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# Simulation-based Bayesian Optimal Design for Ice Sheet Borehole Experiments

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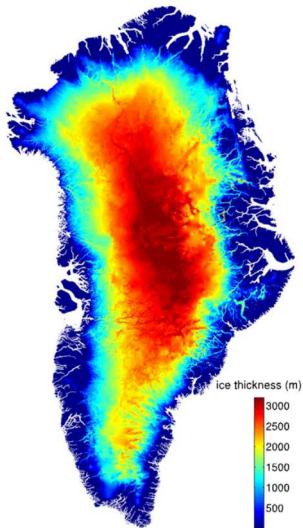
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# Motivation



Source: (left) National Snow & Ice Data Center, (middle) earth-chronicles.com, (right) Andrew D. Davis

# Motivation

Ice sheets **impact future global mean sea level**

- Greenland:  $\approx 6$  meters

Antarctica:  $\approx 60$  meters



Source: National Geographic

# Physical model is nonlinear and complex

- 1 Stress and mass balance equations
- 2 Calving law
- 3 Temperature  $T(x, z, t)$  via advection-diffusion

$$\dot{T} + \kappa \nabla^2 T + \mathbf{u} \cdot \nabla T = 0$$
$$T(x, h(x, t), t) = T_s(t; \theta)$$

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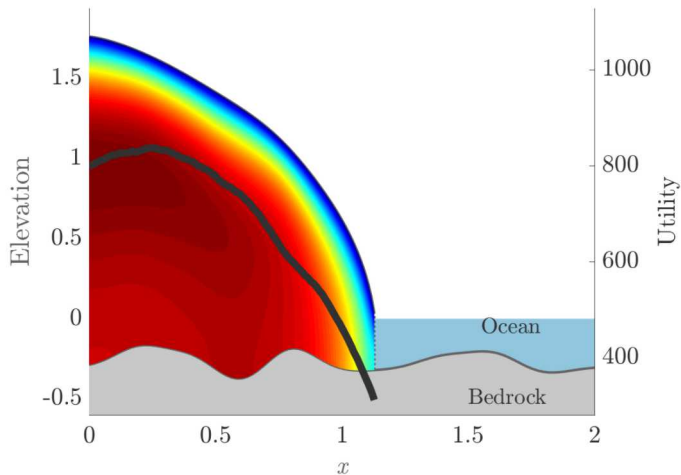
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## Goal of **Optimal Experimental Design**:

Select borehole locations that maximize the expected information gain for inferring past surface temperature

$$\xi^* = \operatorname{argmax} \{ U(\xi) = \mathbb{E}_{\delta|\xi} [D_{\text{KL}}(\text{posterior}||\text{prior})] \}$$

## Expected information gain with inland hiking penalty



**Today 11:35 AM, West Hall B, Poster #1**

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- Massachusetts Institute of Technology
- U.S. Department of Energy
- National Science Foundation

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