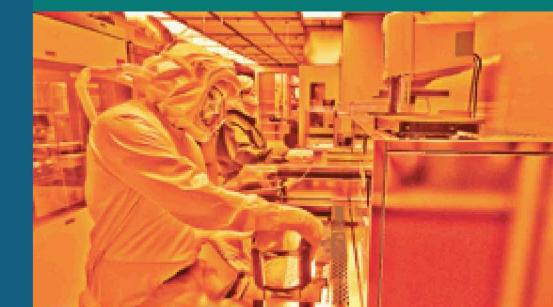
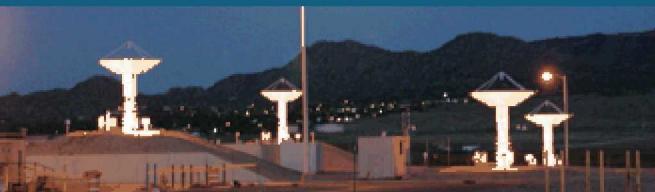


Systematic CMA of the U-slot Patch with FEKO



PRESENTED BY

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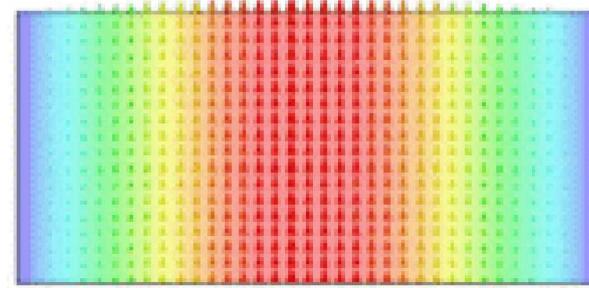
- Characteristic Mode Analysis/dipole example
- Systematic Analysis Steps
- Multimode patches & Coupled Mode Theory
- Apply systematic analysis steps to the U-slot patch

Intro to Characteristic Mode Analysis (CMA)

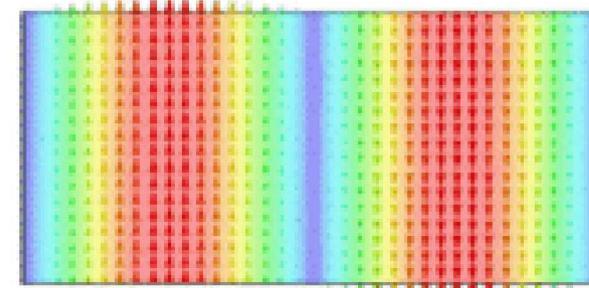
Conceptually similar to waveguide modes, but suited to radiation & scattering problems

$$\nabla_t^2 e = -\beta^2 e$$

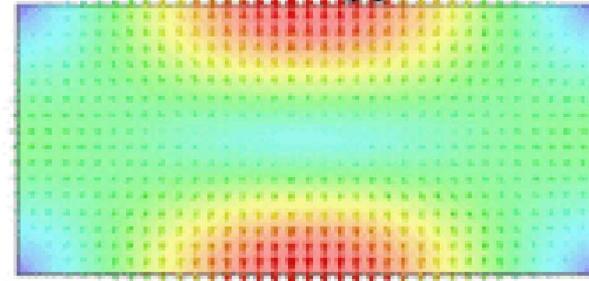
TE₁₀



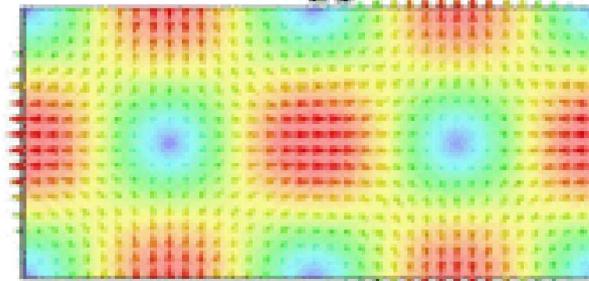
TE₂₀



TM₁₁

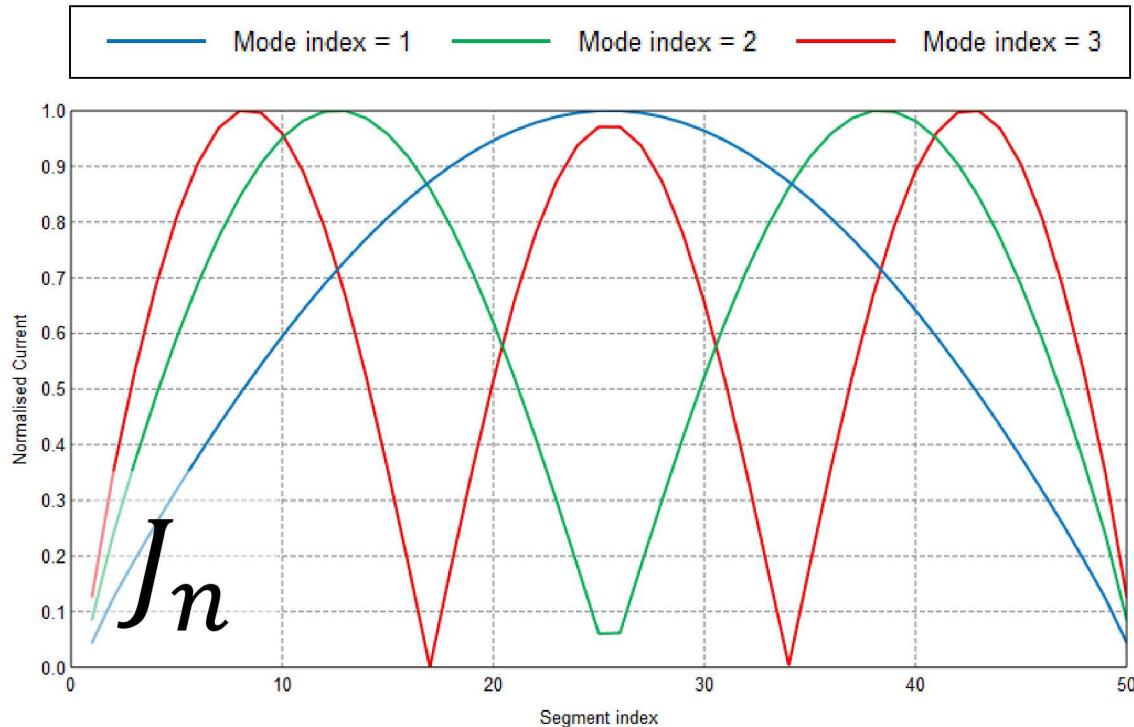


TE₂₁

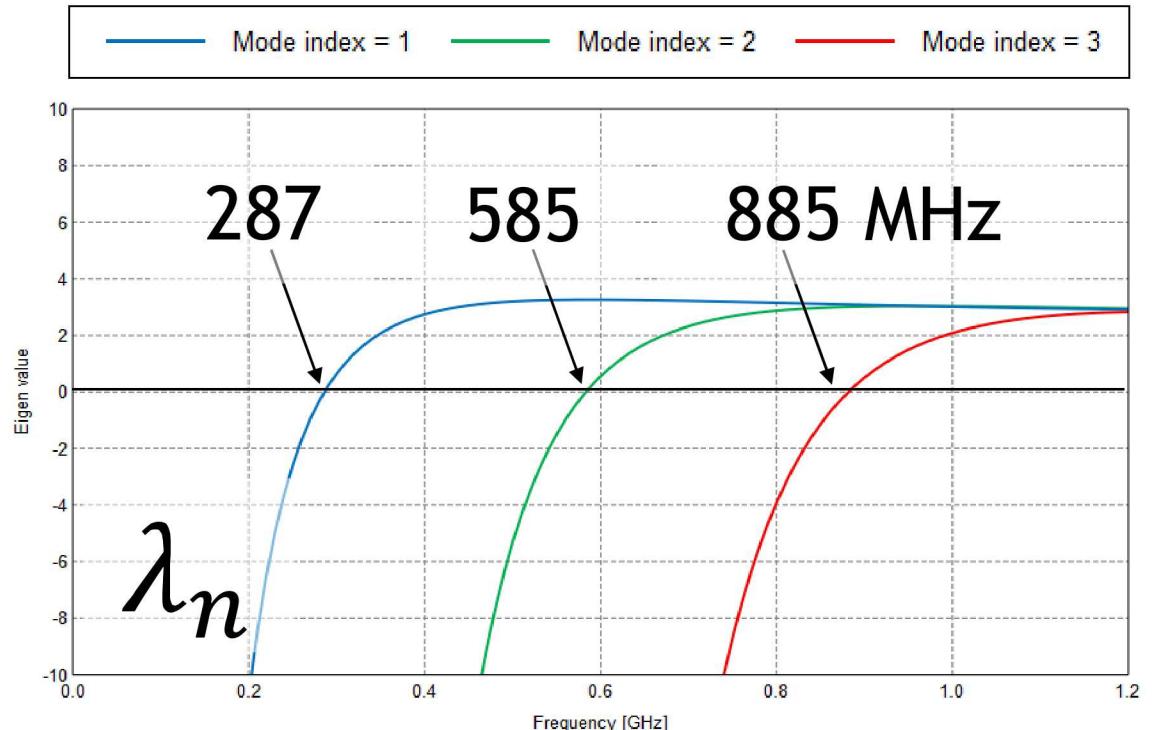
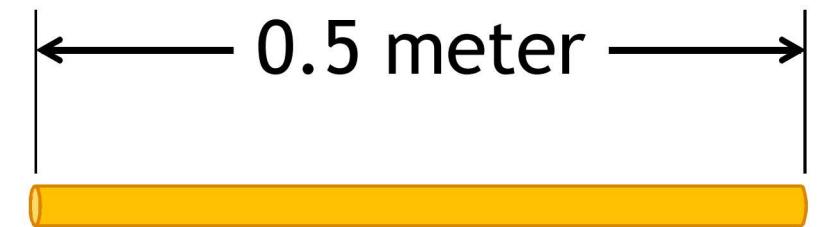


CMA Eigenvalues and Eigenvectors

$$[X] J_n = \lambda_n [R] J_n$$



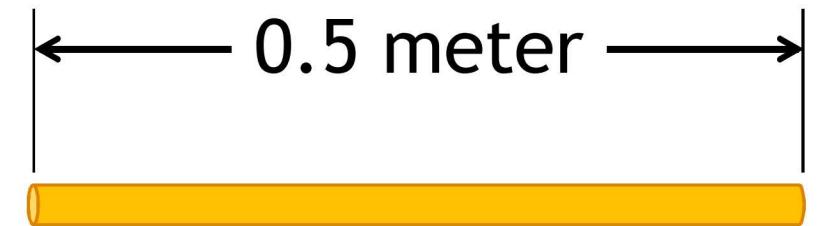
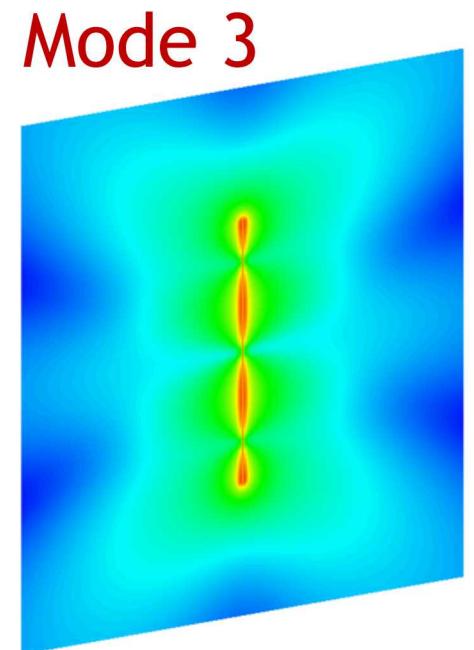
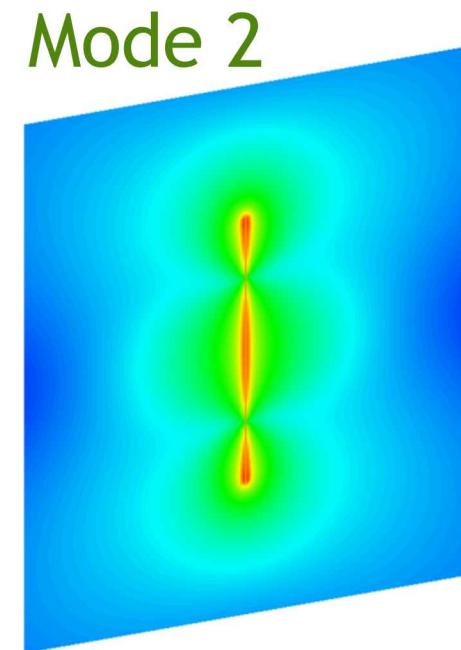
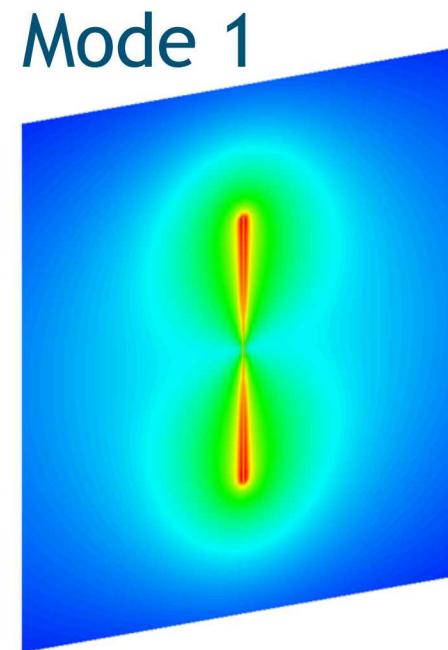
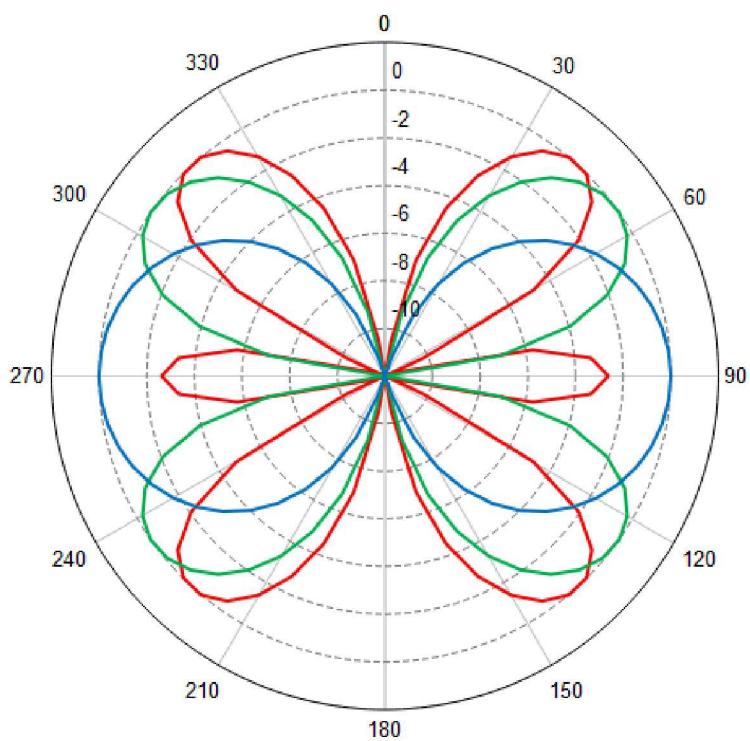
Eigenvectors are currents J_n



Mode resonant when $\lambda_n = 0$

5 Modal Near- and Far-Fields

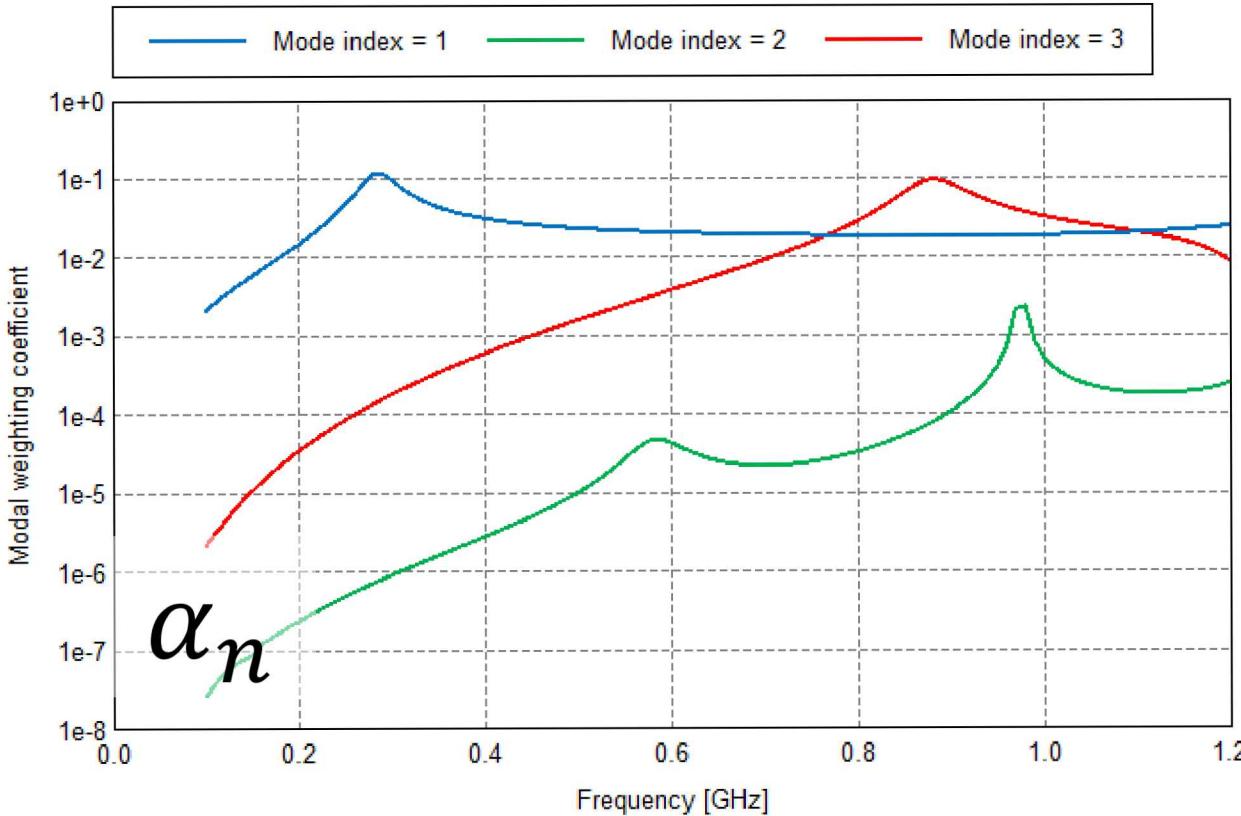
Mode index = 1 Mode index = 2 Mode index = 3



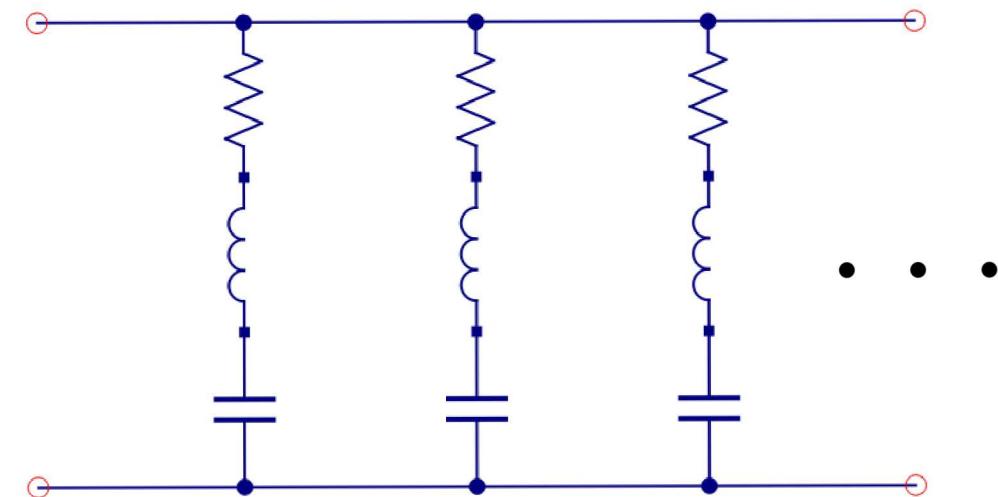
Near- and far-fields are associated with each mode

CMA ***with an Excitation***

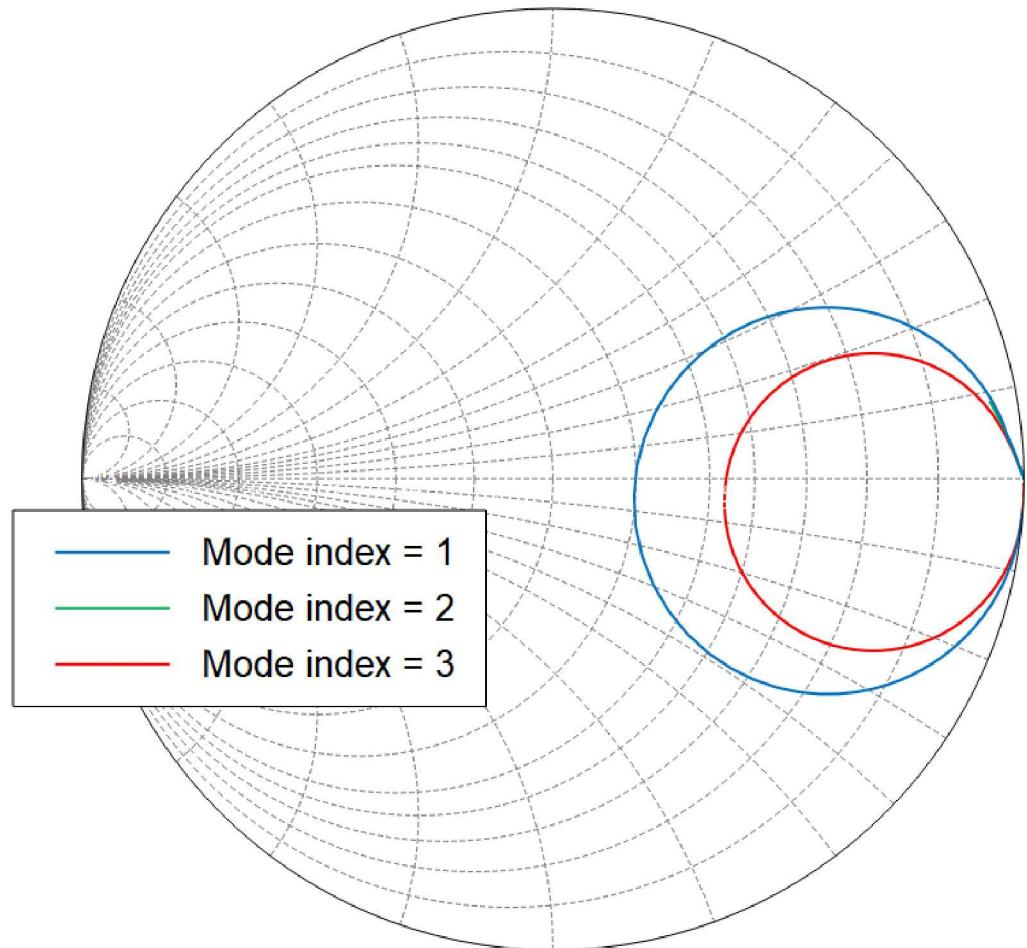
$$J_{tot} = \sum_n \alpha_n J_n \quad \alpha_n = \frac{\langle J_n, E_{tan}^i \rangle}{1 + j\lambda_n}$$



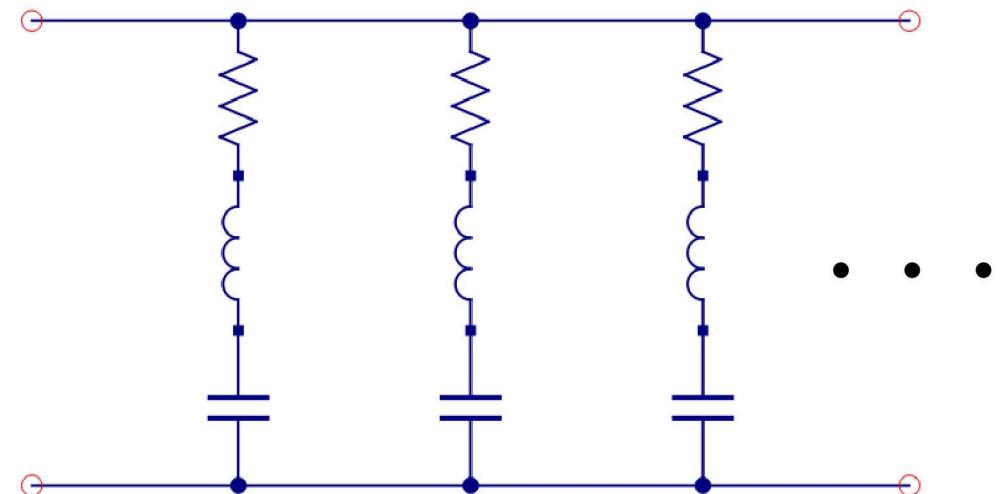
$$Y_{tot}[i] = \sum_n \frac{J_n[i]^2}{1 + j\lambda_n}$$

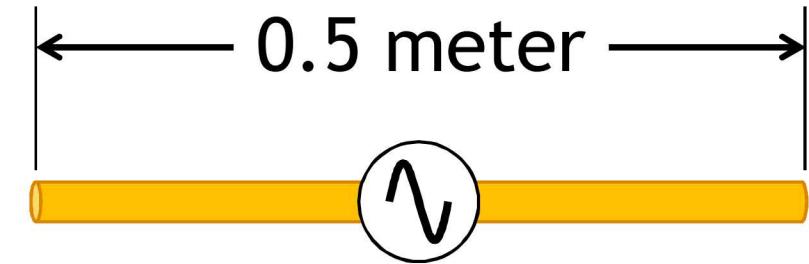
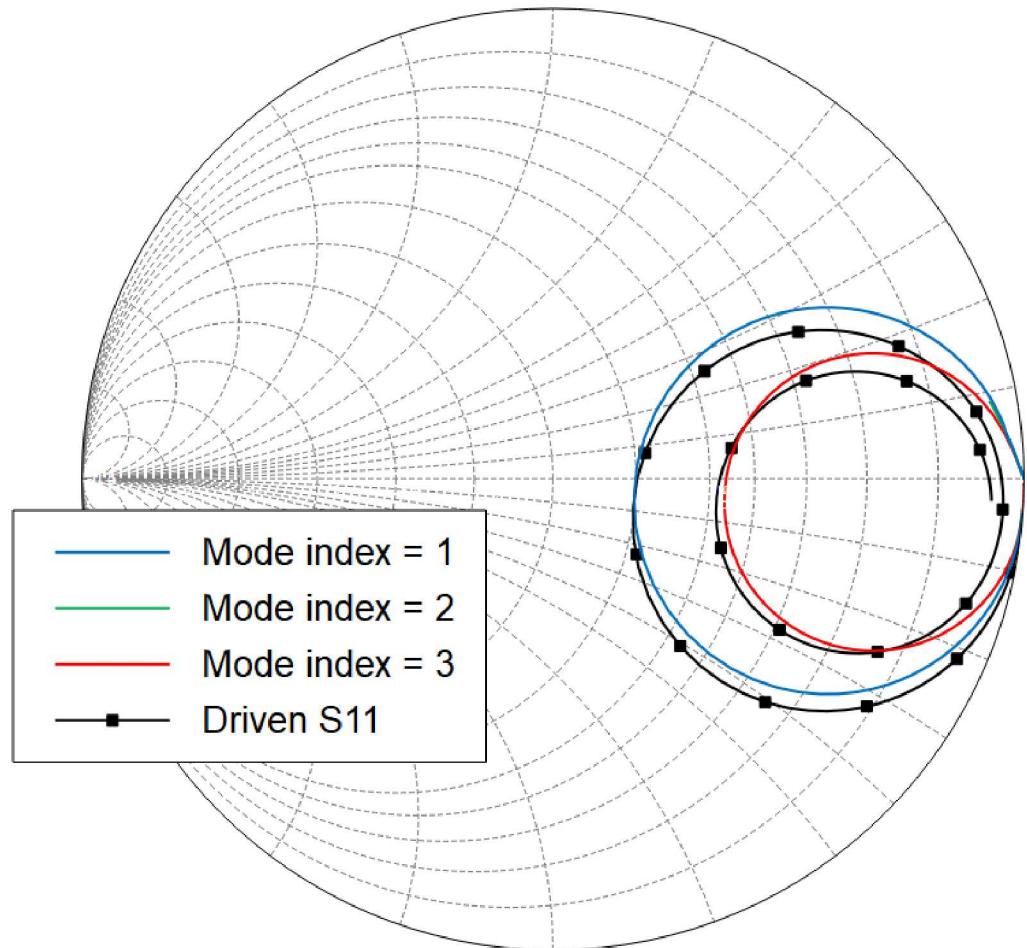


Modal Admittances

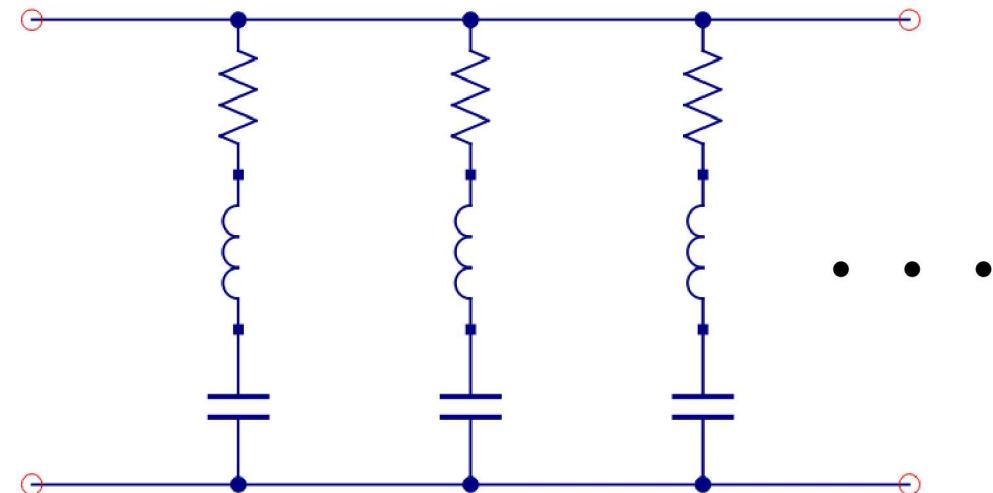


$$Y_{tot}[i] = \sum_n \frac{J_n[i]^2}{1 + j\lambda_n}$$

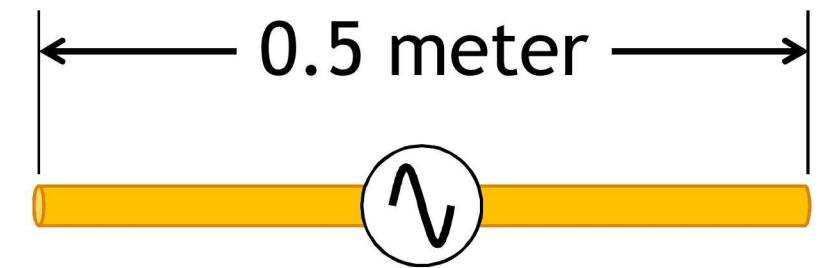
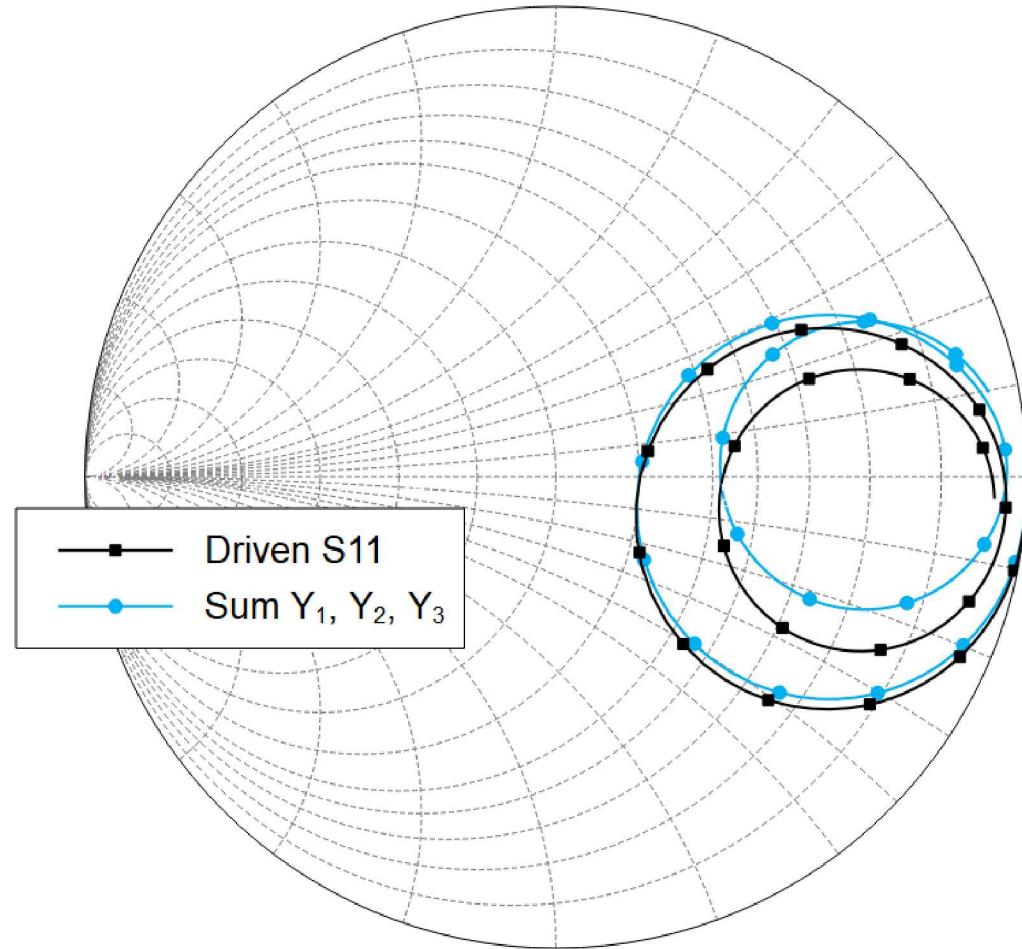




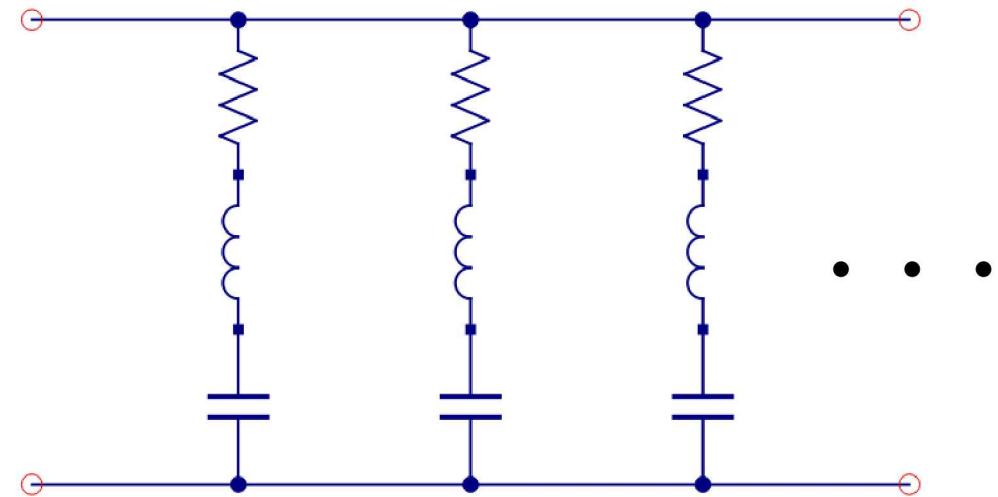
$$Y_{tot}[i] = \sum_n \frac{J_n[i]^2}{1 + j\lambda_n}$$



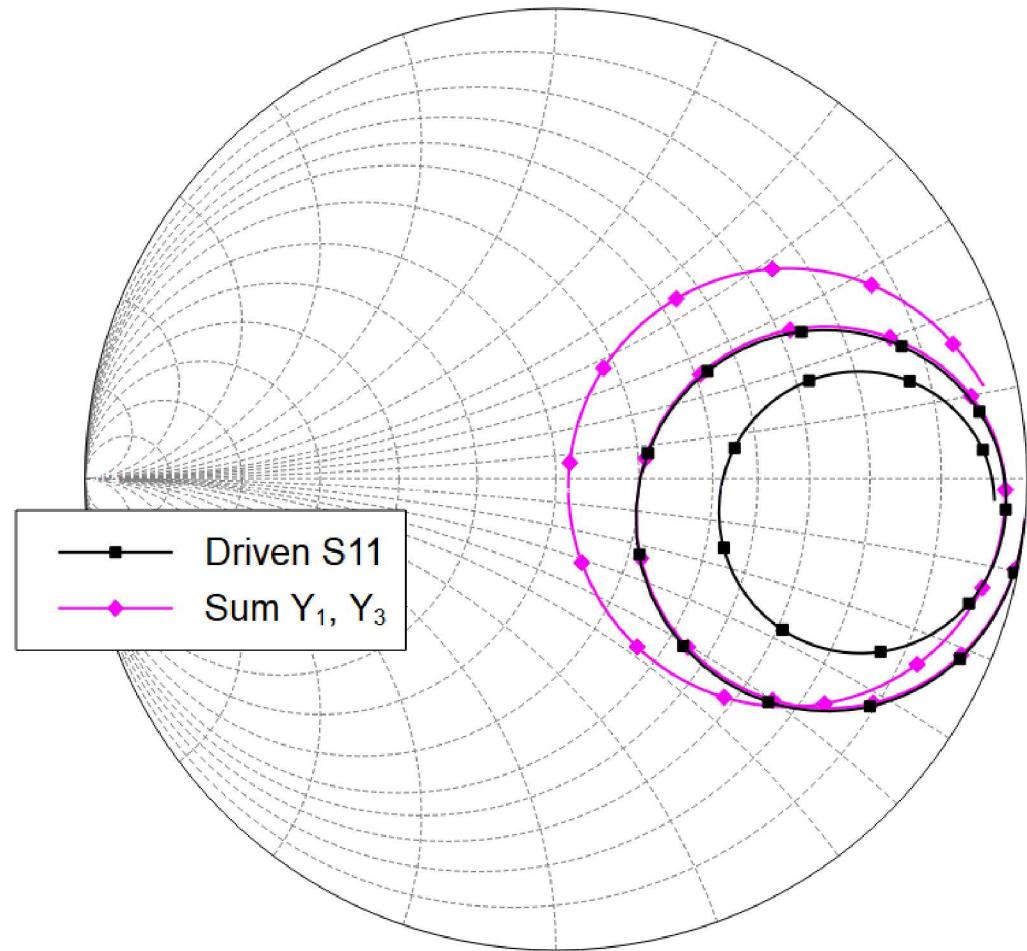
9 Sum of Modal Admittances



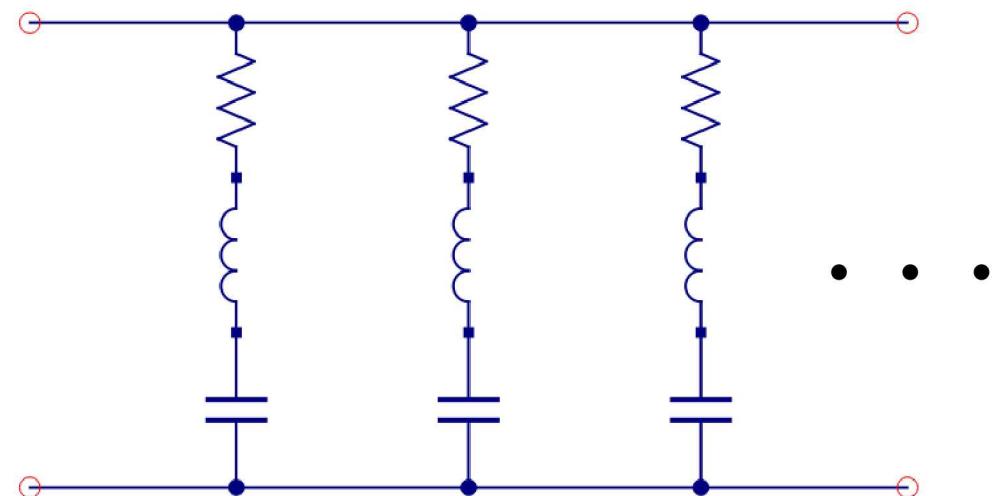
$$Y_{tot}[i] = \sum_n \frac{J_n[i]^2}{1 + j\lambda_n}$$



Sum of Modal Admittances



$$Y_{tot}[i] = \sum_n \frac{J_n[i]^2}{1 + j\lambda_n}$$

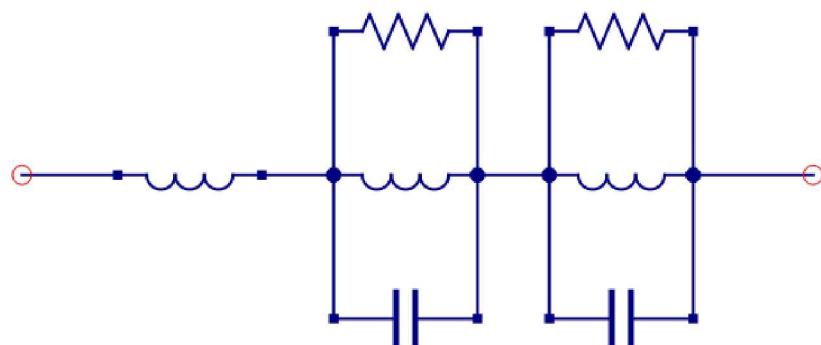
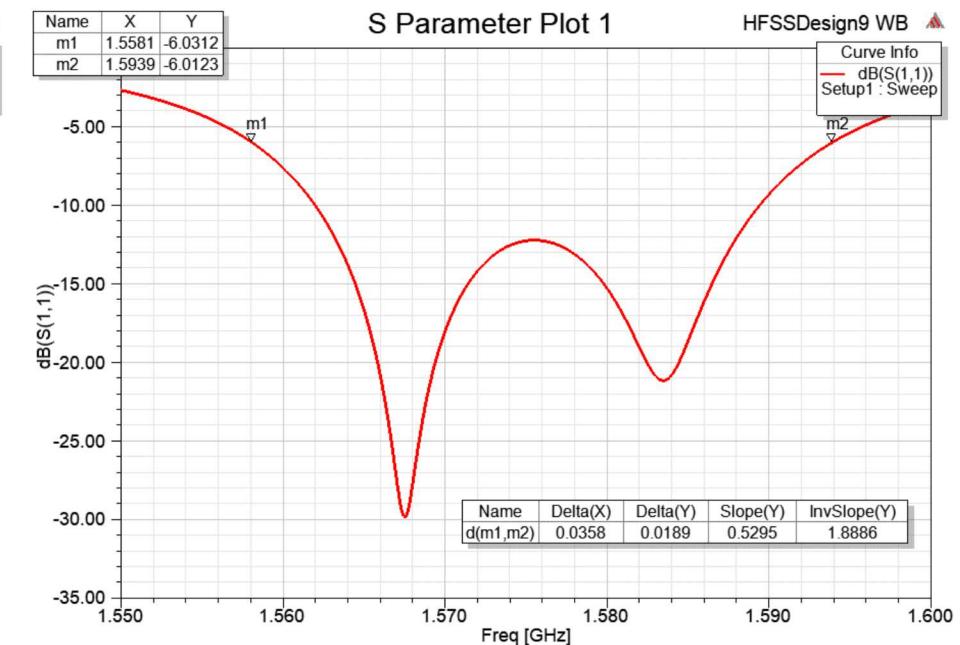
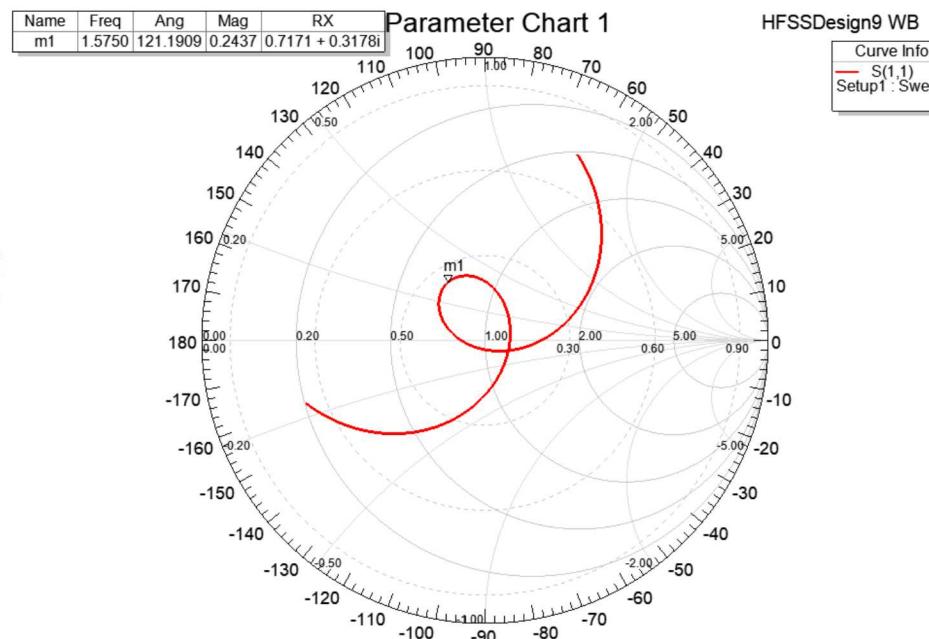


Systematic Analysis of Antennas with CMA

- { (1) include the excitation and run driven MoM problem alongside CMA
- { (2) select resonant modes/select modes with significant MWCs
- { (3) replicate driven admittance with sum of selected modal admittances
- { (4) use CMA current and charge distributions to obtain physical insight
- { (5) for multi-modal antennas establish uncoupled resonator geometries and calculate coupling using near-fields

Patch impedance bandwidth and multi-moding

$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0}$$



$$Z \sim R(1 + j2Q \Delta\omega/\omega_0)$$

Classic U-slot patch

Huynh and Lee, 1995

BW about 30%

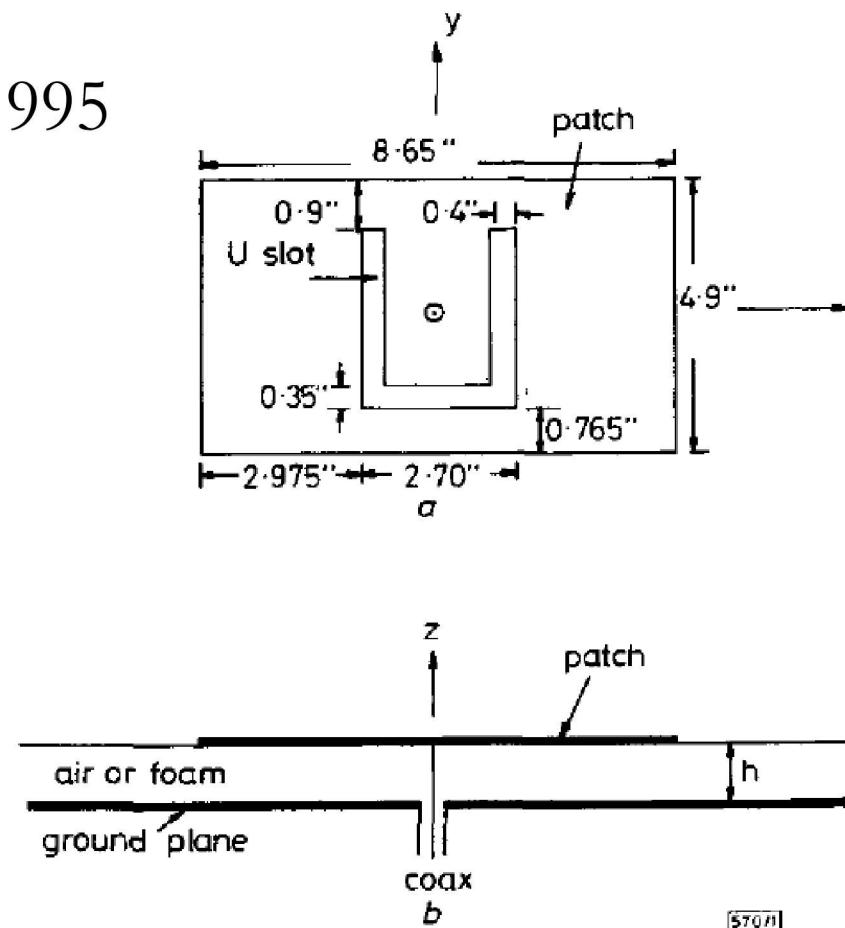
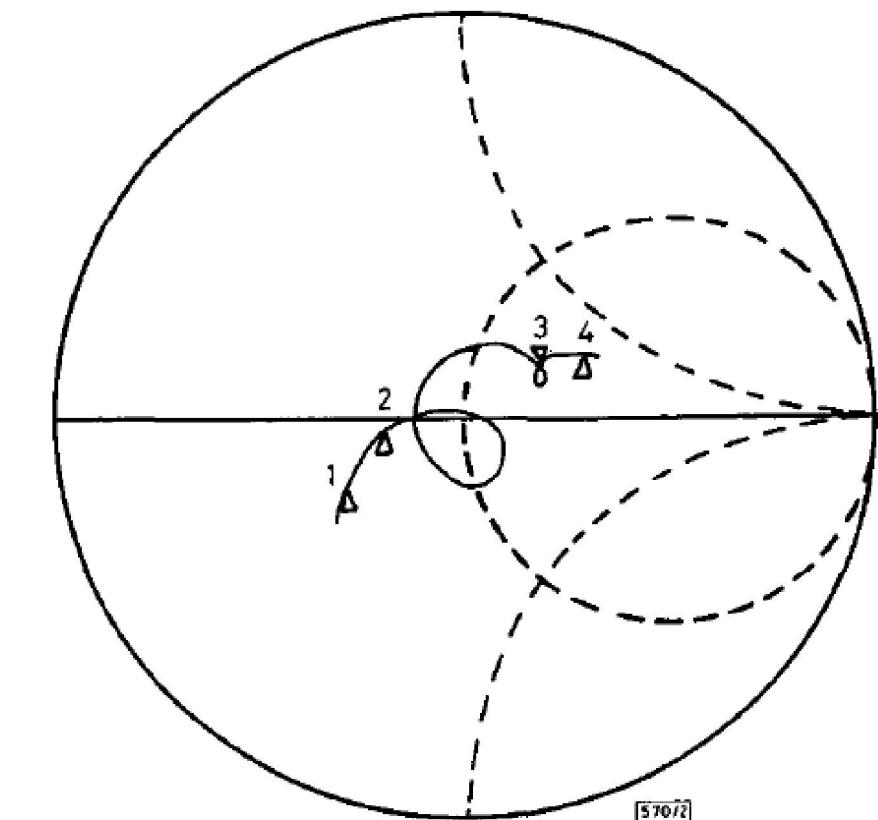
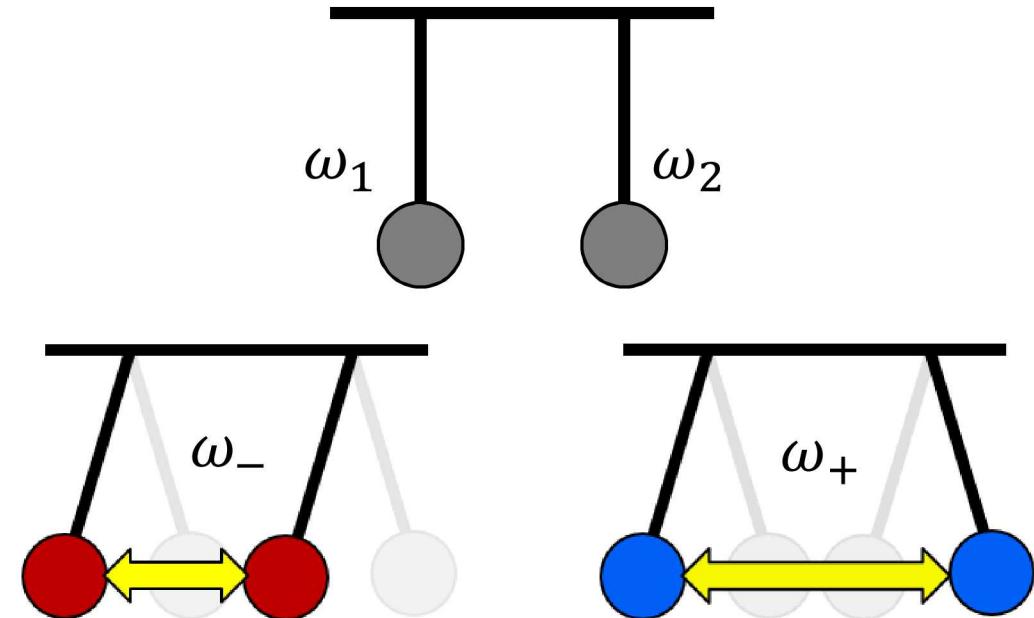
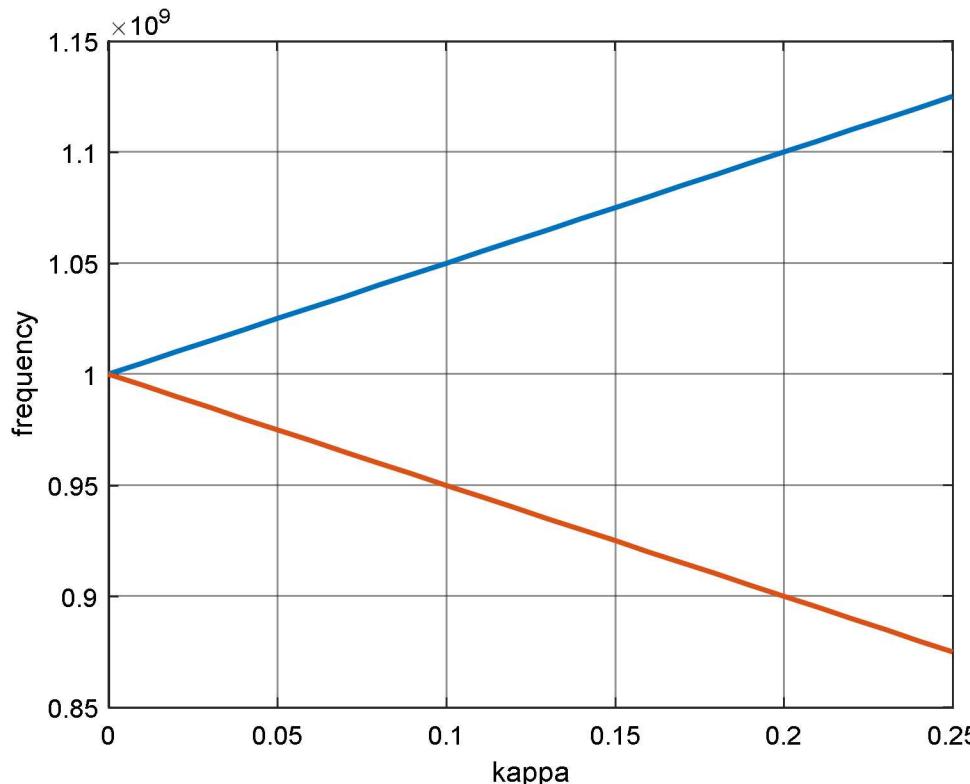


Fig. 1 Geometry of coaxially-fed rectangular patch with U slot. Fig. 2 Measured impedance loci for $h = 1.06$ " ($\approx 0.08\lambda$ at 900 MHz)



Coupled Mode Theory

CMT analyses the motion of a system of two coupled resonators as the combination of in-phase and anti-phase modes of motion

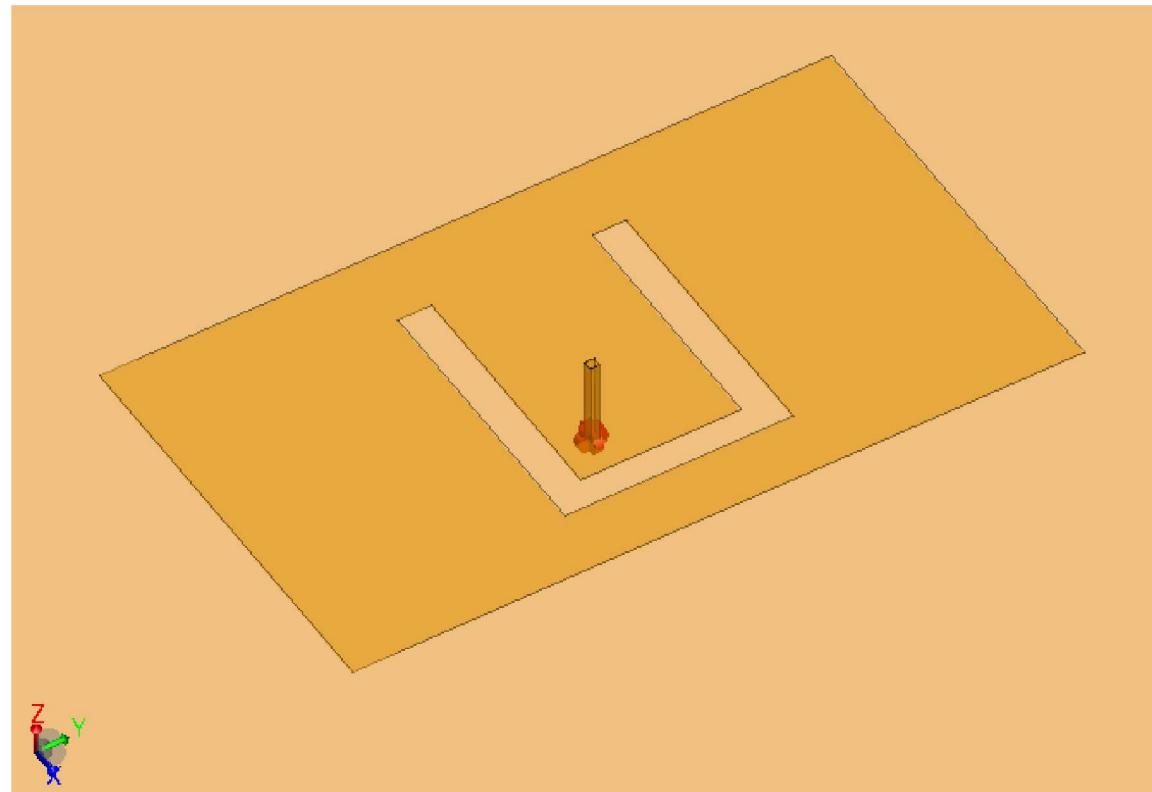
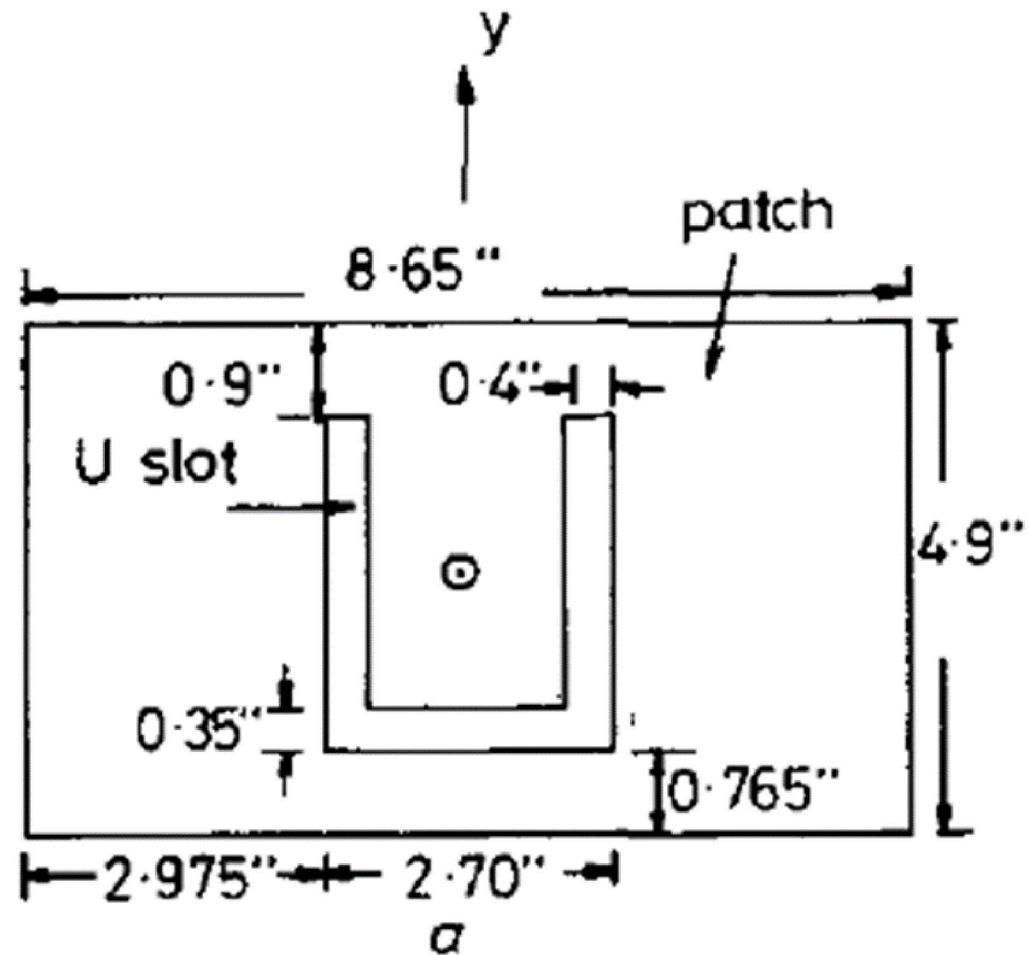


$$\omega_{\pm} = \left(\frac{\omega_2 + \omega_1}{2} \right) \pm \sqrt{\left(\frac{\omega_2 - \omega_1}{2} \right)^2 + |K|^2}$$

$$\omega_2 = \omega_1 \rightarrow \omega_{\pm} = \omega_0 \pm |K|$$

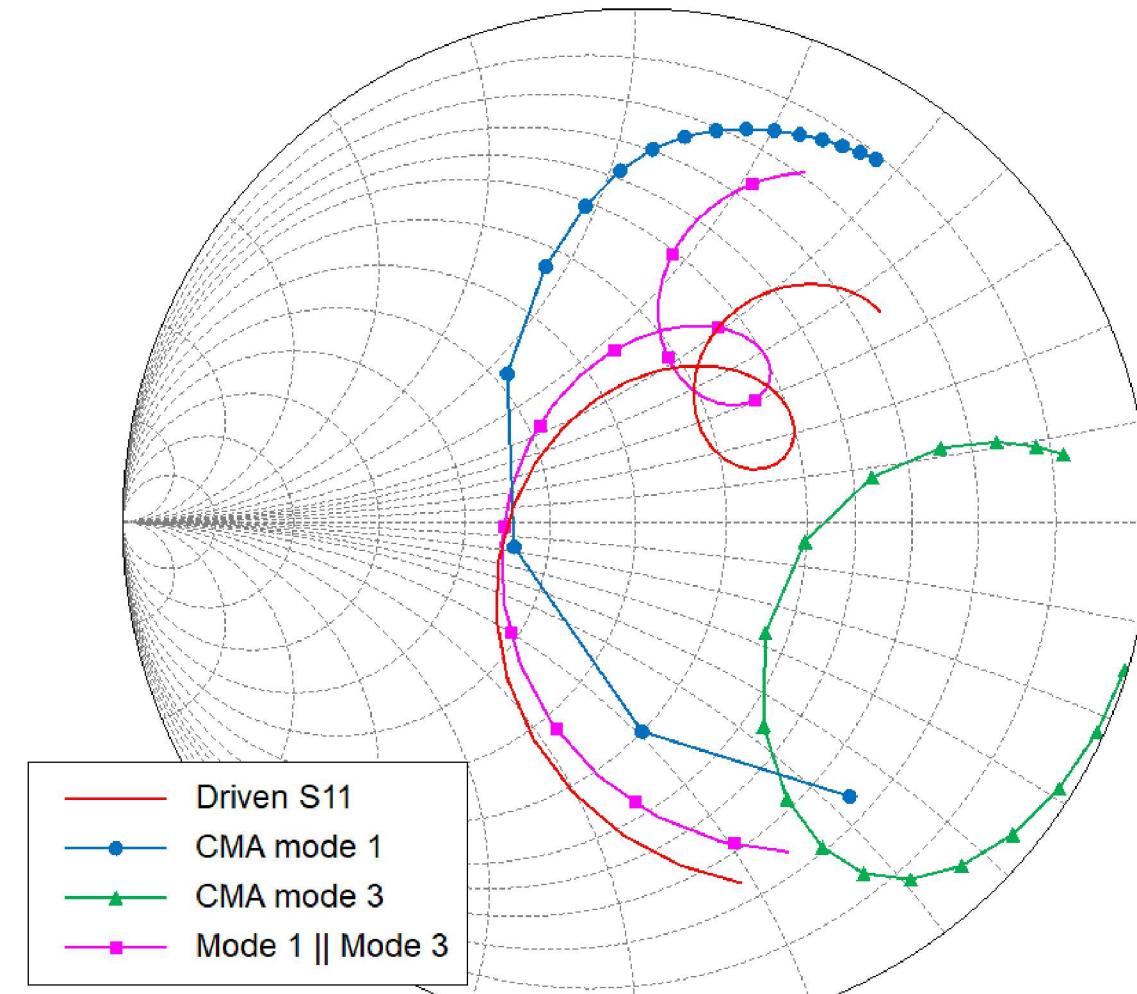
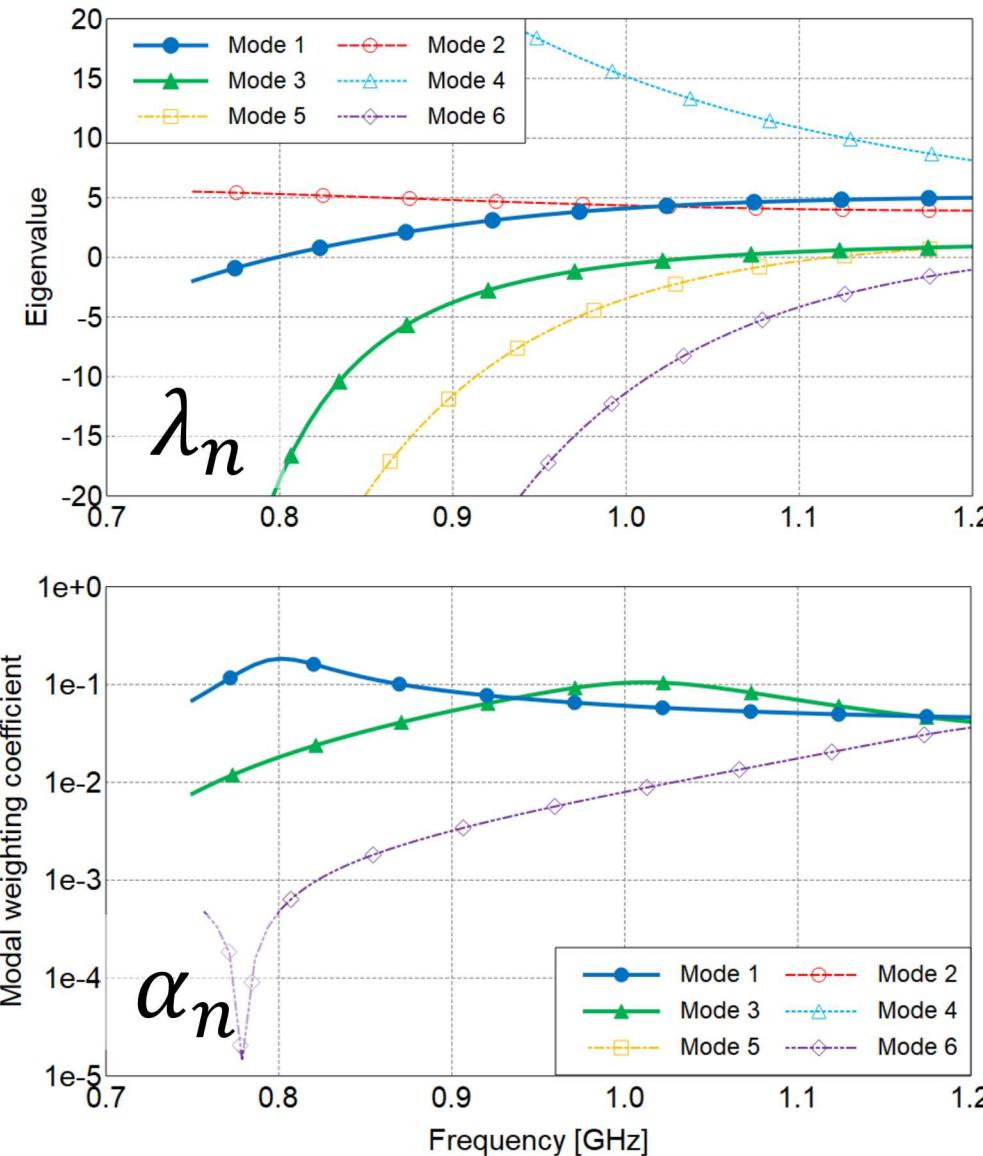
$$\omega_0 = (\omega_2 + \omega_1)/2$$

CMA of the U-slot Patch



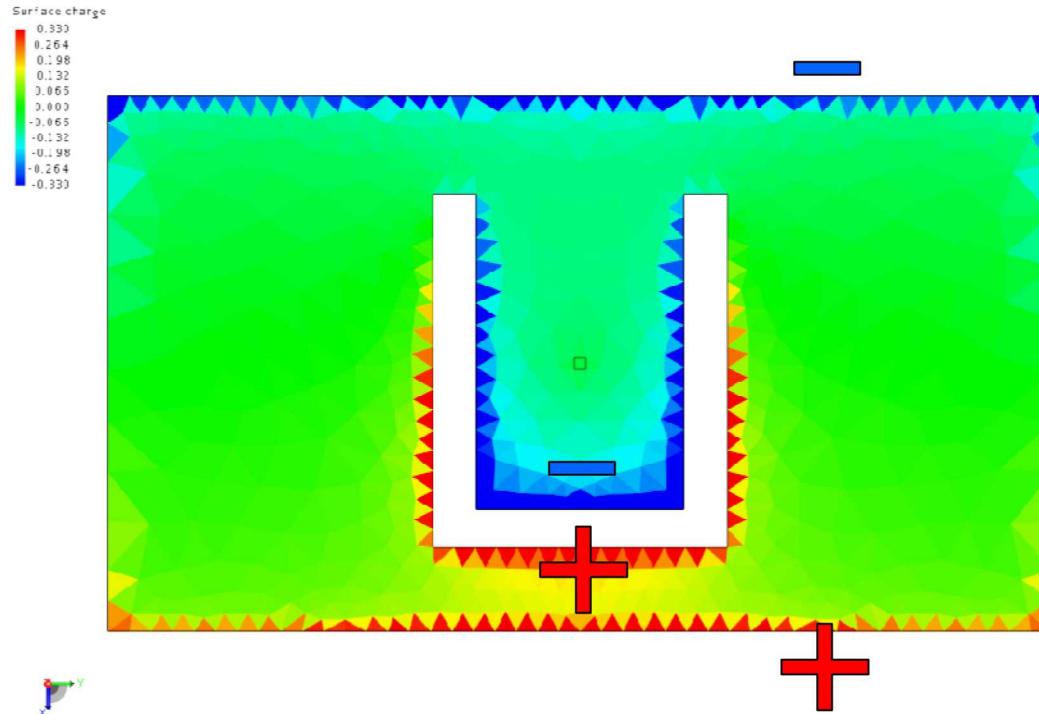
T. Huynh and K. F. Lee, "Single-layer single-patch wideband microstrip antenna," in *Electronics Letters*, vol. 31, no. 16, pp. 1310-1312, 3 Aug. 1995.

Selecting modes



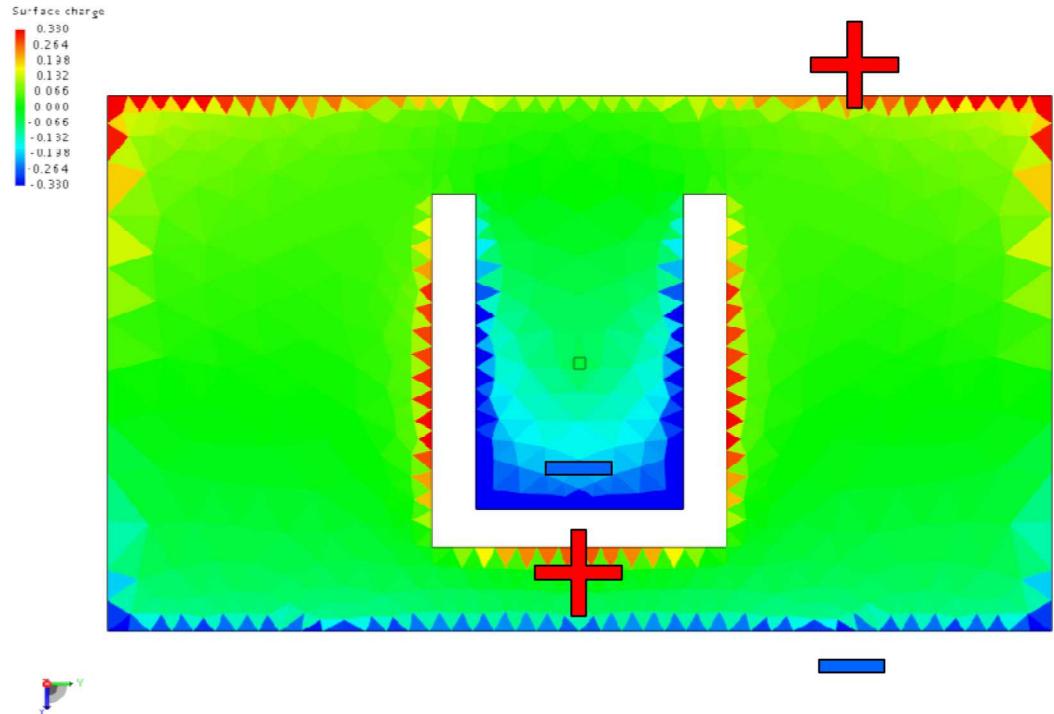
What are these modes?

Mode 1



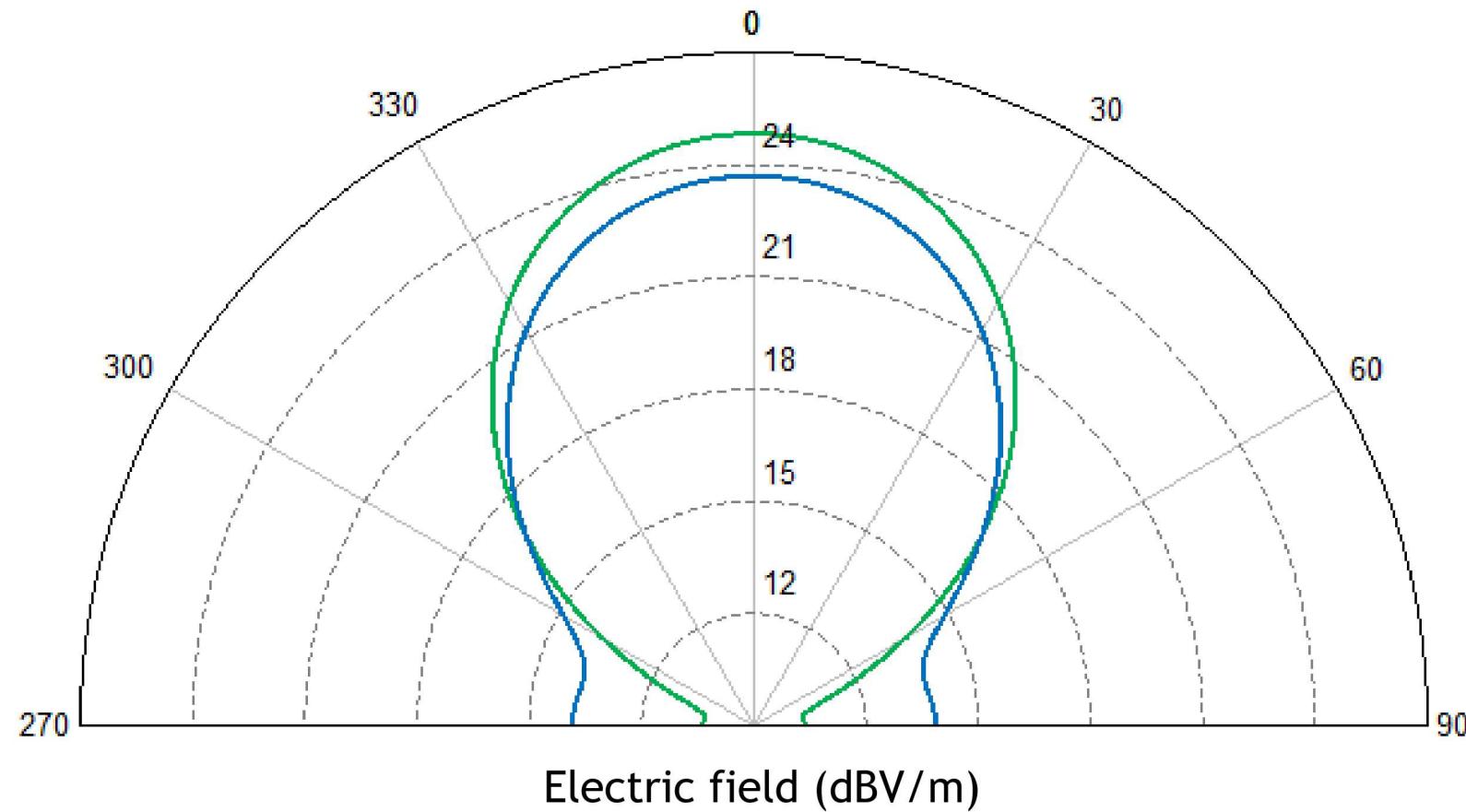
in-phase

Mode 3

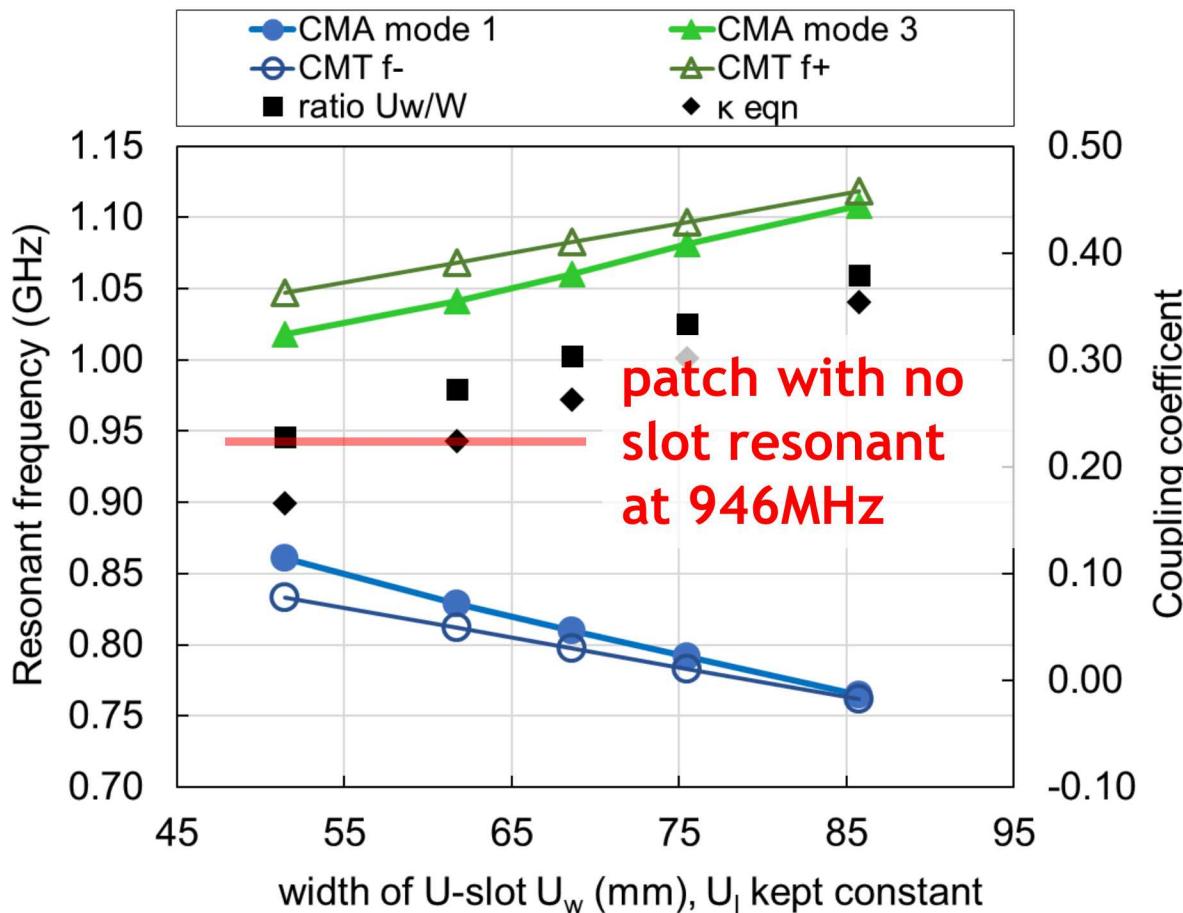


anti-phase

Similar broadside radiation patterns, co-polarized



CMT accurately describes CMA resonances



$$U_l = 2U_h + U_w = \text{constant}$$

$$\kappa = \frac{\omega_+^2 - \omega_-^2}{\omega_+^2 + \omega_-^2}$$

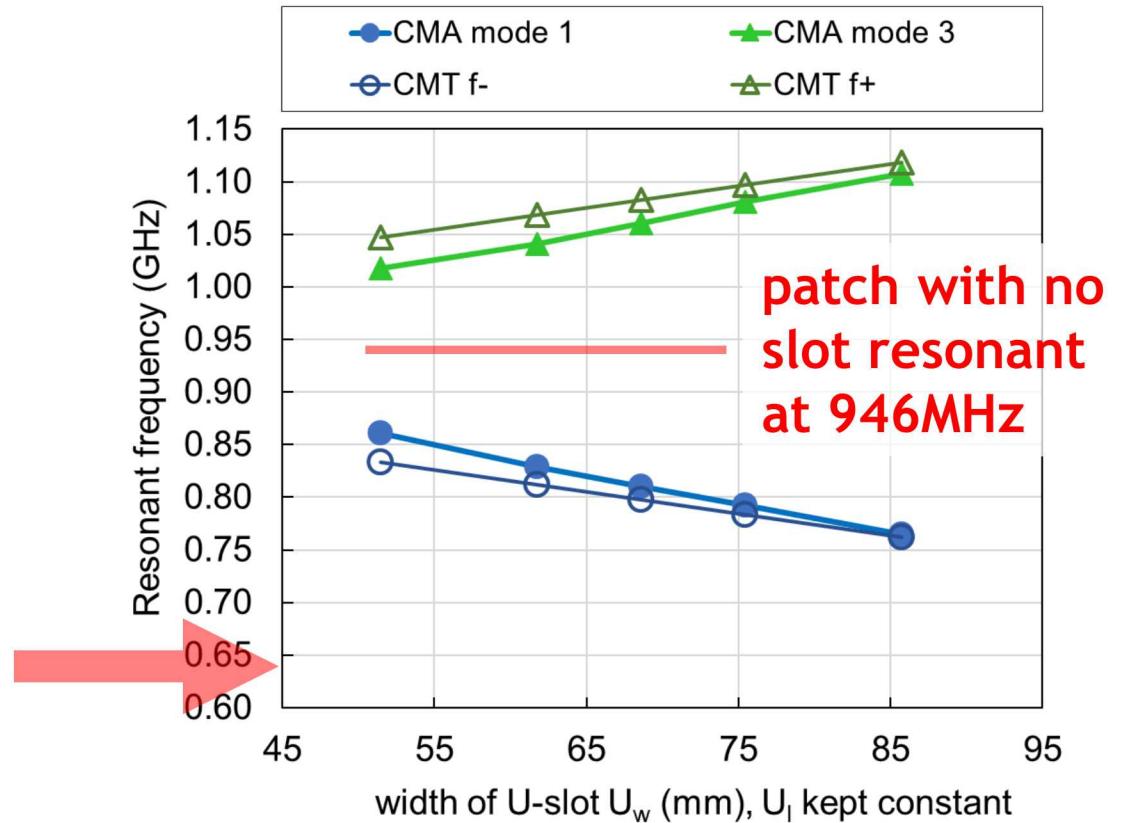
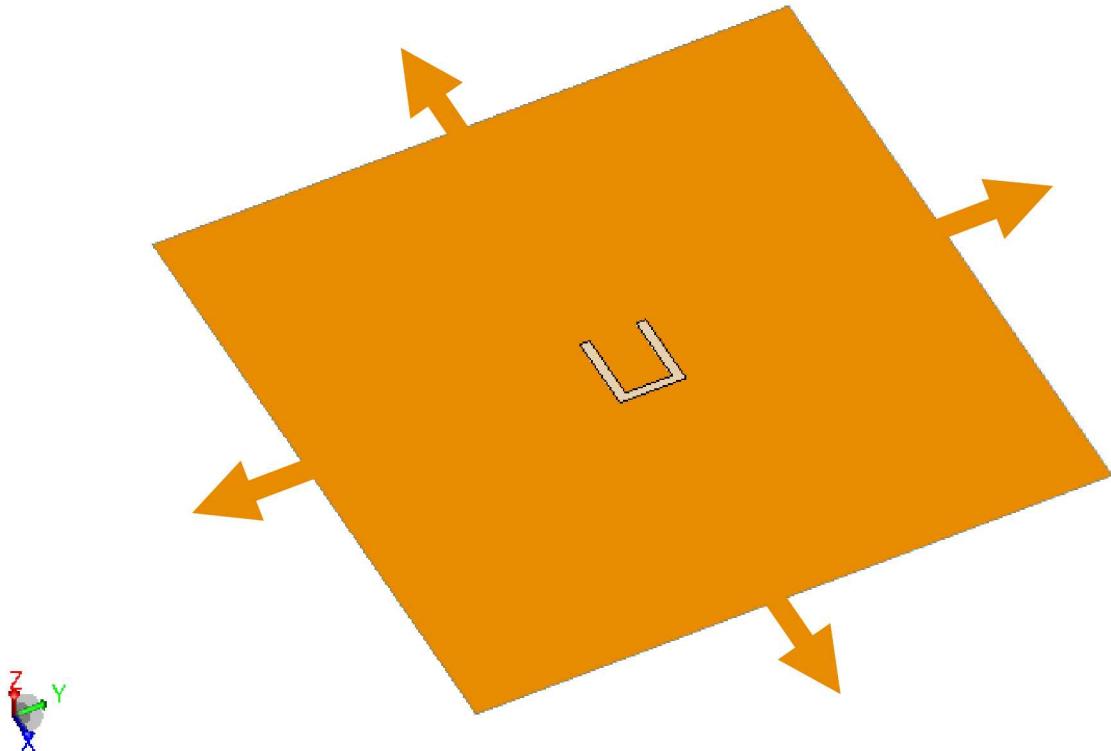
$$\omega_{\pm} = \omega_0 \pm |K| \quad K \sim (\omega_0/2) \kappa$$

$$\kappa \sim U_w/W$$

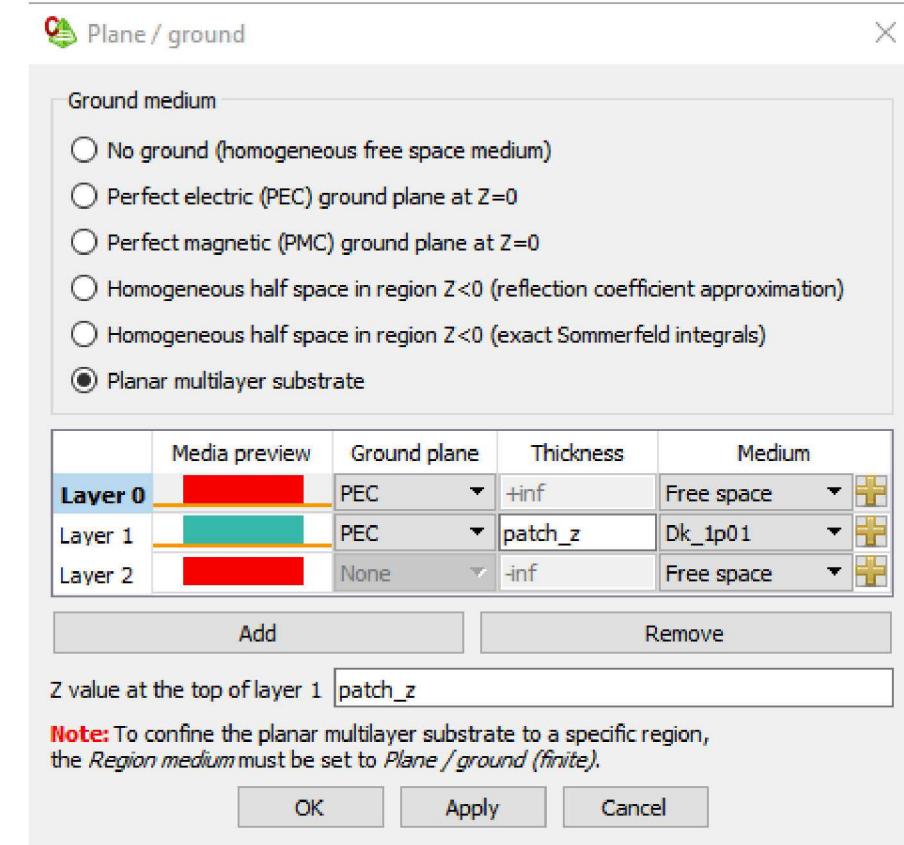
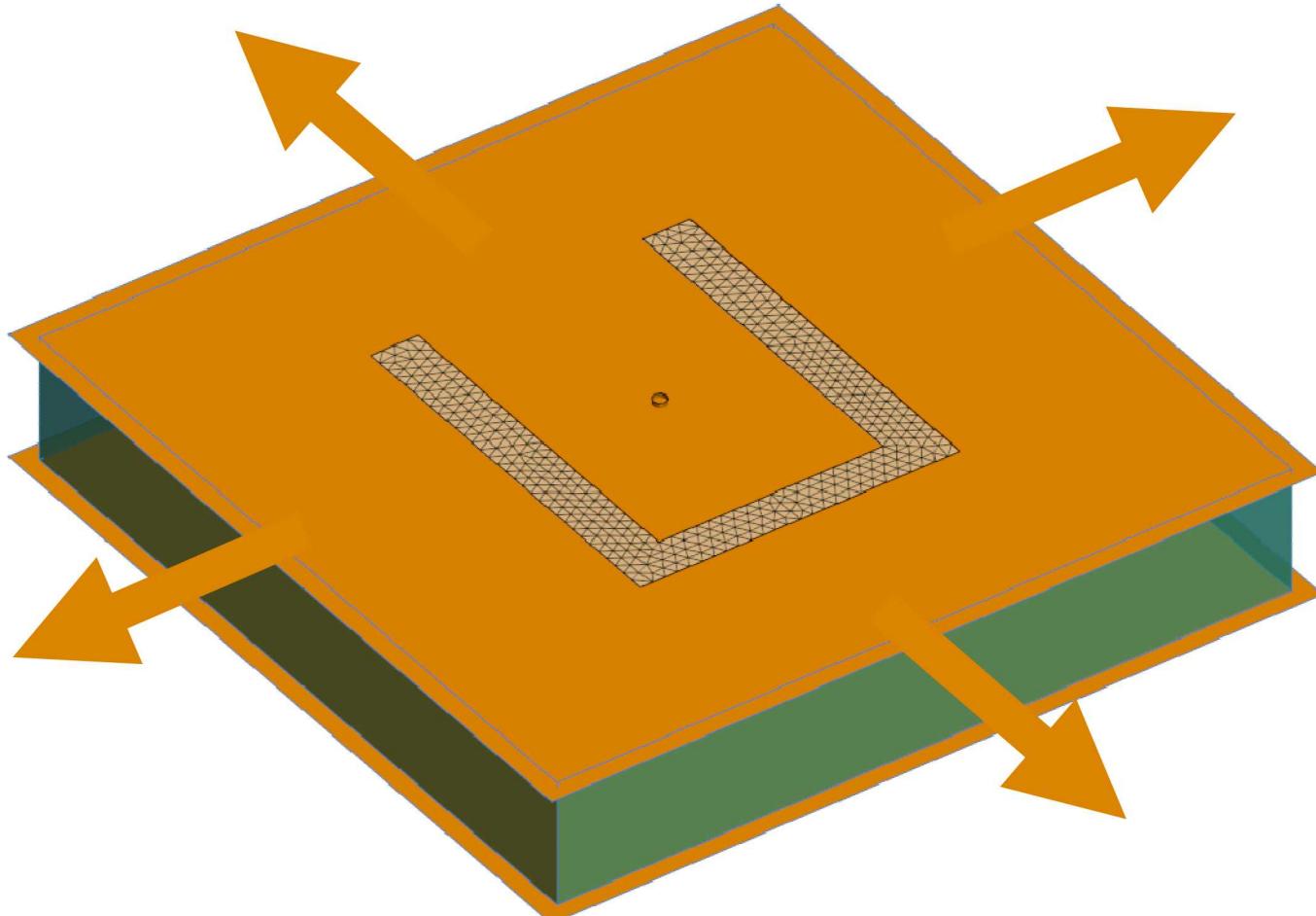
$$\omega_{\pm} = \omega_0 \pm (\omega_0/2) (U_w/W)$$

What is the other resonator?

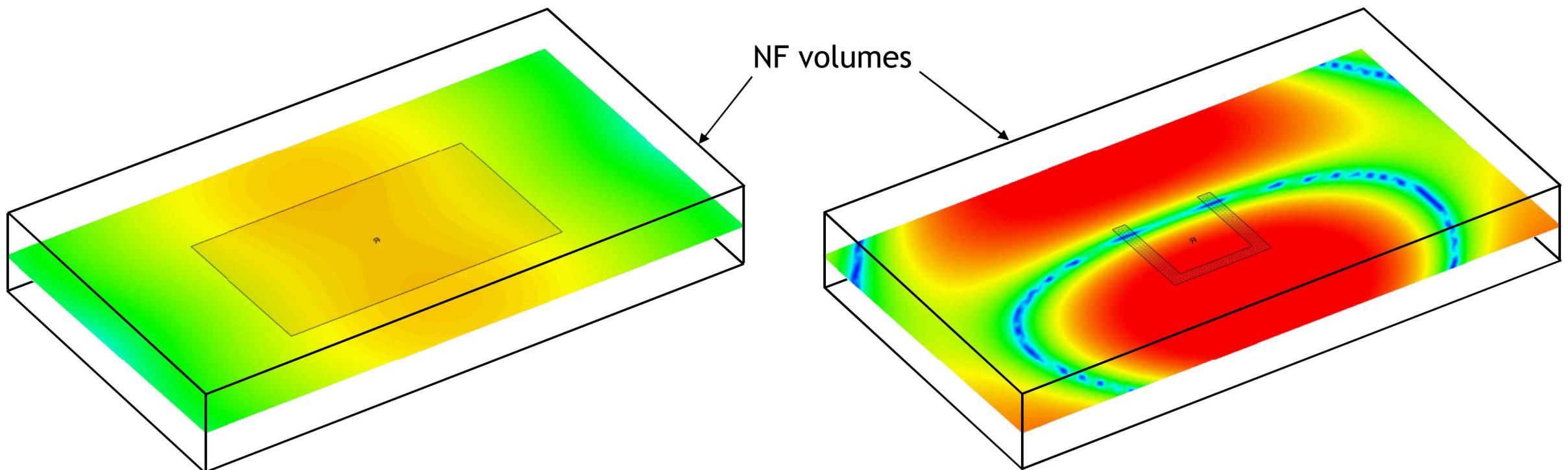
U-slot in single PEC plane gives CM resonance at $\sim 640\text{MHz}$ ($U_l \sim \lambda/2$)...



Uncoupled slot resonator, resonant at ~912MHz



Calculating resonator coupling with modal nearfields



$$\kappa = \frac{\int \epsilon E_1 \circ E_2 \, dV}{\sqrt{W_{e1} W_{e2}}} + \frac{\int \mu H_1 \circ H_2 \, dV}{\sqrt{W_{m1} W_{m2}}}$$

$$|\kappa| = 0.19$$

$$W_{e1,2} = \int \epsilon |E_{1,2}|^2 \, dV \quad W_{m1,2} = \int \mu |H_{1,2}|^2 \, dV$$

J. Hong, IEE Proceedings, vol. 147, no. 5, pp. 354-358, Oct. 2000.



- The U-slot patch operates with **coupled** modes; the patch and slot modes are equally important over the entire impedance bandwidth.
- Include the excitation and run driven MoM problem alongside CMA.
- Use Modal Weighting Coefficients & replicate driven admittance.
- Modal **charge** distributions can be very useful.
- For multi-modal antennas, establish uncoupled resonator geometries and use modal near-fields to calculate coupling.

tinyURL.com/UslotCMA