



Sandia  
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# Identification of nominally nonporous $H_2$ physisorbents via graph theory-based descriptors of MOF flexibility

## PRESENTED BY

Matthew Witman<sup>1</sup>, Sanliang Ling<sup>2</sup>, Andreas Schneemann<sup>1,3</sup>, Pavithra Wijeratne<sup>1</sup>, Robert Horton<sup>1</sup>, Justin Wong<sup>1</sup>, Vitalie Stavila<sup>1</sup>, Mark Allendorf<sup>1</sup>

<sup>1</sup> Sandia National Laboratories, Livermore, CA USA

<sup>2</sup> University of Nottingham, Nottingham, UK

<sup>3</sup> Technical University of Dresden, Dresden, Germany



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## Collaboration Group:

Nottingham University – Sanliang Ling

Sandia National Laboratories – Andreas Schneemann, Pavithra Wijeratne, Robert Horton, Justin Wong, Vitalie Stavila, and Mark Allendorf

## Funding:

The authors gratefully acknowledge research support from the U.S. Department of Energy, Office of Energy Efficiency and Renewable Energy, Fuel Cell Technologies Office through the Hydrogen Storage Materials Advanced Research Consortium (HyMARC).

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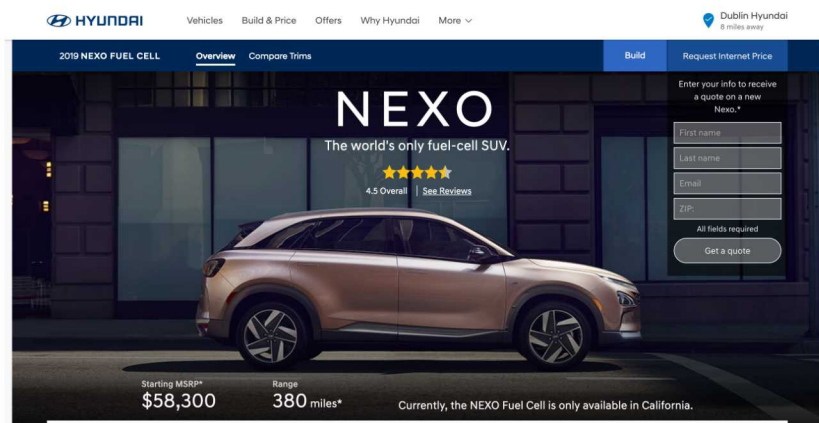
## Economical storage of hydrogen is critical for enabling a variety of zero emission technologies



Commercially available fuel cell vehicles with physical-based hydrogen storage:



<https://www.businessinsider.com/this-toyota-fuel-cell-car-can-power-your-house-2014-11>



<https://www.hyundaiusa.com/nexo/index.aspx>

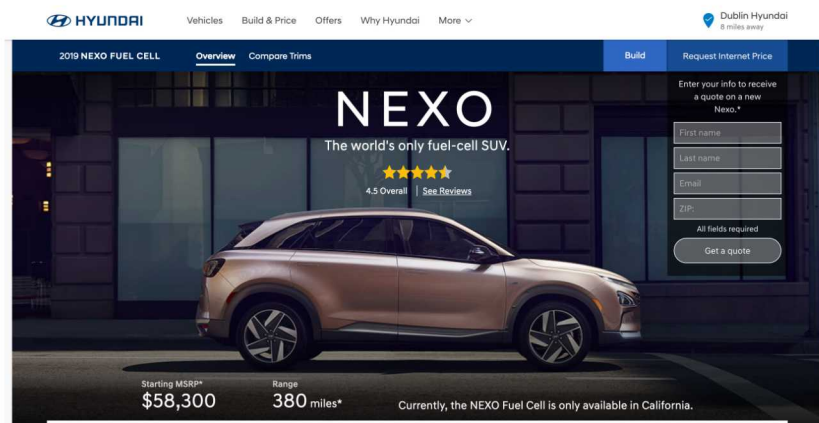
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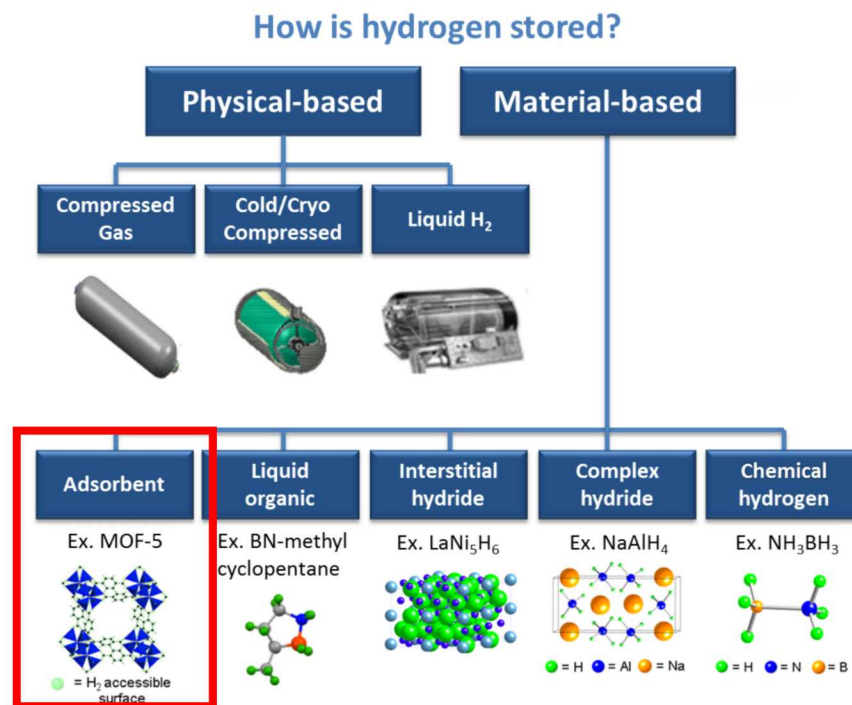


<https://www.businessinsider.com/this-toyota-fuel-cell-car-can-power-your-house-2014-11>



<https://www.hyundaiusa.com/nexo/index.aspx>

A material that meets all DOE technical targets for on board hydrogen storage could help send the technology mainstream:



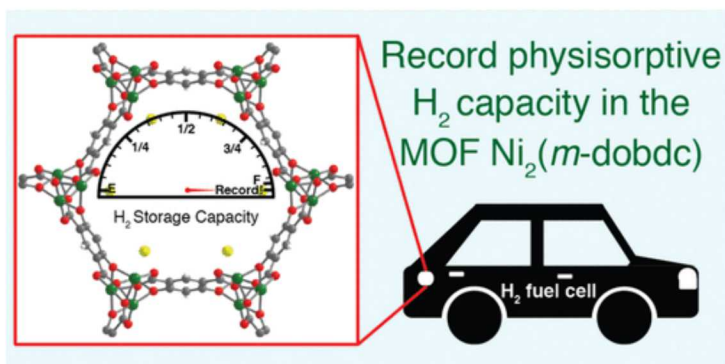
<https://www.energy.gov/eere/fuelcells/hydrogen-storage>



# Physisorbents are attractive due to fast kinetics, but suffer from low volumetric capacities due to weak H<sub>2</sub> interactions



Solution 1: Rationally design best H<sub>2</sub> binding sites at highest possible volumetric density



Kaplelewski, M. et al. *Chem. Mater.* 2018, 30, 22, 8179-8189

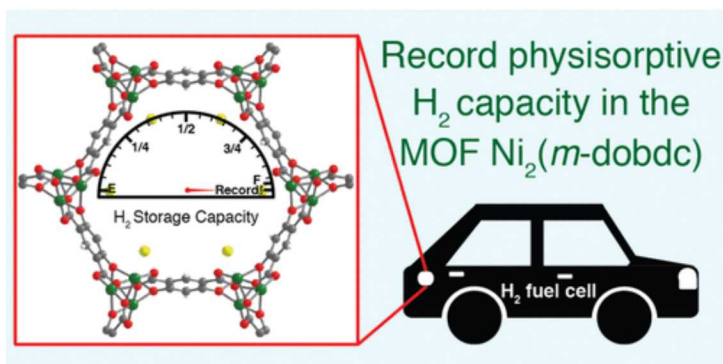


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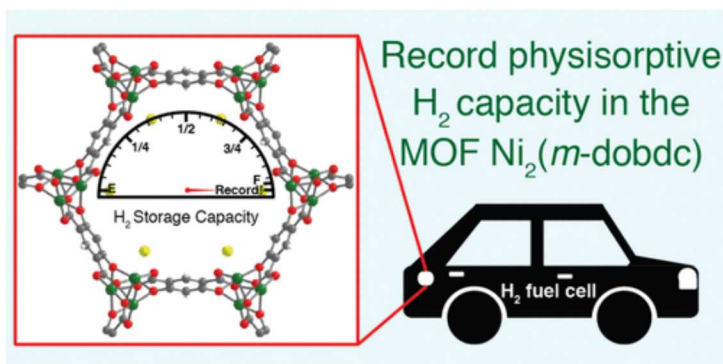


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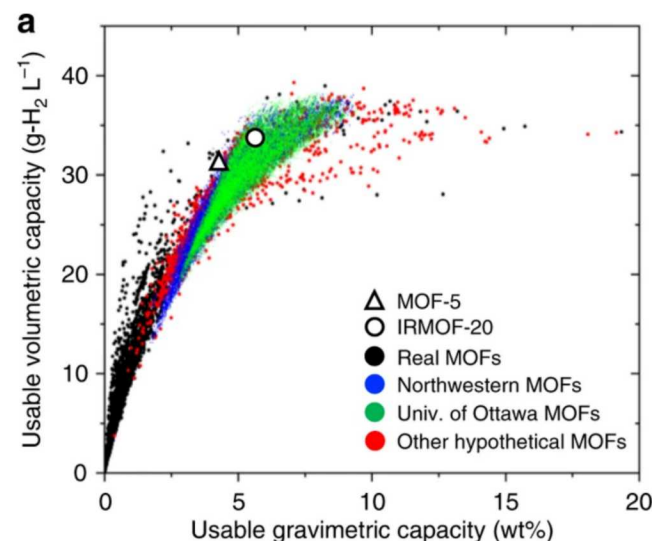


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Witman, M. et al. *J. Phys. Chem. C* 2017, 121, 2, 1171-1181

Solution 2: High-throughput screening of known chemical space to identify top adsorbents



Ahmed, A. et al. *Nat. Commun.* 2019, 10, 1568

## High-throughput screening may miss promising H<sub>2</sub> physisorbents due to two approximations (made for computational tractability)



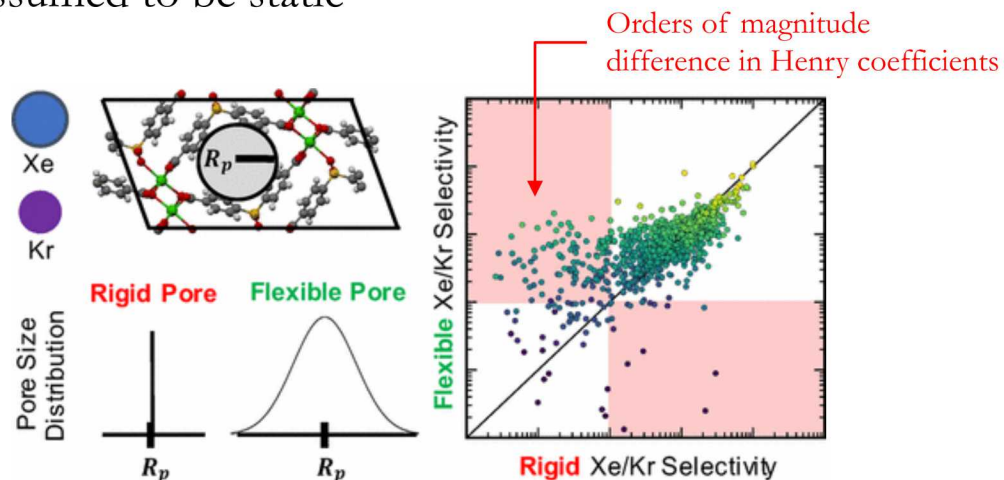
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2. Structures are assumed to be static

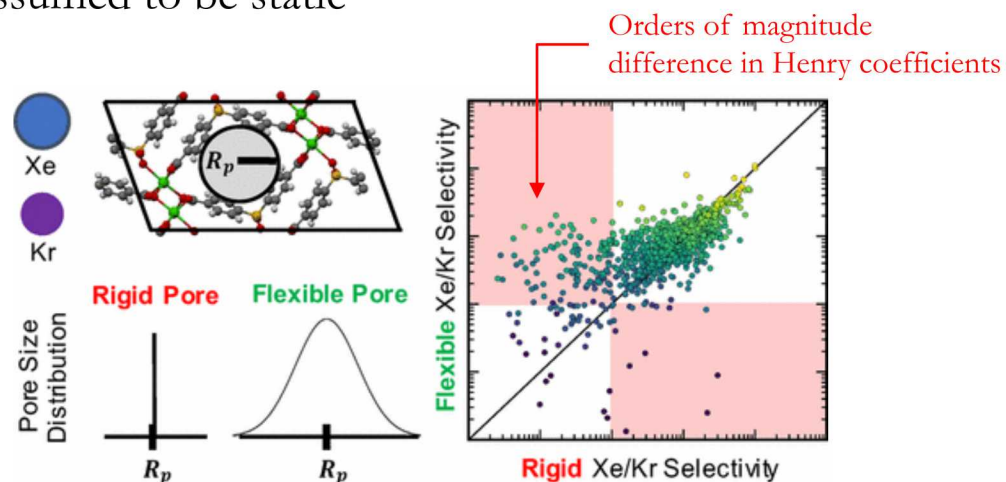


Witman, et al. *J. Am. Chem. Soc.* 2017, 139, 15, 5547-5557

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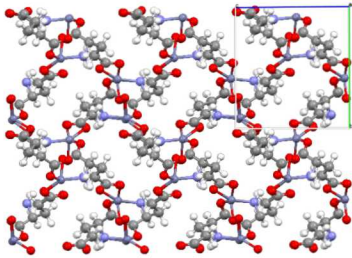


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**3. Research question:** How do we efficiently identify these materials that are nominally non-porous, but are sufficiently flexible that H<sub>2</sub> adsorption is energetically favorable?

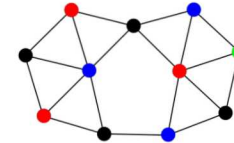
6

## Graph theory-based, high-throughput porous materials' analyses are enabled by open-source **LAMMPS Interface**



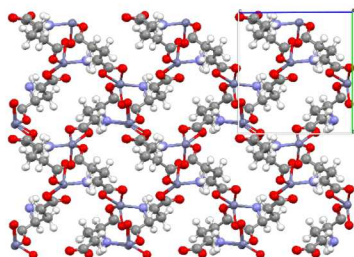
build passing docs passing pypi package 0.1.2

**LAMMPS Interface**



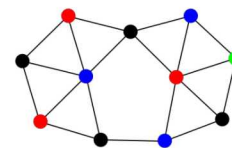
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    { 'element': 'C',  
      'hybridization': 'sp3',  
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  { ('1', '2') :  
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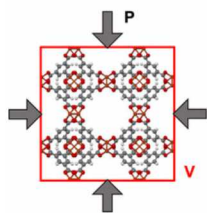
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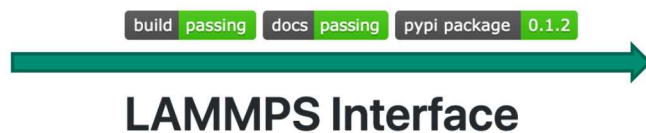
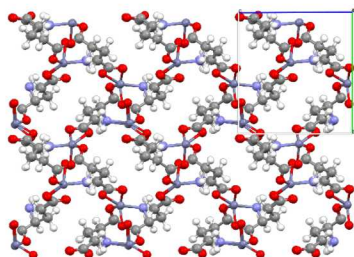
E.g. LAMMPS Interface + graph theory screening has enabled:

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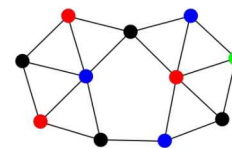


Boyd, et al. *J. Phys. Chem. Lett.* 2017, 8, 2, 357-363

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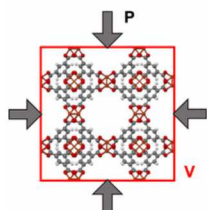
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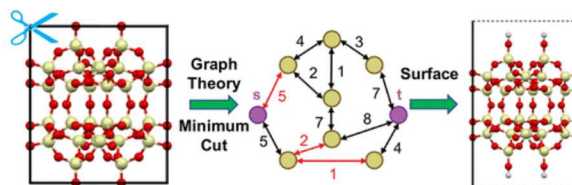
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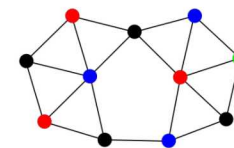
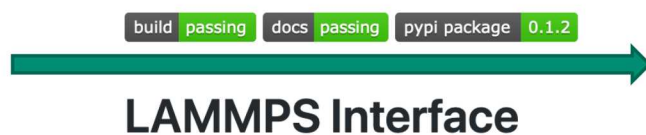
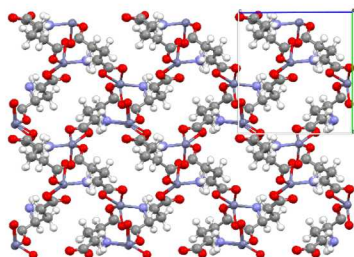


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Witman, et al. *ACS Cent. Sci.* 2018, 4, 2, 235-245



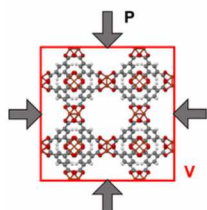
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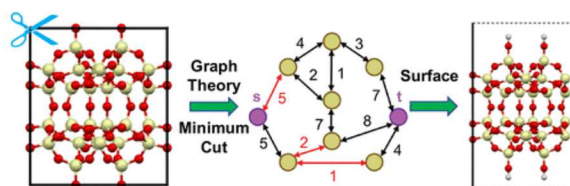
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3. High-throughput identification of flexible MOFs via graph search

**This Work**

## Hypothesis: MOFs containing saturated organic components are likely to display a significant degree of flexibility

### 1. Preliminaries:

$G = (V, E)$  be the MOF's connected, undirected graph

$R \equiv$  the set of all nodes considered rigid

$F \equiv$  the set of all nodes considered flexible

$V' \equiv$  the vertices in a connected subgraph of  $G$

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$f_\alpha$ : a node belongs to  $F$  if it is an  $sp^3$  hybridized, non-metal atom

$f_\beta$ : a node belongs to  $F$  if it is an  $sp^3$  hybridized, non-metal atom and is bonded to at most two other (non-H) atoms

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### 4. Objectives:

$$L = \{V'_1, V'_2, \dots, V'_{|L|}\} \mid (V'_1 \cap V'_2 \dots \cap V'_{|L|} = \emptyset) \wedge (V'_1 \cup V'_2 \dots \cup V'_{|L|} = F)$$

$$N = \{|V'_1|, |V'_2|, \dots, |V'_{|L|}|\}$$

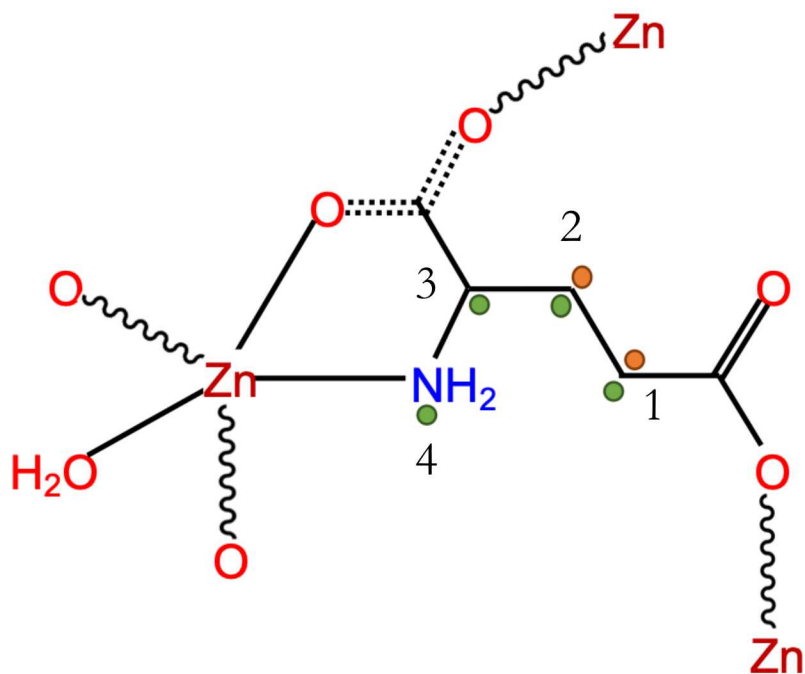
**I.e. what are all the independent, flexible subgroups in the MOF ( $L_\alpha$ ) and how big are they ( $N_\alpha$ ) ?**



[illegible]



2D sketch of a MOF building unit (4 linkers per unit cell):



$f_{\alpha}$  objectives:

$$L_{\alpha} = \{\{1,2,3,4\}, \dots\}$$

$$N_{\alpha} = \{4,4,4,4\}$$

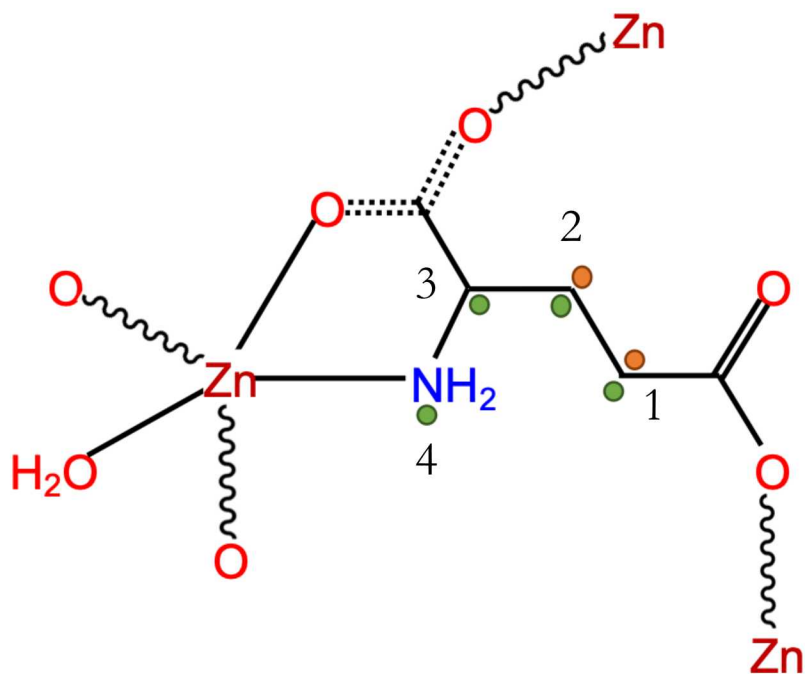
$f_{\beta}$  objectives:

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$f_\alpha$  descriptors:

$$\min(N_\alpha) = 4$$

$$\phi = \frac{\sum N_\alpha}{\# \text{ atoms}}$$

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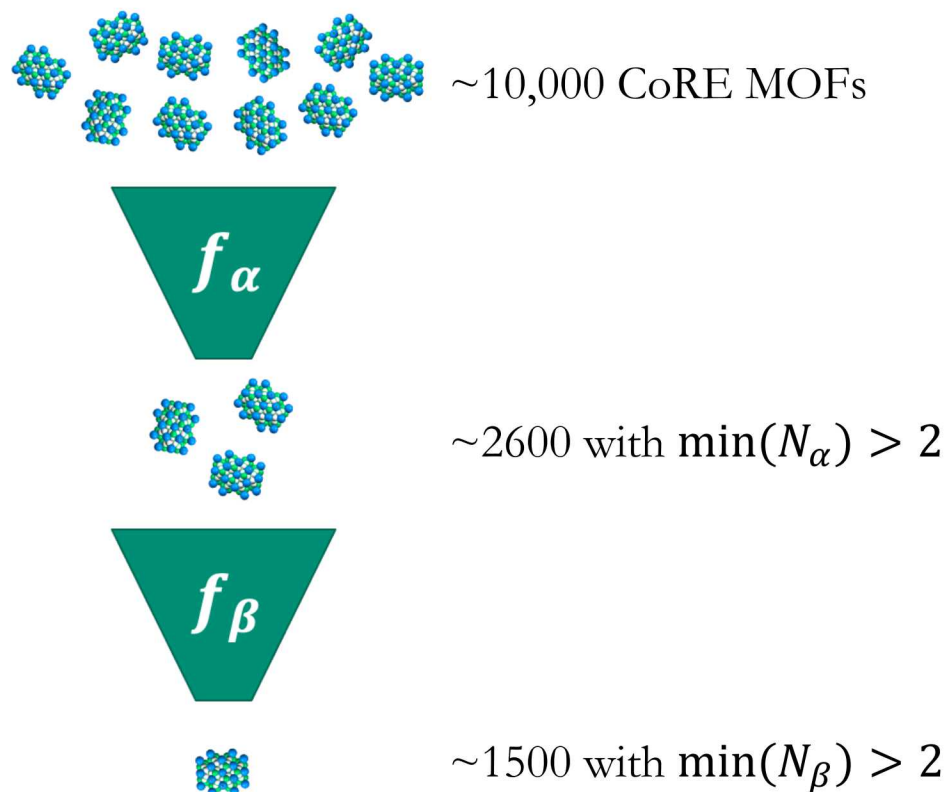


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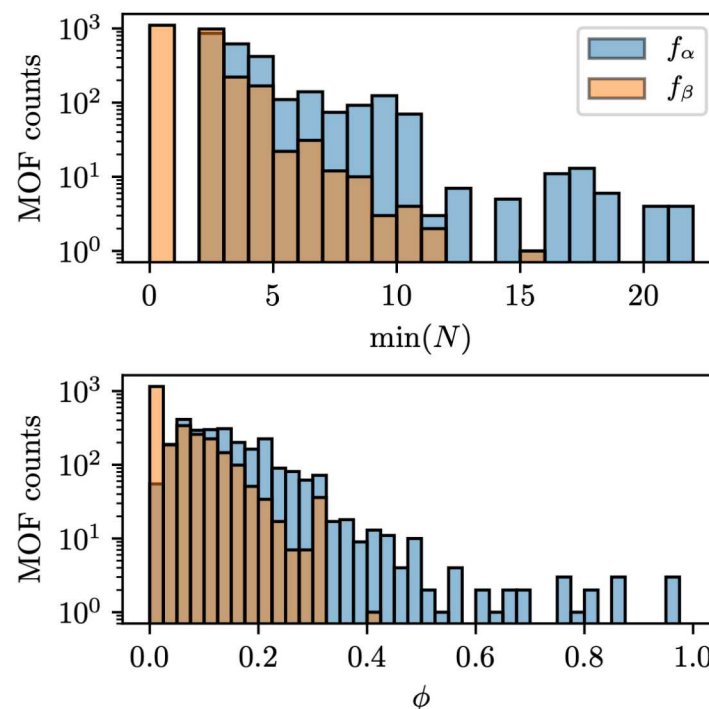
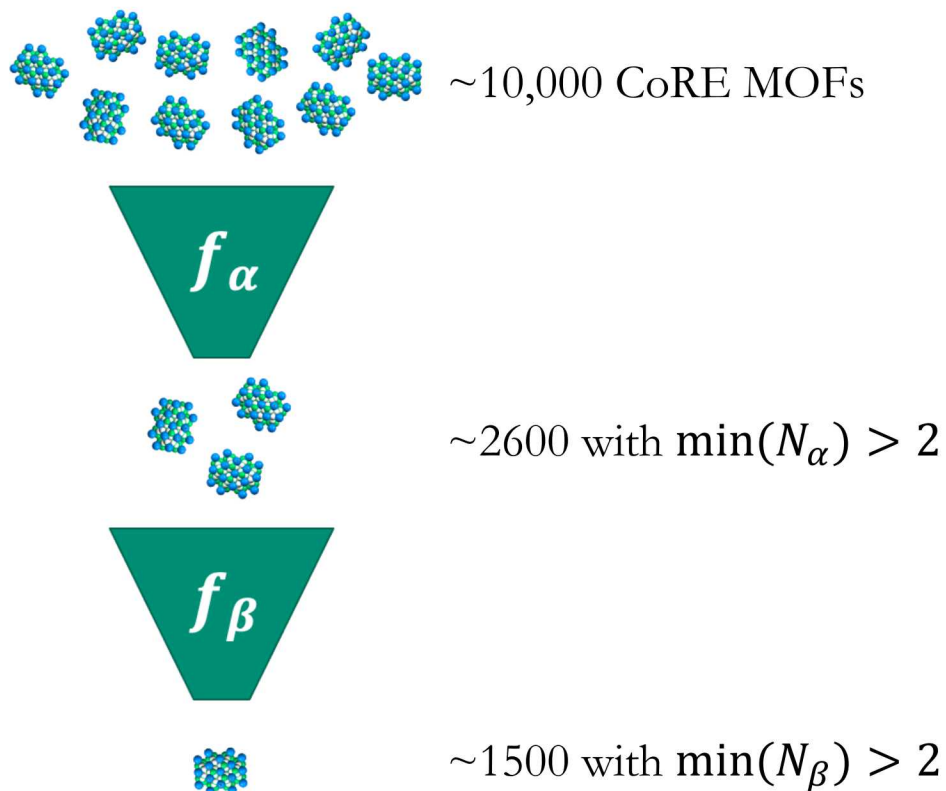
$$\min(N_\beta) = 2$$

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# Automated extraction of CoRE MOFs deemed to be flexible from graph theory descriptors



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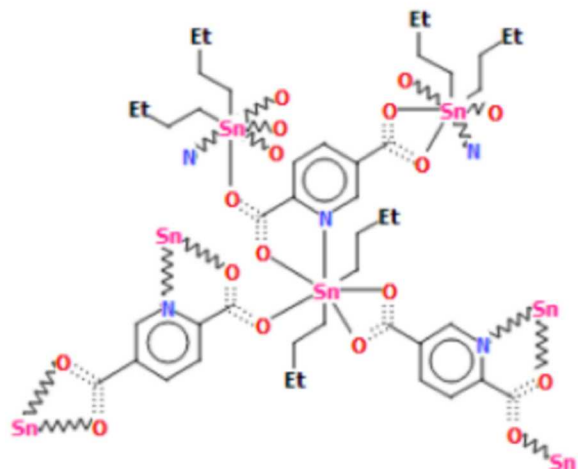




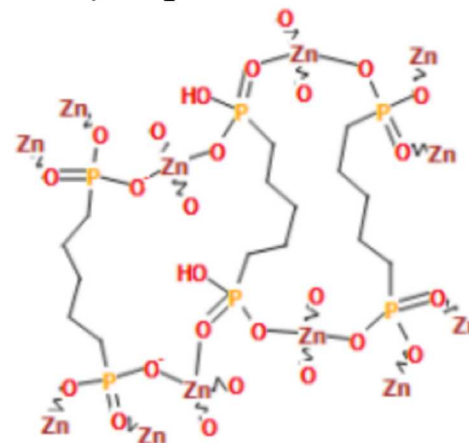
# Structurally diverse flexible moieties are identified by the graph theory screening



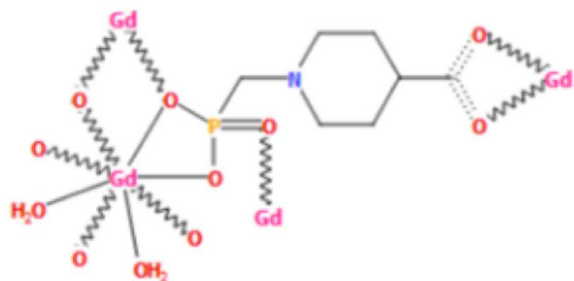
Flexible side chains:



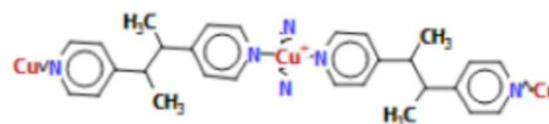
Fully aliphatic backbone:



Saturated ring backbone:



Aliphatic backbone hinges:





## II Computational adsorption experiments portend favorable H<sub>2</sub> adsorption despite “non-porous” 0K structure

DFT calculations on materials with:

1.  $\min(N_\beta) > 2$
2. Pore size similar/slightly smaller than H<sub>2</sub>
3. Contain open metal sites (strong H<sub>2</sub> binding sites)

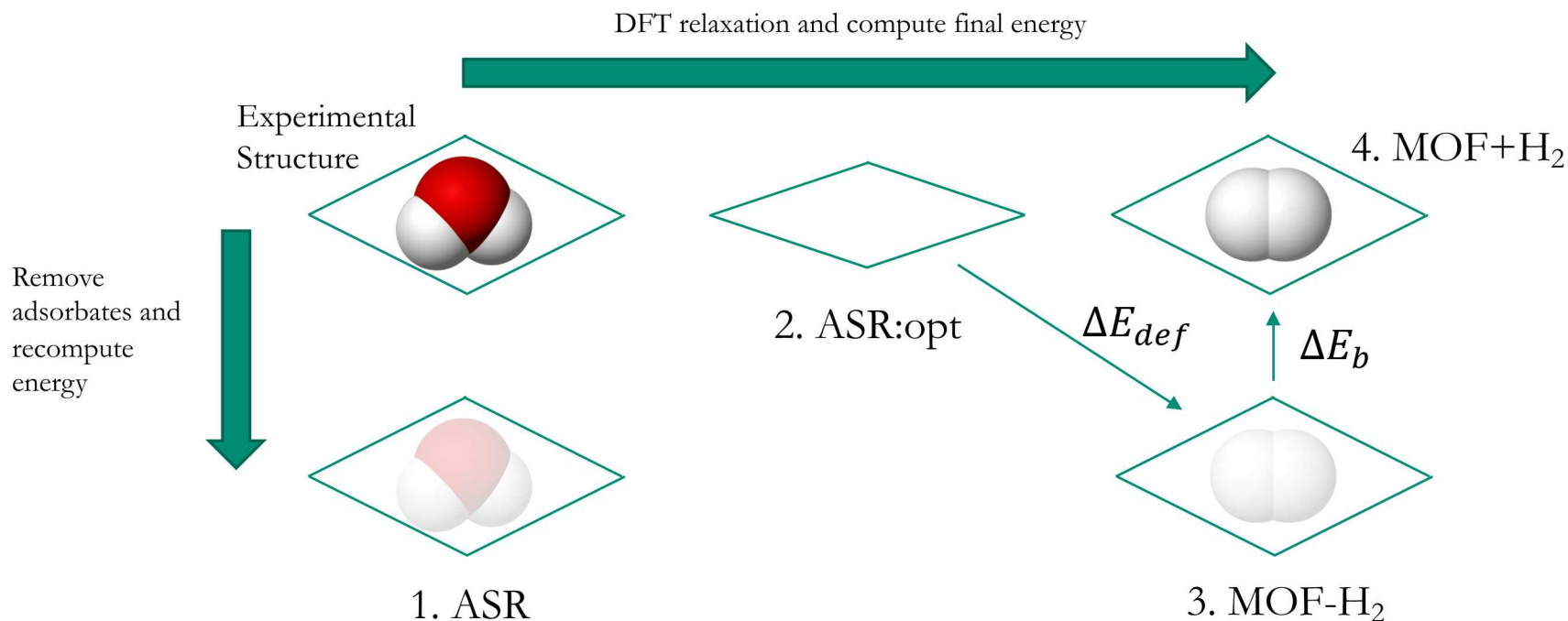
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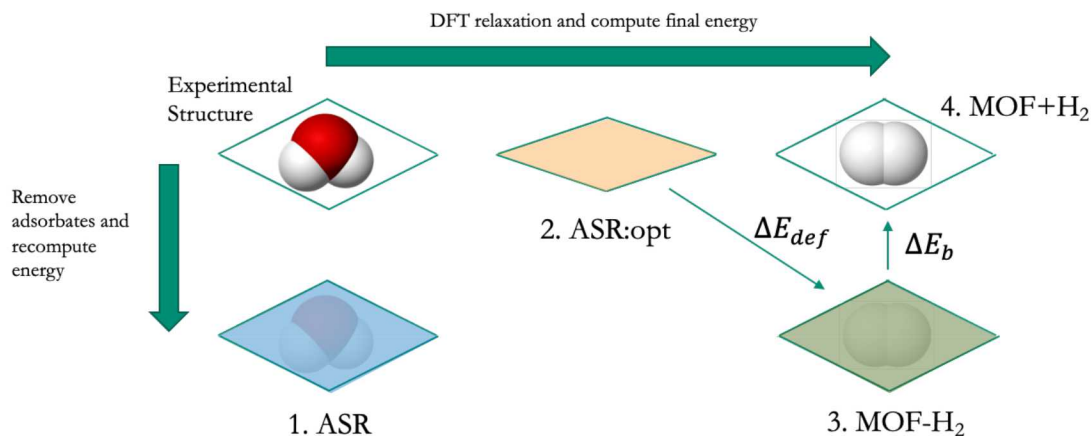
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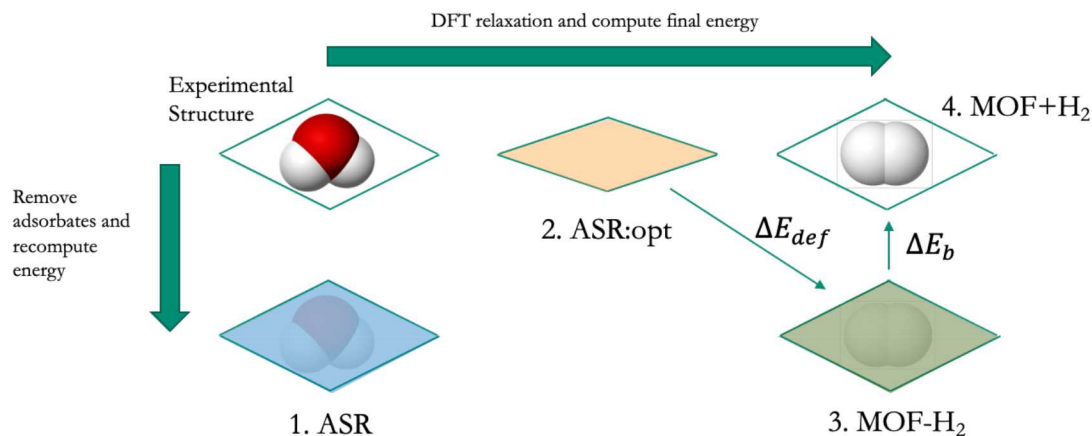
Compute energies/geometries of various adsorption states:



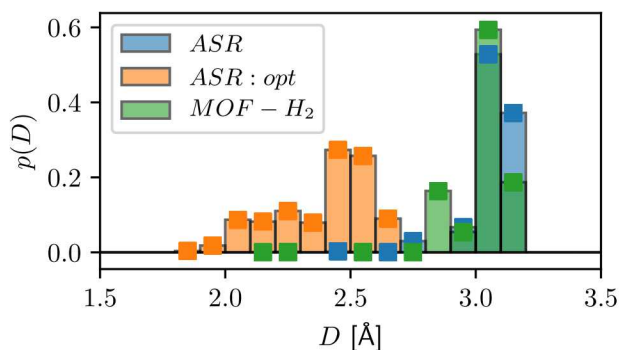
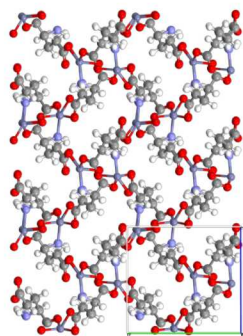
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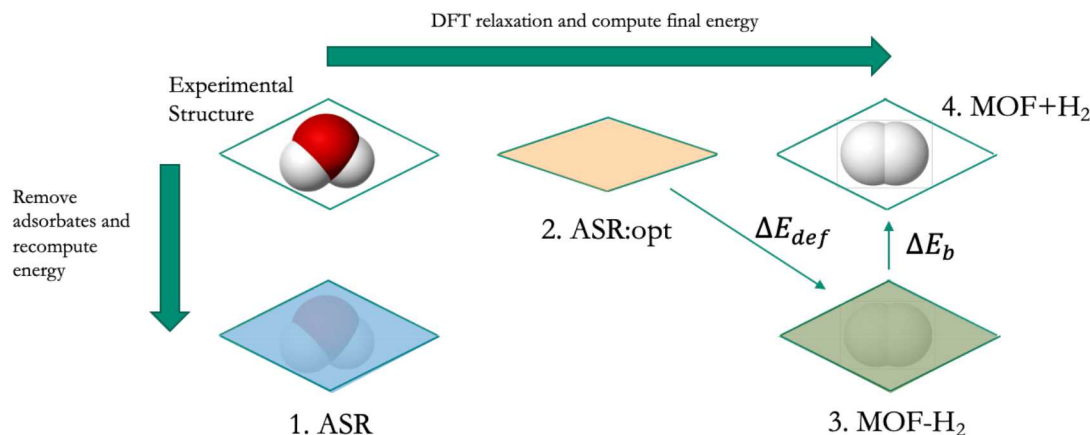


1. Entirely non-porous minimum energy state:

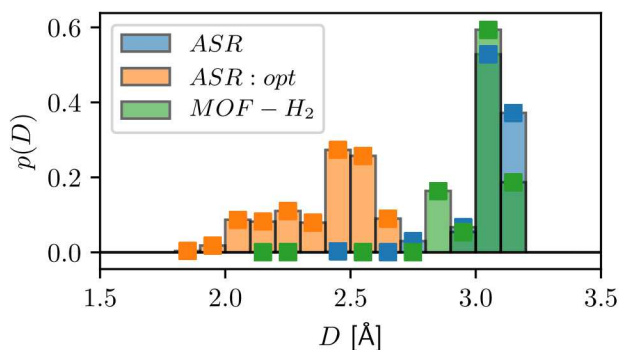
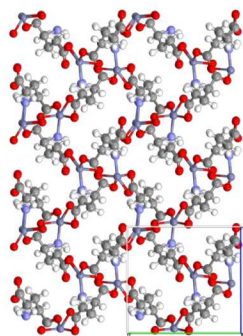




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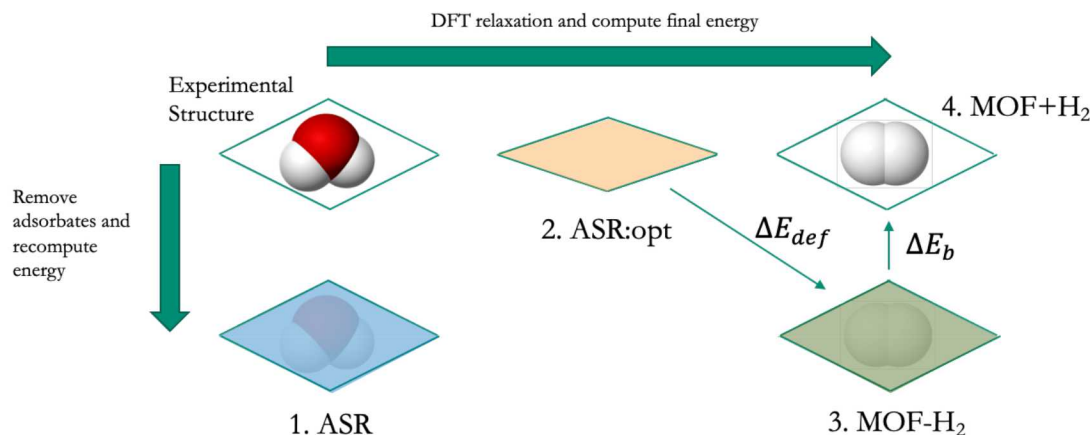


2. Highly favorable H<sub>2</sub> binding yields overall favorable process

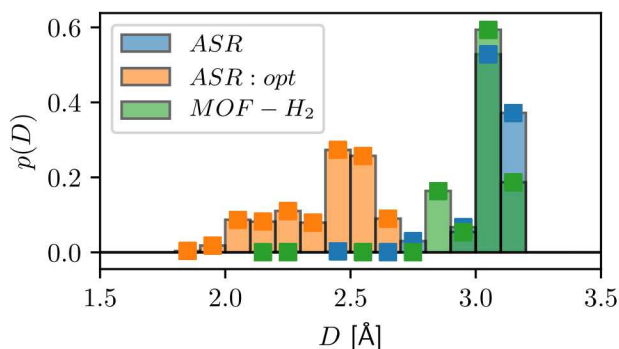
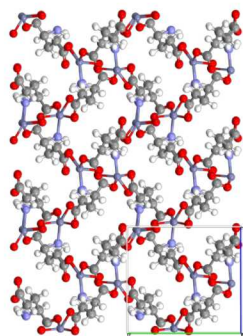
$$\Delta E_{def} = 7.1 \text{ kJ/molH}_2$$

$$\Delta E_b = -11.3 \text{ kJ/molH}_2$$

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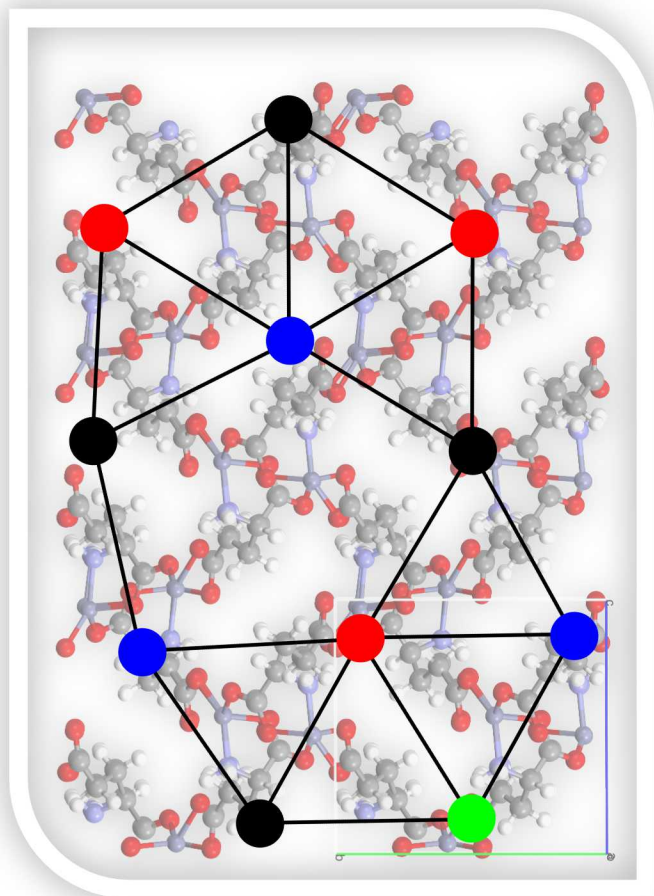
$$\Delta E_b = -11.3 \text{ kJ/molH}_2$$

3. Rigorous isotherm prediction would require osmotic ensemble simulations and *ab initio* accuracy, how to circumvent?

Experimental adsorption studies are ongoing to validate computational predictions



**To be determined**



1.  $\text{H}_2$  adsorption in nominally (i.e., 0 K DFT optimized) nonporous can still be an energetically favorable process
2. 10,000s of porous materials can be efficiently screened with graph-theory based indicators of flexibility
3. DFT can be used to assess the adsorption viability of a handful of high potential, flexible candidates
4. For robust quantitative screening of adsorption, we need *ab initio* accuracy in the osmotic ensemble... How to circumvent?



Thank you for your attention.  
Questions?