



Tran Vinh, Ngoc (Orcid ID: 0000-0001-8272-4843)

Sargsyan Khachik (Orcid ID: 0000-0002-1037-786X)

Ivanov Valeriy, Yuryevich (Orcid ID: 0000-0002-5208-2189)

Kim Jongho (Orcid ID: 0000-0002-4101-7429)

A novel modeling framework for computationally efficient and accurate real-time ensemble flood forecasting with uncertainty quantification

Vinh Ngoc Tran¹, M. Chase Dwelle², Khachik Sargsyan³, Valeriy Y. Ivanov², Jongho Kim^{1*}

¹School of Civil and Environmental Engineering, University of Ulsan, South Korea

²Department of Civil and Environmental Engineering, University of Michigan, USA

³Sandia National Laboratories, Livermore, CA 94550, USA

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*Corresponding author: Prof. Jongho Kim, School of Civil and Environmental Engineering, University of Ulsan, South Korea, tel: (+82) 052-259-2855, email: kjongho@ulsan.ac.kr

Abstract:

A novel modeling framework that simultaneously improves accuracy, predictability, and computational efficiency is presented. It embraces the benefits of three modeling techniques integrated together for the first time: surrogate modeling, parameter inference, and data assimilation. The use of polynomial chaos expansion (PCE) surrogates significantly decreases computational time. Parameter inference allows for model faster convergence, reduced uncertainty, and superior accuracy of simulated results. Ensemble Kalman filters (EnKFs) assimilate errors that occur during forecasting. To examine the applicability and effectiveness of the integrated framework, we developed 18 approaches according to how surrogate models are constructed, what type of parameter distributions are used as model inputs, and whether model parameters are updated during the data assimilation procedure. We conclude that (1) PCE must be built over various forcing and flow conditions and, in contrast to previous studies, it does not need to be rebuilt at each time step; (2) model parameter specification that relies on constrained, posterior information of parameters (so-called *Selected* specification) can significantly improve forecasting performance and reduce uncertainty bounds compared to *Random* specification using prior information of parameters; and (3) no substantial differences in results exist between single and dual EnKFs, but the latter better simulates flood peaks. The use of PCE effectively compensates for the computational load added by the parameter inference and data assimilation (up to ~80 times faster). Therefore, the presented approach contributes to a shift in modeling paradigm arguing that complex, high-fidelity hydrologic and hydraulic models should be increasingly adopted for real-time and ensemble flood forecasting.

Keywords: Real-time ensemble flood forecasting, Uncertainty quantification, Polynomial chaos expansions, Generalized Likelihood Uncertainty Estimation, ensemble Kalman filter

1. Introduction

Real-time forecasting is an important component of flood risk management and mitigation but is subject to multiple uncertainties caused by meteorological inputs, initial states, model structures, and model parameters [Beven, 1989; Ajami *et al.*, 2007; Moradkhani and Sorooshian, 2008; Mockler *et al.*, 2016]. Due to the complexities of natural phenomena represented by equifinality [Beven and Freer, 2001; Beven, 2006], hysteresis [Wei and Dewoolkar, 2006; Ivanov *et al.*, 2010; Fatichi *et al.*, 2015], non-uniqueness [Beven, 2000; McKenna *et al.*, 2003; Kim and Ivanov, 2014; Kim *et al.*, 2016a], non-linearity [Kitanidis and Bras, 1980; Xie and Zhang, 2010; Kim and Ivanov, 2015], and internal variability [Nikiema and Laprise, 2011; Mondal and Mujumdar, 2012; Lafaysse *et al.*, 2014; Kim *et al.*, 2016c; Kim *et al.*, 2016b; Kim *et al.*, 2018], perfect predictions using numerical models are infeasible. The problem exacerbates, if one attempts to simulate constitutive models derived from empirical or phenomenological observations rather than basic conservation laws of physics that would also require embracing a large number of parameters. Forecasting systems must therefore rely on approaches with intrinsic tools to quantify and reduce associated uncertainties and allow end-users to make informed decisions [Todini, 1999; 2004].

Forecasts made with sufficient lead time can mitigate flood damages considerably. Results should therefore be provided within a predetermined time horizon and accurate enough to promote community confidence in actions taken for emergency preparedness [Todini, 2004; APFM, 2013]. Extensive efforts have been devoted to enhance forecast accuracy, predictability, and efficiency in real time with uncertainty quantification (Table 1). However, simultaneous improvement of predictive accuracy and efficiency, while evaluating effectiveness, remains a major challenge [Liu *et al.*, 2012; Cintra and Velho, 2018].

For the purpose of enhancing model accuracy in real-time flood forecasting where no information of model states and parameters is available, data assimilation (DA) has been proven useful. Due to the nature of forecasting, the effect of future unknowns (model parameters and states) on flood prediction will change over time. In addition, uncertainty can be amplified not only by the features of the model itself, but also by errors in forcing data and observations. Therefore, model adjustment for the forecasting period may be necessary [Young, 2002; Moradkhani *et al.*, 2005b]. Several assimilation methods have been developed using Kalman or particle filters and optimization or inference techniques such as the back-fitting algorithm [Zhang *et al.*, 2018], shuffled complex evolution algorithm [Li *et al.*, 2014], shuffled complex evolution metropolis [Vrugt *et al.*, 2005], generalized likelihood uncertainty estimation (GLUE) [Beven and Freer, 2001], and sequential Bayesian combination [DeChant and Moradkhani, 2014]. Due to the higher computational requirements of the latter techniques, filter-type approaches have attracted attention as assimilation tools [Moradkhani and Sorooshian, 2008; Gharamti *et al.*, 2013].

Currently, the ensemble Kalman filter (EnKF) [Evensen, 1994] and its modifications (e.g., ensemble Kalman smoothers, ensemble square-root filters, and gain function) are the most commonly used techniques in the hydrology community (Table 1), despite the issue of slow convergence caused by intrinsic assumptions, especially for domains with complexities [Moradkhani *et al.*, 2005a; Weerts and El Serafy, 2006; Moradkhani *et al.*, 2012; Wang *et al.*, 2017]. Recent studies have suggested that particle filtering (PF) [Arulampalam *et al.*, 2002] is an alternative method to resolve the inclusion of unrealistic Gaussian assumptions in the EnKF. The PF method has more advantages than EnKF in reducing numerical instability by providing particle weights and using non-Gaussian state-space models [Liu *et al.*, 2012]. However, this method is computationally more expensive as it generally requires more ensemble members [Moradkhani *et al.*, 2005a; Liu *et al.*, 2012].

When assimilating data, model parameter specification and state initialization may play a crucial role, especially for short-range forecasting [Houtekamer and Zhang, 2016].

Generally, ensemble initialization of model states and parameters for the forecasting period can be generated approximately, e.g., using a random selection from uniform distributions for parameters and setting up the initial state values as an arbitrary number (e.g., zero) at the beginning of the forecasting period [Moradkhani et al., 2005a; Vrugt et al., 2005; Moradkhani et al., 2012; Xie and Zhang, 2013; DeChant and Moradkhani, 2014; Davison et al., 2017; Abbaszadeh et al., 2018]. Alternatively, the ensemble can be generated more carefully, e.g., specifying parameters from relevant distributions [Beven and Freer, 2001; Madsen and Skotner, 2005; Ajami et al., 2007; Clark et al., 2008; He et al., 2012; Mendoza et al., 2012; Chen et al., 2013; Zahmatkesh et al., 2015] and using a warm-up technique for states [Ajami et al., 2007; He et al., 2012; Mendoza et al., 2012; DeChant and Moradkhani, 2014; Wang et al., 2018], as summarized in Table 1.

The assimilation techniques described above generally require a large number of model evaluations to update parameter and state values and present predictive uncertainties, leading to computational challenges [Vrugt et al., 2008; Vrugt, 2016; Zhang et al., 2017], even with the benefit of parallel computation with multiple processors [Cintra and Velho, 2018]. Because keeping calculation time to a minimum is a key element for timely flood warnings and responding to emergency situations [Ballio and Guadagnini, 2004; Sene, 2008], it is necessary to find alternatives that significantly increase forecast lead time. Surrogate modeling can address this challenge by substituting computationally intensive models with computationally efficient metamodels, such as the polynomial chaos expansion (PCE). Through the expansion of orthogonal polynomials, approximate functions can be constructed and applied to hydrologic models. Recent studies have used PCE to perform robust uncertainty assessment of diverse hydrologic problems [Sochala and Le Maître, 2013; Fan et

al., 2014; *Wu et al.*, 2014; *Wang et al.*, 2015; *Fan et al.*, 2016; *Wang et al.*, 2017; *Wang et al.*, 2018; *Dwelle et al.*, 2019] rather than running deterministic models. However, few studies have tested its effectiveness in a setting of real-time flood forecasting [*Wang et al.*, 2015; *Fan et al.*, 2016; *Wang et al.*, 2017; *Wang et al.*, 2018].

To fill the above gaps, we propose a novel integrated modeling framework that improves accuracy, predictability, and efficiency of real-time flood forecasting. Eighteen approaches to the framework are presented, combining ways of constructing the surrogate models, specifying model parameters and states, and assimilating newly observed data. This study investigates (i) the effects of building methods of the PCE model and its capacity for real-time flood forecasting; (ii) the effects of specifying methods on predictive performance; (iii) the effects of single- and dual-assimilation techniques; and (iv) the computational time of the proposed approaches.

2. Methodologies and Frameworks

2.1. Methodologies

2.1.1. Deterministic rainfall-runoff model: NAM

To construct a surrogate model, simulate streamflow, quantify uncertainty, and assimilate observed data, a Nedbør–Afstrømnings model (NAM) [*Nielsen and Hansen*, 1973] is employed. As one of the widely used deterministic, lumped models, it is considered useful and flexible and has been applied to many catchments [*Madsen*, 2000; *Butts et al.*, 2004; *Thompson et al.*, 2004; *O'Brien et al.*, 2013; *Mockler et al.*, 2016]. Specifically, its design assumes three different and mutually integrated storages representing a surface zone, lower zone, and routing components that simulate overland flow, interflow, and base flow, respectively. The model requires two input forcing variables (M_I) of spatially averaged precipitation and evapotranspiration, five model states ($M_S = 5$), and nine model parameter

values ($M_P = 9$) listed in Table 2 [DHI, 2014]. The latter states and parameters control the amount of water content and the rates of release from the conceptualized storage compartments of the model. Because evapotranspiration is assumed to be negligible during the rainy season with flooding events, the number of inputs used in this study is 1 ($M_I = 1$).

2.1.2. Surrogate model: polynomial chaos expansion

Polynomial chaos expansion (PCE) [Wiener, 1938; Ghanem and Spanos, 1991] can build a surrogate model ($\mathcal{M}^{PCE}$) for any (deterministic rainfall-runoff) model ($\mathcal{M}$) through the expansions of orthogonal polynomials. This enables a polynomial approximation of the model through its deterministic input/output relationship. The form of a PCE model approximating a model output (e.g., streamflow y_t) as a function of model parameters θ_t is given as:

$$y_t = \mathcal{M}(\theta_t) \approx \mathcal{M}^{PCE_t}(\theta_t) \quad (1)$$

Note that the surrogate model ($\mathcal{M}^{PCE}$) in Eq. 1 has the subscript of t , indicating that the surrogate model is a collection of PCEs constructed at each time step of interest. Also, only the parameter θ_t (this includes a subscript of t as well) is chosen as an input variable during PCE construction, and other forcing or state inputs required to simulate hydrologic models are held constant [Sochala and Le Maître, 2013; Fan et al., 2016; Meng and Li, 2018; Wang et al., 2018; Dwelle et al., 2019; Tran and Kim, 2019]. This mathematical formulation conveys that PCE should be built separately for each time step at which a meteorological condition or model state is updated.

Unlike previous studies based on Eq. 1, this study constructs the surrogate PCE model with Eq. 2, which has three characteristics: (i) the model input consists of meteorological data, model states, and model parameters; (ii) model parameters do not change over time,

which is different from Eq. 1; and (iii) there is no need to constantly create the PCE model over time (which is the most important practical feature). The single PCE model represents streamflow phenomena over the entire calibration period during which the PCE model was generated. Specifically, ensemble model output ($\mathbf{Y}_t$) at each time step, including streamflow (y_t) and states ($\mathbf{x}_t$), can be written as a function of model inputs ($\mathbf{X}_t$), including states ($\mathbf{x}_{t-1}$), climate data ($\mathbf{u}_t$), and time-invariant parameters ($\boldsymbol{\theta}$):

$$\mathbf{Y}_t = \mathcal{M}(\mathbf{X}_t) \approx \mathcal{M}^{PCE}(\mathbf{X}_t) = \sum_{\boldsymbol{\alpha} \in A} \varepsilon_{\boldsymbol{\alpha}} \Psi_{\boldsymbol{\alpha}}(\mathbf{X}_t) \quad (2)$$

$$\mathbf{Y}_t = [y_t \ \mathbf{x}_t], \quad \mathbf{X}_t = [\mathbf{x}_{t-1} \ \mathbf{u}_t \ \boldsymbol{\theta}] \quad (3)$$

where $\varepsilon_{\boldsymbol{\alpha}}$ represents the PCE coefficients to be determined for all multi-indices, $\boldsymbol{\alpha} = \{\alpha_1, \dots, \alpha_{M_X}\}$ belonging to a set of candidate polynomials $A, \{\boldsymbol{\alpha} \in A\}$. $\Psi_{\boldsymbol{\alpha}}(\mathbf{X}_t)$ represents the multivariate polynomials corresponding to the given input $\mathbf{X}_t$. The polynomials are constructed as the product of univariate orthonormal polynomials:

$$\Psi_{\boldsymbol{\alpha}}(\mathbf{X}_t) = \prod_{j=1}^{M_X} \Psi_{\alpha_j}^{(j)}(\mathbf{X}_t^j) \quad (4)$$

where $\Psi_{\alpha_j}^{(j)}$ is the univariate orthonormal polynomials of the j -th variables of the degree α_j . In general, the size of $\mathbf{X}_t$, M_X , is equal to the summation of the number of parameters, states, and forcing inputs of the deterministic NAM model (i.e., $M_X = M_p + M_s + M_I$). Set A is determined by M_X and the polynomial degree, p of the PCE model as:

$$A = A^{M_X, p} = \{\boldsymbol{\alpha} \in \mathbb{N}^{M_X} : |\boldsymbol{\alpha}| \leq p\}, \text{card } A^{M_X, p} = \binom{M_X + p}{p} \quad (5)$$

Various polynomial bases (e.g., uniform, Gaussian, beta, and gamma) can be chosen for $\Psi_{\alpha}(\mathbf{X}_t)$ from the Weiner–Askey scheme, depending on the probabilistic characteristics of model input variables $\mathbf{X}_t$ [Xiu and Karniadakis, 2002].

Given the set of multivariate orthonormal polynomials ($\Psi_{\alpha}(\mathbf{X}_t)$), the next step is to compute the PCE coefficients (ε_{α}), which are influenced by the number of model evaluations (called the experimental design, N) and the polynomial degree, p [Blatman and Sudret, 2010; Blatman and Sudret, 2011]. Increasing these numbers requires significant computational resources and the requirement is higher. When using the projection method [Ghiocel and Ghanem, 2002; Le Maître et al., 2002], one of the methods employed to compute PCE coefficients, N is determined based on p and the size of $\mathbf{X}_t$, M_X as $N = (p+1)^{M_X}$. This number is large enough that it takes a considerable time to construct the surrogate model [Blatman and Sudret, 2011; Tran and Kim, 2019]. Reducing N is desirable as it lessens the computational cost. For the least-squares regression method adopted in this study, N is not defined a priori and is provided by the researcher, which can enable a significant decrease for the value of N [Berveiller et al., 2006; Sudret, 2008; Blatman and Sudret, 2010]. Also, p can be determined by the complexity of model outputs and the subjectivity of researcher, with many studies choosing values of 2 or 3 [Sochala and Le Maître, 2013; Fan et al., 2014; Wang et al., 2015; Wang et al., 2017]. Investigating the effects of varying values of N and p on the PCE model allows for determination of the optimal values of the both parameters. According to the approach by Blatman and Sudret [2010], a metric of the leave-one-out (LOO) cross-validation error in Eq. A.5 can illustrate the performance of the PCE model. A brief overview of the construction of the PCE surrogate model is detailed in Appendix A.

2.1.3. Parameter inference: GLUE

GLUE [Beven and Binley, 1992] refers to a series of procedures for inferring parameter posterior distributions and quantifying the associated uncertainties. The objective of GLUE is to select “behavioral” model runs based on the threshold values of likelihood functions with observations, among a large number of runs simulated with random combinations of parameter values. The latter parameter’s values can be sampled randomly from the prior distributions of each parameter (constrained in this study with upper and lower bounds of Table 2) using Monte Carlo or Latin hypercube sampling (LHS). For more efficient performance, LHS was used [Helton and Davis, 2003]. The likelihood functions proposed in this study are three metrics of Nash–Sutcliffe efficiency (NSE), peak error (PE), and volume error (VE) defined in Appendix B, representing the model performance with respect to the shape, peak, and volume of hydrograph, respectively. Acceptance threshold values are determined according to an approach [Tran and Kim, 2019] in which relationships between accuracy and efficiency indices are identified for their determinations. Specifically, cutoff threshold values for the likelihood functions of NSE , PE , and VE are suggested as 0.8, 5%, and 5%, respectively [Tran and Kim, 2019]. The model runs (or parameters) that satisfy the modelling error within the above thresholds for all the likelihood functions are defined here as “behavioral” runs (or parameters).

2.1.4. Ensemble data assimilation: Single and dual EnKFs

Among many reported techniques, the single ensemble Karman filter (EnKF) and the dual-ensemble Karman filter (dual EnKF) are often chosen to optimally update the ensemble of model states (and parameters) of forecasting systems with real-time observations, which can be coupled with any models [Evensen, 1994; Burgers *et al.*, 1998; Moradkhani *et al.*, 2005b; Whitaker, 2012]. Specific details are provided in Appendix C.

The EnKF allows for the perturbation of observations to generate replicates of $\mathbf{x}_{t-1}$ and $\boldsymbol{\theta}_t$, and the correction of the ensemble forecast members through an update step (Eqs. C.10 and C.18) [Moradkhani *et al.*, 2005b]. This prevents the EnKF from a collapse in which all ensemble forecast members are likely to have similar values [Burgers *et al.*, 1998]. As shown in Eq. C.11, observations can be perturbed by adding stochastic noise to the observed value. This observed error in measurements is assumed to be independent and is set to be proportional to the observed values, following a Gaussian distribution with predetermined variance. In this study, we assume that the standard deviation of the observational error is 5% of streamflow observations (i.e., noise) at each time step, similar to prior studies [Clark *et al.*, 2008; DeChant and Moradkhani, 2012; Fan *et al.*, 2016; Bauser *et al.*, 2018]. Sensitivity analysis on the observation error are illustrated in Section S.1 of the Supplementary Material. Furthermore, overshooting or filter divergence problem in data assimilation happens when the ensemble size is small or the initial values of ensemble members are quite different from the true. To resolve this issue, we used a sufficiently large ensemble size and the posterior information of parameters to initialize the ensemble of EnKF.

2.2. New modeling framework

2.2.1. Obtaining prior and posterior parameter distributions of a deterministic model

The first preparation step of the modeling framework is to obtain the *prior* and *posterior* parameter distributions for a deterministic model. There could be various ways to handle this, but in this study the following assumptions and methodologies are specifically applied. We first assume that each of the parameters follows a uniform distribution within specified bounds – the prior parameter distributions are simply attained by utilizing prior-known information for the bounds in Table 2. In contrast, the posterior parameter distributions are fitted to the 500 behavior parameters of GLUE – the 500 NAM behavior

samples are identified as an optimal number from our previous study which has confirmed that more than the 500 parameter sets does not change the shape of the posterior distributions [Tran and Kim, 2019]. For consistency, this number will be also used for making the posterior distributions of PCE-I and PCE-II in Sec. 2.2.2.

The mathematical expression of this step is as follows. For the warm-up and calibration periods, a model $\mathcal{M}$ (NAM) can be simulated to attain behavioral runs with GLUE, i.e.,

$$[y_t^{ii} \ x_t^{ii}] = \mathcal{M}(x_{t-1}^{ii}, \mathbf{u}_t, \boldsymbol{\theta}^{ii}), \quad ii = 1, \dots, n_w; \ t = 1, \dots, t_c \quad (6)$$

where n_w is the number of model runs to obtain the n number of the behavioral set based on the likelihood scores estimated with the GLUE method [Tran and Kim, 2019]. Among the n_w random runs (referring to the light blue shaded region in Fig. 1) that are simulated by using parameter sets ($\boldsymbol{\theta}^{ii}$) sampled randomly from the prior (uniform) distributions, the only n behavior runs (referring to the light red shaded region in Fig. 1) are employed for making the posterior distributions.

Reducing the effects of uncertainty by initial conditions ($\mathbf{x}_0^{ii}$) is necessary for modeling. In this framework, a “warm-up” technique was employed to calibrate the deterministic model. Generally, a sufficient period of time (called the ‘warm-up’ period) can be set such that the influence of the initial condition is dissipated, and the warm-up is performed before entering the calibration period. This technique produces behavioral parameter sets much faster in GLUE, compared with cases that do not use the warm-up technique.

2.2.2. Building PCE with two types of experimental design

We propose two types of approaches for constructing the PCE model, depending on how the sample collections of the experimental design ($\mathcal{X}_t$) is composed. One approach is to build a PCE model (“PCE-I”) by collecting the training samples that are generated from the *prior* parameter distributions. The other approach is (“PCE-II”) uses samples that are formed by the *posterior* parameters distributions. The associated mathematical expression is

$$[y_t^{iii} \ x_t^{iii}] = \mathcal{M}(x_{t-1}^{iii}, u_t, \theta^{iii}), \quad iii = 1, \dots, N; \ t = 1, \dots, t_c \quad (7)$$

where the N_I set of $\mathcal{X}_t$ (i.e., $N = N_I$ for PCE-I) consists of model $\mathcal{M}$ simulation results calculated from parameters sampled from the prior distributions (correspond to N_I set sampled randomly from the results in the light blue shaded region over the calibration period in Fig. 1) [Sudret, 2008; Blatman and Sudret, 2010; Blatman and Sudret, 2011]. In contrast, the experimental design of the latter approach assumes that the N_{II} set of $\mathcal{X}_t$ (i.e., $N = N_{II}$ for PCE-II) are drawn from the more constrained, posterior parameter distributions (correspond to the light red shaded region over the calibration period in Fig. 1) [Tran and Kim, 2019]. All the samples were taken through LHS sampling [McKay et al., 1979].

The former approach can be implemented easily and therefore has been used more commonly in the literature [Sudret, 2008; Blatman and Sudret, 2010; Blatman and Sudret, 2011]. However, for past periods in which observations exist, the second approach using a well-calibrated set of parameters is beneficial in significantly reducing computational time [Tran and Kim, 2019]. It takes less time to build PCE in the second approach because less training samples (N_I is generally larger than N_{II}) are required when estimating coefficients. On the other hand, in the context of real-time forecasting when no observations have been attained, the latter approach might cause a problem. Specifically, PCE models built with a set of “good” posterior parameters sets obtained only for a certain historic period of time would

not necessarily demonstrate validity for unknown prediction periods. Evaluation of the applicability of the two approaches to real-time flood forecasting will be addressed in Section 4.

Once the PCE models were constructed, the same GLUE procedure is made to obtain the posterior parameter distributions of both PCE models:

$$[y_t^{ii} \ x_t^{ii}] = \mathcal{M}^{PCE}(\mathbf{x}_{t-1}^{ii}, \mathbf{u}_t, \boldsymbol{\theta}^{ii}), \quad ii = 1, \dots, n_w; \ t = 1, \dots, t_c \quad (8)$$

Note that the number n_w is different depending on **Model** = {NAM, PCE-I, PCE-II}.

2.2.3. Specifying model parameters for data assimilation

Determining initial conditions and parameter values before assimilating real-time observations over the forecasting period is a necessary step. The mathematical expression for preparing data assimilation (forecasting) is written as:

$$[y_t^i \ x_t^i] = \mathbf{Model}(\mathbf{x}_{t-1}^i, \mathbf{u}_t, \boldsymbol{\theta}^i), \quad i = 1, \dots, n; \ t = 1, \dots, t_c \quad (9)$$

where the initial ensemble of states ($\mathbf{x}_0^i$) is set to an arbitrary number (e.g., zero) at the beginning of simulation (i.e., $t = 0$) (Fig. 1). In terms of specifying the model parameters, two types of approach are proposed. First, similarly to most previous studies of data assimilation [Moradkhani *et al.*, 2005b; Vrugt *et al.*, 2005; Wang *et al.*, 2009; Gharamti *et al.*, 2013; Xie and Zhang, 2013; DeChant and Moradkhani, 2014; Davison *et al.*, 2017], the ensemble of parameters over the periods ($0 \leq t \leq t_c$) is assumed to follow a prior distribution. That is, the n number of parameter sets are sampled from uniform distributions with predefined bounded ranges (i.e., from the results in the light blue shaded region in Fig. 1). The values of parameters remain unchanged, while those of state vectors are continuously updated until the beginning of the forecasting period (i.e., $t = t_c$). This is hereafter named

“*Random*” set — referring to the use of random parameter sets for running **Model** of NAM, PCE-I, and PCE-II.

An alternative way to this *Random* specification method is enabled by taking the advantage of the ability to calibrate model parameters with observed data before the forecasting period. Specifically, this method uses the posterior results of GLUE behavioral runs (referring to the light red shaded region in Fig. 1), i.e., selected parameter sets for running **Model** — called “*Selected*” specification method. The selected parameter sets for **Model** remain unchanged over the warm-up and calibration periods as well. As with the former approach, the values of state vectors are initially set to be zero at $t = 0$ but are continuously updated until $t = t_c$. We expected to see the EnKF process converge much faster and the forecasting results improve.

2.2.4. Modeling approaches for forecasting

In total, 18 modeling approaches (see Fig. 2) were developed by combining the modeling options with various techniques (NAM + PCE + GLUE + EnKF) in Sections 2.2.2 and 2.2.3. The modeling techniques were coupled to successfully perform ensemble flood forecasting and to meet the need for accurate and efficient flood forecasting. The 18 approaches represent permutations of the $3 \times 2 \times 3$ subcases (Table 3). First, they were divided into three subcases corresponding to **Model**, depending on whether a deterministic model or a PCE model was used over the calibration period (see Sec. 2.2.2) and how the latter was developed. Second, these modeling sets were divided into two subcases corresponding to *Random* or *Selected* sets, depending on how the parameter sets before the forecasting period were specified (see Section 2.2.3). Lastly, they were divided into three subcases depending on the methodology of data assimilation. The first of the three subcases did not use any data assimilation, and the other two used single- and dual-ensemble Kalman

filters (see Sec. 2.1.4). We evaluated the modeling performance of the coupling framework by assessing accuracy, efficiency, and predictability in Sec. 4.2. The performance comparisons of the 18 approaches are expected to be a guide to which approach demonstrates better skill and most appropriate and which should be avoided.

2.3. Performance metrics

To assess the modeling performance of the 18 approaches, metrics representing accuracy, predictability, and efficiency were chosen, beginning with the accuracy metrics of Nash–Sutcliffe efficiency (*NSE*), absolute error (*AE*), and relative entropy (*RE*) [Kullback and Leibler, 1951; Kullback, 1997; Kleeman, 2002]. Second, Brier scores (*BS*) [Brier, 1950], and the range of uncertainty (*UR*) were used to assess the predictability of probabilistic forecasts. Lastly, a metric calculating total runtime (*TRT*) was evaluated to compare the computational efficiency of the tested approaches.

NSE, which is traditionally used to evaluate the accuracy power of deterministic models, is computed for each ensemble member (*i*) over the entire computation time. In this study, *NSE* is expressed as:

$$NSE^i = 1 - \frac{\sum_{t=1}^T (y_t^{obs} - y_t^i)^2}{\sum_{t=1}^T (y_t^{obs} - y_{mean}^i)^2}, \quad i = 1, \dots, n \quad (10)$$

where y_t^{obs} and y_t^i are the actual observation and *i*-th predicted output at time *t*; y_{mean}^i is the mean of the *i*-th predicted output over the entire forecasting period; *T* is the total number of time steps over the forecasting period from t_c to t_f .

Absolute error (*AE*) is differences between actual observations and predictions of each ensemble members at each time *t*. Thus, it varies with time and can be written as:

$$AE_t^i = |y_t^{Obs} - y_t^i|, \quad t = 1, \dots, T; i = 1, \dots, n \quad (11)$$

Relative entropy (*RE*) is a measure of the statistical difference between probability distributions over the entire forecasting period of observations and model simulations [Kleeman, 2002; Shukla et al., 2006; Giannakis and Majda, 2012]. Following Kleeman [2002] and Heo et al. [2014], *RE* can be defined as:

$$RE^i = \left[\log \frac{\sigma_{y^{Obs}}^2}{\sigma_{y^i}^2} + \frac{\sigma_{y^i}^2}{\sigma_{y^{Obs}}^2} - 1 \right] + \left[\frac{(\mu_{y^i} - \mu_{y^{Obs}})^2}{\sigma_{y^{Obs}}^2} \right], \quad i = 1, \dots, n \quad (12)$$

where $\mu_{y^{Obs}}$ and μ_{y^i} are the mean, while $\sigma_{y^{Obs}}$ and σ_{y^i} are the variance of streamflow observation and the *i*-th model prediction over the entire computation time from t_c to t_f .

Small values of relative entropy indicate that distribution of a given model is close to that of the observation. This is also called Kullback-Leibler divergence between the two distributions, model and data, assuming Gaussianity of both.

The Brier score (*BS*) is one of the most commonly used verification measures for assessing the predictability of probabilistic forecasts. The score is defined as the mean squared error of the probabilistic forecasts over the verification sample, expressed as:

$$BS = \frac{1}{T} \sum_{t=1}^T (p_t^f - o_t)^2 \quad (13)$$

where p_t^f is the forecast probability for the *t*-th time, which refers to the ratio among ensemble reaching a predefined flow threshold; o_t is the observed probability, which is 1 if observation at *t*-th time, y_t^{Obs} is larger than the threshold, and 0 if it is not. In this study, this threshold value was chosen as the proportional rate of 90% of the true discharge peak.

The uncertainty range (UR) is the range between the 5th and 95th percentiles of the ensemble outcomes (q). It is computed over each computational time t in hydrographs, expressed in Eq. 14:

$$UR_t = q_t^{95} - q_t^5, \quad t = 1, \dots, T \quad (14)$$

Lastly, the total run time (TRT) for all of the approaches is defined as:

$$TRT = (RT_{w+c,Model} \times fac_{Model} + RT_{f,Model,DA}) \times n + RT_{build,Model} \quad (15)$$

where $RT_{w+c,Model}$ is the run time to compute one simulation of **Model** (NAM, PCE-I, and PCE-II) over the warm-up and calibration periods, i.e., from 0 to t_c ; $RT_{f,Model,DA}$ is the run time to compute one simulation of **Model** with different DA methods over the forecasting period, i.e., from t_c to t_f ; and $RT_{build,Model}$ is the run time needed for building **Model**. For example, because it is unnecessary for constructing the deterministic model, the time for NAM is zero. The building run times for PCE-I and PCE-II will be calculated in detail in Sec. 4.1.2. The factor fac_{Model} represents the number of **Model** runs to obtain a single behavior run in GLUE, and remains 1 in A1 to A9, while it depends on **Model** for the rest of approaches.

Eq. 15 is a linear function with respect to the number of ensembles run, in which $RT_{w+c,Model} \times fac_{Model} + RT_{f,Model,DA}$ serves as the slope of the linear function and $RT_{build,Model}$ the intercept. The values of the slope and intercept and the executed times of the 18 approaches are addressed in Section 4.2.

3. Study Area and Experimental Setups

In this study, the unified framework is applied to predict hourly streamflow in the Vu Gia watershed as shown in Fig. 3. The watershed is one of the largest in central Vietnam,

with a total area of 1,679.8 km² in the tropical region. It experiences a typical continental monsoon climate, with concentrated rainfall mainly from September to December. As the Vu Gia watershed is characterized by a large difference in elevation (slopes of approximately 30 %), floods occur rapidly and frequently. The region has experienced intense severe flooding and significant damage [UNDP, 1999; Nga *et al.*, 2015].

Streamflow data used for the outlet of the basin was collected hourly at Thanh My station – the only hydrometric station in the domain. Rainfall data was also observed hourly and obtained from two weather stations near the study area (Thanh My and Kham Duc station). The average rainfall over the basin (Fig. 4) was calculated through the Thiessen polygon method. Observations from Dec. 1 to 17, 2016, are employed, in which the data from Dec. 1 to 13 was used for the warm-up period (i.e., from 0 to t_w), the data from Dec. 13 to 15 for the calibration period (i.e., from t_w to t_c), and the remaining data (assuming numerically that this data was newly provided at an hourly basis) corresponds to the forecasting period (i.e., from t_c to t_f) (Fig. 4). The effects of the length of warm-up period are illustrated in Supplementary Material. Note that rainfall forecasts has not been considered in this experimental design, what is done is hindcasting but one refers to the period between t_c and t_f as the “forecasting period”, allowing for replicating real-life operational flood-forecasting process. Also note that a source of uncertainty for rainfall forecasts has not been presented, but it could have been addressed in Eq. 2 that has the flexibility to include *ensemble* precipitation inputs ($\mathbf{u}_t$).

Determining the size of ensemble for forecasting (n) is related to quantifying the uncertainty bounds and representing the EnKF. In previous studies, the ensemble size was selected randomly or large enough (at least 100 members) to fully identify the uncertainty confidence intervals [Cameron *et al.*, 2000; Beven and Freer, 2001; Hossain and

Anagnostou, 2005; Choi and Beven, 2007; Blasone et al., 2008; Jin et al., 2010; Shen et al., 2012]. A sufficient number of ensemble parameter sets to achieve both goals of efficiency and uncertainty quantification should be determined. Following our previous study [*Tran and Kim, 2019*], we used an n of 500 as the optimal size of the ensemble.

4. Results

4.1. Preparation steps before forecasting

4.1.1. Attaining parameter posterior distributions

The posterior distributions of parameters can be generally attained by using Bayesian inference. As detailed in Section 2.1.3, we employed a relatively simple and robust method, GLUE [*Beven and Binley, 1992*], that does not require reformulation of the deterministic model code. Details on why we choose the likelihood functions of NSE , PE , and VE (presented in Appendix B), how we determine the cutoff threshold values of each function, and which parameters are more sensitive, are described in *Tran and Kim [2019]*. We confirmed the benefits of a warm-up technique that significantly speeds up the GLUE process of finding the behavioral sets: without warm-up, no behavioral set was obtained from GLUE even after a sufficiently large number of NAM model runs, while with warm-up, a behavioral set was obtained after approximately 118.0 model runs for NAM (A10 to A12), 26.9 for PCE-I (A13 to A15), and 3.6 for PCE-II (A16 to A18), respectively. Therefore, the factors, fac_{Model} are 118.0, 26.9, and 3.6 for NAM, PCE-I, and PCE-II, respectively in A10 to A18.

4.1.2. Constructing the PCE models

Determining the coefficients of the PCE-I and PCE-II models depends on the number of the experimental design (N) and the polynomial degree (p) [*Blatman and Sudret, 2010; Blatman and Sudret, 2011*]. To discover appropriate values for N and p , the effect of

experimental design N on PCE performance was first evaluated. Specifically, a number of simulations were repeated with the N value varied between 10 and 5,000 but the value of p was set as 3, and the performance results of LOO for streamflow (y) and the five model states (Table 2) computed. Fig. 5 shows that the LOO values for streamflow and five state variables become smaller as the value of N increases, and ceases to become smaller when N approaches a certain value. For N values larger than this threshold, the model performance was almost indistinguishable (the left column plots in Fig. 5). From a visual inspection of Fig. 5, the optimal N value for constructing the PCE-I and PCE-II models would be 1,000 and 100, respectively.

A selection of the polynomial degree p was made in a fashion similar to the aforementioned procedure. The value of p was varied from 1 to 6 and N was set as 1,000 (PCE-I) and 100 (PCE-II). From the results of Fig. 5 (the right column), the gradients of the LOO metrics assessed changed considerably when p was set to 3 and the values remained stable for large magnitudes of p . In terms of reducing the computational time to construct a PCE model, a low polynomial degree would be preferred. Thus, a p of 3 would be an appropriate value to use when building both PCE models. With optimal values of N of 1,000 and 100, and a p of 3, PCE-I and PCE-II models can be built to quantify the uncertainty range for flow prediction and to compare the degree of accuracy and efficiency with the results of the deterministic NAM.

The total time to establish both PCE models is described (further details are in *Tran and Kim [2019]*). Obviously, the larger the number of the experimental design set, the more time is needed for computing N ensemble runs. The time required to perform the N_I and N_{II} ensemble runs of NAM was 121.9 and 12.6 seconds for PCE-I and PCE-II, respectively. It also takes much more time to estimate PCE-I coefficients if one uses an ensemble set (N_I)

generated from the prior distribution of the parameters than to compute PCE-II coefficients from parameter sets informed by the likelihood function. The time required to estimate PCE coefficients was 419.3 and 11.3 seconds, respectively. The summation of these two times was considered to be the total time required to build the PCE models before forecasting: approximately 541.2 and 23.9 seconds for PCE-I and PCE-II, respectively. The construction time of PCE-II is much (~ 22 times) faster than that of PCE-I.

4.1.3. Comparing the ensemble results of NAM and PCE models

Over the calibration period, ensemble results composed of 500 *Random* and *Selected* runs were compared for three different models. To make the 500 *Selected* behavioral results, 58,977, 13,444, and 1,822 (n_w) random runs were required for NAM, PCE-I, and PCE-II, respectively. Compared with the NAM itself, using PCE models can reduce the amount of computational runs by a factor of about 4.4 for PCE-I and 32.4 times for PCE-II model. The composing behavioral set for PCE-II was even faster (~ 7.4 times) than for PCE-I.

Fig. 6 shows hydrographs for the 500 *Random* (A1 to A9) and *Selected* (A10 to A18) simulations for the three models. Their uncertainties are illustrated with a 90% confidence interval, which corresponds to 5 and 95% quantiles of the 500 ensemble members. Because we controlled the conditions for the behavioral set of GLUE, the overall comparison with the observed values for the results of the *Selected* cases (A10 to A18) is very satisfactory. Specifically, the *NSE* value was always higher than 0.9 and both *PE* and *VE* values were less than 5% for all cases. However, streamflow curves for the *Random* simulations (A1 to A9) clearly show different patterns depending on the model. It can be anticipated that the results of these *Random* cases will not be encouraging and their uncertainties will be large. However, the results of some cases using PCE-II model were very satisfactory and their uncertainties small.

As mentioned above, when making using observations to constrain the parameter sets (A10 to A18), the results of both PCE models are similar to those of the NAM and no substantial differences were observed. This confirmed that both PCE models have an equivalent degree of accuracy as the NAM and can provide an excellent match to the deterministic model. In terms of efficiency, it is also advantageous to use the PCE model (discussed in Sections 4.2.1 and 5.1), and there is no reason to hesitate adopting the PCE model for streamflow prediction.

4.2. Flood forecasting with 18 approaches

For past periods when observations for calibration were collected, all models performed well. We then tested the forecasting performance of the three models using the permutation that resulted in 18 approaches in Table 3. Results of the real-time flood forecasting for these approaches are shown in Fig. 7 and 8, in which the 500 ensemble results are illustrated with a 90% confidence interval at each time step. The verification metrics for the simulations, specifically *NSE*, *AE*, *RE*, *BS*, and *UR*, and the peak values of hydrographs are compared in Fig. 9 and Fig. 11. Lastly, the total run time with respect to the ensemble size was computed for the 18 approaches in Fig. 10. In this section, we analyze the results and draw conclusions from the following four perspectives: (i) the applicability of PCE-I and PCE-II models for real-time flood forecasting, (ii) the impact of estimating appropriate parameter conditions for forecasting, (iii) the effect of using EnKF and dual EnKF, and (iv) the degree of improving efficiency performance among the approaches.

4.2.1. PCE-I versus PCE-II model for real-time flood forecasting

Depending on the model used in forward simulations (NAM, PCE-I, and PCE-II), the results for the 18 approaches were divided into three groups. Almost all of the results of the six approaches using the PCE-II model were worse than those obtained with both NAM and

PCE-I (Figs. 7 and 8). The only exception is for the A1 and A4, which did not have assimilation and whose parameter sets used were based on prior uniform distributions. No verification metrics computed using the results of forecasting based on PCE-II were satisfactory, except for the metric of $\overline{UR}$. However, if the accuracy is not ensured, the better performance in terms of $\overline{UR}$ is not meaningful. Specifically, NSE values were low, approximately 0.7; AE values at flood peak time (AE_{peak}) were larger than 750 m³/s; RE was approximately 0.01; and BS was equal to 1 (Fig. 9). No metric improvements was found for the approaches based on PCE-II, even if combinations of assimilation and calibration techniques were applied. We concluded that the PCE-II model can reproduce streamflow characteristics well for the past period, but not for the future.

Conversely, the forecasting results of the approaches based on the PCE-I model are almost similar to those obtained with NAM, and in some cases even better. The latter can be seen in Fig. 9; the verification metrics of NSE , AE_{peak} , RE , and $\overline{UR}$ show better performance for PCE-I than for NAM results (e.g., A5 vs. A2, A6 vs. A3, A14 vs. A11, and A15 vs. A12) (see Table 4). In particular, the RE results in Fig. 9c illustrate that the PCE-I results are closer to the observed values than those obtained with NAM (A15 is the best result with the smallest value of RE). BS corresponding to PCE-I also has smaller values, close to zero, which indicates instances of when predictability of probabilistic forecasts matched predictability of observation (Fig. 9d). Therefore, the PCE-I model can be adapted to substitute the NAM in performing real-time flood forecasting, as well as in capturing the uncertainty of calibration period.

Comparing the modeling results in terms of the computation speed, it is clear that simulating a surrogate model using the PCE theory is significantly faster than with a deterministic model such as NAM. The “slopes” of the runtime curves of Fig. 10 indicate

both PCE approaches are approximately 20 times faster (A4 to A9) and ~80 times faster (A13 to A18) than the corresponding approaches using the NAM. Similarly, if we compare efficiency between PCE model approaches, using PCE-II may or may not offer much improvement in efficiency over PCE-I. There is only 10 % improvement when *Random* specification is applied (see the slope of A4, A5, A6 vs. A7, A8, A9 in Fig. 10), while there is about six times improvement when simulating *Selected* approaches (see the slope of A13, A14, A15 vs. A16, A17, A18). The use of surrogate models therefore did not sacrifice accuracy. The flood prediction accuracy of PCE-I model presented here is similar to that of the original NAM, and computational efficiency has been found to be highly superior.

4.2.2. Random versus Selected specification for forecasting

The approaches using the *Selected* specification generally show a better performance than those using the *Random* specification. This is especially noticeable in the NAM and PCE-I approaches, and rarely in PCE-II. First, in the approaches without data assimilation, their accuracy was significantly improved (compare A1 vs. A10 and A4 vs. A13). The performance of A10, represented by the NSE , AE_{peak} , RE , and $\overline{UR}$ metrics, was improved by about 95, 73, 61, and 89% compared with A1, and the performance of A13 about 86, 72, 79, and 92% over A5, respectively. Despite the noticeable improvement of A10 and A13, these results were still not ideal. The large AE error at the peak of A10 and A13 was approximately 450 m³/s less than the observation, and the BS value was close to 1 (Fig. 9, Table 4). On the other hand, in the approaches in which data assimilation was used, the improvement effect for *Selected* specification was not greater than when it was not used. The increasing performance for the same metrics was about 55, 22, 36, and 56% (A2 vs. A11), and about 56, 52, 44, and 49% (A3 vs. A12). Here, the parameter specification effect was smaller because DA improves the absolute error magnitude.

Determination of states and parameters that can increase accuracy and predictability requires more computation time because a large number of model runs are carried out to make an inference for posterior distributions. For approaches using NAM (A1 vs. A10, A2 vs. A11, and A3 vs. A12), it took 56, 41, and 30 times longer; while for PCE-I (A4 vs. A13, A5 vs. A14, and A6 vs. A15), it took 13, 10, and 8 times, respectively (Fig. 10). Because of this computational burden, parameter inference can be a weakness for real-time flood forecasts where it is important to ensure sufficient time ahead. However, if the surrogate model is employed, the necessary repetition of estimating the posterior distribution can be performed quickly, and such a weakness can be overcome.

4.2.3. Single versus dual EnKF in real-time flood forecasting

Convincing evidence is presented that both single and dual EnKF can improve accuracy and predictability during real-time forecasting (with the exception of approaches using PCE-II). Both of these techniques perform well but the dual EnKF is the superior choice. As an example of the approaches using NAM, the three metrics of AE_{peak} , BS , and $\overline{UR}$ in the *Random* cases provided slightly better results: 515.64 vs. 500.45, 0.75 vs. 0.66, and 367.34 vs. 340.12, respectively (A2 vs. A3). But, in the *Selected* cases, there was a relatively large performance improvement for the two metrics of AE_{peak} and BS : 401.26 vs. 242.62 and 0.78 vs. 0.24 (A11 vs. A12). Similar trends were observed when using PCE-I, and the difference is remarkable, especially for the AE_{peak} metric (e.g., about 2.5 times for A5 vs. A6).

From the overall inspection, it can be determined that the dual EnKF can adjust the peak of a hydrograph more accurately, and give a more confident result with a smaller uncertainty range. Therefore, we compared the distribution of flood peak values for 500 ensemble members in Fig. 11. This figure confirms that the joint update of states and

parameters improves accuracy at flood peak more effectively than a single update of states. Also for the joint update, the expected value of the distribution was closer to the peak observation, and its variability is smaller (a narrower distribution).

Because the updating process is made twice, the dual EnKF is computationally more expensive. The computation time it takes to update states and parameters increased almost linearly. That is, the calculation time doubled or tripled for the cases of single and dual EnKF (using *Random* specification), respectively, as compared to the case without assimilations. However, for the approaches using the *Selected* specification, the calculation time did not seem to change significantly (Fig. 10), not because the time required for Kalman filtering was reduced, but because the time required for the parameter inference was so large that the filtering effect was masked.

5. Discussion

5.1. How can PCE be constructed for flood forecasting?

From the simulated flood forecasting results presented in Section 4.2, it is apparent that the manner of PCE construction has a significant impact on forecasting. The biggest difference in building PCE-I and PCE-II involves setting the range of the training sample (called experimental design). It is not surprising that a surrogate model trained for an event provides acceptable results only for the event trained. The flexibility to generalize to well-behaved outcomes for another event (e.g., a future event) is relatively low. This is why the calibrated model is often not appropriate for future forecasting. On the other hand, if a surrogate model can mimic the behavior of the original model to the greatest extent possible in a wide variety of situations and conditions, it will be able to capture its characteristics more comprehensively, thus playing a sufficient role in forecasting future events. Here we provide evidence the PCE-I model behaves like the NAM for the forecasting period, while

the PCE-II behaves differently (despite both models behaving properly for the calibration period). To examine the robustness of both PCE model results, the Sobol' method (detailed in Appendix D) was used to implement the variance-based measures of parameter sensitivities [Sobol', 2001], which is commonly used as a global sensitivity analysis technique to determine the key parameters in the model [Wang *et al.*, 2018].

First, the PCE-I posterior histograms of the nine parameters obtained from GLUE for the calibration period are similar to those of the NAM, except for Lm and TG (Fig. 12). For these two parameters, a posterior histogram difference is a minor issue because the choice of the parameter values does not affect the end result, i.e., the sensitivity of the parameters is low. Other parameters of CQOF (1st) and CK12 (2nd) are the two most influential parameters to the model results, that is, their sensitivities are high. This result is consistent for both NAM and PCE-I (Fig. 13). The slight difference between the results of PCE-I and NAM, observed from the investigation of the sensitivity and the posterior distribution, is because we chose an appropriate number of training samples when constructing the PCE-I model. If one greatly increases the number of training sets, the difference in the above results will essentially disappear.

Second, the failure of PCE-II to mimic the NAM for the forecasting period can be explained largely due to the fact that PCE-II was trained using the only 100 behavioral parameter sets that were optimized for the calibration event. Model results will only vary within the boundaries that its trained data understand, and it will not be able to simulate the behavior of another event with a high skill, i.e., model “overfitting” occurs. However, over the calibration period, PCE-II always shows a good predictive performance for almost all parameter sets (compare the hydrographs of A1 to A3 with A7 to A9 in Fig. 6). In other words, no matter what parameter one chooses, satisfactory results are always achieved, which indicates that the influence of parameters is excluded. The posterior histograms of parameters

for PCE-II (Fig. 12c) are almost uniform, except for the parameter of CQOF, which is the only one that can affect the end result, especially maintain the accuracy of the flood peak (note that the sensitivity of this parameter for PE is unusually high in Fig. 13c). If we change the threshold value of the likelihood function corresponding to the flood peak chosen to make the behavior set a slightly less constrained, this parameter will no longer play a role in constraining the result and follow a uniform distribution as well.

Another interesting aspect of the sensitivity test is that the sensitivity results of PCE-II differ from those of NAM and PCE-I, but are similar to those of NAM-II. The sensitivities of parameters have been altered in PCE-II. The NAM-II in Fig. 13d is hypothetically introduced to mimic the situations of PCE-II. Specifically, it refers to the sensitivity results when the NAM model was tested based on the posterior distributions (which are also used to select the training parameter set for building PCE-II), not the prior distributions of the parameters.

5.2. Is it feasible to construct a time-invariant PCE model?

A long-lasting challenge in hydrologic modeling is how to estimate parameters or state vectors optimized for all external and internal conditions. This would not be an issue for estimating previously described variables if the amount of data for calibration was sufficient. However, in the case of future forecasts during which no observation for calibration is available, it poses a problem. To tackle this challenging problem, *Fan et al.* [2016] and *Wang et al.* [2017] adopted a modeling framework in Eq. 1, so that PCE models should be reconstructed continuously at every time step. This method is flawless in theory, but requires additional computational resources (see efficiency comparisons in Supplementary Material). That is, the time to configure the PCE at every time step must be added to the total model simulation time, i.e., making the slope of Fig. 10 steeper. This disadvantage can be more

pronounced when constructing surrogate models for complex, process-based deterministic models.

Unlike previous efforts, this study adopted an alternative modeling framework such as Eq. 2; that is, the PCE model is time invariant and thus developed only once over the calibration period. Therefore, during real-time forecasting, the total run time consists only of computational intervals needed for data assimilation of all ensemble members. This enhances computational efficiency significantly (see efficiency comparisons in Supplementary Material). This framework is not perfect, but the potential error that can occur by using the time-independent PCE model is minimized by coupling the data assimilation technique, thus complementing accuracy. From a comparison of the results of 18 approaches, we confirmed that the modeling framework needed for building a PCE model (especially PCE-I) is feasible. This embraces the notion that the PCE construction does not require information for future conditions but can be made with historically available data available prior to the forecasting period.

5.3. Do surrogate and specification sacrifice efficiency?

Our results indicate that a sophisticated combination of three independent techniques (i.e., surrogate modeling, parameter inference, and data assimilation) supplies superior predictive performance for real-time ensemble flood forecasting. The combination of many methods however leads to an essential reduction in efficiency. Because data assimilation has been shown to be necessary, we must accept efficiency deterioration. However, for surrogate modeling and parameter specification, it remains to be determined whether the additional time required by the technique combination leads to efficiency deterioration. First, for construction of the surrogate model, particularly PCE-I, the efficiency issue may not be relevant because the task does not require any observations for calibration and can be

completed before the flooding season. In contrast, obtaining an ensemble of parameter sets from posterior distributions should be carried out immediately prior to the flood forecasting period, when observations are necessary. Therefore, it may take an appreciable time for completing this task, and method efficiency may be affected.

5.4. What are the differences between PCE and data-driven models?

Both PCE and data-driven models can provide satisfactory results for short-term forecast, but key differences between them exist. (1) PCE has a functionality of including model parameters and states as an input vector – this enables formal uncertainty quantification and model sensitivity analysis; (2) hydrologic/hydraulic model state variables (and parameters) are theoretically observable and in the case of process-based models have their own physical meaning, making it easier to physically interpret the results of PCE; (3) while purely data-driven methods are trained with observations, PCE is trained through high-fidelity samples supervised by physical relations, thus requiring fewer data samples for training; (4) data-driven models often have assumptions about the distributions governing variability of their outputs, and therefore this can lead to non-physical results (e.g., negative outputs quantifying mass, streamflow, etc.) and fail to display non-normal, bi-modal, or other complex behaviors.

5.5. Can modeling framework be applied to high-dimensional problems?

While the implementation and analysis of experiments is valid for the presented scope of the experimental design, one needs to proceed with care when extending this approach to more complex models. The most fundamental concern that remains is whether the proposed framework can be applied to high-dimensional problems in which fully distributed models are used. The dimension of a distributed model can be defined as the product of the number of grids cells and the number of parameters (and states). The dimension order of any truly

physical models is therefore large, and extending our framework directly to such a model is not straightforward – known as the “curse of dimensionality” [Caflisch, 1998; Davis and Rabinowitz, 2007; Sudret, 2007]. By examining how each of the methods mentioned in the framework resolves the problem of reducing dimensions efficiently and to what extent it has been applied, the feasibility of applying the proposed framework can be estimated.

Regarding the surrogate modelling (PCE), techniques such as Bayesian compressive sensing [Sargsyan *et al.*, 2014] and sparse regression [Blatman and Sudret, 2008; Blatman and Sudret, 2010] proved capability and efficiency in many prior studies using complex models with high dimensions, up to 80 dimension [Sargsyan *et al.*, 2014]. However, these studies avoided the calculation of fully distributed problems by assuming the spatial variability of parameters to be homogeneous. Second, for the parameter specification, any optimization technique applied to high-dimensional problems could be relevant. For example, one of the large scale optimization algorithms, the competitive swarm optimizer (CSO) [Cheng and Jin, 2015] was employed up to the dimension of 5,000. These algorithms have been successfully optimized for problems of very large scale, but their optimizations have been applied to simple analytical functions rather than (hydrologic or meteorological) models. To our knowledge, the number of dimensions has not yet been high in problems of hydrologic optimization, in which the dimension order is almost identical to the number of parameters. The spatial variability of parameters is not fully addressed in most studies, although a “multiplier” concept [Pokhrel *et al.*, 2008]. Last, EnKF is made possible in problems of higher dimensionality through covariance localization. It is mainly applied in meteorological models with many parameters, and the number of dimensions can be up to the order of millions, e.g., 2,592,000 [Fujita *et al.*, 2007]. The localization technique was able to reduce the dimensions efficiently.

6. Conclusions

This study presents a new robust, accurate, and efficient modeling framework that consists of the novel integration of three individual techniques: surrogate modeling, parameter inference, and data assimilation. This unified framework is suited for ensemble flood forecasts quantifying prediction uncertainty. The strengths of each technique are (i) the use of PCE offers significant computational savings; (ii) the inference of parameters before data assimilation allows for faster convergence, smaller uncertainties, and greater accuracy of the end results; and (iii) the Kalman filters assimilate errors that occur in real-time flood forecasting. Based on the results of the 18 refined approaches according to the permutations of the above methods, the following conclusions can be drawn:

- Of the two methods for PCE construction, only PCE-I (constructed based on prior, uniform distributions) is acceptable for forecasting, although both methods reproduce observations of the calibration period well. Note that PCE-II (constructed based on posterior distributions) does not provide satisfactory results, even when coupled with other inference and assimilation techniques. The results obtained from PCE-I are similar, and in some cases even superior to those based on the original deterministic NAM model. The PCE used is a single model constructed before the forecast period and thus does not change over time — this is a unique feature different from previous studies in which PCE was rebuilt at each calibration or forecasting time step.
- Especially for short-range forecasting, model parameter input and state initialization plays a crucial role. In some previous studies, posterior distributions were employed to derive a parameter ensemble before forecasting, but the effect of such parameter specification was not quantified for the data assimilation. *Selected* parameter specification (made through the GLUE framework in this study) offers improved accuracy and predictability of forecast outcomes over the *Random* parameter

specification. However, it is less computationally efficient, and the issue is expected to be especially problematic when using complex deterministic models.

- The usefulness of single and dual EnKFs is demonstrated through comparisons of the 18 approaches. Both techniques have excellent overall performance, but the dual EnKF showed a slightly better performance than the single EnKF. There was a remarkable improvement in reproducing the hydrograph peak values (Table 4). In the absence of assimilation, the *Selected* approach offers superior results and if it cannot be used, data assimilation must be applied.
- The computational time discussed in this study consists of three principal components: surrogate building time, parameter inference time, and data assimilation time. Our conclusions may marginally vary depending on the particular model used and the region in which it is applied, but here the efficiency improvement from using the surrogate modeling technique overwhelms any efficiency deterioration derived from the other two components. That is, the use of the metamodel makes it possible to effectively address computational efficiency. This feasibility is maximized when many ensemble outcomes are needed and when complex, physically-based models should be simulated.
- From the comprehensive analyses presented above, A15 is our first choice and A14 is the second. When only a deterministic model is used, we recommend A12 (or A11). Using the unified framework developed here, real-time and ensemble flood forecasting are promising directions, allowing for satisfactory measures of accuracy, predictability, and efficiency. Ultimately, the framework developed in this study contributes to a shift in modeling paradigm arguing that complex, high-fidelity, physical hydrologic and hydraulic models should be increasingly adopted for real-time and ensemble flood forecasting

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Appendix A. The construction of PCE surrogate model

A.1. The determination of PCE coefficients

The least-square regression method is employed to establish the PCE coefficients:

$$\varepsilon = \operatorname{argmin}_{\varepsilon \in \mathbb{R}^{|A|}} \mathbb{E} \left[\left(Y_t - \sum_{\alpha \in A} \varepsilon_{\alpha} \Psi_{\alpha}(X_t) \right)^2 \right] \quad (\text{A.1})$$

where $\mathbf{X}_t = \{\mathbf{x}_t^{(1)}, \dots, \mathbf{x}_t^{(N)}\}$ consists of N sets of input variables $\mathbf{X}_t$ (the set $\mathbf{X}_t$ is called the *experimental design*), and $\mathbf{y}_t = \{\mathcal{M}(\mathbf{x}_t^{(1)}), \dots, \mathcal{M}(\mathbf{x}_t^{(N)})\}$ be the corresponding model

evaluations $\{y_t^{(k)} = \mathcal{M}(x_t^{(k)}), k = 1, \dots, N\}$. The estimates of the PCE coefficients are thus given by:

$$\hat{\varepsilon} = \operatorname{argmin}_{\varepsilon \in \mathbb{R}^{|A|}} \frac{1}{N} \sum_{k=1}^N \left(y_t^{(k)} - \sum_{\alpha \in A} \varepsilon_{\alpha} \Psi_{\alpha}(x_t^{(k)}) \right)^2 \quad (\text{A.2})$$

which is equivalent to:

$$\hat{\varepsilon} = (\mathbf{F}^T \mathbf{F})^{-1} \mathbf{F}^T \mathbf{y}_t \quad (\text{A.3})$$

where $\mathbf{F}$ is so-called the *information matrix* of size $N \times |A|$ whose elements are defined as

$$\mathbf{F}_{k,l} = \Psi_l(x_t^{(k)}) \quad k = 1, \dots, N; l = 0, \dots, \operatorname{card} A - 1 \quad (\text{A.4})$$

Once a PCE model is derived, the prediction using the model is extremely simple and straightforward: Input the values of model input to Eq. 2 and then obtain the values of model response $\mathbf{Y}_t$.

A.2. PCE error estimates

The leave-one-out cross-validation error (*LOO*) was designed to overcome the over-fitting limitation of normalized empirical error by using cross-validation [Blatman and Sudret, 2010]. In this study, after the number of sets $\mathbf{x}_t$ is defined, the *LOO* is used to determine the polynomial degree. The leave-one-out cross-validation error can be written as:

$$LOO = \frac{1}{N} \sum_{k=1}^N \left(\frac{\mathcal{M}(x_t^{(k)}) - \mathcal{M}^{PCE}(x_t^{(k)})}{1 - h_k} \right)^2 \quad (\text{A.5})$$

where h_k is the k -th diagonal term of the matrix $\mathbf{F}(\mathbf{F}^T \mathbf{F})^{-1} \mathbf{F}^T$.

Several software tools are currently available for research purposes to carry a range of UQ tasks, including PCE regression, e.g., the MIT Uncertainty Quantification Library [Parno *et al.*], the Uncertainty Quantification Toolkit [Debusschere *et al.*, 2016], Dakota [Eldred *et al.*, 2010], Chaospy [Feinberg and Langtangen, 2015], and the UQLab [Marelli and Sudret, 2017]. The latter libraries are used in this study.

Appendix B. Likelihood functions used in GLUE

Nash–Sutcliffe efficiency (NSE , [-]):

$$NSE^i = 1 - \frac{\sum_{t=1}^T (y_t^{Obs} - y_t^i)^2}{\sum_{t=1}^T (y_t^{Obs} - y_{mean}^i)^2}, \quad i = 1, \dots, n \quad (B.1)$$

Peak error (PE , [%]):

$$PE^i = \frac{|y_{max}^{Obs} - y_{max}^i|}{y_{max}^{Obs}} \times 100, \quad i = 1, \dots, n \quad (B.2)$$

Volume error (VE , [%]):

$$VE^i = \frac{|V^{Obs} - V^i|}{V^{Obs}} \times 100, \quad i = 1, \dots, n \quad (B.3)$$

where V is the total volume of hydrograph.

Appendix C. Ensemble Kalman filter (EnKF)

C.1. States updated

An ensemble of state vector, $\mathbf{x}$ consisting of n by M_S is propagated through **Model** of both deterministic model and PCE models, such that each state vector represents one realization of the model states. Then, the state forecast is made for each ensemble member as follows (forecast step):

$$\mathbf{x}_t^{i-} = f(\mathbf{x}_{t-1}^{i+}, \mathbf{u}_t, \boldsymbol{\theta}^i) + \mathbf{w}_t^i, \quad i = 1, \dots, n \quad (\text{C.1})$$

where $\mathbf{x}_t^{i-}$ is the i -th forecasted states vector at time t , $\mathbf{x}_{t-1}^{i+}$ is the i -th updated states vector at time $t - 1$, M_S is the number of model states $\mathbf{x} = \{x_j, j = 1, \dots, M_S\}$, and n is the number of ensemble members. The nonlinear propagator $f(\cdot)$ contains M_I model input vector $\mathbf{u}_t, \{u_{1,t}, \dots, u_{M_I,t}\}$ and the i -th model parameter vector $\boldsymbol{\theta}^i$ corresponding to the model state $\mathbf{x}_{t-1}^{i+}$. The term $\mathbf{w}_t^i$ is the i -th model error and presents all uncertainty related to model structure, forcing data and model parameter [Moradkhani *et al.*, 2005b]. In this study, the model error is represented by the uncertainty of model parameters.

Suppose that the actual observation (y_{t+1}^{obs}) is taken at time $t + 1$ and that we intend to assimilate the vector of observations into the model. The predicted output of model, y_{t+1}^i at time $t + 1$ is computed with the propagator $h(\cdot)$ as a function of $\boldsymbol{\theta}^i$, $\mathbf{u}_{t+1}$, and $\mathbf{x}_t^{i-}$, which can be written as:

$$y_{t+1}^i = h(\mathbf{x}_t^{i-}, \mathbf{u}_{t+1}, \boldsymbol{\theta}^i) \quad (\text{C.2})$$

To represent the error statistics in the forecast step, we assume that at time $t + 1$, we have an ensemble of n forecasted states, $\mathbf{x}_t^- \triangleq (\mathbf{x}_t^{1-}, \dots, \mathbf{x}_t^{n-})$ and an ensemble of n forecasted outputs, $y_{t+1}^- \triangleq (y_{t+1}^1, \dots, y_{t+1}^n)$. Then the ensemble means of forecasted state ($\bar{\mathbf{x}}_t^-$) and the ensemble mean of forecasted output ($\bar{y}_{t+1}$) are estimated by:

$$\bar{\mathbf{x}}_t^- \triangleq \frac{1}{n} \sum_{i=1}^n \mathbf{x}_t^{i-} \quad (\text{C.3})$$

$$\bar{y}_{t+1} \triangleq \frac{1}{n} \sum_{i=1}^n y_{t+1}^i \quad (\text{C.4})$$

Then, we define the ensemble error matrix of forecasted state, E_{t+1}^- around the ensemble mean by:

$$E_{t+1}^- \triangleq [\mathbf{x}_t^{1-} - \bar{\mathbf{x}}_t^- \dots \mathbf{x}_t^{n-} - \bar{\mathbf{x}}_t^-] \quad (\text{C.5})$$

and the ensemble of output error matrix, E_{t+1}^y is:

$$E_{t+1}^y \triangleq [y_{t+1}^1 - \bar{y}_{t+1} \dots y_{t+1}^n - \bar{y}_{t+1}] \quad (\text{C.6})$$

The error covariance matrix is calculated including:

- The error covariance matrix of ensemble forecast state:

$$Q_{t+1}^x = \frac{1}{n-1} E_{t+1}^- (E_{t+1}^-)^T \quad (\text{C.7})$$

- The error covariance matrix of model output:

$$Q_{t+1}^y = \frac{1}{n-1} E_{t+1}^y (E_{t+1}^y)^T \quad (\text{C.8})$$

- The forecast cross-covariance of the states and output:

$$Q_{t+1}^{xy} = \frac{1}{n-1} E_{t+1}^- (E_{t+1}^y)^T \quad (\text{C.9})$$

In order for the EnKF to maintain sufficient spreads in ensemble and to prevent from filter divergence [Whitaker and Hamill, 2002], observations should be treated as random variables. At each time, an observation is perturbed by adding noise drawn from a Gaussian distribution of mean zero and predefined covariance [Burgers *et al.*, 1998]. Thus, in the updated step, the forecasted state set $\mathbf{x}_{t+1}^{i-}$ is updated using the Kalman gain K_{t+1}^x as follow:

$$\mathbf{x}_t^{i+} = \mathbf{x}_t^{i-} + K_{t+1}^x (y_{t+1}^{Obs,i} - y_{t+1}^i) \quad (\text{C.10})$$

where $y_{t+1}^{Obs,i}$ is the i -th trajectory of the observation replicates generated by adding to the actual observation (y_{t+1}^{Obs}) error, η (i.e., a perturbation to observation) that has zero mean and the covariance, $E_{t+1}^{y^{Obs}}$, which is determined in Section 2.1.4, as follow:

$$y_{t+1}^{Obs,i} = y_{t+1}^{Obs} + \eta_{t+1}^i, \quad \eta_{t+1}^i \sim N(0, E_{t+1}^{y^{Obs}}) \quad (C.11)$$

The Kalman gain matrix can be calculated by:

$$K_{t+1}^x = Q_{t+1}^{xy} [Q_{t+1}^y + Q_{t+1}^{Obs}]^{-1} \quad (C.12)$$

where Q_{t+1}^{Obs} is the covariance matrix of the observation, $y_{t+1}^{Obs,i}$, which is defined similar to Q_{t+1}^y .

$$Q_{t+1}^{Obs} = \frac{1}{n-1} E_{t+1}^{Obs} (E_{t+1}^{Obs})^T \quad (C.13)$$

$$E_{t+1}^{Obs} \triangleq [y_{t+1}^{Obs,1} - y_{t+1}^{Obs} \dots y_{t+1}^{Obs,n} - y_{t+1}^{Obs}] \quad (C.14)$$

C.2. Dual parameters-states updated

The dual EnKF requires two interactive and parallel filters for the states and parameters estimation [Moradkhani *et al.*, 2005b]. The parameters are first updated and then the states. In order to extend the applicability of the single EnKF to the simultaneous parameters–states EnKF, one needs to treat the ensemble size of parameter sets similar to the model state. However, the parameter values are not changed after the forecast step:

$$\theta_{t+1}^{i-} = \theta_t^{i+} \quad (C.15)$$

Using the parameters forecasted and the replicates of forcing data, states of the ensemble model and model prediction are computed as follows:

$$\mathbf{x}_t^{i-} = f(\mathbf{x}_{t-1}^{i+}, \mathbf{u}_t, \boldsymbol{\theta}_{t+1}^{i-}) + w_t^i, \quad i = 1, \dots, n \quad (\text{C.16})$$

$$y_{t+1}^i = h(\mathbf{x}_t^{i-}, \mathbf{u}_{t+1}, \boldsymbol{\theta}_{t+1}^{i-}) \quad (\text{C.17})$$

Updating the ensemble parameter member is made:

$$\boldsymbol{\theta}_{t+1}^{i+} = \boldsymbol{\theta}_{t+1}^{i-} + K_{t+1}^{\boldsymbol{\theta}} (y_{t+1}^{Obs,i} - y_{t+1}^i) \quad (\text{C.18})$$

where $K_{t+1}^{\boldsymbol{\theta}}$ is the Kalman gain for correcting the parameter trajectories obtained with:

$$K_{t+1}^{\boldsymbol{\theta}} = Q_{t+1}^{\boldsymbol{\theta}y} [Q_{t+1}^y + Q_{t+1}^{Obs}]^{-1} \quad (\text{C.19})$$

where $Q_{t+1}^{\boldsymbol{\theta}y}$ is the cross-covariance matrix of model parameters and model output. Now use the updated parameter $\boldsymbol{\theta}_{t+1}^{i+}$ to the step given in Appendix C.1 to update the ensemble model states simultaneously.

Appendix D. Sobol' sensitivity analysis

Sobol' method is a variance-based sensitivity analysis that identifies parameter sensitivities by evaluating the variance of model output (y) due to the variability of individual parameters and their parameter interactions [Sobol', 2001; Saltelli, 2002; Crestaux *et al.*, 2009]. Instead of the model output, model performance measures (e.g., NSE , PE , and VE in this study) can be used [Tang *et al.*, 2007]. The total variance, $D(y)$ is decomposed as:

$$D(y) = \sum_{a=1}^{M_P} D_a + \sum_{a < b} D_{ab} + \dots + D_{1\dots M_P} \quad (\text{D.1})$$

where D_a is the variance of y due to the changes of a -th model parameter, $\boldsymbol{\theta}_a$, denoting the first order contribution to $D(y)$; D_{ab} is the variance of y due to the pairwise interactions of a -th and b -th parameters, referring to the second order contribution.

The first (S_a) and total ($S_{Total,a}$) order Sobol' sensitivity indices can be respectively expressed as:

$$S_a = \frac{D_a}{D(y)} \quad (D.2)$$

$$S_{Total,a} = 1 - \frac{D_{\sim a}}{D(y)} \quad (D.3)$$

where $D_{\sim a}$ is the variance averaged over the contributions resulting from all parameters except for θ_a .

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Table 1. Literature review of applications involving real-time, ensemble streamflow forecasting. The last column corresponds to the taxonomy of the predictive approach (A) that we define in Table 3. “Warm-up” methods have a warm-up period, while “Arbitrary” do not.

Study	Deterministic model	Surrogate model	Parameter specification	State initialization	DA	A
<i>Zhang et al.</i> [2018]	Xinjiang	-	Optimization	Warm-up	Dual	A12
<i>Abbaszadeh et al.</i> [2018]	SAC-SMA	-	Random	Arbitrary	Dual	A12
<i>Wang et al.</i> [2018]	HyMOD	PCE	NA	Warm-up	Dual	A6
<i>Davison et al.</i> [2017]	MESH	-	Random	NA	Dual	A3
<i>Thibault et al.</i> [2016]	Multimodels	-	NA	Warm-up	Single	A2
<i>Fan et al.</i> [2016]	HyMOD	PCE	Random	NA	Dual	A6
<i>Zahmatkesh et al.</i> [2015]	HyMOD, HBV, SWMM	-	Bayesian inference	Warm-up	None	A10
<i>Li et al.</i> [2014]	GR4H	-	Optimization	NA	Dual	A12
<i>DeChant and Moradkhani</i> [2014]	VIC	-	NA	Warm-up	Dual	A3
<i>Xie and Zhang</i> [2013]	SWAT	-	Random	Warm-up	Dual	A3
<i>Chen et al.</i> [2013]	HyMOD	-	Bayesian inference	NA	Single	A11
<i>Moradkhani et al.</i> [2012]	HyMOD	-	Random	Warm-up	Dual	A3
<i>He et al.</i> [2012]	SNOW17+ SAC-SMA	-	Bayesian inference	Warm-up	Single	A11
<i>Mendoza et al.</i> [2012]	TopNet	-	Manual calibration	Warm-up	Single	A11
<i>Clark et al.</i> [2008]	TopNet	-	Bayesian inference	Warm-up	Single	A11
<i>Ajami et al.</i> [2007]	HyMOD, SWB	-	Bayesian inference	Warm-up	None	A10
<i>Weerts and El Serafy</i> [2006]	HBV-96	-	NA	NA	Single	A2
<i>Vrugt et al.</i> [2005]	HyMOD	-	Random	Arbitrary	Dual	A3
<i>Moradkhani et al.</i> [2005]	HyMOD	-	Random	Arbitrary	Dual	A3
<i>Madsen and Skotner</i> [2005]	Mike 11	-	Optimization	Warm-up	Single	A11
<i>Beven and Freer</i> [2001]	TOPMODEL	-	Bayesian inference	Warm-up	Dual	A12

NA: Not Available

Table 2. Description of the NAM model states and parameters

	Unit	Description	Lower Bound	Upper Bound
States	U	Water content in surface storage	0	35
	L	Water content in lower zone/root storage	0	400
	OF	Overland flow	0	$+\infty$
	IF	Inter flow	0	$+\infty$
	BF	Base flow	0	$+\infty$
Parameters	Um	Maximum water content in surface storage	5	35
	Lm	Maximum water content in lower zone/root storage	50	400
	CQOF	Overland flow coefficient	0	1
	CKIF	Interflow drainage constant	200	2000
	TOF	Overland flow threshold	0	0.9
	TIF	Interflow threshold	0	0.9
	TG	Groundwater recharge threshold	0	0.9
	CK12	Time constant for routing interflow and overland flow	3	72
	CKBF	Time constant for base flow	500	5000

Table 3. Forecasting approaches employed in this study

Approach	Specification	Model	Data assimilation
A1	<i>Random</i>	NAM	None
A2			EnKF
A3			Dual EnKF
A4		PCE-I	None
A5			EnKF
A6			Dual EnKF
A7		PCE-II	None
A8			EnKF
A9			Dual EnKF
A10	<i>Selected</i>	NAM	None
A11			EnKF
A12			Dual EnKF
A13		PCE-I	None
A14			EnKF
A15			Dual EnKF
A16		PCE-II	None
A17			EnKF
A18			Dual EnKF

Table 4. Performance metric values of 18 approaches. The values in the first 3 columns are the medians of NSE , AE_{peak} , and RE , which match the values in Fig. 9.

Approach	median of NSE [-]	median of AE_{peak} [m ³ /s]	median of RE [-]	BS [-]	$\overline{UR}$ [m ³ /s]
A1	-3.62	2292.19	0.019	1.00	1834.18
A2	0.70	515.64	0.009	0.75	367.34
A3	0.75	500.45	0.009	0.66	340.12
A4	-3.84	1928.86	0.015	0.97	1760.11
A5	0.82	126.48	0.005	0.16	327.86
A6	0.79	55.84	0.005	0.20	131.92
A7	0.68	904.21	0.009	1.00	26.52
A8	0.68	901.91	0.010	1.00	20.59
A9	0.68	902.79	0.010	1.00	19.63
A10	0.82	612.60	0.007	1.00	193.95
A11	0.88	401.26	0.005	0.78	161.69
A12	0.89	242.62	0.005	0.24	172.18
A13	0.44	532.35	0.004	1.00	139.54
A14	0.74	157.07	0.003	0.25	102.98
A15	0.80	176.00	0.003	0.26	91.98
A16	0.73	787.18	0.010	1.00	55.75
A17	0.71	839.31	0.010	1.00	44.64
A18	0.71	840.19	0.010	1.00	46.37

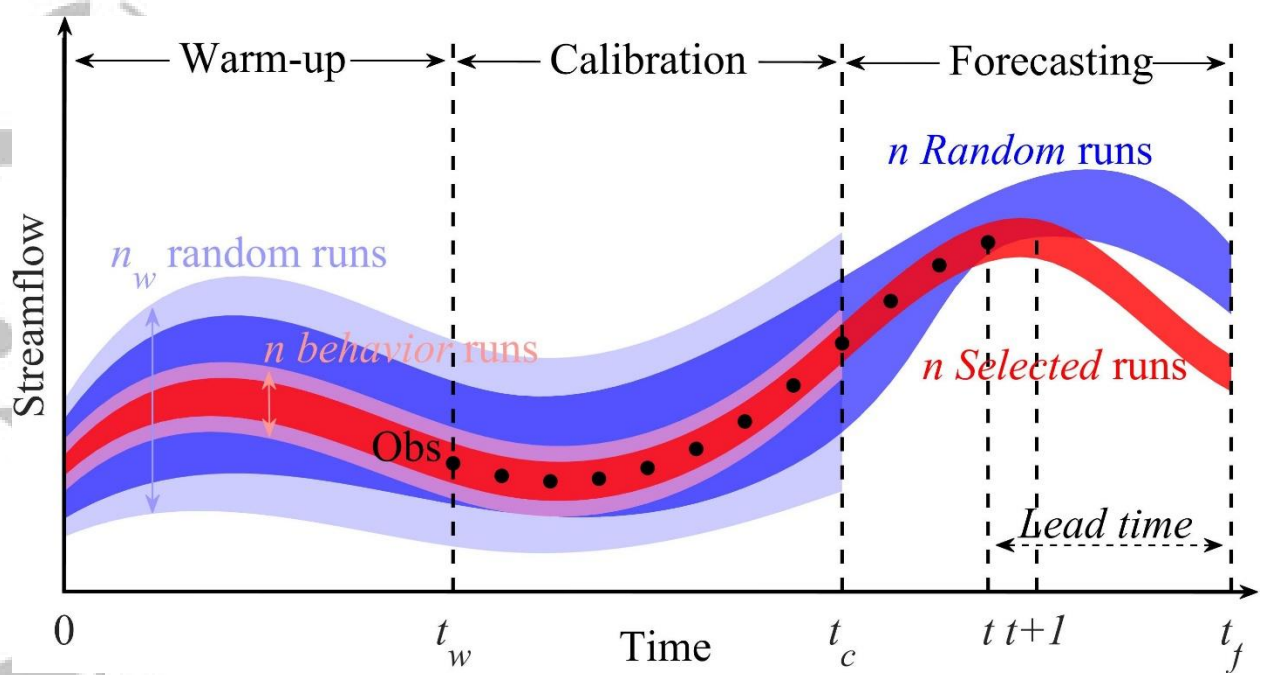


Figure 1. A schematic illustration for real-time ensemble flood forecasting, which consists of 3 intervals: warm-up, calibration, and forecasting periods. The light red shaded region in the warm-up and calibration periods refers to the n behavior results of GLUE that are employed to estimate posterior parameter distributions, while the light blue region refers to the n_w random results obtained from parameter sets sampled from prior (uniform) distributions to attain the n behavior runs. The construction of PCE models is carried out over the calibration period: PCE-I model is built from the N_I training samples extracted from the light blue region, while PCE-II is from the N_{II} samples from the light red region. The (dense) blue and red shaded regions correspond to the approaches using the “Random” (A1 to A9) and “Selected” (A10 to A18) parameter specifications with the same n ensemble runs, respectively.

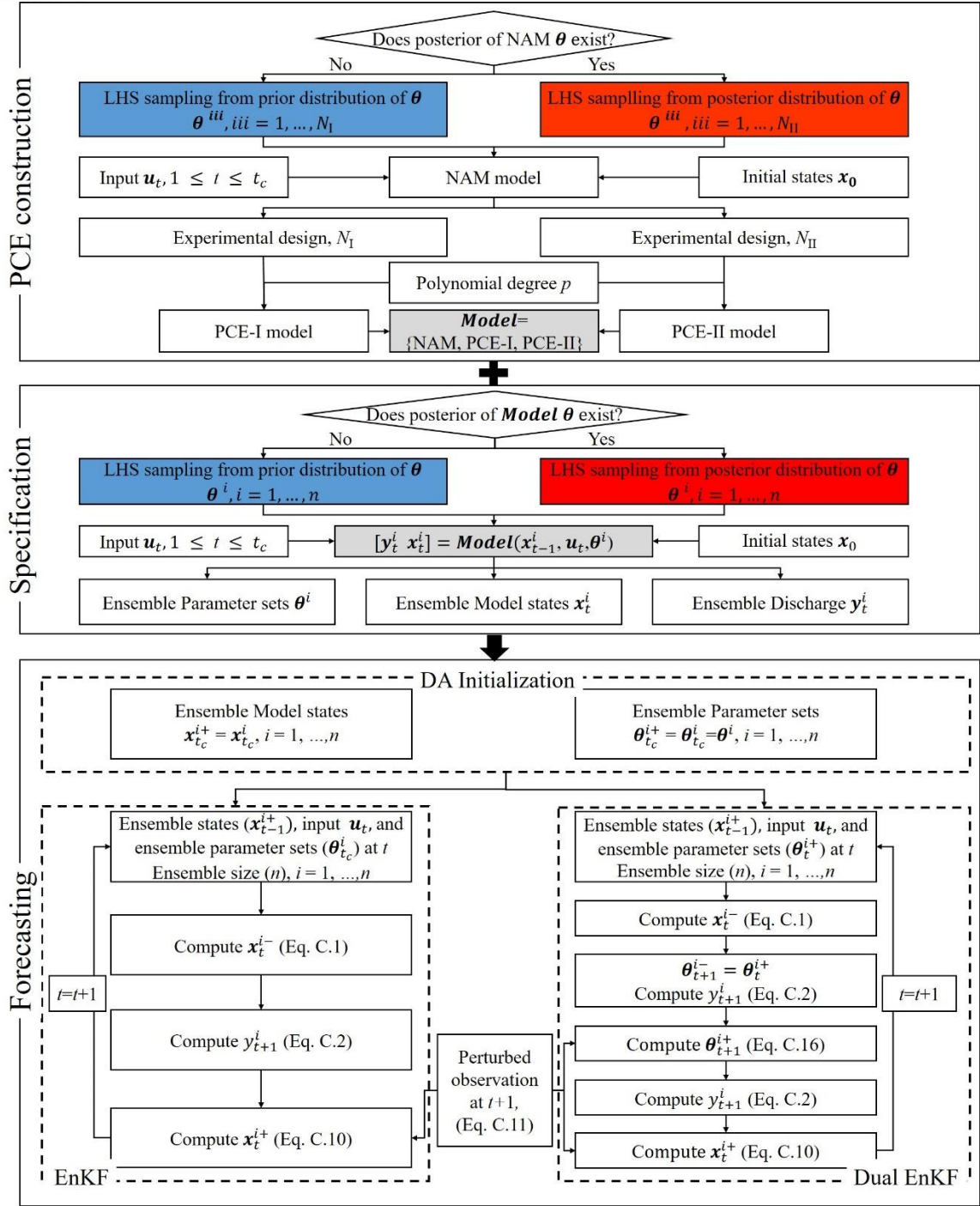


Figure 2. The overview of an ensemble flood forecasting framework. The top box, “PCE construction” is for the process of building 2 PCE models (blue box for PCE-I and red box for PCE-II). The middle box, “Specification” describes 2 distinct approaches of specifying model parameters before forecasting including *Random* (blue box) and *Selected* (red box). The bottom box, “Forecasting” corresponds to data assimilation for flood forecasting in real-time (single and dual EnKFs). The top and middle blue boxes correspond to sampling N_I and n , independently from the same prior uniform distributions, respectively, while the red boxes sampling N_{II} and n from the same posterior distributions.

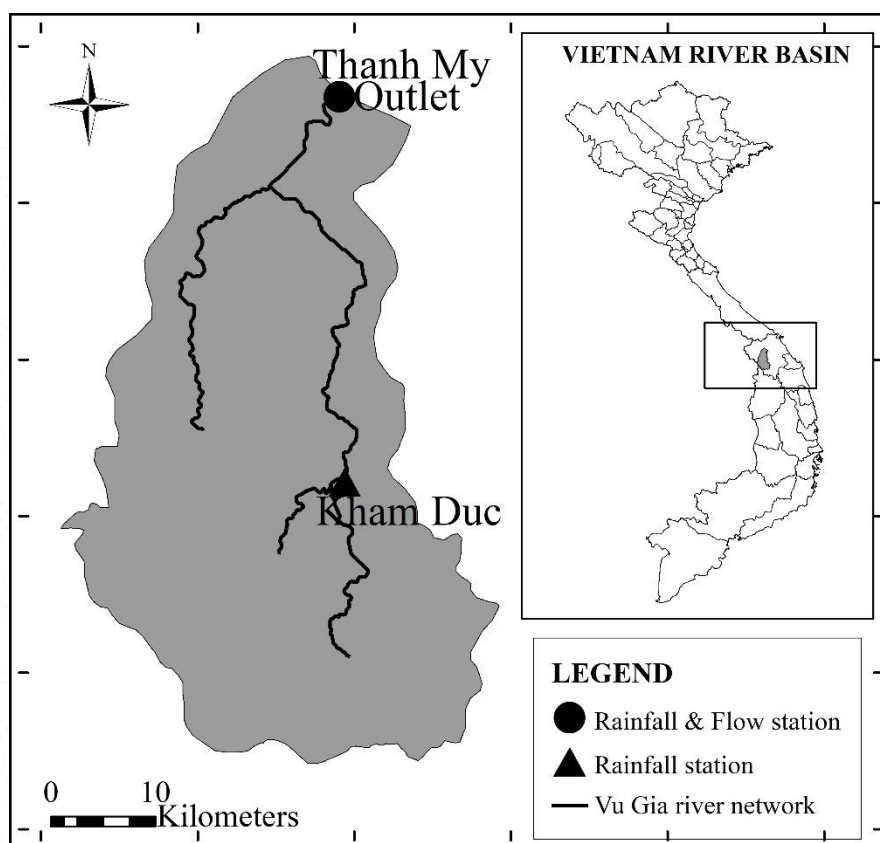


Figure 3. Study area: Vu Gia watershed

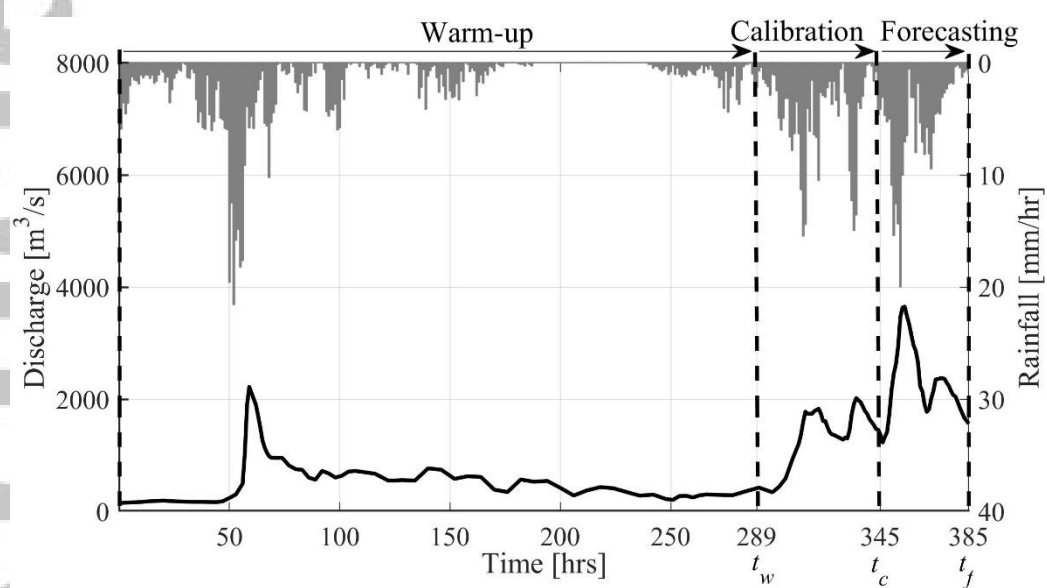


Figure 4. Flood event used in the study. The black line is the discharge of outlet and the gray hyetograph represents the average rainfall of Vu Gia watershed.

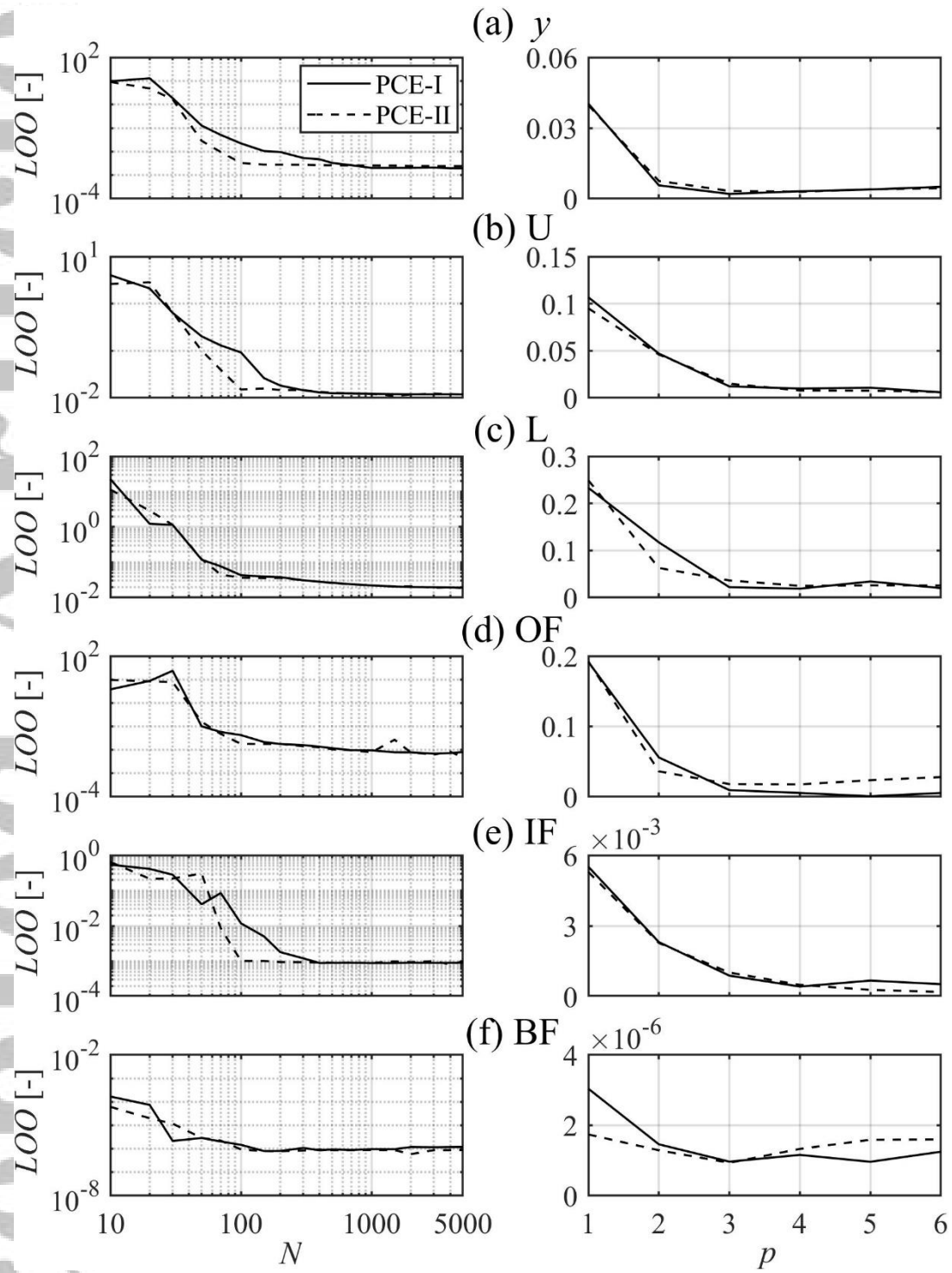


Figure 5. The effects of (left plots) the experimental design, N and (right plots) the polynomial degree, p on the leave-one-out cross-validation error (LOO) in constructing PCE-I and PCE-II models, for (a) streamflow and (b to f) 5 model states in Table 2.

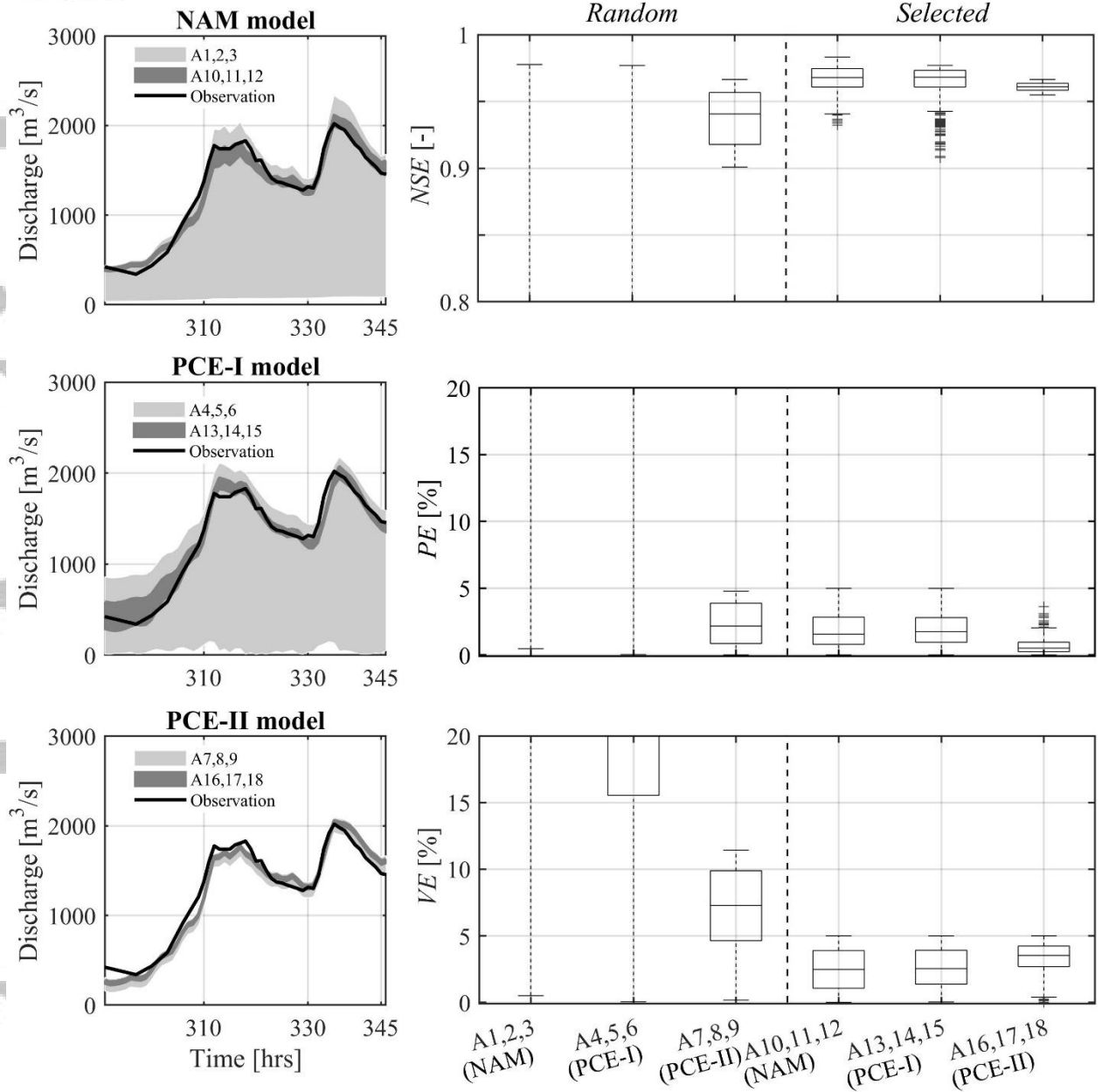


Figure 6. The left column plots show hydrographs for the calibration period. The shades in the plots correspond to 90% confidence interval for 500 *Random* model runs (A1 to A9, light gray shade) and 500 *Selected* model runs (A10 to 18, dark gray shade) for 18 approaches in Table 3. The boxplots in the right column demonstrate the verification metrics of *NSE*, *PE*, and *VE* for the 18 approaches used.

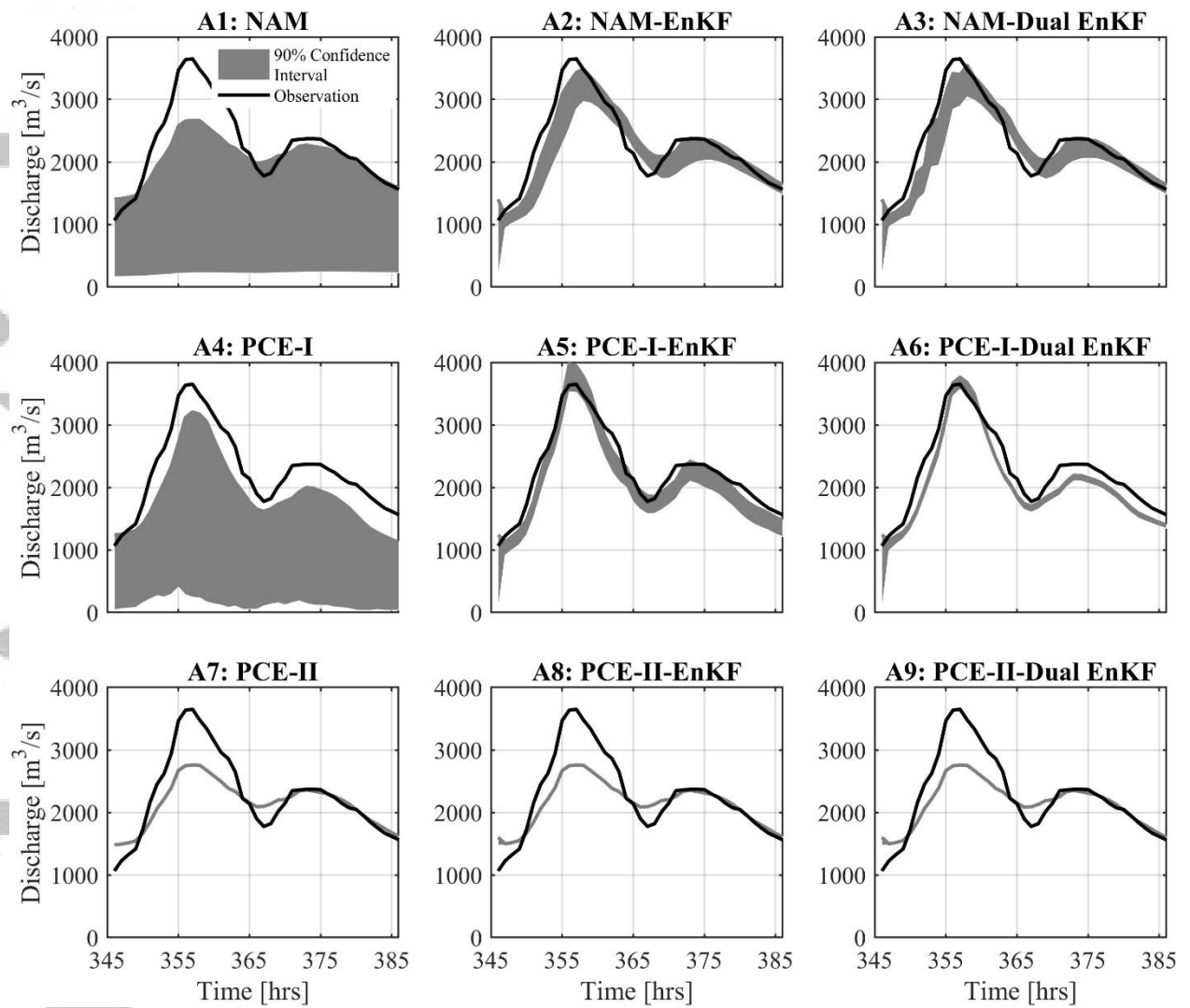


Figure 7. Hydrographs over the forecasting period, with a 90 % confidence interval of 500 *Random* model runs (A1 to A9).

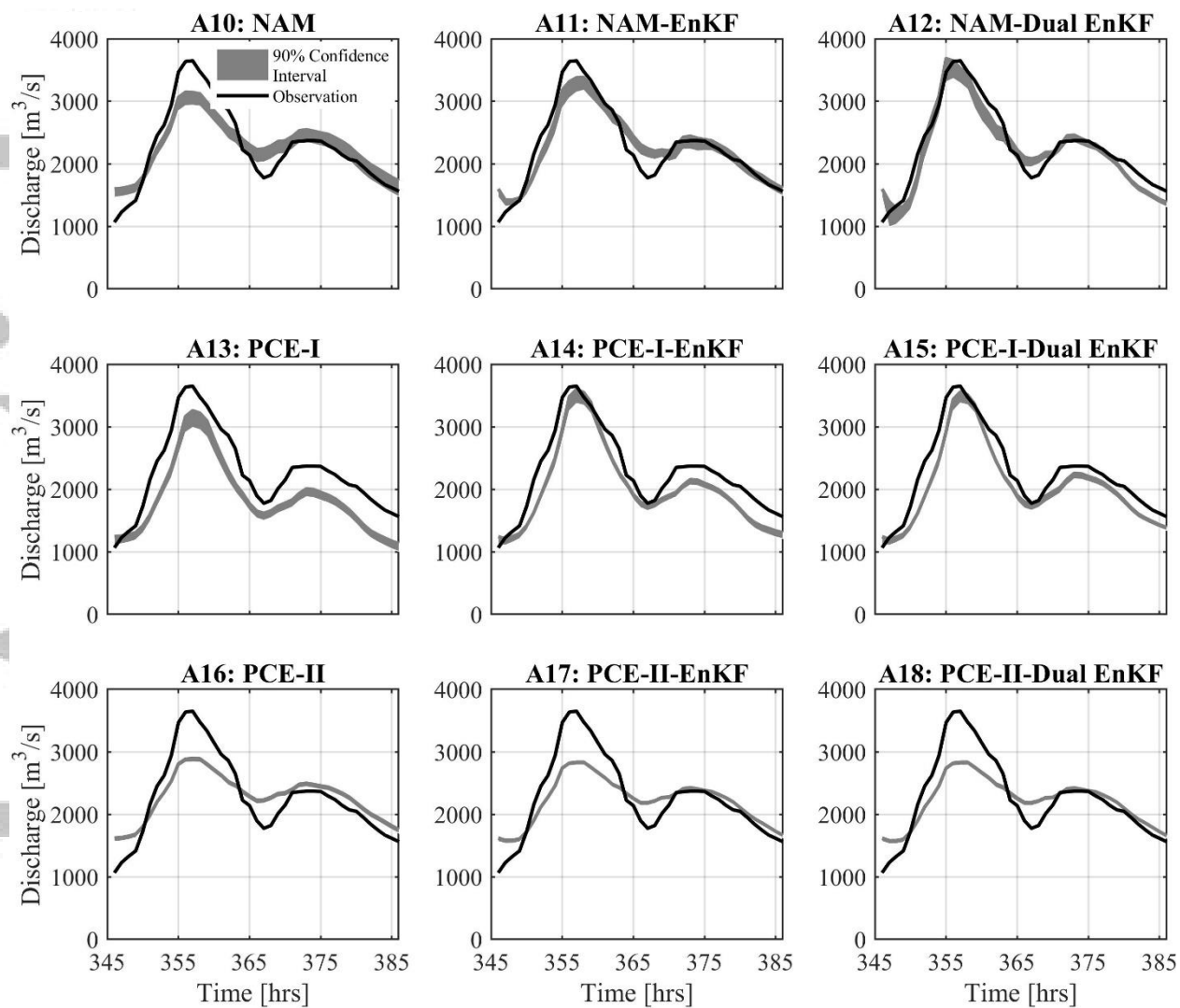


Figure 8. Hydrographs over the forecasting period, with a 90 % confidence interval of 500 *Selected* model runs (A10 to A18).

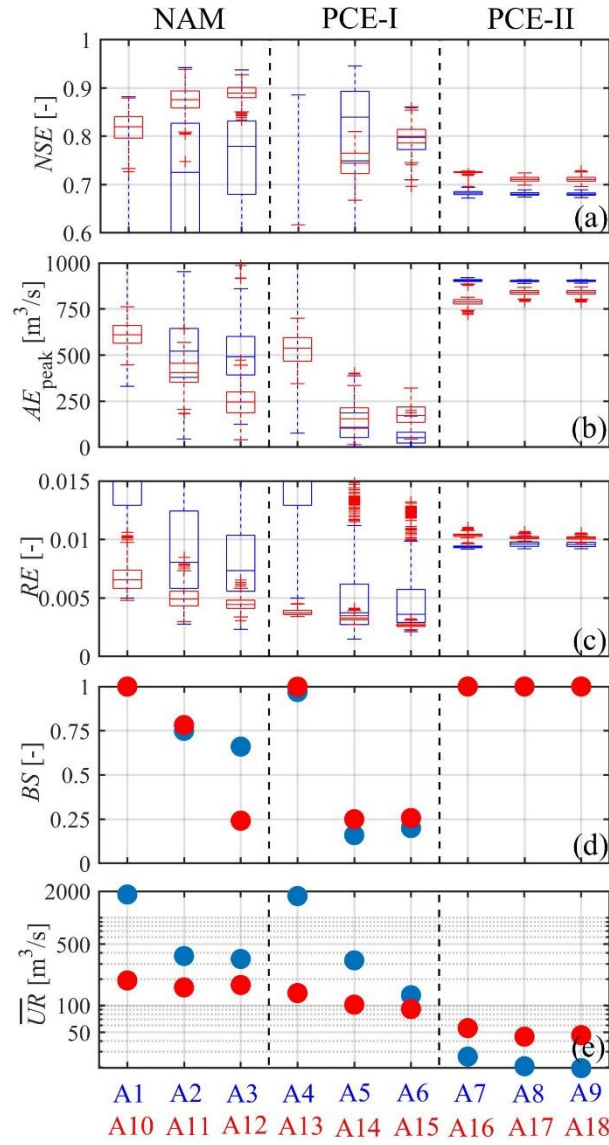


Figure 9. The performance metrics reflecting accuracy and predictability of the 18 approaches for the forecasting period. Boxplots of (a) NSE , (b) AE_{peak} (AE at flood peak time) and (c) RE show 500 ensemble values with the statistics of median (central mark), the 25th and 75th percentiles (edges of the box), and maximum and minimum except for outliers (whiskers). (e) UR is the mean of uncertainty range, UR_t over the entire forecasting period.

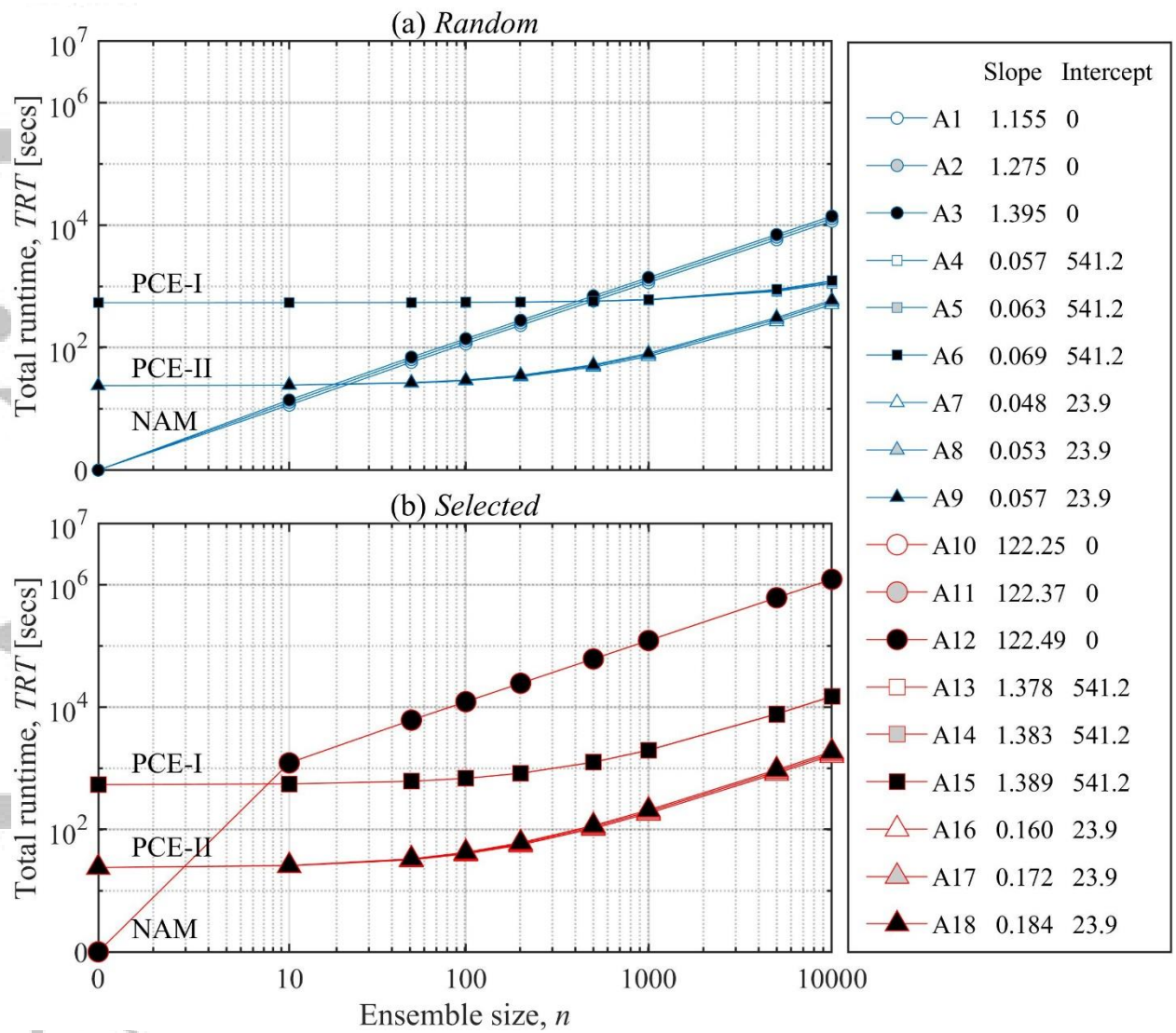


Figure 10. The total runtime (TRT) corresponding to 18 approaches in the forecasting period versus ensemble size (n). Note that although we plot on logarithmic axis, the actual total runtime has the form of a linear function with the ensemble size at linear scale; its slope and intercept values for all approaches are tabulated on the right.

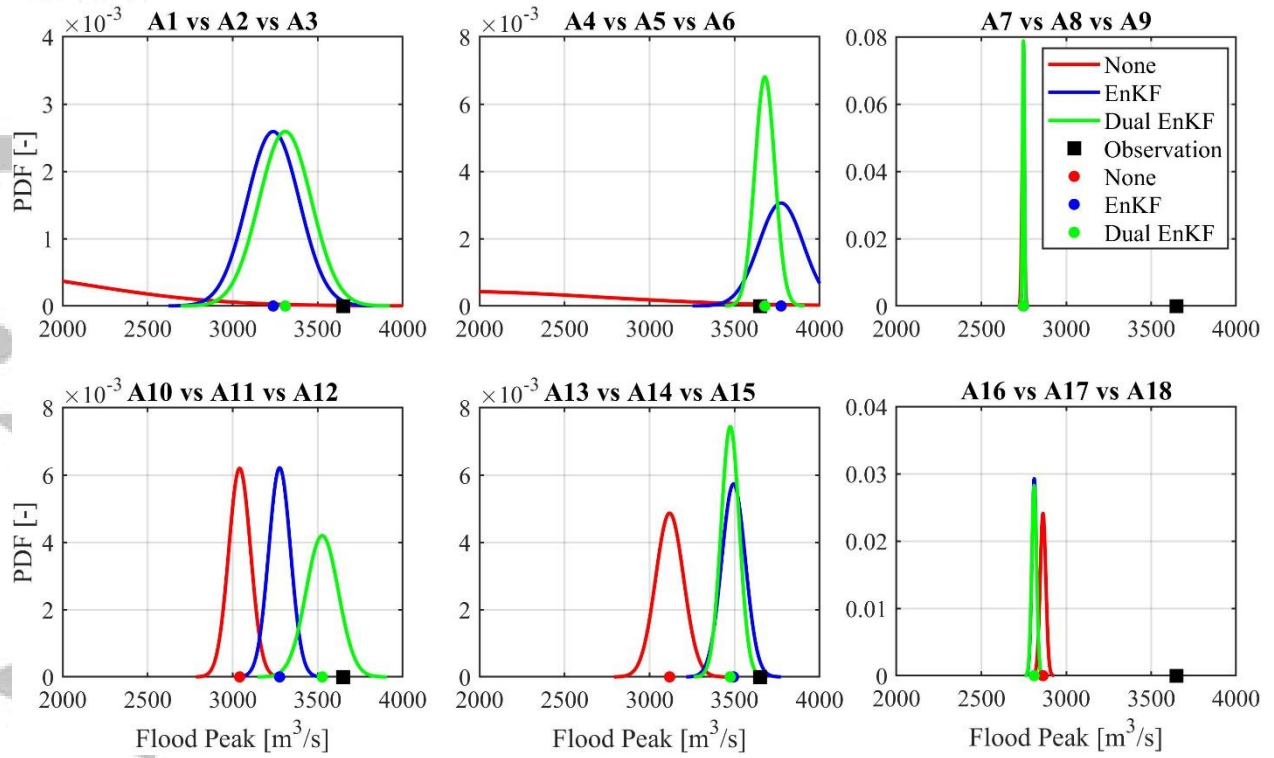


Figure 11. Comparisons of the three assimilation methods (none, EnKF, and Dual EnKF) for 500 ensemble flood peaks over the forecasting period. The left, middle, and right plots correspond to the approaches using NAM, PCE-I, and PCE-II, respectively. The first and second row plots correspond to the approaches using *Random* and *Selected* methods for parameter specification. The black square represents observed value at peak time; the circles are the expected values of the sample probability density functions.

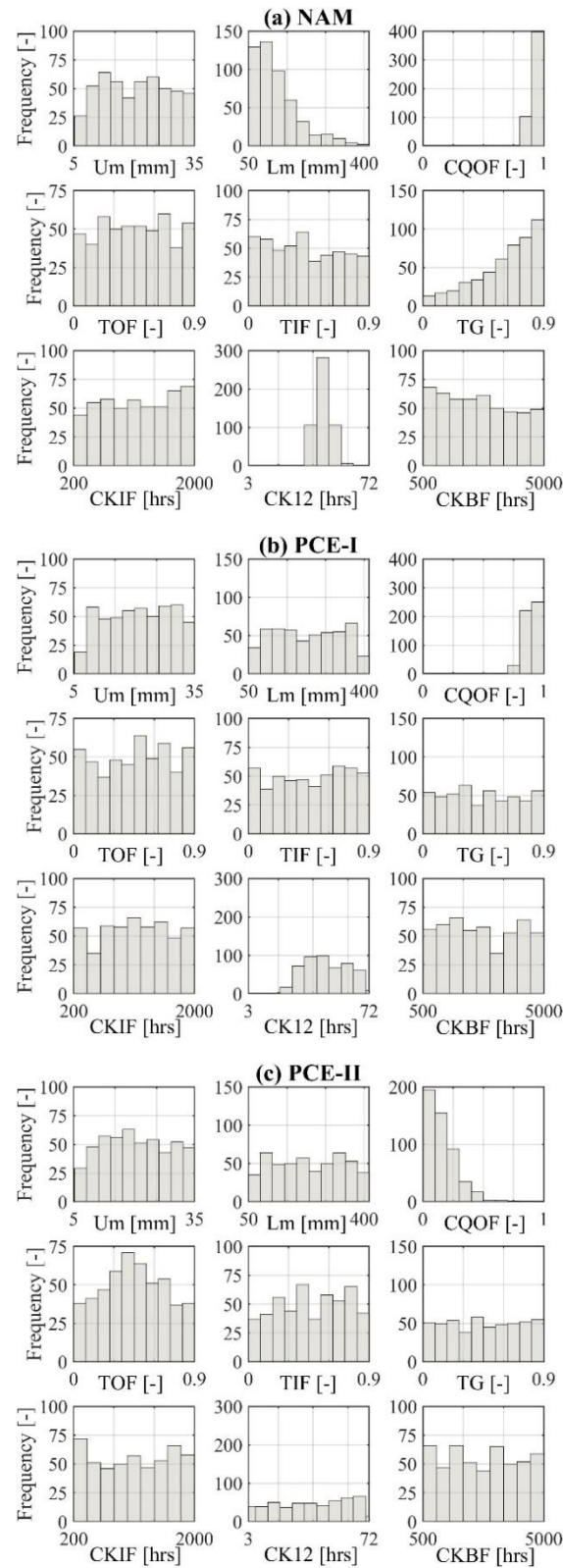


Figure 12. The posterior histograms for the 9 model parameters in Table 2 from 500 behavioral sets of 3 models (NAM, PCE-I and PCE-II) inferred by GLUE over the calibration period.

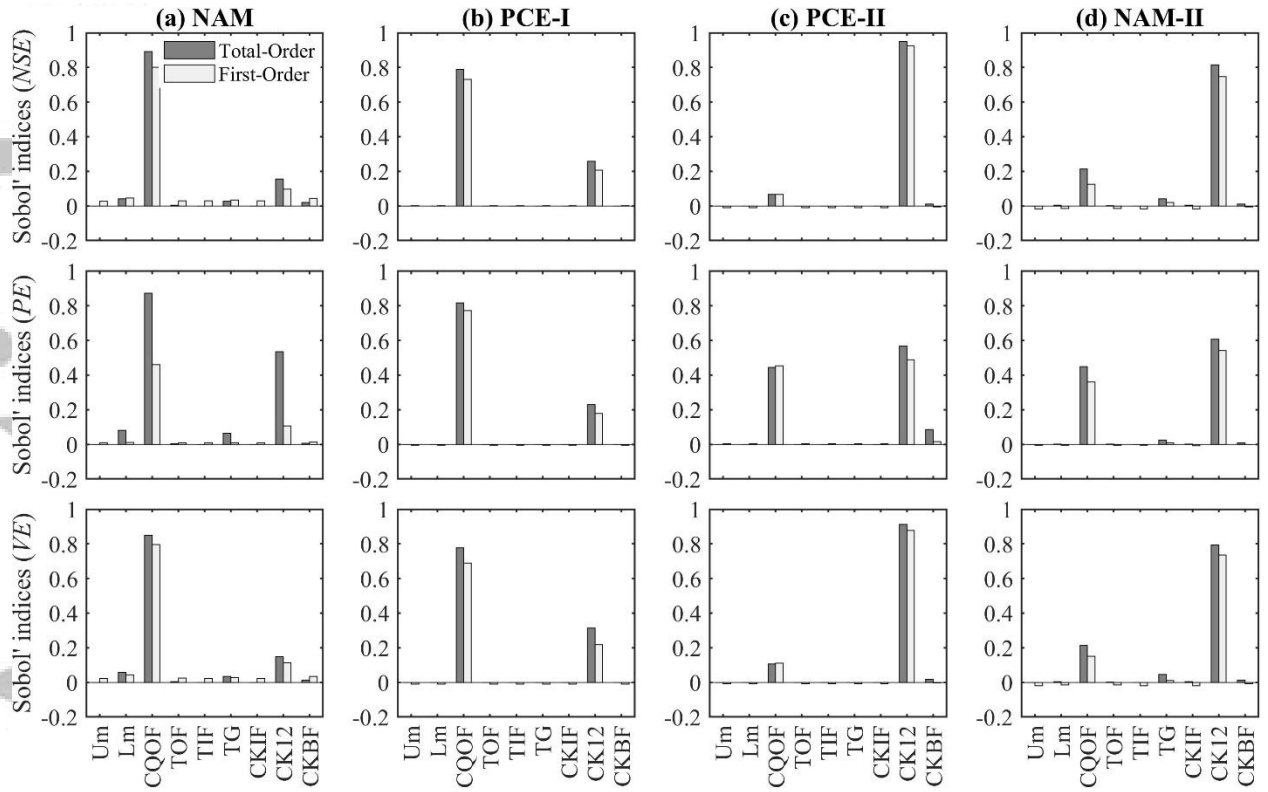


Figure 13. Sobol' sensitivity analysis for the 9 parameters, computed for the 3 likelihood functions of (top) *NSE*, (middle) *PE*, and (bottom) *VE* over the calibration period. The sensitivity results are attained based on (a, b, and c) the prior distributions of parameters for the 3 models of NAM, PCE-I, and PCE-II, respectively; and (d) the posterior distributions of parameters for NAM model. The posterior are also used to select the training parameter set for building PCE-II.