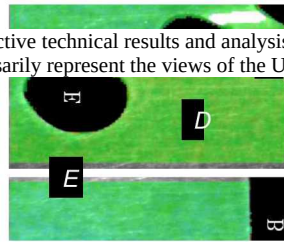
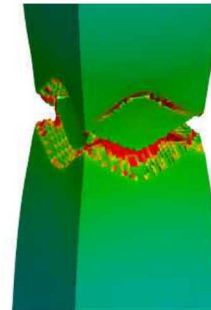
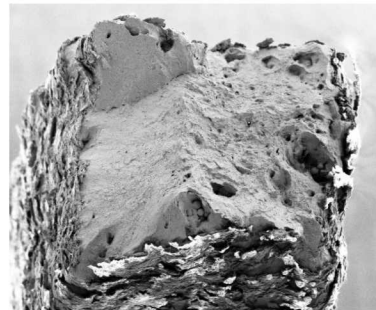
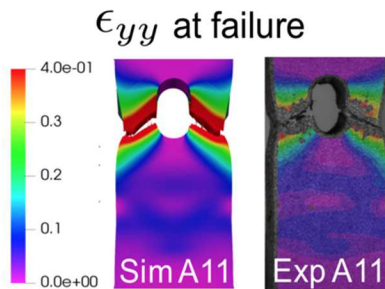
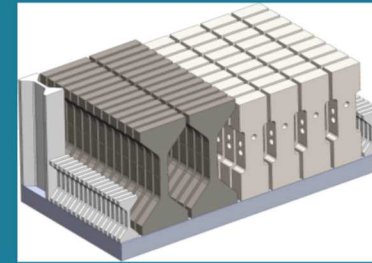


This paper describes objective technical results and analysis. Any subjective views or opinions that might be expressed in the paper do not necessarily represent the views of the U.S. Department of Energy or the United States Government.



SAND2018-13109C

Exploration of Anisotropic Plasticity Models



PRESENTED BY

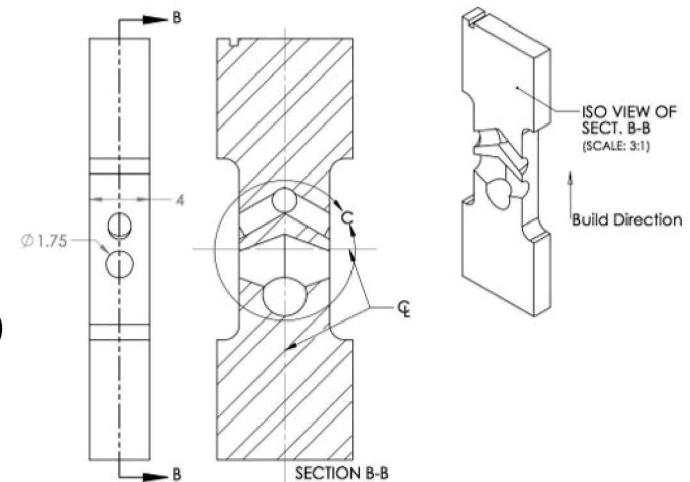
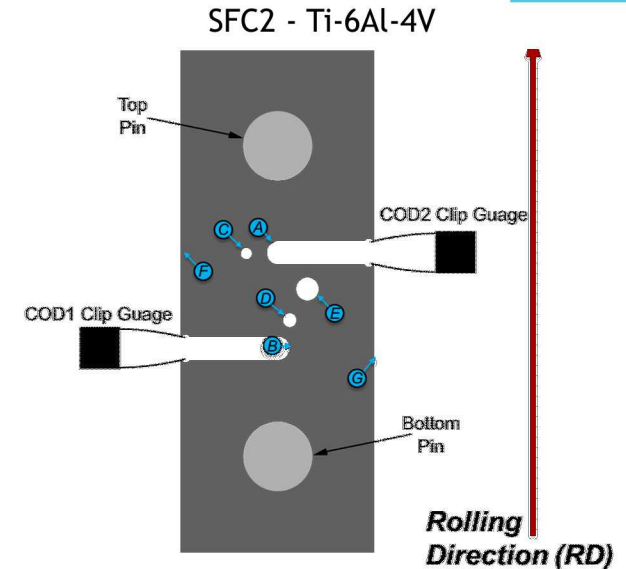
C. Alleman, J. Foulk, K. Karlson, K. Manktelow,
J. Ostien, M. Stender, A. Stershic, M. Veilleux, A. Brown



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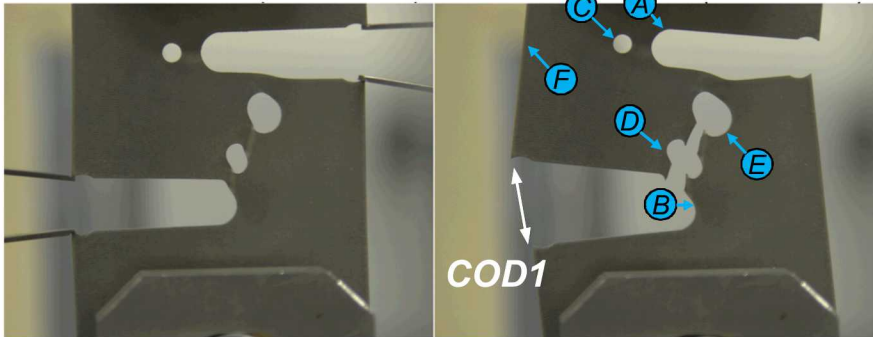
Motivation

- Structural alloy used in engineering applications come in various product forms
 - Rolled plate
 - Forged
 - Sheet
 - Additively Manufactured (AM)
- Worked alloys result in anisotropic plastic response and can have significant performance departures from isotropic and/or annealed material
 - Particularly in terms of localization and failure
 - Creates calibration challenges
- This work is an exploration of the relative importance of using anisotropic yield strength for two structural alloys
 - Case study 1: Ti-6Al-4V - quasistatic and dynamic loading (SFC2)
 - Case study 2: AM SS317L - quasistatic loading (SFC3)



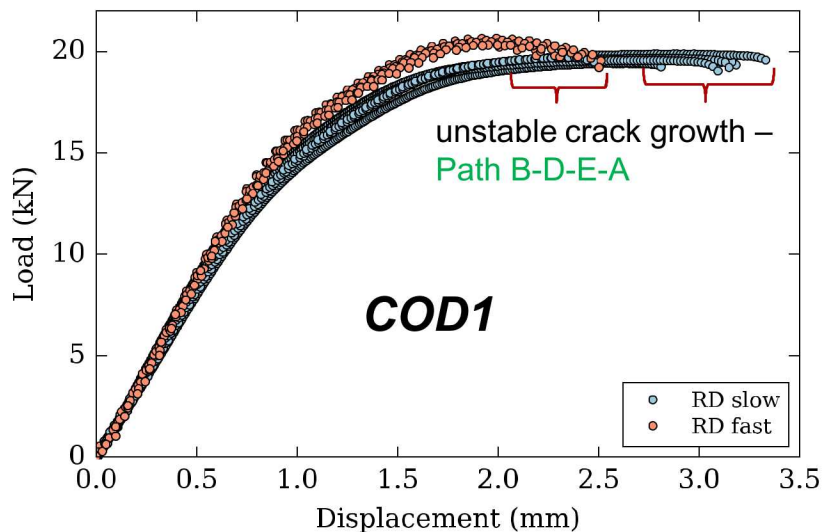
SFC3 - AM 316L

Case Study: Sandia Fracture Challenge 2



A single specimen failed with Path A-C-F
 All others failed B-D-E-A

**Caused by sample defects.
 Out-of-plane warpage.**

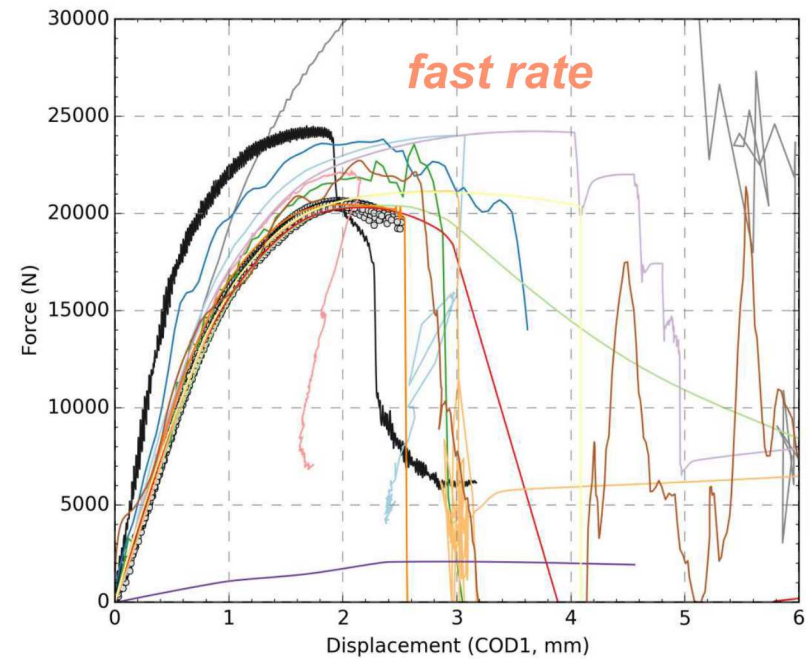


Where will the failure occur?

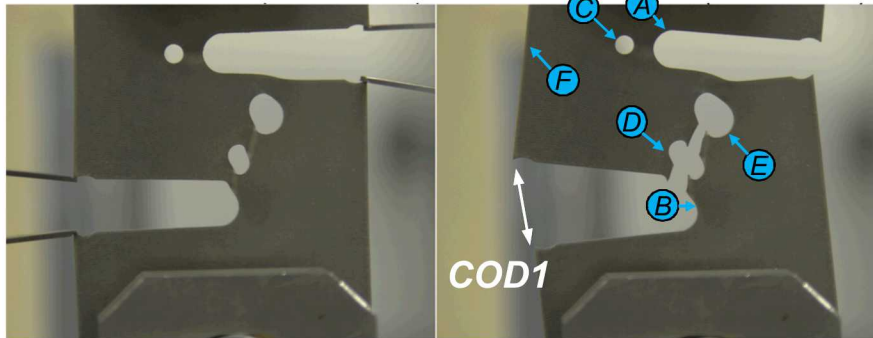
- 2 teams predicted wrong failure path or could not decide
- 4 teams predicted B-D-E-A or A-C-F as possible failure paths
- 9 teams predicted B-D-E-A as only failure path

How did it fail?

- Most teams predict unstable crack growth
- 2 did not

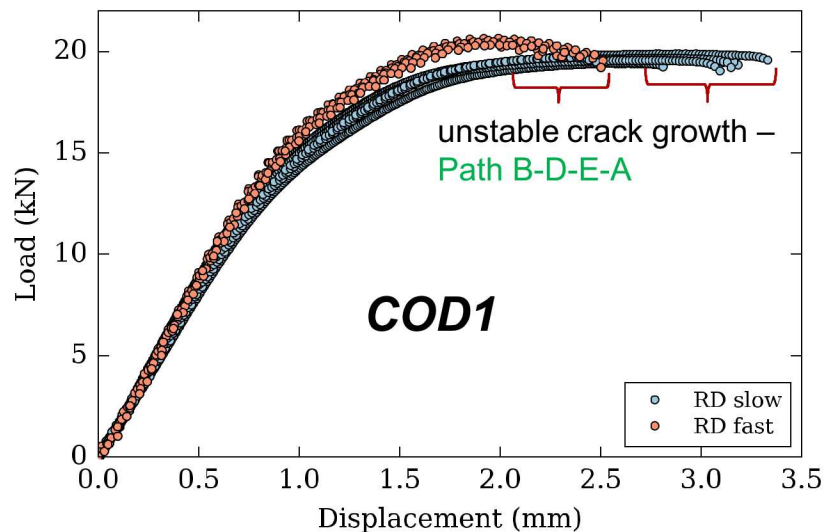


Case Study: Sandia Fracture Challenge 2



A single specimen failed with Path A-C-F
 All others failed B-D-E-A

↓
Caused by sample defects.
Out-of-plane warpage.

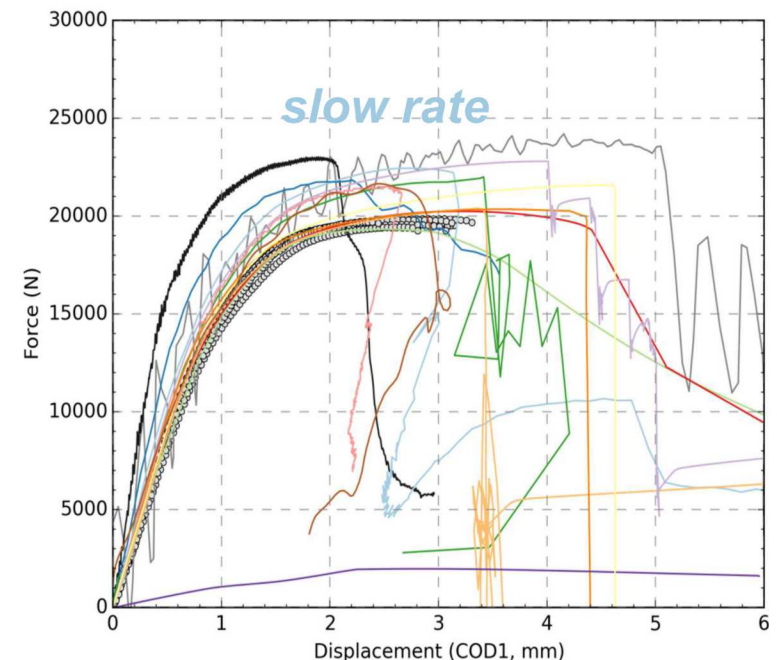


Where will the failure occur?

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- 9 teams predicted B-D-E-A as only failure path

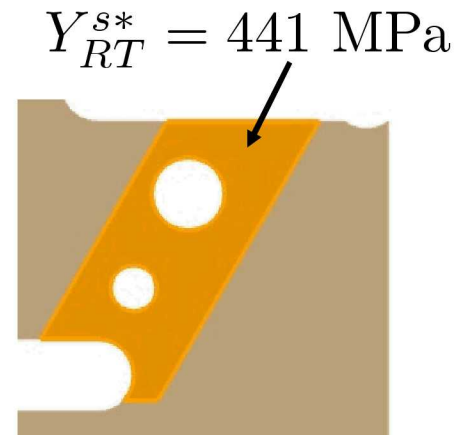
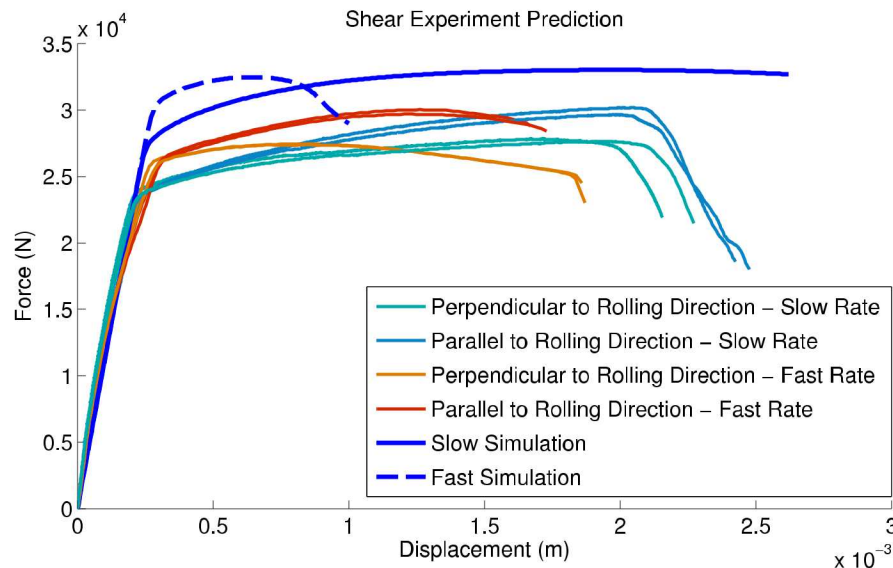
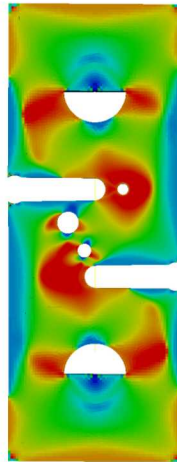
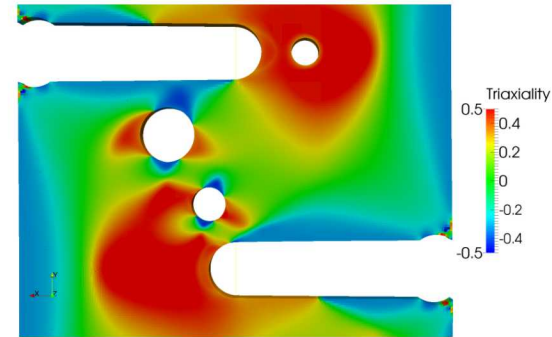
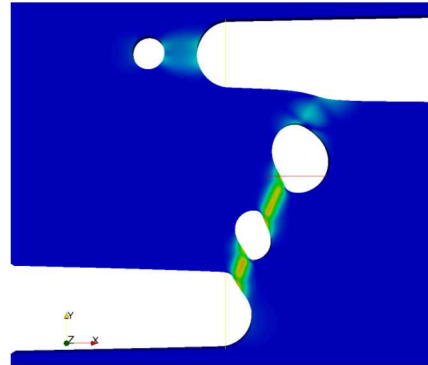
How did it fail?

- Most teams predict unstable crack growth
- 2 did not



Case Study: Sandia Fracture Challenge 2

- Including anisotropy
- Shear data is not captured by isotropic yield surface
- ~13% overprediction
- Lacking an anisotropic model a region experiencing shear used a lower strength

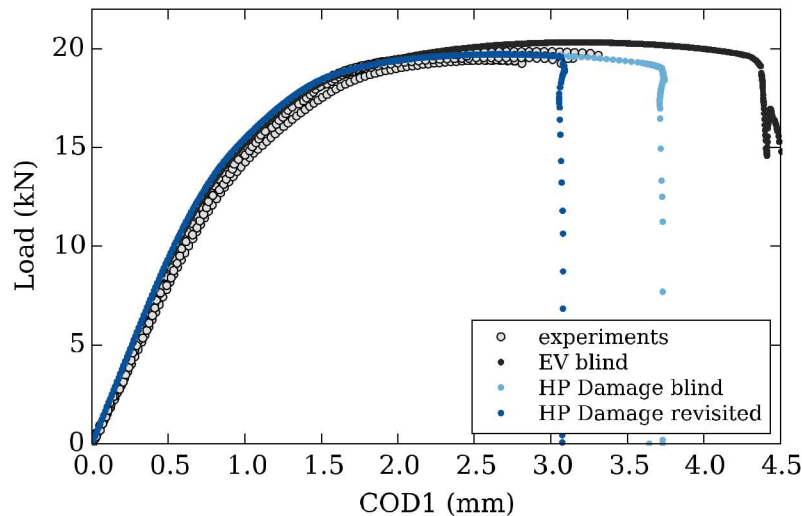


Case Study: Sandia Fracture Challenge 2

EV damage model

$$\dot{\phi} = \sqrt{\frac{3}{2}} \dot{\epsilon}_p \frac{1 - (1 - \phi)^{m+1}}{(1 - \phi)^m} \sinh \left[\frac{2(2m - 1)}{2m + 1} \frac{\langle \frac{I_1}{3} \rangle}{\sqrt{3J_2}} \right]$$

$$\dot{\eta} = \eta \dot{\epsilon}_p N_1 \left[\frac{4}{27} - \frac{J_3^2}{J_2^3} \right]$$

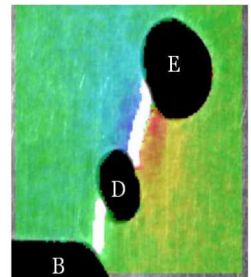
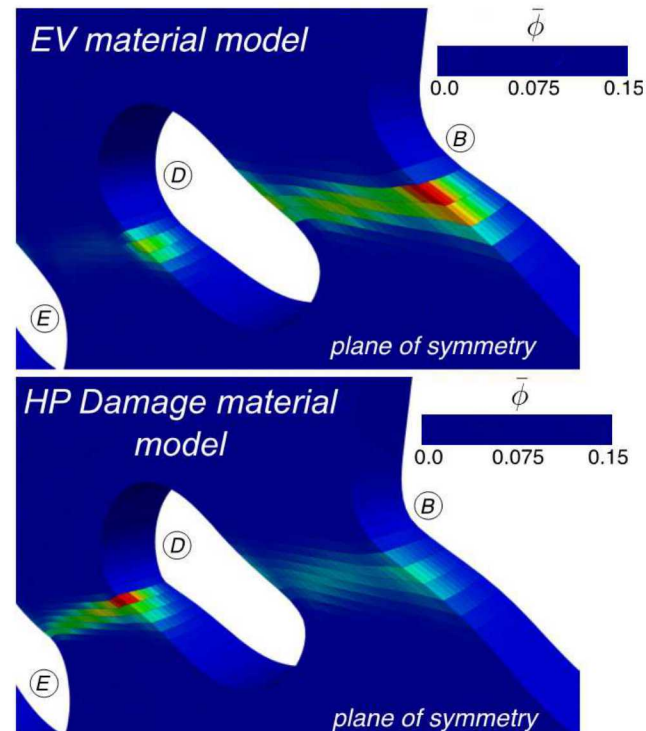


+

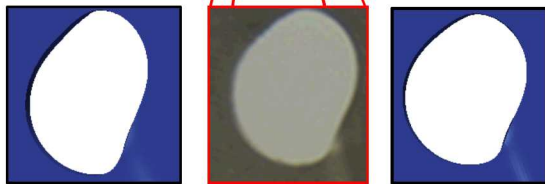
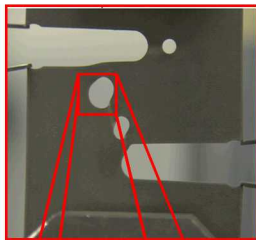
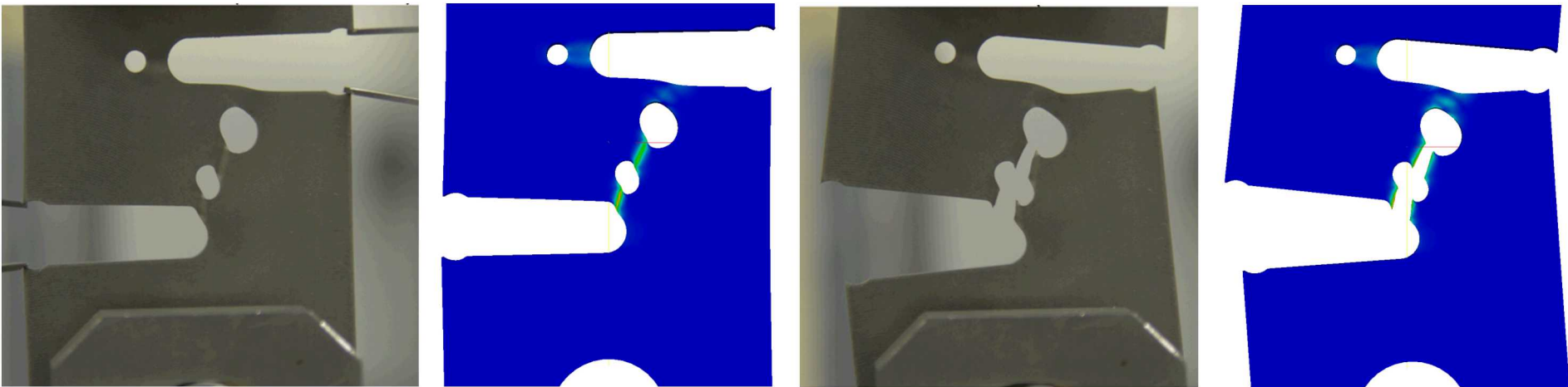
Hill yield surface

$$f_Y^2(\sigma_{ij}) \equiv F(\sigma_{22} - \sigma_{33})^2 + G(\sigma_{33} - \sigma_{11})^2 + H(\sigma_{11} - \sigma_{22})^2 + 2L\sigma_{23}^2 + 2M\sigma_{31}^2 + 2N\sigma_{12}^2 = \bar{\sigma}_e^2(\epsilon_p)$$

→ **HP Damage material model**



Case Study: Sandia Fracture Challenge 2



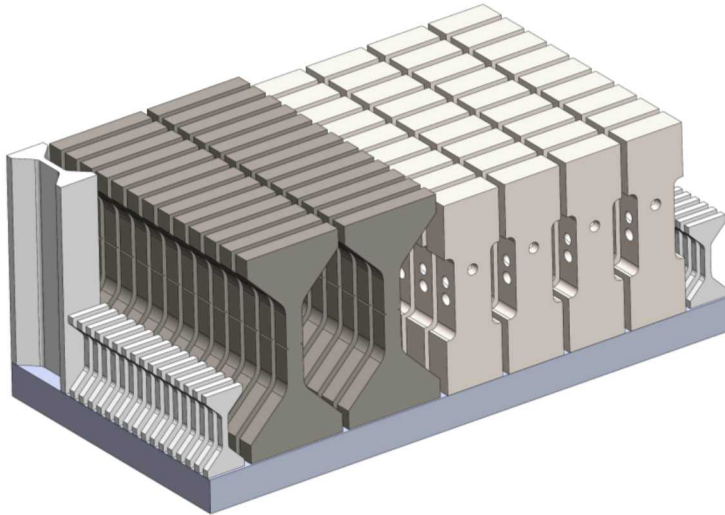
J₂ model

HP Damage model

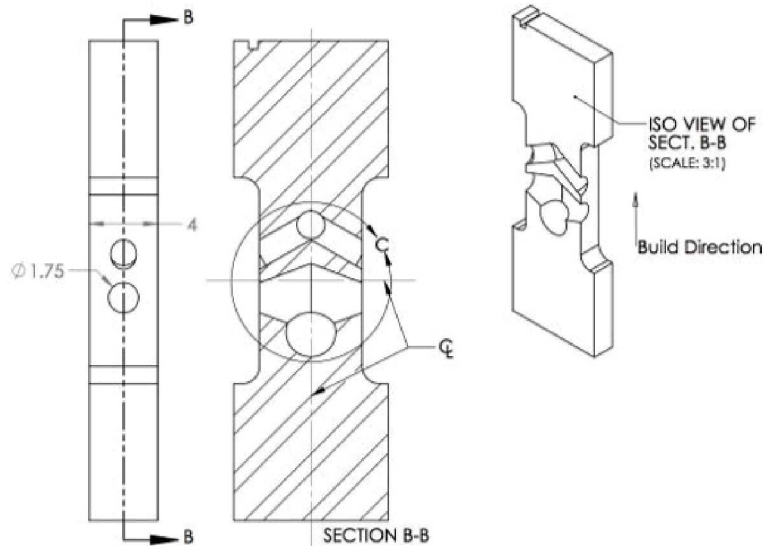
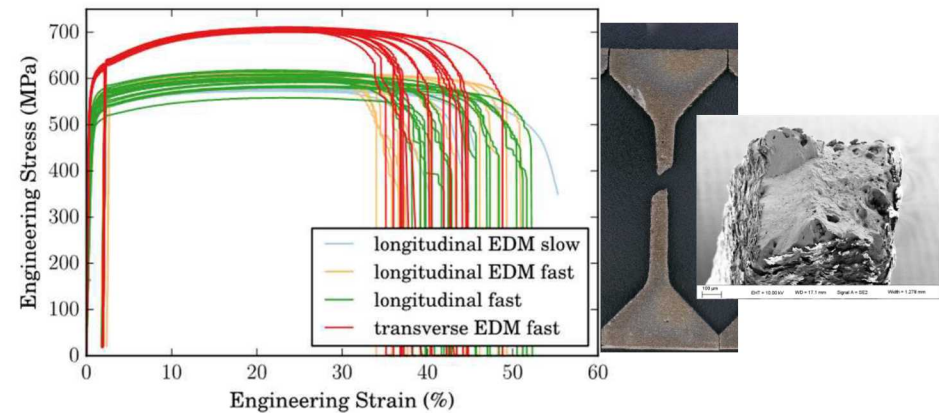
- Lessons learned from this modeling exercise
 - Isotropic yield, even with rate and temperature dependence produced an incorrect fracture path
 - Looking at rate and temperature independent anisotropic yield (Hill) improved localization location predictions
 - Sensitivity studies demonstrate importance of temperature, damage models
 - *Need anisotropy AND rate dependence AND damage AND temperature dependence!!*

Case Study: Sandia Fracture Challenge 3

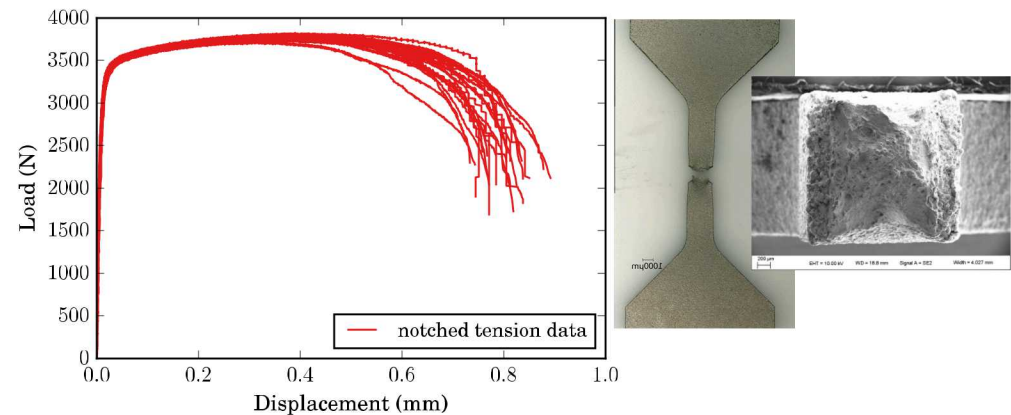
- Additively Manufacture 316L



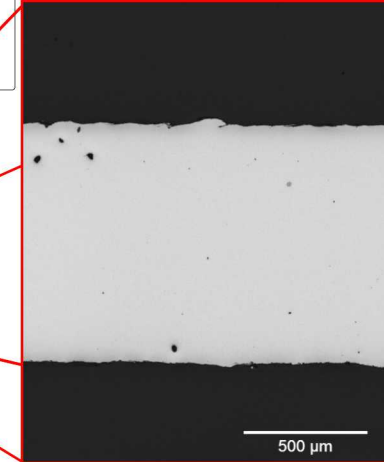
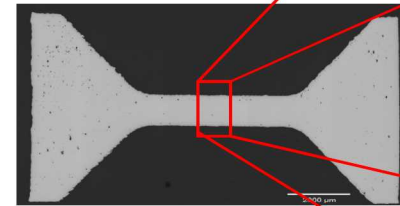
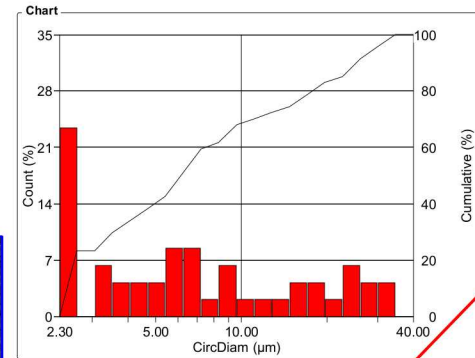
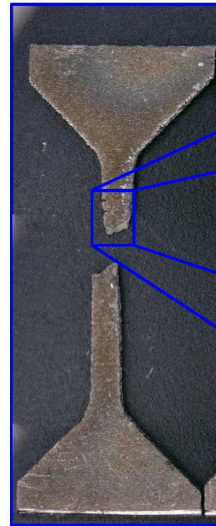
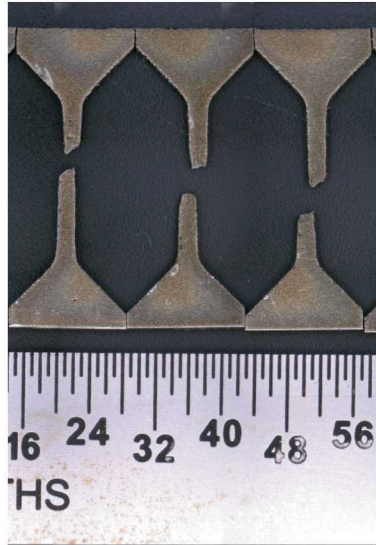
tension tests



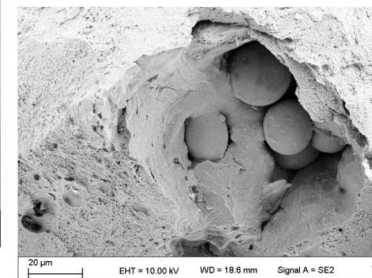
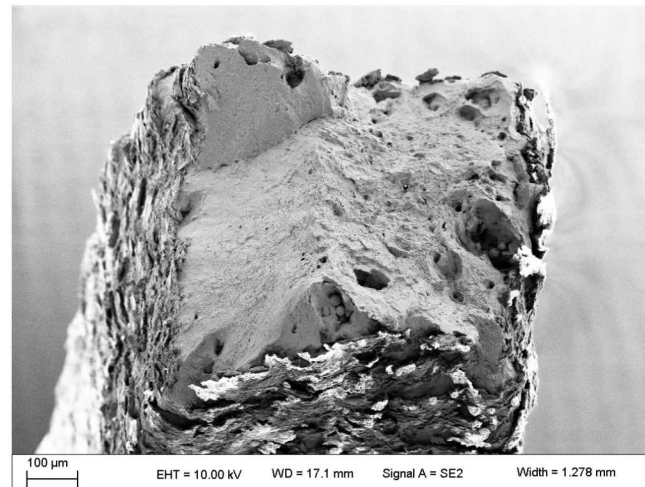
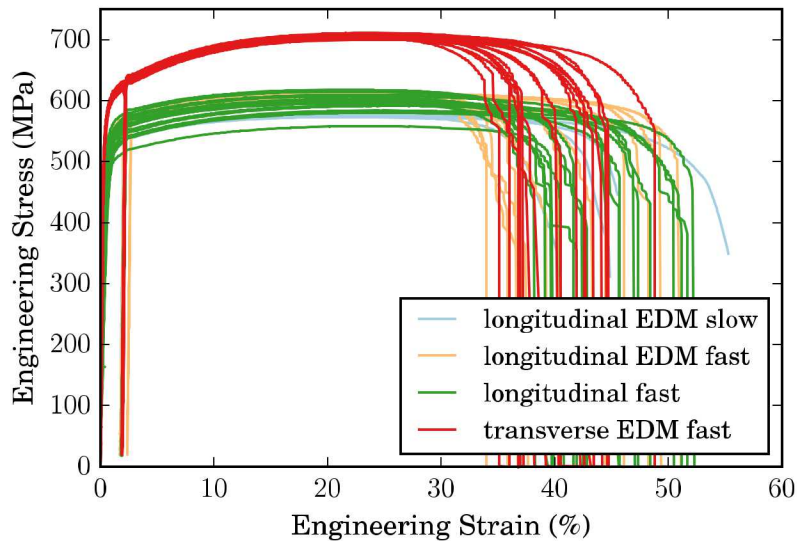
notched tension tests



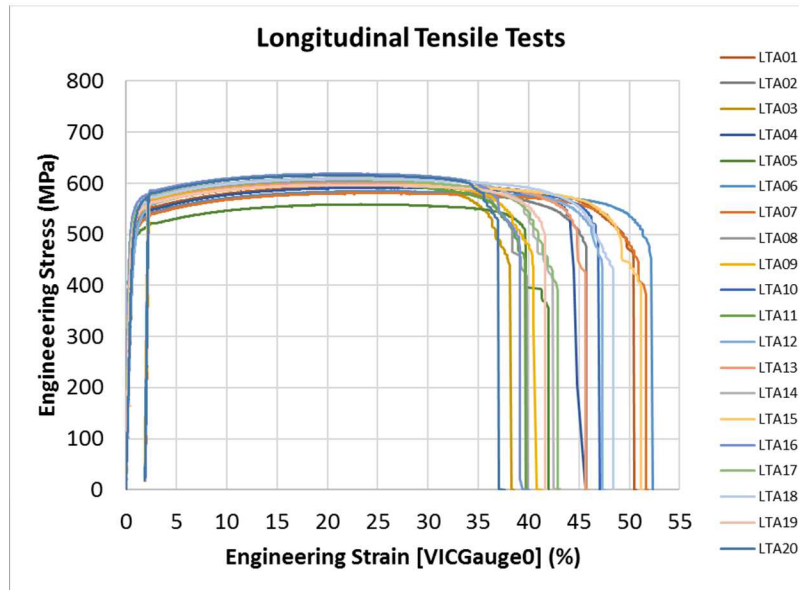
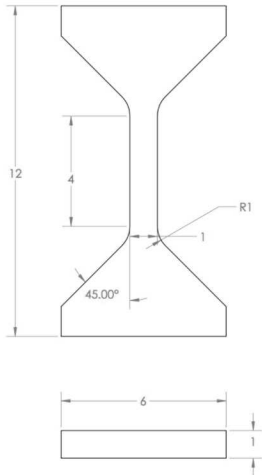
SFC3: Tension data



surface defects (cracks) internal defects (voids)



SFC3: Tension data

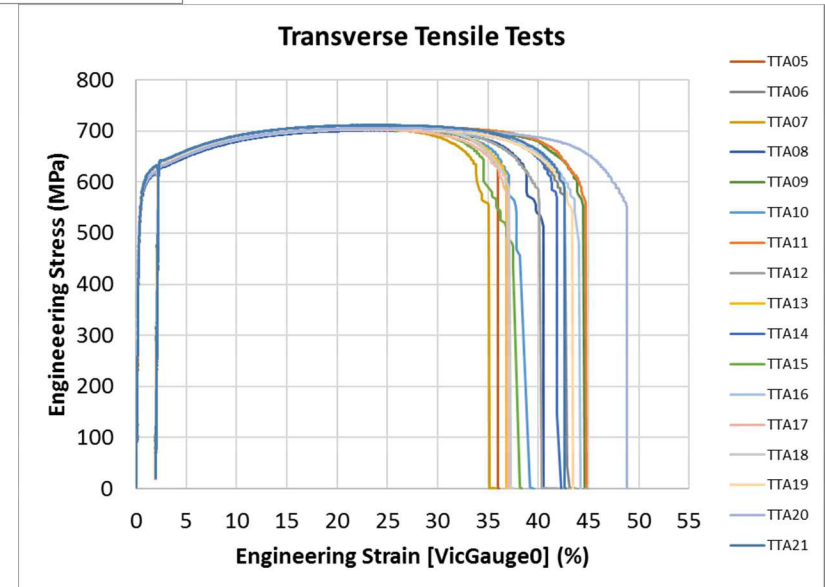


Longitudinal vs. transverse

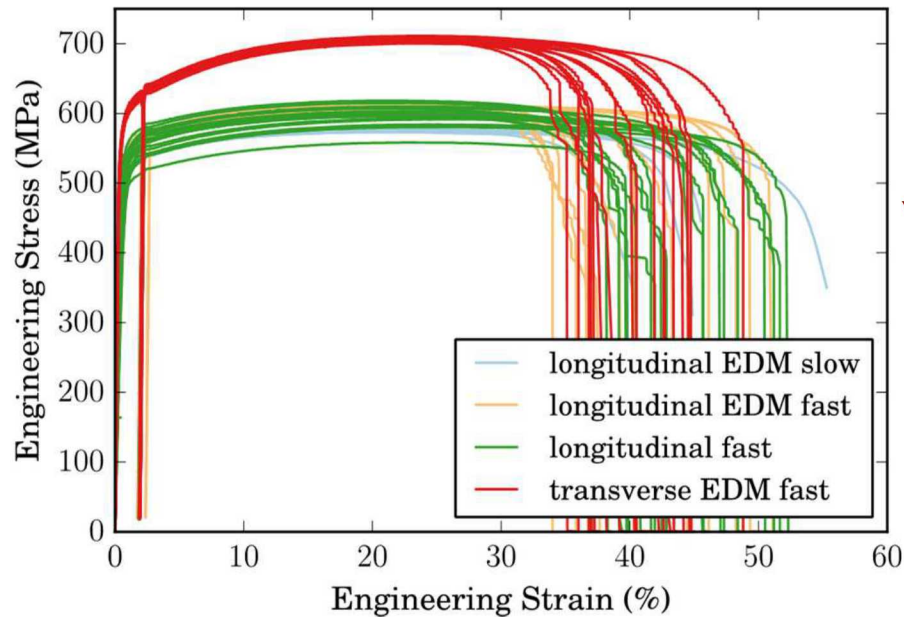
- Lower yield strength
- More variable strain-to-failure

Hypotheses

- Grain size/morphology
- Texture
- Defect size/morphology
- Residual stresses

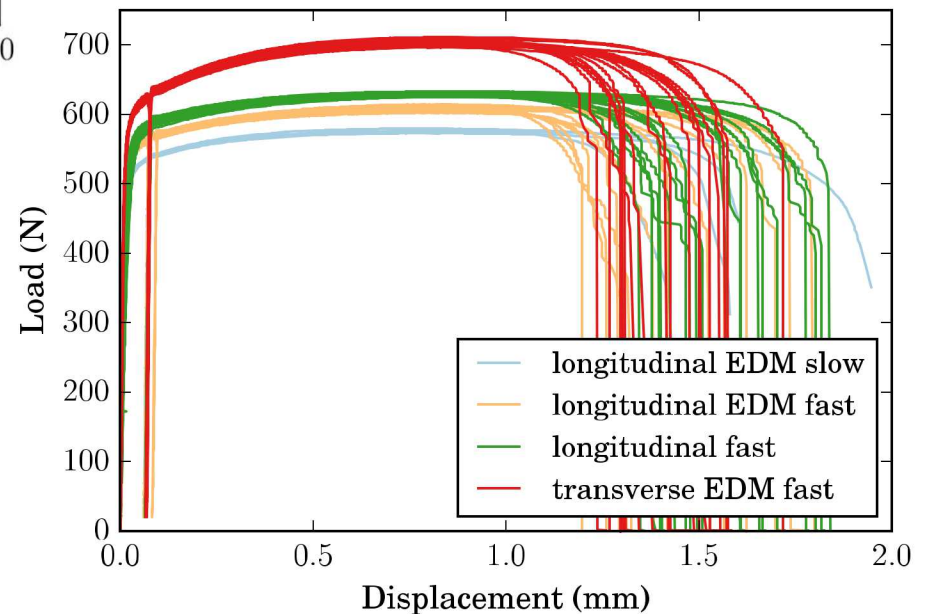
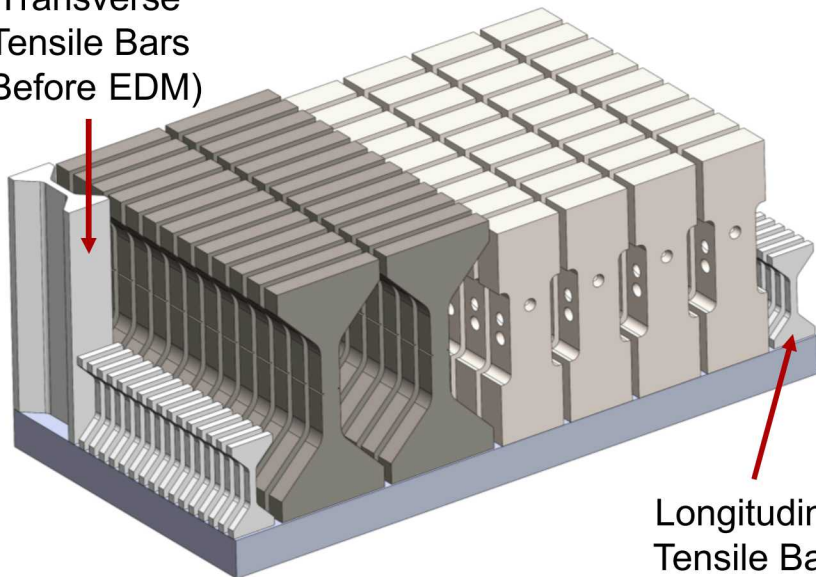


SFC3: Tension data

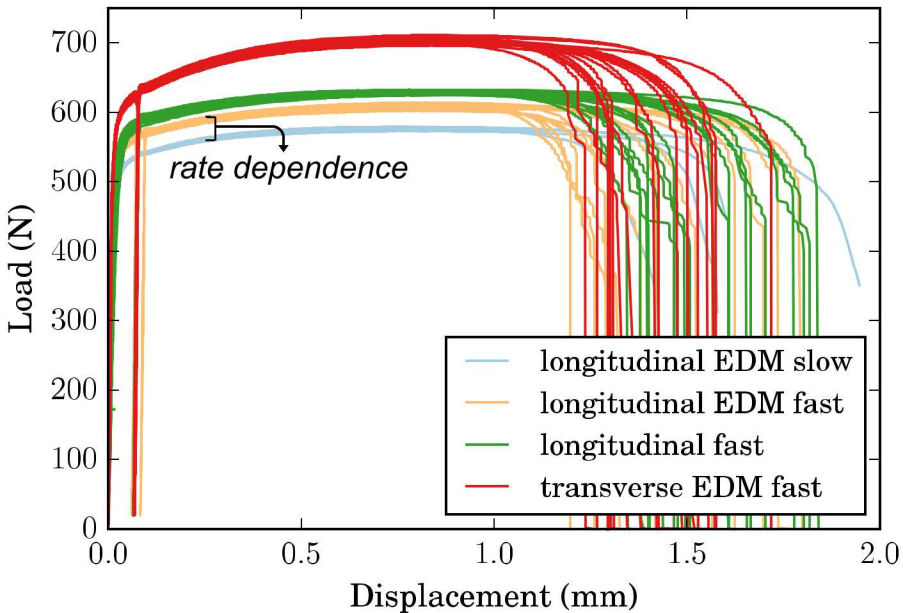


Apparent variability in flow stress for longitudinal (as-printed) specimens does not appear in load data

Transverse Tensile Bars (Before EDM)



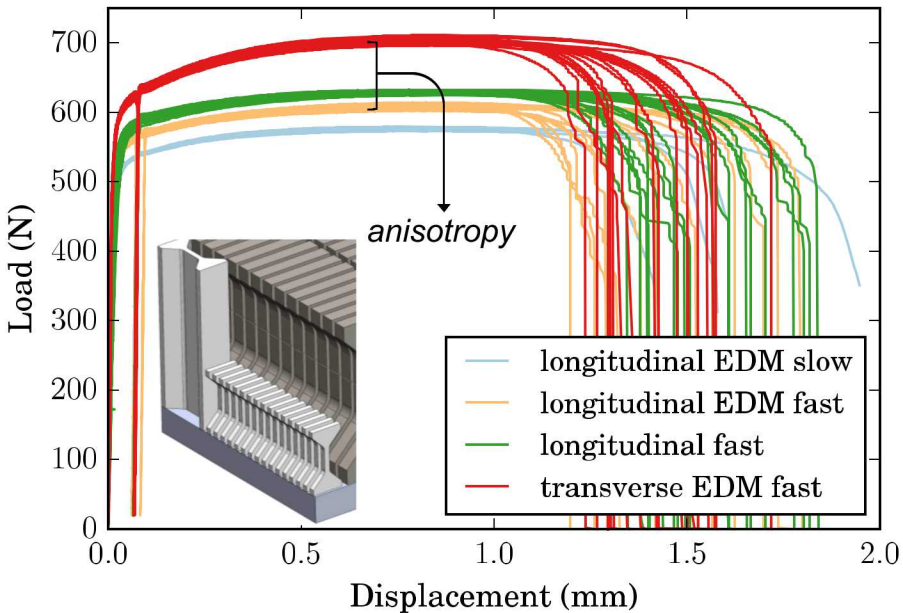
SFC3: Modeling assumptions and calibration



Modeling methodologies

- Temperature and rate dependent plasticity
- Plastic anisotropy
- Geometric variability, surface defects/voids
 - Explicit representation of geometries
 - Inclusion of surface defects
- Void nucleation, growth

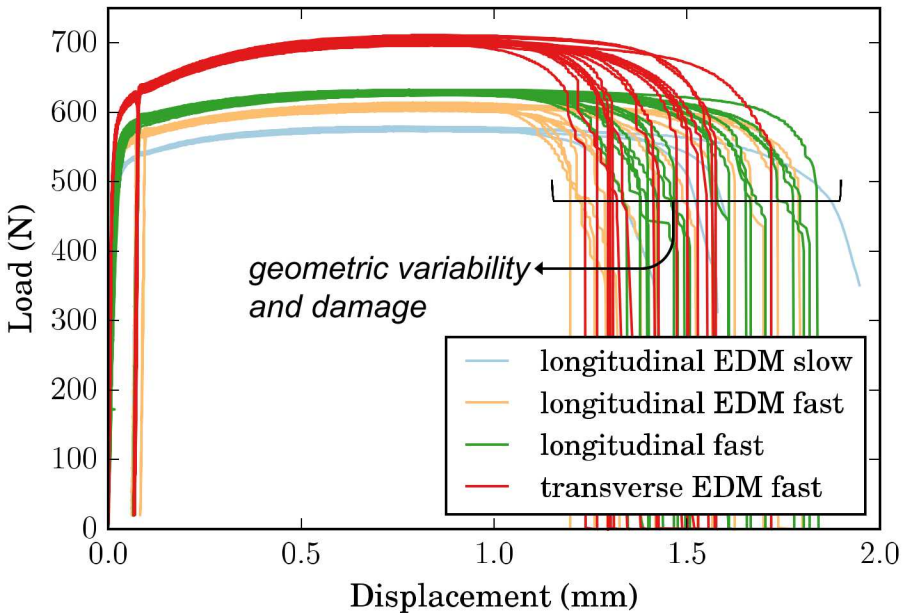
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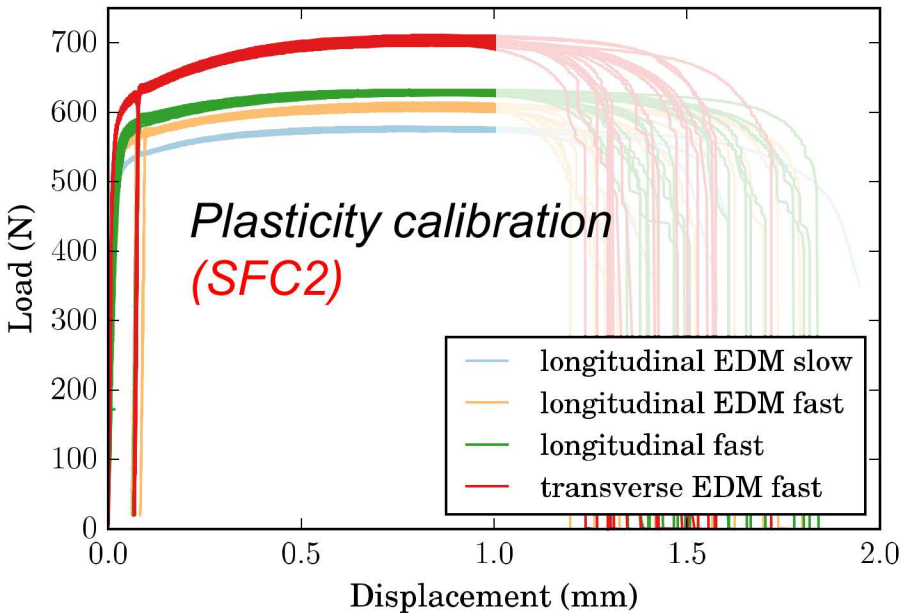
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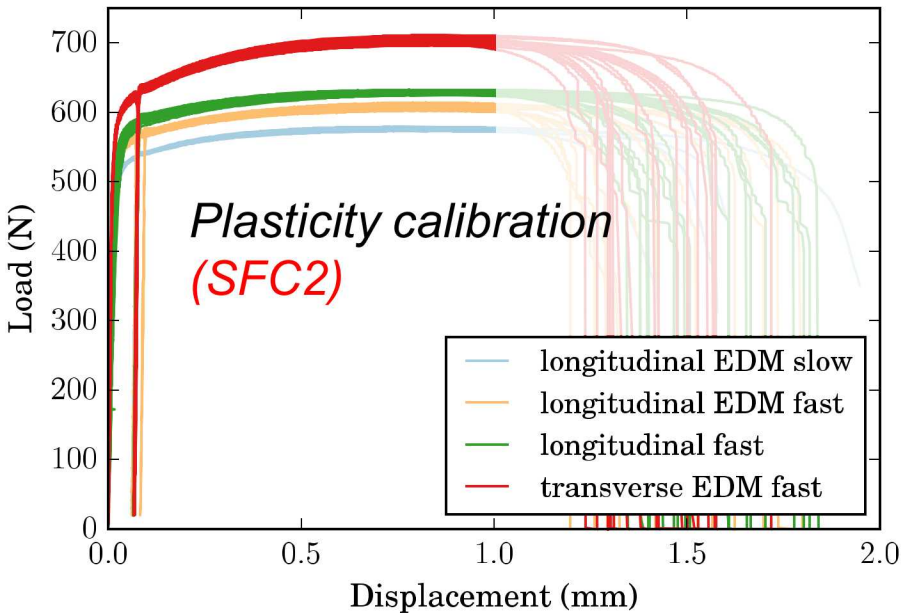
SFC3: Modeling assumptions and calibration



Modeling methodologies

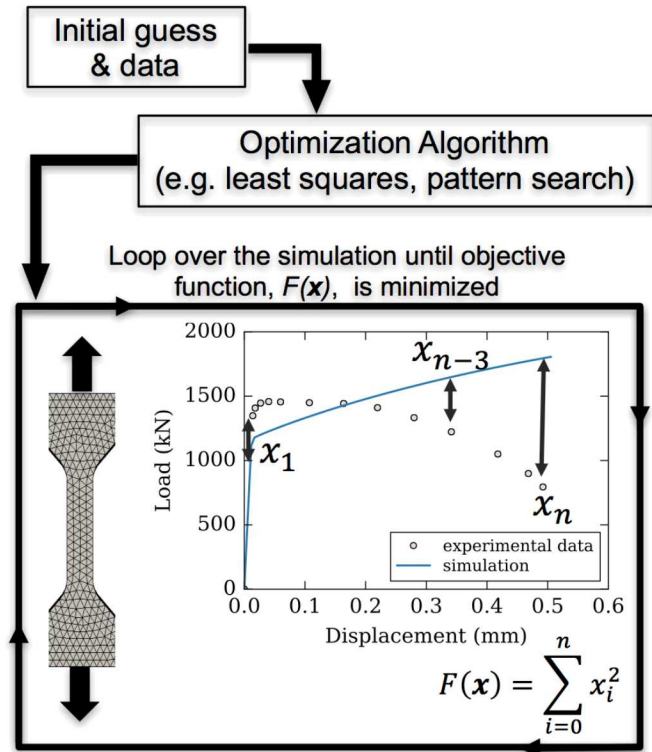
- Temperature and rate dependent plasticity
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- Void nucleation, growth

SFC3: Modeling assumptions and calibration



Modeling methodologies

- Temperature and rate dependent plasticity
- Plastic anisotropy
- Geometric variability, surface defects/voids
 - Explicit representation of geometries
 - Inclusion of surface defects
- Void nucleation, growth



- *Sierra/SM* for FEA
- *Dakota* for Optimization Algorithm
- *MatCal* for file and model management

With **18 unknown parameters**, calibrate using an iterative approach with increasing complexity :
 (1) rate dependence (2) hardening (3) anisotropy (4) damage

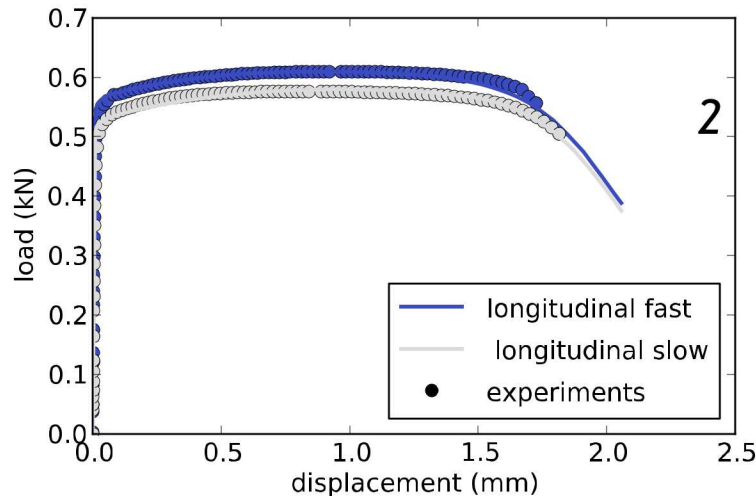
SFC3: Calibration Process for Flow

Rate-dependent anisotropic plasticity model with power-law hardening

$$\bar{\sigma}_e = Y_0 \left\{ 1 + \sinh^{-1} \left[\left(\frac{\dot{\epsilon}_p}{f} \right)^{1/n} \right] \right\} + A \langle \epsilon_p \rangle^b + \kappa_m$$

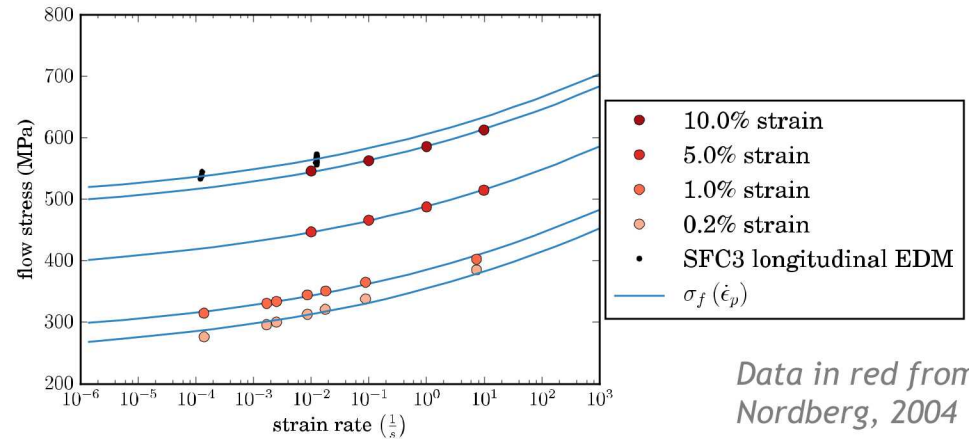
$$f_Y^2(\sigma_{ij}) \equiv F(\sigma_{22} - \sigma_{33})^2 + G(\sigma_{33} - \sigma_{11})^2 + H(\sigma_{11} - \sigma_{22})^2 + 2L\sigma_{23}^2 + 2M\sigma_{31}^2 + 2N\sigma_{12}^2 = \bar{\sigma}_e^2(\epsilon_p)$$

$$R_{ii} = \frac{\sigma_{ii}^y}{Y_0} \quad R_{ij} = \sqrt{3} \frac{\tau_{ij}^y}{Y_0}$$

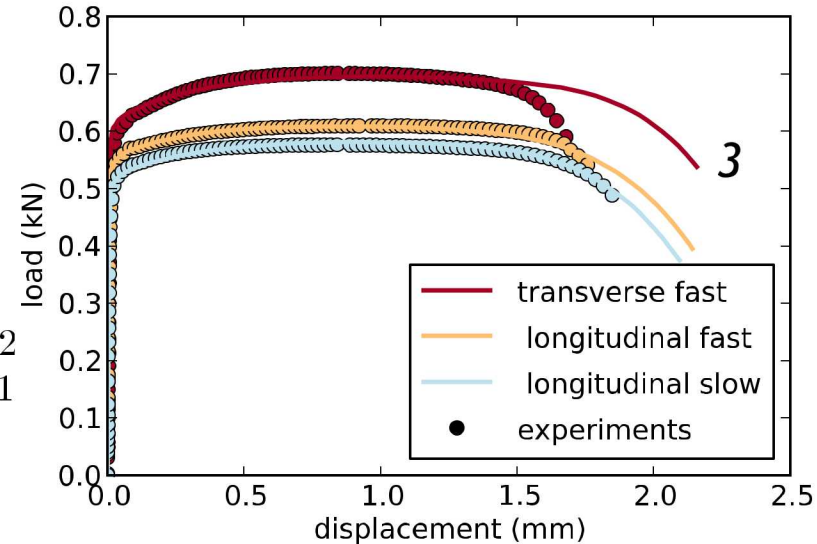


$$\begin{aligned} Y_0 &= 475 \text{ MPa} \\ \kappa_m &= 0 \text{ MPa} \\ f &= 26854 \left(\frac{1}{s} \right) \\ n &= 9.15 \\ A &= 753 \\ b &= 0.764 \\ R_{11} &= R_{33} = 1.072 \\ R_{22} &= R_{ij} = 0.961 \end{aligned}$$

Rate-dependence fit from challenge tests and literature data

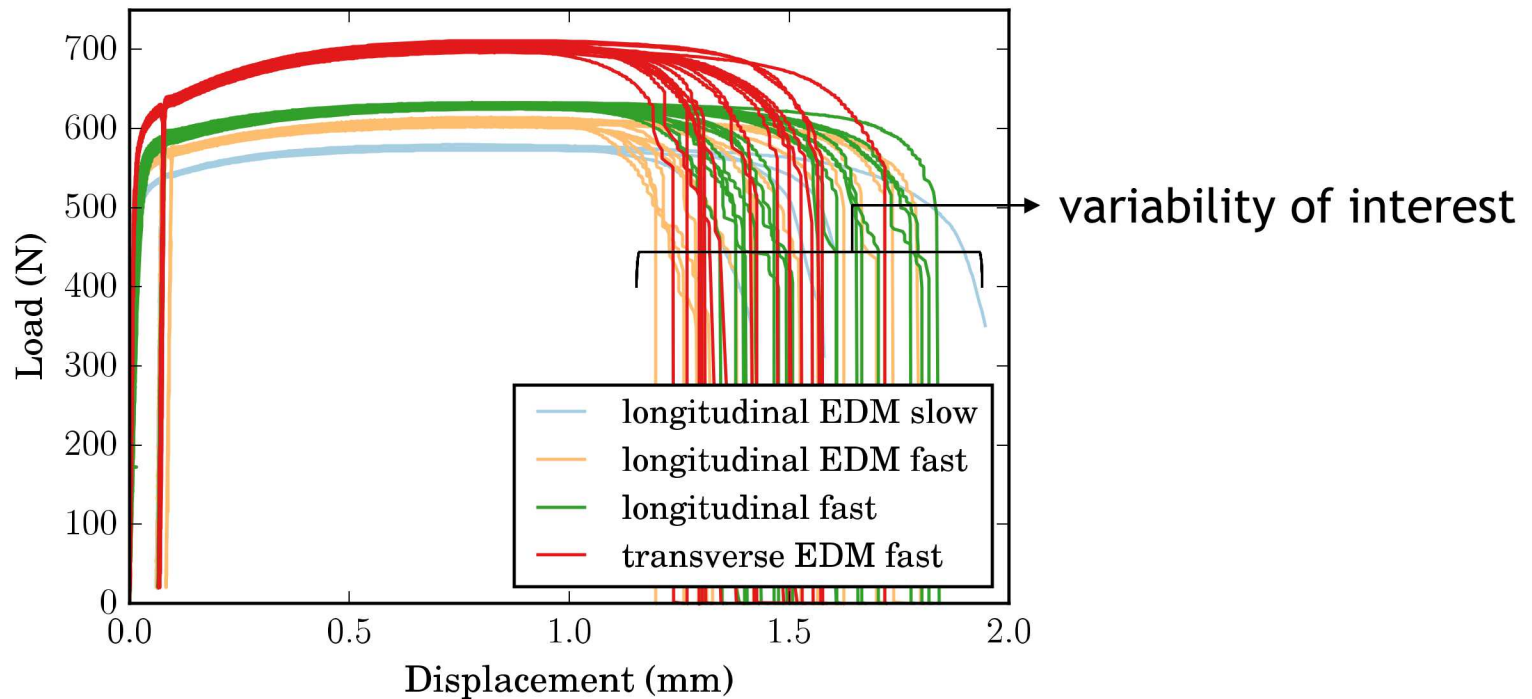


Data in red from Nordberg, 2004



SFC3: Material variability from damage

Significant variability exists in displacement-to-failure. Where does this come from?



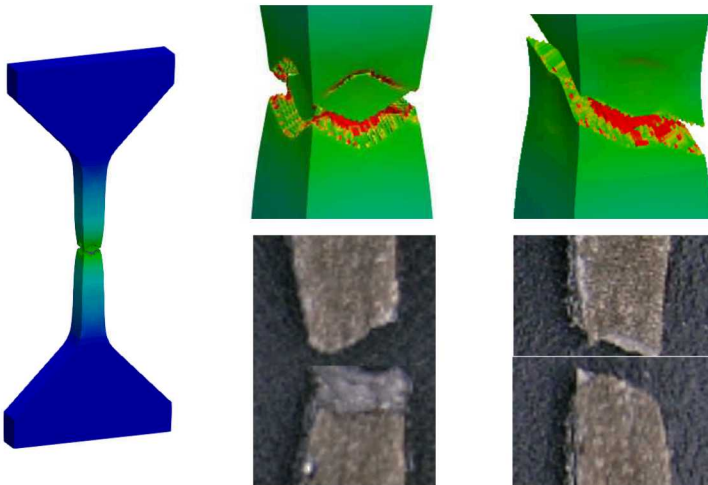
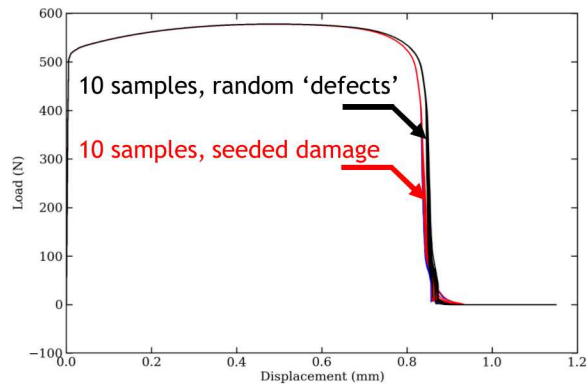
Hypothesis 1: constitutive model
can account for observed variability

Hypothesis 2: explicit modeling of defects
required to accurately capture variability

SFC3: Material variability from damage

Hypothesis 1: constitutive model can account for observed variability

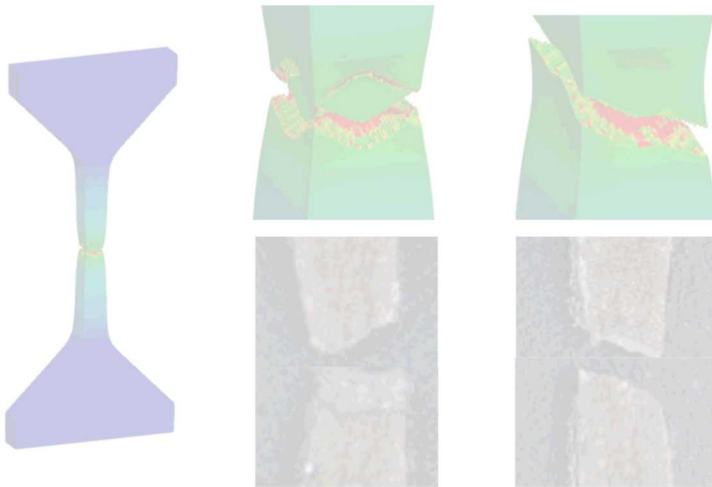
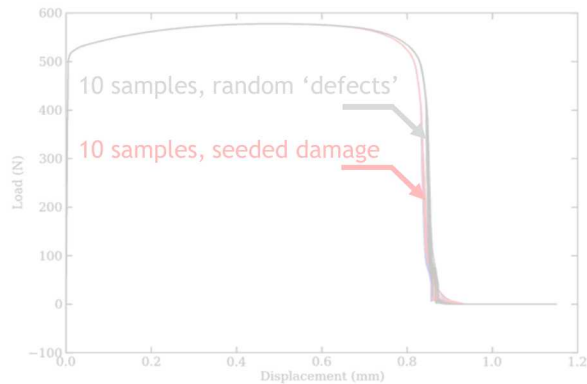
Hypothesis 2: explicit modeling of defects required to accurately capture variability



Conclusion: Damage field changes fracture surface, but not displacement-to-failure

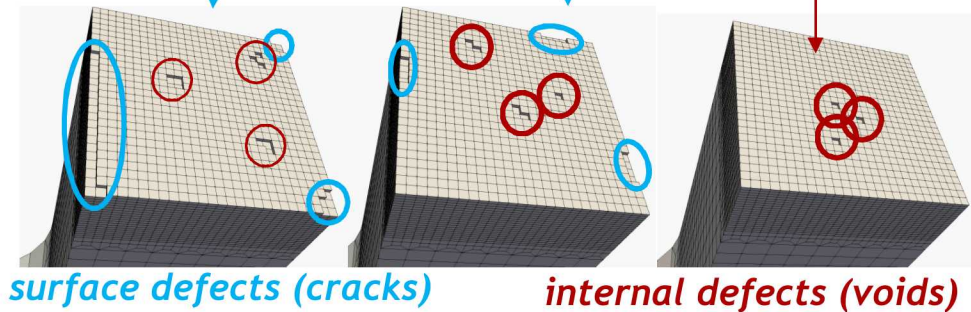
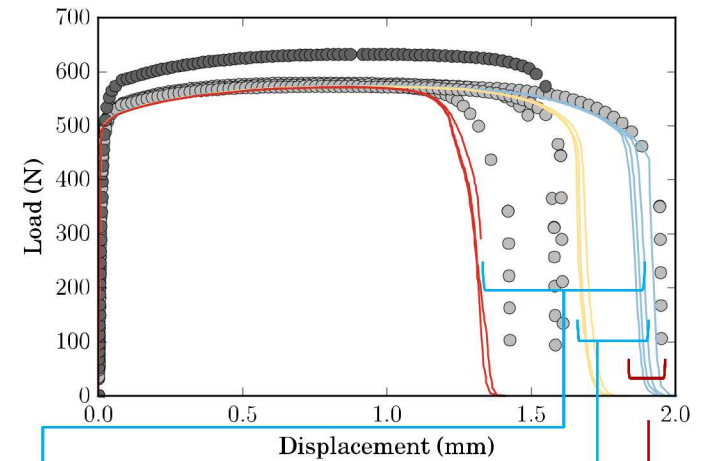
SFC3: Material variability form damage

Hypothesis 1: constitutive model can account for observed variability



Conclusion: Damage field changes fracture surface, but not displacement-to-failure

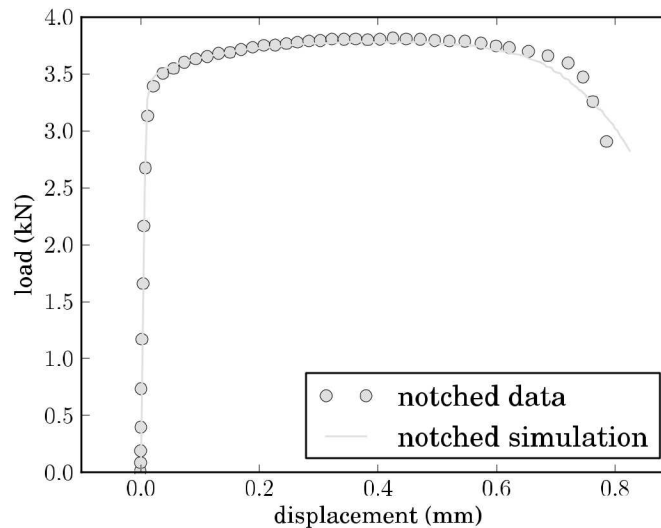
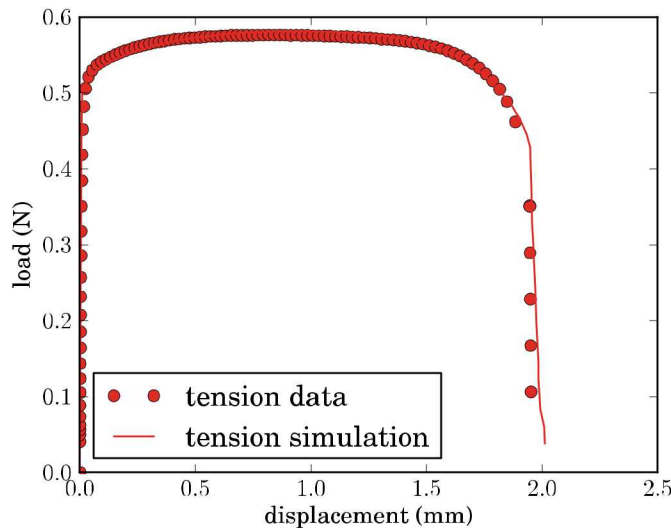
Hypothesis 2: explicit modeling of defects required to accurately capture variability



Conclusion: Yes. Internal defects cause marginal change, surface defects dominate

SFC3: Model for damage nucleation/evolution

- Calibrated to uniaxial and notched specimens with largest displacements
- Attributed variability in failure displacements in uniaxial tension tests to surface defects introduced by AM.



Final parameter values

$$Y_0 = 475 \text{ MPa}$$

$$\kappa_m = 0 \text{ MPa}$$

$$f = 26854 \left(\frac{1}{s} \right)$$

$$n = 9.15$$

$$A = 753$$

$$b = 0.764$$

$$R_{11} = R_{33} = 1.072$$

$$R_{22} = R_{ij} = 0.961$$

$$m = 2.9$$

$$N_1 = 2.0$$

$$N_3 = 2.5$$

$$\phi_0 = 6.3 \times 10^{-5}$$

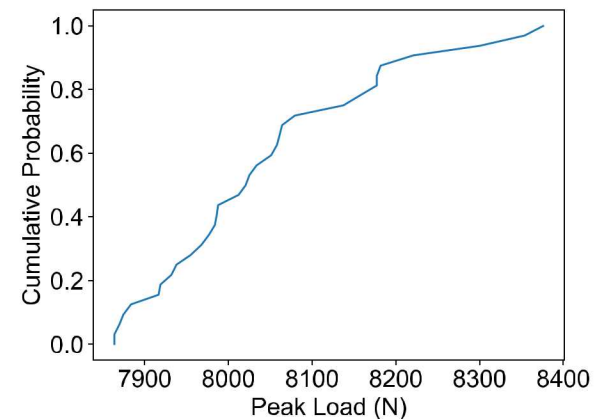
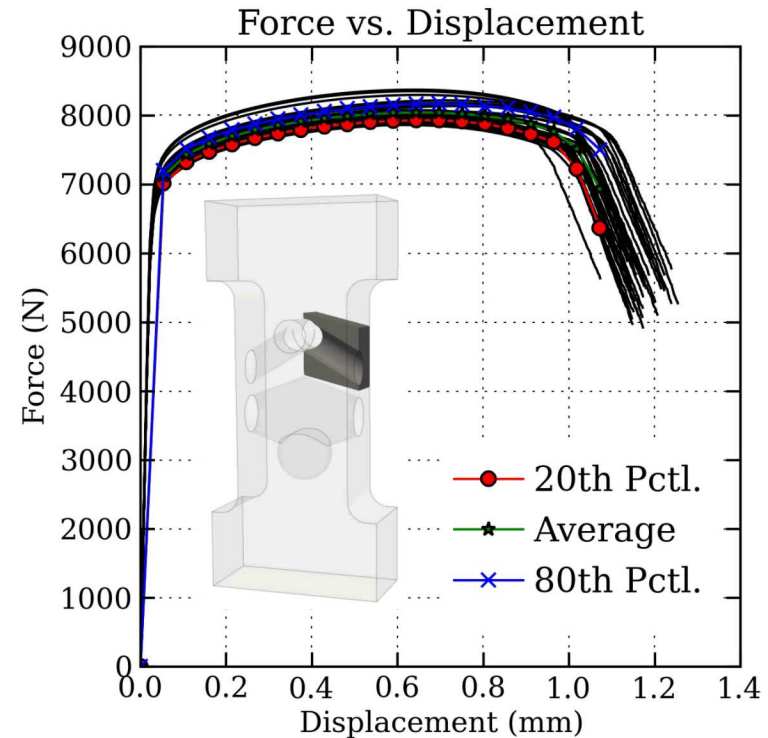
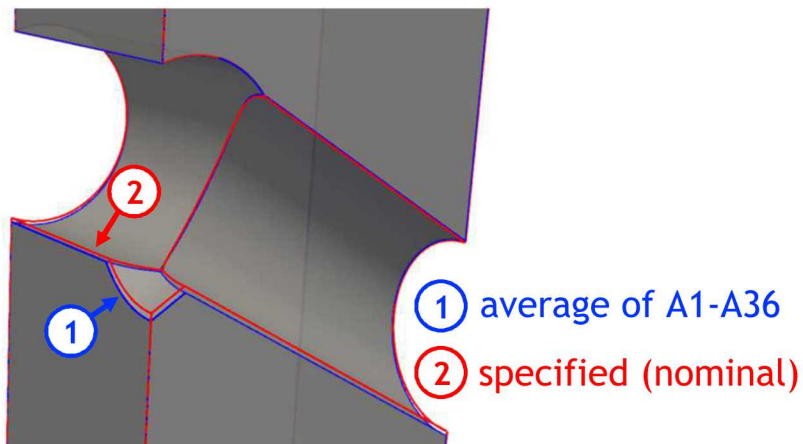
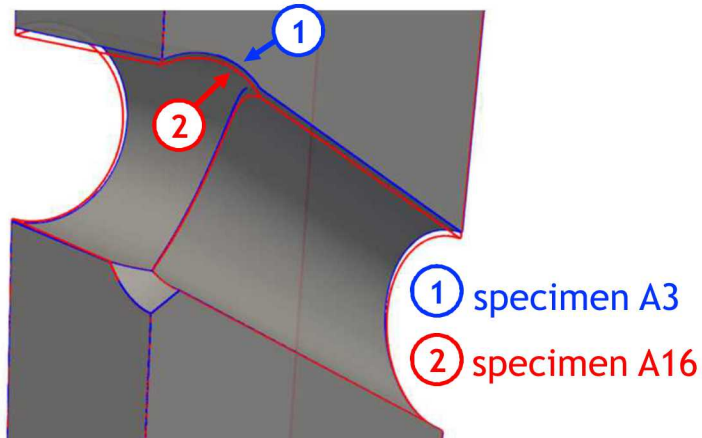
$$\eta_0 = 1.59 \times 10^{-5}$$

$$\eta_n = 4$$

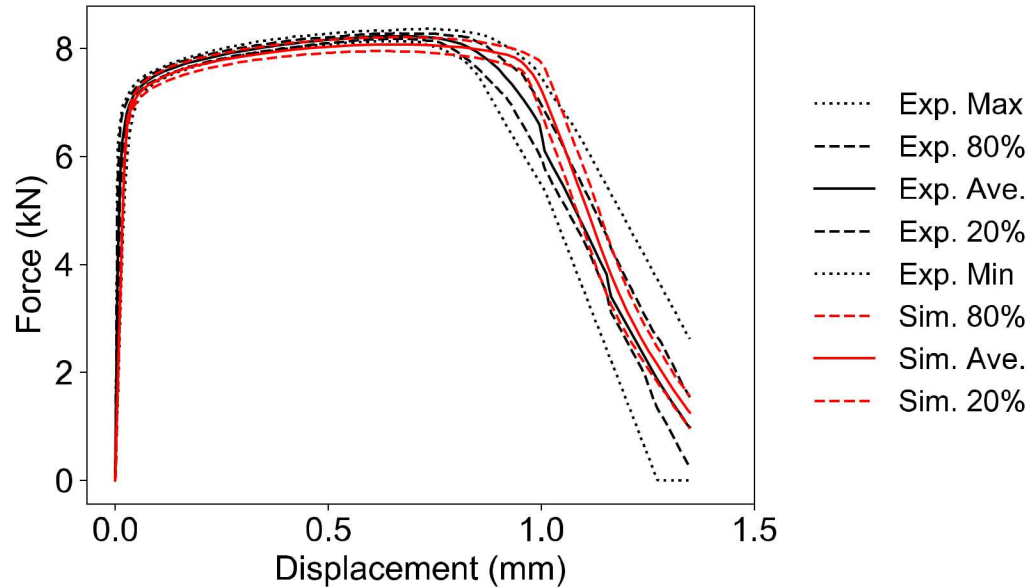
$$\dot{\phi} = \sqrt{\frac{2}{3}} \dot{\epsilon}_p \frac{1 - (1 - \phi)^{m+1}}{(1 - \phi)^m} \sinh \left[\frac{2(2m - 1)}{2m + 1} \frac{\langle p \rangle}{\sigma_e} \right] \quad \dot{\eta} = \eta \dot{\epsilon}_p \left(N_1 \left[\frac{4}{27} - \frac{J_3^2}{J_2^3} \right] + N_3 \left[\frac{\langle p \rangle}{\sigma_e} \right] \right)$$

SFC3: Assessing structural variability/uncertainty

Geometric variability plays a significant role in uncertainty in the structural performance



SFC3: Comparison and uncertainty

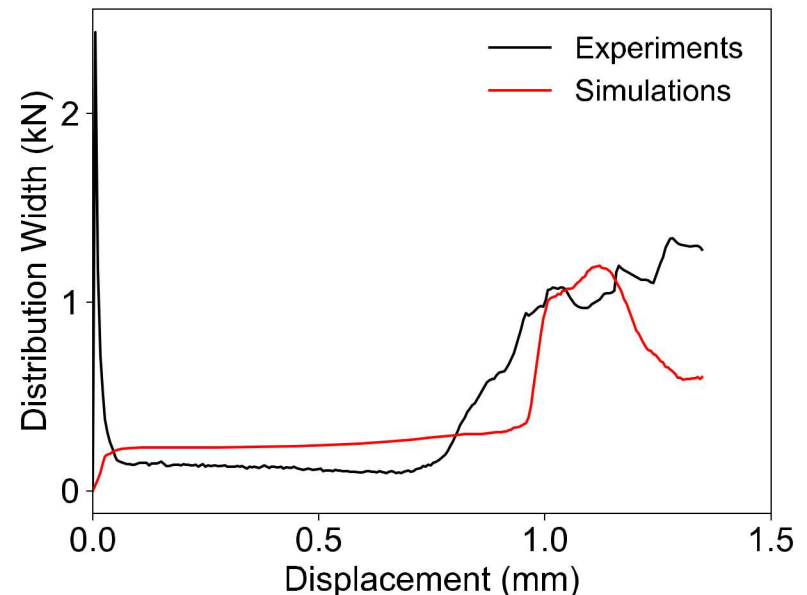


Global trends in experimental load-displacement results reproduced by models

Take away message:

- Geometric fluctuations in these AM specimens are a major contributor to variability
- Just as important as material variability (if not more so)
- *Having robust and accurate models of anisotropic behavior facilitate these studies and conclusions*

Variability in experiments also well-captured



- Boyce, B. L., et al. "The second Sandia Fracture Challenge: predictions of ductile failure under quasi-static and moderate-rate dynamic loading." *International Journal of Fracture* 198.1-2 (2016): 5-100.
- Karlson, Kyle N., et al. "Sandia fracture challenge 2: Sandia California's modeling approach." *International Journal of Fracture* 198.1-2 (2016): 179-195.
- Scherzinger, William M. "A return mapping algorithm for isotropic and anisotropic plasticity models using a line search method." *Computer Methods in Applied Mechanics and Engineering* 317 (2017): 526-553.
- Lester, Brian T., and William M. Scherzinger. "Trust-region based return mapping algorithm for implicit integration of elastic-plastic constitutive models." *International Journal for Numerical Methods in Engineering* 112.3 (2017): 257-282.
- Brown, Arthur A., and Douglas J. Bammann. "Validation of a model for static and dynamic recrystallization in metals." *International Journal of Plasticity* 32 (2012): 17-35.
- SFC3 journal articles *in prep for International Journal of Fracture*

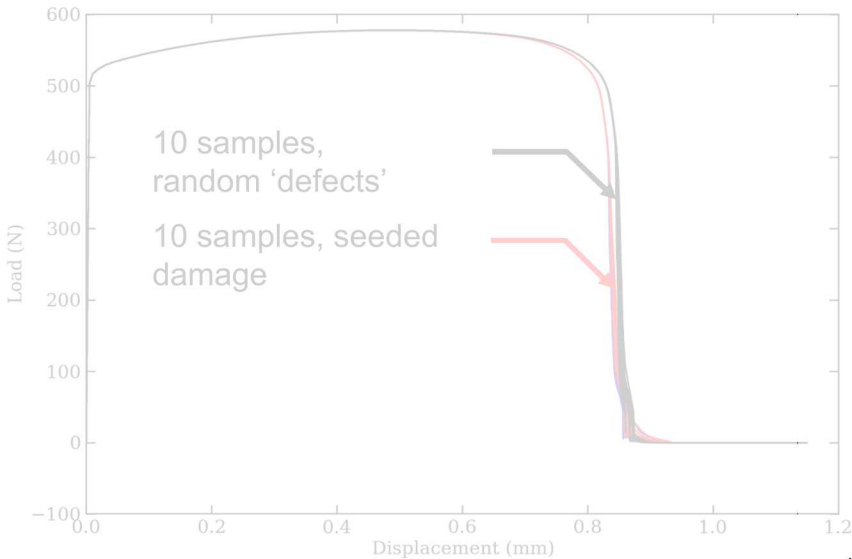
Thank you

Supporting Slides

Material variability: Damage

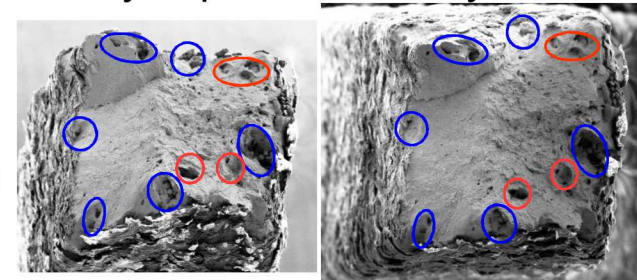
Hypothesis 1 – constitutive model can account for observed variability

Hypothesis 2– explicit modeling of defects required to accurately capture variability

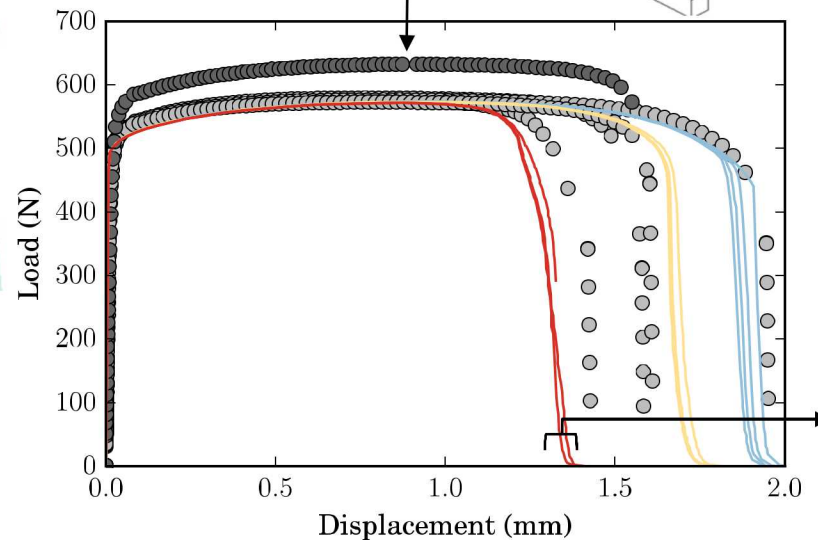
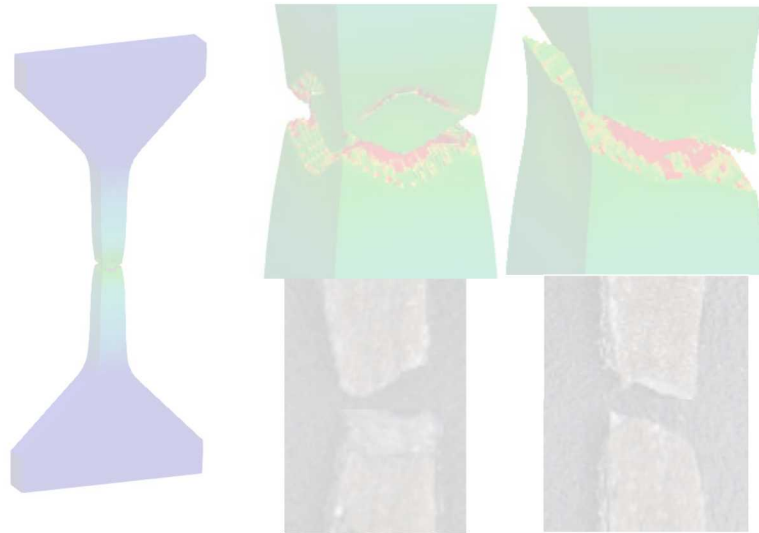
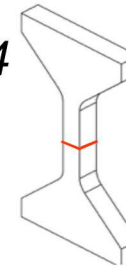


surface defects (cracks)

internal defects (voids)

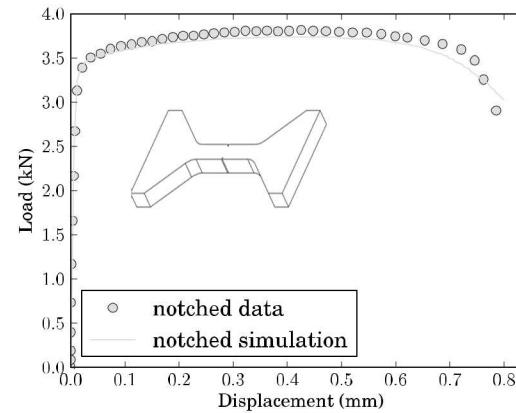
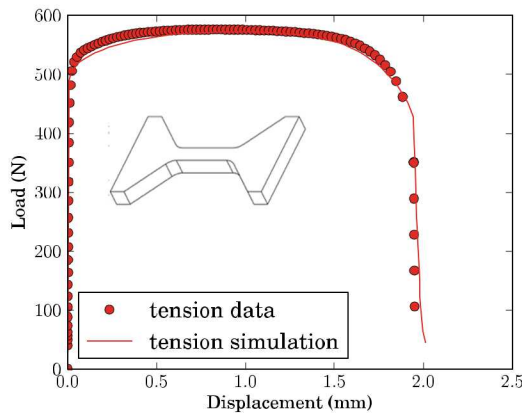


Specimen LTA04

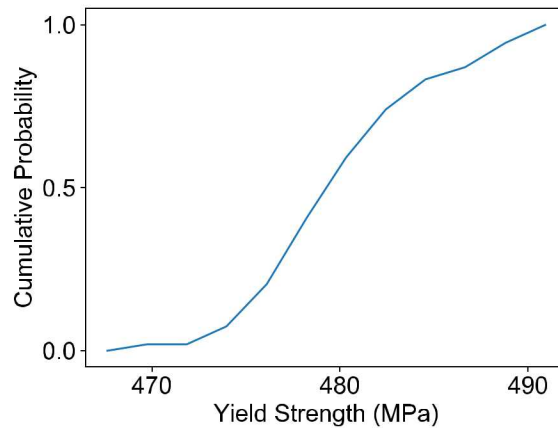


Assessing material variability/uncertainty

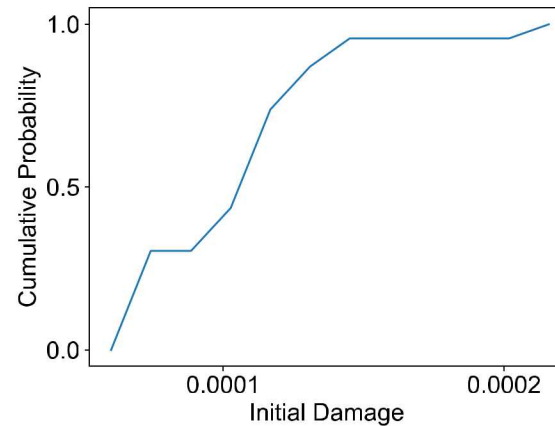
Calibrate material model for each specimen individually to obtain parameter variability



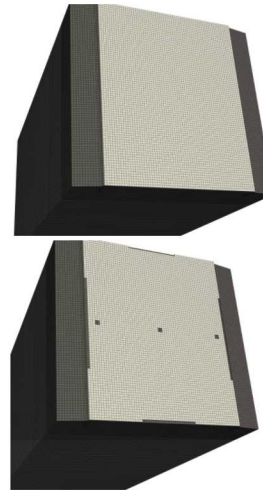
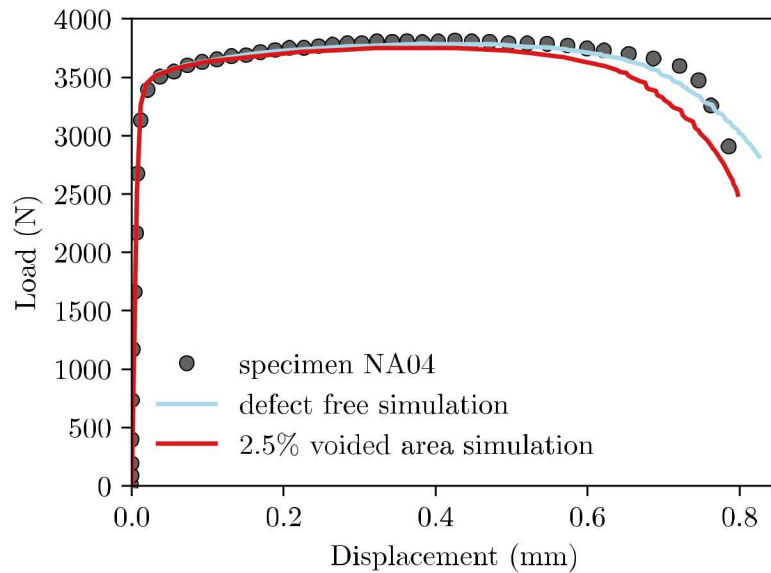
53 calibrations for plasticity



22 calibrations for damage

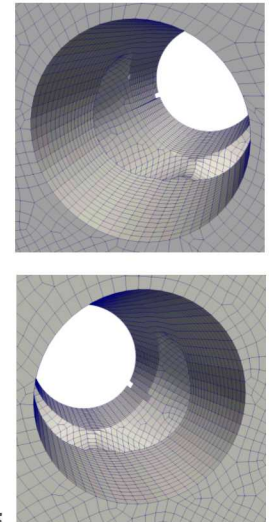
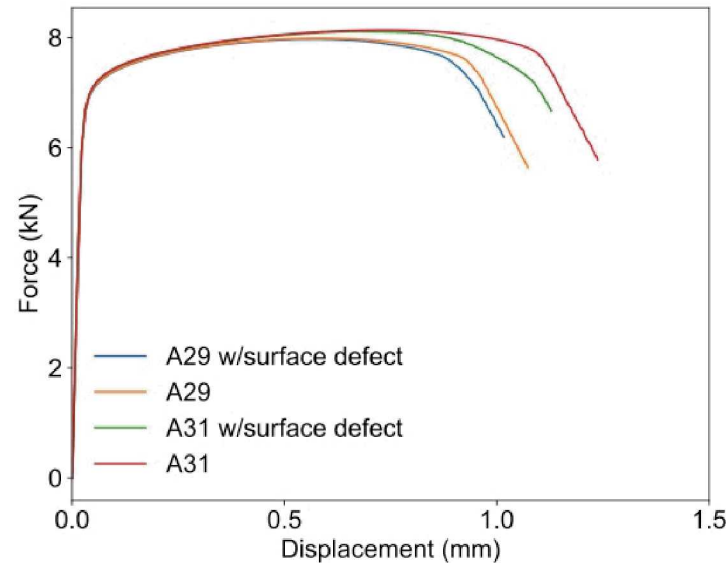


SFC3: Defect effect



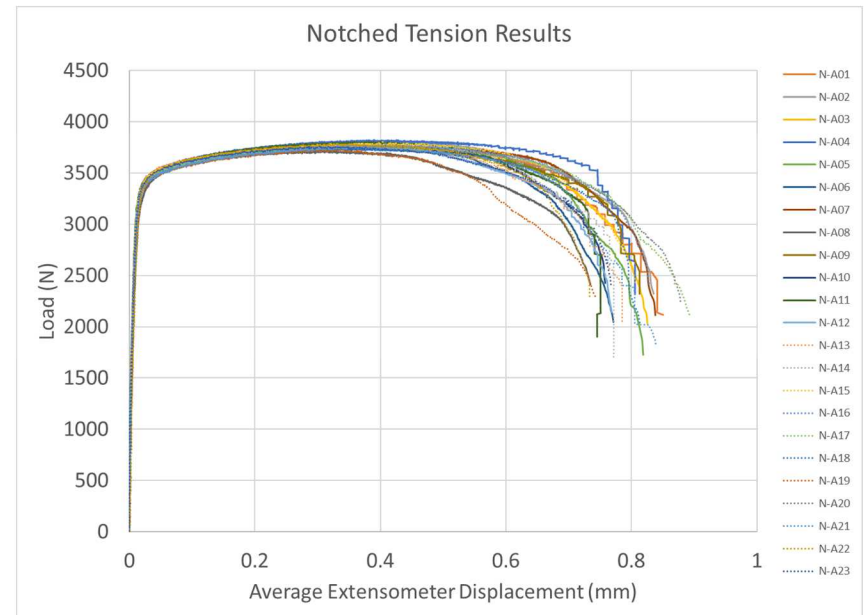
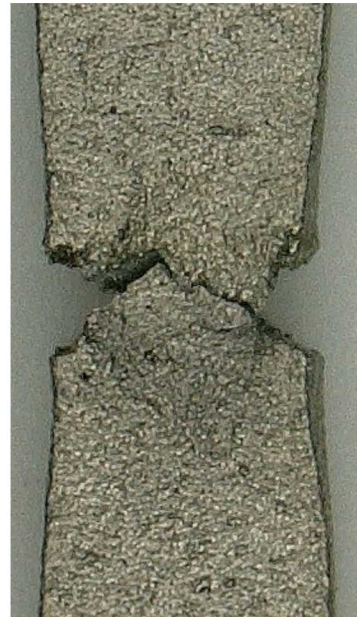
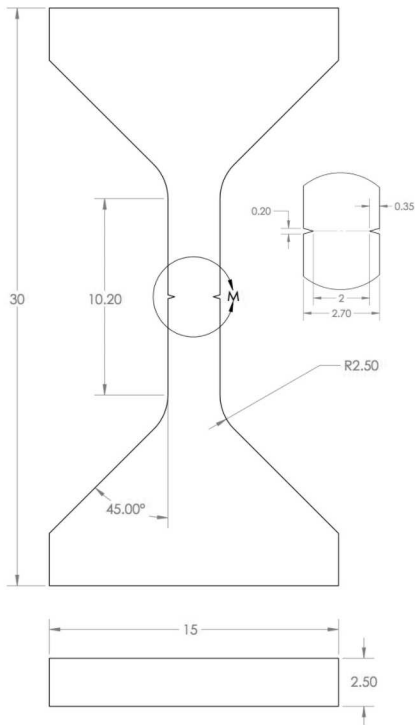
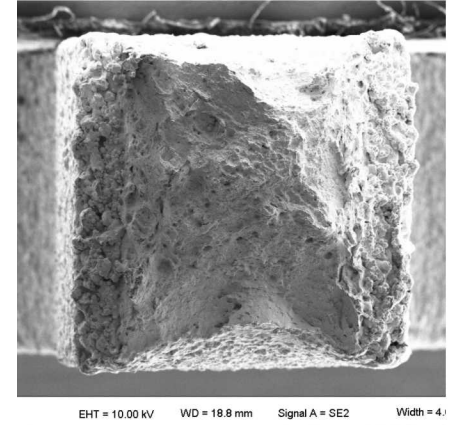
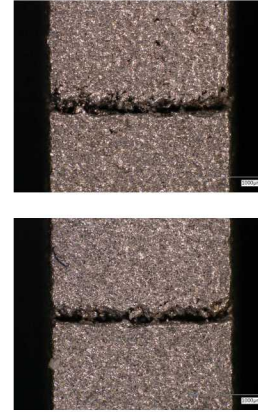
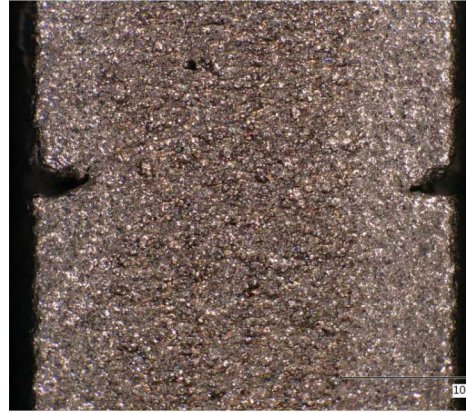
Notched tension specimens show a 50% decrease in reduction in displacement-to-failure over smooth tension specimens

For challenge specimens, worst-case scenario (very large surface defect in region of highest stress concentration) shows some effect; variability in structure geometry dominates



Characterization of AM 316L (Notched tension)

Notched data provided to calibrate crack initiation and propagation. We employed notches to check flow and fit damage evolution.

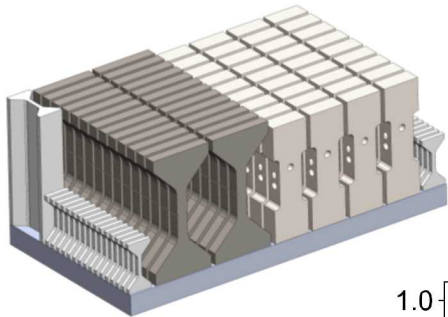


Accounting for material and structural variability

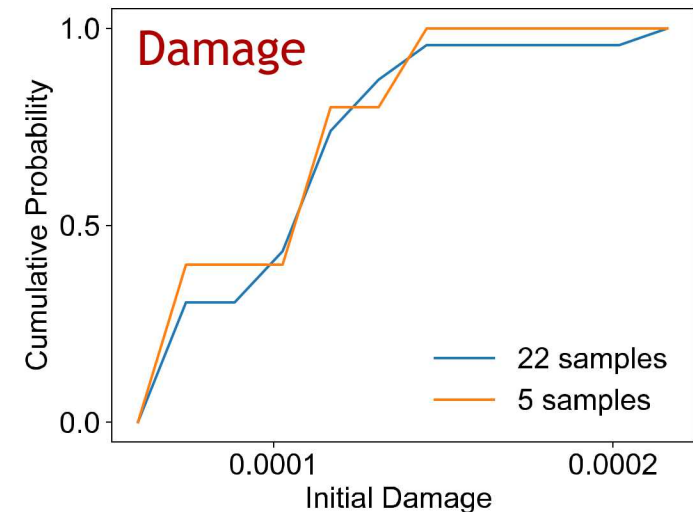
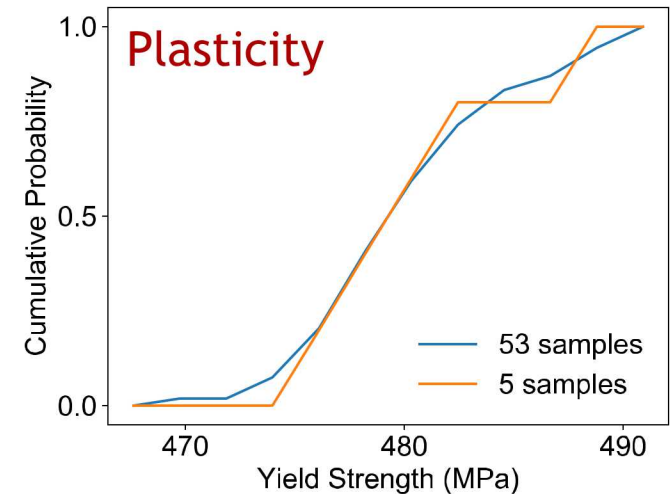
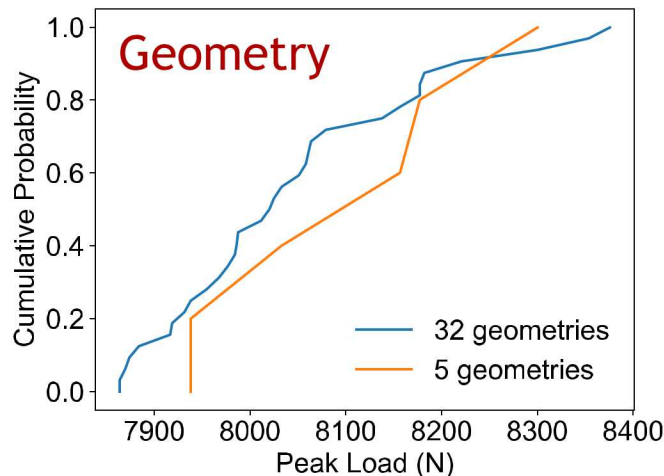
The **Kolmogorov-Smirnov** test statistic was used to obtain optimal downsampled subsets

5 parameters selected from each parameter set

- Yield strengths for each *smooth tension experiment*
- Initial damages for each *notched tension experiment*
- Principal components for each *challenge geometry*



**Reduced ~42000
simulations to 125
simulations total**



Accounting for Geometric Variability

Significant correlations were found between a number of the quantities of interest. To reduce the data by eliminating redundancy in the sampled specimens, apply principal component analysis to output data

Data matrix X (36 specimens, 21 variables)

X_{ij} : i -th measurement of j -th variable

Correlation matrix C (21 x 21)

$$C = \frac{1}{n-1} X^T \cdot X$$

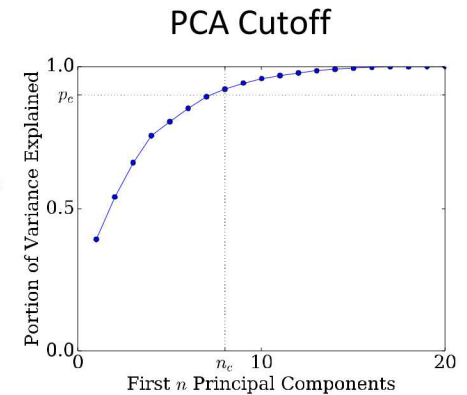
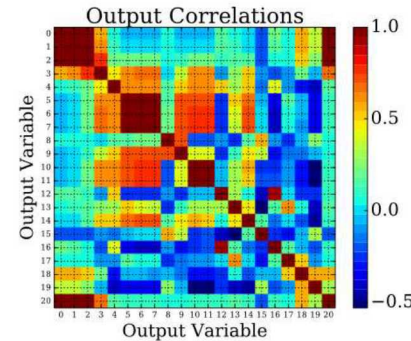
Set threshold of p_c , and keep n_c of the largest principal components S_{kk} , such that

$$\sum_{i=1}^{n_c} S_{kk} \geq p_c$$

The Kolmogorov-Smirnov test statistic used to obtain an optimal reduced set of specimens

$$D_{n,m} = \sup_x |F_{1,n}(x) - F_{2,m}(x)|$$

quantifies similarity of $F_{1,n}(x)$ and $F_{2,m}(x)$ of two samples of size n and m , respectively



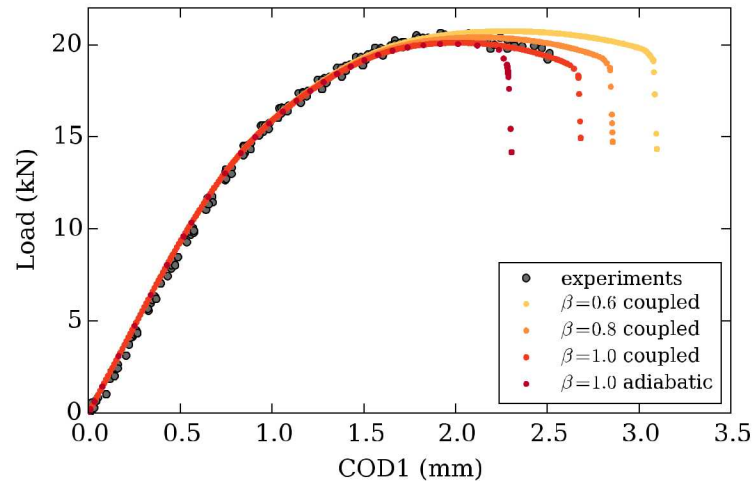
Downsampled vs Full Sample CDFs

Compute $D_{n,m}^*$ for $m = 5$ and pick a reduced set of inputs that best represent the full sample

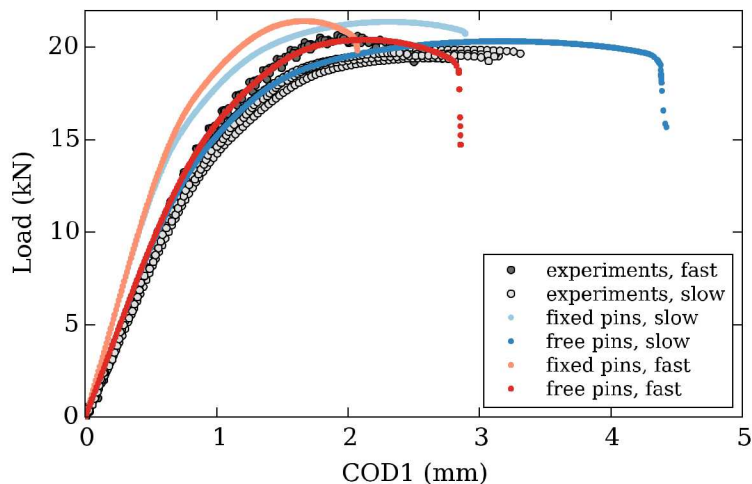
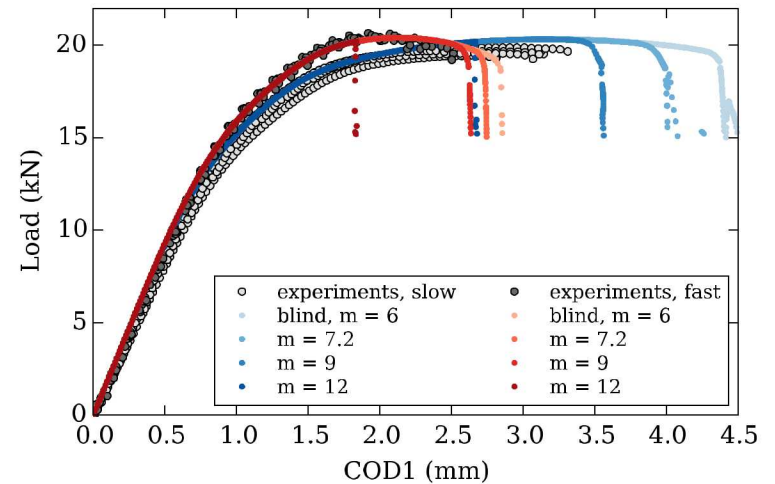
$A1, A11, A20, A27, A28$

Sensitivity to uncertain parameters

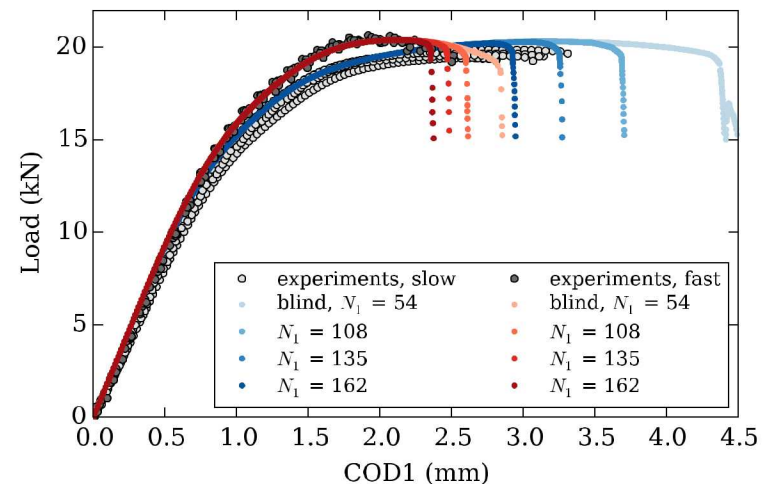
thermal parameter, β



void growth damage, m



pin boundary condition



Void nucleation damage, N_1