

# Stereoscopic high-speed microscopy to understand transient internal flow processes in high-pressure nozzles

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## Abstract

The flow and cavitation behavior inside fuel injectors is known to affect spray development, mixing and combustion characteristics. While diesel fuel injectors with converging and hydro-eroded holes are generally known to limit cavitation and feature higher discharge coefficients during the steady period of injection, less is known about the flow during transient periods corresponding to needle opening and closing. Multiple injection strategies involve short injections, multiplying these aspects and giving them a growing importance as part of the fuel delivery process. In this study, single-hole transparent nozzles were manufactured with the same hole inlet radius and diameter as the Engine Combustion Network Spray D nozzle, mounted to a modified version of a common-rail Spray A injector body and needle. Needle opening and closing periods were visualized with stereoscopic high-speed microscopy at injection pressures relevant to modern diesel engines. Time-resolved sac pressure was extracted via elastic deformation analysis of the transparent

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nozzles. Sources of cavitation were observed and tracked, enabling the identification of a gas exchange process after the end of injection with ingestion of chamber gas into the sac and orifice. We observed that the gas exchange contributed widely to disrupting the start of injection and outlet flow during the subsequent injection event.

*Keywords:*

Transparent nozzles, Diesel injection, Internal flow, Cavitation, Microscopy.

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## 1. Introduction

Spray formation and mixing are crucial phenomena for combustion systems, especially those featuring direct injection technology. In reciprocating engines, the processes of direct fuel injection into the cylinder is highly transient and closely tied to efficiency and potential for pollutant formation. Although our understanding of high-pressure sprays is progressing, a missing component is the linkage between flows inside the nozzle and the effect on the emerging spray. Several studies have linked internal flow hydraulic characteristics to spray development and mixing [1, 2], through correlation of injection mass flow rate or momentum flux to spray penetration and dispersion. Hydraulic characterization under the appropriate operating conditions is valuable to understand the flow behavior of the injection system and necessary to provide the correct boundary conditions to computational fluid dynamic (CFD) simulations. However, these measurements fail to capture the detailed physics of the phenomena occurring within the injector, namely the inception and development of cavitation, as well as the highly important transient processes.

18 Taking advantage in material science and improving machining capabil-  
19 ities, researchers have been able to manufacture transparent fuel injector  
20 nozzles with real-size holes, despite typical diameters of only a fraction of a  
21 millimeter, to permit study of internal flow at practical conditions. Prototype  
22 nozzles made of various materials such as acrylic or quartz, have permitted  
23 the application of optical diagnostics to scrutinize the flow behavior inside  
24 micro-orifice [3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14]. These studies have made  
25 substantial progress in our understanding of hydraulic and cavitation behav-  
26 ior in high-pressure flow and spray processes.

27 On the other hand, there has been less focus on the transient periods  
28 of the injection event in this emerging field. High temporally resolved tech-  
29 niques, with repeatable control, are necessary to capture the fast, transitory  
30 processes driving global hydraulic characteristics, spray development and  
31 mixing processes. This aspect becomes particularly important in modern  
32 diesel engines, where injection strategies rely on multiple injections per cy-  
33 cle. In most cases, quasi-steady quantities are not representative of the flow,  
34 as the needle valve moves throughout the entirety of the injection, requiring  
35 study of the entire transient process of each injection and of multiple succes-  
36 sive injections. With the progress made in high-speed digital imaging, as well  
37 as manufacturing techniques, recent studies employed high-speed microscopy  
38 to track the evolution of the inside flow and injected spray at relevant injec-  
39 tor and ambient operating conditions. Hayashi and coworkers [11] have even  
40 used a quartz nozzle featuring three side-located, 0.14-mm orifices injecting  
41 into a reacting combustion environment prepared in an optically-accessible  
42 rapid compression machine. Swantek et al. [15] visualized the injection pro-

cesses in real-size metal nozzles in detail using x-ray phase-contrast imaging. They observed left-over gas bubbles in the sac of high-pressure diesel injectors after the end of injection, which they believed came from ingested chamber gas. The lack of temporal resolution did not allow them, however, to explain the origin of the presence of gas in the sac following the end of injection.

Parallel to the experimental efforts, CFD modeling of the internal flow is needed to develop more predictive models about spray breakup and mixing processes. However, one weakness in this area is that the state of the nozzle sac, defined as the volume between the needle valve and the holes, is often unknown and undefined. The transient, in-nozzle processes and the status of the sac in high-pressure diesel injectors was numerically studied by Battistoni et al. [16], whose simulations predicted cavitation and the presence of gas in the sac after the end of injection. Building on the experimental results of Swantek et al. [15], they also concluded that the residual gas in the sac comes from ingested chamber gas, but did not propose a physical explanation. This aspect is particularly significant for highly-resolved volume-of-fluids simulations, where high computational costs limit the simulation time to only the early transient period. Consequently, if boundary conditions, such as the amount of gas present in the sac before injection, are unknown, the relevance and universal conclusions of these simulations should be questioned. Microscopic visualization of starting spray from metal fuel injectors at engine conditions already showed evidence of gas injection leading liquid injection [2, 17] with collateral effects on initial flow characteristics and spray development. For example, recent measurements showed that once liquid is injected, the initial flow velocity exiting the injector does not ramp up from zero, thus

68 affecting transient rate of injection used in CFD [18, 19].

69 In this work, we designed real-size optically transparent nozzles match-  
70 ing the Engine Combustion Network (ECN) Spray D geometry (see exact  
71 surface geometry at [ecn.sandia.gov](http://ecn.sandia.gov)). A cylindrical, sharp-edged version  
72 of the nozzle was also tested to observe the effect of cavitation on the tran-  
73 sient phenomena. Based upon availability, the nozzles were mounted on a  
74 modified ECN Spray A injector. Experiments were performed in an optically-  
75 accessible pressure chamber able to emulate pressurized ambient conditions,  
76 typical of modern Direct-Injection (DI) diesel engines. We performed stereo-  
77 scopic high-speed microscopy to visualize the internal flow and cavitation, as  
78 well as the near-nozzle spray formation. The remaining of the manuscript  
79 is organized as follows. The experimental methods are described, detailing  
80 the constant-flow, high-pressure optical chamber, the stereoscopic high-speed  
81 imaging arrangement, and the transparent nozzle, including advanced geom-  
82 etry characterization. The results section presents the temporally-resolved  
83 needle lift and sac pressurization process, followed by the end of injection gas  
84 exchange, leading to particularities of the start of injection.

## 85 **2. Experimental methods**

86 All the work on real-size, transparent nozzles introduced earlier paved the  
87 way to the experiments conducted in this work. Because of the high pressures  
88 involved in diesel injection, the priority was to design and manufacture op-  
89 tically transparent nozzles that would withstand pressures above 100 MPa.  
90 In addition to finite element analysis, extensive stress testing was carried  
91 out to evaluate the elastic and plastic deformation characteristics of the noz-

zles. More details about these tests are provided in Ref. [20]. The fast and highly transient nature of the processes involved in internal flow, especially cavitation, are favorable to high-speed microscopy. While challenging, our experience in such diagnostic helped take the technique to new levels. We developed a spatially and temporally correlated stereoscopic high-speed microscopy system to visualize the internal flow processes from two orientations and extract near-3-D information.

### 2.1. Stereoscopic imaging diagnostic

A stereoscopic system was developed to acquire detailed high-speed visualizations of the internal flow and near-nozzle spray from optically-transparent nozzles (Fig. 1). To maximize the stereoscopic effect in three dimensions, the systems were arranged orthogonal to one another. Each imaging system is composed of a long-working-distance microscope objective (Infinity K2-DistaMax or Infinity KV), a high-speed CMOS camera (Phantom v2512 or Photron SA-X2) and a custom-built illumination system.

Optical resolution is of primary importance when performing visualization at microscopic scales. The resolution of a microscope imaging system is generally referred to as the diffraction limit [21]. Criteria such as the Abbe or Rayleigh resolution limits are often used to theoretically assess an imaging system's performance. They provide a relationship between fundamental optical parameters, namely the illumination wavelength and numerical aperture of the receiving optics, a parameter equivalent to the collection angle in photography. In this context, short illumination wavelength and large numerical aperture contribute to achieving high-resolution images. The numerical aperture of the system for the primary configuration was 0.15, while

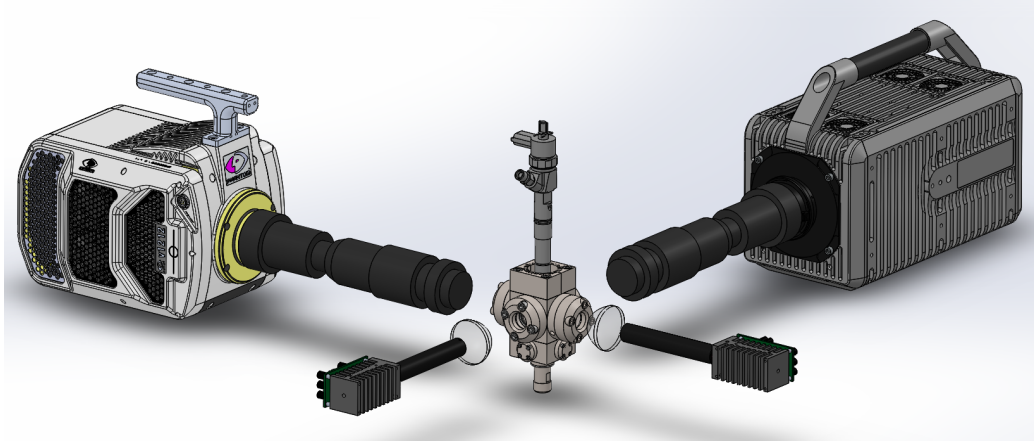


Figure 1: Schematic of the experimental arrangement, showing both high-speed cameras and illumination sources. The pressure vessel is located in the center of the sketch, between the two systems.

117 it was 0.10 for the secondary system. For both configurations, the Rayleigh  
 118 resolutions are less than half a pixel, meaning that the systems' are not  
 119 considered diffraction-limited, in part due to the relatively large working dis-  
 120 tance, limiting optical magnification, but also to the large pixels used in  
 121 high-performance, high-speed camera sensors [22].

122 The high velocities involved in internal and near-nozzle flow in high-  
 123 pressure injection systems make for stringent requirements to capture the  
 124 flow features motionlessly, or with no velocity-induced image blur. The effec-  
 125 tive optical resolution of the system and flow velocities set the pulse duration  
 126 requirements. The illumination systems rely on a custom blue LED emitter  
 127 centered on 455 nm (22 nm bandwidth) for the primary system, and a red  
 128 LED chip (620 nm, 19 nm bandwidth) for the secondary arrangement. At  
 129 the core of each LED illumination source is an ultrafast, high-current driver,  
 130 capable of producing pulses shorter than 10 ns at megahertz repetition rates.

131 For these experiments, the pulse duration was set to 30 ns for the primary  
132 system and 100 ns for the secondary.

133 The primary system operated at frequencies between 120 and 380 kHz,  
134 while the secondary system acquired at 270 kHz throughout the experiments.  
135 Although the cameras exposure times were set to 2 and 2.5  $\mu$ s for the pri-  
136 mary and secondary systems, respectively, the illumination pulse durations  
137 determined the exposure timescales. By synchronizing the two systems, the  
138 dual-camera arrangement allows simultaneous stereo or three-dimensional vi-  
139 sualization of the needle motion, internal flow and spray dynamics. To assist  
140 in the description of the systems and to allow the reader to become famil-  
141 iar with the configurations of each system, we labeled them primary and  
142 secondary systems. The primary corresponds to the Phantom v2512 cam-  
143 era, with the Infinity K2-DistaMax objective, while the secondary system is  
144 composed of the Photron SA-X2 and the Infinity KV lens. The microscope  
145 objectives were configured to provide magnification levels of  $8\times$  for the pri-  
146 mary system and  $3\times$  for the secondary one, resulting in digital resolutions  
147 of 3.5 and 7  $\mu$ m/pixel, respectively. More information about the cameras  
148 and their performance under general scientific application is available in Ref.  
149 [22].

## 150 2.2. Pressure chamber and transparent nozzles

151 Experiments were conducted using an optically-accessible chamber de-  
152 signed specifically for internal flow visualization and measurements in optically-  
153 transparent nozzles, as shown in Fig. 2. The vessel is equipped with four  
154 25.4-mm (1-in) diameter fused silica windows, providing dual or stereoscopic  
155 line-of-sight optical access to the transparent nozzle. The geometry of the



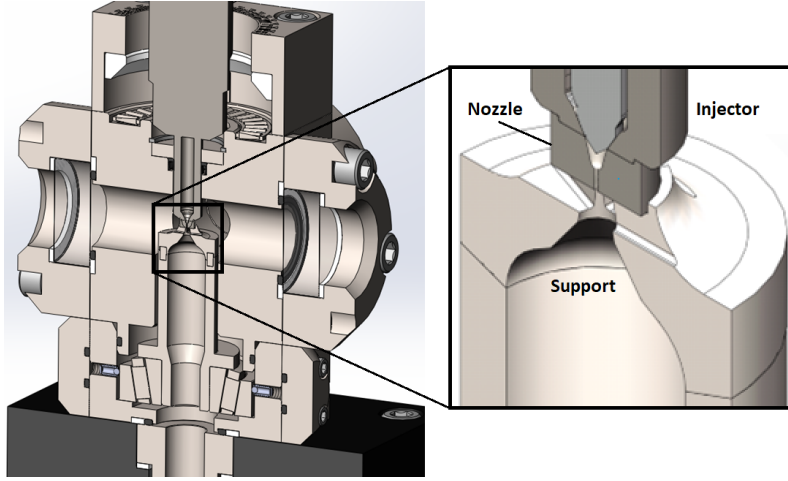


Figure 2: Schematic of the purposely-designed and built pressure vessel to optically access the internal flow processes of high-pressure transparent nozzles. The zoomed-in area shows the acrylic tip replacing the metal nozzle mounted on a modified Spray A injector, as well as geometric details of the nozzle support with cutouts to allow air entrainment and visualize the near-field spray.

156 chamber was tailored to allow short working distances and large numeri-  
 157 cal apertures for microscope imaging to perform optimally. The nozzle is  
 158 placed on a pedestal with open slots on four sides, allowing direct visualiza-  
 159 tion of the flow exiting the transparent nozzle as well as within the nozzle.  
 160 The open slots also permit air entrainment into the spray. The orifice is  
 161 vertically-aligned and a modified ECN Spray A solenoid-actuated injector is  
 162 mounted atop the transparent nozzle. More details on the nozzle geometries  
 163 and assemblies are provided in a later section. The chamber operates with  
 164  $N_2$  gas at constant-pressure. A flow is typically maintained to scavenge the  
 165 chamber internal volume, limiting the likelihood of window contamination  
 166 during repeated spray operation.

167 We used n-Dodecane fuel in the injection system for these experiments.  
168 The fuel was pressurized by a high-pressure syringe pump, and injection  
169 pressure was varied between 25 and 150 MPa, but repeated nozzle failures at  
170 150 MPa convinced us to set the upper injection pressure target to 100 MPa.  
171 It should be noted that the fuel was not degassed for these tests, and that  
172 a trace amount of air should be expected to dissolve under the conditions  
173 kept in the laboratory. This is reasonable as dissolved gas is also expected in  
174 regular diesel fuel tanks. The ambient conditions tested in this work ranged  
175 from atmospheric to 2.0 MPa, while the temperature was kept constant at  
176 20°C, resulting in a peak ambient density condition of  $22.8 \text{ kg/m}^3$ , matching  
177 the ECN Spray A target density condition.

178 Real-size, optically-transparent nozzles were designed to be mounted at  
179 the end of a modified solenoid-actuated ECN Spray A injector. The process  
180 is similar to the one described by Liverani et al. [9], where the tip of a  
181 production injector nozzle is machined out and replaced by the transparent  
182 model. The transparent nozzles were made from cast acrylic, and significant  
183 time and effort has been spent to ensure that the nozzle shape was made as  
184 specified. Cast acrylic was selected above quartz to avoid brittle material  
185 problems, and over sapphire to more closely match the refractive index of  
186 the fuel and the nozzle [10]. The ECN Spray D metal nozzle was chosen as  
187 the target nozzle. Spray D, is a conical orifice nozzle, with a target nominal  
188 diameter of 0.186 mm, a  $k$ -factor of 1.5 and hydro-grinding was performed  
189 to achieve a flow number of 188 g/min with 10 MPa pressure drop. The  
190 measured mean exit nozzle diameter for Spray D is about 0.189 mm. Spray  
191 D internal 3-D nozzle geometry and hydraulic characterization at realistic

192 diesel injection conditions have been performed by ECN participants and are  
193 available to download ([ecn.sandia.gov](http://ecn.sandia.gov)).

194 The transparent acrylic tips were micro-machined using custom tools for  
195 the sac and undersized drills for the hole, and then hydro-eroded to match  
196 the flow number of Spray D. Hydro-erosion rounded the inlet and produced  
197 an overall geometry that is an excellent match to Spray D, as shown in Fig.  
198 3. The upstream region of the sac is not that of Spray D, because an extra  
199 metal injector with the same dimensions as Spray D was not available for  
200 modification at the time. Instead, a complete Spray A injector was modified  
201 to be mated with the acrylic nozzle. Since the acrylic nozzle was designed  
202 to mate and seal with a modified Spray A injector (with support from the  
203 bottom and clamping forces from the injector above), as shown in Fig. 2, the  
204 sac (and needle) reflect that of the Spray A nozzle, which is slightly smaller  
205 than the Spray D sac. The acrylic tips were characterized by microscopic  
206 imaging while submerged in a liquid fluid which refractive index was close to  
207 the acrylic, proving to be the most reliable way to optically detect and locate  
208 internal geometries. Note that perfectly matching refractive indices reduces  
209 sensitivity, making it difficult to properly determine the location of nozzle  
210 sac and orifice boundaries. The measured metal Spray D (red) and Spray A  
211 (blue) profiles are overlaid on the photograph for comparison in Fig. 3.

212 The characteristic geometrical features of the target Spray D nozzle ap-  
213 pear well-represented by the transparent equivalent, with a good match be-  
214 tween orifice entrance curvature and overall dimensions. The measured out-  
215 let diameter of the acrylic tip under operating conditions was within a few  
216 micrometers of the target geometry, at 0.189 mm, effectively matching the

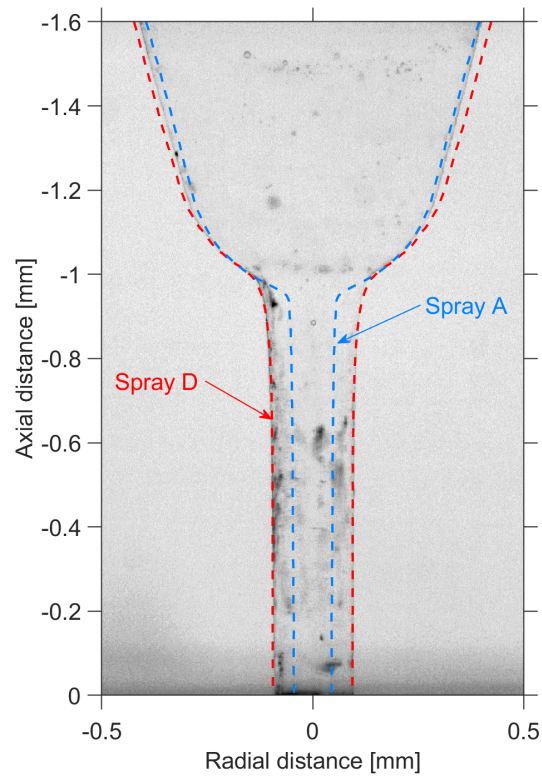


Figure 3: Optical microscopy photograph of the transparent nozzle with comparison to metal nozzle target geometries for ECN Spray A (blue profiles) and Spray D (red profiles).

217 measured metal Spray D nozzle outlet diameter. It can be noted that many  
218 acrylic nozzles of the same geometry were manufactured, and that geometri-  
219 cal characterization via pin gauge insertion or optical analysis showed excel-  
220 lent repeatability. The set of analyzed and used nozzles showed less than 2.5  
221  $\mu\text{m}$  via the pin gauge method (corresponding to the pin gauge diameter reso-  
222 lution), which matched the maximum dispersion from the optical microscopy  
223 measurements exactly, equivalent to 1.3 % total variation in outlet diameter.  
224 Such small nozzle-to-nozzle geometrical differences are noticeably better than  
225 what was observed for Spray A and Spray D metal injectors [23, 24]. Table 1  
226 summarizes parameters relevant to the experiments conducted in this work,  
227 including nozzle geometry, operating conditions and flow characteristics.

228 Surface quality is another important parameter because cavitation has  
229 been observed to be sensitive to surface roughness [25]. Because of the dif-  
230 ferent machining methods used to manufacture the transparent nozzles, com-  
231 pared to EDM or laser-drilled metal injectors, variation in surface quality is  
232 expected. The surface quality of the nozzle was imaged directly with opti-  
233 cal microscopy, with resolution on the order of 0.3  $\mu\text{m}$ . The images showed  
234 left-over machining marks, as well as the effects of abrasive flow machin-  
235 ing. Images acquired in the region between the sac and the orifice entrance  
236 highlighted the effects of abrasive flow machining, effective in the orifice, but  
237 apparently not in the sac, transitioning from relatively large non-oriented  
238 geometrical features to smaller ridge-looking geometries oriented along the  
239 orifice, on the order of a few micrometers in size.

240 Several nozzles were also investigated under a scanning electron micro-  
241 scope (SEM) after one half of the nozzle was removed by high-precision ma-

Parameters	Quantities
Nozzle type	Mini-sac
Orifice diameter	0.186 mm (0.189 mm)
Orifice geometry	Converging
k-factor	1.5 (1.0)
Flow rate (at 10 MPa)	188 g/min
Injected fuel	n-dodecane
Injection pressure	25 - 100 MPa
Ambient gas	N <sub>2</sub>
Ambient pressure	0.1 - 2.0 MPa
Ambient temperature	20°C
Theoretical outlet velocity	253 - 527 m/s
Cavitation number (Ca)	1.0002 - 1.004
Reynolds number (Re)	$5.97 \times 10^4$ - $1.24 \times 10^5$
Weber number (We)	$4.36 \times 10^5$ - $1.89 \times 10^6$

Table 1: Parameters relevant to the nozzle, injection, ambient gas, and flow characteristics for the various conditions tested in this work. The orifice diameter and  $k$ -factor in parentheses indicate measured quantities.

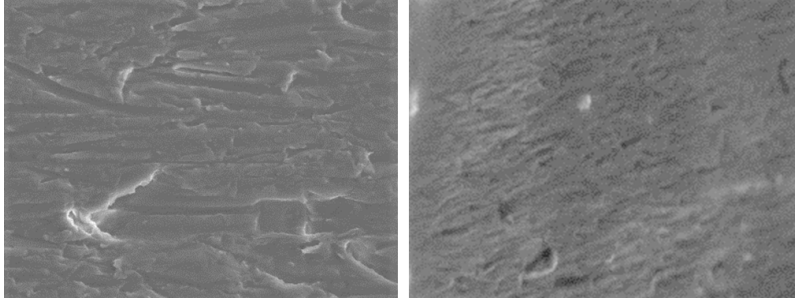


Figure 4: SEM imaging of the geometrical details observed near the orifice exit of a sample transparent nozzle used in this work on the left, and a Spray A injector on the right showing noticeably smaller geometric features. Images are approximately  $16\text{ }\mu\text{m}$  in length and  $12\text{ }\mu\text{m}$  in height.

chining and a thin coat of gold was applied to the samples for electron con-  
duction. The left image of Fig. 4 shows an example of SEM results for a  
transparent nozzle acquired about  $100\text{ }\mu\text{m}$  from the orifice exit. The right  
picture is a similar example of SEM imaging acquired near the orifice exit of  
an ECN Spray A nozzle, to provide a comparison to the geometrical features  
observed in the transparent nozzle. Both images represent equivalent areas  
approximately  $16 \times 12\text{ }\mu\text{m}^2$ , with the long dimension aligned with the orifice  
axis.

The SEM images of the transparent and metal nozzles show apparent  
differences, with visually larger geometrical features resembling ridges and  
crests, extending about half the length of the imaged area, or between 5 and  
 $10\text{ }\mu\text{m}$  long for the transparent nozzle (left image of Fig. 4). These long  
marks contrast with the comparably small features observed on the right  
example for the metal nozzle, with the largest feature in this image only a  
couple of micrometers, with most features below  $1\text{ }\mu\text{m}$ .

### 257 **3. Results and discussions**

#### 258 *3.1. Needle-lift and sac pressurization*

259 The tip of the needle can be observed in the sac of the transparent noz-  
260 zles, thereby offering a direct measurement of needle lift and motion. While  
261 needle motion has been reported by other groups, whether via Foucault sen-  
262 sors attached to the rod, or x-ray phase contrast imaging [15], needle motion  
263 is system-dependent and such measurements are valuable to understand the  
264 impact of needle throttling during opening and closing transient periods. The  
265 needle profile is the result of complex hydraulics initiated as the solenoid is  
266 energized, a control volume above the needle is depressurized, and hydraulic  
267 force on the other side overcomes the force exerted by the spring keeping the  
268 needle closed under non-energized conditions (e.g., see [26]). Visualization  
269 within the transparent nozzle permits visualization of this needle movement  
270 along with flow and fuel pressure indicators to better understand the open-  
271 ing and closing stages of the fuel injector. The needle profiles as function  
272 of time measured during operation under different injection and chamber  
273 pressure conditions are plotted in Fig. 5. The traces were averaged over  
274 five repetitions and are reported with respect to the time after the start of  
275 injection (ASOI), therefore accounting for the hydraulic delay corresponding  
276 to the time between the start of energizing and the actual start of injec-  
277 tion. The light-colored areas around the profiles report the total error of the  
278 mean, combining bias (experimental) and statistical uncertainties, with a 95  
279 % confidence interval [27].

280 The needle lift profiles of Fig. 5 show that, as observed by others previ-  
281 ously on similar injectors, the lift rate is pressure-dependent, with the 100



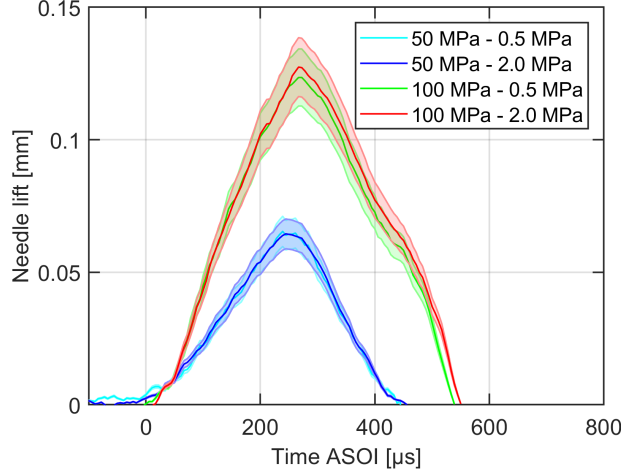


Figure 5: Needle lift as function of time at 50 and 100 MPa injection pressures into 0.5 and 2.0 MPa chamber pressure conditions. The lighter shade areas represent the total error of the mean for these measurements.

282 MPa injection pressure producing faster lift, approximately twice as fast as  
 283 the 50 MPa injection pressure. In both cases, the needle rises for over 250  
 284  $\mu\text{s}$ , to reach peak lifts on the order of 65 and 125  $\mu\text{m}$  from the initial po-  
 285 sition, respectively for the 50 and 100 MPa injection pressure cases. We  
 286 should add that even though energization time was kept constant at 795  $\mu\text{s}$   
 287 for both conditions, total injection duration is substantially shorter for 50  
 288 MPa compared to 100 MPa, as observed in previous works [26, 28]. The rel-  
 289 atively large error-bands are mostly the result of experimental uncertainty,  
 290 as opposed to event-to-event dispersion, and despite the limited number of  
 291 repetitions. Needle motion has been observed to be a fairly repeatable pro-  
 292 cess, in both lift and radial oscillations, as demonstrated by Kastengren et  
 293 al. via x-ray radiography on Spray A injectors [28].

294 The physical properties of the transparent nozzles, namely the slight elas-  
 295 tic deformation of the acrylic nozzles under pressure, allowed correlating the  
 296 deformation in the sac with pressure as function of time. The sac only de-  
 297 forms by a few micrometers, but the highly-resolved imaging systems could  
 298 measure the change in sac diameter, treating the measured elastic deforma-  
 299 tion of the acrylic as an indirect measure of fuel pressure. A calibration for  
 300 fuel pressure was taken at no sac pressure, and at the time of peak needle lift  
 301 at different injection pressures, therefore assuming that the sac reaches the  
 302 upstream pressure during the quasi-steady period of long injections. This  
 303 calibration process showed the linear relationship between deformation and  
 304 pressure, as expected under elastic deformation. Sac diameter measurements  
 305 were taken orthogonal to the injector axis at the sac location of the tip of the  
 306 needle (needle position before energization). It should be noted that pres-  
 307 sure across the sac is assumed constant at a given time. This assumption is  
 308 supported by wave propagation calculations, indicating that pressure waves  
 309 travel across the sac filled with n-dodecane in about  $0.54\text{ }\mu\text{s}$  at  $0.1\text{ MPa}$  sac  
 310 pressure (speed of sound increases with pressure [29]), when the minimum  
 311 interframe time for these experiments was  $5\text{ }\mu\text{s}$ . The measurement estimates  
 312 of the sac pressurization process as a function of time are reported in Fig.  
 313 6 under the different conditions of Fig. 5. These profiles are the results of  
 314 averaging over five injection events, and the total error of the mean is also  
 315 reported for these measurements, via the light-colored areas around the mean  
 316 profiles. It is important to note that these results were extracted with the  
 317 sac and orifice filled with liquid, and that sac pressurization has been found  
 318 to be significantly slower when the sac and orifice contain large amounts of

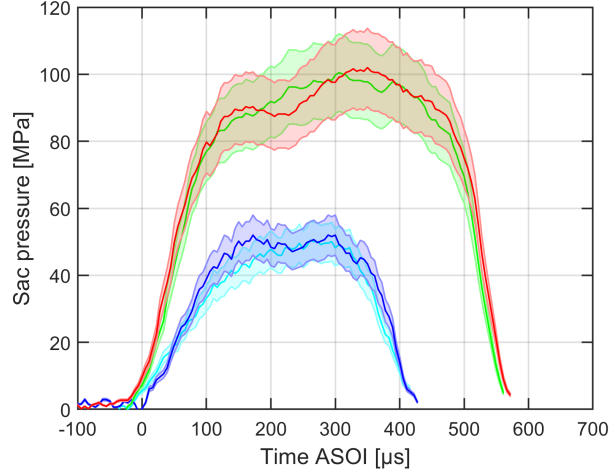


Figure 6: Pressure in the sac estimated as the amount of deformation exhibited by the transparent nozzle as function of time. The light-colored areas represent the total error of the mean for these experiments. Same conditions and style as in Fig. 5.

gas.

By contrast to the needle lift measurements, the estimated sac pressure rises and reaches a steady value, and does so much faster than the needle lift. Note that the sac pressure measurement is admittedly sensitive to noise because of the slight sac displacement, but the behavior is still quite clear. For either injection pressure, stable sac pressures are obtained within 100  $\mu$ s. Note that this behavior is expected if the needle lifts high enough such that the throttling restriction is no longer in the needle-seat area, but within the hole. An analysis of the flow areas at the needle seat compared to the orifice area shows that the needle-seat flow area exceeds the orifice area with only 0.020 mm lift. This requirement is met by 100  $\mu$ s for either injection pressure. Even though the needle lift is higher at 100 MPa, additional time to pressurize the sac may be expected because of frictional losses through

332 the small-passage seat area and the inertia associated with pressurizing all  
 333 fluid already in the sac to a higher pressure. The transient rate of depressur-  
 334 ization appears to be faster than the pressurization ramp up. As noted for  
 335 the needle lift, the magnitude of the total error is mostly attributed to ex-  
 336 perimental uncertainty, rather than injection-to-injection variation. Higher  
 337 resolution imaging experiments would be needed to understand sac pressur-  
 338 ization repeatability. The end of injection dynamics are discussed in the  
 339 following section, bringing supporting evidence for pressure oscillations after  
 340 the needle closes. In summary, the needle lift and sac pressure measurements,  
 341 obtained together, offer new opportunities to understand injector transient  
 342 opening and closing effects.

### 343 *3.2. End of injection gas exchange*

344 At first sight, it may seem odd to describe the end of the injection pro-  
 345 cesses before the start of injection. But to establish the conditions that exist  
 346 within the injector at the beginning of injection, it is important to understand  
 347 the dynamics and processes occurring at the end of previous injections. The  
 348 status of the injector sac and holes will change if created by short, multiple  
 349 injections, or after expansion and compression in an engine. Recent experi-  
 350 ments [12, 13, 15] observed that gas bubbles were present in the sac after the  
 351 end of injection. Mitroglou et al. [12] suggested that these vapor bubbles  
 352 originate from the end of injection cycle, while Swantek and coworkers [15]  
 353 hypothesized that the bubbles come from ambient gas, rather than fuel va-  
 354 por. They found that the presence of gas depends on operating conditions,  
 355 injection and chamber pressures. At the same time, CFD simulations with  
 356 different initializations showed that the presence of gas in the sac and orifice

357 affects initial spray development, vaporization rate and liquid penetration  
358 [16].

359 The high-speed visualizations help understand the phenomena happening  
360 at the end of injection. The two sequences presented in Fig. 7 show examples  
361 of an end-of-injection processes. The top sequence corresponds to the end of  
362 injection when the injection pressure is set to 50 MPa, and the chamber is set  
363 at 2.0 MPa ambient pressure. The bottom sequence features a similar event,  
364 but with a chamber pressure set to atmospheric (approximately 0.1 MPa).  
365 A high-speed video showing a side-by-side comparison of the two events of  
366 Fig. 7 is available as supplemental material (M1). The images show the  
367 transparent injector tip, with the needle inside the sac, located at the top  
368 of the images. The spray exiting the orifice is visible at the bottom of the  
369 frame. The imaging focus is on the sac, needle, and hole, while the emerging  
370 sprays outside of the nozzle are not in focus. Because of the different object  
371 planes caused by whether there is or is not acrylic and fuel along the ray path,  
372 and the limited depth of field of the microscope setup, one must choose best  
373 focus for internal-flow features or the emerging spray. Fortunately, with our  
374 two-camera setup, one camera can be setup for best focus in the sac, and the  
375 other for best focus on the spray, if desired. The time reported in the top of  
376 the frames is taken with respect to the end of injection, or when the needle  
377 closes. No treatment has been applied to these movies, as they come from  
378 the raw data acquired by the high-speed camera of the primary system.

379 The appearance of gas bubbles after the end of injection is clear from  
380 the bottom sequence of Fig. 7, as marked by the darker regions due to a  
381 different refractive index with the fuel (and nozzle material). Comparing the

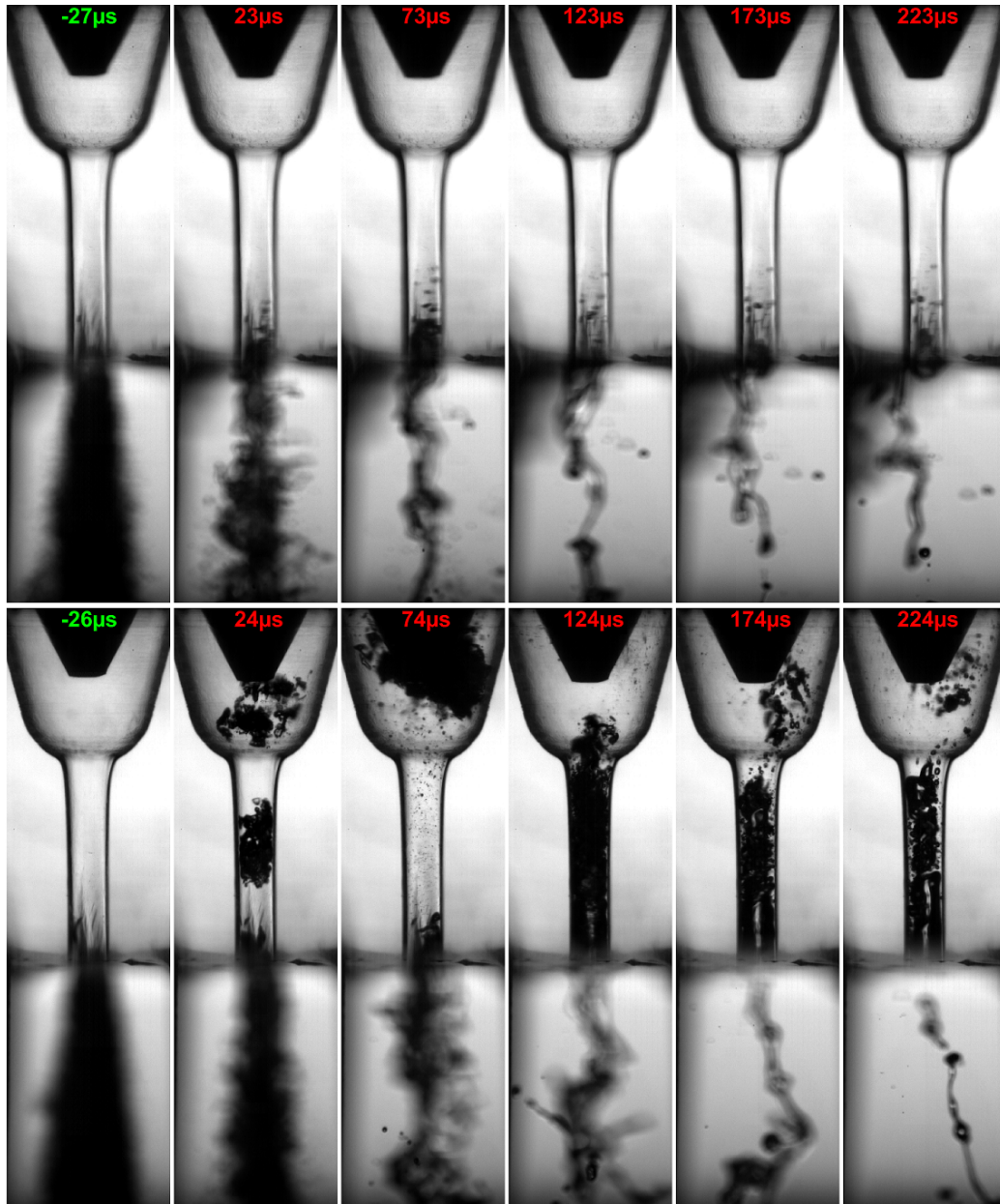


Figure 7: Sequences showing the end of injection processes at two chamber conditions. Top: 50 MPa into 2.0 MPa, no gas exchange is observed; Bottom: 50 MPa into 0.1 MPa, shows bulk cavitation and gas exchange. The top half of all images is the nozzle, where the tip of the needle can be seen, while the chamber is at the bottom. Transparency in the nozzle indicates liquid, with gaseous regions in black, while transparency indicates gas in the chamber, with dark region as liquid.<sup>22</sup> The time indicated at the top refers to the time with respect to needle closing.

low-pressure sequence to the higher chamber pressure condition, where the sac remains filled with liquid fuel, a large amount of gas can be observed in the sac after the injection ends. This low-pressure chamber operating point was chosen as an example condition to enhance the differences and slows down the process such that the phenomena are clearly identified. The low-pressure experiments show that when the needle closes, cavitation forms near the needle seat and moves downstream closer to the tip of the needle (from needle closing to 24  $\mu$ s). Cavitation may also occur in the orifice, as shown by the bubbles present in the hole at the same time. A short time later (74  $\mu$ s), the fuel vapor region has grown to almost fill the sac visually. The phase change occurs in the bulk of the sac, and it does not appear to be connected to fast moving sections of fluid. This bulk cavitation process can occur if there is an intense pressure drop throughout all of the fluid, analogous to a fluid-hammer effect in piping systems, where fuel flowing at high-speed, carrying inertia and momentum, is suddenly throttled. For a brief instant, the pressure locally drops below the vapor pressure of the fuel, inducing the fuel to change phase into vapor. The fluid in the sac quickly relaxes back to higher pressures (above the vapor pressure point), thus changing the vaporized fuel back into liquid, collapsing the vapor fuel bubbles. The volume change in the nozzle sac region induced by the collapse rapidly pulls gas from the chamber into the orifice and sac (124  $\mu$ s and forward), leaving the orifice and sac with chamber gas.

The high-speed movies and movements of the vapor regions seen in the supplemental material can be used as tracers to understand the pressure behavior in the nozzle during the end of injection and gas exchange processes.

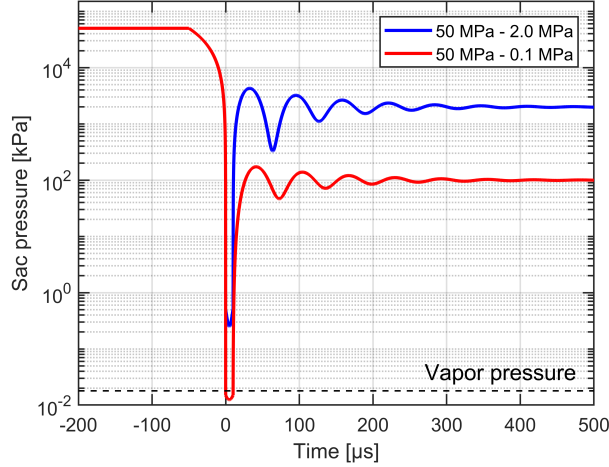


Figure 8: Damped harmonic oscillator model representing the pressure in the sac around the end of the injection period, when the needle closes the fuel passage at the seat immediately upstream of the sac for the two conditions shown in Fig. 7.

Figure 8 offers a depiction of the process from the perspective of the pressure in the sac, comparing the two sequences of Fig. 7. Initially high during injection, the sac pressure quickly drops as the needle makes contact with its seat, momentarily reaching values below the vapor pressure of the fluid under certain conditions. The pressure goes back up in an oscillatory manner until it stabilizes at the chamber pressure.

The model description provided in Fig. 8 was built based the observations made at various conditions, showing the oscillatory behavior regarding bulk cavitation following the closing of the fuel passage at the needle seat region, coinciding with the end of the injection. Though not shown here, certain conditions even showed bulk cavitation happening, then collapsing, and happening again at lower intensity, further providing supporting evidence of the oscillatory/periodic behavior shown in Fig. 8. Such observations were



made for cases with high injection pressure and low chamber pressure, favoring both an intense fluid hammer and an already low sac pressure. The elastic properties of the system composed of the transparent nozzle, the needle, and the injected fluid, drive the acoustic characteristics of the system, which appears to behave like a damped harmonic oscillator [20]. The different material used for the transparent nozzle is likely to modify the acoustic characteristics compared to the metal nozzle target, increasing the damping properties of the system, meaning that higher bulk cavitation intensity should be expected in metal nozzles.

Our findings support the experimental observations made by Swantek et al. [15], as well as the numerical simulations by Battistoni et al. [16] suggesting that ambient gas is ingested into the sac after the end of injection. However, with high-speed visualization, we were able to ascertain these claims and clarify the underlying mechanism: Cavitation formed in the bulk of the fluid, collapses to ingest gas into the injector. Note that while Battistoni et al. [16] predicted cavitation at similar operating conditions (0.1 MPa ambient pressure) at the end of injection, the cavitation was confined to the needle-seat area, whereas our experiments at comparable conditions show cavitation regions in the sac and orifice.

Recent experimental evidence by Abers and coworkers [30] using the same experimental setup described earlier in this manuscript linked the gas trapped in the sac to the fuel dribble observed after the end of injection during the expansion and exhaust phases in diesel engines [31]. The decreasing pressure inside the combustion chamber, or constant flow chamber, induces a volumetric expansion of the gas bubbles still in the sac, resulting in the left-over

Injection pressure	Chamber pressure			
	0.1 MPa (1 atm.)	0.5 MPa	1.0 MPa	2.0 MPa
25 MPa	✓	✓	✗	✗
50 MPa	✓	✓	✓	✗
100 MPa	✓	✓	✓	✓

Table 2: Summary of the observations made over various test conditions regarding bulk cavitation and the presence of gas left over after the end of injection. The tick mark corresponds to an operating condition where bulk cavitation and gas exchange in the sac is observed (Fig. 7, bottom), while a cross indicates no cavitation-induced gas exchange (Fig. 7, top).

liquid fuel to be expelled through the orifice(s).

The various experimental conditions tested in this work also correlate with the findings reported by Swantek et al. [15] about the presence or absence of gas bubbles as function of ambient gas pressure. With increasing ambient gas pressure, fewer bubbles are found in the sac, a change more significant than just the expected change in gas volume with increasing pressure. Table 2 summarizes the observations made across the different test conditions within our transparent nozzles, which are consistent with the aforementioned results, suggesting that operating conditions, rather than nozzle geometry, dominate the phenomenon.

The table shows that, in general, higher injection pressure favors bulk cavitation, as shown in the bottom sequence of Fig. 7, due to a more-intense fluid deceleration at needle closing, resulting in a larger pressure drop in the sac and orifice. At the same time, higher ambient pressure reduces the likelihood of cavitation, either in the bulk, or in flow-separation regions within the injector. This is explained by the equilibrium pressure point in

461 the nozzle being higher above the vapor pressure of the fluid, making it more  
462 difficult for the local pressure to drop as low as the vapor pressure point and  
463 cause bulk cavitation of the fuel.

464 As anticipated, the rounded and tapered nozzle does not show signs of  
465 significant cavitation at the inlet of the orifice during steady-state operation  
466 under the range of conditions tested in this work. Other sharp-edge-inlet  
467 nozzles that had no hydro-erosion operation (experiment performed but not  
468 shown in this paper), did show signs of cavitation at the inlet, as has been  
469 shown previously (e.g. [7]).

### 470 *3.3. Nozzle status and start of injection*

471 The experiments show that a significant amount of gas can be left over in  
472 the sac and orifice after the end of injection, which, as explained earlier, can  
473 affect the next injection. The residual gas present in the sac and orifice will  
474 be entrained with the liquid flow at the start of the following injection event,  
475 as shown numerically by Battistoni et al. [16]. Experiments were performed  
476 with different sac status, from almost completely empty to completely full,  
477 within what the experiments allow. Figure 9 presents two extreme examples,  
478 with one injection starting with the sac and orifice nearly full of gas (no  
479 liquid), and another similar injection condition, but with the sac and orifice  
480 full of liquid (no gas). A high-speed video showing a comparison of the start  
481 of injection between an event with the sac full of gas and another with the  
482 sac full of liquid is available as supplemental material (M2).

483 The difference between these two movies (M2) is clear at the start of  
484 injection. When filled with chamber gas, a substantial amount of time is  
485 needed for the sac and orifice to be filled with liquid as it mixes with the gas

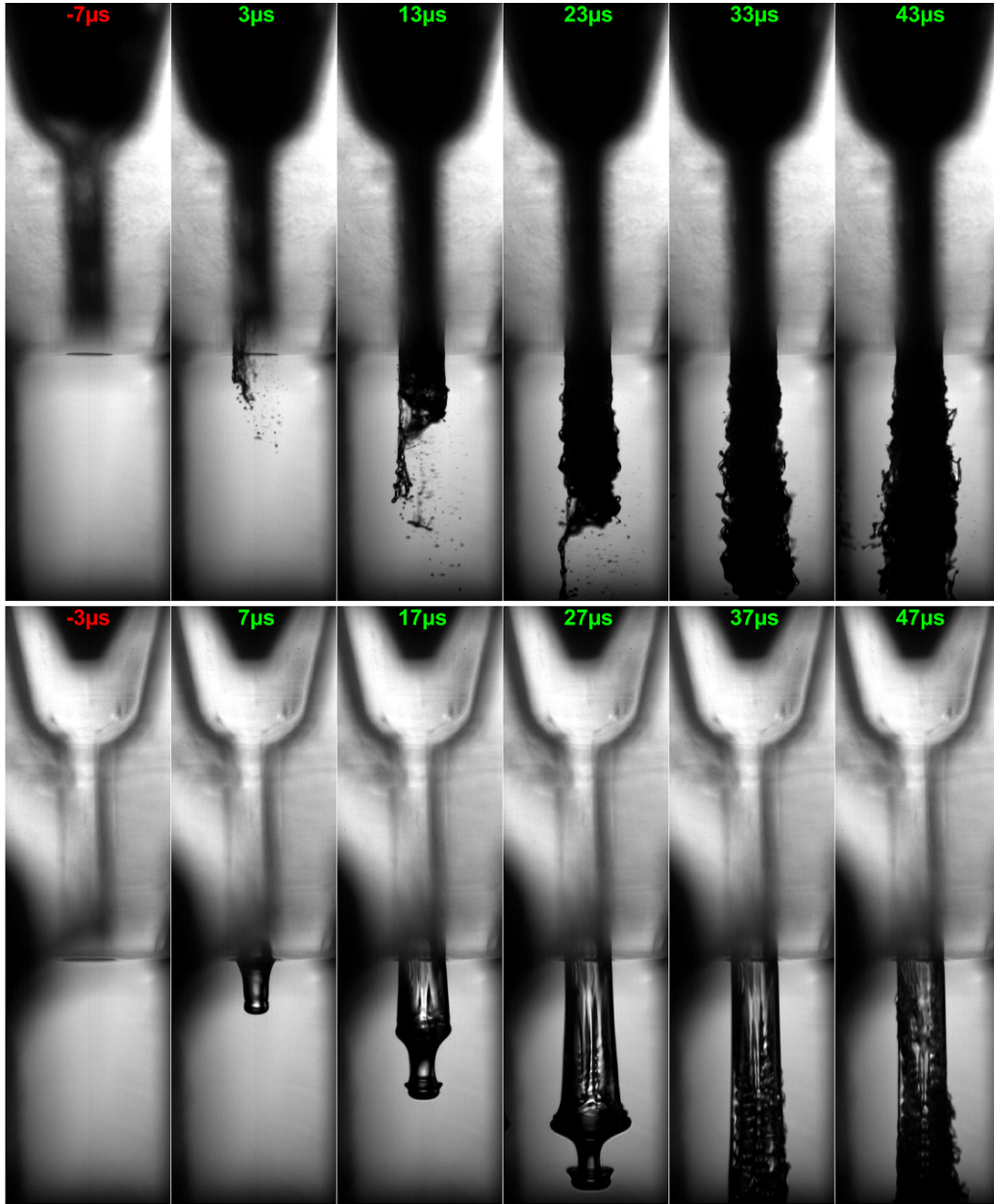


Figure 9: Sequences showing the start of injection with different sac status regarding the presence of gas. Top: 25 MPa into 0.1 MPa, sac and orifice full of gas; Bottom: 50 MPa into 0.1 MPa, nozzle full of liquid. The time indicated at the top refers to the time with respect to the start of injection.

486 present in the nozzle. Across the different sac and orifice conditions tested  
487 during this campaign, it appeared that the time required for the flow to  
488 clear the nozzle of gas depends, as expected, on the quantity of gas initially  
489 present in the nozzle. This is indicated by the shadow produced by the  
490 gas contained in the sac, as opposed to the relatively clear sac and orifice  
491 when filled with fuel. Contrasting with the empty nozzle, the sac and orifice  
492 initially full of liquid feature an intact liquid body flowing out of the hole.  
493 Spray development, such as initial tip penetration or spray dispersion, also  
494 appears to be affected by the initial status of the sac and orifice, whether gas  
495 is present or not.

496 Another interesting aspect of the initially full sac and orifice is that a small  
497 amount of gas is pulled from the ambient into the orifice prior to the start  
498 of injection (as seen in the frame captured 3  $\mu\text{s}$  before the start of injection).  
499 This is attributed to the slight needle lift following the opening of the control  
500 volume [28], producing a volume change significant enough for some gas to  
501 enter the orifice. With gas already in the orifice, the first liquid flowing out of  
502 the orifice (7  $\mu\text{s}$  after the start of injection in the bottom sequence of Fig. 9)  
503 already carries momentum as it accelerates through the orifice and exits the  
504 nozzle at a non-zero velocity. An implication of this observation, either from  
505 a sac initially or partially full of gas, or from the immediate gas ingestion at  
506 the beginning of needle movement, is that the initial rate of injection at the  
507 start should not be zero, as suggested by Manin et al. [18].

508 Detailed microscopic images of the initial flow exiting the orifice also  
509 presents interesting features when the nozzle is initially full of liquid. As  
510 shown in Fig. 9, geometrical aspects of the flow have been imaged by the

511 high-speed microscopic systems. These sample images show the first 10 to 20  
 512  $\mu\text{s}$  after the flow exits the nozzle. The near-field flow images at the start of  
 513 injection present smooth geometries and surfaces, as expected with laminar  
 514 flows, showing noticeable light transmission. With imaging inside the nozzle,  
 515 which showed ingestion of gas into the hole, we can see that the initial thin  
 516 section of liquid originates from liquid-gas interfaces formed within the hole,  
 517 not outside of the hole. Also, features such as the initial mushroom shape of  
 518 the spray head, surface ripples or thin liquid films and sheets can be observed.  
 519 The later timings have further time for sac pressurization and velocity in-  
 520 crease, as given in the rightmost photographs. The structures in these images  
 521 are signs that the flow is accelerating, inducing aerodynamic wave oscillations  
 522 on the flow surface. As expected due to the high flow velocities, subsequent  
 523 timings (not shown in Fig. 9 but available in supplemental material M2)  
 524 highlight the turbulent nature of the spray. The high-magnitude light atten-  
 525 uation is believed to be the result of the multiple droplets surrounding the  
 526 core of the sprays, as well as the highly-curved surfaces of the core. Another  
 527 aspect highlighted by the video sequence available in supplemental material  
 528 M2 is the filling process of the sac and orifice with liquid, when the sac and  
 529 orifice are initially contain gas. In this example, it takes about 200  $\mu\text{s}$  for  
 530 the gas to be completely evacuated, and the sac and orifice to be filled with  
 531 liquid. Considering the typically short injections performed in modern diesel  
 532 engines, the initial status of the sac and orifice with respect to gas content  
 533 appears to be of high importance.

#### 534 4. Summary and conclusions

535 Stereoscopic high-speed microscopy was applied to investigate the internal  
536 flow details of high-pressure injections. Transparent nozzles were designed  
537 based on the well-studied Engine Combustion Network hydro-eroded Spray  
538 D. The transparent nozzles were mated to a modified ECN Spray A solenoid-  
539 actuated injector, and detailed high-speed visualizations were performed at  
540 injection pressures upward of 100 MPa. The injector and transparent nozzles  
541 were mounted inside an optically-accessible pressure vessel, with simulated  
542 chamber pressure conditions up to 2.0 MPa in this work, matching the ECN  
543 Spray A target ambient density. The geometries of the nozzles were investi-  
544 gated in detail via optical microscopy and scanning electron microscopy to  
545 ensure that the target nozzle geometries were closely matched.

546 The temporal information obtained using a synchronized and spatially-  
547 correlated two-camera imaging system operating at speeds greater than 100  
548 kHz allowed measurement of the needle motion, internal flow features, and  
549 the emerging spray structure. The high spatial resolution of the system  
550 enabled monitoring of the elastic deformation of the acrylic nozzle, which  
551 was used to extract information about the sac pressurization process. Beyond  
552 the typical cavitation behavior observed in cylindrical nozzles, the temporal  
553 information obtained from the different injection events revealed that the end  
554 of injection produces a fluid hammer responsible for bulk cavitation of the  
555 fuel present in the sac under realistic conditions. The subsequent collapse  
556 and volume change ingests gas from the chamber, thus leaving the sac and  
557 orifice partly filled with chamber gas. The gas present in the sac greatly  
558 affects the following injection, with gas being injected with the liquid fuel for

559 a substantial amount of time, thereby reducing fuel mass flow rate.

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