

Cathode Modeling and Diode Performance in Planar Geometry using SCL Emission

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SCL emission and instabilities

- 1D planar SCL current density [1]:

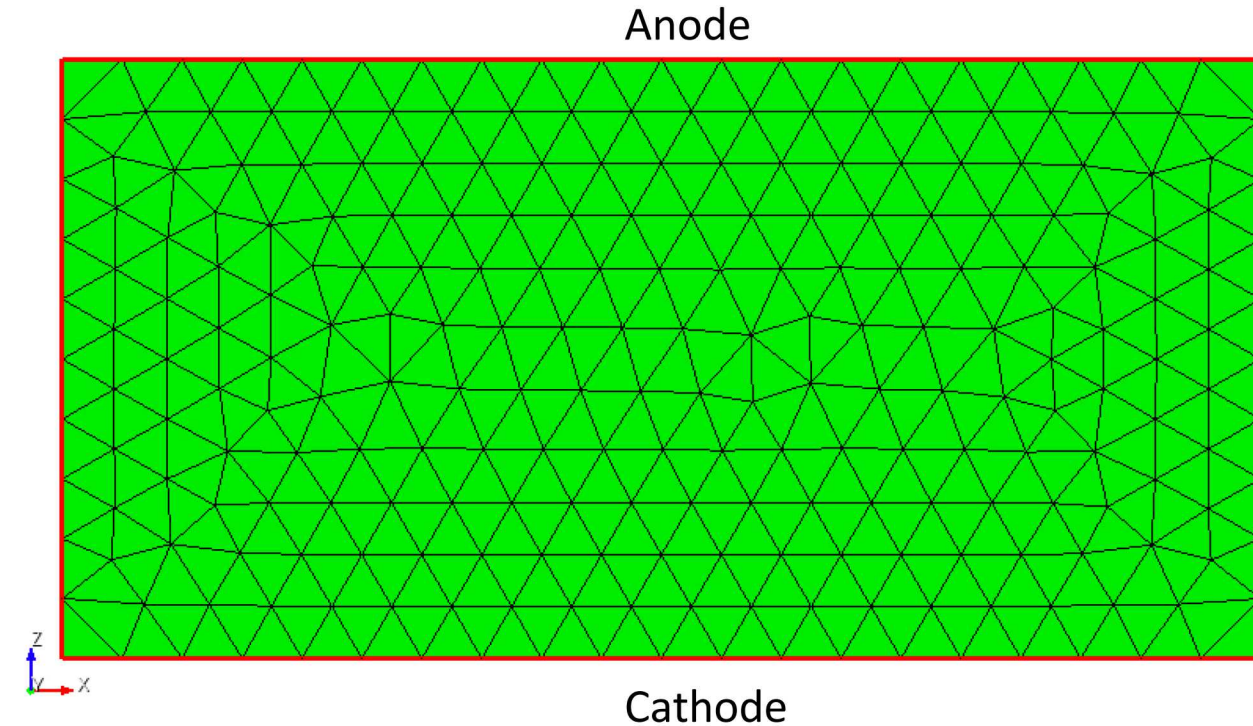
$$J_{SCL} = \frac{4\epsilon_0}{9} \sqrt{\frac{2e}{m}} \frac{V^{3/2}}{d^2}$$

- Patchy emission
 - Emission suppression of neighboring cells
- Transit time oscillations (TTOs) [2,3]

$$\frac{1}{t_{transit}} = \frac{2d}{nC}$$

- Virtual cathode oscillator formation (vircator) [4]

$$\omega_P = \sqrt{\frac{n_e e^2}{\gamma_0 m_e \epsilon_0}}$$



[1] - Child, C. D. "Discharge from hot CaO". *Physical Review*. Series I. 32(5): 492-511. May 1911

[2] - Luginsland, J. W., Arman, M. J., and Lau, Y. Y., "High-power transit-time oscillator: onset of oscillation and saturation" *Physics of Plasmas* 4, 4404. September 1997

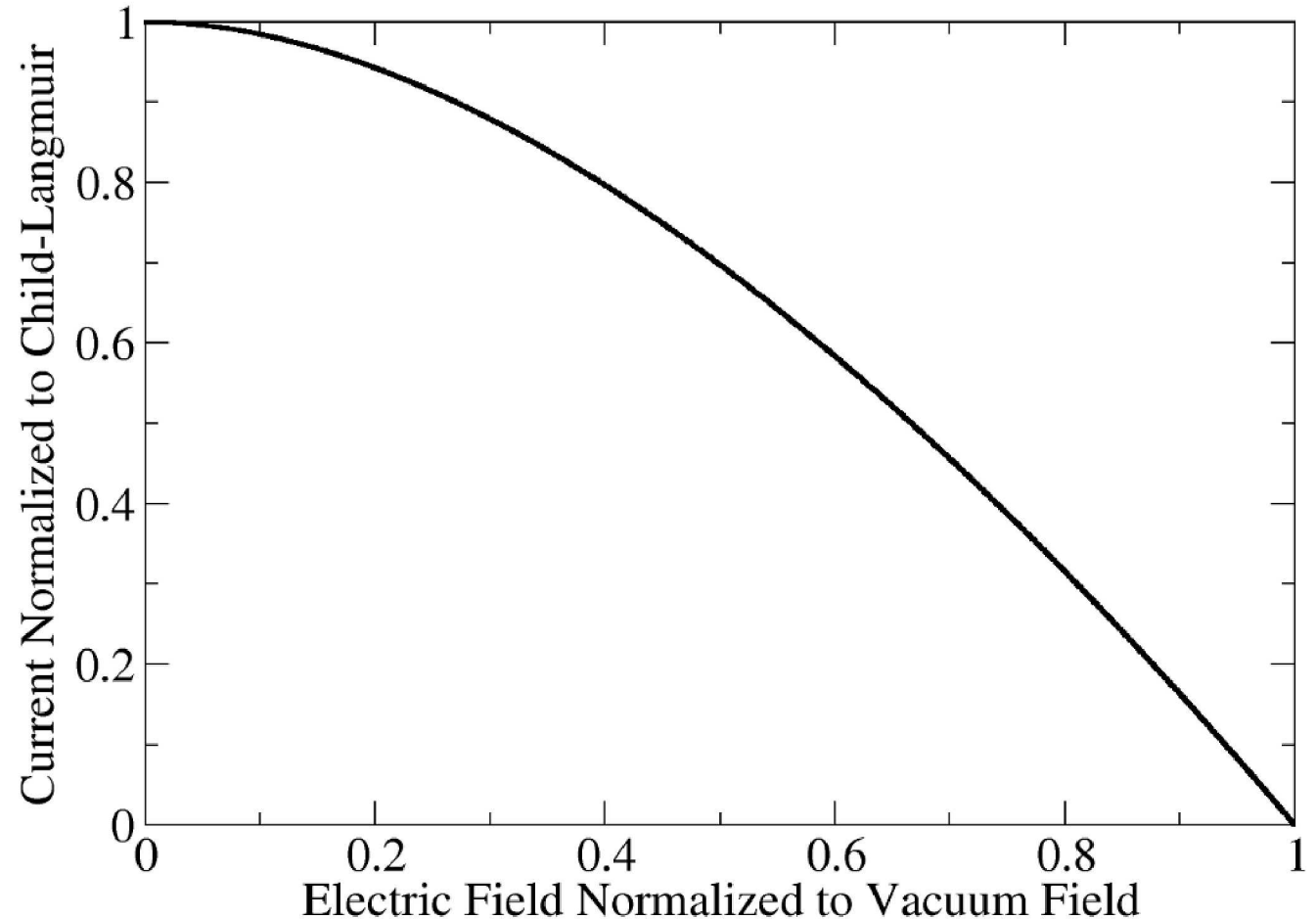
[3] - Pozar, D. M., "Microwave Engineering" *Wiley*, 1998

[4] - Benford, J., Swegle, J. A., Schamiloğlu, E., "High Power Microwaves" 3rd. Edition. *CRC Press*. 2016

SCL Emission and Instabilities

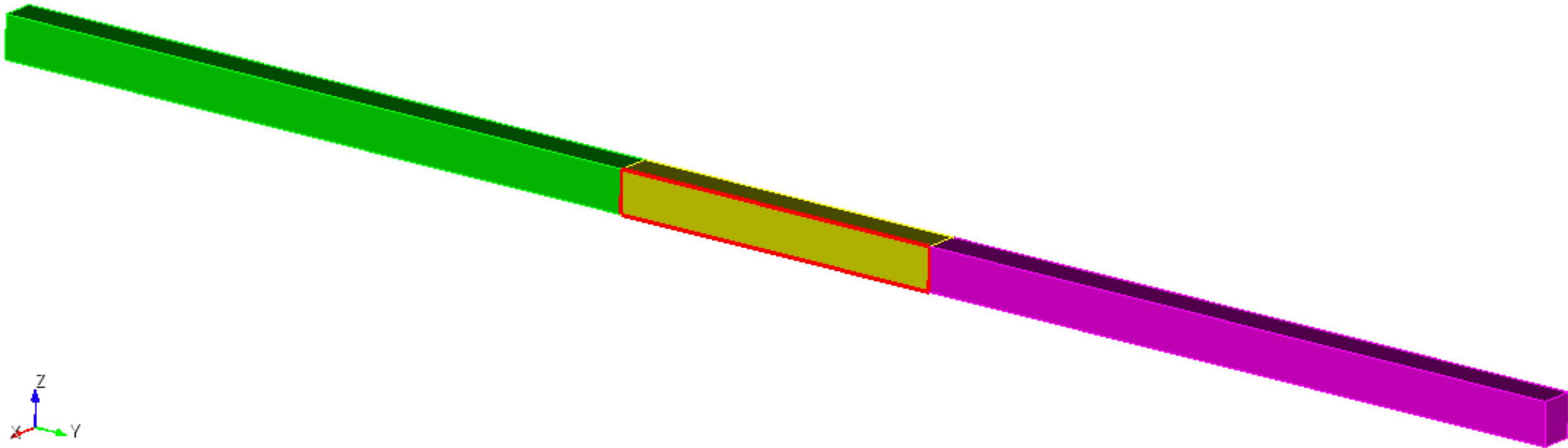
- Delay time
 - Delay cathode emission for specified time after breakdown threshold is surpassed
- Ramp time
 - Begin emission at specified initial fraction
 - Current density ramps below function over specified ramp time

$$J = \frac{1}{4}(2 + (2 - 3E_0)\sqrt{1 + 3E_0})$$



Modeling and Simulation Code

- EMPIRE – unstructured time domain electromagnetic particle-in-cell code (UTDEM PIC)
- CUBIT – code-based modelling and meshing

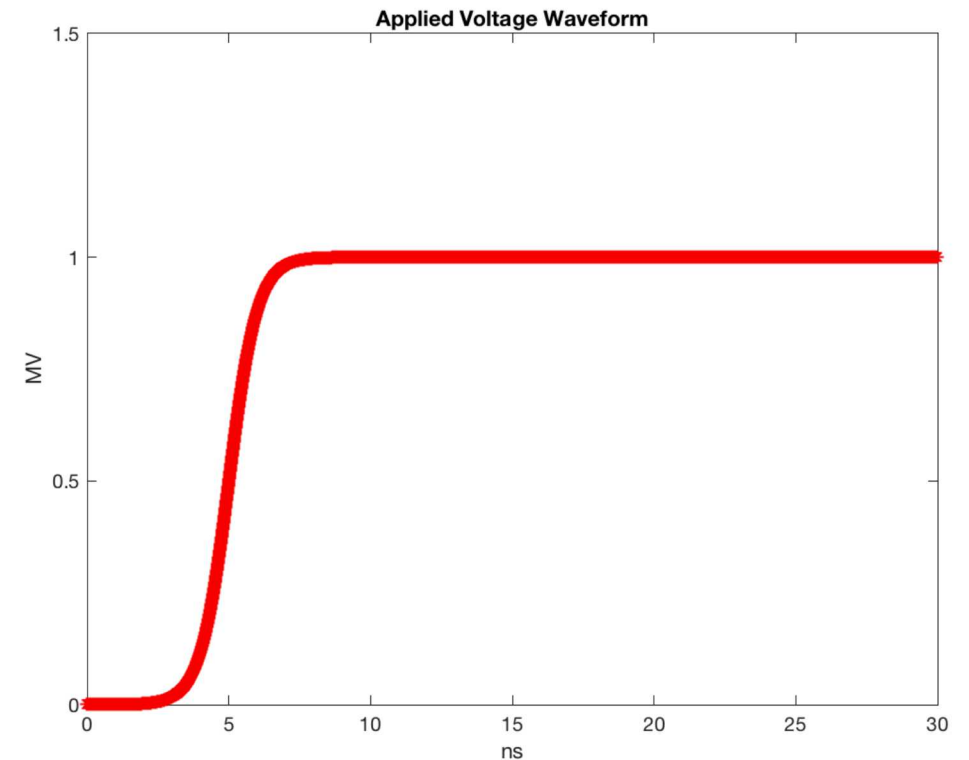
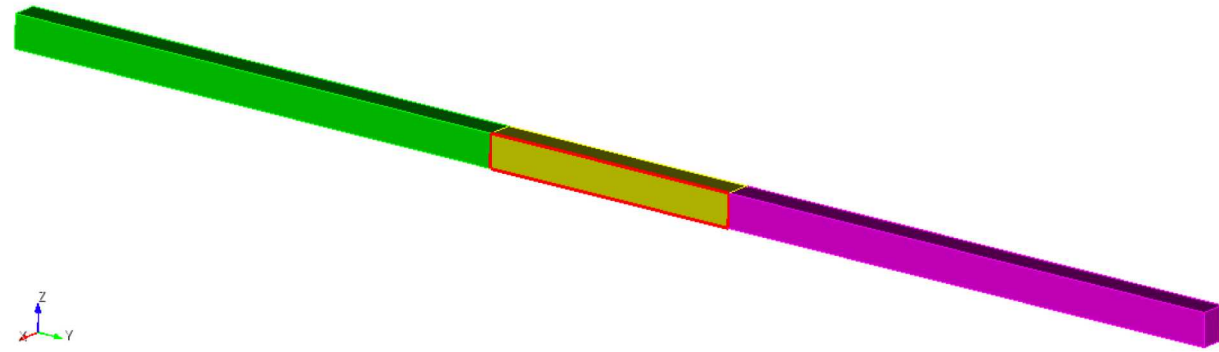


Modeling

- 1m transmission line BCs
- 1m model length
- 20cm diode region
- 2.5cm AK gap
- 2cm width
- Vacuum impedance[3]: 471Ω
- Steady state diode impedance[4]: 67Ω

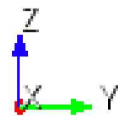
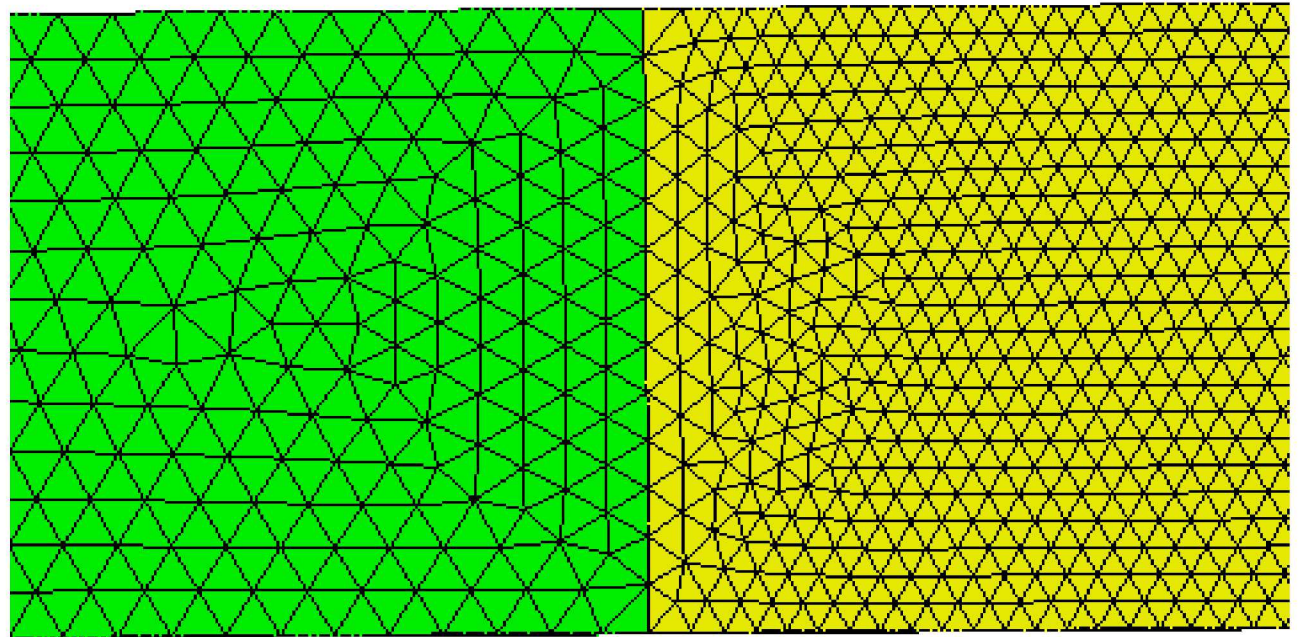
$$Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} \frac{d}{W}$$

$$Z_D = 429 \frac{d^2}{A} \frac{1}{\sqrt{V_0}}$$



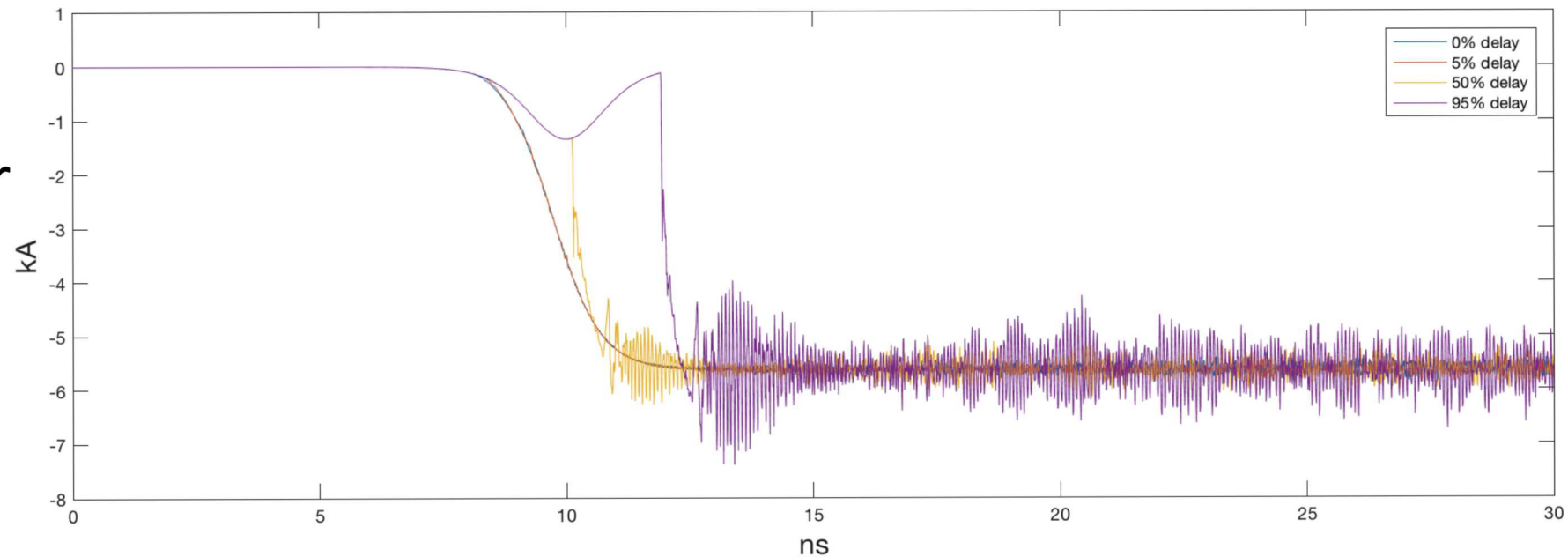
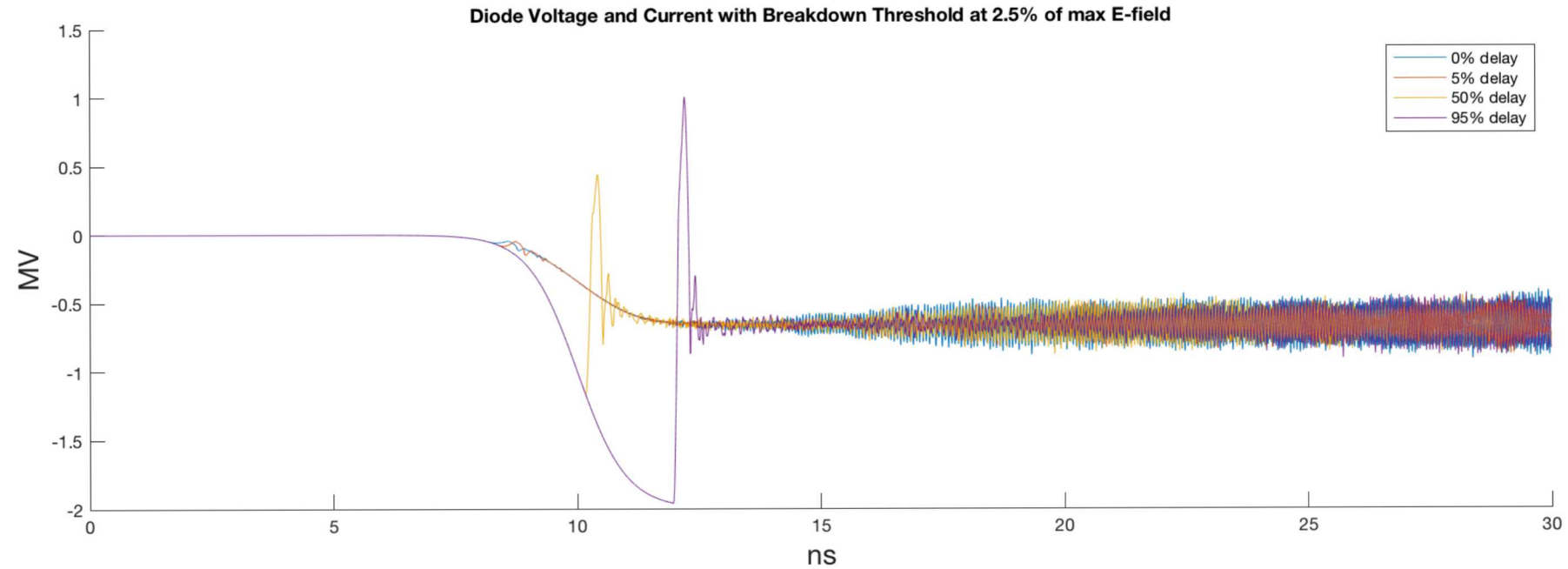
Modeling

- Vacuum wave mesh
 - $dx = d/10$
- Diode mesh
 - $Dx = d/20$
- Smooth transition between mesh sizes to minimize numerical impedance reflections



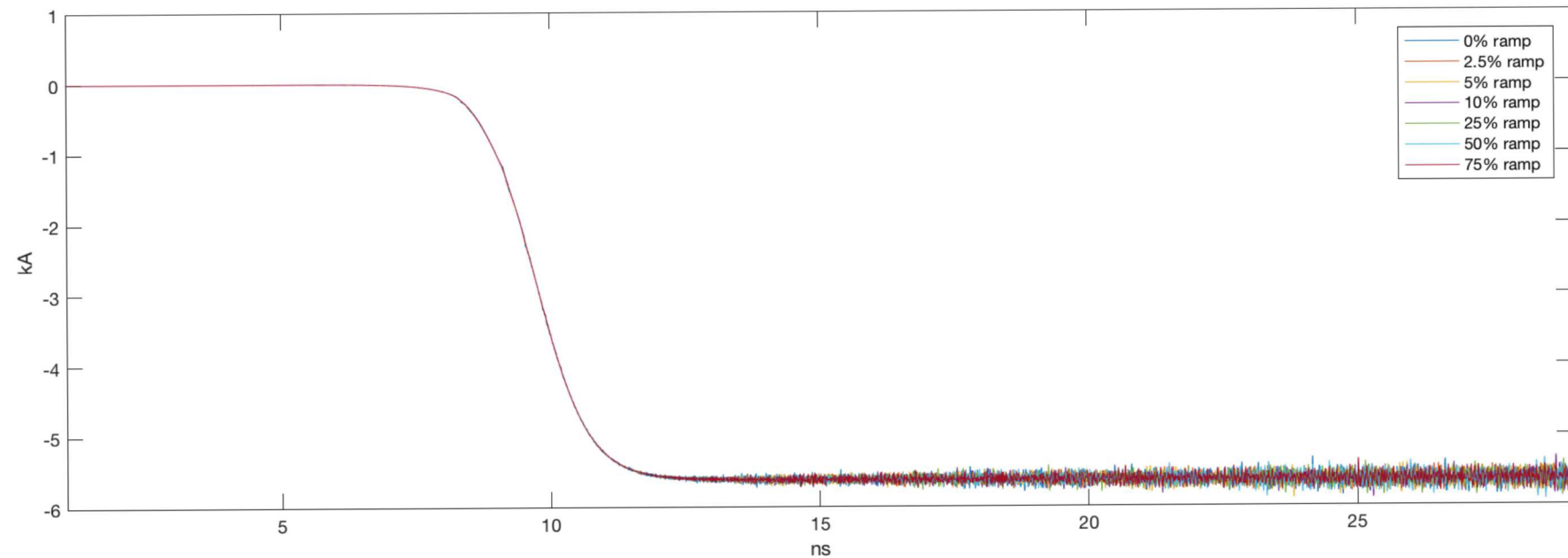
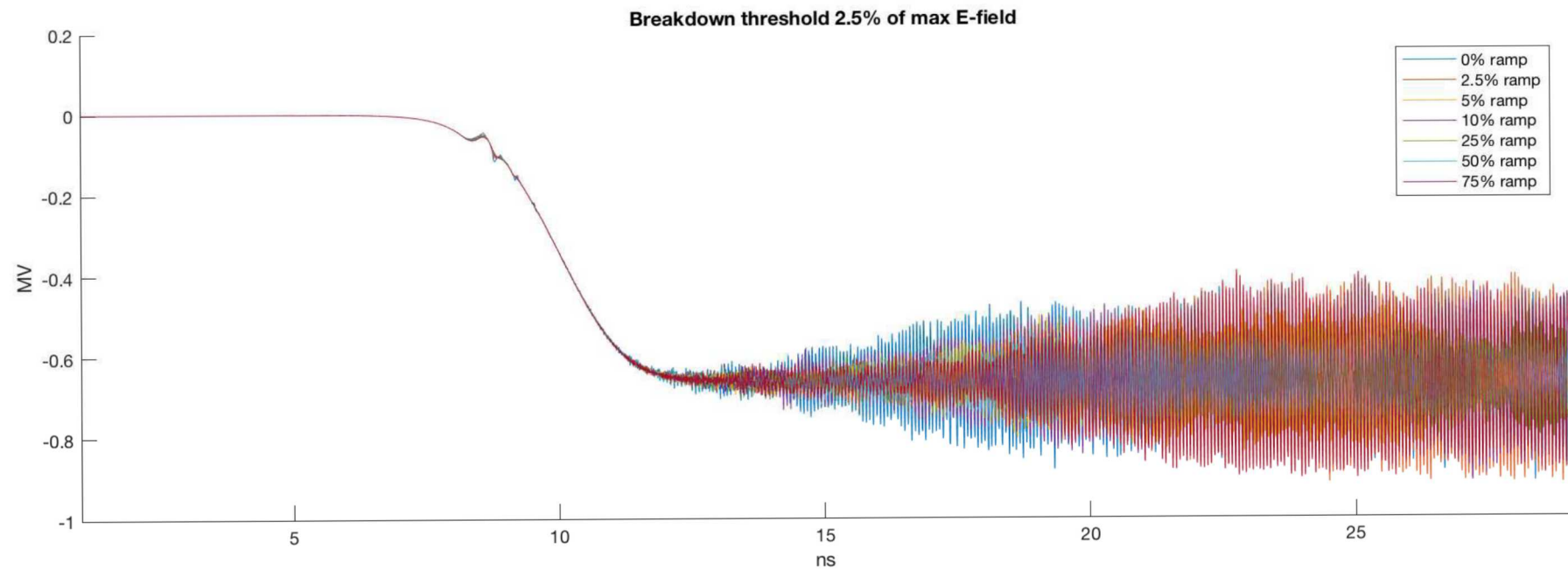
Delay Time

- Delay performs as expected
- Behaves similarly to simply increasing the breakdown threshold
- Primary benefit lies in tens of timesteps after breakdown
- $dt = 1ps$



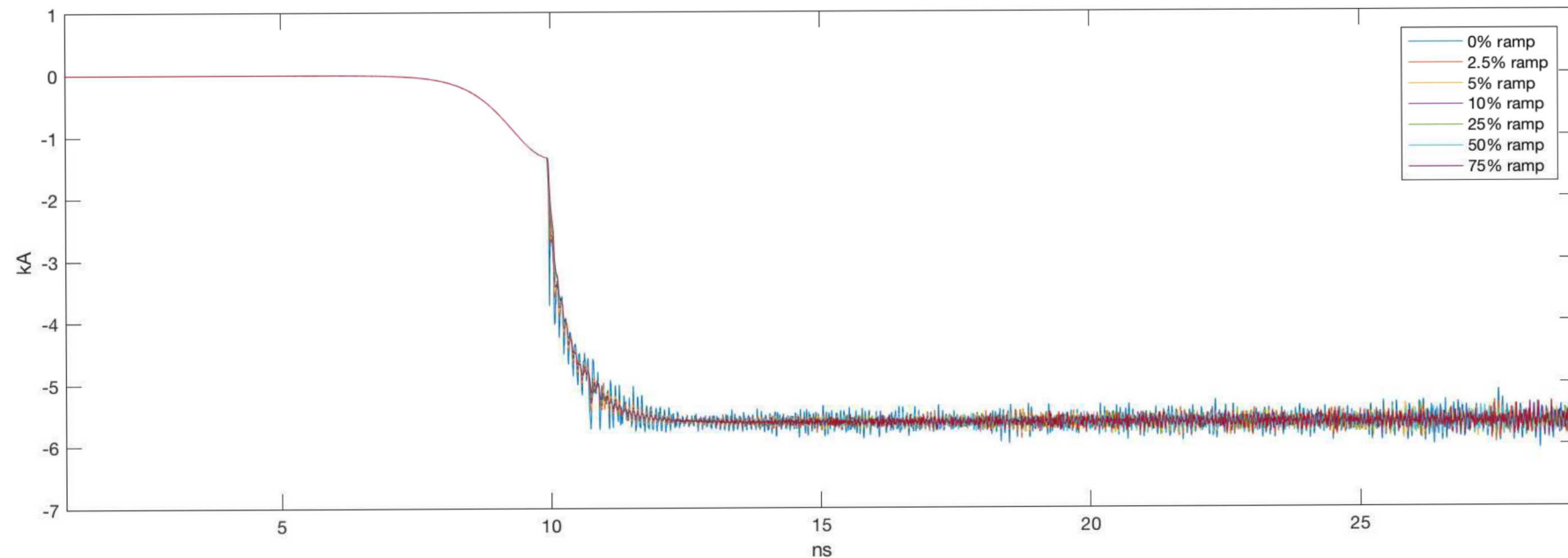
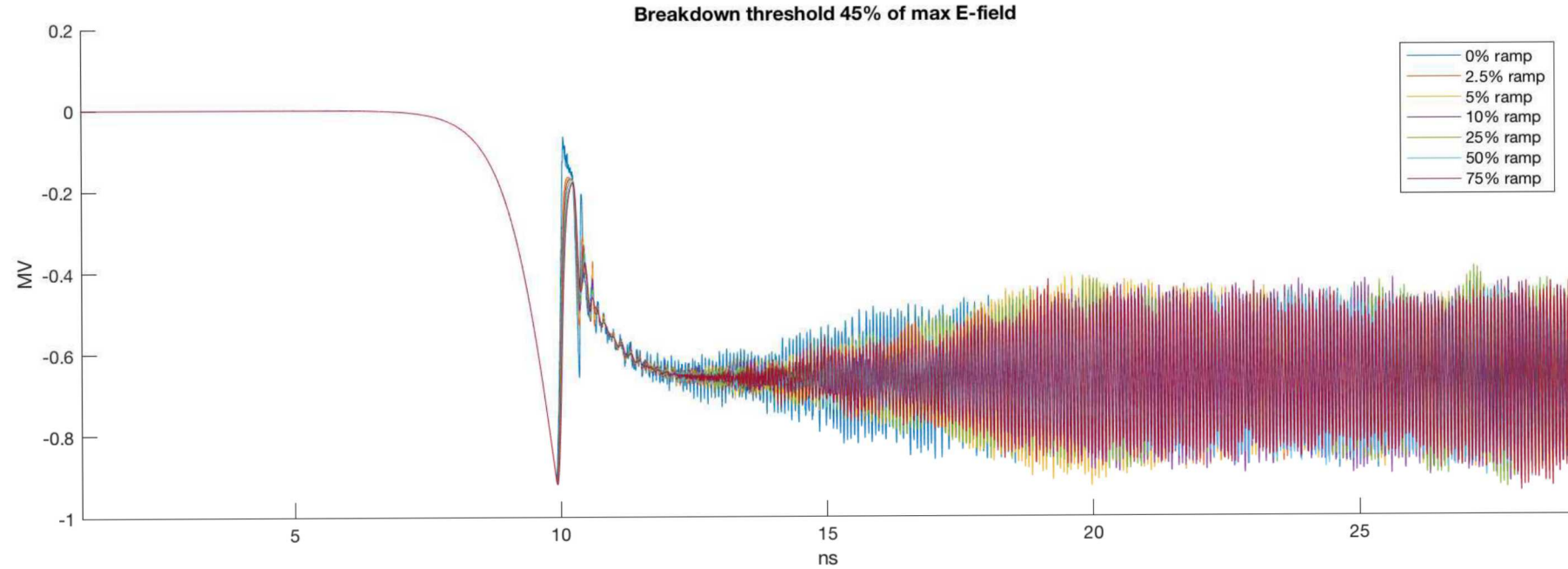
Ramp Time

- Early TTO excitation?
- Perform FFTs to see what this is



Ramp Time

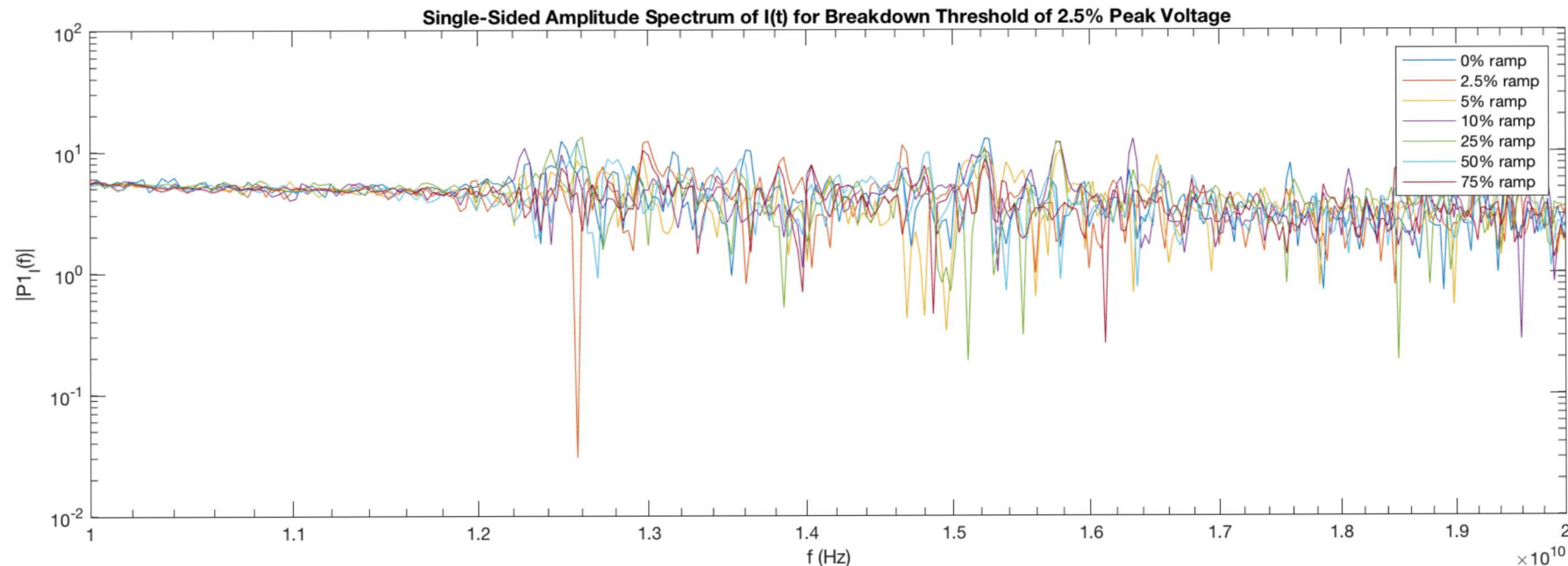
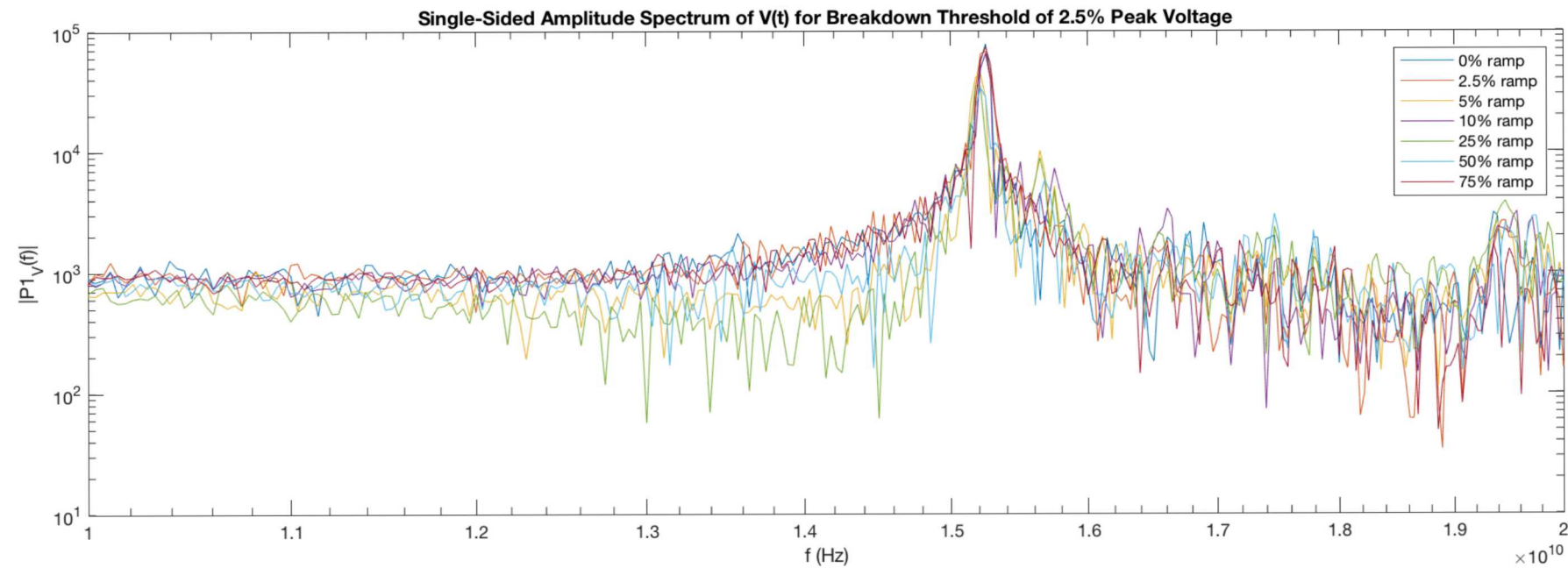
- Early TTO excitation?
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Ramp Time FFTs

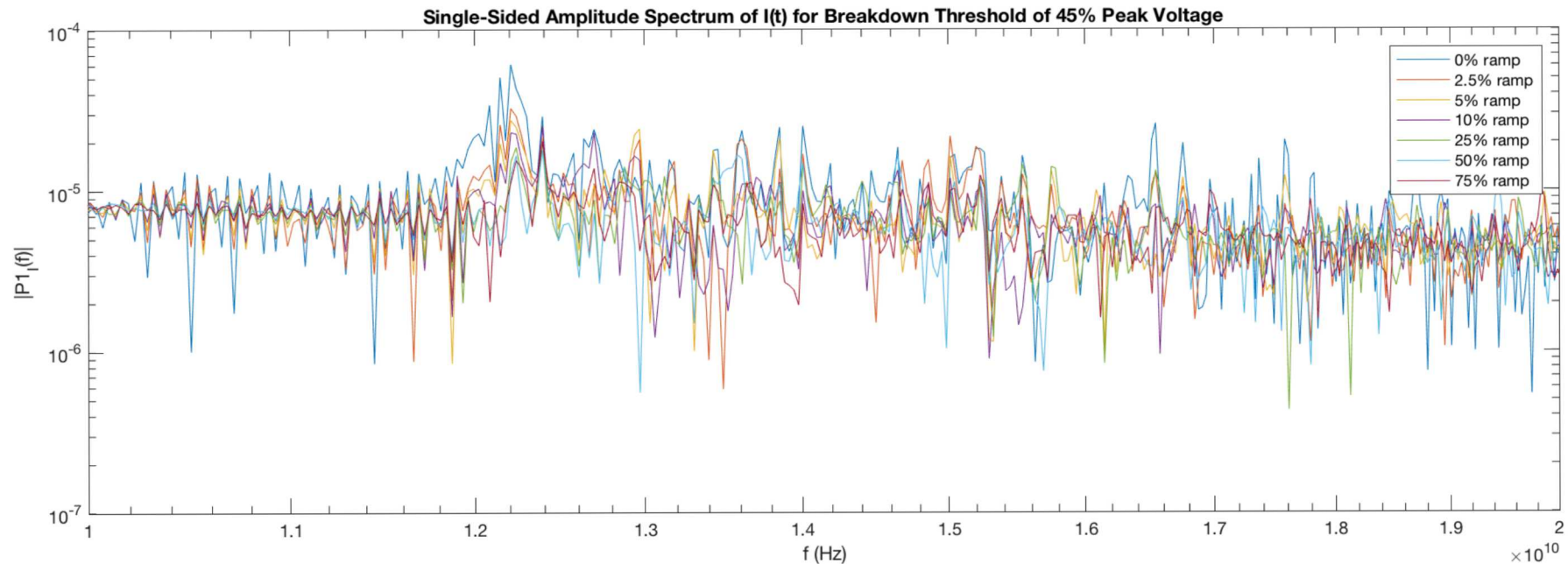
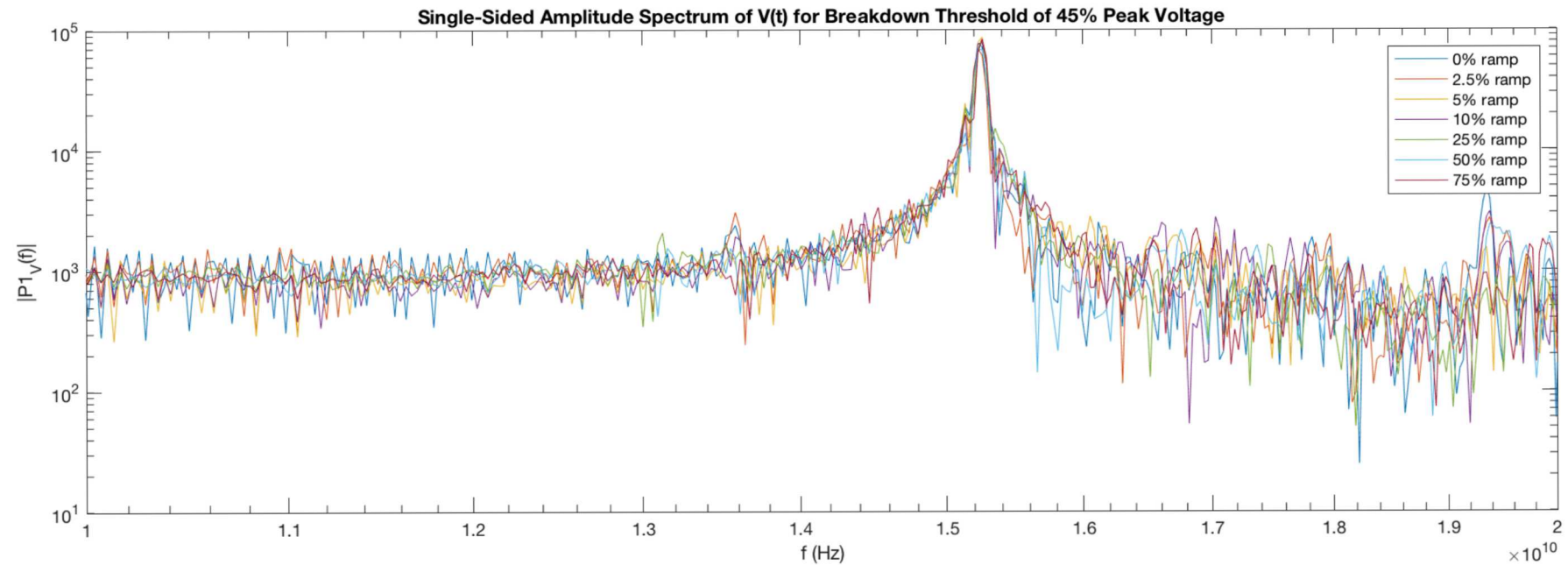
- Oscillations are primarily in voltage waveform
- 15GHz oscillation

$$\frac{1}{t_{transit}} = \frac{2d}{nC}$$



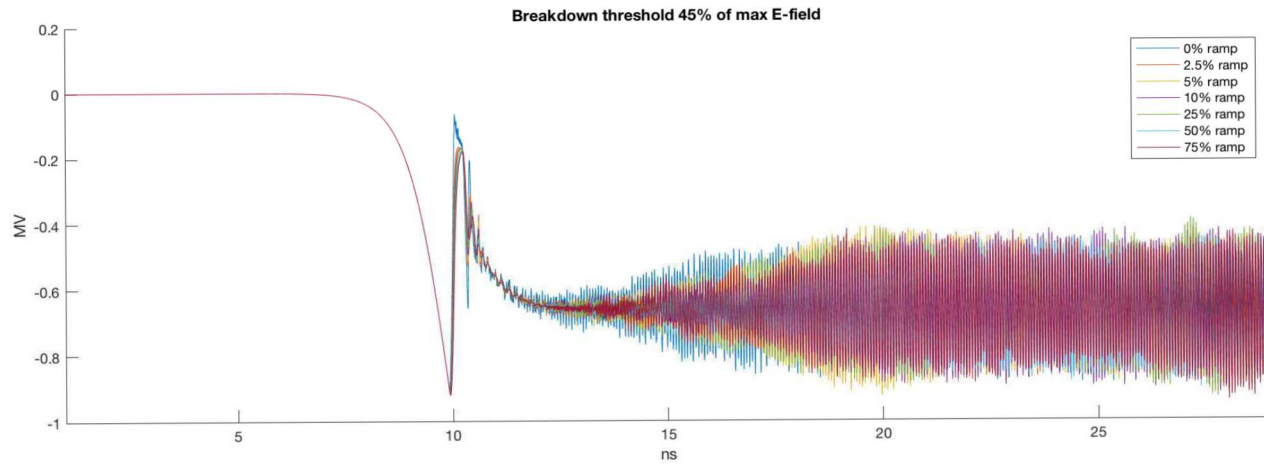
Ramp Time FFTs

- Oscillations are primarily in voltage waveform
- 15GHz oscillation
- Current has small 12GHz oscillation

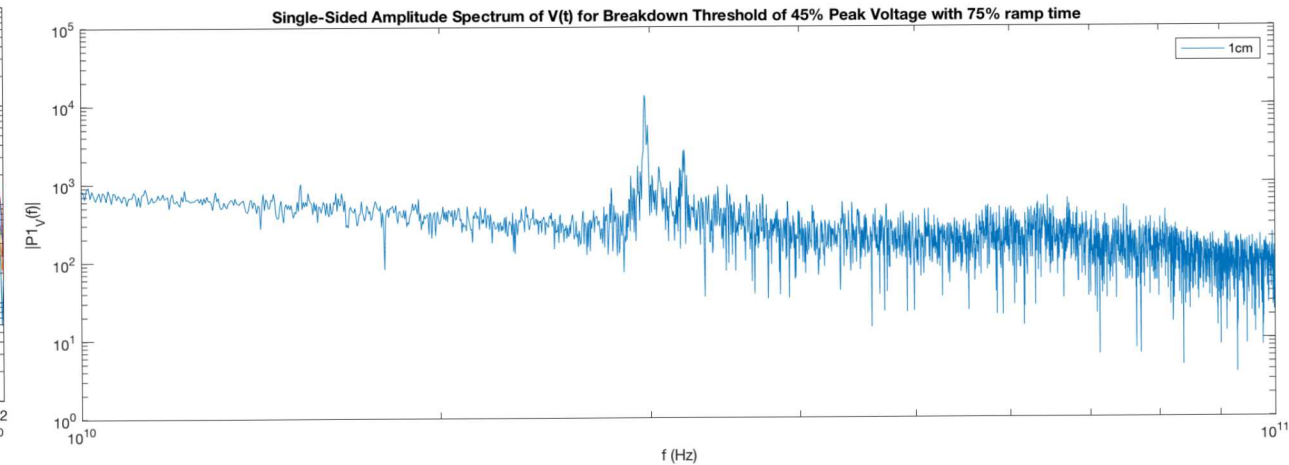
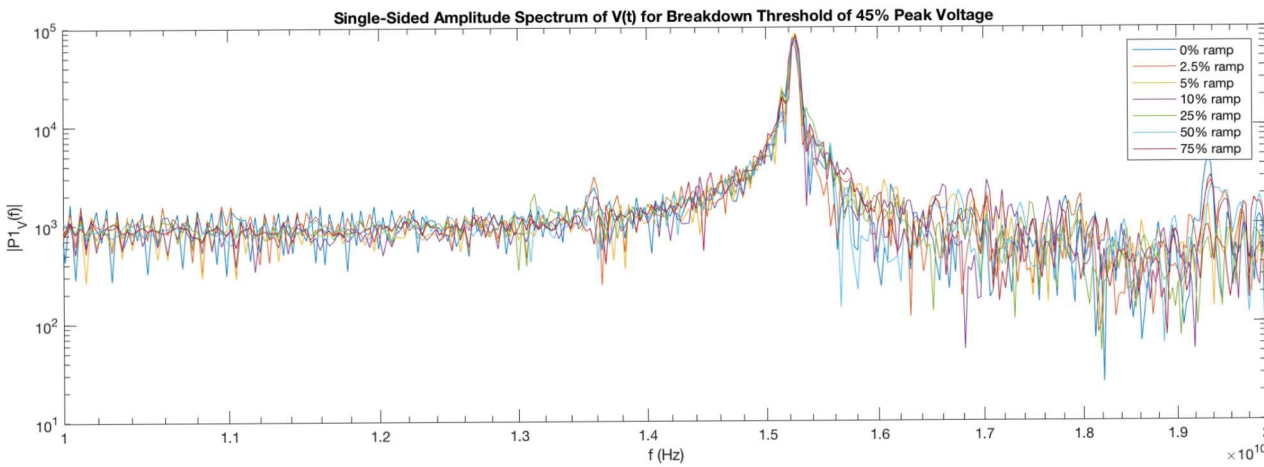
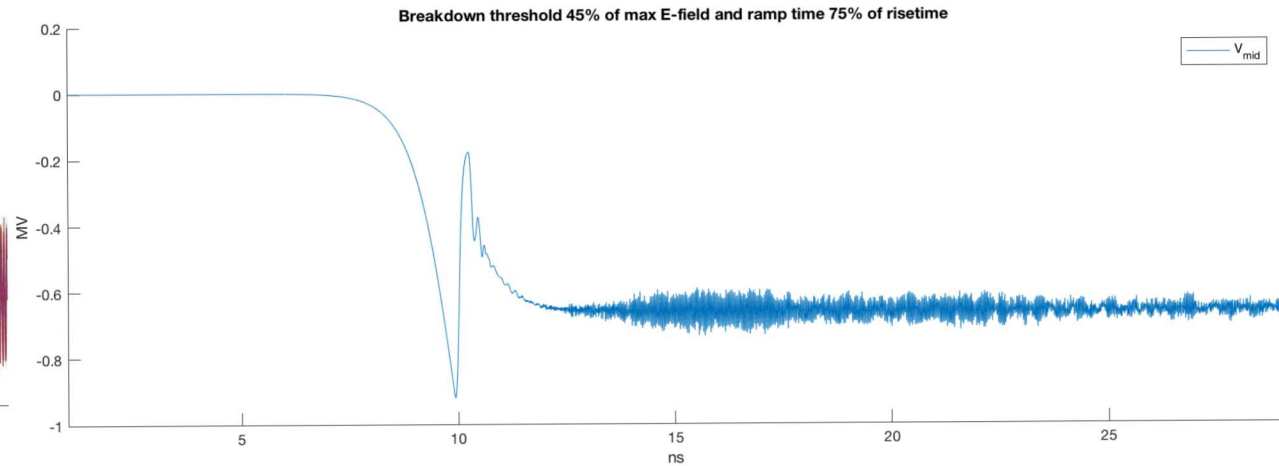


PMC ringing

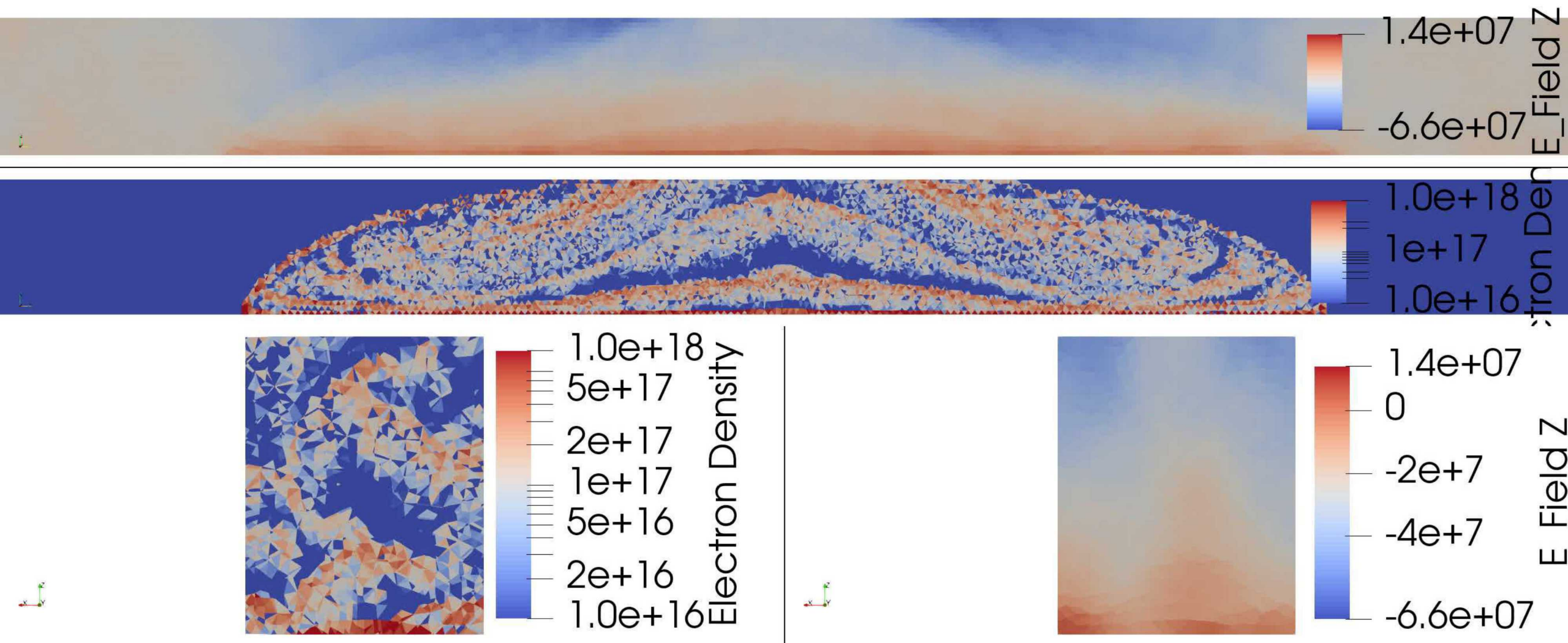
2cm width



1cm width

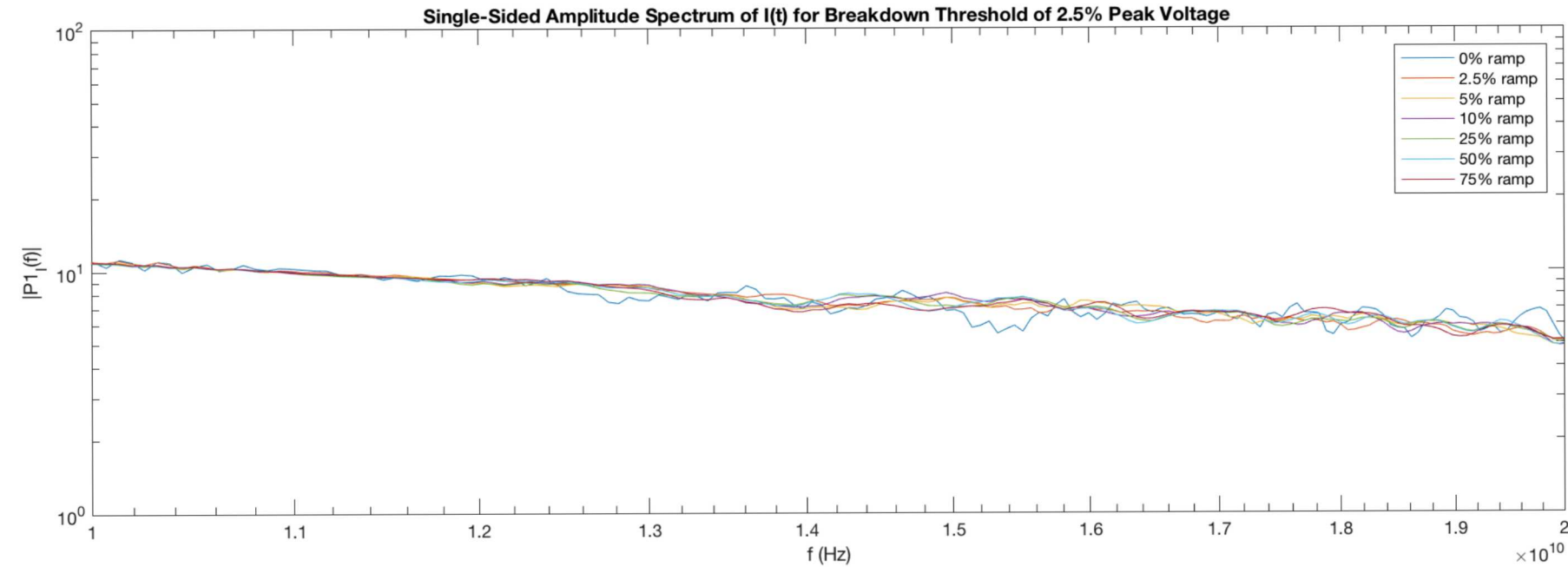
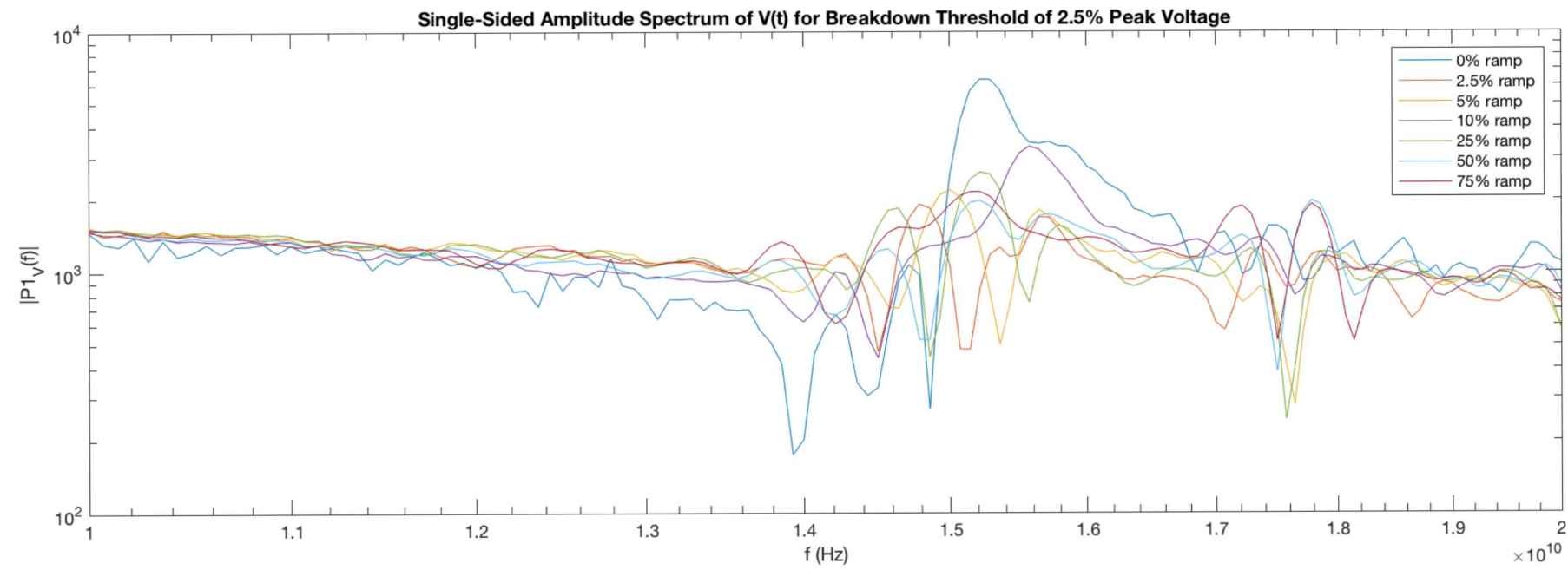


PMC ringing



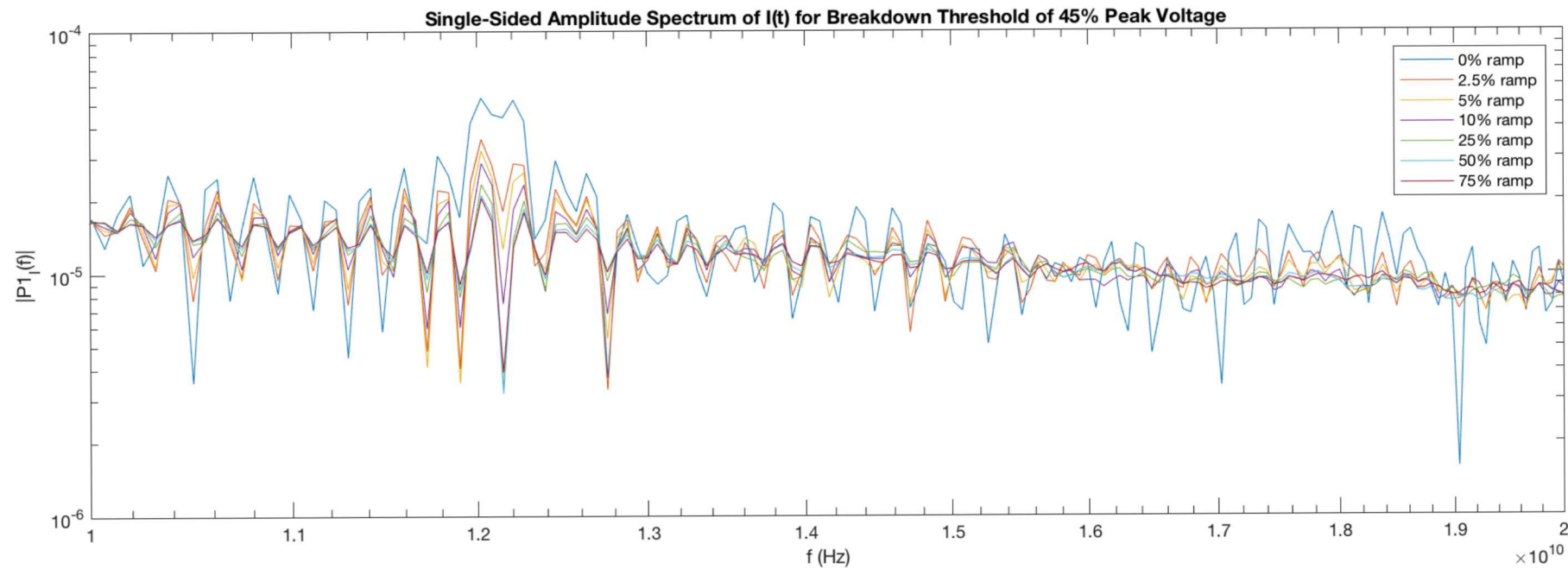
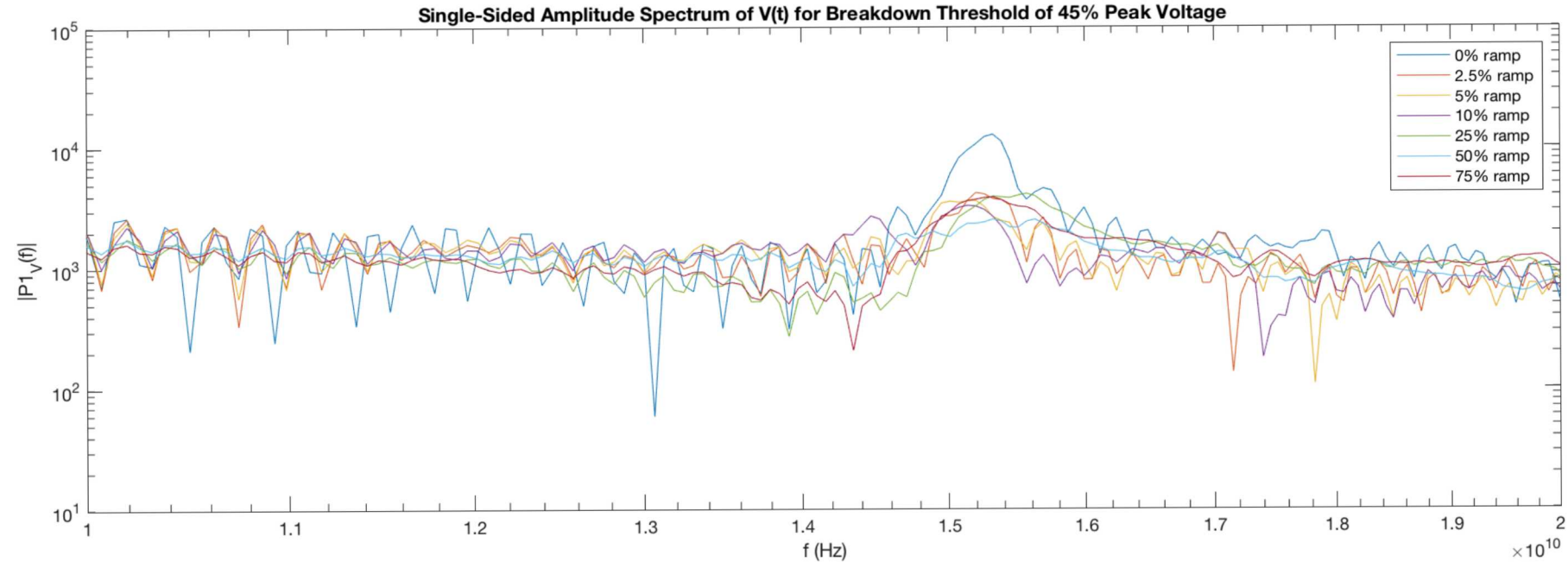
PMC Ringing and TTO Growth

- Cut off FFTs at 15ns



PMC Ringing and TTO Growth

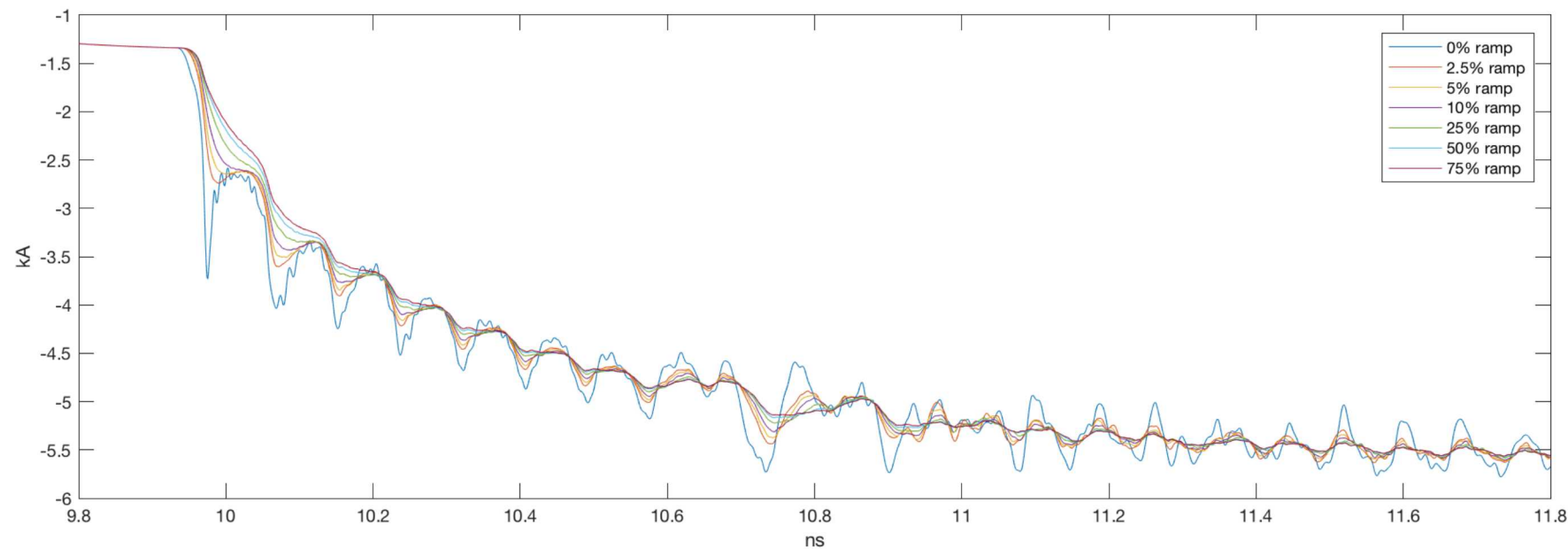
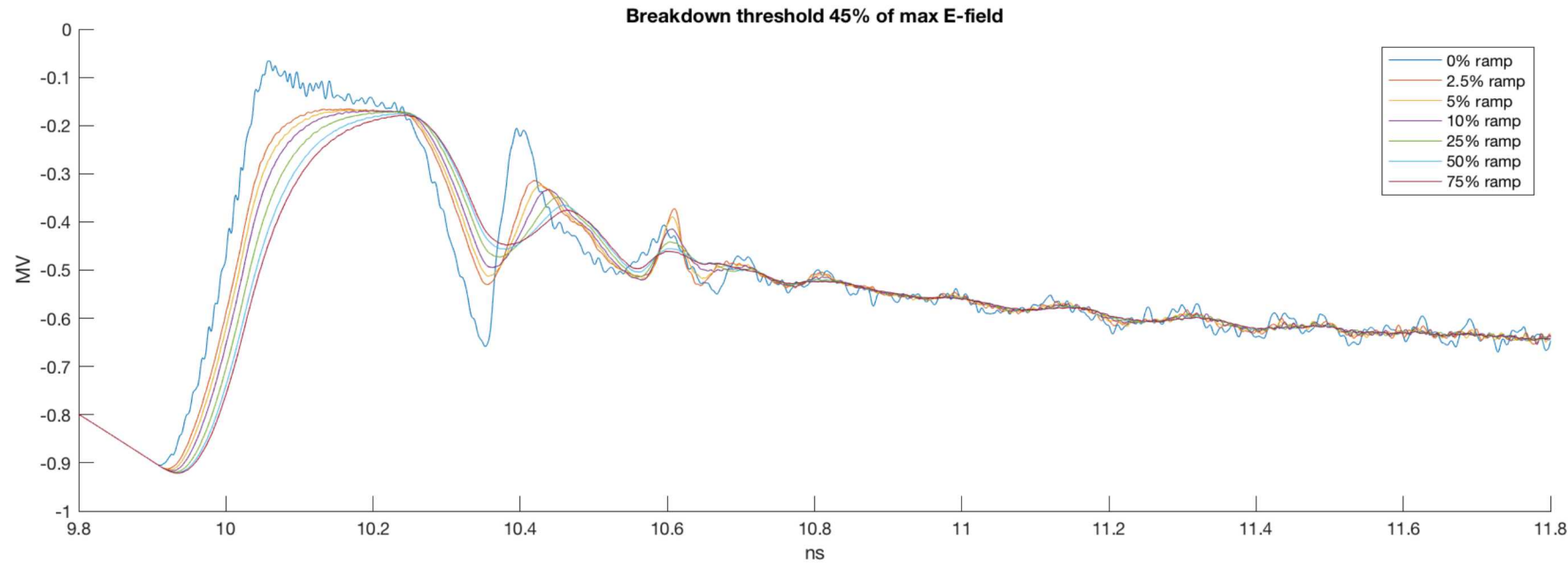
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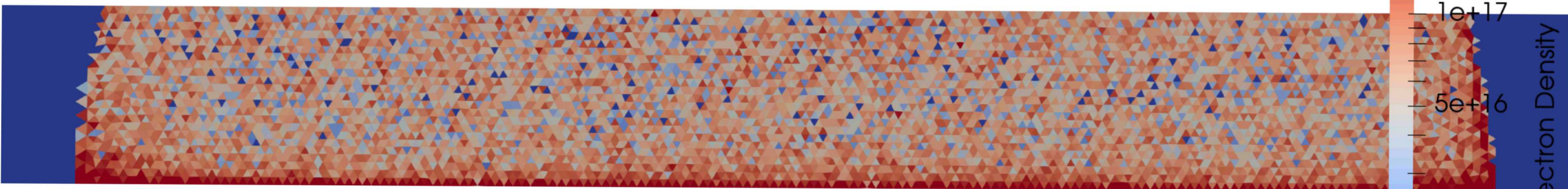
Possible Vircator

- Flat FFTs
- $f \sim 1.1\text{GHz}$
- $n_e \sim 5e16$

$$\omega_P = \sqrt{\frac{n_e e^2}{\gamma_0 m_e \epsilon_0}}$$



Possible Vircator



Conclusions and Future Work

- Problems with PMC boundary conditions
 - Change to periodic BCs
- Possible vircator
 - Plot in phase space
- Non-planar solutions
 - Increase impedance
 - Lower injected current (electrostatic problem with injected beam?)
- Meaningful ramp time definition
 - Increase timestep
- Run 90% breakdown case