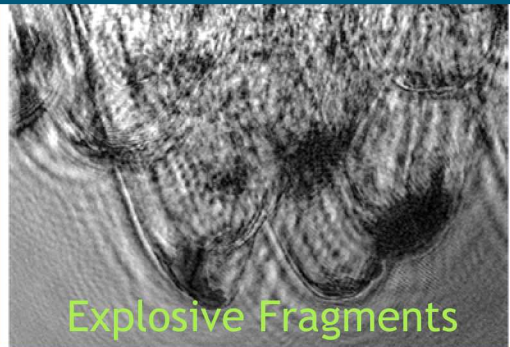
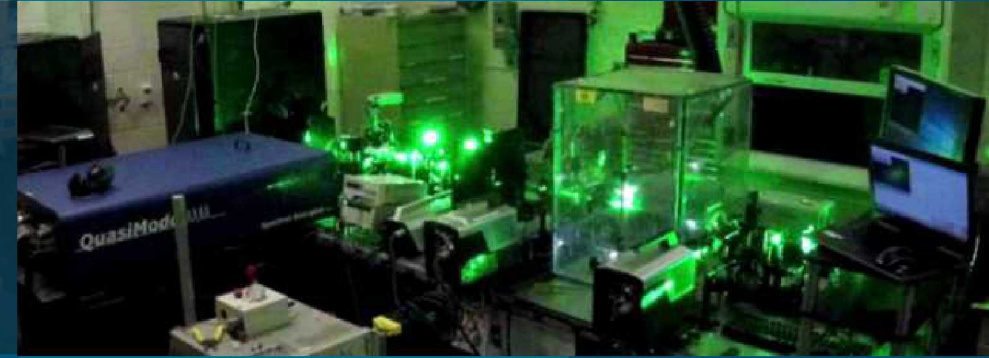
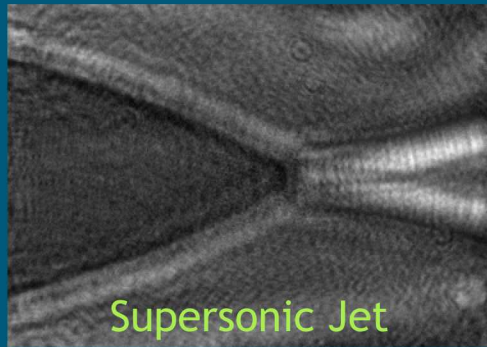


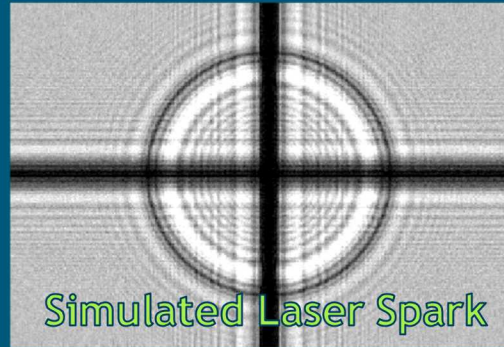
Ultra-high-speed Pulse-burst Phase Conjugate Digital-Inline Holography for Imaging through Shock-wave Distortions



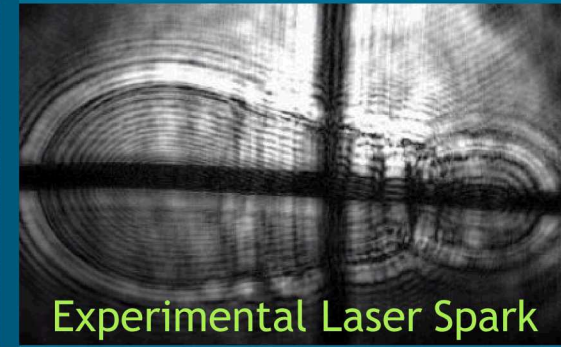
Explosive Fragments



Supersonic Jet



Simulated Laser Spark



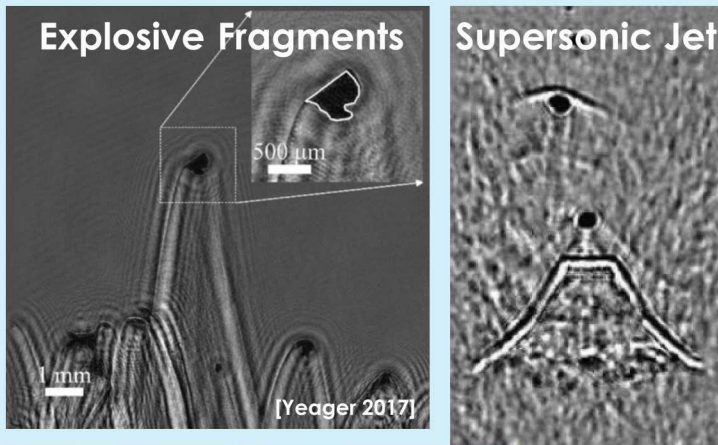
Experimental Laser Spark

Ellen Yi Chen, Jeffery D. Heyborne, Daniel R. Guildenecher, Michael E. Smyser and Mikhail N. Slipchenko

AIAA SciTech
San Diego, California, January 7th-11th, 2018

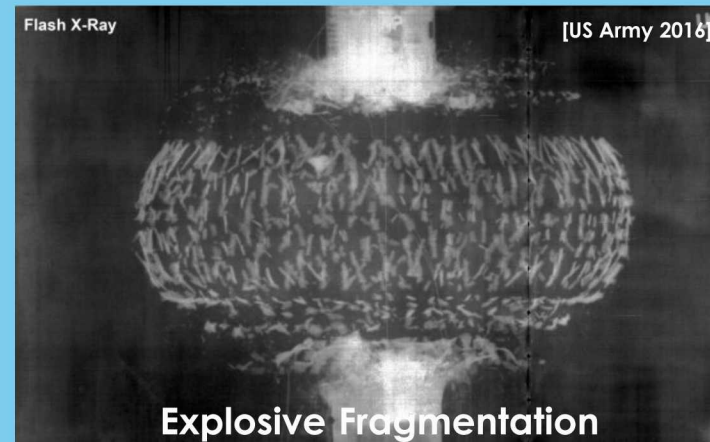
Problem Statement

- Shock-wave distortions prevent accurate 3D interrogation in supersonic, hypersonic, and explosive environments
- Ultra-high-speed acquisition is desired for time-resolved measurements



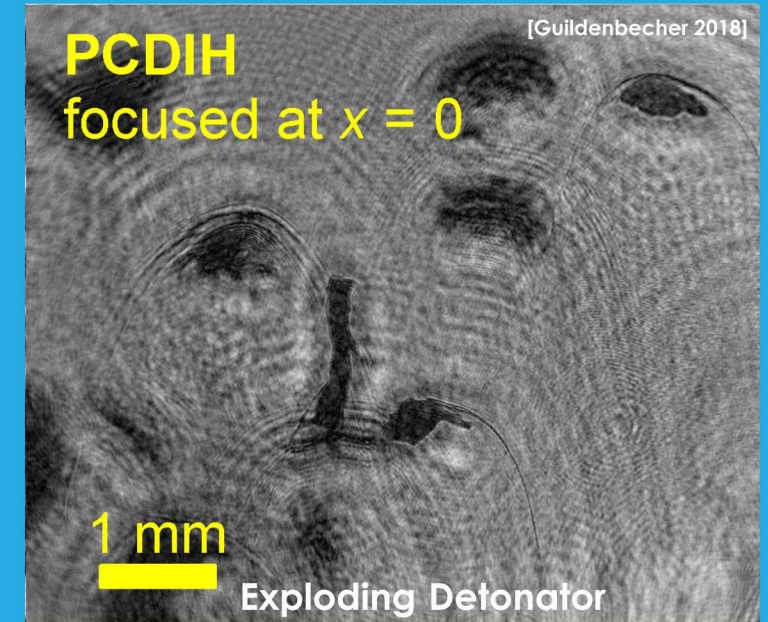
Existing Approaches

- Testing in vacuum
- Synchrotron x-rays and experimental repetition



Proposed Solution

- Cancelling the distortion using phase conjugate digital in-line holography (PCDIH)

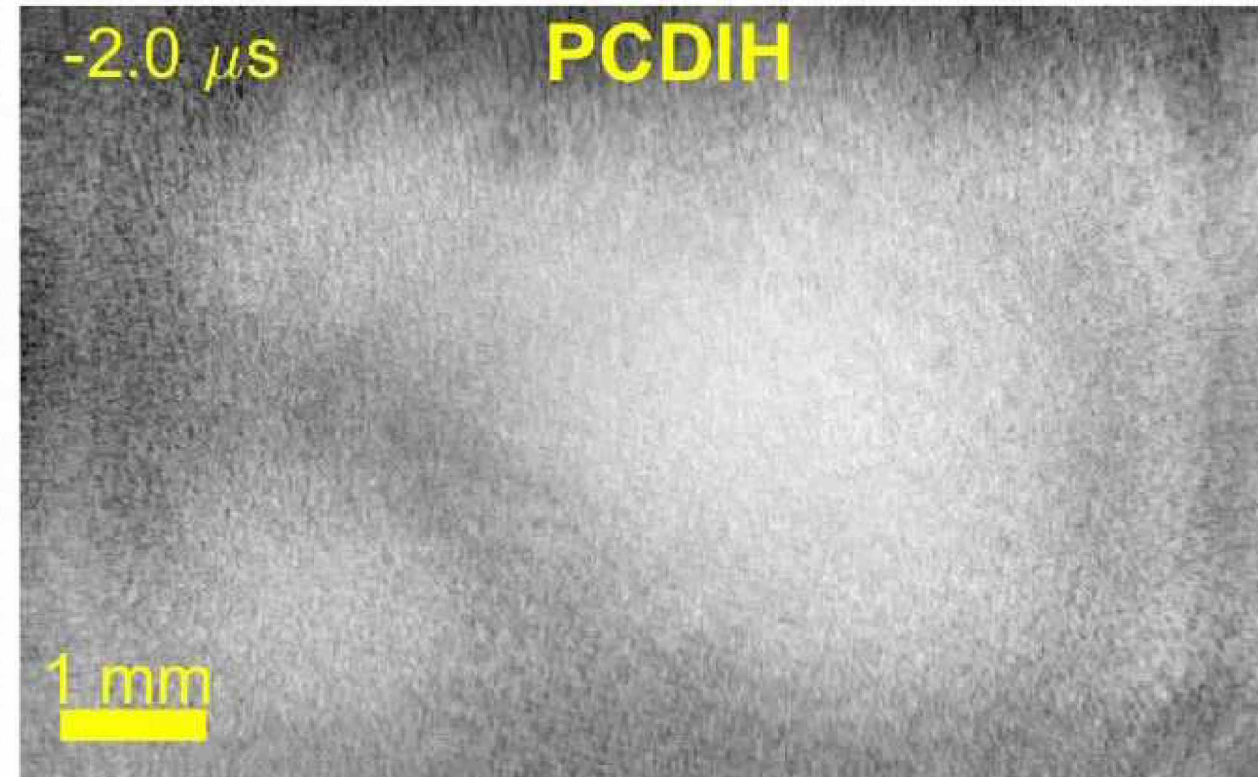
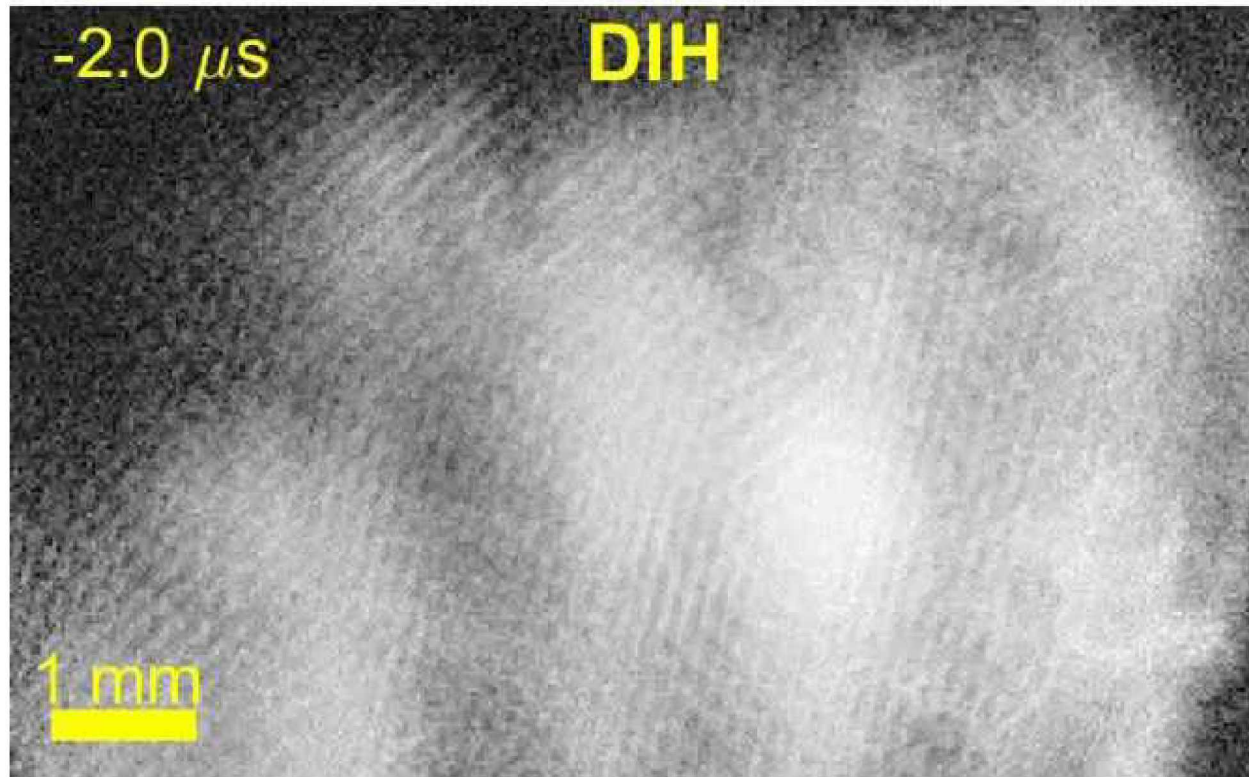


- Previous work limited to 10 to 20 Hz due to peak power requirements → one image per experiment
- Implementing the method with a pulse burst laser and ultra-high-speed cameras for time-resolved measurements.

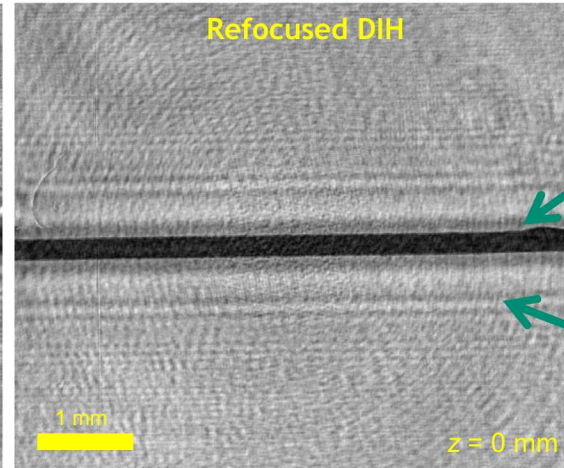
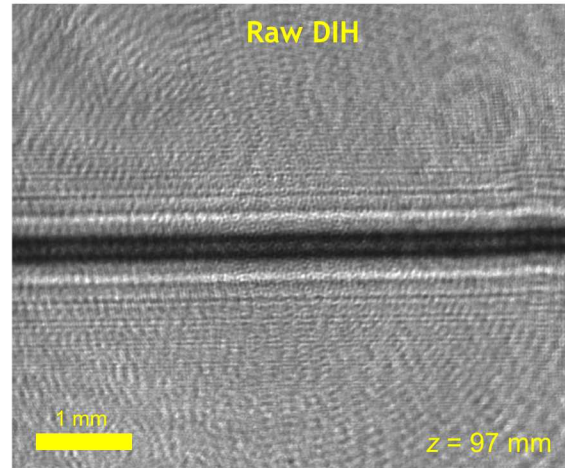
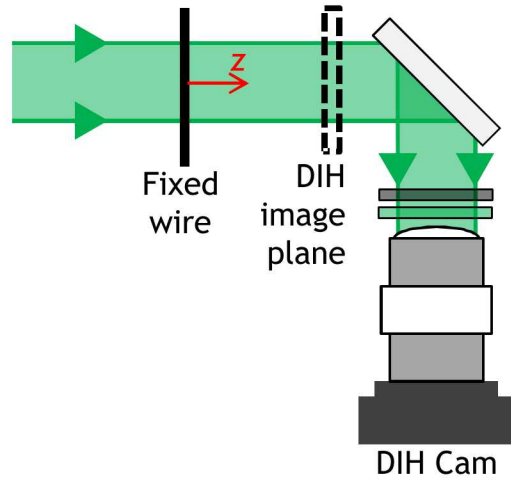
- Track hypersonic fragments from an explosive detonator in 3D through shock-wave distortions
- Increase acquisition from 10 to 20 Hz → 2 to 5 MHz (increase by > 5 orders of magnitude)
- Understand the physical mechanisms that produce unknown features in DIH and PCDIH images

DIH versus PCDIH

2 MHz Holograms



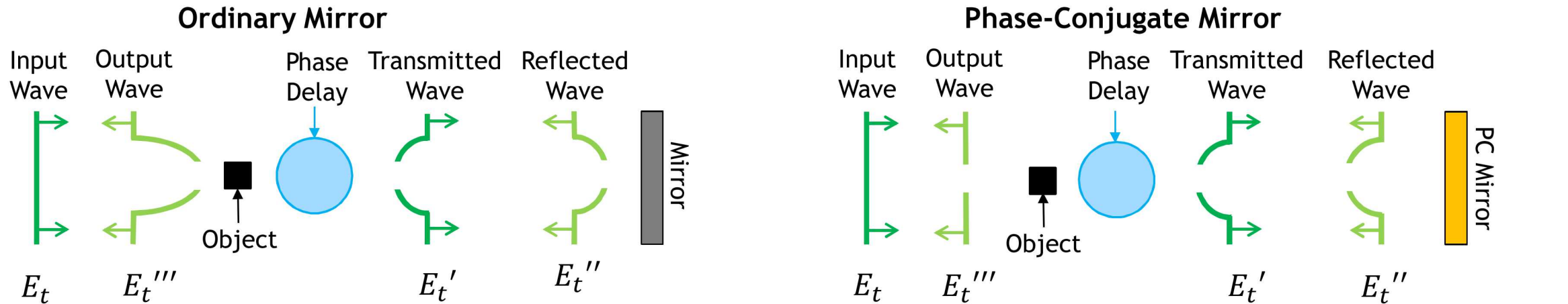
4 Digital In-line holography



In-focus hologram with sharp edges
 Diffraction patterns from "virtual image"

- Digital In-line holograms (Gabor 1948) are collected out-of-focus and are later numerically refocused
- Holograms are collected at the image plane z_h as $h(x, y) = |E_t(x, y, z_h)|^2$
- Holograms are numerically refocused using $E_h(x, y, z) = [h(x, y)E_r^*(x, y)] \otimes g_b(x, y, z)$
 where $g_b = FT^{-1}(G^*)$ and $G = e^{\frac{2\pi iz}{\lambda} \sqrt{1 - (\lambda x)^2 - (\lambda y)^2}}$
- The amplitude is determined from $A_h = |E_h|$
- In-focus z-planes are determined using maximum edge sharpness and minimum amplitude criteria.
- Tracking across multiple frames gives 3D velocity
- How do phase-distortions affect this process?

Phase Conjugate Mirror for Distortion Cancellation



Transmitted Wave

$$E_t' = E_t(x, y, z)e^{i\phi_s(x, y)}$$

Reflected Wave

$$E_t'' = R_m E_t(x, y, z)e^{i\phi_s(x, y)}$$

Output Wave

$$E_t''' = R_m E_t(x, y, z)e^{i\phi_s(x, y) + i\phi_s(x, y)}$$

Doubled phase delay

Transmitted Wave

$$E_t' = E_t(x, y, z)e^{i\phi_s(x, y)}$$

Reflected Wave

$$E_t'' = R_{pc} E_t(x, y, z)e^{-i\phi_s(x, y)}$$

Conjugate phase

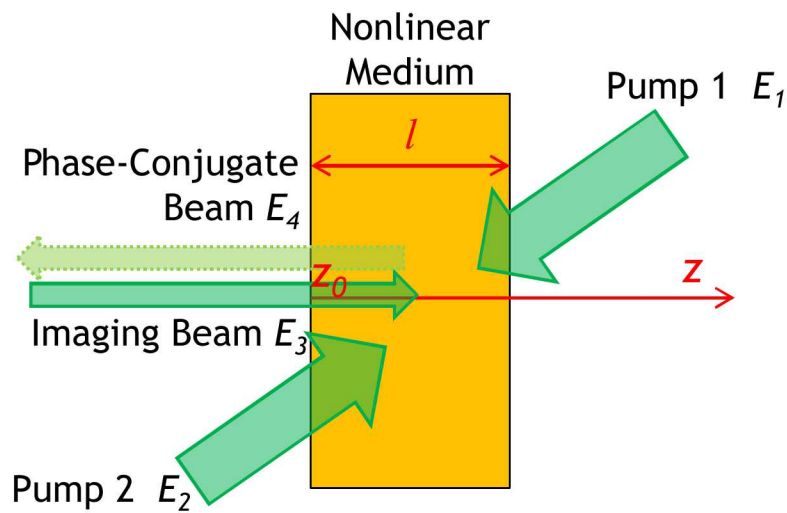
Output Wave

$$E_t''' = R_{pc} E_t(x, y, z)e^{-i\phi_s(x, y) + i\phi_s(x, y)}$$

Cancelled phase delay

Phase Conjugation via Degenerate Four-Wave-Mixing

- Phase-conjugate beam needs to be generated quickly and at high repetition rates
- Degenerate four-wave-mixing: 1 imaging beam and 2 pump beams produces a 4th beam
- Phase-matching \rightarrow 4th beam travels in opposite direction as imaging beam
- Solving nonlinear coupled wave equations \rightarrow 4th beam is conjugate of imaging beam
- Phase conjugate mirror reflectivity is a function of \tan^2



Electric Fields

$$E_1 = A_1(r)e^{ik_1 \cdot r - i\omega t}$$

$$E_2 = A_2(r)e^{ik_2 \cdot r - i\omega t}$$

$$E_3 = A_3(x, y, z)e^{ik_3 z - i\omega t}$$

$$E_4 = A_4(x, y, z)e^{ik_4 z - i\omega t}$$

Phase Matching

$$k_1 + k_2 = k_3 + k_4$$

$$k_1 = -k_2$$

Nonlinear Coupled Wave Equations

$$\frac{dA_3^*(z)}{dz} = i\gamma^* A_4(z)$$

$$\frac{dA_4(z)}{dz} = i\gamma A_3^*(z)$$

$$\gamma = \frac{\omega}{2cn_0(\omega)} \chi_e^{(3)} A_1 A_2$$

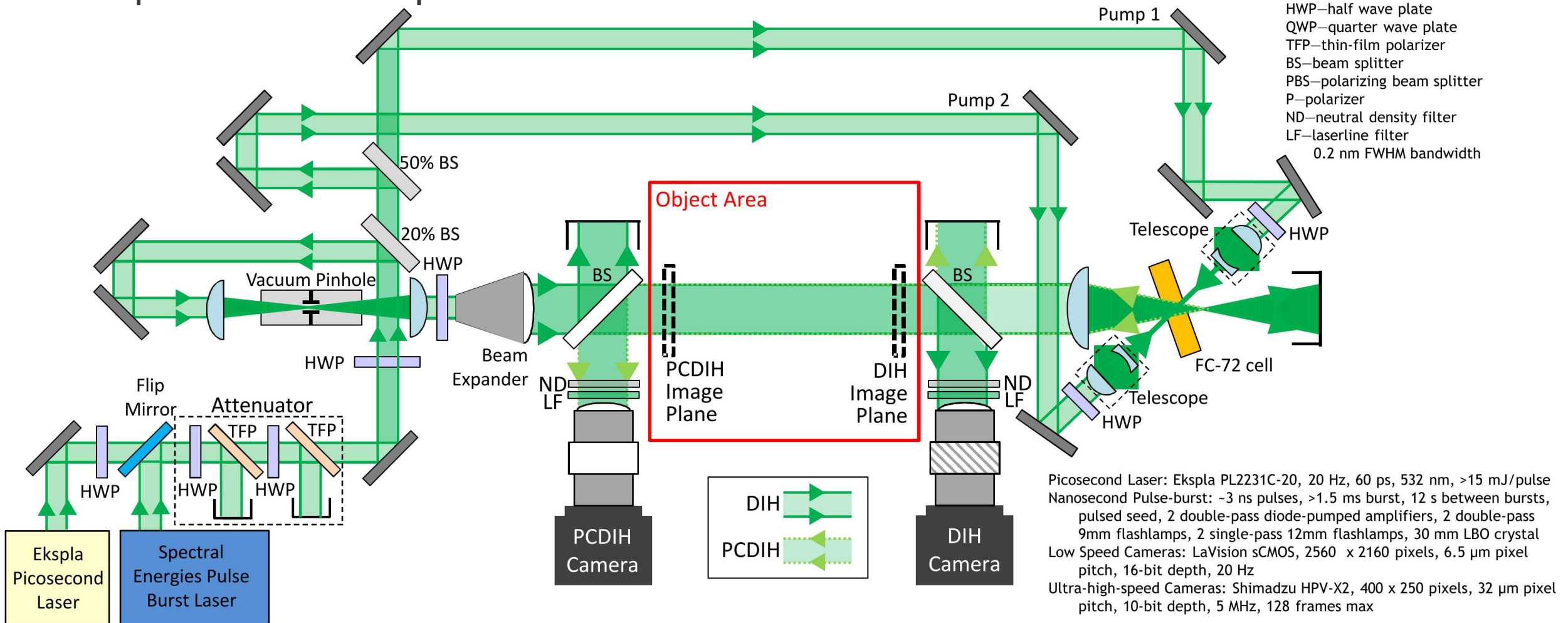
Phase-conjugate Beam

$$A_4(z_0) = -i \frac{\gamma}{|\gamma|} \tan(|\gamma|l) A_3^*(z_0)$$

Phase Conjugate Mirror Reflectivity

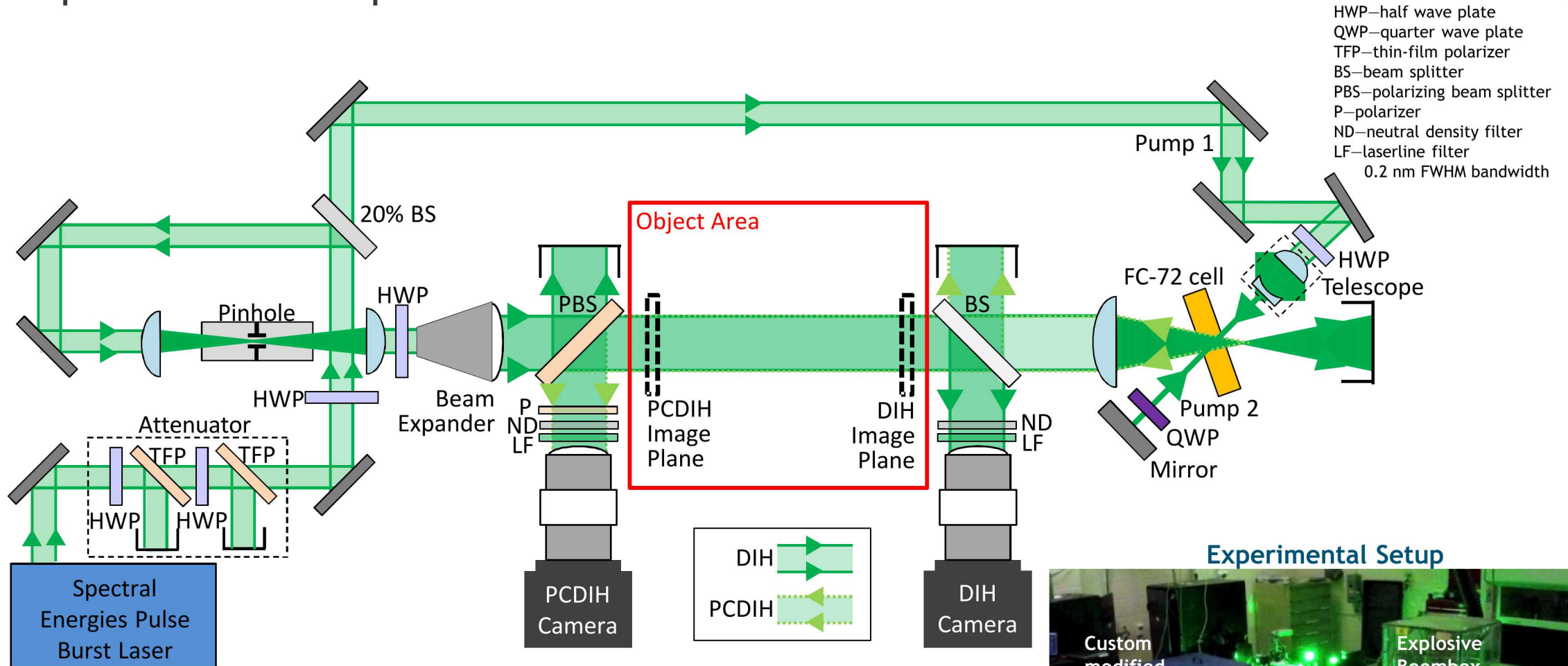
$$R_{pc} = \frac{|A_4|^2}{|A_3|^2} = \tan^2 \left(\left| \frac{\omega}{2cn_0(\omega)} \chi_e^{(3)} A_1 A_2 \right| l \right)$$

Experimental Setup: Picosecond or Nanosecond PCDIH

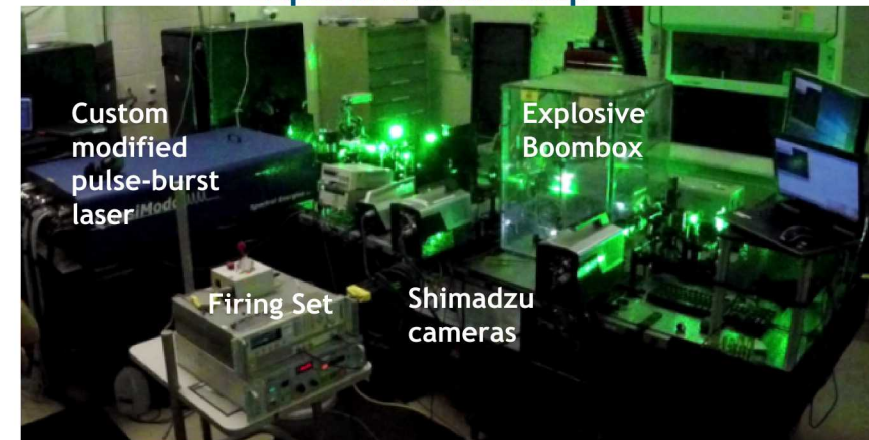


- Laser split into 3 beams, 1 imaging and 2 pump beams
- Capable of simultaneous measurement with traditional DIH and PCDIH
- Polarizations: pump1 → p, pump2 → s, imaging → p, phase conjugate → s
- Configuration works for both picosecond and nanosecond lasers

Experimental Setup: Nanosecond Pulse Burst PCDIH

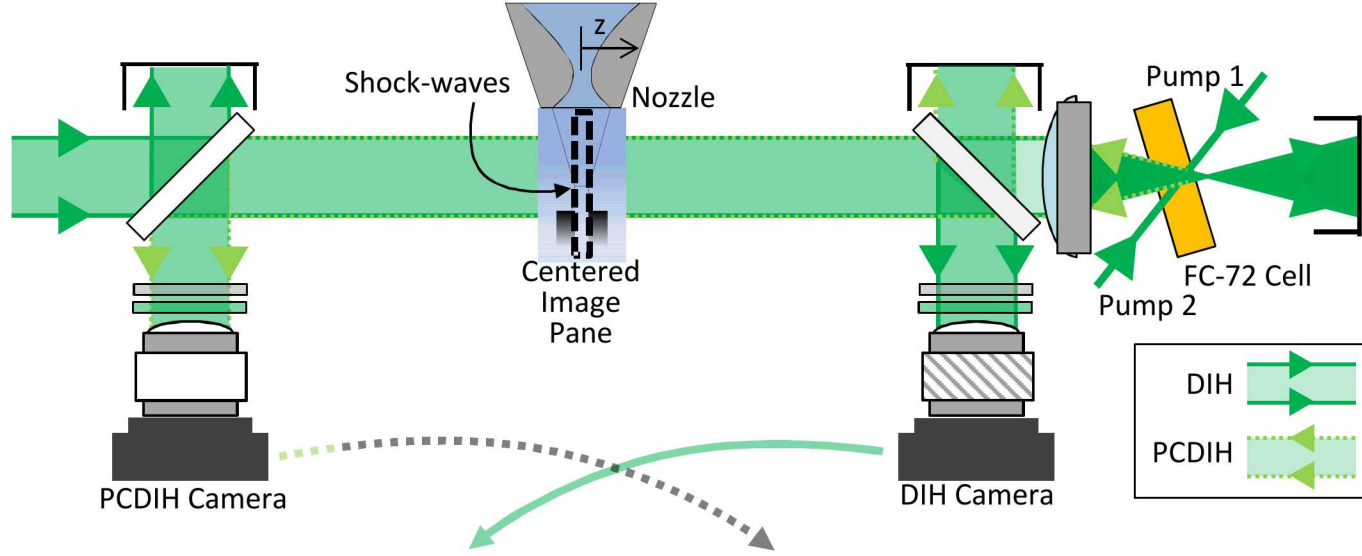


Experimental Setup

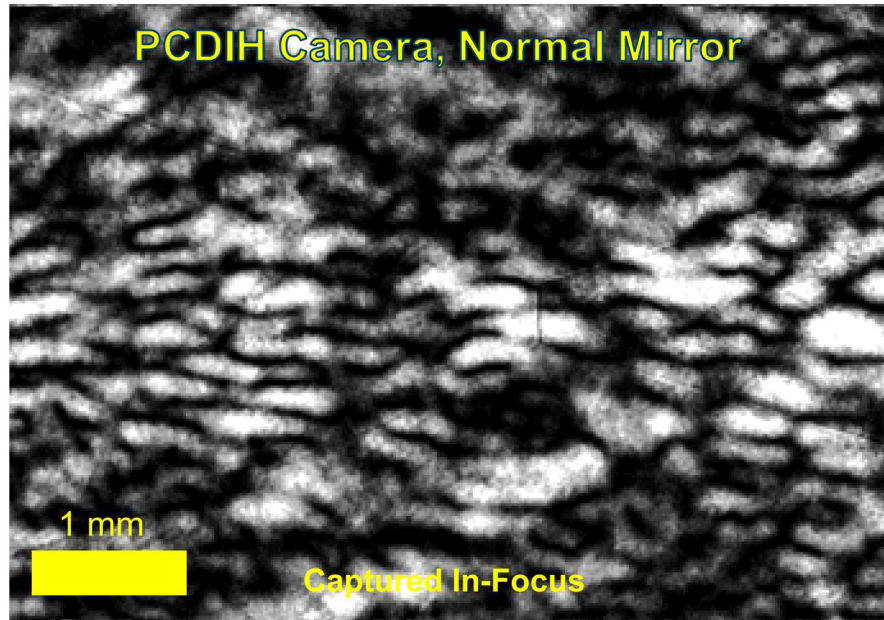
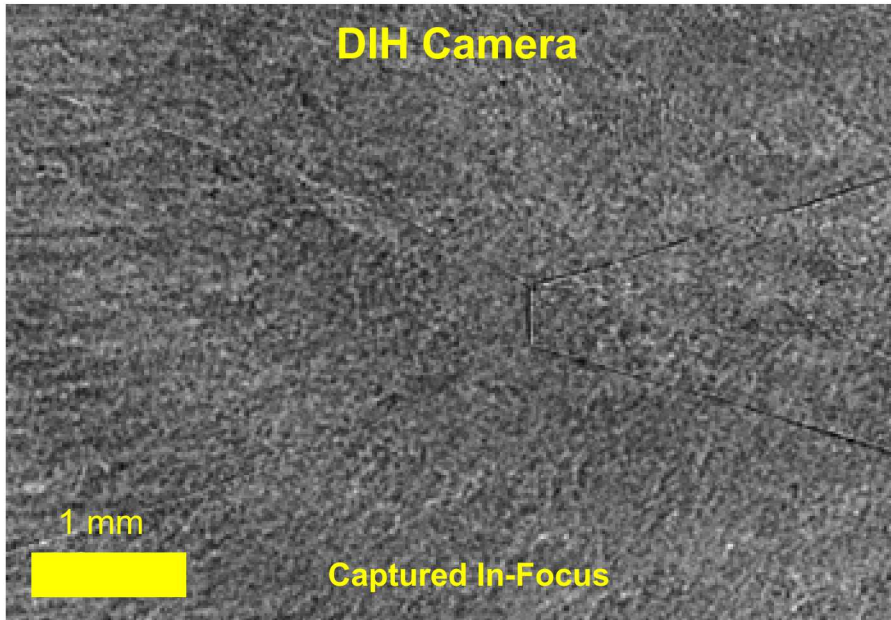


- More efficient design for nanosecond lasers
- Fewer optical components and easier to align
- 1 imaging and 1 pump beam (reflected for second pump beam)
- Inherent optical isolation in the pump beams

9 Stationary Supersonic Shock-waves (picosecond laser)

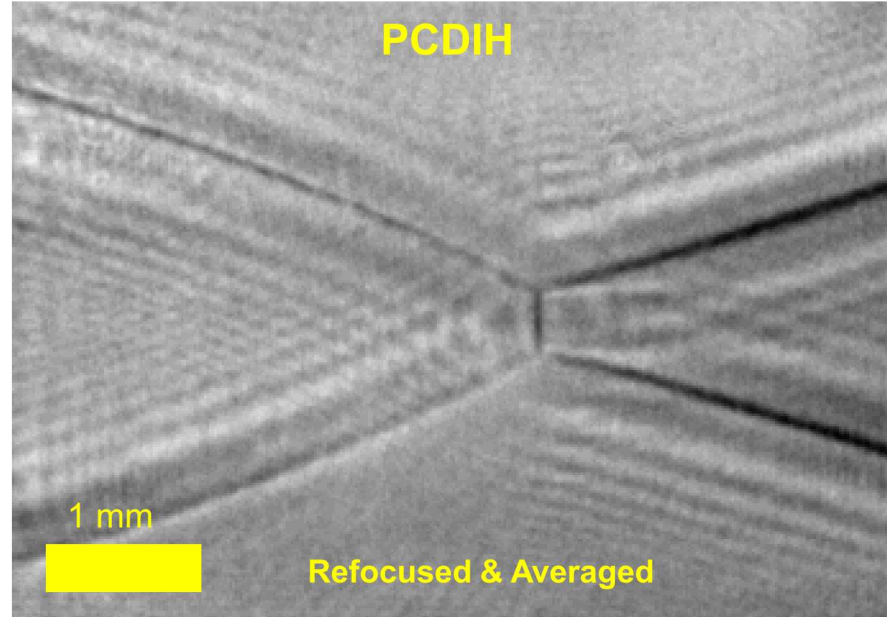
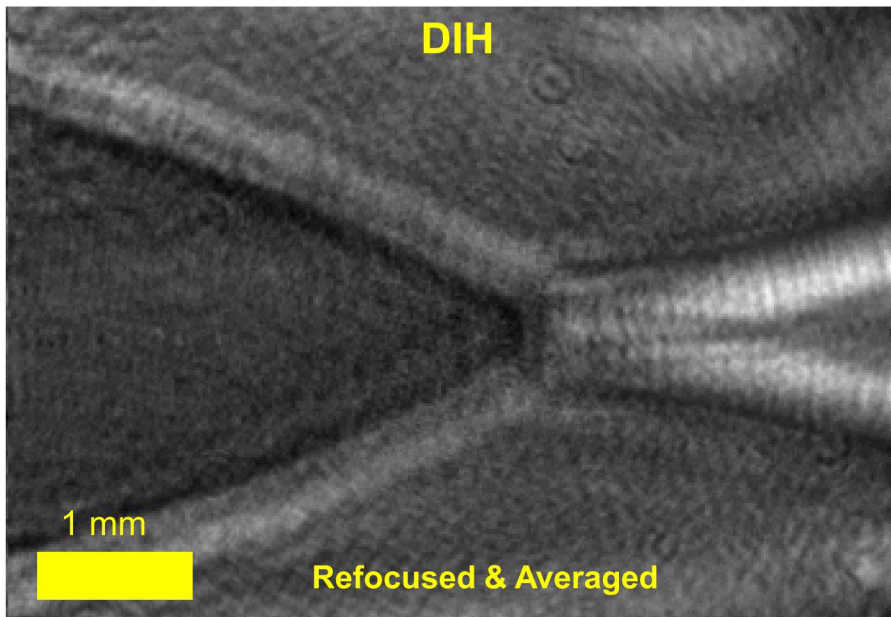
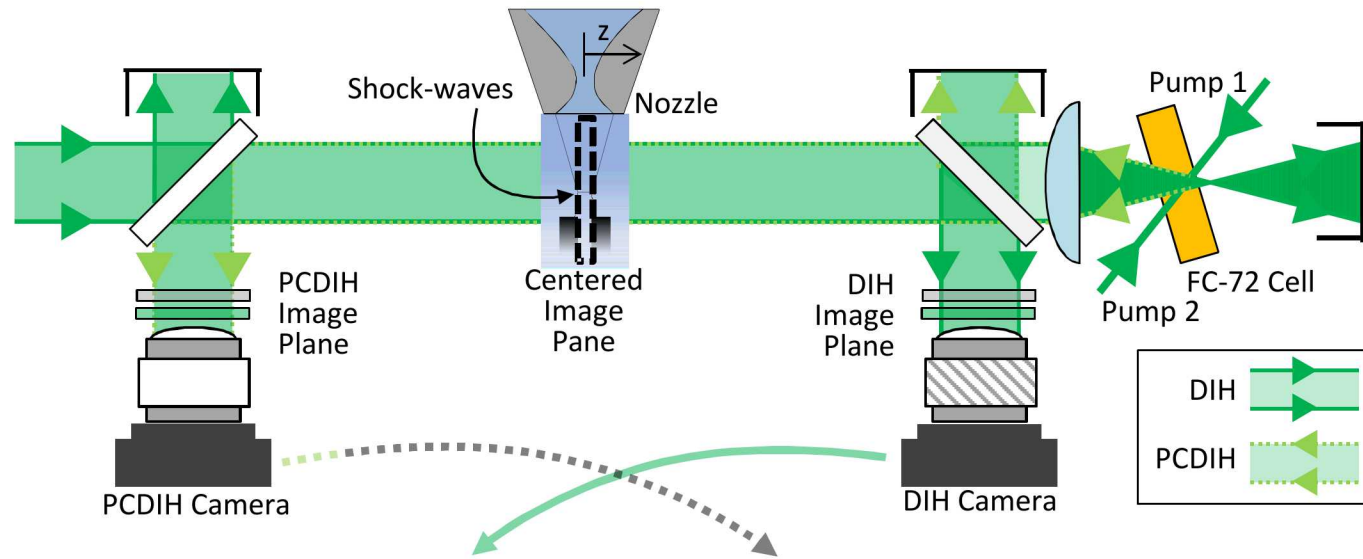


- Supersonic jet allows us to study stationary shock-waves
- Start by investigating in-focus normal imaging
- DIH camera shows clear shock-wave edges & some turbulence
- Shock-wave edges are visible due to refraction
- PCDIH camera shows shadows from acceptance angles of the PC mirror
- PCDIH camera with ordinary mirror shows out-of-focus diffraction patterns from the first pass and shock-wave edges from second pas



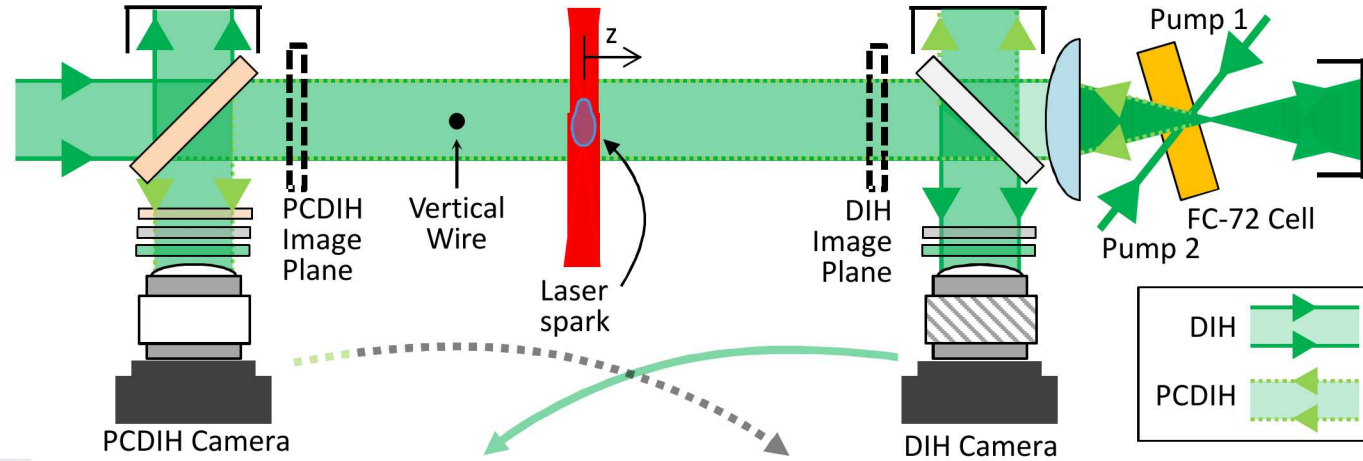
over-expanded jet
 design Mach number of 3.7
 6.35 mm nozzle outlet
 stagnation pressure 4.3 Mpa
 atmospheric pressure 84 kPa

Stationary Supersonic Shock-waves (picosecond laser)

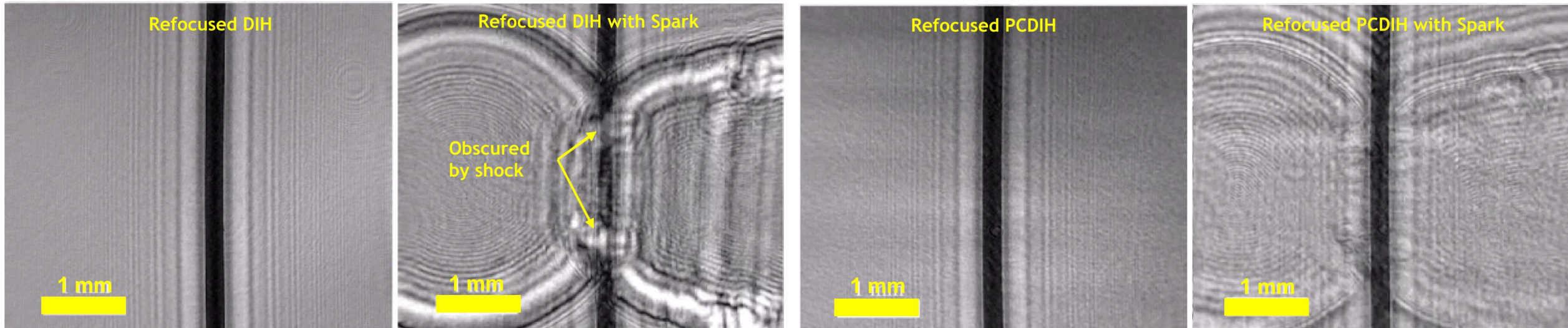


- Focal planes are next moved back for in-line holography
- Holograms are numerically refocused to the focal plane of the shock-wave.
- Single-shot DIH does not numerically refocus to any edges
- Single-shot PCDIH does refocus to shock-wave edges
- Averaging 500 holograms removes turbulence effects
- The DIH hologram does not refocus due to shock-wave distortions
- The PCDIH image refocuses successfully

11 Laser-spark plasma-generated shock-waves (picosecond laser)



200 μm diameter wire
 Continuum Surelite III focused laser
 10 Hz, 1064 nm, 5 ns pulse duration
 operating at 400 mJ per pulse

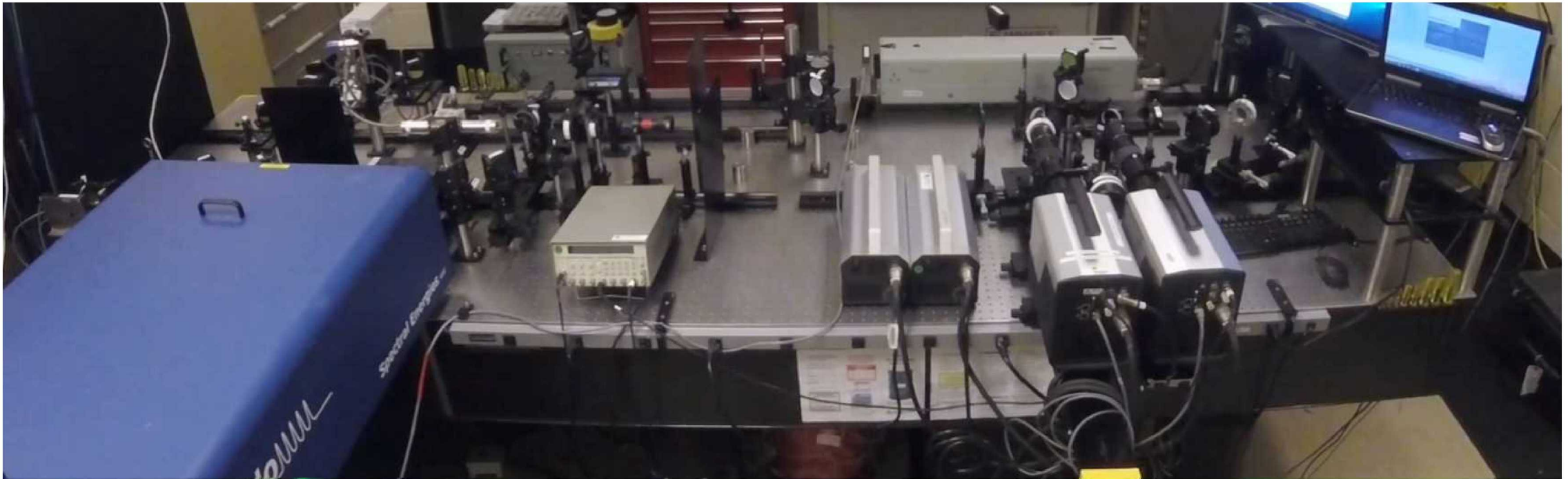
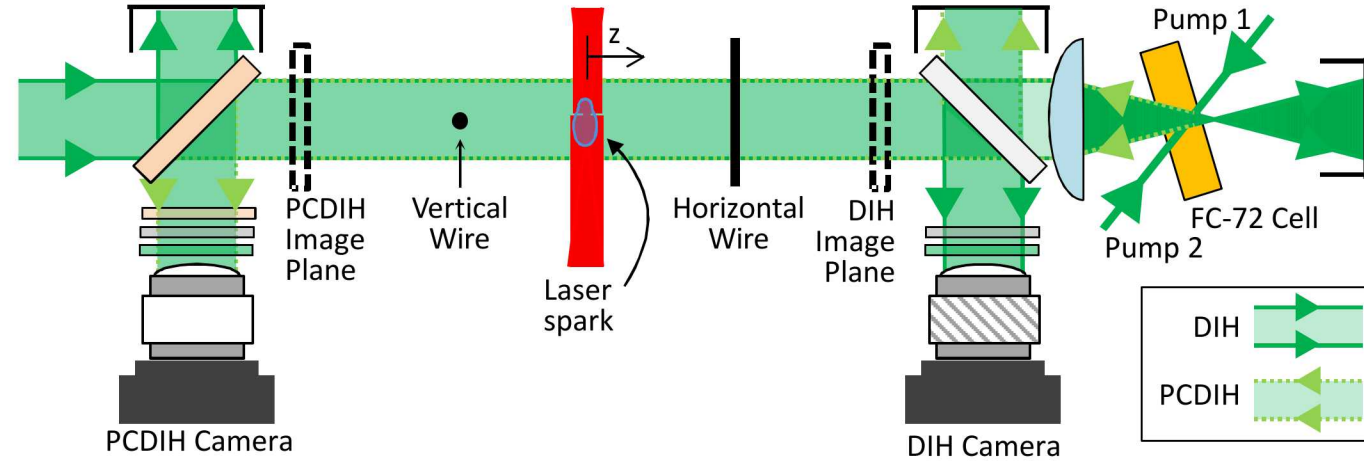


- PCDIH successfully cancels distortions generated by shockwaves that are obscured in DIH images
- Does the order of the wire and phase distortion matter?
- What does the shock-wave phase distortion look like as a function of time?
- Why do the shock-waves come into focus in DIH and PCDIH?
- What is the source of the remaining interference patterns in PCDIH if phase is cancelled?

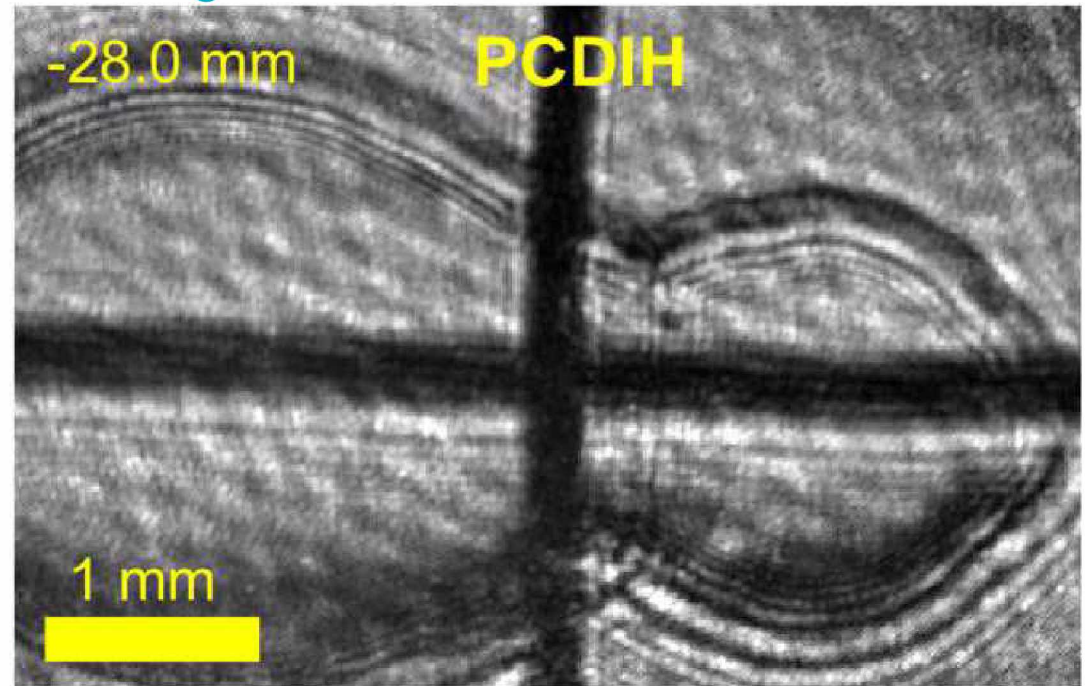
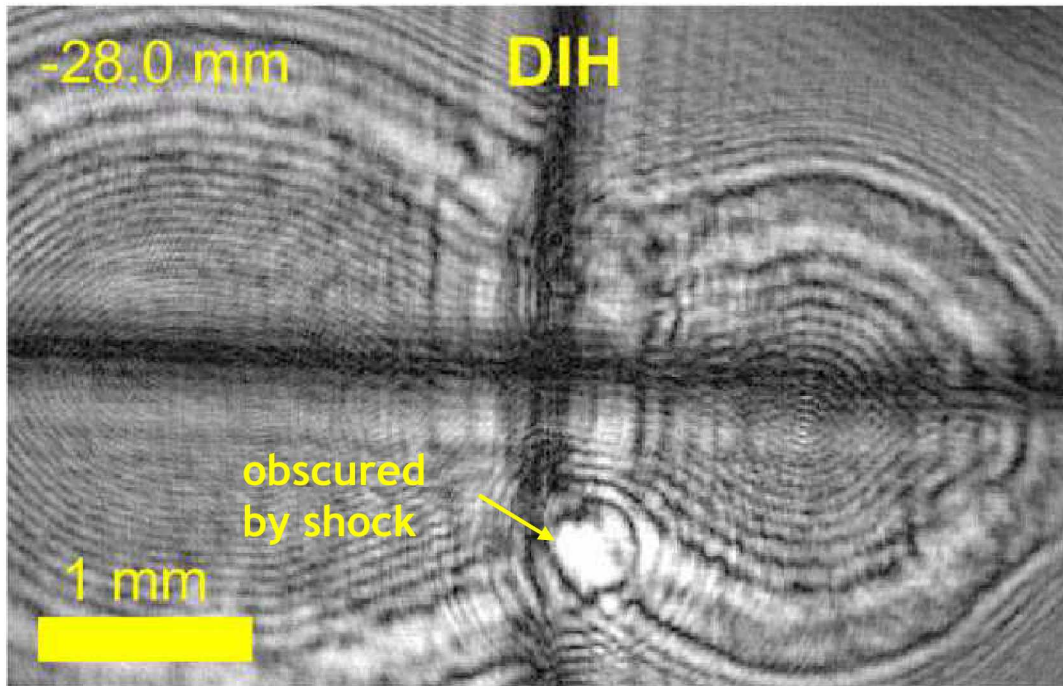
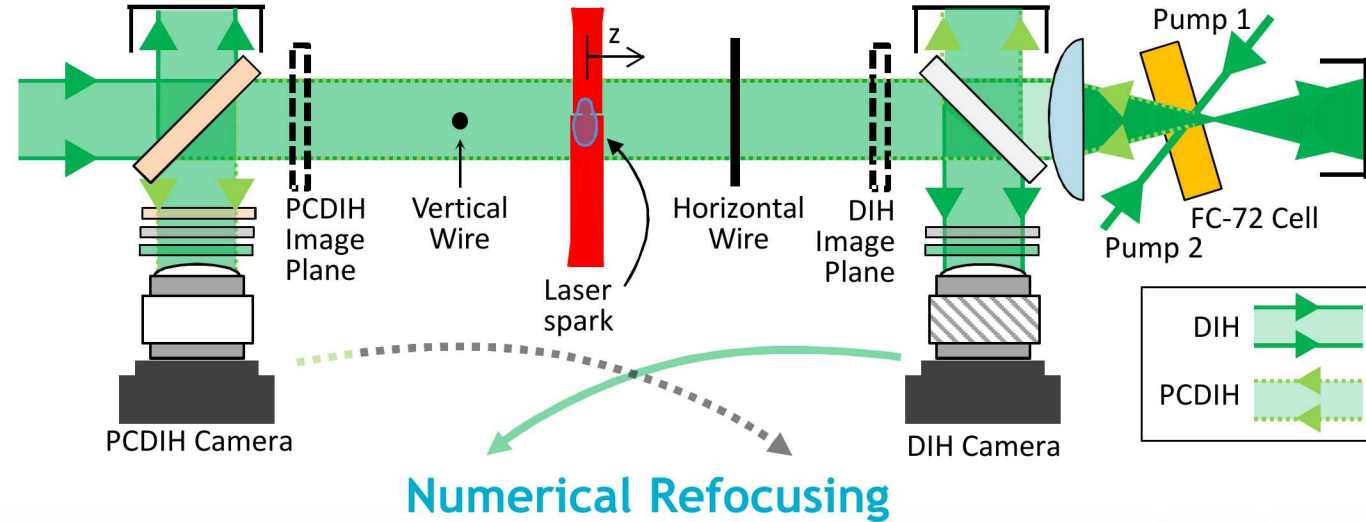
Pulse-burst Experiment

Numerical Simulation

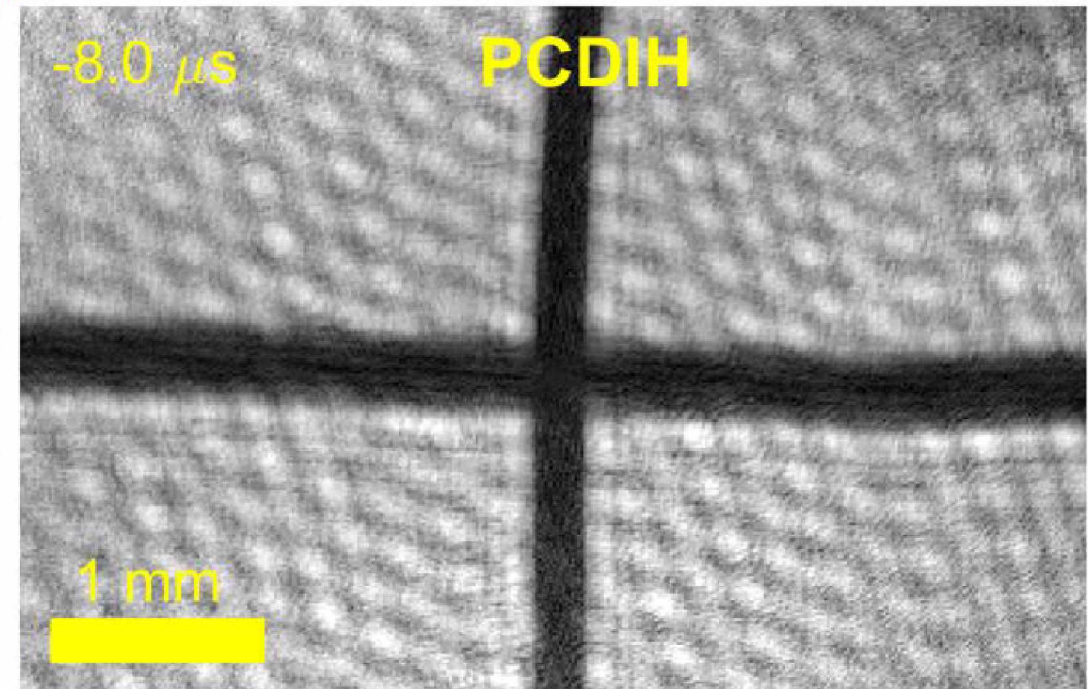
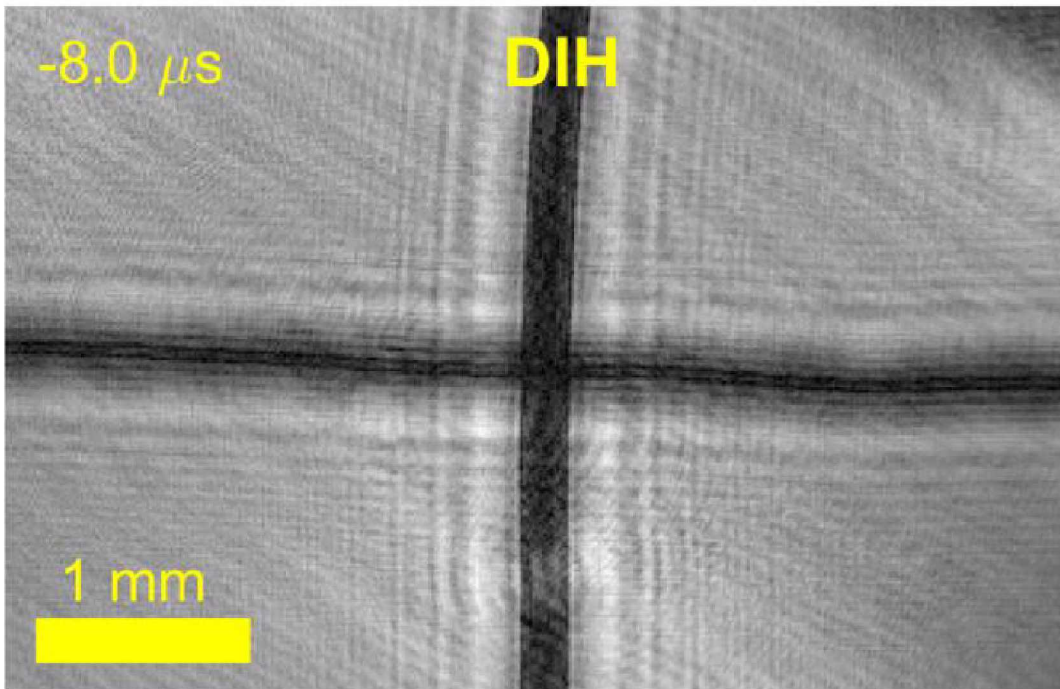
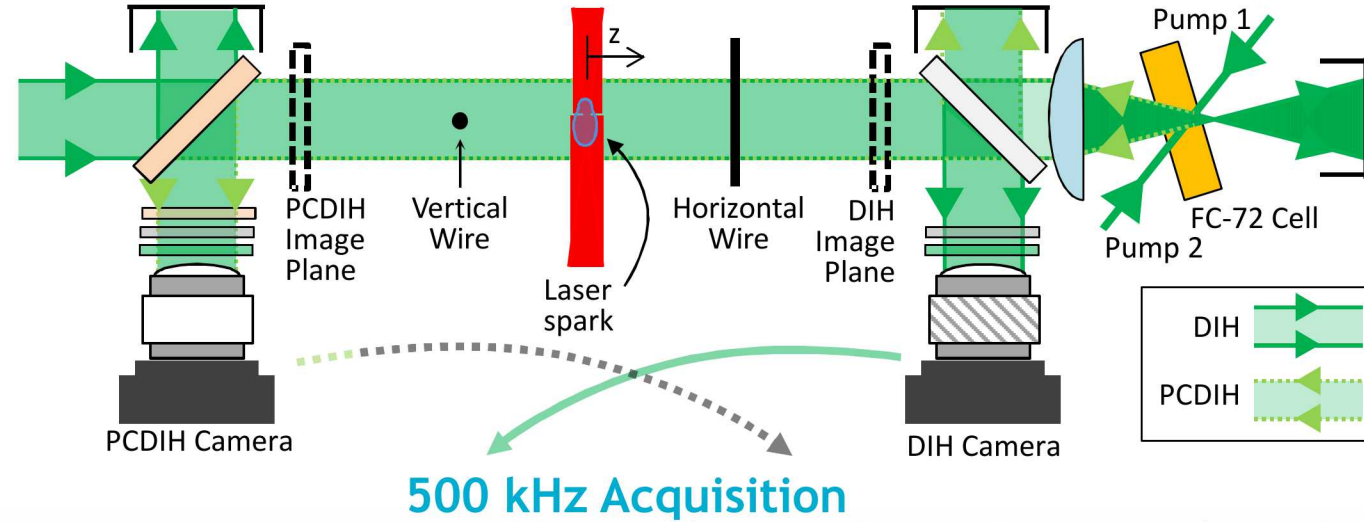
Laser-spark plasma-generated shock-waves (nanosecond pulse burst)



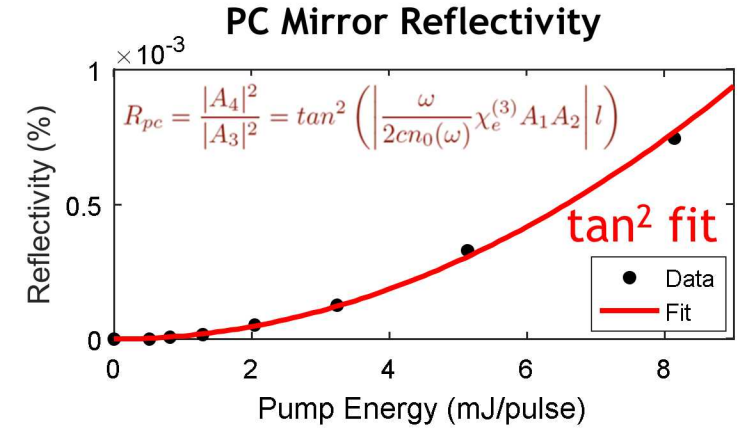
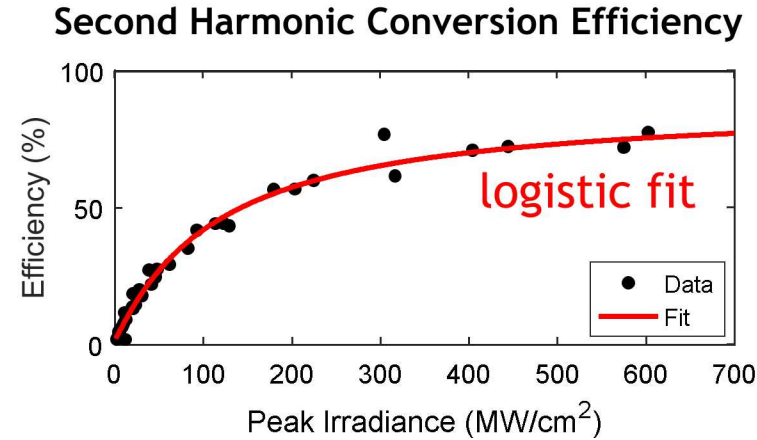
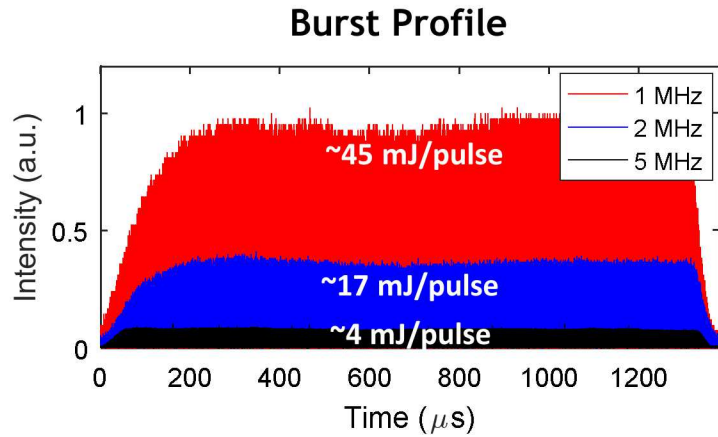
Laser-spark plasma-generated shock-waves (nanosecond pulse burst)



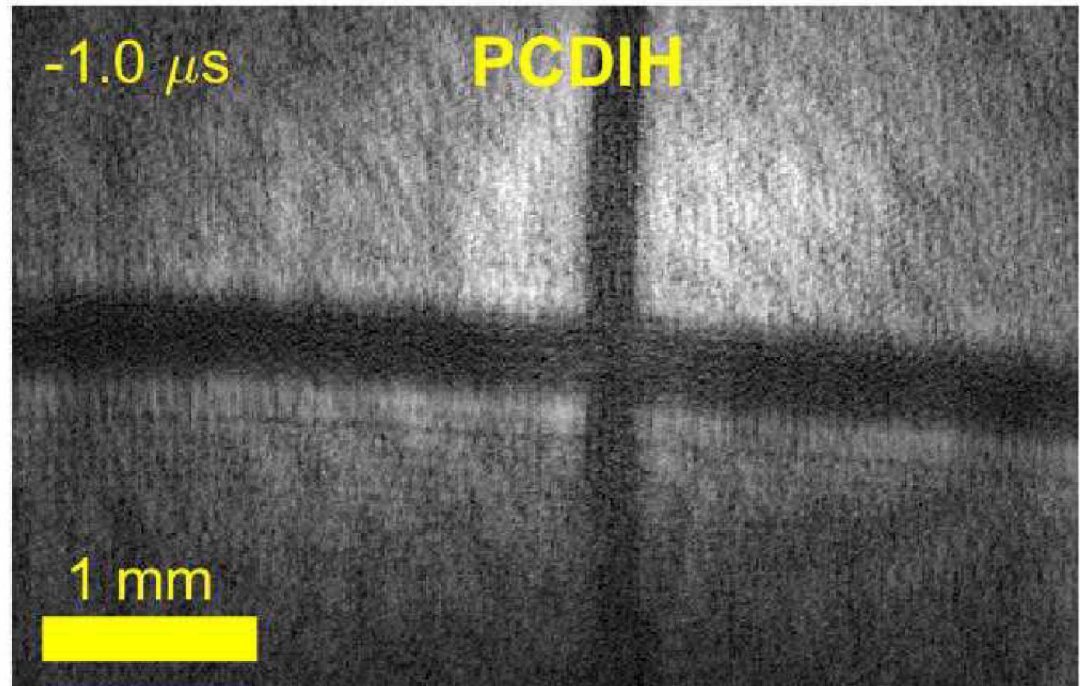
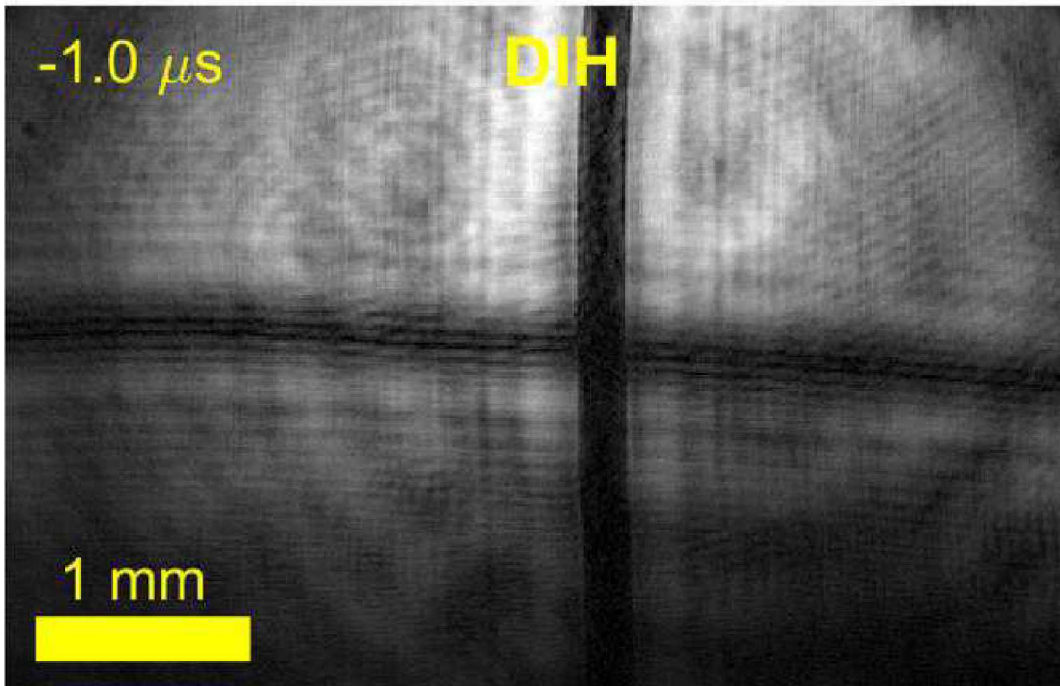
Laser-spark plasma-generated shock-waves (nanosecond pulse burst)

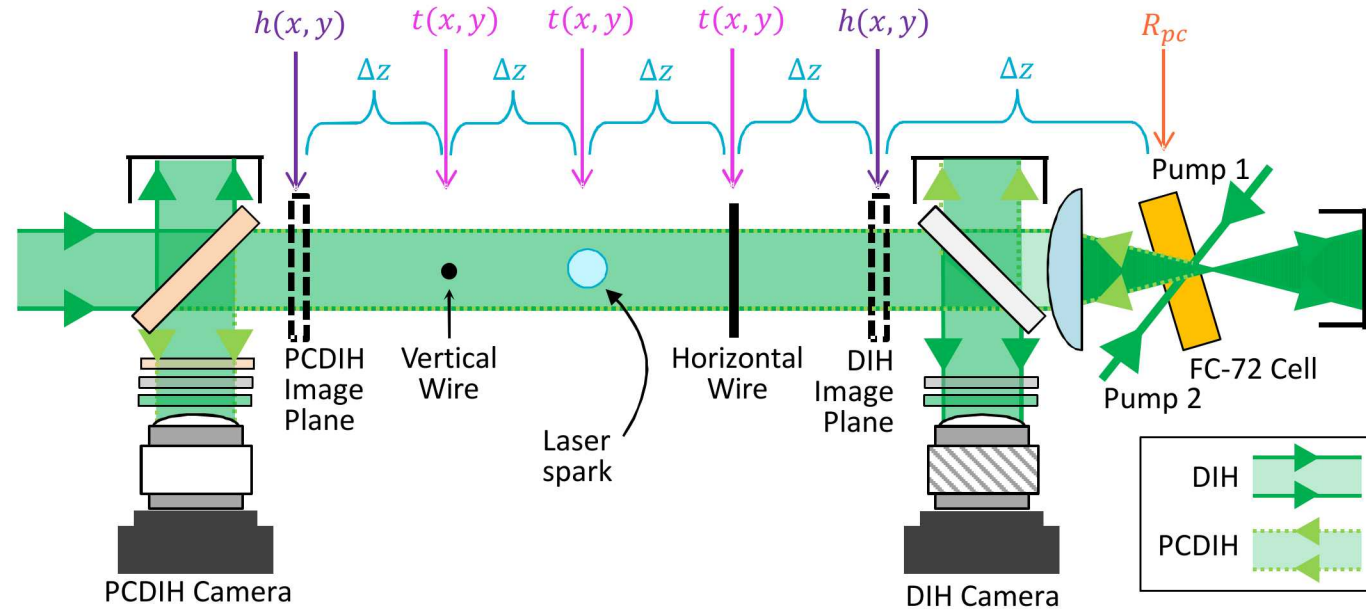


Laser-spark plasma-generated shock-waves (nanosecond pulse burst)



5 MHz Acquisition





$$\text{Coherent light } E_r(x, y) = A_r(x, y)e^{ikz - i\omega t}$$

$$\text{Interaction with object } t(x, y) = e^{-a(x, y) + i\phi(x, y)}$$

$$\text{Diffraction Propagation } E_t(x, y, z) = (E_r(x, y) \cdot t(x, y)) \otimes g_f(x, y, z),$$

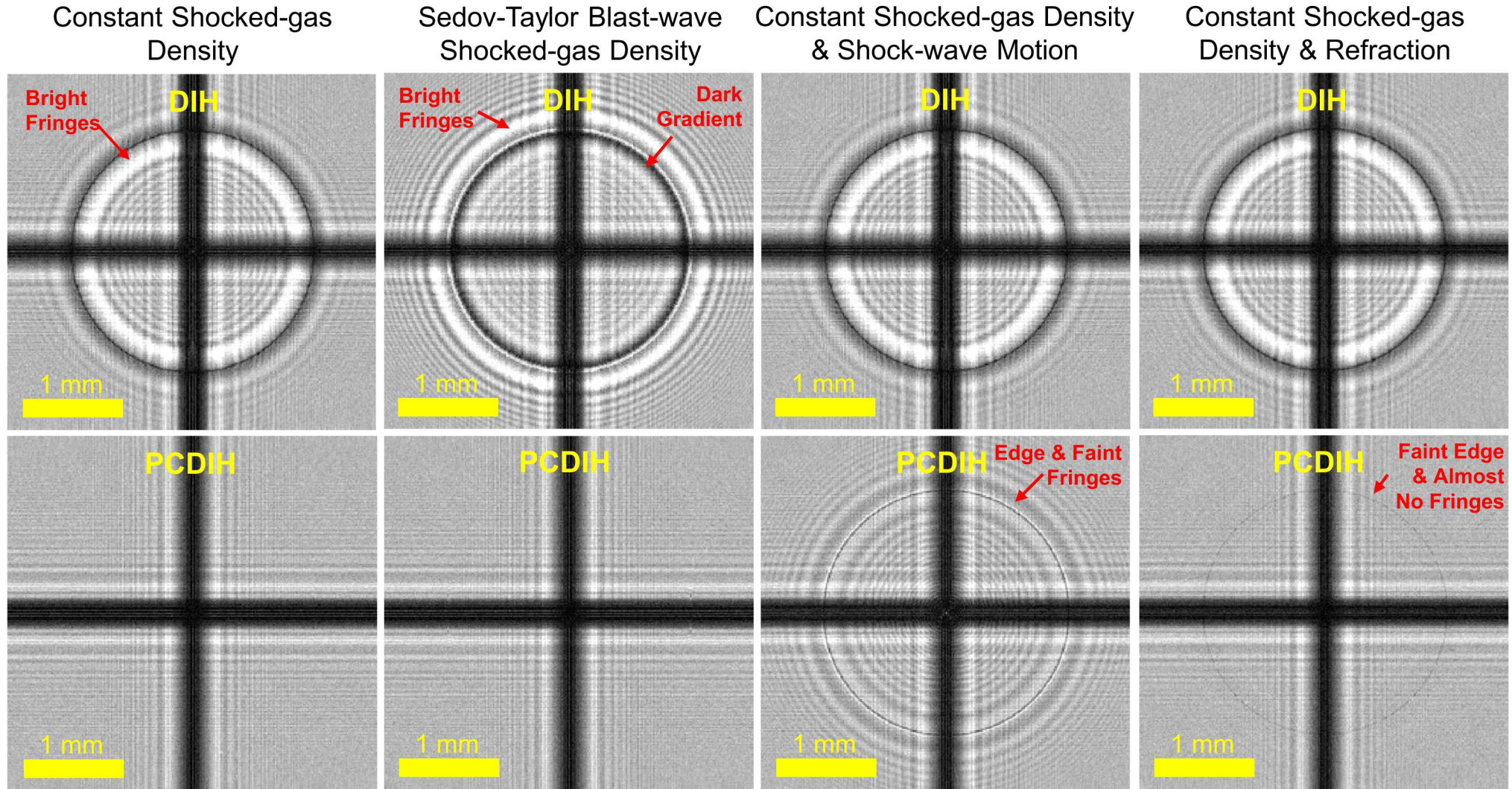
$$\text{where } ig_f = FT^{-1}(G) \text{ and } G = e^{\frac{2\pi iz}{\lambda} \sqrt{1 - (\lambda x)^2 - (\lambda y)^2}}$$

$$\text{Spherical shock-wave phase delay } \phi(x, y) \approx 2\pi R(n_{gas} - n_{air}) / \lambda \sqrt{1 - z^2/R^2}$$

$$\text{Hologram collected at the image plane } z_h \text{ as } h(x, y) = |E_t(x, y, z_h)|^2$$

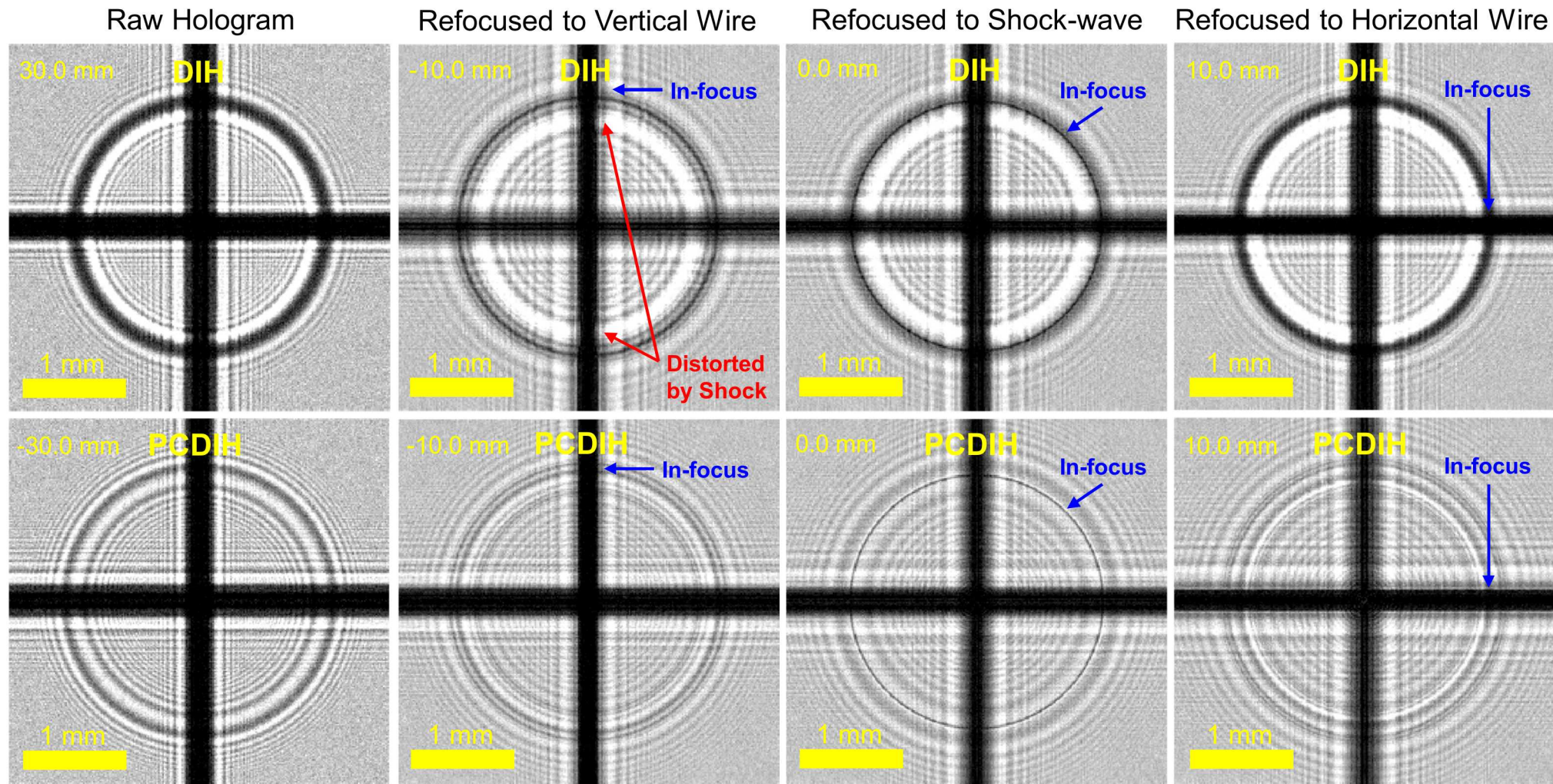
$$\text{Phase conjugate mirror reflection } E_t'' = R_{pc} E_t^*(x, y, z)$$

Shockwave simulations: Interference pattern sources



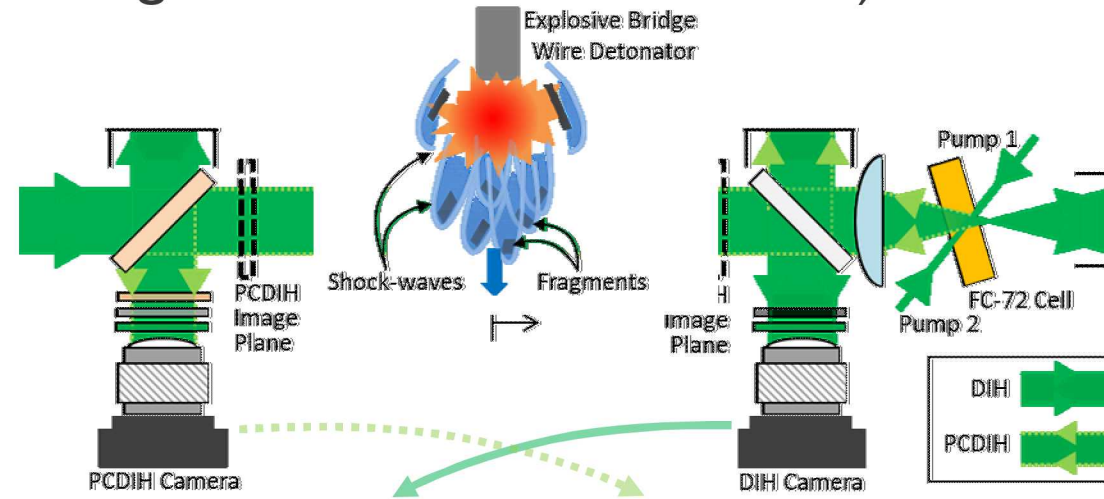
- Shock-wave motion during laser beam time-of-flight (6.8 to 12.8 μm) produces faint fringes
- Small misalignments or beam divergence can cause similar features
- From stationary supersonic shock-wave experiment, we know refraction also plays a role

Shockwave simulations: Refocusing of features

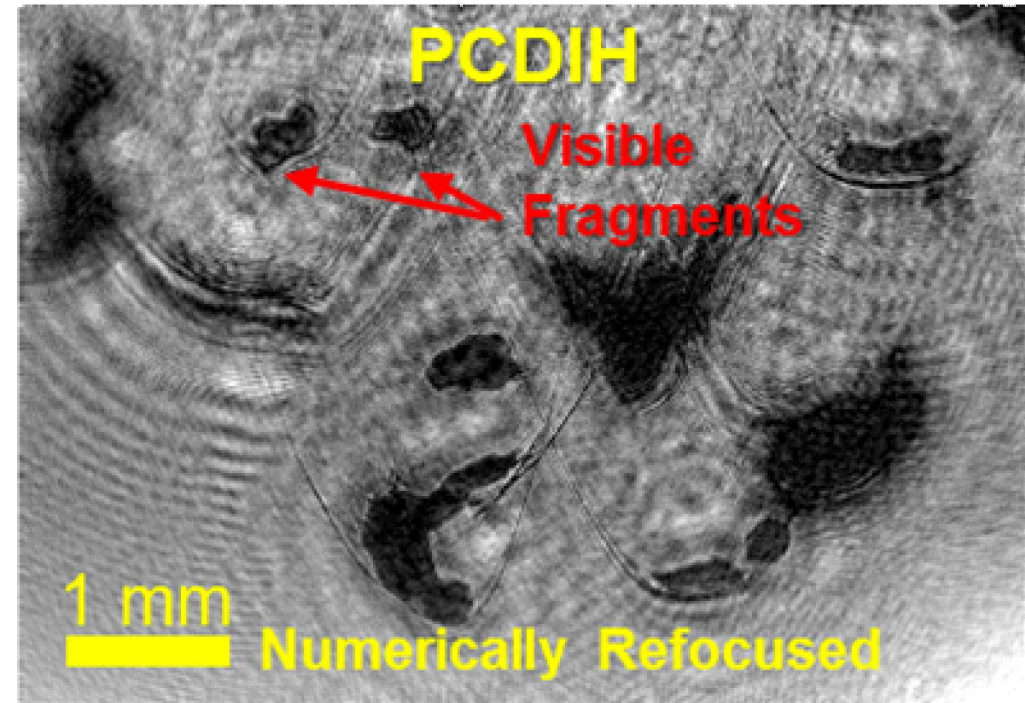
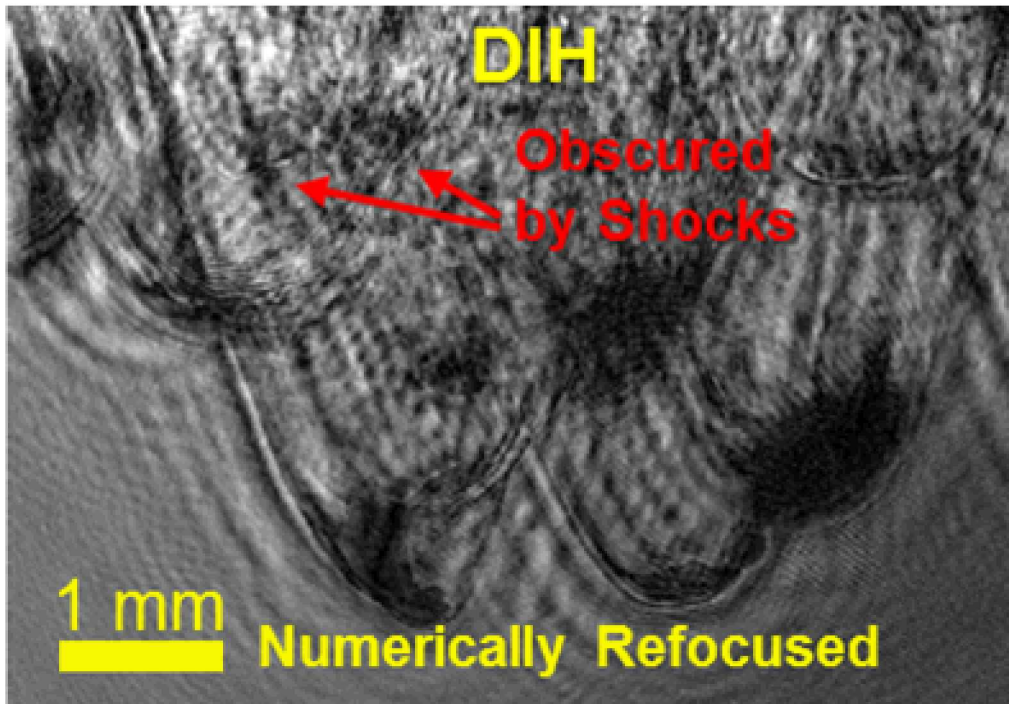


- Combining all the features, we get simulations that are very similar to experimental data
- Refocusable shock-wave edges in DIH and PCDIH
- Wire distortions (mostly on the vertical wire) from shock-wave phase delay due to order of objects

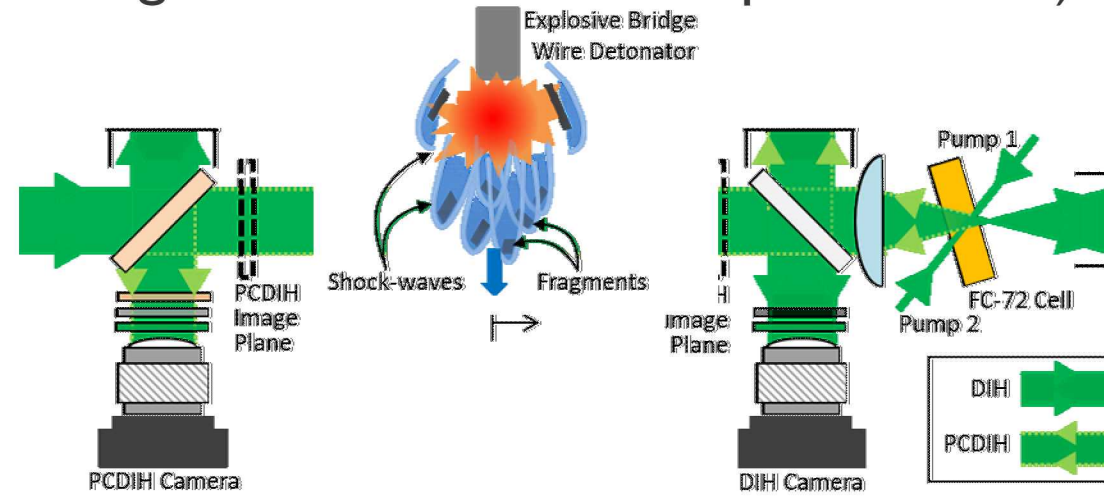
Explosively generated fragments (picosecond laser)



RP-80 EBW from Teledyne RISI
 custom aluminum cap
 Placed 50 mm from field-of-view



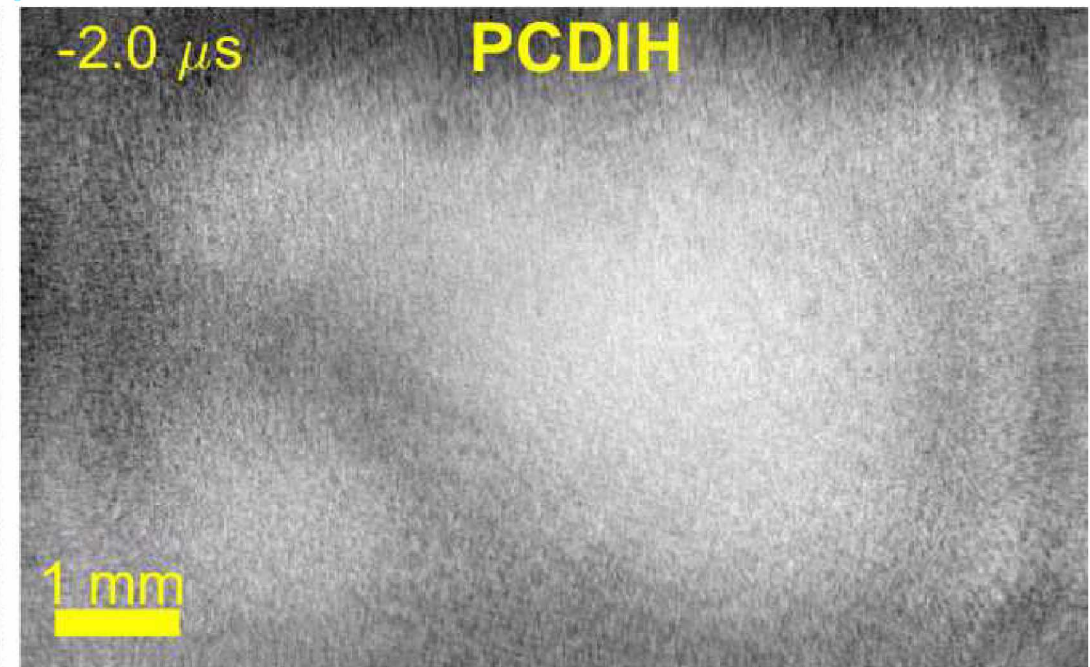
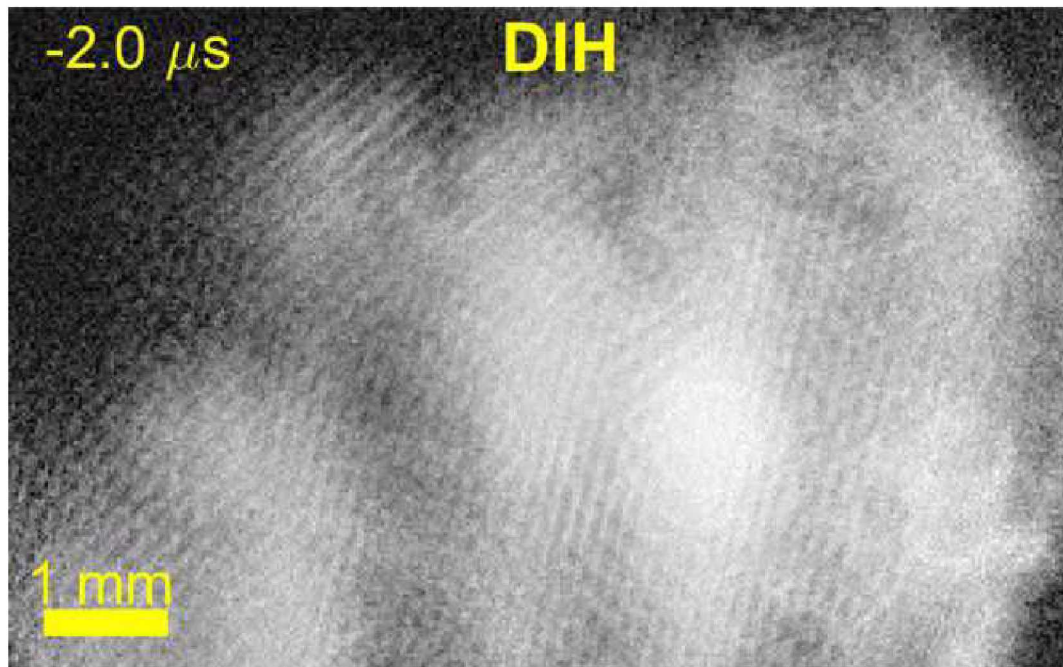
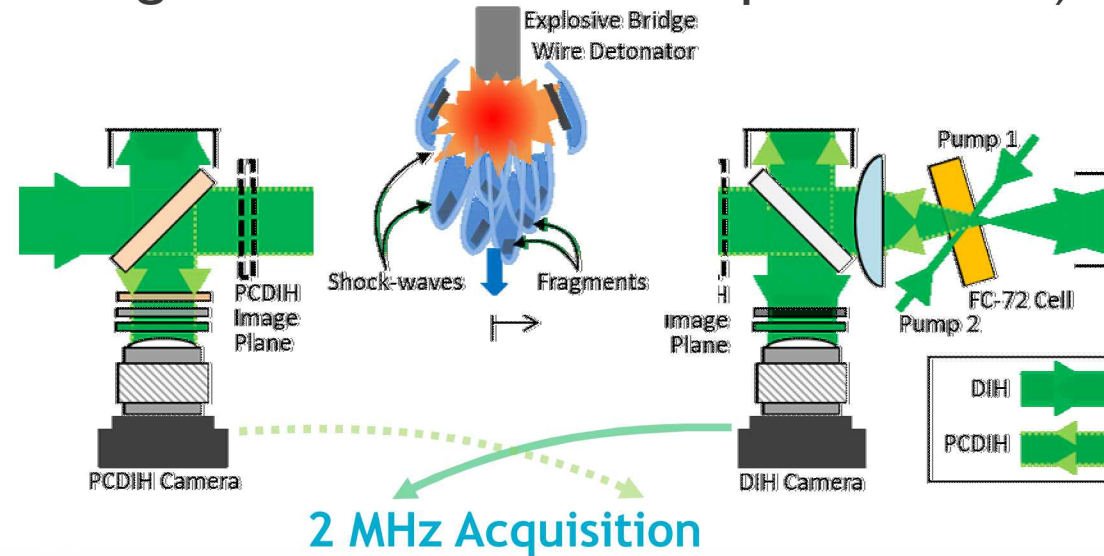
Explosively generated fragments (nanosecond pulse burst)



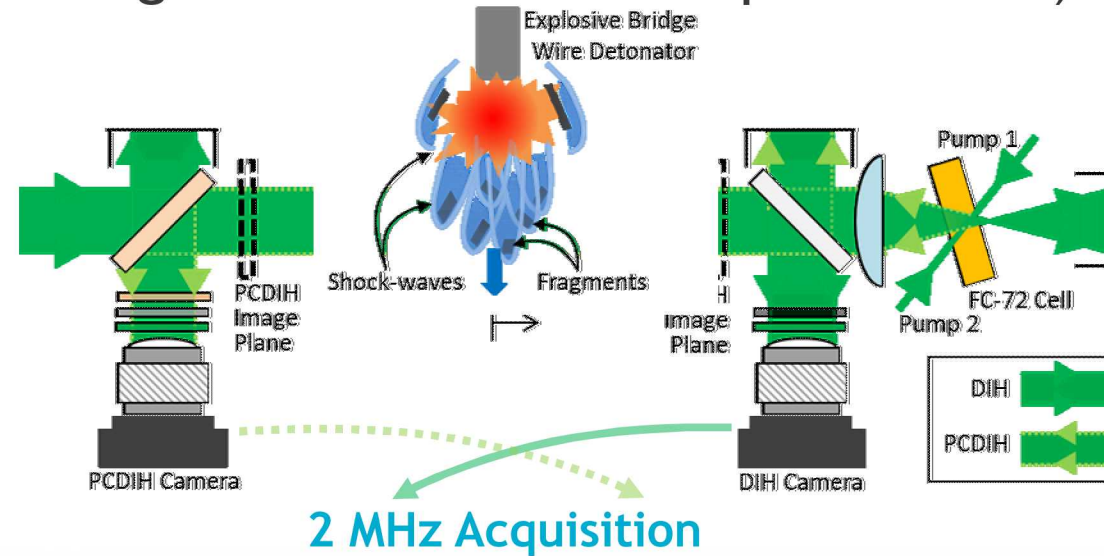
RP-80 EBW from Teledyne RISI
 custom 180 μm thick brass cap
 Placed 50 mm above field-of-view
 facing downward



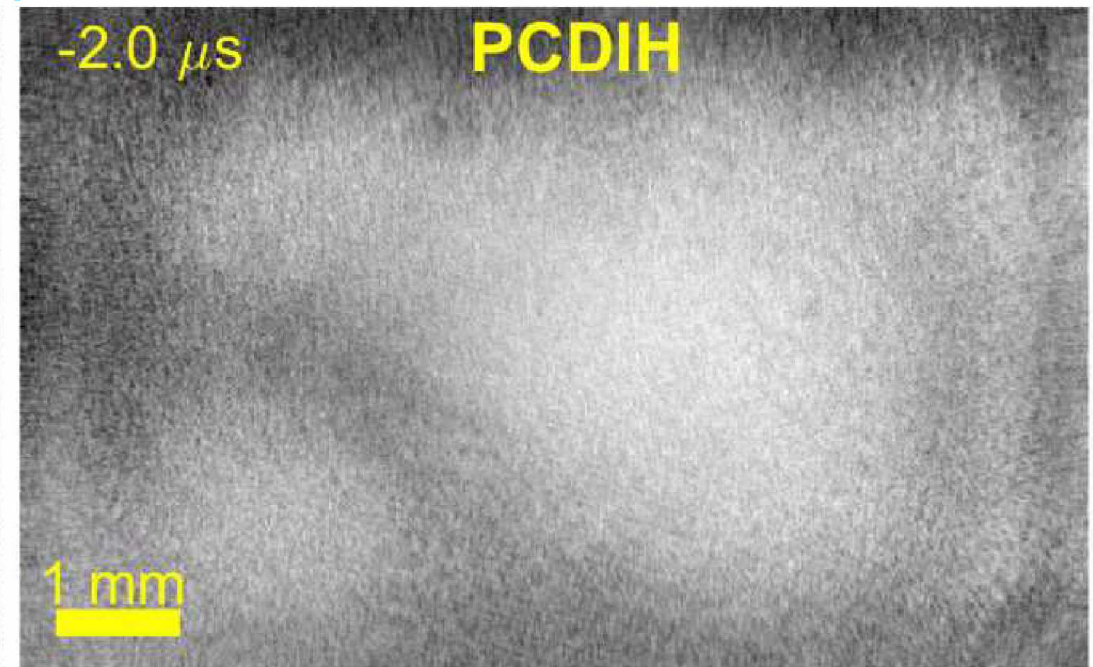
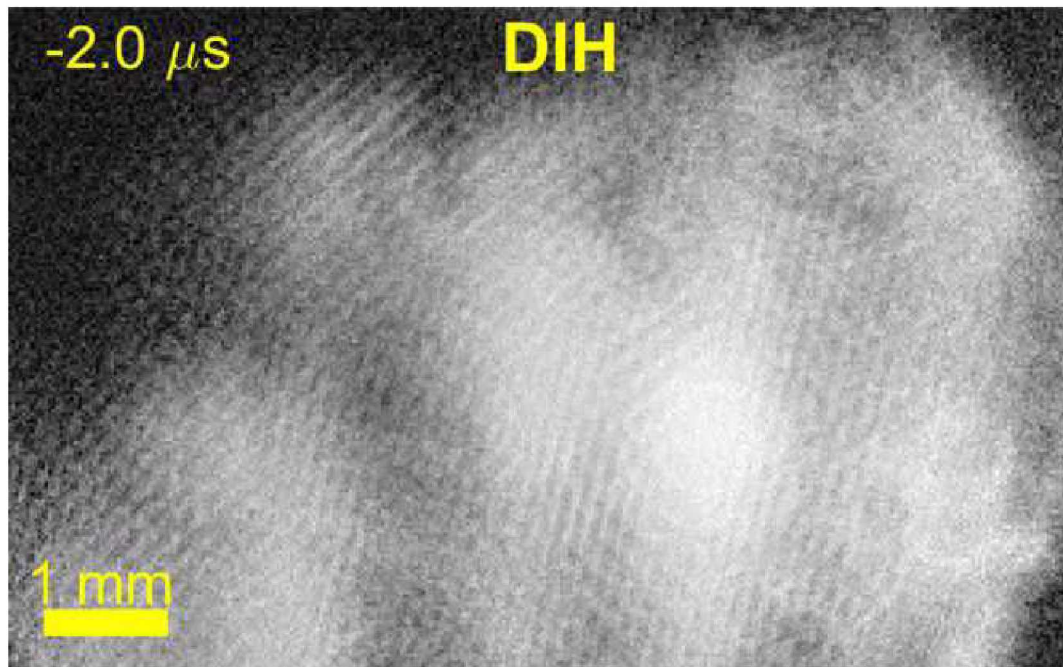
Explosively generated fragments (nanosecond pulse burst)



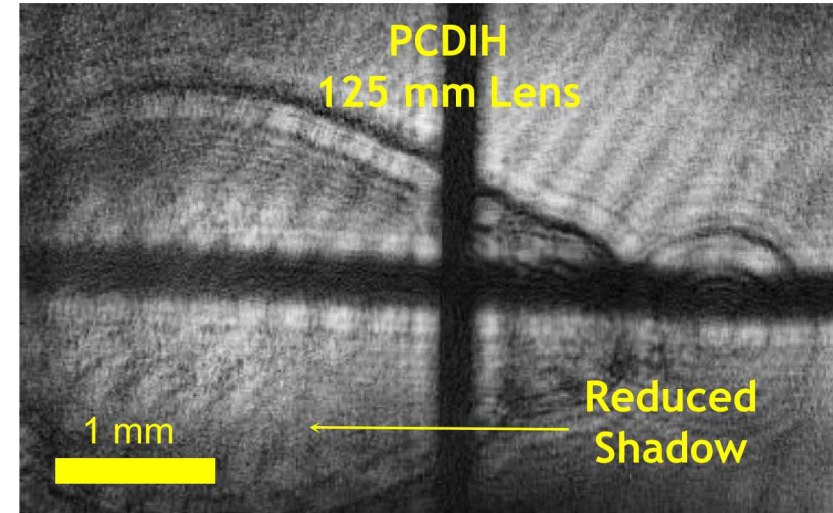
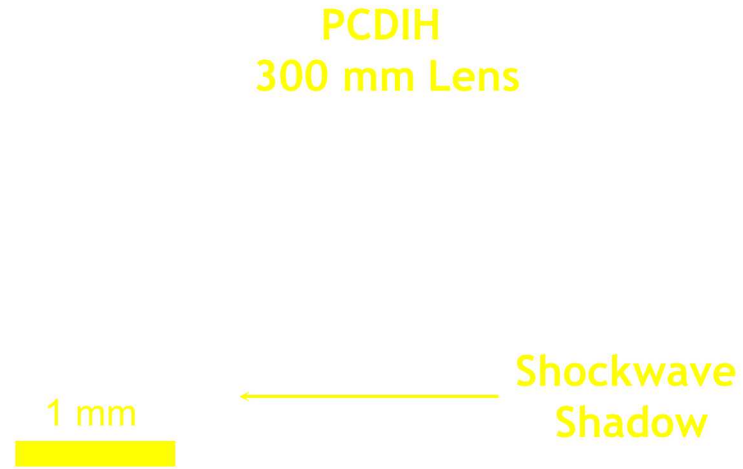
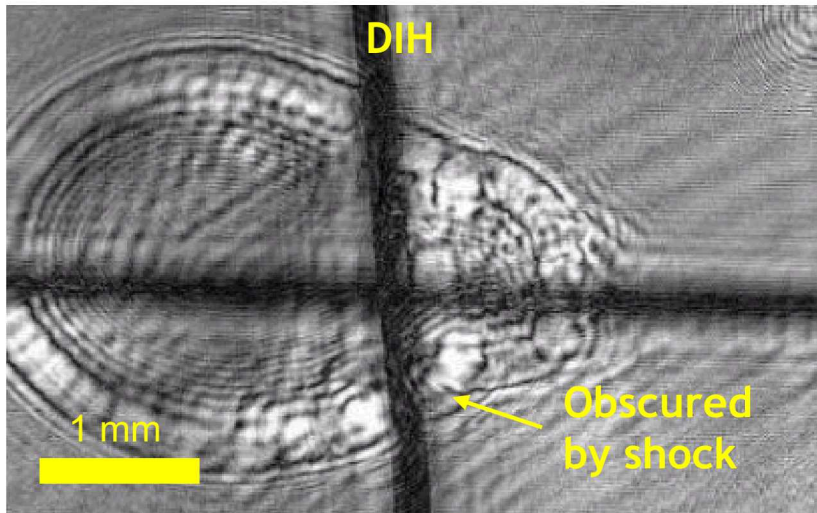
Explosively generated fragments (nanosecond pulse burst)



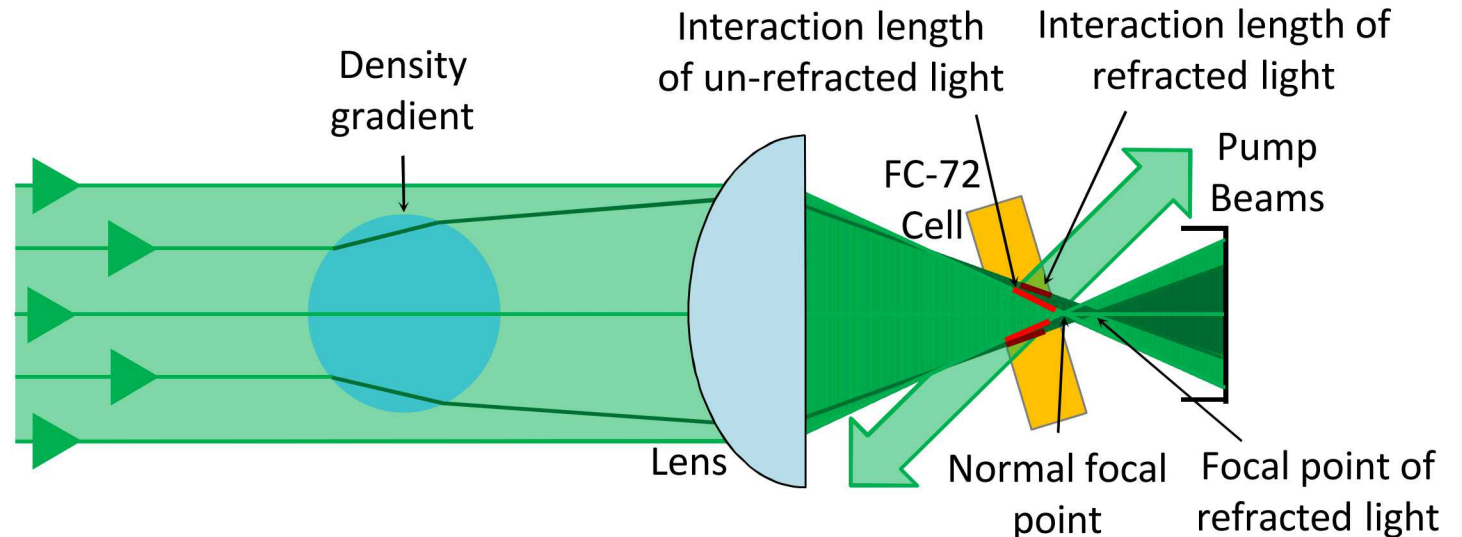
Fragment Speeds:
2.34 to 2.83 km/s
Mach 6.8 to Mach 8.2



Shock-wave edge enhancement (nanosecond pulse burst)

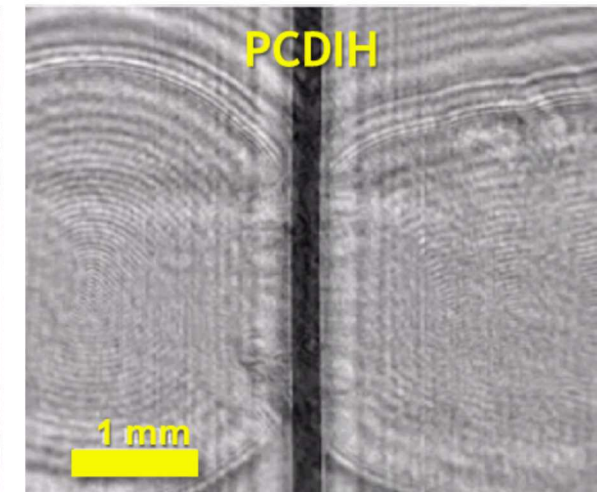
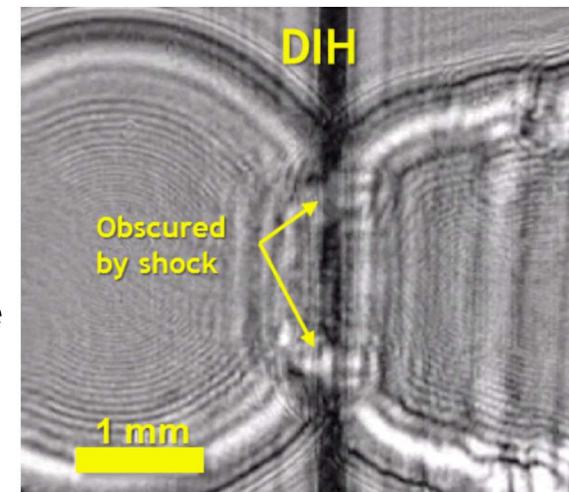
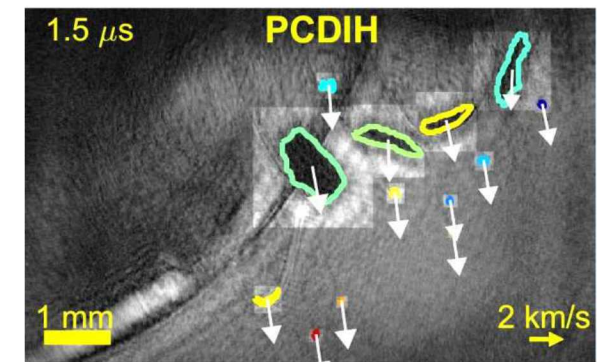
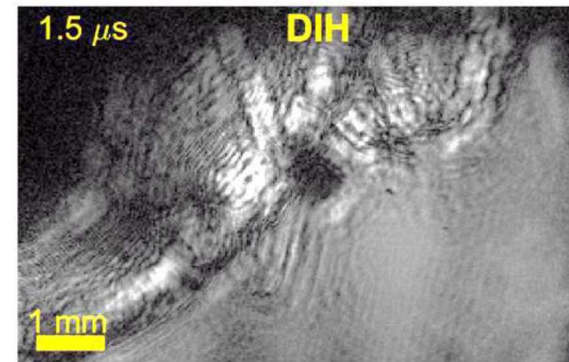
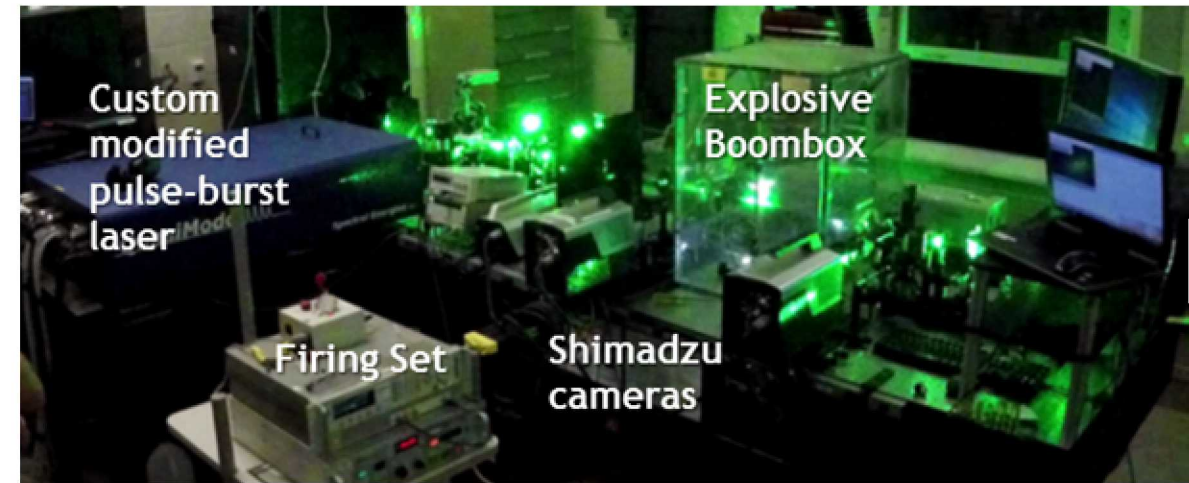


- Shock-wave edges can be enhanced depending on the geometry of the phase conjugate mirror
- Edge enhancement effect is similar to Schlieren or Shadowgraphy except:
 - Effect is nonlinear
 - Shock-wave edge locations can be refocused to find z-position



Conclusions

- Shock-wave phase distortions prevent 3D time-resolved holographic imaging
- We introduce ultra-high-speed PCDIH for phase-distortion canceled 3D imaging and object tracking using only one line of sight
- Custom modified nanosecond pulse-burst laser and ultra-high-speed cameras were used
- Demonstrated up to 5 orders-of-magnitude increase in speed from 10-20 Hz up to 5 MHz
- Fastest digital in-line holograms collected to date
- Experiments were conducted on:
 - Stationary supersonic shock-waves
 - Laser-spark plasma-generated shock-waves
 - Explosively generated fragments
- Simulations show that:
 - Object and phase delay order determines degree of distortion
 - Shock-wave edges are visible and refocusable in PCDIH due to shock-wave motion and refraction



Acknowledgements

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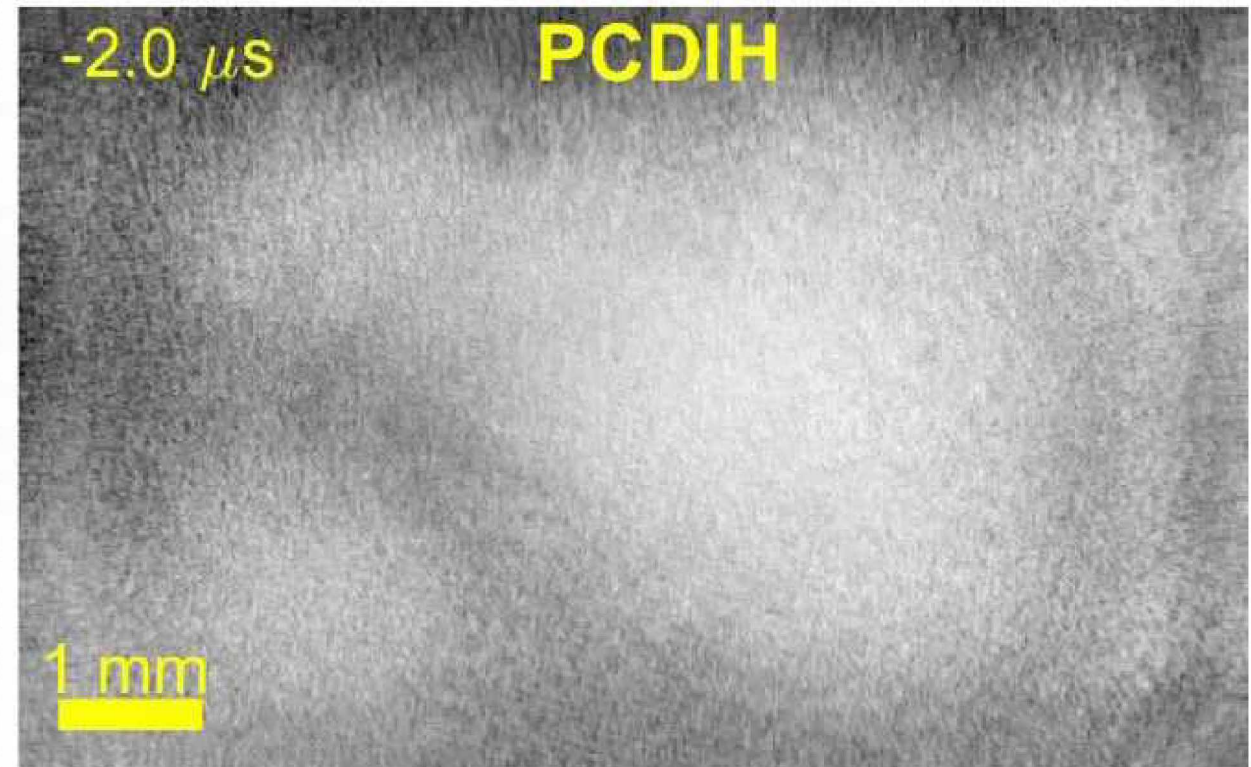
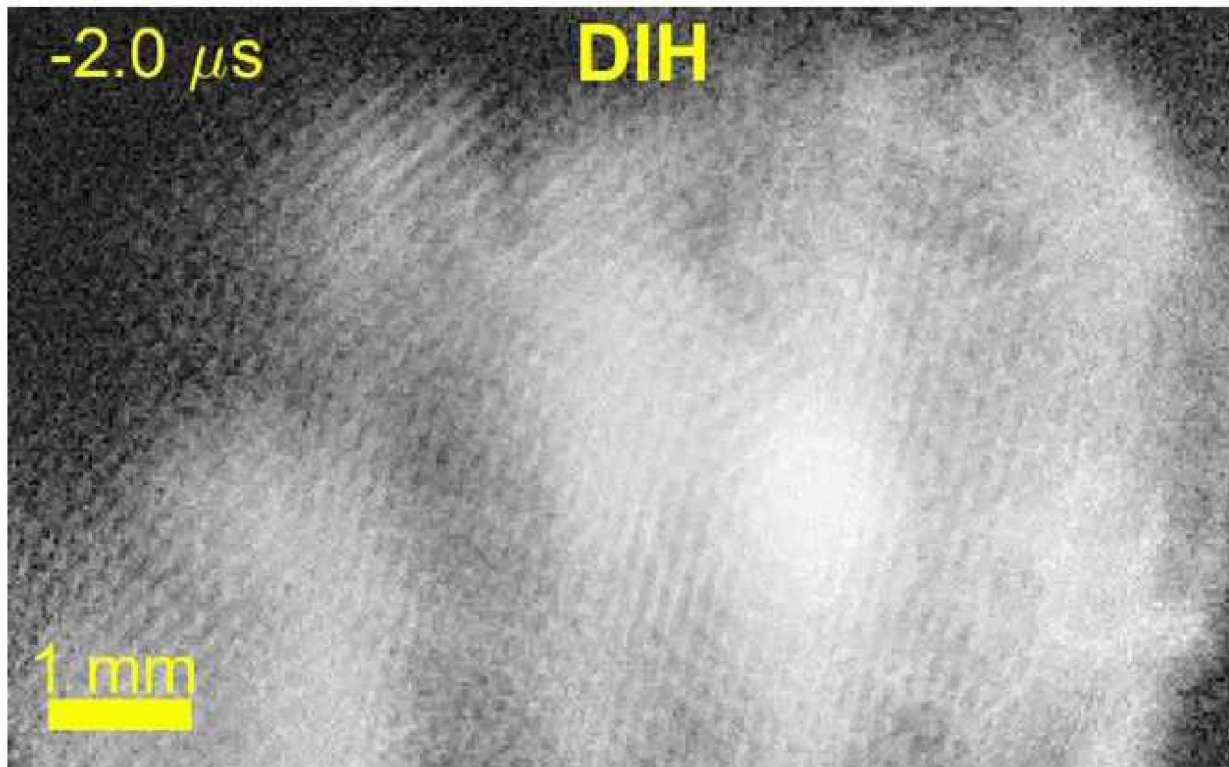
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Questions?

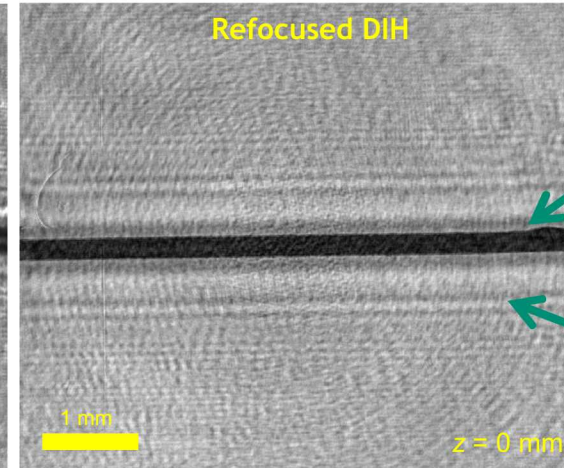
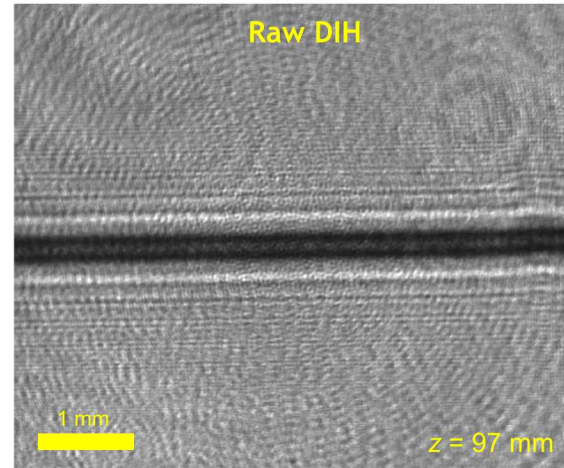
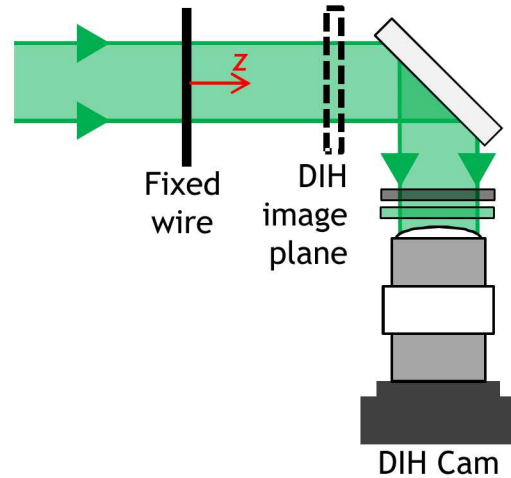
DIH versus PCDIH





Additional Backup Slides





In-focus
hologram with
sharp edges

Diffraction
patterns from
“virtual image”

- Digital In-line holograms (Gabor 1948) are collected out-of-focus and are later numerically refocused

- Holograms are generated

- When coherent light $E_r(x, y) = A_r(x, y)e^{ikz - i\omega t}$ passes over a diffractive object with transmission $t(x, y) = e^{-a(x, y) + i\phi(x, y)}$
- Fresnel-Kirchhoff diffraction can be used as $E_t(x, y, z) = (E_r(x, y) \cdot t(x, y)) \otimes g_f(x, y, z)$
- Where the diffraction kernel is $g_f = FT^{-1}(G)$ where $G = e^{\frac{2\pi iz}{\lambda} \sqrt{1 - (\lambda x)^2 - (\lambda y)^2}}$

- Holograms are collected at the image plane z_h as $h(x, y) = |E_t(x, y, z_h)|^2$

- Holograms are numerically refocused

- Using $E_h(x, y, z) = [h(x, y)E_r^*(x, y)] \otimes g_b(x, y, z)$ where $g_b = FT^{-1}(G^*)$
- The amplitude is determined from $A_h = |E_h|$
- In-focus z-planes are determined using maximum edge sharpness and minimum amplitude criteria.

Hologram
Generation
Process

Hologram
Refocusing
Process

