



Identification of nominally nonporous H₂ physisorbents via graph theory-based descriptors of MOF flexibility

PRESENTED BY

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Collaboration Group:

Nottingham University – Sanliang Ling

Sandia National Laboratories – Andreas Schneemann, Pavithra Wijeratne, Robert Horton, Justin Wong, Vitalie Stavila, and Mark Allendorf

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3

Economical storage of hydrogen is critical for enabling a variety of zero emission technologies



Commercially available fuel cell vehicles with physical-based hydrogen storage:



<https://www.businessinsider.com/this-toyota-fuel-cell-car-can-power-your-house-2014-11>

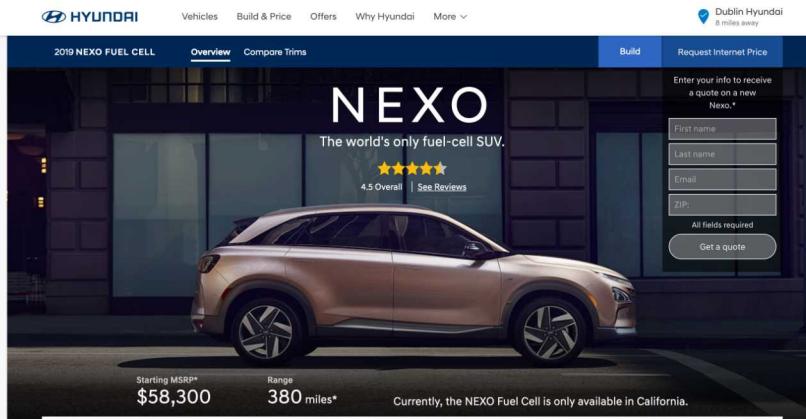
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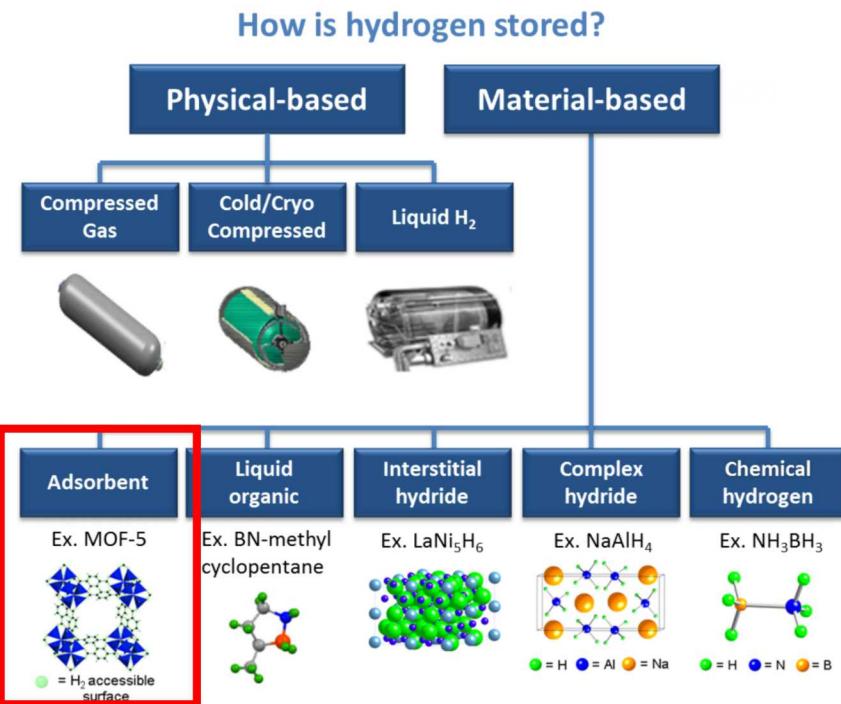


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A material that meets all DOE technical targets for on board hydrogen storage could help send the technology mainstream:

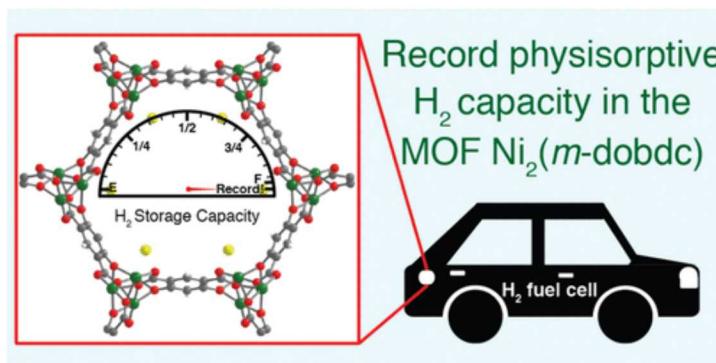


<https://www.energy.gov/eere/fuelcells/hydrogen-storage>

Physisorbents are attractive due to fast kinetics, but suffer from low volumetric capacities due to weak H₂ interactions



Solution 1: Rationally design best H₂ binding sites at highest possible volumetric density



Kapelewski, M. et al. *Chem. Mater.* 2018, 30, 22, 8179-8189

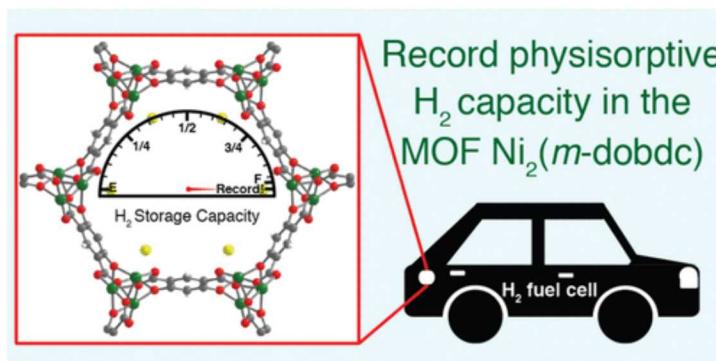


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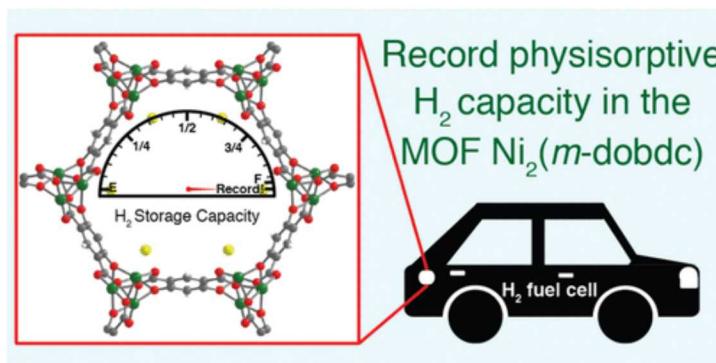


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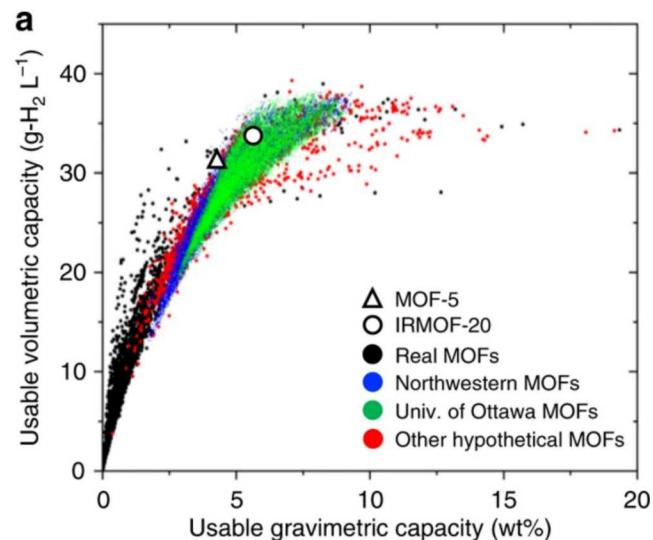


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Solution 2: High-throughput screening of known chemical space to identify top adsorbents



Ahmed, A. et al. *Nat. Commun.* 2019, 10, 1568

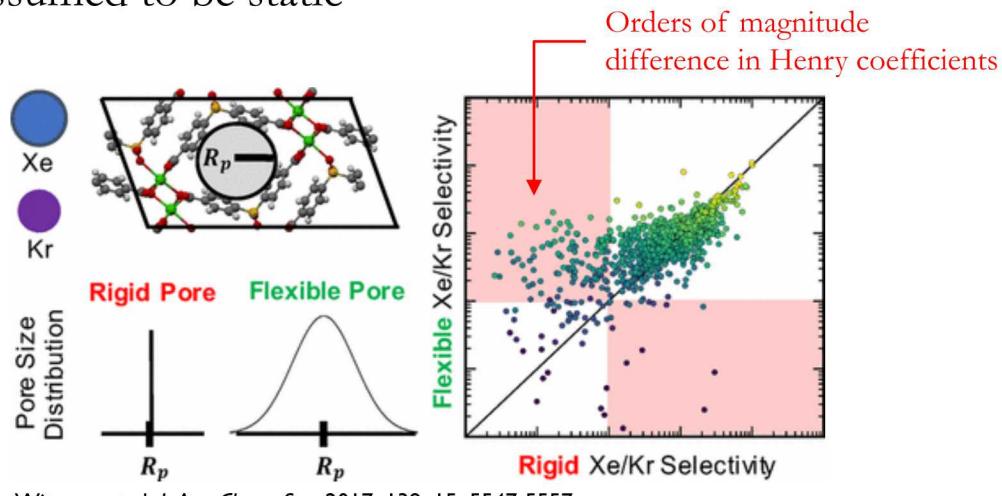
High-throughput screening may miss promising H₂ physisorbents due to two approximations (made for computational tractability)

1. Off-the-shelf “transferable” force fields don’t accurately capture the interactions of H₂ with the strongest binding sites in MOFs



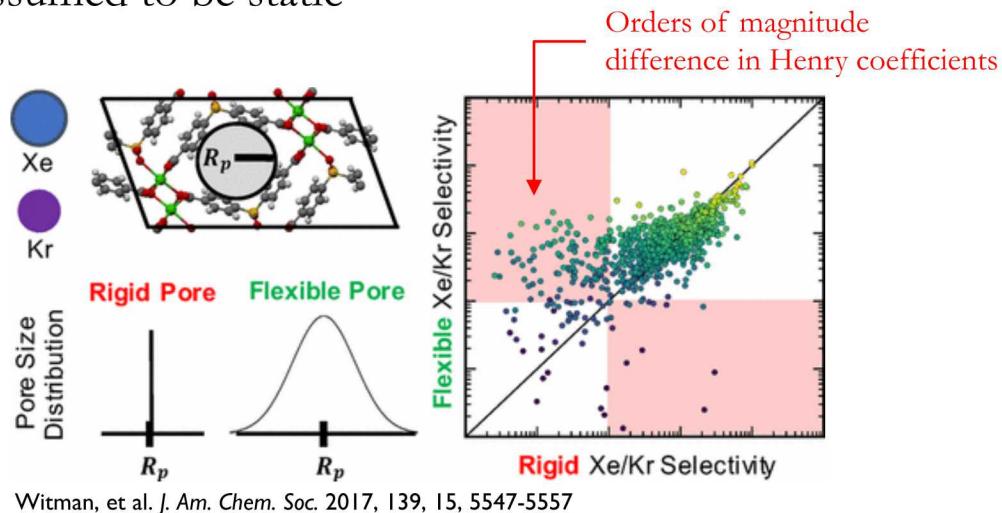
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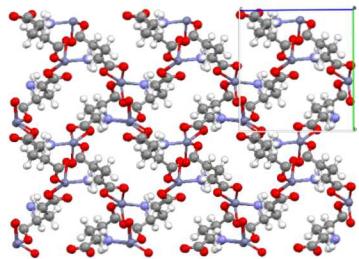
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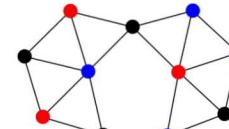
3. **Research question:** How do we efficiently identify these materials that are nominally non-porous, but are sufficiently flexible that H₂ adsorption is energetically favorable?

Graph theory-based, high-throughput porous materials' analyses are enabled by open-source **LAMMPS Interface**



build passing docs passing pypi package 0.1.2

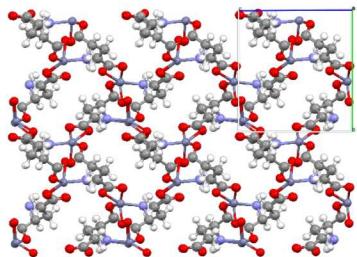
LAMMPS Interface



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{ '1':  
  { 'element': 'C',  
   'hybridization': 'sp3',  
   ... }}  
edges =
```

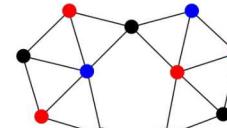
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{ ('1', '2'):  
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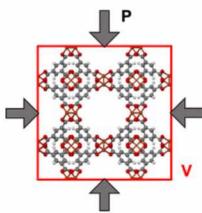
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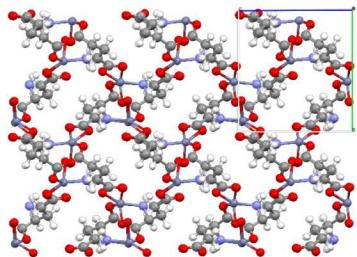
E.g. LAMMPS Interface + graph theory screening has enabled:

1. High-throughput FF assignment and determination of mechanical properties:



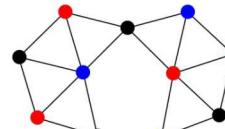
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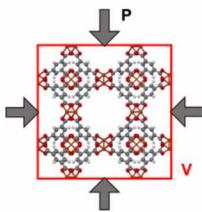
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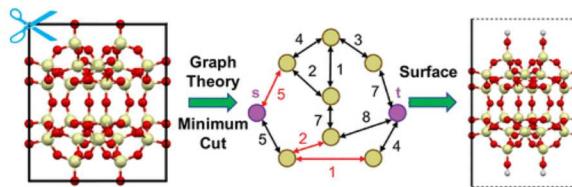
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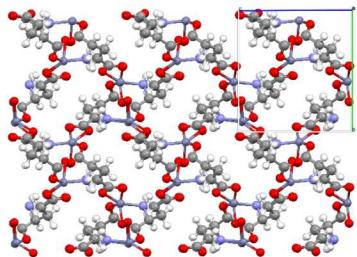
2. Min cut analysis of zeolite graphs reveals 2D forming topologies:



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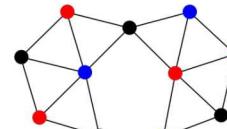
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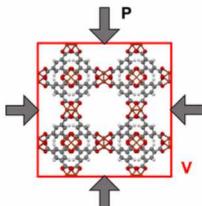
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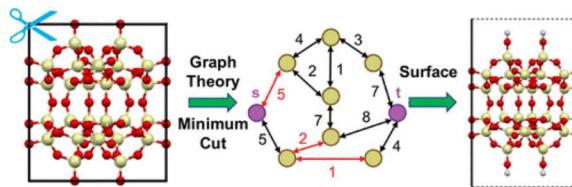
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3. High-throughput identification of flexible MOFs via graph search

This Work

Hypothesis: MOFs containing saturated organic components are likely to display a significant degree of flexibility



1. Preliminaries:

$G = (V, E)$ be the MOF's connected, undirected graph

$R \equiv$ the set of all nodes considered rigid

$F \equiv$ the set of all nodes considered flexible

$V' \equiv$ the vertices in a connected subgraph of G

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f_α : a node belongs to F if it is an sp³ hybridized, non-metal atom

f_β : a node belongs to F if it is an sp³ hybridized, non-metal atom and is bonded to at most two other (non-H) atoms

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4. Objectives:

$$L = \{V'_1, V'_2, \dots, V'_{|L|}\} \mid (V'_1 \cap V'_2 \dots \cap V'_{|L|} = \emptyset) \wedge (V'_1 \cup V'_2 \dots \cup V'_{|L|} = F)$$

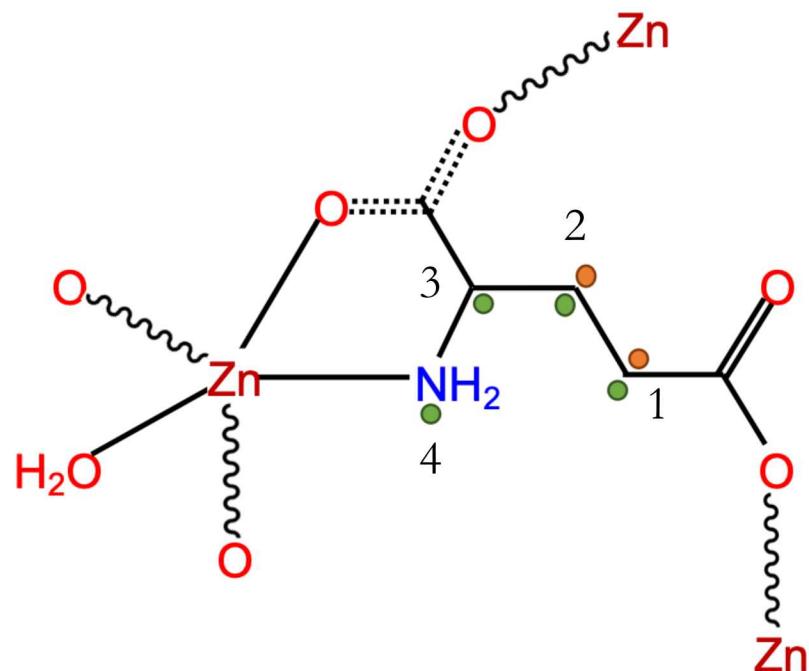
$$N = \{|V'_1|, |V'_2|, \dots, |V'_{|L|}|\}$$

I.e. what are all the independent, flexible subgroups in the MOF (L_α) and how big are they (N_α) ?

Visualized: Graph theoretic identification of flexible subunits

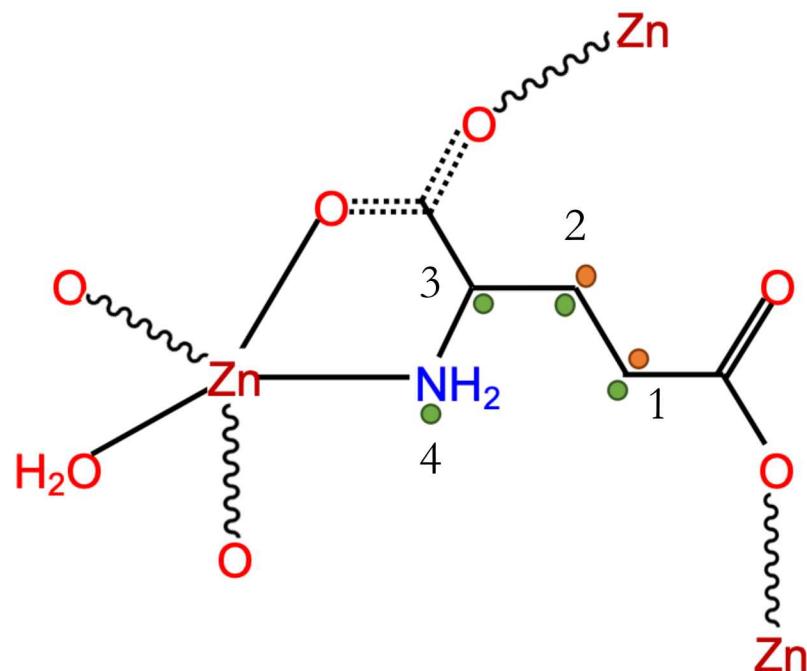


2D sketch of a MOF building unit (4 linkers per unit cell):





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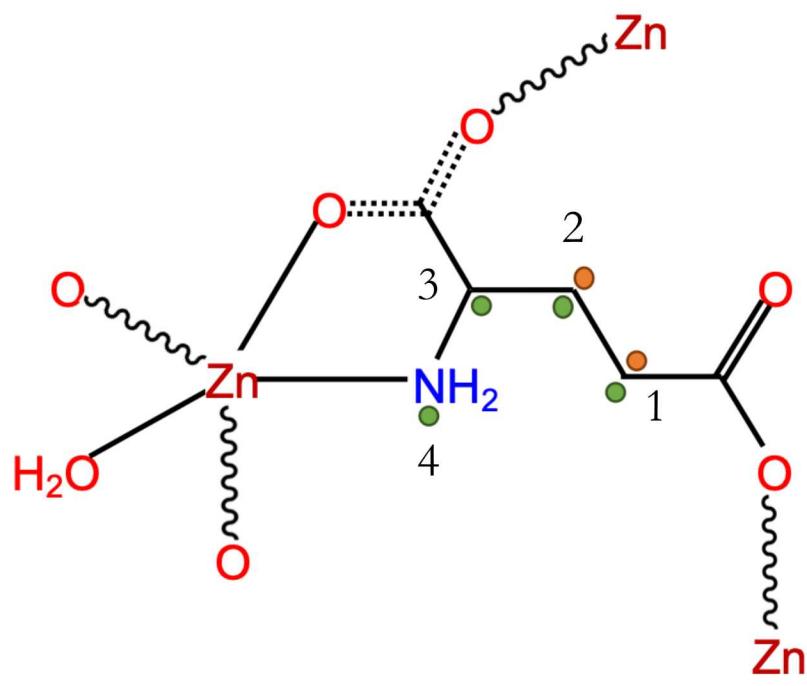
f_α objectives:
 $L_\alpha = \{\{1,2,3,4\}, \dots\}$
 $N_\alpha = \{4,4,4,4\}$

f_β objectives:
 $L_\beta = \{\{1,2\}, \dots\}$
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f_α descriptors:

$$\min(N_\alpha) = 4$$

$$\phi = \frac{\sum N_\alpha}{\# atoms}$$

f_β objectives:

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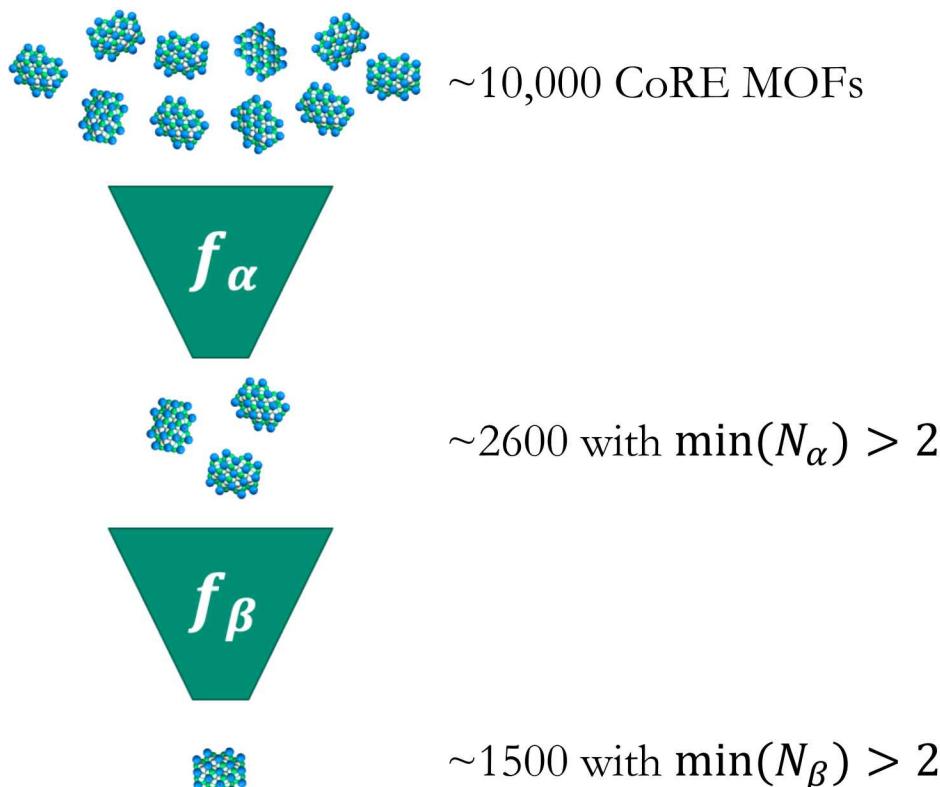
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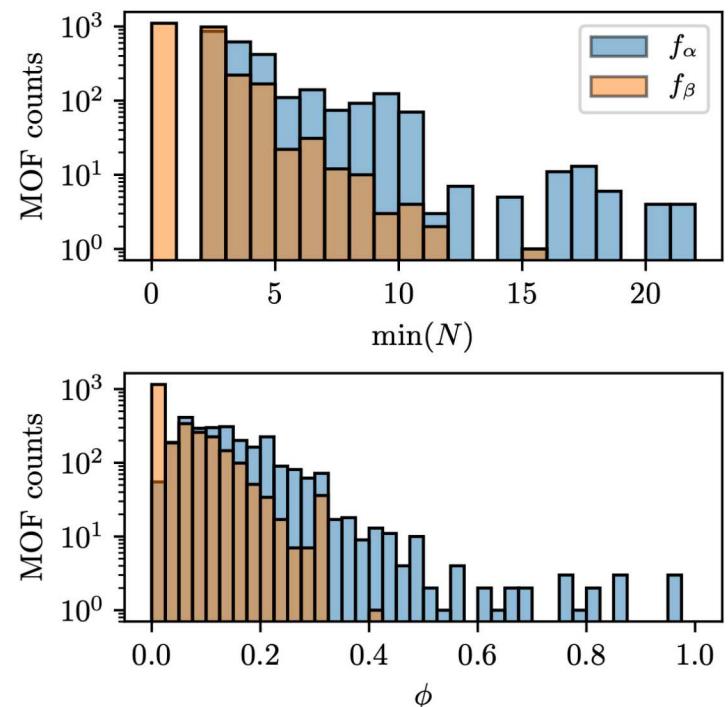
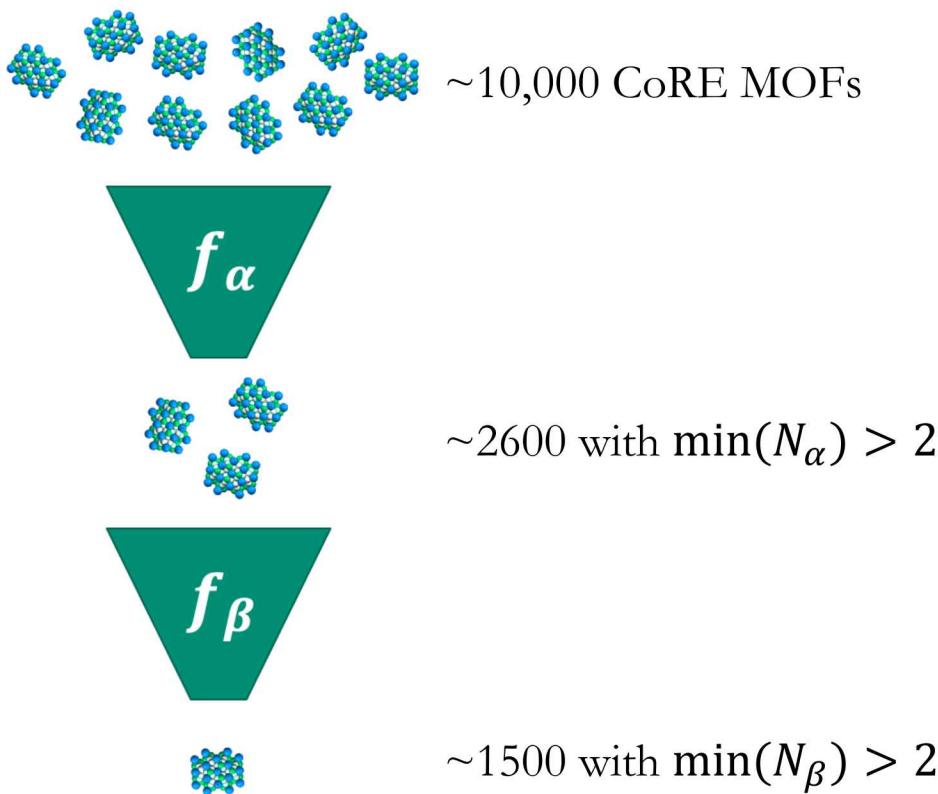
$$\min(N_\beta) = 2$$

$$\phi = \frac{\sum N_\beta}{\# atoms}$$

Automated extraction of CoRE MOFs deemed to be flexible from graph theory descriptors



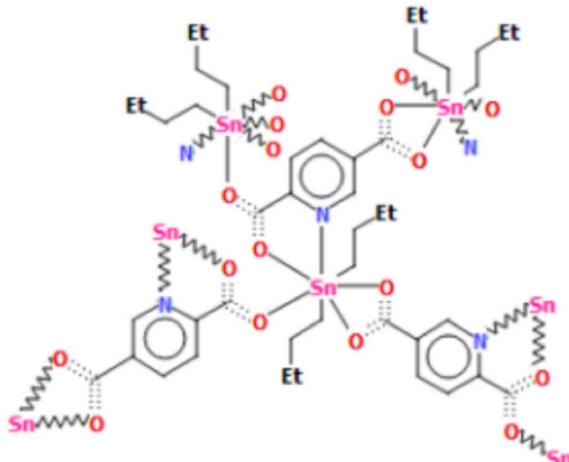
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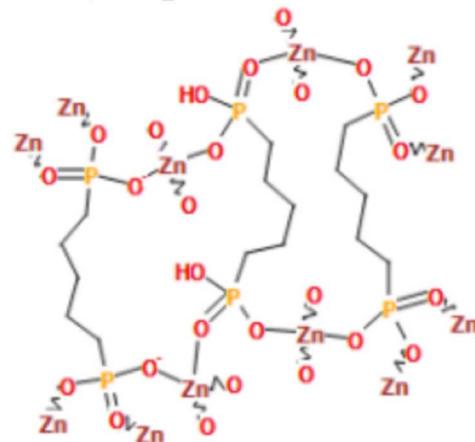
Structurally diverse flexible moieties are identified by the graph theory screening



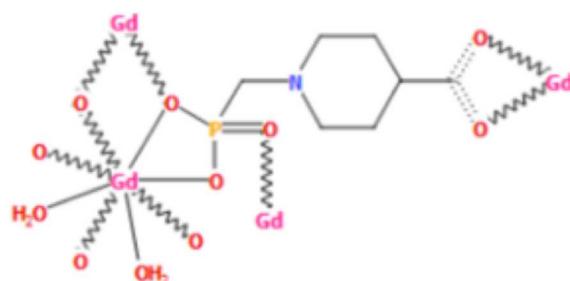
Flexible side chains:



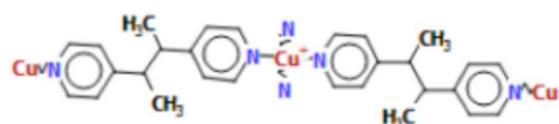
Fully aliphatic backbone:



Saturated ring backbone:



Aliphatic backbone hinges:





Computational adsorption experiments portend favorable H₂ adsorption despite “non-porous” OK structure

DFT calculations on materials with:

1. $\min(N_\beta) > 2$
2. Pore size similar/slightly smaller than H₂
3. Contain open metal sites (strong H₂ binding sites)

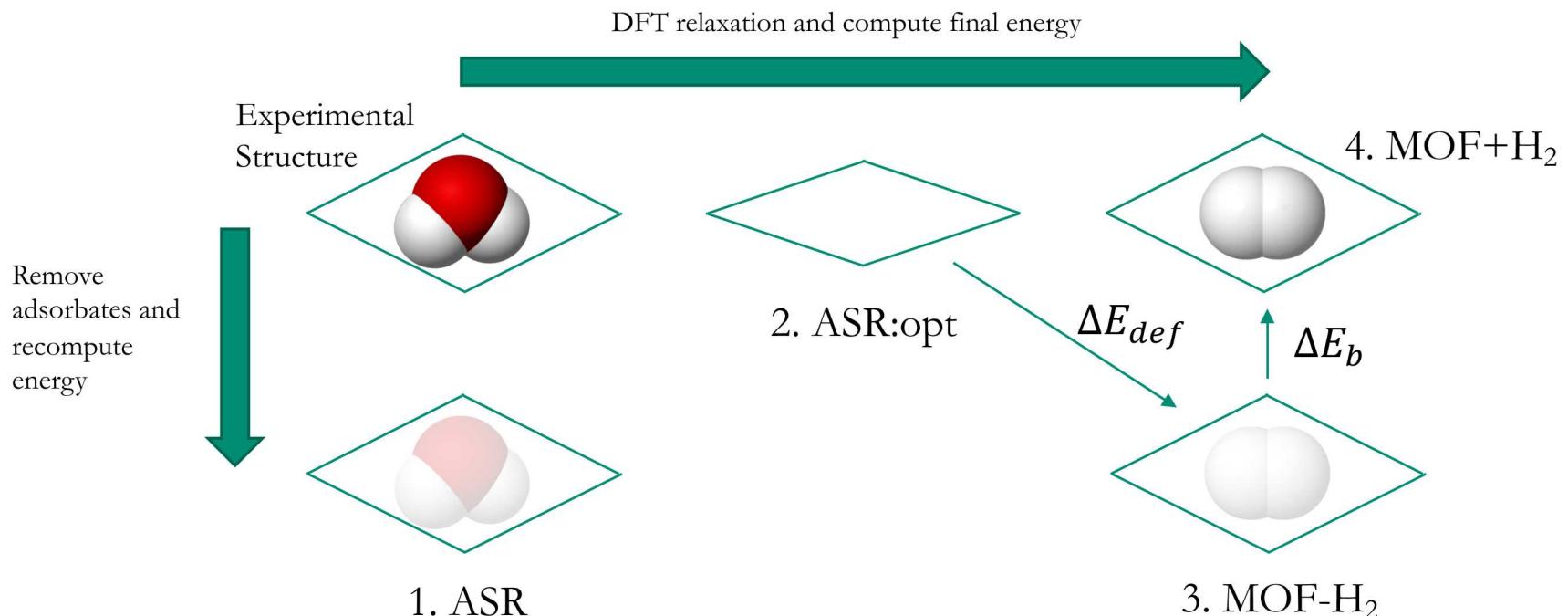
Computational adsorption experiments portend favorable H₂ adsorption despite non-porous 0K structure



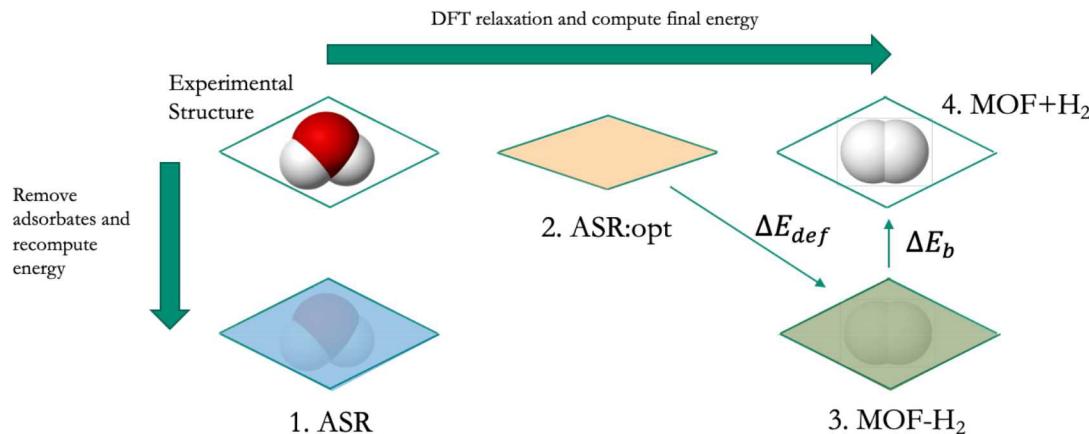
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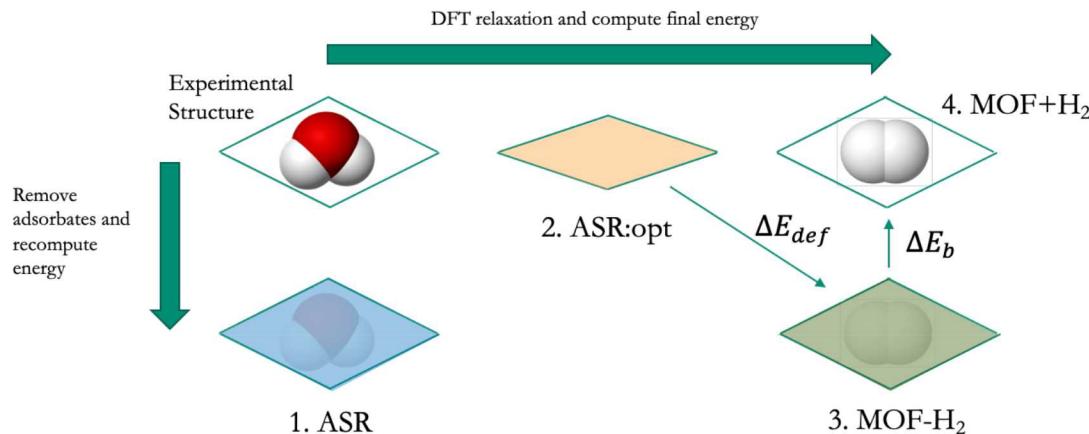
Compute energies/geometries of various adsorption states:



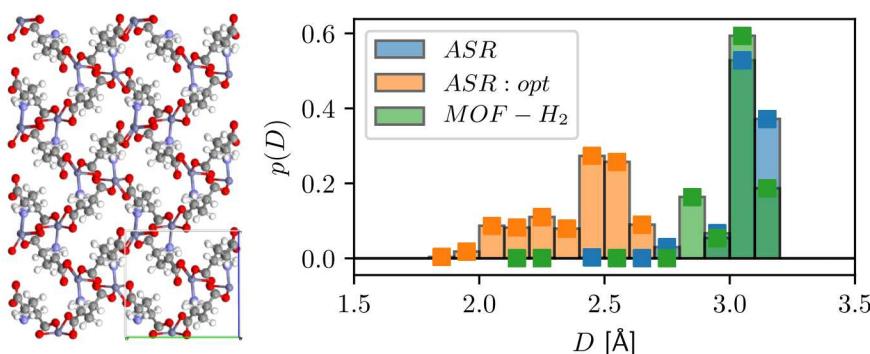
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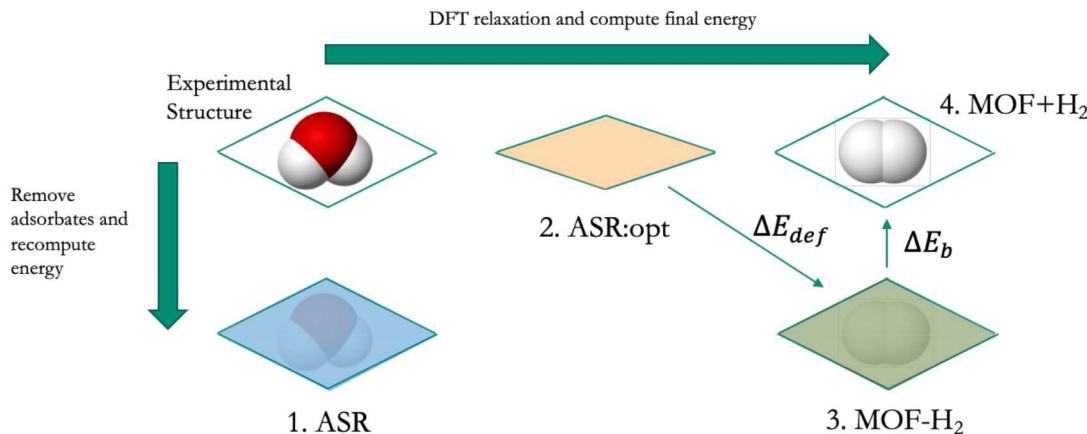
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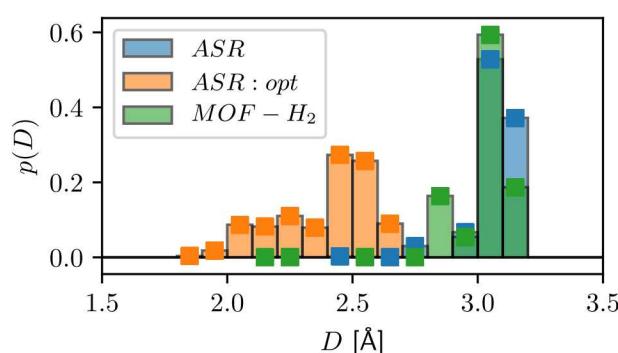
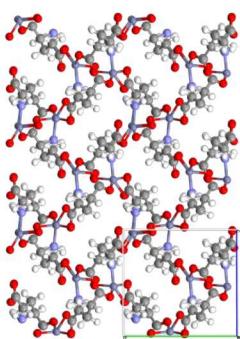
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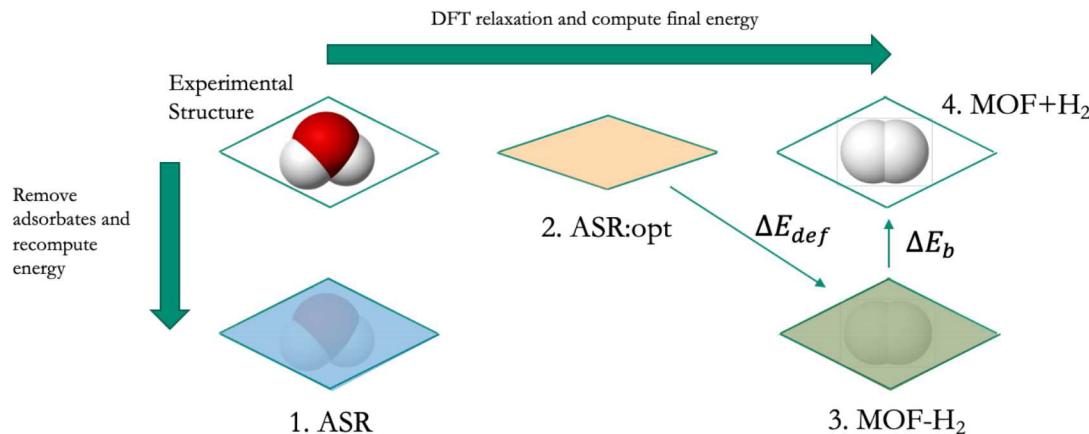


2. Highly favorable H₂ binding yields overall favorable process

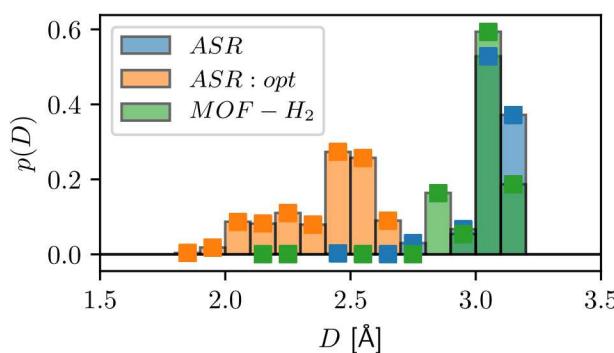
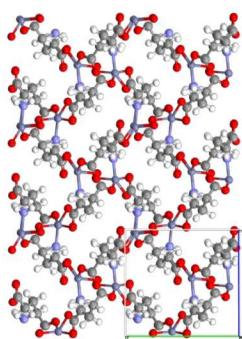
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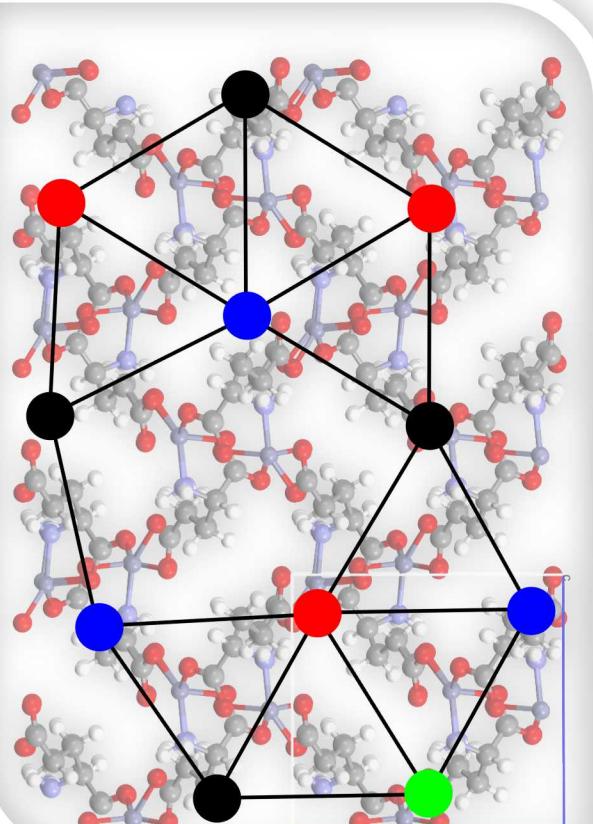
3. Rigorous isotherm prediction would require osmotic ensemble simulations and *ab initio* accuracy, how to circumvent?

Experimental adsorption studies are ongoing to validate computational predictions



To be determined

Key Takeaways



1. H_2 adsorption in nominally (i.e., 0 K DFT optimized) nonporous can still be an energetically favorable process
2. 10,000s of porous materials can be efficiently screened with graph-theory based indicators of flexibility
3. DFT can be used to assess the adsorption viability of a handful of high potential, flexible candidates
4. For robust quantitative screening of adsorption, we need *ab initio* accuracy in the osmotic ensemble... How to circumvent?



Thank you for your attention.

Questions?