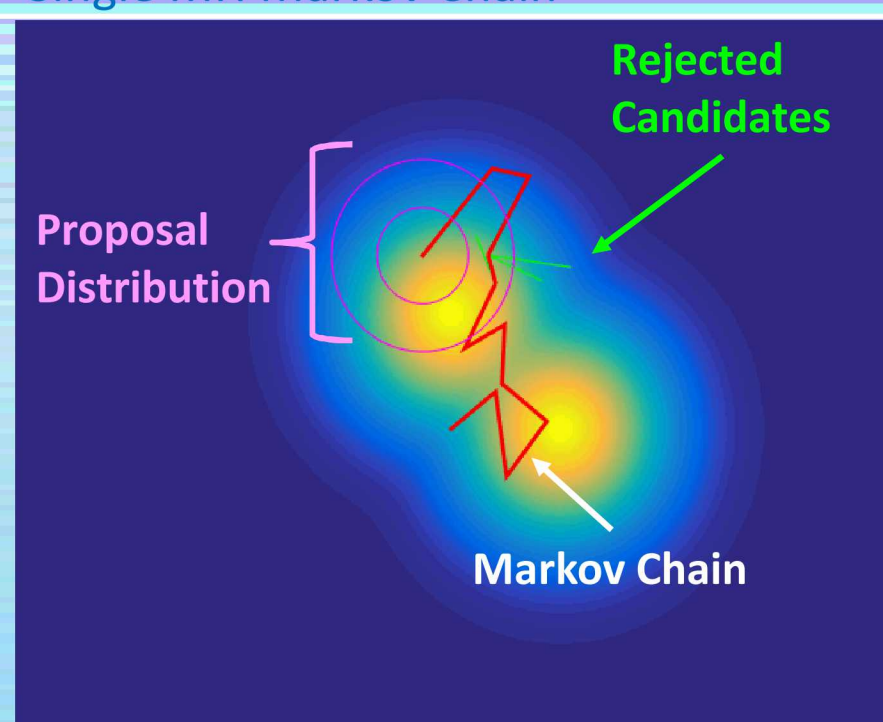
Sequential Tempered MCMC[†] (ST-MCMC):

- Update prior to posterior through intermediate distributions to **aid exploration**
- These distributions can gradually introduce data, **adjust model fidelity**, or relax failure thresholds

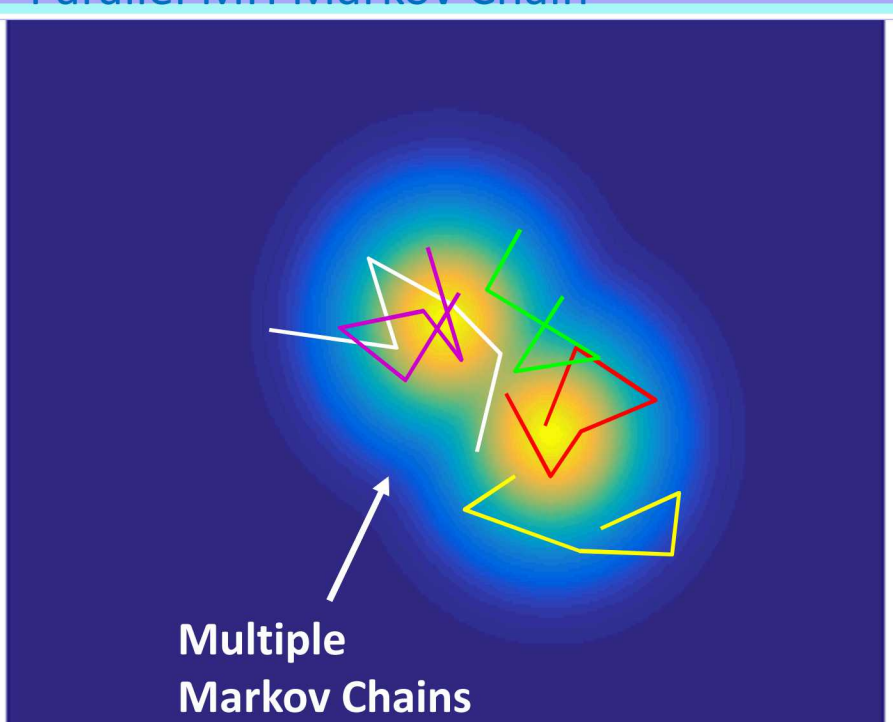


- Parallel** MCMC chains quickly explore and sample the intermediate distributions

Single MH Markov Chain



Parallel MH Markov Chain



- ST-MCMC adapts online based on statistics from the intermediate samples with **little user tuning**

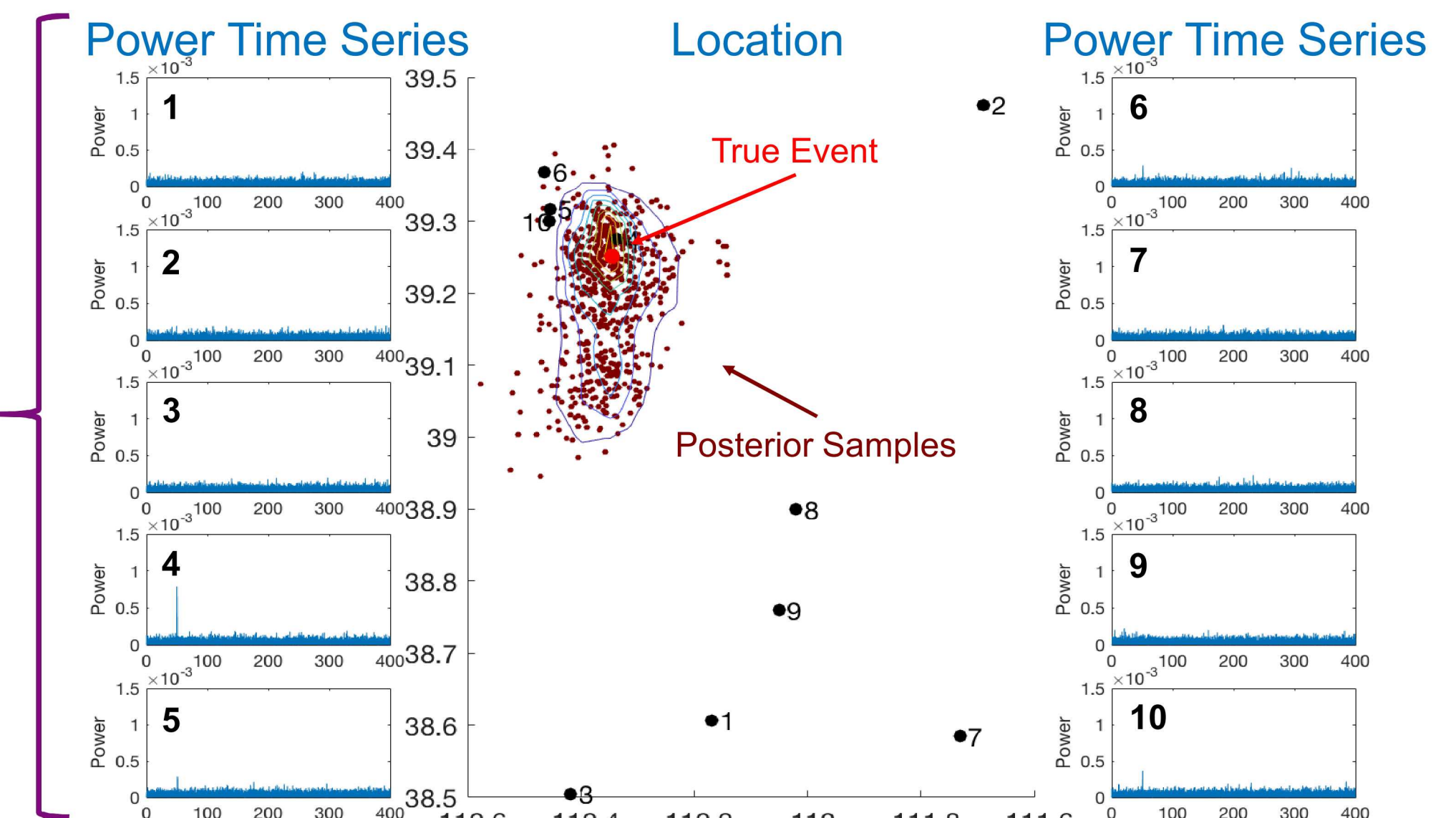
Results

Seismic Monitoring via Bayesian Inference:

- Identify the location and magnitude of weak seismic events from observed waveforms with uncertainty
- ST-MCMC adapts to integrate sensors and improve uncertainty models

Example

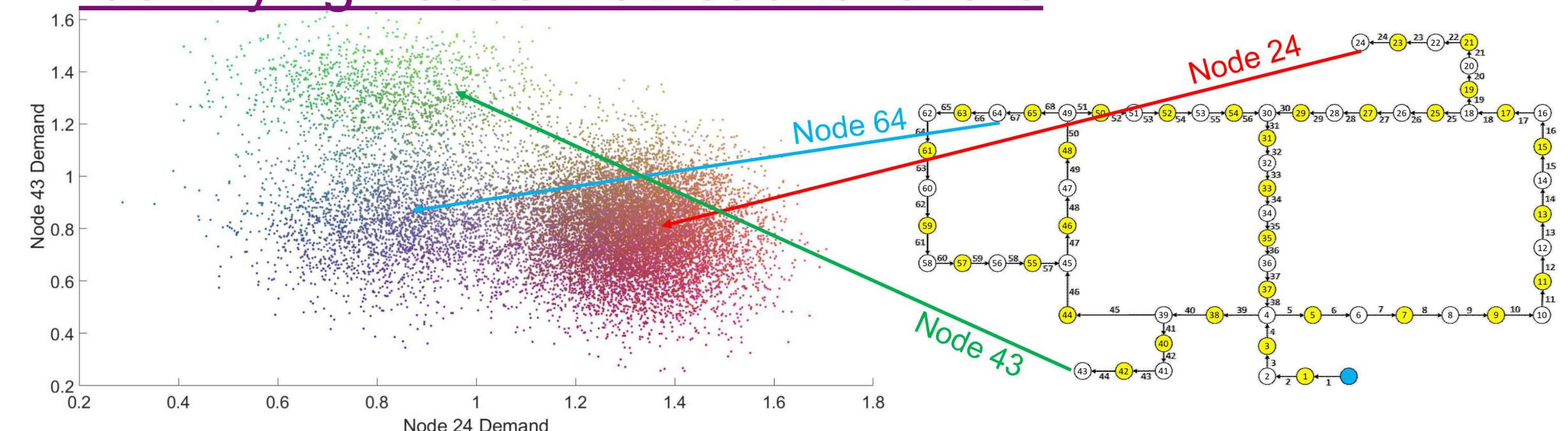
Identification of weak event



Water Distribution System Reliability:

- Estimate the failure probability for a system with unknown parameters using water pressure data
- ST-MCMC simultaneously solves the model calibration and reliability problem over 10x faster than state-of-the-art

Identifying nodes that lead to failure



Significance

ST-MCMC Impact:

- ST-MCMC provides **an efficient, flexible, and robust method for Bayesian uncertainty quantification**
- ST-MCMC enables waveform-based seismic monitoring, which has been held back by computational cost
- ST-MCMC addresses **posterior system reliability**, which has not been done previously

Future Work:

- Information theory for intermediate distributions
- Improve adaptation methods via machine learning

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