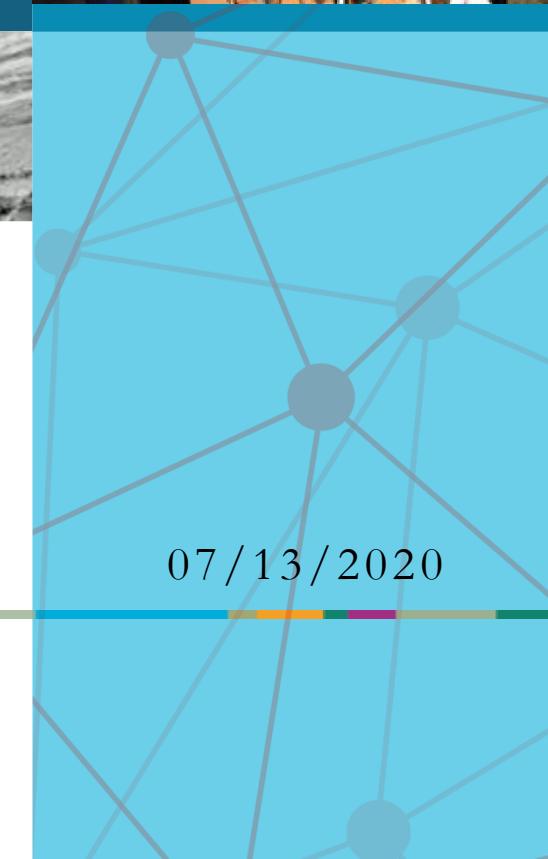
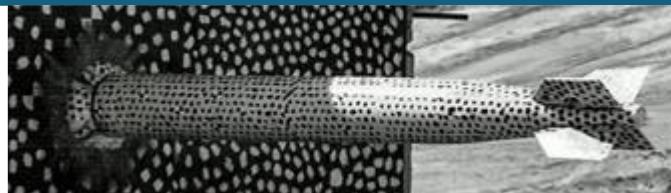




Sensing Depths in Periodic Thermal Measurements



07/13/2020

PRESENTED BY

Wyatt Hedges, Jacob Mahaffey, Elbara Ziade

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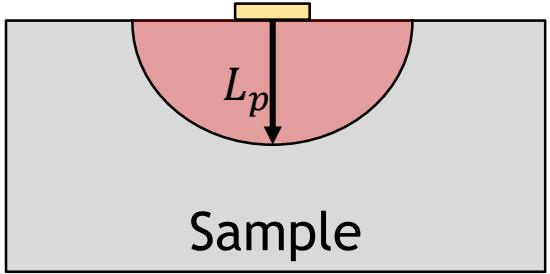
Outline

- Motivation
- Thermal Length Scales
 - Sensing Length
- Simulation of Sensing Lengths in Silicon and SiO_2
- Experimental Results
- Conclusions



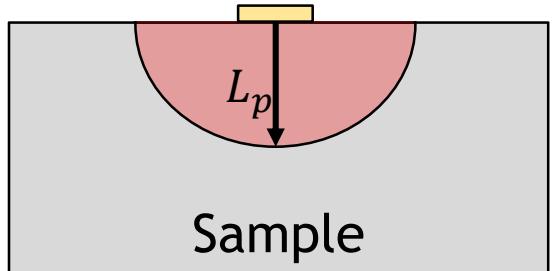
Motivation

3ω



Motivation

3ω



2-5 “thermal penetration depths”
to appear semi-infinite

$$L_p = \sqrt{\frac{2\alpha}{\omega}}$$

$\alpha \rightarrow$ Thermal diffusivity [W/mK]; $k/\rho c_p$
 $\omega \rightarrow$ Heating frequency [rad/s]

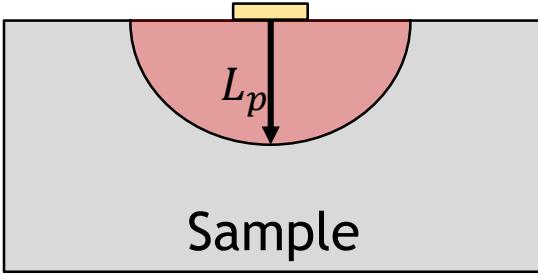


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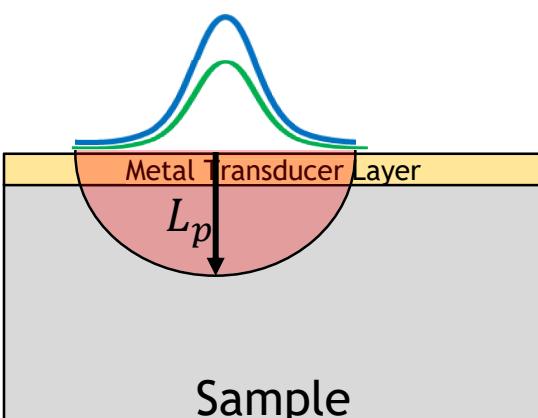
Motivation



3 ω



TDTR/FDTR

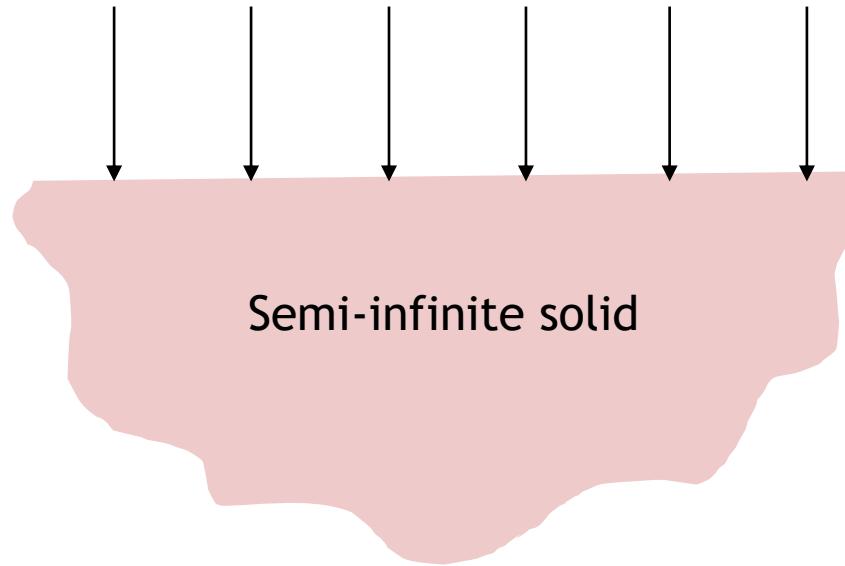


2-5 “thermal penetration depths”
to appear semi-infinite

How deep does a measurement
“see” into the sample?



$$\frac{T(x, t) - T_i}{\Delta T} = \exp\left(-x\sqrt{2\alpha/\omega}\right) \sin\left(\omega t - x\sqrt{2\alpha/\omega}\right)$$



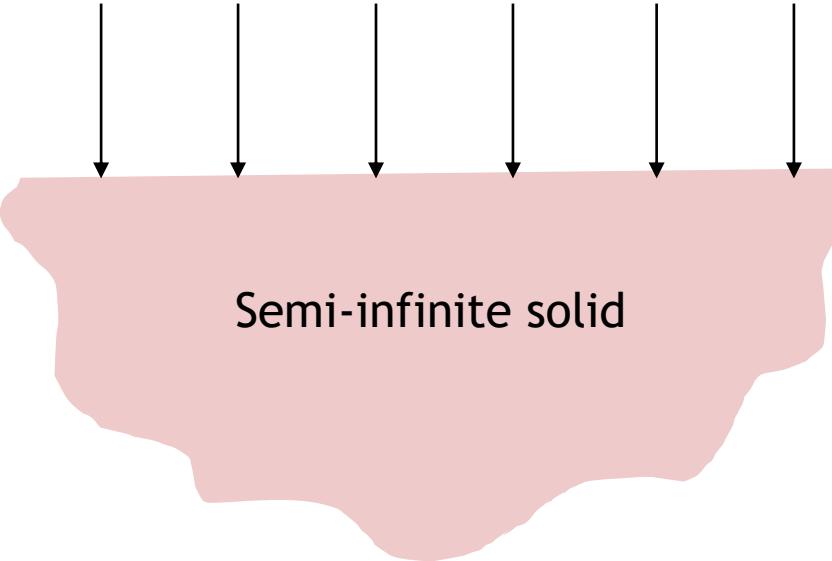
Semi-infinite solid



Thermal Length Scales

$$\frac{T(x, t) - T_i}{\Delta T} = \exp\left(-x\sqrt{2\alpha/\omega}\right) \sin\left(\omega t - x\sqrt{2\alpha/\omega}\right)$$

$$L_p = \sqrt{\frac{2\alpha}{\omega}}$$

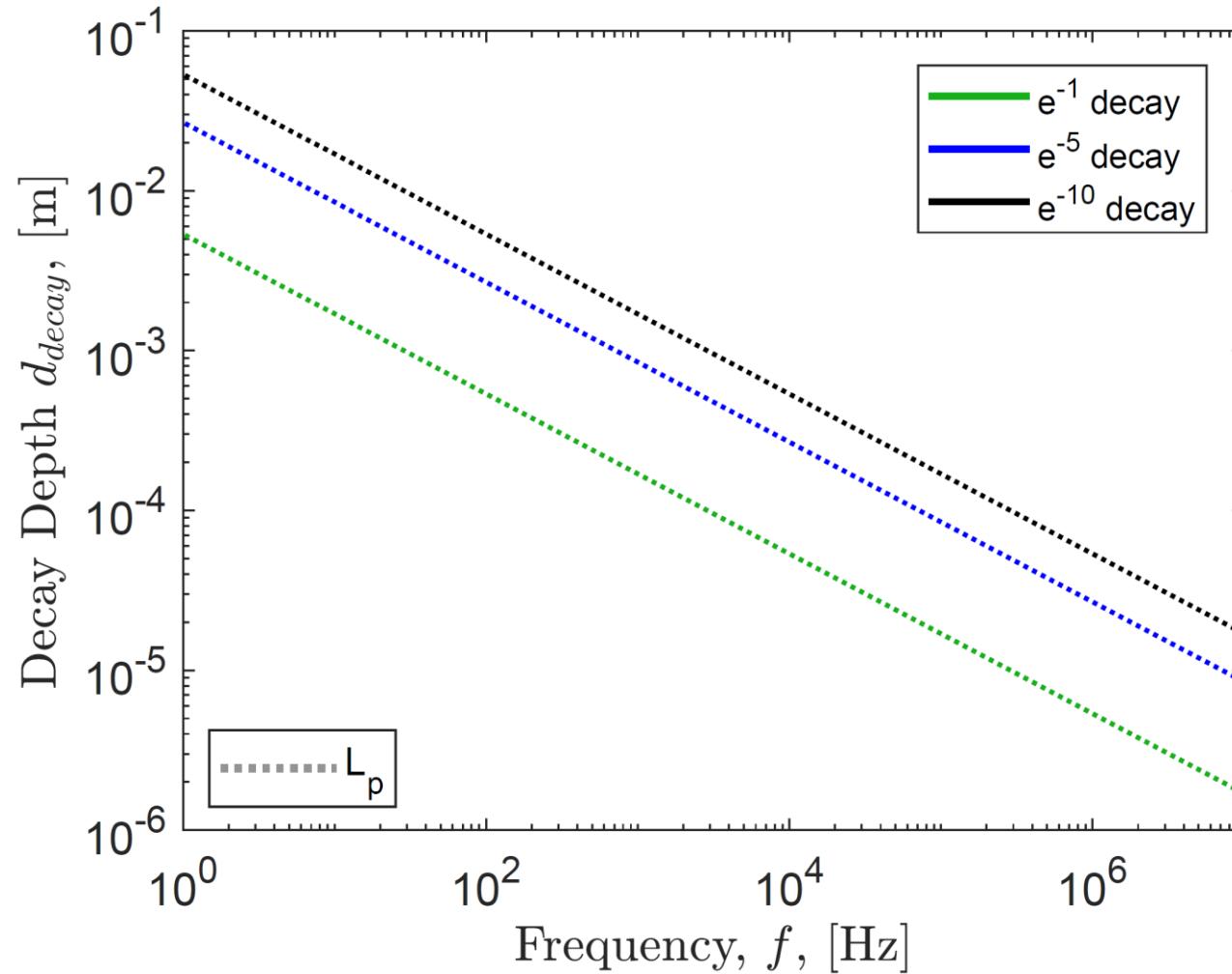


$\alpha \rightarrow$ Thermal diffusivity [m^2/s]; $k/\rho c_p$
 $\omega \rightarrow$ Heating frequency [rad/s],

Thermal Length Scales

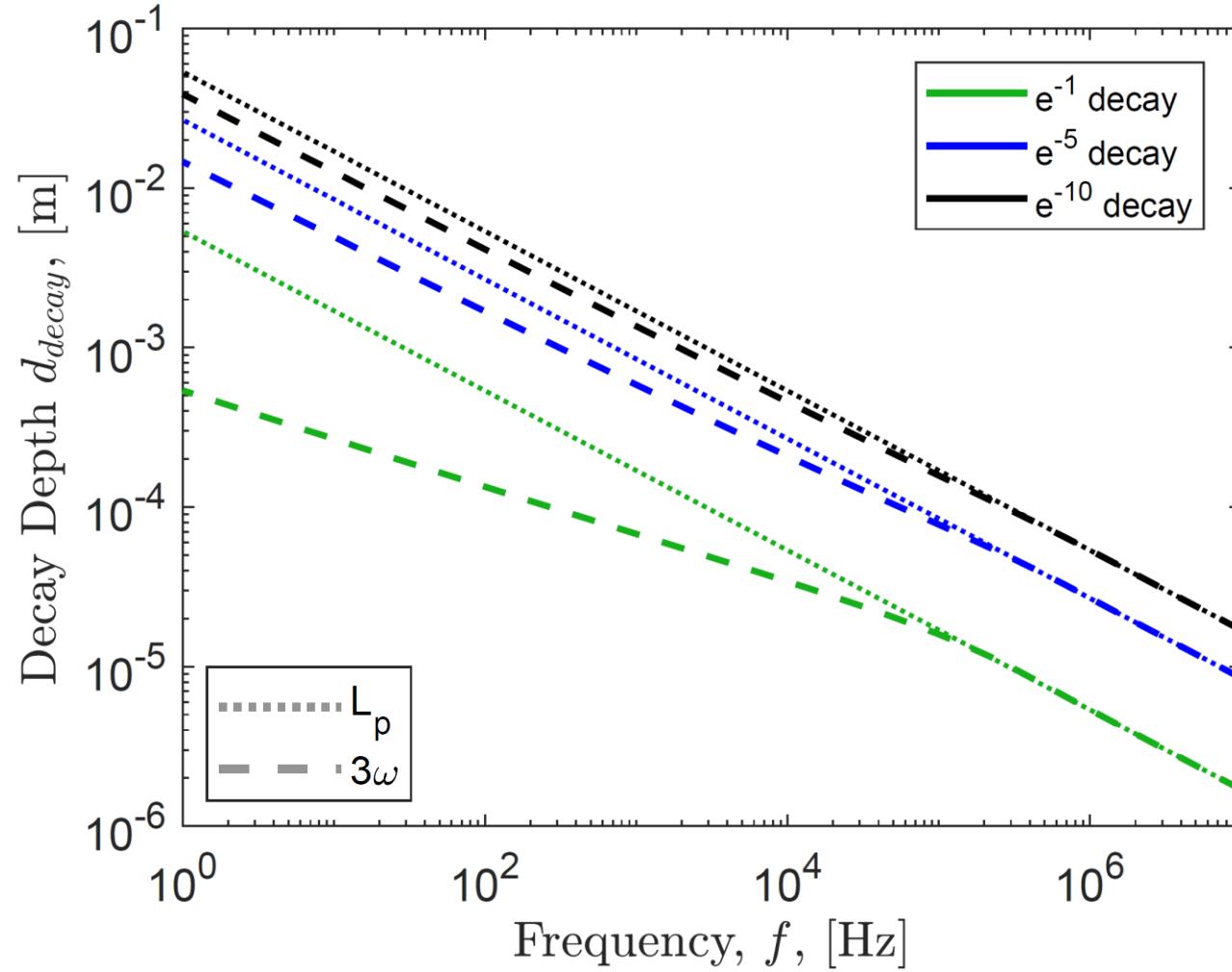


$$L_p = \sqrt{\frac{2\alpha}{\omega}}$$



9 | Thermal Length Scales

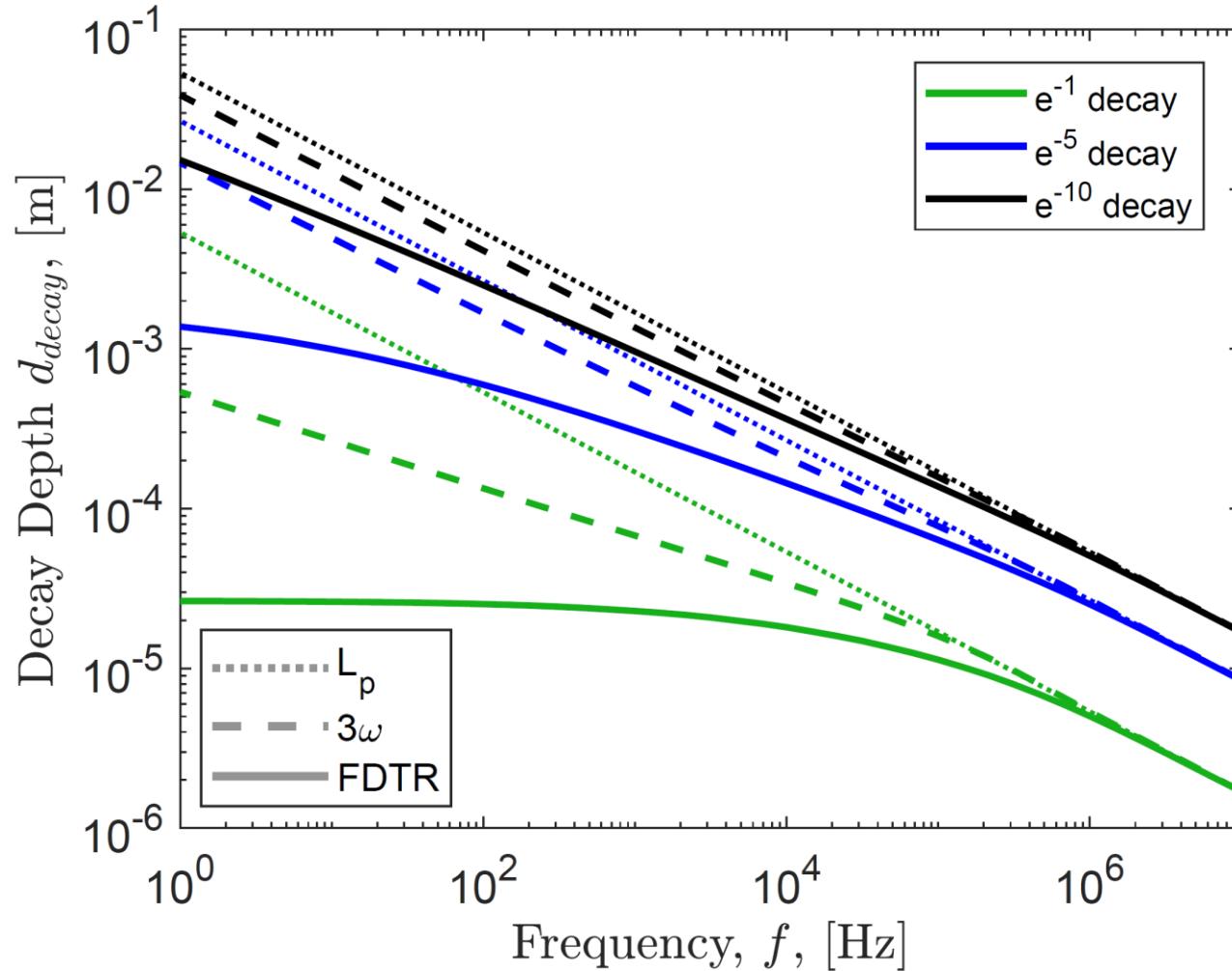
$$L_p = \sqrt{\frac{2\alpha}{\omega}}$$



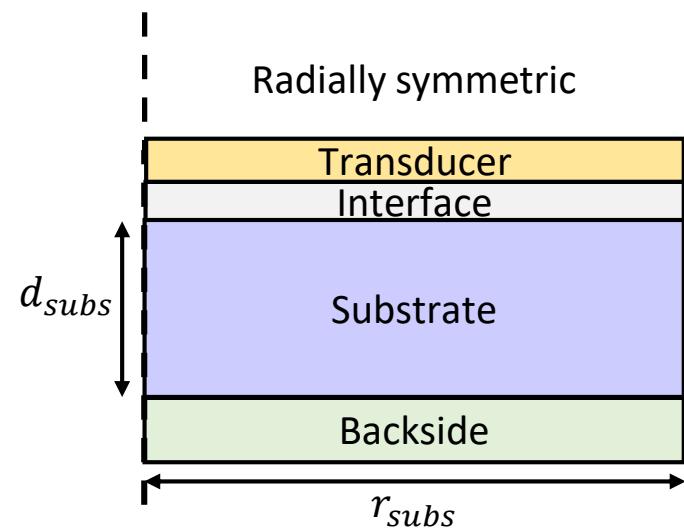
Thermal Length Scales



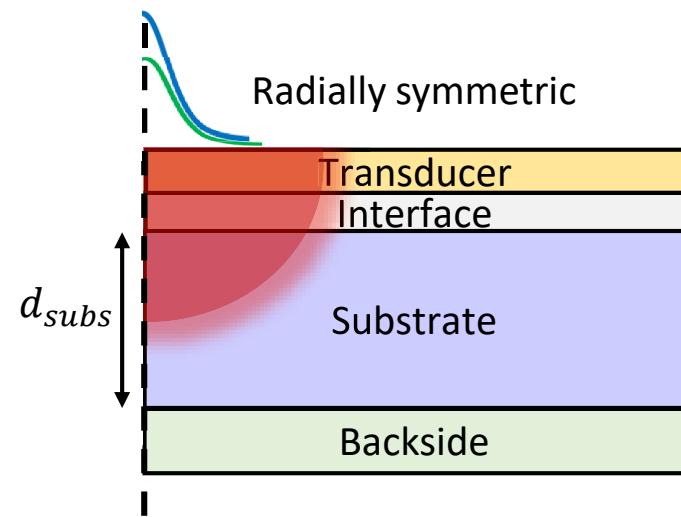
$$L_p = \sqrt{\frac{2\alpha}{\omega}}$$



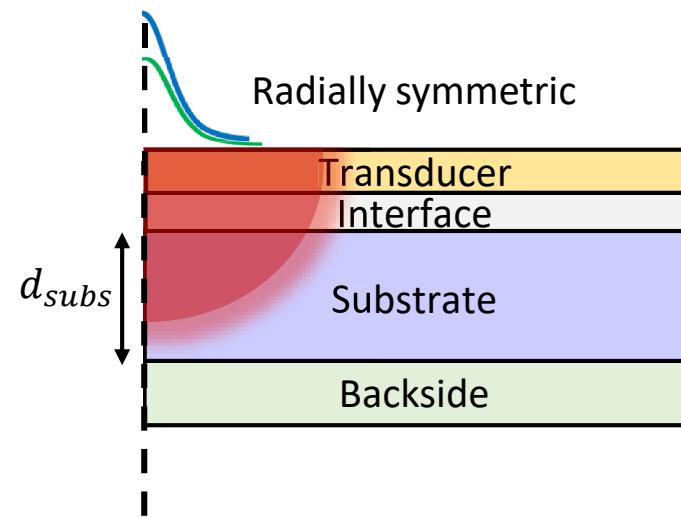
Sensing Lengths [L_s]



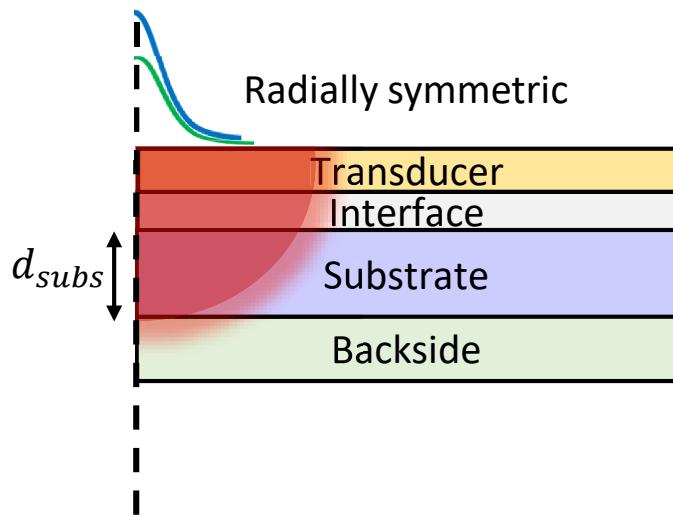
Sensing Lengths [L_s]



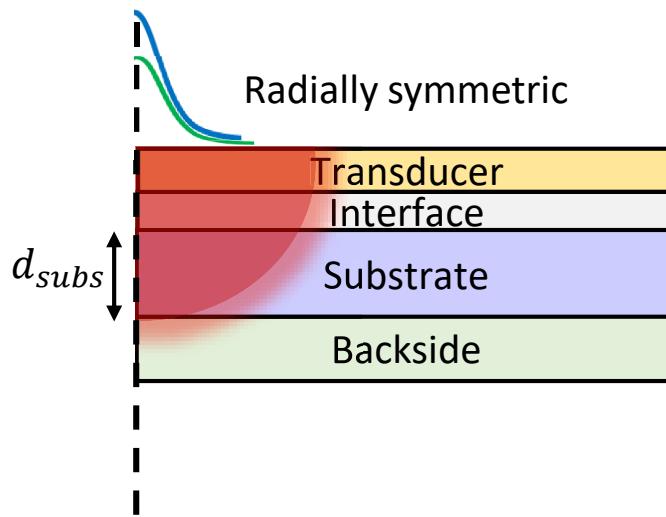
Sensing Lengths [L_s]



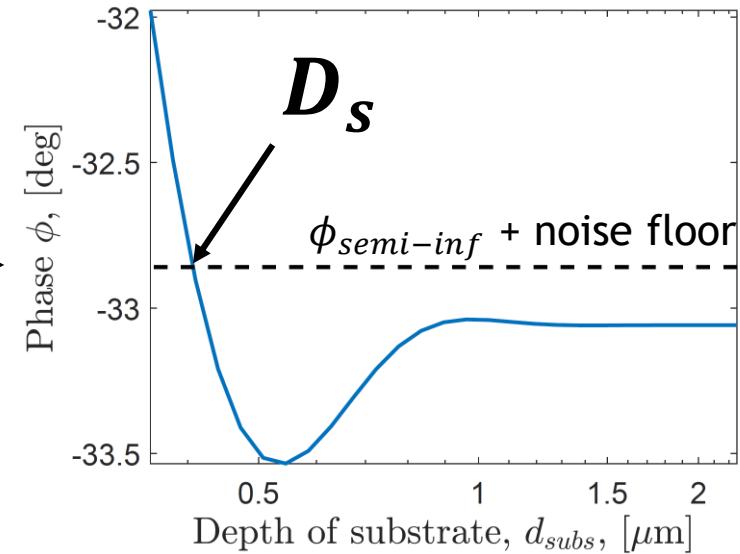
Sensing Lengths [L_s]



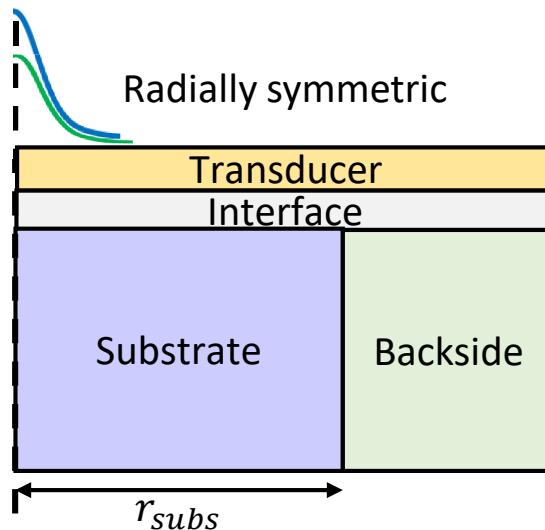
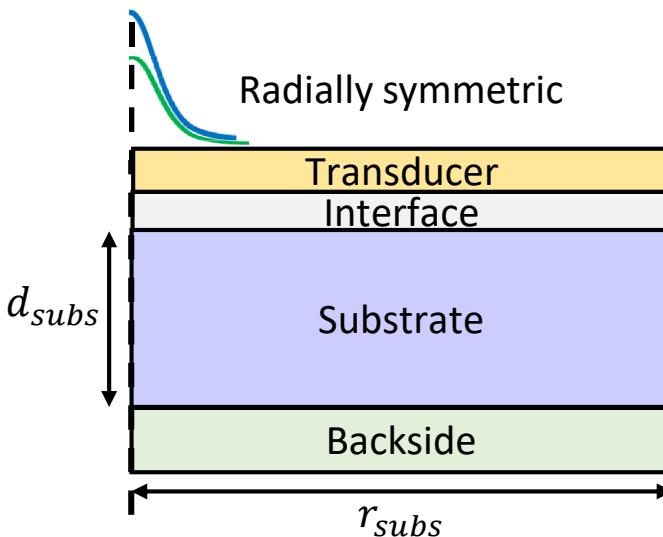
Sensing Lengths [L_s]



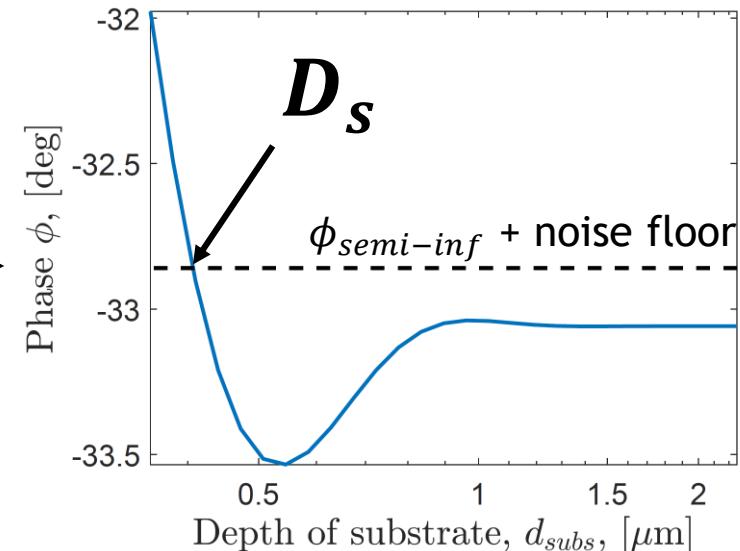
Vary d_{sub}



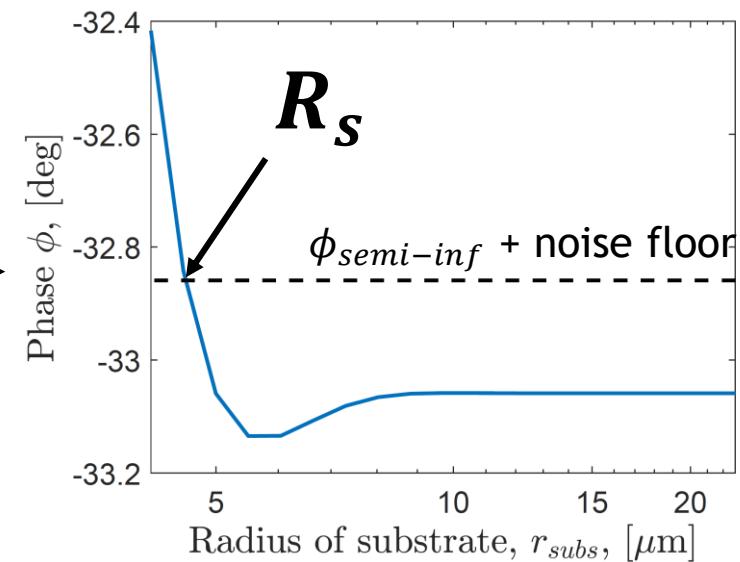
Sensing Lengths [L_s]

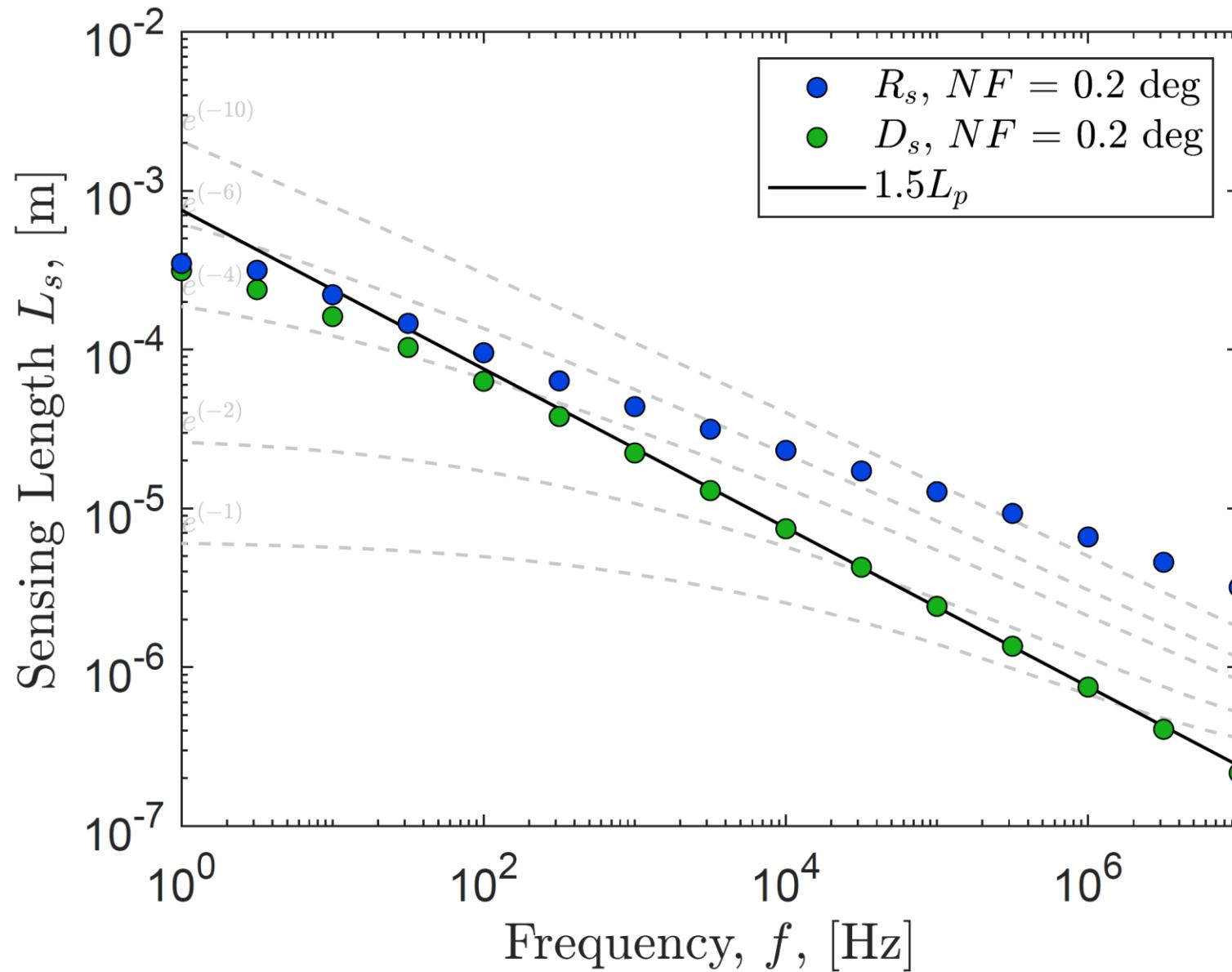


Vary d_{sub}

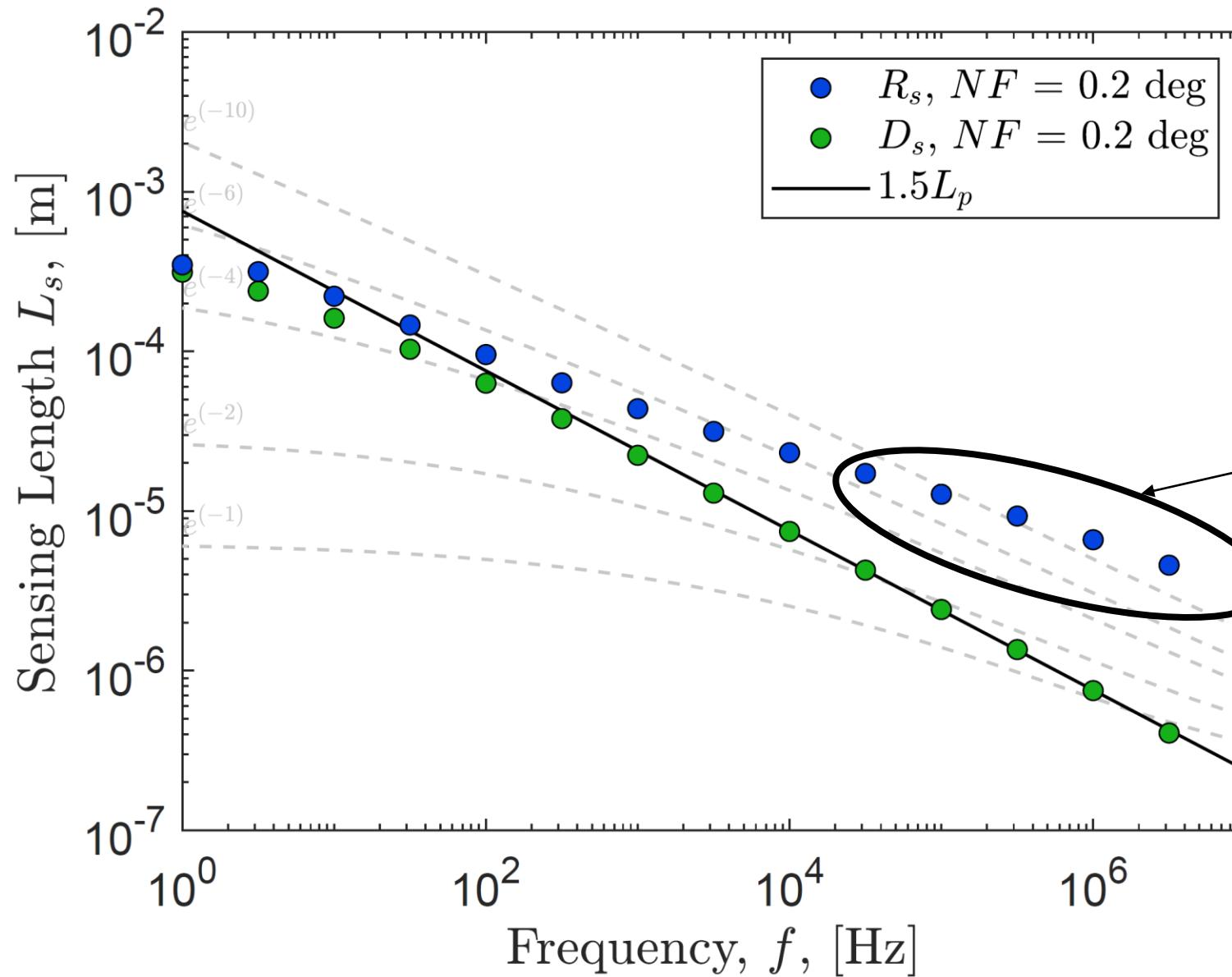


Vary r_{sub}



Sensing Lengths - SiO_2 

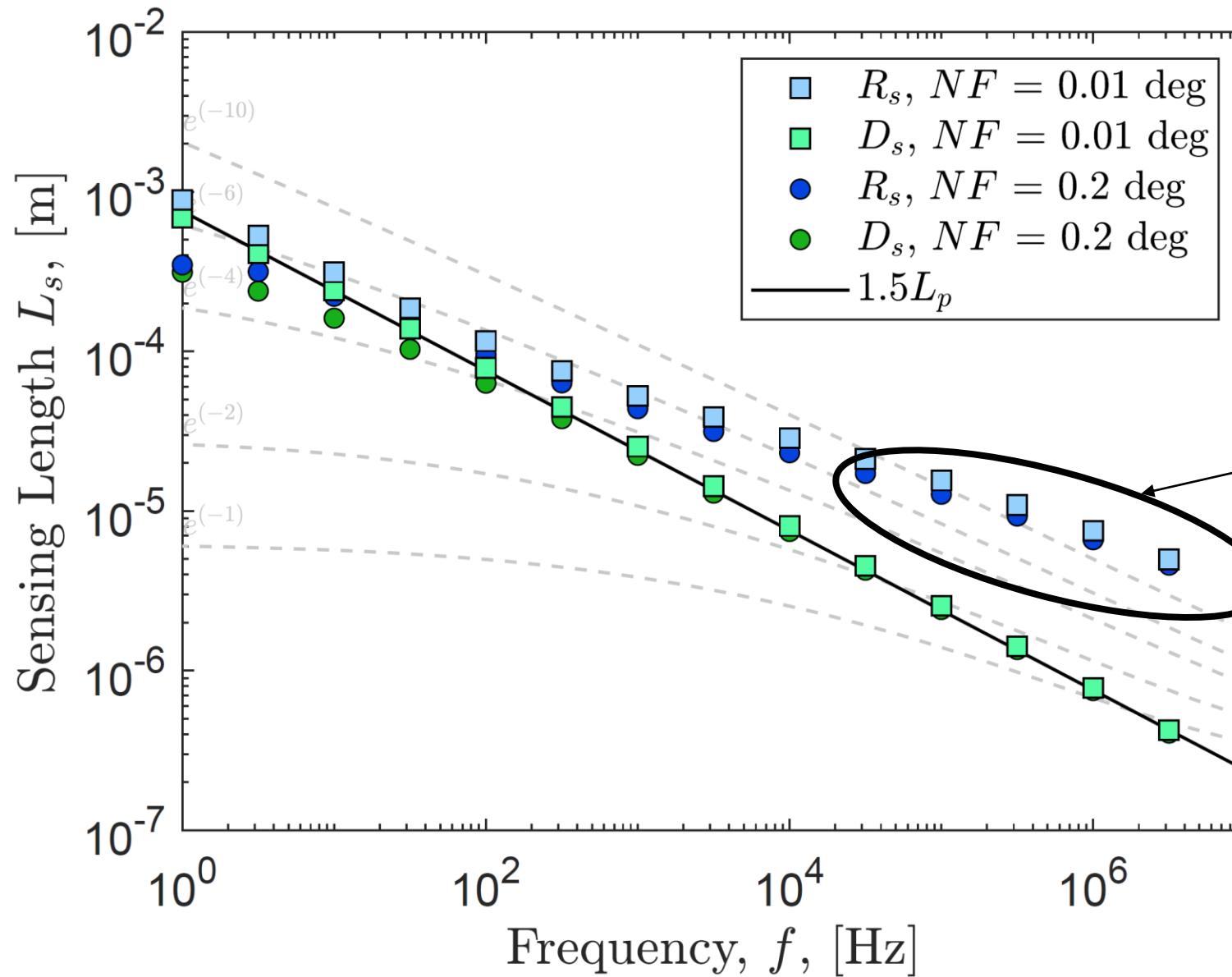
Sensing Lengths - SiO_2



$$\alpha_{Transducer} \gg \alpha_{SiO_2}$$



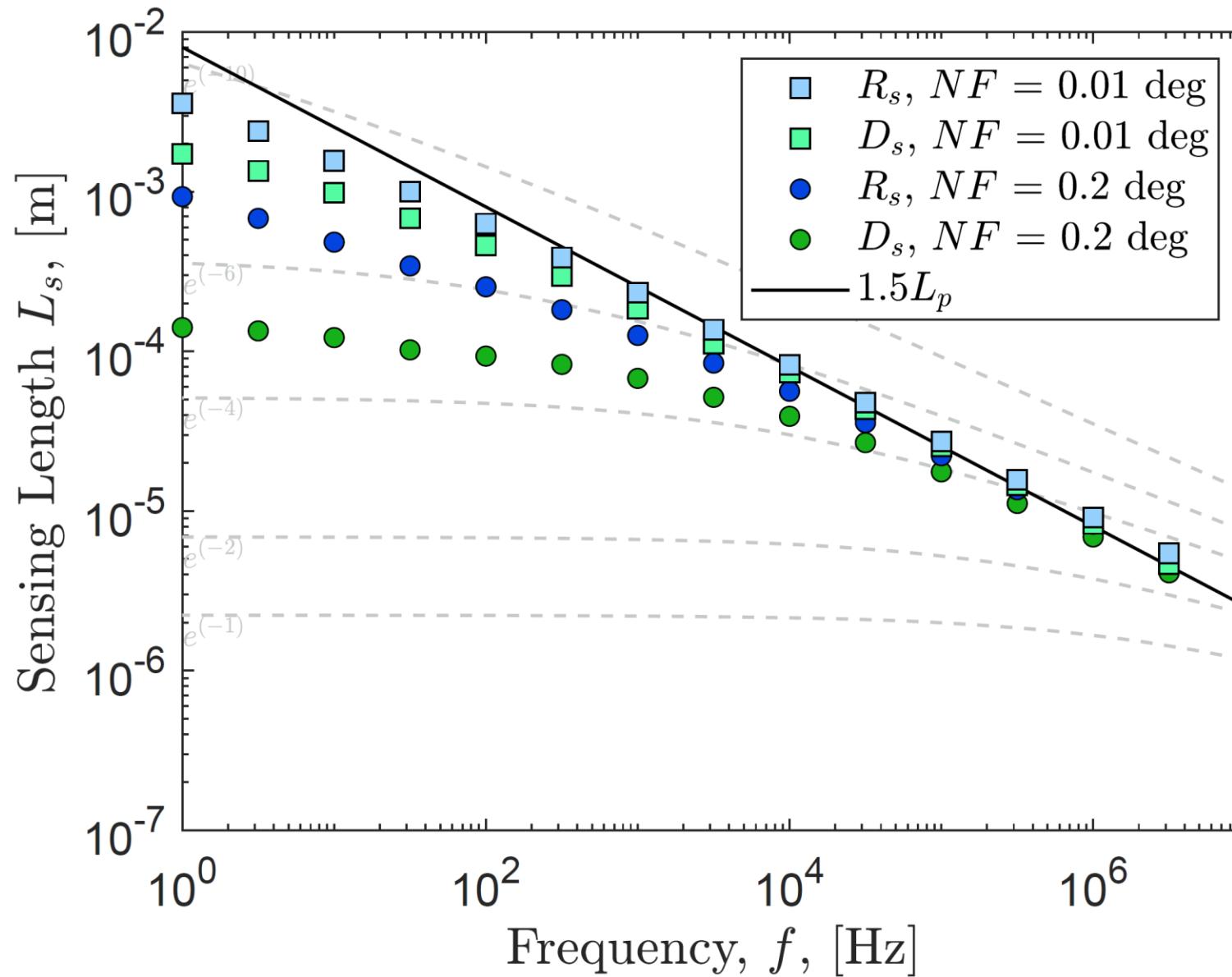
Sensing Lengths - SiO_2



Transducer layer causes increased radial heat spreading

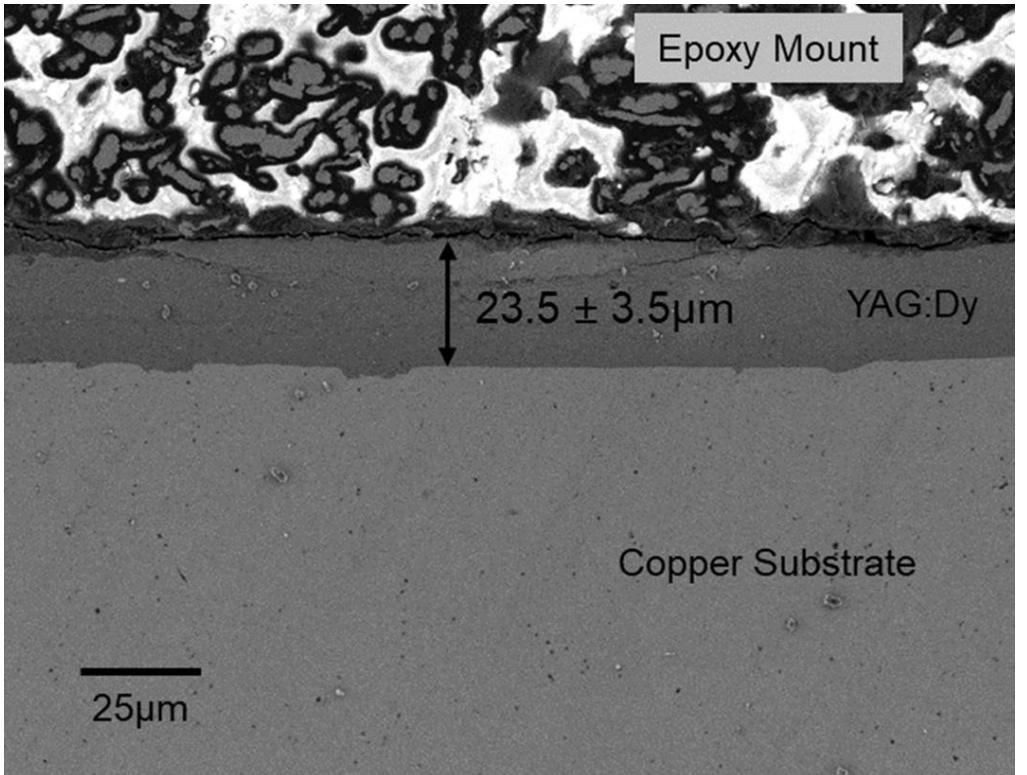
$\alpha_{Transducer} \gg \alpha_{SiO_2}$

Sensing Lengths - Silicon



$$\alpha_{Transducer} \sim \alpha_{Si}$$

Experimental Results – YAG film

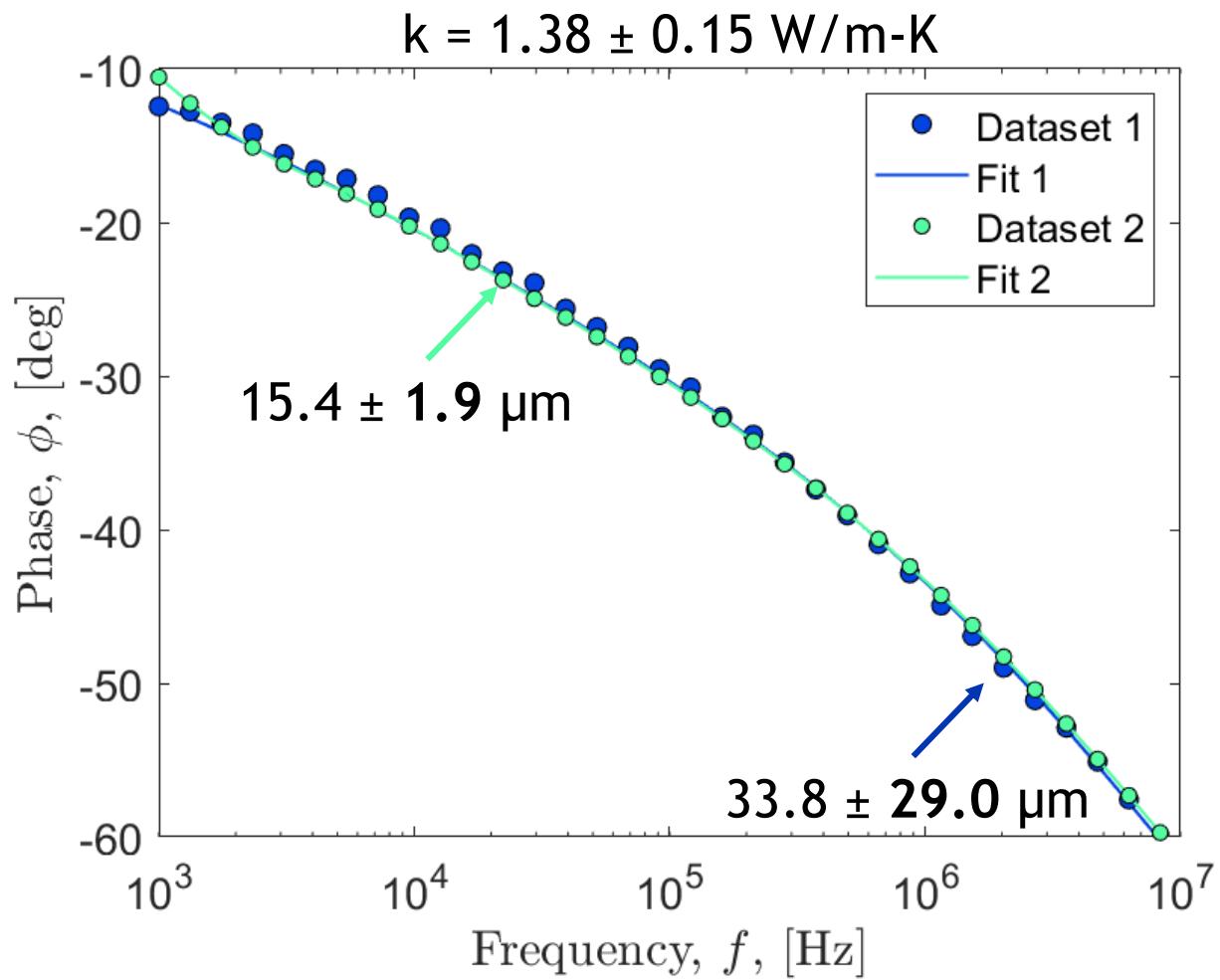
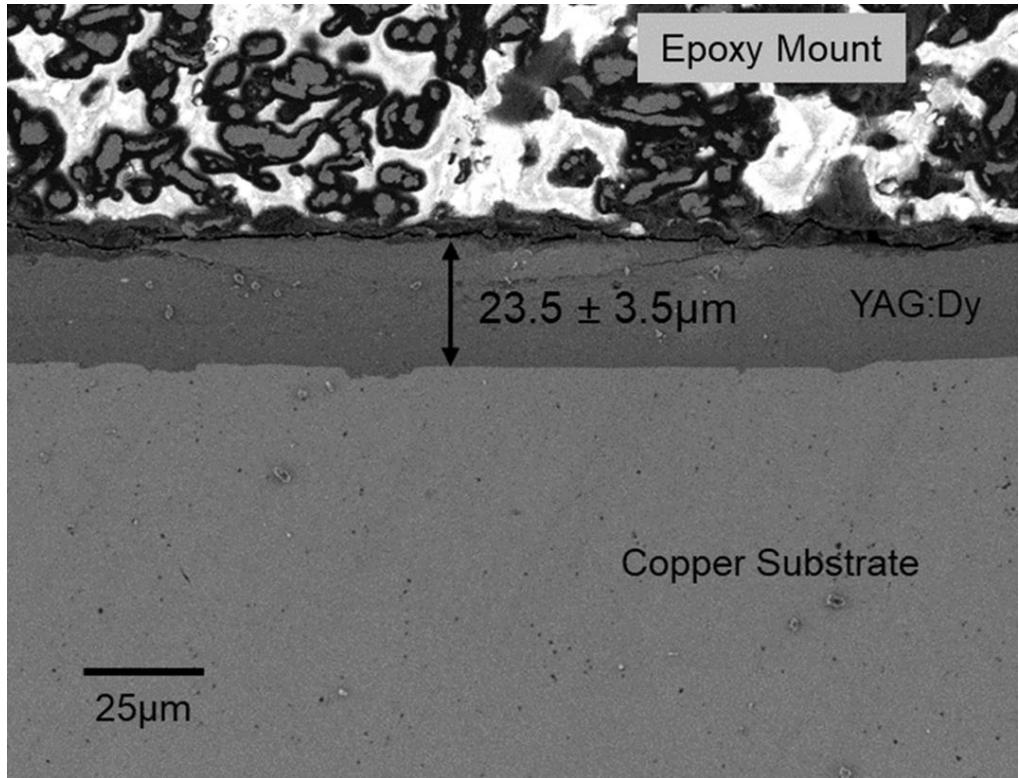


YAG → Yttrium Aluminum Garnet, $\text{Y}_3\text{Al}_5\text{O}_{12}$



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Experimental Results – YAG film thickness fitting



YAG → Yttrium Aluminum Garnet, $\text{Y}_3\text{Al}_5\text{O}_{12}$

Conclusions

- Thermal penetration depth, temperature decay depth and sensing length are distinct concepts
- Sensing lengths in FDTR scales with thermal penetration depth at high frequency
- Lowering noise floor increases sensing length at low frequency
- Measurement of films thicker than sensing depth results in higher uncertainty, matching predictions

