Towards Scalable Dataframe Systems

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ABSTRACT

Dataframes are a popular abstraction to represent, prepare, and analyze data. Despite the remarkable success of dataframe libraries in R and Python, dataframes face performance issues even on moderately large datasets. Moreover, there is significant ambiguity regarding dataframe semantics. In this paper we lay out a vision and roadmap for scalable dataframe systems. To demonstrate the potential in this area, we report on our experience building MODIN, a scaled-up implementation of the most widely-used and complex dataframe API today, Python's `pandas`. With pandas as a reference, we propose a simple data model and algebra for dataframes to ground discussion in the field. Given this foundation, we lay out an agenda of open research opportunities where the distinct features of dataframes will require extending the state of the art in many dimensions of data management. We discuss the implications of signature dataframe features including flexible schemas, ordering, row/column equivalence, and data/metadata fluidity, as well as the piecemeal, trial-and-error-based approach to interacting with dataframes.

1. INTRODUCTION

For all of their commercial successes, relational databases have notable limitations when it comes to "quick-and-dirty" exploratory data analysis (EDA) [62]. Data needs to be defined schema-first before it can be examined, data that is not well-structured is difficult to query, and any query beyond SELECT * requires an intimate familiarity with the schema, which is particularly problematic for wide tables. For more complex analyses, the declarative nature of SQL makes it awkward to develop and debug queries in a piecewise, modular fashion, conflicting with best practices for software development. Due in part to these limitations, SQL is often not the tool of choice for data exploration. As an alternative, programming languages such as Python and R support the so-called *dataframe* abstraction. Dataframes provide a functional interface that is more

tolerant of unknown data structure and well-suited to developer and data scientist workflows, including REPL-style imperative interfaces and data science notebooks [51].

Dataframes have several characteristics that make them an appealing choice for data exploration:

- an intuitive data model that embraces an implicit ordering on both columns *and* rows and treats them symmetrically;
- a query language that bridges a variety of data analysis modalities including relational (e.g., filter, join), linear algebra (e.g., transpose), and spreadsheet-like (e.g., pivot) operators;
- an incrementally composable query syntax that encourages easy and rapid validation of simple expressions, and their iterative refinement and composition into complex queries; and
- native embedding in a host language such as Python with familiar imperative semantics.

Characteristics such as these have helped dataframes become incredibly popular for EDA. The dataframe abstraction provided by pandas within Python (`pandas.pydata.org`), has as of 2020 been downloaded over 300 million times, served as a dependency for over 222,000 repositories in GitHub, and accumulated more than 25,000 stars on GitHub. Python's own popularity has been attributed to the success of pandas for data exploration and data science [7, 8].

Pandas has been developed from the ground up via open-source contributions from dozens of contributors, each providing operators and their implementations to the DataFrame API to satisfy immediate or ad-hoc needs, spanning capabilities that mimic relational algebra, linear algebra, and spreadsheet computation. To date, the pandas DataFrame API has ballooned to over 200 operators [12]. R, which is both more mature and more carefully curated, has only 70 operators—but this still far more than, say, relational and linear algebra combined [13].

While this rich API is sometimes cited as a reason for pandas' attractiveness, the set of operators has significant redundancies, often with different performance implications. These redundancies place a considerable burden on users, who must perform query planning (via selection of the appropriate pandas API calls) manually. For example, one blog post cites five different ways to express the same goal, with performance varying from 0.3ms to 600ms (a 1700× increase) [6]; meanwhile, the pandas documentation itself offers multiple recommendations for how to enhance performance [9]. As a result, many users eschew the bulk of the API, relying only on a small subset of operators [11]. The complexity of the API and evaluation semantics also makes it difficult to apply traditional query optimization techniques. Indeed, each operator within a pandas "query plan" is executed completely before subsequent operators are executed with limited optimization and without reordering or pipelining (unless explicitly done so by the user using `.pipe`). More-
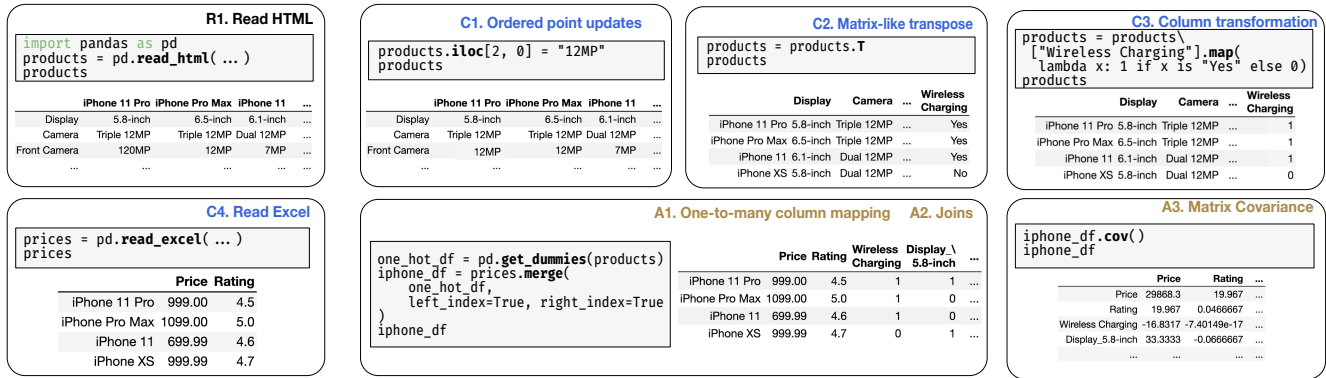
Figure 1: Example of an end-to-end data science workflow, from data ingestion, preparation, wrangling, to analysis.

over, the performance of the `pandas.DataFrame` API breaks down when processing even moderate volumes of data that do not fit in memory (demonstrated in Section 3)—this is especially problematic due to pandas' eager evaluation semantics, wherein intermediate data size often surpasses memory limits and must be paged to disk.

To address pandas' scalability challenges, we developed MO-DIN (`github.com/modin-project/modin`), our early implementation of a scalable dataframe system, which employs parallel query execution to enable unmodified pandas code to run more efficiently on large dataframes. MODIN is used by over 60 downstream projects, and has over 250 forks and 4,800 stars on GitHub in its first 20 months, indicating the impact and need for scalable dataframe implementations. MODIN rewrites pandas API calls into a sequence of operators in a new, compact dataframe algebra. MODIN then leverages simple parallelization and a new physical representation to speed up the execution of these operators by up to $30\times$ in certain cases, and is able to complete queries on datasets $25\times$ larger than pandas in others.

Our initial optimizations in MODIN are promising, but only scratch the surface of what's possible. Given the success of our first experience with MODIN, we believe there is room for a ***broad, community research agenda on making dataframe systems scalable and efficient***, with many novel research challenges. Our original intent when developing MODIN was to adapt standard relational database techniques to help make dataframes scalable. However, while the principles (such as parallelism) do apply, their instantiation in the form of specific techniques often differ, thanks to the differences between the data models and algebra of dataframes and relations. Therefore, a more principled foundation for dataframes is needed, comprising a formal data model and an expressive and compact algebra. We describe our first attempt at such a formalization in Section 4. Then, armed with our data model and algebra, we outline a number of research challenges organized around unique dataframe characteristics and the unique ways in which they are processed.

In Section 5, we describe how the dataframe data model and algebra result in new scalability challenges. Unlike relations, dataframes have a flexible schema and are lazily typed, requiring careful maintenance of metadata, and avoidance of the overhead of type inference as far as possible. Dataframes treat rows and columns as equivalent, and metadata (column/row labels) and data as equivalent, placing new metadata awareness requirements on dataframe query planners. In addition, dataframes are ordered—and dataframe systems often enforce a strict coupling between logical and physical layout; we identify several opportunities to deal with order in a more light-weight, decoupled, and lazy fashion. Finally, the new space of operators—encompassing relational, linear algebra, and spreadsheet operators—introduce new challenges in query optimization.

In Section 6, we describe new challenges and opportunities that emerge from how dataframes are used for data exploration. Unlike SQL, which offers an all-or-nothing query modality, dataframe queries are constructed one operator at a time, with ample think-time between query fragments. This makes it more challenging to perform query optimization by reordering operators for higher overall efficiency. At the same time, the additional thinking time between steps can be exploited to do background processing. Dataframe users often inspect intermediate results of query fragments, usually for debugging, which requires a costly materialization after each step of query processing. However, users are only shown an ordered prefix or suffix of this intermediate dataframe as output, allowing us to prioritize the execution to return this portion quickly and defer the execution of the rest. Finally, users often revisit old processing steps in an ad-hoc process of trial-and-error data exploration. We consider opportunities to minimize redundant computation for operations completed previously.

Outline and Contributions. In this paper, we begin with an example dataframe workflow capturing typical dataframe capabilities and user behavior. We then describe our experiences with MO-DIN (Section 3). We use MODIN to ground our discussion of the research challenges. We ***(i) provide a candidate formalism for dataframes*** and enumerate their capabilities with a new algebra (Section 4). We then outline research challenges and opportunities ***to build on our formalism and make dataframe systems more scalable,*** by optimizing and accounting for ***(ii) the unique characteristics of the new data model and algebra*** (Section 5), as well as ***(iii) the unique ways in which dataframes are used in practice for data exploration*** (Section 6). We draw on tools and techniques from the database research literature throughout and discuss how they might be adapted to meet novel dataframe needs.

In describing the aforementioned challenges, we focus on the pandas dataframe system [12] for concreteness. Pandas is much more popular than other dataframe implementations, and is therefore well worth our effort to study and optimize. We discuss other dataframe implementations and related work in Section 7. Many details about MODIN and our dataframe data model and algebra are omitted and can be found in our technical report [52].

2. DATAFRAME EXAMPLE

In Figure 1, we show the steps taken in a typical workflow of an analyst exploring the relationship between various features of different iPhone models in a Jupyter notebook [51].

Data ingest and cleaning. Initially, the analyst reads in the iPhone comparison chart using `read_html` from an e-commerce webpage, as shown in R1 in Figure 1. The data is verified by printing out the first few lines of the dataframe `products`. (`products.head()` is

also often used.) Based on this preview of the dataframe, the analyst identifies a sequence of actions for cleaning their dataset:

- C1 [Ordered point updates]: The analyst fixes the anomalous value of 120MP for Front Camera for the iPhone 11 Pro to 12MP, by performing a point update via `iloc`, and views the result.
- C2 [Matrix-like transpose]: To convert the data to a relational format, rather than one meant for human consumption, the analyst transposes the dataframe (via T) so that the rows are now products and columns features, and then inspects the output.
- C3 [Column transformation]: The analyst further modifies the dataframe to better accommodate downstream data processing by changing the column "Wireless Charging" from "Yes/No" to binary. This is done by updating the column using a user-defined `map` function, followed by displaying the output.
- C4 [Read Excel]: The analyst loads price/rating information by reading it from a spreadsheet into `prices` and then examines it.

Analysis. Then, the analyst performs the following operations to analyze the data:

- A1 [One-to-many column mapping]: The analyst encodes non-numeric features in a one-hot encoding scheme via the `get_dummies` function.
- A2 [Joins]: The iPhone features are joined with their corresponding price and rating using the `merge` function. The analyst then verifies the output.
- A3 [Matrix Covariance]: With all the relevant numerical data in the same dataframe, the analyst computes the covariance between the features via the `cov` function, and examines the output.

This example demonstrated only a sample of the capabilities of dataframes. Nevertheless, it serves to illustrate the common use cases for dataframes: immediate visual inspection after most operations, each incrementally building on the results of previous ones, point and batch updates via user-defined functions, and a diverse set of operators for wrangling, preparing, and analyzing data.

3. THE MODIN DATAFRAME SYSTEM

While the pandas API is convenient and powerful, the underlying implementation has many scalability and performance problems. We therefore started an effort to develop a "drop-in" replacement for the pandas API, MODIN[1], to address these issues. In the style of embedded database systems [37, 53], MODIN is a library that runs in the same process as the application that imports it. We briefly describe the challenges we encountered and the lessons we learned during our implementation in Section 3.1, followed by a preliminary case study of MODIN's performance in Section 3.2. We defer detailed treatment of MODIN's architecture to our technical report [52].

3.1 Modin Engineering Challenges

When we started our effort to make pandas more scalable, we identified that while many operations in pandas are fast, they are limited by their single-threaded implementation. Therefore, our starting point for MODIN was to add multi-core capabilities and other simple performance improvements to enable pandas users to run their same unmodified workflows both faster and on larger datasets. However, we encountered a number of engineering challenges.

Massive API. The pandas API has over 240 distinct operators, making it challenging to individually optimize each one. After manually

trying to parallelize each operator within MODIN, we tried a different approach. We realized that there is a lot of redundancy across these 240 operators. Most of these operators can be rewritten into an expression composed using a much smaller set of operators. We describe our compact set of dataframe operators—our working dataframe algebra—in Section 4.3. Currently, MODIN supports over 85% of the `pandas.DataFrame` API, by rewriting API calls into our working algebra, allowing us to avoid duplicating optimization logic as much as possible. The operators we prioritized were based on an analysis of over 1M Jupyter notebooks, the results of which are discussed in our technical report [52]. Specifically, we targeted all the functionality in `pandas.DataFrame`, `pandas.Series`, and pandas utilities (e.g., `pd.concat`). To use MODIN instead of pandas, users can simply invoke "`import modin.pandas`", instead of "`import pandas`", and proceed as they would previously.

Parallel execution. Since most pandas operators are single-threaded, we looked towards parallelism as a means to speed up execution. Parallelization is commonly used to improve performance in a relational context due to the embarrassingly parallel nature of relational operators. Dataframes have a different set of operators than relational tables, supporting relational algebra, linear algebra, and spreadsheet operators, as we saw in Section 2, and we will discuss in Section 4. We implemented different internal mechanisms for exploiting parallelism depending on the data dimensions and operations being performed. Some operations are embarrassingly parallel and can be performed on each row independently (e.g., C3 in Figure 1), while others (e.g., C2, A1, A3) cannot. To address the challenge of differing levels of parallelism across operations, we designed MODIN to be able to flexibly move between common partitioning schemes: row-based (i.e., each partition has a collection of rows), column-based (i.e., each partition has a collection of columns), or block-based partitioning (i.e., each partition has a subset of rows and columns), depending on the operation. Each partition is then processed independently by the execution engine, with the results communicated across partitions as needed.

Supporting billions of columns. While parallelism does address some of the scalability challenges, it fails to address a major one: the ability to support tables with billions of columns—something even traditional database systems do not support. Using the pandas API, however, it is possible to transpose a dataframe (as in Step C2) with billions of rows into one with billions of columns. In many settings, e.g., when dealing with graph adjacency matrices in neuroscience or genomics, the number of rows and number of columns can both be very large. For these reasons, MODIN treats rows and columns essentially equivalently, a property of dataframes will discuss in detail in Section 4. In particular, to transpose a large dataframe, MODIN employs block-based partitioning, where each block consists of a subset of rows and columns. Each of the blocks are individually transposed, followed by a simple change of the overall metadata tracking the new locations of each of the blocks. The result is a transposed dataframe that does not require any communication.

3.2 Preliminary Case Study

To understand how the simple optimizations discussed above impact the scalability of dataframe operators, we perform a small case study evaluating MODIN's performance against that of pandas using microbenchmarks on an EC2 x1.32xlarge (128 cores and 1,952 GB RAM) node using a New York City taxicab dataset [48] that was replicated 1 to 11 times to yield a dataset size between 20 to 250 GB, with up to 1.6 billion rows. We consider four queries:

- map: check if each value in the dataframe is null, and replace it with a `TRUE` if so, and `FALSE` if not.

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[1] MODIN's name is derived from the Korean word for "every", as it targets every dataframe operator.
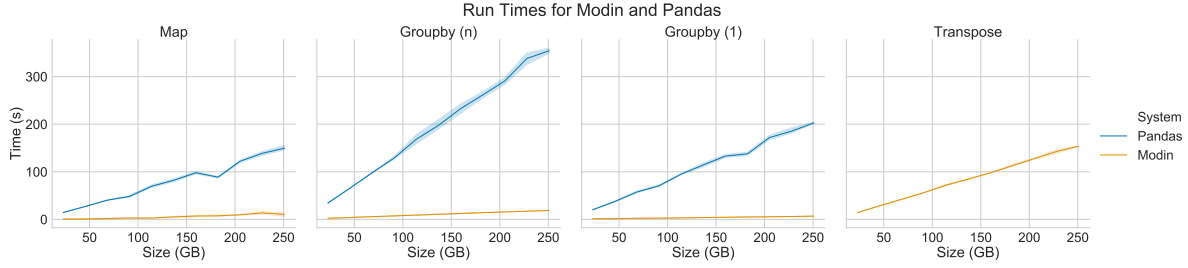
Figure 2: Each function shows runtime and 95% confidence region for both MODIN and pandas. We omit pandas transpose as it is unable to scale beyond 6 GB.

- group-by (n): group by the non-null "passenger_count" column and count the number of rows in each group.
- group-by (1): count the number of non-null rows in the dataframe.
- transpose: swap the columns and rows of the dataframe and apply a simple (map) function across the new rows.

We highlight the difference between group by with one group and n groups, because with n groups data shuffling and communication are a factor in performance. With group-by(1), the communication overheads across groups are non-existent. We include transpose to demonstrate that MODIN can handle data with billions of columns.

Figure 2 shows that for the group-by (n) and group-by (1) operations, MODIN yields a speedup of up to $19\times$ and $30\times$ relative to pandas, respectively. For example, a group-by (n) on a 250GB dataframe, pandas takes about 359 seconds and MODIN takes 18.5 seconds, a speedup of more than $19\times$. For map operations, MODIN is about $12\times$ faster than pandas. These performance gains come from simple parallelization of operations within MODIN, while pandas only uses a single core. During the evaluation of transpose, pandas was unable to transpose even the smallest dataframe of 20 GB ($\sim$150 million rows) after 2 hours. Through separate testing, we observed that pandas can only transpose dataframes of up to 6 GB ($\sim$6 million rows) on the hardware we used for testing.

Takeaways. Our preliminary case study and our experience with MODIN demonstrates the promise of integrating simple optimizations to make dataframe systems scalable. Next, we define a dataframe data model and algebra to allow us to ground our subsequent discussion of our research agenda, targeting the unique characteristics of dataframes and the unique ways in which they are used. We defer further performance analyses of MODIN to future work.

4. DATAFRAME FUNDAMENTALS

There are many competing open-source and commercial implementations of dataframes, but there is no formal definition or enumeration of dataframe properties in the literature to date. We therefore propose a formal definition of dataframes to allow us to describe our subsequent research challenges on a firm footing, and also to provide background to readers who are unfamiliar with dataframes. In this section, we start with a brief history (Section 4.1), and provide a reference data model (Section 4.2) and algebra (Section 4.3) to ground discussion. We then demonstrate the expressiveness of the algebra via a case study (Section 4.4). Our technical report has additional details about the formalism, the mapping to the pandas API, other extensions to the data model, as well as quantitative statistics on dataframe usage [52].

4.1 A Brief History of Dataframes

The S programming language was developed at Bell Laboratories in 1976 to support statistical computation. Dataframes were first introduced to S in 1990, and presented by Chambers, Hastie, and Pregibon at the Computational Statistics conference [24]. The authors state: "We have introduced into S a class of objects called

`data.frames`, which can be used if convenient to organize all of the variables relevant to a particular analysis ..." Chambers and Hastie then extended this paper into a 1992 book [25], which states "Data frames are more general than matrices in the sense that matrices in S assume all elements to be of the same mode—all numeric, all logical, all character string, etc." and "... data frames support matrix-like computation, with variables as columns and observations as rows, and, in addition, they allow computations in which the variables act as separate objects, referred to by name."

The R programming language, an open-source implementation of S, was first released in 1995, with a stable version released in 2000, and gained instant adoption among the statistics community. Finally, in 2008, Wes McKinney developed pandas in an effort to bring dataframe capabilities with R-like semantics to Python, which as we described in the introduction, is now incredibly popular. We discuss other dataframe implementations in Section 7.

4.2 Dataframe Data Model

As Chambers and Hastie themselves state, dataframes are not familiar mathematical objects. Dataframes are not quite relations, nor are they matrices or tensors. In our definitions we borrow textbook relational terminology from Abiteboul, et al. [15, Chapter 3] and adapt it to our use.

The elements in the dataframe come from a known set of domains $Dom = \{\mathbf{dom}_1, \mathbf{dom}_2, ...\}$. For simplicity, we assume in our discussion that domains are taken from the set $Dom = \{\Sigma^*, \mathbf{int}, \mathbf{float}, \mathbf{bool}, \mathbf{category}\}$, though a few other useful domains like datetimes are common in practice. The domain Σ^* is the set of finite strings over an alphabet Σ, and serves as a default, uninterpreted domain; in some dataframe libraries it is called **Object**. Each domain contains a distinguished $null$ value, sometimes written as `NA`. Each domain $\mathbf{dom}_i$ also includes a *parsing function* $p_i : \Sigma^* \to \mathbf{dom}_i$, allowing us to interpret the values in dataframe cells as domain values.

A key aspect of a dataframe is that the domains of its columns may be induced from data *post hoc*, rather than being declared *a priori* as in the relational model. We define a **schema induction function** $S : (\Sigma^*)^m \to Dom$ that assigns an array of m strings to a domain in Dom. This schema induction function is applied to a given column and returns a domain that describes this array of strings; we will return to this function later.

Armed with these definitions, we can now define a dataframe:

Definition 4.1. A **dataframe** is a tuple (A_{mn}, R_m, C_n, D_n), where A_{mn} is an array of entries from the domain Σ^*, R_m is a vector of row labels from Σ^*, C_n is a vector of column labels from Σ^*, and D_n is a vector of n domains from Dom, one per column, each of which can also be left unspecified. We call D_n the *schema* of the dataframe. If any of the n entries within D_n is left unspecified, then that domain can be induced by applying $S(\cdot)$ to the corresponding column of A_{mn}.

We depict our conceptualization of dataframes in Figure 3. In our example of Figure 1, dataframe `products` after step R1 has R_m corresponding to an array of labels [Display, Camera, ...]; C_n corresponding to an array of labels [iPhone 11 Pro, iPhone Pro

Max, ...]; A_{mn} corresponding to the matrix of values beginning with `5.8-inch`, with $m = 6, n = 4$. Here, D_n is left unspecified, and may be inferred using $S(\cdot)$ per column to possibly correspond to $[\Sigma^*, \Sigma^*, \Sigma^*, \Sigma^*]$, since each of the columns contains strings.

Rows and columns are symmetric in many ways in dataframes. Both can be referenced explicitly, using either numeric indexing (positional notation) or label-based indexing (named notation). In our example in Figure 1, the `products` dataframe is referenced using positional notation in step C1 with `products.iloc[2, 0]` to modify the value in the third row and first column, and by named notation in step C3 using `products ["Wireless Charging"]` to modify the column corresponding to `"Wireless Charging"`. The relational model traditionally provides this kind of referencing only for columns. Note that row position is exogenous to the data—it *need not* be correlated in any way to the data values, unlike sort orderings found in relational extensions like SQL's `ORDER BY` clause. The positional notation allows for (row, col) references to index individual values, as is familiar from matrices.

A subtler distinction is that row and column labels are from the same set of domains as the underlying data (Dom), whereas in the traditional relational model, column names are from a separate domain (called **att** [15]). This is important to point out because there are dataframe operators that copy data values into labels, or copy labels into data values, discussed further in Section 4.3.

One distinction between rows and columns in our model is that columns have a schema, but rows do not. Said differently, we parse the value of any cell based on the domain of its column. We can also imagine an orthogonal view, in which we define explicit schemas (or use a schema induction function) on rows, and a corresponding row-wise parsing function for the cells. In our formalism, this is achieved by an algebraic operator to transpose the table and treat the result column-wise (Section 4.3). By restricting the data model to a single axis of schematization, we provide a simple unique interpretation of each cell, yet preserve a flexibility of interpretation in the algebra. In Sections 5.1.2 and 5.2.2 we return to the performance and programming implications of programs that make use of schemas on a dataframe and its transpose (i.e. "both axes").

When the schema D_n has the same domain **dom** for all n columns, we call this a *homogeneous* dataframe. As a special case, consider a homogeneous dataframe with a domain like **float** or **int** and operators $+, \times$ that satisfy the algebraic definition of a field. We call this a *matrix* dataframe, since it has the algebraic properties required of a matrix, and can participate in linear algebra operations simply by parsing its values and ignoring its labels. The dataframe `iphone_df` after step A2 in Figure 1 is one such example; thus it was possible to perform the covariance operation in step C3. Matrix dataframes are commonly used in machine learning pipelines.

Overall, while dataframes have roots in both relational and linear algebra, they are neither tables nor matrices. Specifically, when viewed from a relational viewpoint, the dataframe data model differs in the following ways:

Dataframe Characteristic	Relational Characteristic
Ordered table	Unordered table
Named rows labels	No naming of rows
A lazily-induced schema	Rigid schema
Column names from $d \in Dom$	Column names from att [15]
Column/row symmetry	Columns and rows are distinct
Support for linear alg. operators	No native support

And when viewed from a matrix viewpoint, the dataframe data model differs in the following ways:
We will exploit these two viewpoints in our dataframe algebra to allow us to define both relational and linear algebra operations. Due

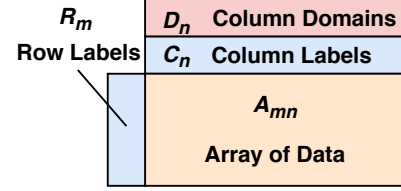| Dataframe Characteristic	Matrix Characteristic
Heterogeneously typed	Homogeneously typed
Both numeric and non-numeric types	Only numeric types
Explicit row and column labels	No row or column labels
Support for rel. algebra operators	No native support

Figure 3: The Dataframe Data Model

to these differences, a new body of work will be needed to support the scale required for modern data science workflows.

4.3 Dataframe Algebra

While developing MODIN, we discovered that there exists a "kernel" of operators that encompasses the massive APIs of pandas and R. We developed this "kernel" into a new dataframe algebra, which we describe here, while explicitly contrasting it with relational algebra. We do not argue that this set of operators is minimal, but we do feel it is both expressive and elegant; we demonstrate via a case study in Section 4.4 that it can be used to express `pivot`. Based on the contrast with relational algebra, we are in a position to articulate research challenges in optimizing dataframe algebra expressions in subsequent sections.

We list the algebra operators we have defined in Table 1: the rows correspond to the operators, and the columns correspond to their properties. The operators encompass ordered analogs of extended relational algebra operators (from `SELECTION` to `RENAME`), one operator that is not part of extended relational algebra but is found in many database systems (`WINDOW`), one operator with that admits independent use unlike in database systems (`GROUPBY`), as well as four new operators (`TRANSPOSE`, `MAP`, `TOLABELS`, and `FROMLABELS`). The ordered analogs of relational algebra operators preserve the ordering of the input dataframe(s). If there are multiple arguments, the result is ordered by the first argument first, followed by the second. For example, `UNION` simply concatenates the two input dataframes in order, while `CROSS-PRODUCT` preserves a nested order, where each tuple on the left is associated, in order, with each tuple on the right, with the order preserved.

We succinctly describe the new operators as well as highlight any deviating semantics of `GROUPBY` and `WINDOW` and leave detailed semantics to our technical report [52]. The output schema for most other relational operators can be carried over from the inputs (indicated as *static* in Table 1).

Transpose. `TRANSPOSE` interchanges rows and columns, so that the columns of the dataframe become the rows, and vice-versa. Formally, given a dataframe $DF = (A_{mn}, R_m, C_n, D_n)$, we define `TRANSPOSE`($DF$) to be a dataframe $(A_{nm}^T, C_n, R_m, null)$, where A_{nm}^T is the array transpose of A_{mn}. Note that the schema of the result may be induced by S, and may not be similar to the schema of the input. `TRANSPOSE` is useful both for matrix operations on homogenous dataframes, and for data cleaning or for presentation of "crosstabs" data. In step C2 in our example in Figure 1, the table was not oriented properly from ingest, and a transpose was required to give us the desired table orientation.

Map. The map operator takes some function f and applies it to each row individually, returning a single output row of fixed arity. The purpose of the map operator is to alter each dataframe row uniformly. `MAP` is useful for data cleaning and feature engineering (e.g., step C3 in Figure 1). Given a dataframe $DF = (A_{mn}, R_m, C_n, D_n)$,

Table 1: Dataframe Algebra. †: Ordered by left argument first, then right to break ties. ◊: Order of columns is inherited from order of rows and vice-versa.

Operator	(Meta)data	Schema	Origin	Order	Description
SELECTION		×	static	REL	Parent	Eliminate rows
PROJECTION		×	static	REL	Parent	Eliminate columns
UNION		×	static	REL	Parent†	Set union of two dataframes
DIFFERENCE		×	static	REL	Parent†	Set difference of two dataframes
CROSS PRODUCT / JOIN		×	static	REL	Parent†	Combine two dataframes by element
DROP DUPLICATES		×	static	REL	Parent	Remove duplicate rows
GROUPBY		×	static	REL	New	Group identical values for a given (set of) attribute(s)
SORT		×	static	REL	New	Lexicographically order rows
RENAME	(×)		static	REL	Parent	Change the name of a column
WINDOW		×	static	SQL	Parent	Apply a function via a sliding-window (either direction)
TRANSPOSE	(×)	×	dynamic	DF	Parent◊	Swap data and metadata between rows and columns
MAP	(×)	×	dynamic	DF	Parent	Apply a function uniformly to every row
TOLABELS	(×)	×	dynamic	DF	Parent	Set a data column as the row labels column
FROMLABELS	(×)	×	dynamic	DF	Parent	Convert the row labels column into a data column

the result of `MAP(DF, f)` is a dataframe $(A'_{mn'}, R_m, C'_{n'}, D'_{n'})$ with $f : D_n \to D'_{n'}$, where $A'_{mn'}$ is the result of the function f as applied to each row, $C'_{n'}$ is the resulting column labels, and $D'_{n'}$ is the resulting vector of domains. Notice that in this definition, the number of columns (n') *and* the column labels ($C'_{n'}$) can change based on this definition, but they must be changed uniformly for every row. The vector of domains $D'_{n'}$ may, in many cases, be inferred from the type of the function f.

ToLabels. The `TOLABELS` operator projects one column out of the matrix of data, A_{mn}, to be set as new row labels for the resulting dataframe, replacing the old labels. Given $DF = (A_{mn}, R_m, C_n, D_n)$ and some column label L, `TOLABELS(DF, L)` returns a dataframe $(A'_{m(n-1)}, L, C'_n, D'_n)$, where C'_n (respectively D'_n) is the result of removing the label L from C_n (respectively D_n). With this capability, data from A_{mn} can be promoted into the metadata of the dataframe and referenced by name during future interactions.

FromLabels. `FROMLABELS` creates a new dataframe with the row labels inserted into the array A_{mn} as a new column of data at position 0 with a provided column label. The data type of the new column starts as $null$ until it can be induced by the schema induction function S. The row labels of the resulting dataframe are set to the default label: the order rank of each row (positional notation). Formally, given a dataframe $DF = (A_{mn}, R_m, C_n, D_n)$ and a new column label L we define `FROMLABELS(DF, L)` to be a dataframe $(R_m + A_{mn}, P_m, [L] + C_n, [null] + D_n)$, where $R_m + A_{mn}$ is the concatenation of the row labels R_m with the array of data A_{mn}, P_m is the positional notation values for all of the rows: $P_m = (0, ..., m-1)$, and $[L] + C_n$ is the result of prepending the new column label L to the column labels C_n.

GroupBy. As in relational algebra, our `GROUPBY` operator groups by one or more columns, and aggregates one or more columns together or separately. Unlike relational algebra, where aggregation must result in atomic values, dataframes can support composite values within a cell, allowing a broader class of aggregation functions to be applied. One special function, `collect`, groups rows with the same grouping attribute values into separate dataframes and returns these as the (composite) aggregate values. Pandas's `groupby` function has similar behavior and applies `collect` to the non-grouped attributes. We will use `collect` in our examples subsequently.

Window. `WINDOW`-type operations are largely analogous to those used in recent SQL extensions to RDBMSs like PostgreSQL and SQL Server. The key difference is that, in SQL, many windowing functions such as `LAG` and `LEAD` require an additional `ORDER BY` to

Figure 4: Pivot table example, reproduced from [27], demonstrating pivoting over two separate columns, "Month" and "Year".
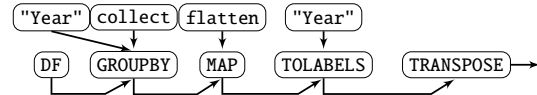
Figure 5: Logical plan for pivoting a dataframe around the "Year" column using the dataframe algebra from this section.

be well-defined; in dataframe algebra, the inherent ordering already present in dataframes makes such a clause purely optional.

4.4 Pivot Case Study

To demonstrate the expressiveness of the algebra above, we show how it can express `pivot`, which is particularly challenging in relational databases due to the need for relations to be declared schema-first [27, 67]. The `pivot` operator (Figure 4) elevates a column of data into the column labels and creates a new dataframe reshaped around these new labels.

Since there is no need to know the names of the new columns or the resulting schema *a priori*, a pivot can be expressed concisely in dataframe algebra as a combination of four operators in the plan shown in Figure 5. Recall that it is possible to elevate data to the column labels by using `TOLABELS` followed by `TRANSPOSE`. In this case, the `TOLABELS` operator would be applied on the label of the column being pivoted over, `"Year"` in this example. After this step, we perform a `GROUPBY` on the pivoted attribute, `"Year"` with a `collect` aggregation applied to the remaining attributes to produce a per-`Year` dataframe as a composite aggregated value. This aggregated value is manipulated by a `MAP` operator with a function that flattens the grouped data into the correct orientation. This results in a table pivoted around the attribute selected for the `TOLABELS` operator. Notice in Figure 4 that transposing the dataframe labeled "Wide Table in Months" results in the correct data layout for the "Wide Table in Years". This is one example of how `TRANSPOSE` can

be exploited: cost models in dataframe query optimizers can choose the more efficient pivot column and `TRANSPOSE` at the end.

5. DATA MODEL CHALLENGES

Supporting the dataframe data model and algebra from Section 4 efficiently motivates a new set of research challenges. We organize these challenges based on unique properties of dataframes, and discuss their impact on query optimization, data layout, and metadata management. We first discuss the impact of flexible schemas.

5.1 Flexible Schemas, Dynamic Typing

Major challenges arise from the flexible nature of dataframe schemas. Dataframes require more than data; as noted in Section 4.2 they also require a schema to interpret the data. In the absence of explicit types for certain columns, we must run the type induction function S, and the resulting parsing functions—both of which can be expensive. Note that the type of a column must be known before we can parse the value of any cell in that column. Mitigating the costs inherent in flexible schemas and dynamic types therefore presents a major challenge for dataframes.

In database terms, dataframes are more like views than tables. Programming languages like Python and R do not store data; they access data from external storage like files or databases. Hence every time a program is executed, it constructs dataframe objects anew. Unfortunately, external storage in data science is often untyped. Dataframe-friendly file formats like Apache Feather include explicit schemas and pre-parsed data, but most data files used in data science today (notably those in the ever-popular csv format) do not.

Another source of dynamism arises from schema mutations, e.g., adding or removing columns. These are first-class citizens of the dataframe algebra, unlike in relational databases, which relegate such operations to a separate DDL. As such, they are not only allowed, but are in fact frequent during data exploration with dataframes, especially during data preparation and feature engineering. We consider the challenge of efficient schema induction from three angles: rewriting, materialization, and query processing.

5.1.1 Rewrite Rules for Schema Induction

Due to their flexible schemas, dataframes support the addition and removal of columns as first-class operations, and at any point in time could have several columns with unknown type. Certain dataframe operators need type information, however—e.g. avoid attempting to `JOIN` two dataframes on columns with mismatched types or using a numeric predicate on a column with some strings. The schema induction function, S, could be used to induce the requisite typing information, but it is expensive and must be explicitly considered when modeling cost for query plans. Specifically, if certain columns are not operated on, inferring their type via S can be deferred to when they are first manipulated and omitted entirely if, for example, they are dropped before ever being accessed.

In some cases, schema inference rules might be able to avoid the application of S altogether. For example, if ordered relational operations are chained together, schema induction can be omitted between operations, suggesting the possibility of employing rewrite rules to skip applying S. Another example involves UDFs with known output types (e.g., a `MAP` with a UDF that returns an integer).

In the case of operations which merely shuffle rows around (e.g. moving even-indexed rows to the beginning of a dataframe, reordering), schema induction can be omitted entirely. When filtering or taking a sample of a dataframe, schema induction can be omitted if the type is already fairly constrained and will not be additionally constrained based on the sample. For example, if we drop all rows

with strings in a specific column, we may end up with that column having a restricted type such as float or int, requiring special care.

While omitting or deferring schema inference is promising, additional complications arise from the fact that, in a dataframe system, metadata *is* data (see also Section 5.2) that may itself be queried by a user. In particular, it is common for users to perform *runtime type inspections* as a sanity check. As a result, the extra effort for eschewing or deferring schema induction may prove futile if the user chooses to inspect types anyway.

5.1.2 Reusing Type Information

It is common to reuse a dataframe across multiple statements in a program. In cases where the dataframe lacks explicit types, it can be very helpful to materialize the results of both schema induction and parsing—both within the invocation of a program (internal state), and across invocations in storage.

Materialization of flexibly-typed schemas introduces a new set of challenges. Both schema induction and parsing can be a significant fraction of the cost of processing. This raises optimization choices for materialization: we can cache the results of S (for one or more columns), and additionally we can cache the results of parsing functions (in principle, at a granularity down to the cell level). For complex multistep dataframe expressions, we can choose to make these decisions at each operator in the pipeline that introduces a dynamically-typed column. Hence the optimization search space is large. Moreover, the workload of "queries" is different from traditional materialized view settings—languages like Python are more difficult to analyze statically than SQL, and we can expect usage patterns to differ from databases as well (Section 6).

In some cases, it is reasonable to expect that a data scientist will want to declare the types of the dataframe explicitly—e.g., an expression like `df_t = TRANSPOSE(df, [myschema])` where `myschema` is an array of type names for the columns. In this case, there is no need to run schema induction. In a loosely-typed language like Python, `myschema` can be an arbitrary expression returning an array of strings. For example, it might read a list of type names from a very large file with the same number of rows as `TRANSPOSE(df)`. Alternatively, the dataframe `df` itself might have "row types" stored as strings in the i'th column of the data, leading to an expression like `df_t = TRANSPOSE(df, df[i])`.

View maintenance has a role in the dataframe context, with new challenges for type induction. The most direct use is in delta-computation of expressions that have the effect of "adding" rows to their inputs. For example, consider a `MAP` operator with a data validation function: for each column it returns the input if it passes a validation test, else it returns an error message in that column. The new rows may all respect the constraints of the types of the input dataframe, or some new rows could break those constraints—e.g. a string-typed error message appearing in a column of numbers. In both cases, we'd like the type induction to take advantage of the work done to induce a schema for the input, and differentially decide on a schema for the output. Note that these issues get more subtle as the type system gets richer—e.g., consider an input with a column of type *percent* that is passed into an arithmetic `MAP` function—the output may be statically guaranteed to be numeric, and for a given dataframe may or may not still be of type *percent*.

5.1.3 Pipelining Schema Induction in Query Plans

When applying S and the parsing function to columns is unavoidable, we may be able to reduce its cost by trying to fuse it with other operations that are type-agnostic and lightweight (e.g., data movement or serialization/deserialization) while adding minimal overhead, which we foresee to be a fruitful research direction.

For other operations, the position of S within the query plan can have major performance implications. Consider a `MAP` operation that is being applied to a column of strings. If the `MAP` operation is relatively inexpensive (e.g., if it measures string length), it may make sense to to skip type checking via schema induction before the `MAP` operation. Although a type error (due to, e.g., the presence of an unexpected integer value) leads to wasted effort, it may be acceptable if the overhead paid by actual application of the `MAP` is not too high. On the other hand, a `MAP` which performs heavy-duty regular expression parsing over long strings may delay error detection unacceptably if schema induction is fused into the `MAP`.

Overall, the positioning of the schema induction operator within the query plan, by possibly fusing it with existing operators, combined with schema induction avoidance and reuse, is crucial for the development of a full-fledged dataframe query optimizer.

5.2   Order and Equivalence

Unlike relations, dataframes are ordered along both rows and columns—and users rely on this ordering for debugging and validation as they compose dataframe queries incrementally. This order is maintained as rows are transformed into columns and columns into rows via `TRANSPOSE`, ensuring near-equivalence of rows and columns. Additionally, as we saw in Section 4.4, row and column label metadata is tightly coupled with the dataframe content, and inherits the order and typing properties. In this section, we discuss the challenges imposed by enforcing order and the frequently changing schema across row and column labels and row/column orientation.

5.2.1   Order is Central

The order of a dataframe is determined by the order of ingested data. For example, a CSV file ingested as a dataframe would have the same row and column order as the file. This ordering is crucial for the trial-and-error-based interaction between a user and a dataframe system. Users expect to see the rows in their dataframe stay in the same order as they process it—allowing them to validate and debug each step by comparing its result to the previous step. For example, to ensure that a CSV file is ingested and parsed correctly, users will expect the first few rows of the dataframe to be the same as those they would see when examining the CSV file. To examine a dataframe, users will either use the operator `head/tail` to see the prefix/suffix or simply type the name of the dataframe for both the prefix and suffix in the expected order. Additionally, operators such as `WINDOW` and `MAP` from Section 4.3 expect a specific order for the rows (`WINDOW`) and columns (`MAP`). Perhaps most challenging is the frequency at which the order can be changed, as each operator has a deterministic output order (shown in Table 1). since the UDF argument to these operators may rely on that order. Dataframes also support `SELECTION` and `PROJECTION` based on the position of the rows and columns respectively.

Current dataframe systems such as pandas physically store the dataframe in the order defined by the user and do not implement physical data independence. Physical independence may open up new optimization opportunities, recognizing that as long as the displayed results preserve the desired order semantics to the users, it is not necessary that all intermediate products or artifacts (unobserved by user) adhere to the order constraint. For example, a sort operation can be "conceptual" in that a new order can be defined without actually performing the expensive sorting operation. Likewise, a transpose doesn't require the data to be reoriented in physical storage unless beneficial for subsequent operations; the transpose can be captured logically to reflect the new orientation of the dataframe.

To ensure correct semantics while respecting physical data independence, we must devise a means to capture ordering information,

either tracked as a separate "order column" if it is not implied via existing columns, or recording as metadata that the dataframe must be ordered based on one or more of the preexisting columns. Then, the `ORDER BY` on this "order column" or one of the existing columns will be treated as an operator in the query plan, and will only need to be done "on-demand" when the user requests to view a result. Additionally, since users are only ever looking at the first and/or last few lines of the dataframe, those are the only lines that are required to be ordered; we discuss this further in Section 6.1.

Extending physical data independence even further, we can adapt other data representation techniques from the database community, optimized for dataframes. This includes columnar or row-column hybrid storage [14], as well as those from scientific computing [26], array databases [57], or spreadsheets [22]. Since dataframes are neither relations, matrices, arrays, or spreadsheets, none of these representations are a perfect fit.

The order of the dataframe also creates some interesting new challenges in query planning. Operators that are commutative in the relational data model are not necessarily commutative in dataframes, e.g., `SELECTION` based on a positional predicate. Due to this, a dataframe query optimizer must now be aware of and manipulate an internal representation of the order. The added complexity of maintaining order in the query plan due to the presence of non-commutative operators in dataframes will be a significant challenge for dataframe systems wishing to preserve these semantics.

5.2.2   Row/Column Equivalence

The presence of a `TRANSPOSE` operator in the dataframe algebra presents novel challenges in data layout and query optimization. `TRANSPOSE` allows users to flexibly alter their data into a desired shape or schema that can be parsed according to an appropriate schema, and queried using ordered relational operators.

To keep our data model and algebra compact, we have schemas only for columns and our operators are defined on ordered sets of rows. By contrast, in pandas and other dataframe implementations, it is possible to perform many operations along either the rows or columns via the `axis` argument. Hence, programs written in (or translated to) our algebra are likely to have more uses of `TRANSPOSE` than dataframe programs in the wild, to represent columnwise operations and/or to reason about per-row schemas. These operations are expressible logically in our simpler algebra by first performing a `TRANSPOSE`, applying the operation, and then a `TRANSPOSE` again to return to the original orientation. Doing frequent physical reorganizations for these operations would be a mistake, however.

The prevalence of `TRANSPOSE` in dataframe programs overturns many axis-specific assumptions made in traditional database storage. Axis-specific data layouts like columnar compression are problematic in this context. Metadata management also requires rethinking, since dataframes are as likely to be extremely "wide" (column-wise) as they are "tall" (rowwise). Both traditional and embedded RDBMSs typically limit the number of columns in a relation (e.g., SQL Server has an upper limit of 1024 columns, or 30k columns using the wide-table feature) [37,53]. By applying `TRANSPOSE` on a tall and narrow dataframe, the number of columns can easily exceed the millions in the resulting short and wide dataframe.

Dataframe systems will need careful consideration to ensure that a `TRANSPOSE` call does not break assumptions made by the data layout layer used to perform optimizations. To ensure these optimizations are harmonious with respect to `TRANSPOSE`, we can do a *logical* `TRANSPOSE` "pull-up". The proposed rewrite delays transpose in the physical plan as much as possible, since it will often destroy many data layout optimizations that would otherwise apply.
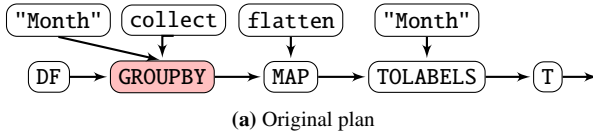
(a) Original plan
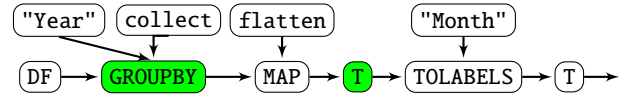
(b) Optimized rewrite that leverages sorted `Year` column

Figure 6: Alternative query plans for pivoting a dataframe around the "Month" column using the algebra from Section 4.3. TRANSPOSE is abbreviated as T.

In certain cases, we may indeed want to consider optimizing the *physical* layout of the data given a `TRANSPOSE` operator as a part of a query plan. This is in contrast with existing data systems that create and optimize for a static data layout. A physical transpose may help the optimizer match the layout to the access pattern (e.g., matrix multiplication). A fixed data layout is likely to have a significant performance penalty when the access pattern changes. Additionally, consider a case where `TRANSPOSE` allows us more flexibility in query planning. In the `pivot` case in Section 4.4, we observed that transposing the result of a pivot is effectively a pivot across the other column. Specifically, if we must pivot into the wide table with `Month`s as columns, we can either use the original plan (Figure 6a) or one where we proceed as if the pivot is over `Year`, but then transpose the final result so that the `Month` attribute values are used as column headers (Figure 6b). The latter plan will be faster if the optimizer leverages knowledge about the sorted order of the `Year` column to avoid hashing the groups. This is an interesting example of a new class of potential optimizations within dataframe query plans that exploit an efficient `TRANSPOSE`. Because the axis transpositions are happening in query expressions, the data layout becomes a physical plan property akin to "interesting orders" [58] or "hash teams" [33], expanding the rules for query optimization.

5.2.3 Metadata is Data (and Data is Metadata)

A standard feature of dataframes is the ability to fluidly move values from data to metadata and back. This is made explicit in the `TOLABELS` and `FROMLABELS` operators of our algebra, especially in combination with `TRANSPOSE`. These semantics cannot be represented in languages like SQL or relational algebra that are grounded in first-order logic; this is a signature of second-order logic, as explored in languages like OQL [18], SchemaSQL [44] and XQuery [23]. There is significant prior work on optimizing second-order operations like the unnesting of nested data (e.g. [30, 60, 65]). A distinguishing aspect of our setting is that a dataframe operation like `TOLABELS` commonly generates a volume of schema-level metadata that is dependent on the size of the data; this raises new challenges. The closest prior work to our needs studies spreadsheet-style pivot/unpivot in databases (e.g. [27, 67]); this work needs to be generalized to the richer semantics of a dataframe algebra.

To address representational aspects, we could treat row labels the way we treat primary keys in a relational database—by noting the sequence of label columns in a metadata catalog. Some additional details arise in the support of positional notation: invoking `TOLABELS(`c_1`, ..., `c_n`)` removes the relevant columns from their positions, requiring a recalculation of the positions of all labels to the right of c_1. This can be handled by representing column order in dynamic ranked data structures like ranked B-trees [43] or range min-max trees [47]. In terms of data access, we may want to efficiently process data columns without paying to access (dynamically reassigned) metadata columns, and vice versa. In this case, columnar layouts become attractive for projection. Alternatively, labels can be moved into separate *property tables* [27], a form of "vertical partitioning" that does not rely on columnar storage layouts.

Challenges arise in more complex expressions that include both `TOLABELS` and other operators–notably `MAP` and `TRANSPOSE`. In these cases, the number and types of *columns* in the dataframe is data-dependent. This exacerbates the metadata storage issues discussed in the previous section, and brings up additional challenges.

In terms of query optimization, we now have a two-dimensional estimation problem: both cardinality estimation (# of rows) and *arity estimation* (# of columns). For most operations in our algebra this would appear straightforward: even for `TRANSPOSE`, we know the cardinality and arity of output based on input. The challenge that arises is easy to see in a standard data science "macro", namely 1-hot encoding (`get_dummies` in pandas). This operation takes a single column as input, and produces a result table whose schema concatenates the input schema with an (typically large) array of boolean-typed columns, one column per distinct data value of the input. Pivot presents a similar challenge: the width of the output schema is based on the number of distinct data values in the input columns. In our algebra, these macros can be implemented using `GROUPBY` followed by `MAP` and `TRANSPOSE`. The resulting arity estimation problem reduces to distinct value estimation for the input to `GROUPBY`. While techniques like hyperloglog sketches [31] could assist here, note that we need to compute these estimates not only on base tables that may be pre-sketched, but on intermediate results of expressions! In short, we need to do distinct value estimation for the *outputs* of query operators—including arithmetic calculations (e.g. sums, products) and string manipulations (e.g. expanding a document into constituent words).

In some scenarios, arity *estimation* is insufficient—we need exact numbers and labels of columns. Consider the example of performing a `UNION` of feature vectors generated from two different text corpora, say Wikipedia articles unioned with DBLP articles. Each text corpus begins as a dataframe with schema (`documentID, content`). After a standard series of text featurization steps (word extraction with stemming and stop-word filtering followed by 1-hot encoding), each corpus becomes a dataframe with a `documentID` column, and one boolean column for each word in the corpus. The problem is that the `UNION` needs to dynamically check for compatibility of the input schemas—it needs to first generate the full (large!) schema for each input, and compare the two. Even if we relax our semantics to an "outer" union, we want to identify and align the common words across the corpora. These metadata requirements seem to require two passes of the inner expression's data: one to compute and align metadata, and another to produce a result. There are opportunities for optimization here to return to single-pass pipelining techniques, but they merit investigation. This pipeline-breaking problem generalizes to any operator that reasons about its input schema(s), so it needs to be handled comprehensively.

In short, we expect that the fluid movement of large volumes of data into metadata and vice versa introduces new challenges for query processing and optimization in dataframes.

6. USER MODEL CHALLENGES

Unlike in SQL where queries are submitted *all-or-nothing*, dataframe users construct queries in an incremental, iterative, and interactive fashion. Queries are submitted as a series of *statements* (as we saw in Figure 1) a few operators at a time in trial-and-error-based *sessions*. Users rely on immediate feedback to debug and rapidly iterate on these statements and frequently revisit results of intermediate statements for experimentation and composition during exploration. This interactive session-based programming model

for dataframes creates novel challenges for overall system performance and imposes additional constraints on query optimization. For example, operator reordering is often not beneficial when the results are materialized for viewing after every statement. At the same time, dataframe query development sessions are bursty, with ample think time between issuance of statements, and tolerant of incomplete results as feedback—as long as the original goals of experimentation and debugging are met, offering new opportunities for query optimization. In this section, we discuss new challenges and opportunities in query optimization arising from the interactive and incremental trial-and-error query construction of a typical user.

6.1 Interactive Feedback and Control

Dataframes are typically used in exploratory workloads, where interactive response times are crucial to providing a fluid user experience. Past studies have shown that latency in response times of greater than 500ms can lead to fewer hypotheses explored and insights generated during data exploration [45]. As another example, for data preparation—often performed on dataframes—users often rely on system feedback to guide and decide what operations to determine their next steps [35]. This feedback usually comes in the form of a display output by the dataframe system that contains a prefix or suffix of rows and columns, as in Figure 1. The need for frequent materialization of intermediate results to provide feedback to the user makes it particularly difficult to satisfy the 500ms query latency requirement for interactivity. Fortunately, we can leverage two user behavior characteristics to improve interactivity: that users spend time thinking between steps, and that the inspected intermediate results are typically restricted to a prefix/suffix of rows/columns which is sufficient for debugging and validation.

6.1.1 Intermediate Result Inspection & Think Time

Present-day dataframe systems such as pandas are targeted toward ensuring users can inspect intermediate results for debugging and validation, so they operate in an *eager* mode where every statement is evaluated as soon as it is issued. Program control is not returned to the user until the statement has been completely evaluated, forcing the user to be idle during that time. However, there are many cases where users do not inspect the intermediate results, or where results are discarded; in such cases, the user is still forced to wait for each statement to be evaluated. Moreover, users are either rewarded or punished based on the efficiency of a query as it is written.

On the other hand, with the *lazy* mode of evaluation, which is adopted by some dataframe-like systems [19, 28] (See Section 7), control is returned to the user immediately, and the system defers the computation until the user requests the result. By scheduling computation later, the system can wait for larger query sub-expressions to be assembled, leading to greater opportunities for optimization. The downside of lazy evaluation is that computation only begins when the user requests the result of a query. This introduces new burdens for users, particularly for debugging, since bugs are not revealed until computation is triggered.

For example, consider two commutative operations `op1`, and `op2`. Say the user submits the statement `x = df.op1()` followed by `y = x.op2()`. In eager evaluation, `x` will be fully materialized before execution begins on `y`, even if `x` is never used again. Computing `y` could be done using `df.op2().op1()`, but it is often more beneficial to use the materialized version of `x` instead. In lazy evaluation, execution will be deferred until explicitly requested, so the expression that creates `y` could be optimized to run `df.op2().op1()`. The drawback of this approach is that the user must explicitly request `y` in order to realize that there is a potential bug in `x`.

Furthermore, neither the lazy nor the eager mode take advantage of the fact that the users spend time thinking between steps, during which the system is idle. We can can leverage this time for computation, allowing us to effectively achieve the benefits of both paradigms. While interactive latency is important to support immediate feedback, recent empirical studies have also shown that optimizations can be relaxed to account for users' long think time between operations in exploratory analysis [20]. We describe a novel *opportunistic* query evaluation paradigm suitable for optimizing dataframes in an interactive setting.

Like lazy evaluation, opportunistic evaluation does not require the user to wait after each statement. Instead, the system opportunistically starts execution, while passing control back to users with a pointer to the eventually computed dataframe (a "future"), which is asynchronously computed in the background. We can then use system resources to compute results in the background as users are composing the next step. Like eager evaluation, opportunistic evaluation does not wait for users to complete the entire query to begin evaluation. However, when a user requests to view a certain output, opportunistic evaluation can prioritize producing that output over all else. Opportunistic evaluation allows queries to be rewritten as new statements are submitted (e.g., `df.op2().op1()`) to get to the requested answer as fast as possible, taking into account what is partially computed. There are also new opportunities within opportunistic evaluation to do speculation, where during idle time the system can start executing statements that commonly follow previous ones. Opportunistic evaluation also leads to new challenges in sharing and reuse across many query fragments whose computation has been scheduled in the background (see also Section 6.2).

6.1.2 Prefix and Suffix Inspection

The most common form of feedback provided by dataframe systems is the tabular view of the dataframe, as shown in Figure 1. The tabular view serves as a form of visualization that not only allows users to inspect individual data values, but also convey the structural information associated with the dataframe. Structural information, especially as it relates to order, is important for validating the results of queries that manipulate and reshape the dataframe. This tabular visualization typically contains a partial view of the dataframe displaying the first and last few rows of the dataframe, accessed using `head`, `tail`, or other print commands.

One way to give the users immediate feedback is to return the output to the user as soon as these k rows are assembled, computing the rest of the output in the background using opportunistic evaluation. This is reminiscent of techniques that optimize for early results [63, 64] for `LIMIT` queries [42], or for representative tuple identification [61], but a key difference in dataframes is that order must be preserved (so "any-k" result tuples will not suffice [42]), and there are many more blocking operators. One starting point would be to design or select physical operator implementations that not just prioritize high output rate [63], but also preserve order, thereby ensuring that the first k rows will be produced as quickly as possible. As an example, if only the first k rows of an ordered join were to be computed, a nested loop join where the result displayed after k rows are computed might work well. We can progressively process more portions of the input dataframes until k output rows are produced in order: this may mean processing more than k rows of the inputs if there are very selective predicates. Figuring out the right way to exploit parallelism to prioritize processing the prefixes of the ordered input dataframes to produce the ordered prefix of the output is likely to be a substantial challenge.

Additionally, certain blocking operators will cause problems. While returning the first k rows following a `TRANSPOSE`, especially

when using columnar storage, can be fairly efficient, it may be hard to produce the first k tuples of a `GROUP BY` or `SORT` without examining the entire data first. `SORT` is an obvious example where the top k rows cannot be narrowed down a priori; a full scan is inevitable also for `GROUPBY` on non-clustered columns. That said, since the top and bottom k rows are often the only results inspected for dataframe queries, we may benefit from materializing additional intermediates or supporting indexes to retrieve them efficiently. We could, for example, materialize the prefix and suffix of a dataframe in original and transposed orientations, or the prefix or suffix of the dataframe sorted by various columns to allow for efficient processing subsequently. These materializations could happen during think-time as discussed in Section 6.1.1. We may also be able to exploit approximate query processing to produce the prefix/suffix early for blocking operators [16, 29, 36, 50, 69]. Since the tabular view is only a special form of visualization, a rich body of related work from visualization on how to allow users to quickly but approximately make decisions or perform debugging or validation may be applicable [17, 41, 46, 49]; however, the rich space of operators that goes beyond simple `GROUPBY` aggregation will lead to new challenges. Another interesting usability-oriented challenge is whether this tabular view of prefixes or suffixes is indeed best for debugging—perhaps highlighting possible erroneous values or outliers in dataframe rows or columns that are not in the prefix or suffix may also be valuable [54].

6.2 Incremental Query Construction

In addition to challenges around enabling immediate feedback, query optimization is further complicated by the need to frequently evaluate and display results for intermediate sub-expressions (i.e., the results of statements) over the course of a session (see also Section 6.1.1). While incrementally constructing dataframe queries over the course of an interactive session, users iterate on query sub-expressions through trial-and-error, frequently inspecting and revisiting intermediate results to try alternate exploration paths. Such fragmented workloads limit the optimizations that can be applied to each sub-expression. However, since user statements often build on others, we can jointly optimize across these statements and resulting sub-expressions, sharing work as much as is feasible. Further, since users commonly return to old statements to try out new exploration paths, we can leverage materialization to avoid redundant reexecution. We discuss these two ideas next.

6.2.1 Composable Subexpression Support

As a result of opportunistic evaluation, there are often many statements that are not completely executed when issued by the user, and are instead executed in the background asynchronously during user think time. Moreover, by prioritizing the return of a prefix or suffix of the results (Section 6.1.2), many statements are often not computed entirely, with the computation either deferred (in lazy or eager evaluation) or being scheduled in the background (in opportunistic evaluation). Thus, there are many statements that may be scheduled for execution at the same time. These statements may operate over similar or identical subsets of data. These overlapping queries that can be batch processed make dataframes particularly amenable to multi-query optimization (MQO), e.g., [32, 34, 55, 59]. However, new challenges emerge because of the new space of operators, as well as the prioritization of the return of prefixes/suffixes over the entire result when requested by the user.

One approach is to allow operations that share inputs to share scans. We can go even further if we recognize that many statements are essentially portions of a query composed incrementally (e.g., a `TRANSPOSE` followed by a `PROJECT` to simulate `SELECT`). There-

fore, we simply need to construct a query plan wherein sub-plans that correspond to intermediate dataframe results are materialized as by-products. These intermediates are also likely to be reused by the user in the future. This presents an interesting conundrum because ensuring that the sub-plan results are materialized "along the way" may result in suboptimal overall plan selection (e.g. if the user cares more about the final dataframe than intermediates). For example, the optimal way to compute a `SELECT` may not be to first compute a `TRANSPOSE` and then do a `PROJECT`, even though this may have the benefit of producing the appropriate intermediate results. Unlike MQO in relational databases, wherein it is important to share join subexpressions, here, an even more expensive operation is `TRANSPOSE`—necessitating sharing if at all possible. By using partial results to help users avoid debugging mistakes, we may be able to reduce the importance of constructing many of the intermediate results in entirety, unless explicitly requested. Moreover, by observing the user's likelihood of inspecting the intermediates over the course of many sessions, we can do a weighted joint optimization of all query subexpressions, where the weights for each intermediate dataframe correspond to its importance.

6.2.2 Debugging & Building Queries Incrementally

The incremental and exploratory nature of dataframe query construction over the course of a session leads to nonlinear code paths wherein the users revisit the same intermediate results repeatedly as a step towards constructing just the right queries they want. In such cases, intelligently materializing key intermediate results can save significant redundant computation and speed up query processing. The optimizer needs to handle the trade off between materialization overhead and the reduced execution time facilitated by availability of such intermediates to utilize storage in a way that maximizes saved compute—small intermediate dataframes that are time-consuming to compute and reused frequently should be prioritized over large intermediate dataframes that are fast to compute. Note, however, that materialization doesn't necessarily need to happen on-the-fly, and can be also performed in the background asynchronously during during user think time. Determining what to materialize requires us to predict which intermediates are likely to be used frequently. The prediction algorithm should take into consideration several factors, including user intent, past workflows, and operator lineage.

Depending on the underlying intent, users can interact with dataframes in very different ways. A user who is performing data cleaning is likely to issue point queries and focus on regions with missing or anomalous values; users exploring the data for building machine learning models tend to focus on manipulating columns with high mutual information with the target column, or more broadly on feature engineering. Taking advantage of user intent can lead to highly effective materialization and reuse strategies befitting specific access patterns, such as in machine learning workflows [68]. The interactive sessions in dataframe development make it possible for the system to infer and adapt to user intent.

User intent inference involves extensive offline analysis of workloads with known intents as well as online processing of relevant telemetry: recent Jupyter notebook corpora can provide a promising starting point [56]. One challenge is that unlike SQL workloads, dataframe queries tend to be interleaved with non-dataframe operators in the same session, which requires special considerations to identify the dataframe portion of the workload and to handle the interaction between the dataframe system and other frameworks.

In terms of costing operators for materialization and reuse, the dataframe setting introduces two novel challenges. Partial views to support fast inspection in conjunction with opportunistic evaluation can break up operators into multiple partial operators evaluated at

Table 2: Table of comparison between dataframe and dataframe-like implementations. Blue indicates dataframe systems, red indicates dataframe-like implementations. †: Spark can be treated as ordered for some operations. +: R dataframe operators can be invoked lazily or eagerly. *: Dask sorts by the row labels after TOLABELS.

Feature	Modin	Pandas	R	Spark	Dask
Ordered model	✓	✓	✓	✓†	
Eager execution	✓	✓	✓+		
Row/Col Equivalency	✓	✓	✓		
Lazy Schema	✓	✓	✓		✓
Relational Operators	✓	✓	✓	✓	✓
MAP	✓	✓	✓	✓	✓
WINDOW	✓	✓	✓	✓	✓
TRANSPOSE	✓	✓	✓		
TOLABELS	✓	✓	✓		✓*
FROMLABELS	✓	✓	✓		

different times, motivating the need for short and long term costs on partial views for each operator. The materialization and reuse decisions derived from these costs can feed back into the decisions on filtering for partial views or delaying evaluation. For example, if several queries based on a new sort order require immediate feedback in the near future, it might be prudent to incur a delay on the first query to materialize the new sort order in its entirety in order to significantly speed up subsequent queries on the new order through reuse. Of course, being able to make such decisions hinges on the ability to predict future reuse as discussed above. Secondly, the constantly growing dataflow graph requires eviction of old materialized results from memory. The interesting challenge in the dataframe context is that future reuse is determined by both what the user will do in the future and what the opportunistic evaluator will choose to compute, with the former being purely speculative and the latter being known within the system. We can reconcile the "two futures" by passing the model we build of the future workflow to the opportunistic scheduler for unified materialization/reuse planning.

7. ADDITIONAL RELATED WORK

While our focus on pandas is driven by its popularity, in this section, we discuss other existing dataframe and dataframe-like implementations. Table 2 outlines the features of these dataframe and dataframe-like implementations. We will discuss how existing dataframe implementations fit into our framework, thus showing how our proposed research is applicable to these systems.

Data model and algebra. To the best of our knowledge, an algebra for dataframes has never been defined previously. Recent work by Hutchinson et al. [38, 39] proposes an algebra called Lara that combines linear and relational algebra, exposing only three operators: JOIN, UNION, and Ext (also known as "flatmap"); however, dataframe metadata manipulation operators are not supported. Other differences stem from the flexible data model and lazily induced schema. We will draw on Lara as we continue to refine our algebra.

Dataframe Implementations: R. As we discussed in Section 4.1, the R language (and the S language before it), both support dataframes in a manner similar to pandas and can be credited for initially popularizing the use of dataframes for data analysis [40]. R is still quite popular, especially among the statistics community. An R dataframe is a list of variables, each represented as a column, with the same number of rows. While both the rows and columns in an R dataframe have names, row names have to be unique; thus the pandas dataframe is more permissive than the R one. As shown in Table 2, R supports all of the operations in our algebra. The R dataframe fully captures our definition of a dataframe, and thus, implementational support of R dataframes requires only conforming

the R API to our proposed algebra. External R packages such as readr, dplyr, and ggplot2 operate on R dataframes and provide functionalities such as data loading, transformation, and visualization, similar to ones from the pandas API [5, 66].

Dataframe-like Implementations. Some libraries provide a functional or object-oriented programming layer on top of relational algebra. These libraries include SparkSQL dataframes [2], SQL generator libraries like QueryDSL [3] and JOOQ [1], and object relational-mapping systems (ORMs) such as Ruby on Rails [4] and SQLAlchemy [21]. All of these systems share some of the benefits with respect to incremental query construction mentioned in Section 6. However, they generally do not support the richness and expressiveness of dataframes, including ordering of rows, symmetry between rows and columns, and operations such as transpose.

SparkSQL and Dask are scalable dataframe-like systems that take advantage of distributed computing to handle large datasets. However, as shown in Table 2, Spark and Dask do so at the cost of limiting the supported dataframe functionalities. For example, a dataframe in SparkSQL does not treat columns and rows equivalently and requires a predefined schema. As a consequence, SparkSQL does not support TRANSPOSE and is not well optimized for dataframes where columns substantially outnumber rows. Thus, SparkSQL is closer to a relation than a dataframe. Koalas [10], a wrapper on top of the SparkSQL API, attempts to be more dataframe-like in the API but suffers from the same limitations.

8. CONCLUSION

In recent years, the convenience of dataframes have made them the tool of choice for data scientists to perform a variety of tasks, from data loading, cleaning, and wrangling to statistical modeling and visualization. Yet existing dataframe systems like pandas have considerable difficulty in providing interactive responses on even moderately-large datasets of less than a gigabyte. This paper outlines our research agenda for making dataframes scalable, without changing the functionality or usability that has made them so popular. Many fundamental assumptions made by relational algebra are entirely discarded in favor of new ones for dataframes, including rigid schemas, an unordered data model, rows and columns being distinct, and a compact set of operators. Informed by our experience in developing MODIN, a drop-in replacement for pandas, we described a number of research challenges that stem from revisiting familiar data management problems, such as metadata management, layout and indexing, and query planning and optimization, under these new assumptions. As part of this work, we also proposed a candidate formalism for dataframes, including a data model as well as a compact set of operators, that allowed us to ground our research directions on a firm foundation. We hope our work serves as a roadmap and a call-to-action for others in the database community to contribute to this emergent, exciting, and challenging research area of scalable dataframe systems development.

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