

RECENT INTERATOMIC POTENTIAL DEVELOPMENT ACTIVITIES AT SANDIA

**X. W. Zhou, N. Bartelt, R. B Sills, C. D. Spataru,
and M. D. Allendorf**

Sandia National Laboratories, CA, USA

S. Kang, T. W. Heo, and B. C. Wood

Lawrence Livermore National Laboratory, CA, USA

Sandia National Laboratories is a multi-mission laboratory managed and operated by National Technology and Engineering Solutions of Sandia, LLC., a wholly owned subsidiary of Honeywell International, Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA-0003525. The authors gratefully acknowledge research support from the U.S. Department of Energy, Office of Energy Efficiency and Renewable Energy, Fuel Cell Technologies Office. The views expressed in the article do not necessarily represent the views of the U.S. Department of Energy or the United States Government.

Two Topics

- **Pd-H-He potential**
- **Mg-B-H potential**



Pd-H-He Potential - Motivation

- **Pd is a solid-state tritium storage material**
- **Tritium decays to He, forming He bubbles**
- **Bubbles causes PCT shift, swelling, He release, all leading to failures**
- **MD can study bubble nucleation / growth**



Criteria for Acceptable Pd-H-He Potential

- Octahedral interstitial sites in fcc
- Low He diffusion barrier (~ 0.1 eV)
- Large He swelling ($\sim 10 \text{ \AA}^3$)
- Short He-He spacing in Pd ($\sim 1.7 \text{ \AA}$)
- Non-bonding in pure He (equation of state)
- Strong He-He attraction in Pd (~ -0.85 eV)
- Correct volume and energy for PdHe rock-salt
- Correct Pd vacancy and He insertion energies as a function of He number
- Stringent MD tests



Two Paradoxes

- **Increasing swelling is against a low diffusion energy barrier**
- **Increasing He-He attraction in Pd is against He-He repulsion in pure He**



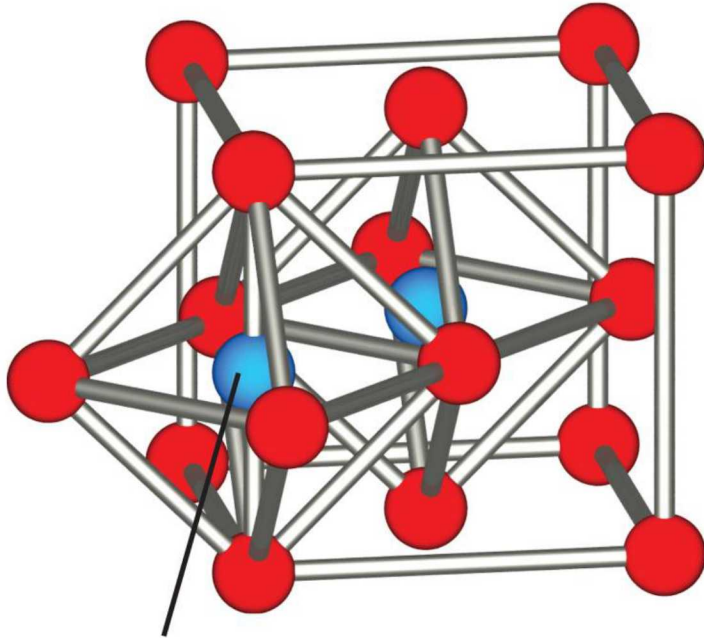
Past MD Simulations of He Bubbles

- Two papers are published after 2016
- Nuc. Sci. Tech. 27, 106 (2016) prescribes incorrect tetrahedral H sites and manually creates He bubbles
- J. Chem. Phys. 144, 194705 (2016) prescribes a He diffusion energy barrier of > 3.0 eV
- He bubbles in W have been successfully studied, see, for example, Nucl. Fusion, 53, 073015 (2013), and J. Nucl. Mater., 432, 61 (2013)



Difference between Pd and W

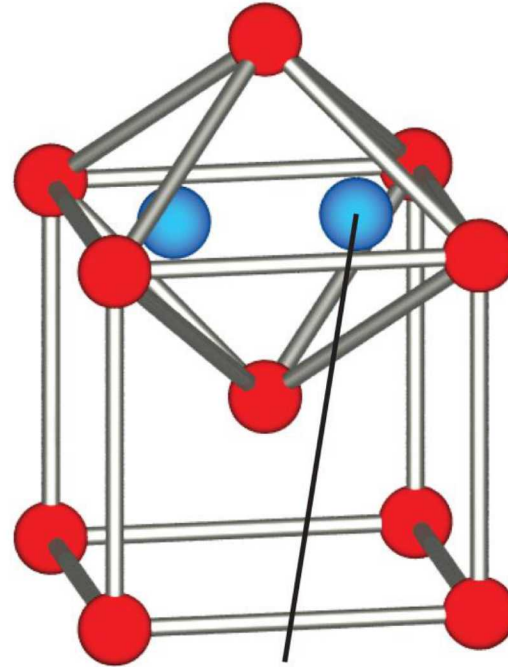
(a) He sites in fcc Pd



octahedral sites
(with spacing = 2.75 Å)

DFT He-He spacing in Pd = 1.7 Å

(b) He sites in bcc W



tetrahedral sites
(with spacing 1.58 Å)

- He at octa sites in fcc Pd but tetra sites in bcc W
- Diffusion barrier is smaller in bcc than in fcc
- Octa spacing in Pd is way longer than He-He spacing
- Tetra spacing in W is short than He-He spacing

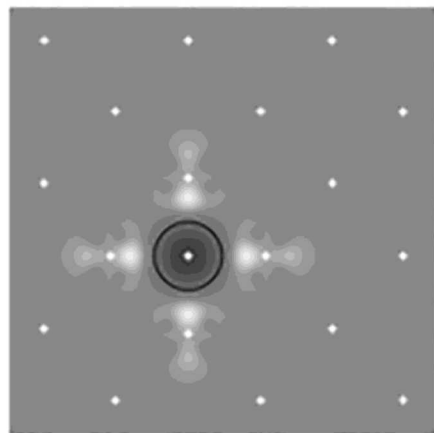
Solution

- Use the EAM potential by Finnis-Sinclair*: $\rho_i = \rho_j^i(r_{ij})$, as opposed to the one by Daw-Baskes**: $\rho_i = \rho_j(r_{ij})$
- Electron density created by Pd at He sites is negative
- Electron density created by He at He sites is positive
- He embedding energy is minimum at zero electron density
- Use EAM's many-body effect to increase swelling

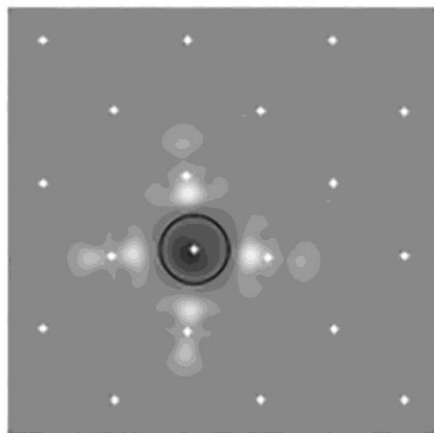
*Phil. Mag. A 50, 45 (1984), **Phys. Rev B. 29, 6443 (1984).

DFT Justification

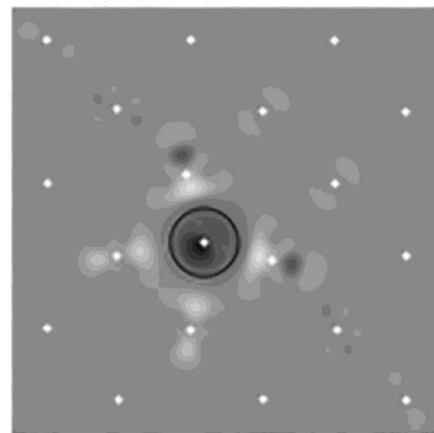
(a) octahedral site



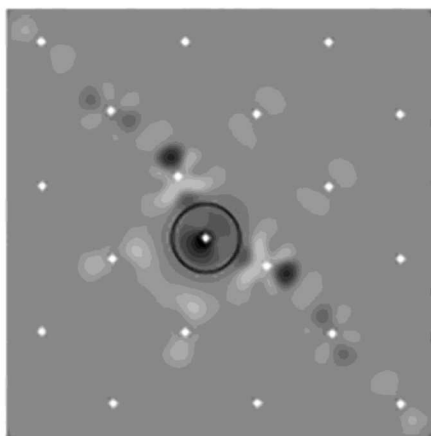
(b) step 1



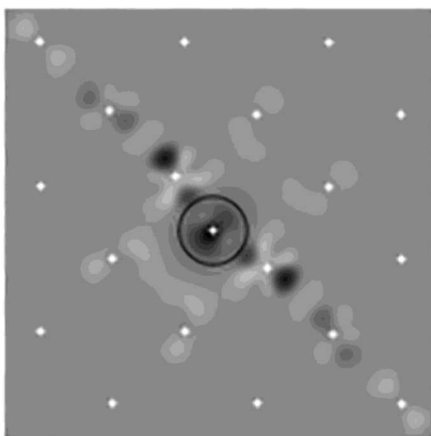
(c) step 2



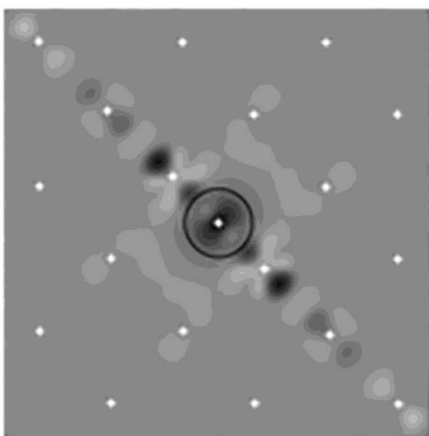
(d) step 3



(e) step 4



(f) saddle point



($e/\text{\AA}^3$)

0.05

0.00

-0.05

-0.10

-0.15

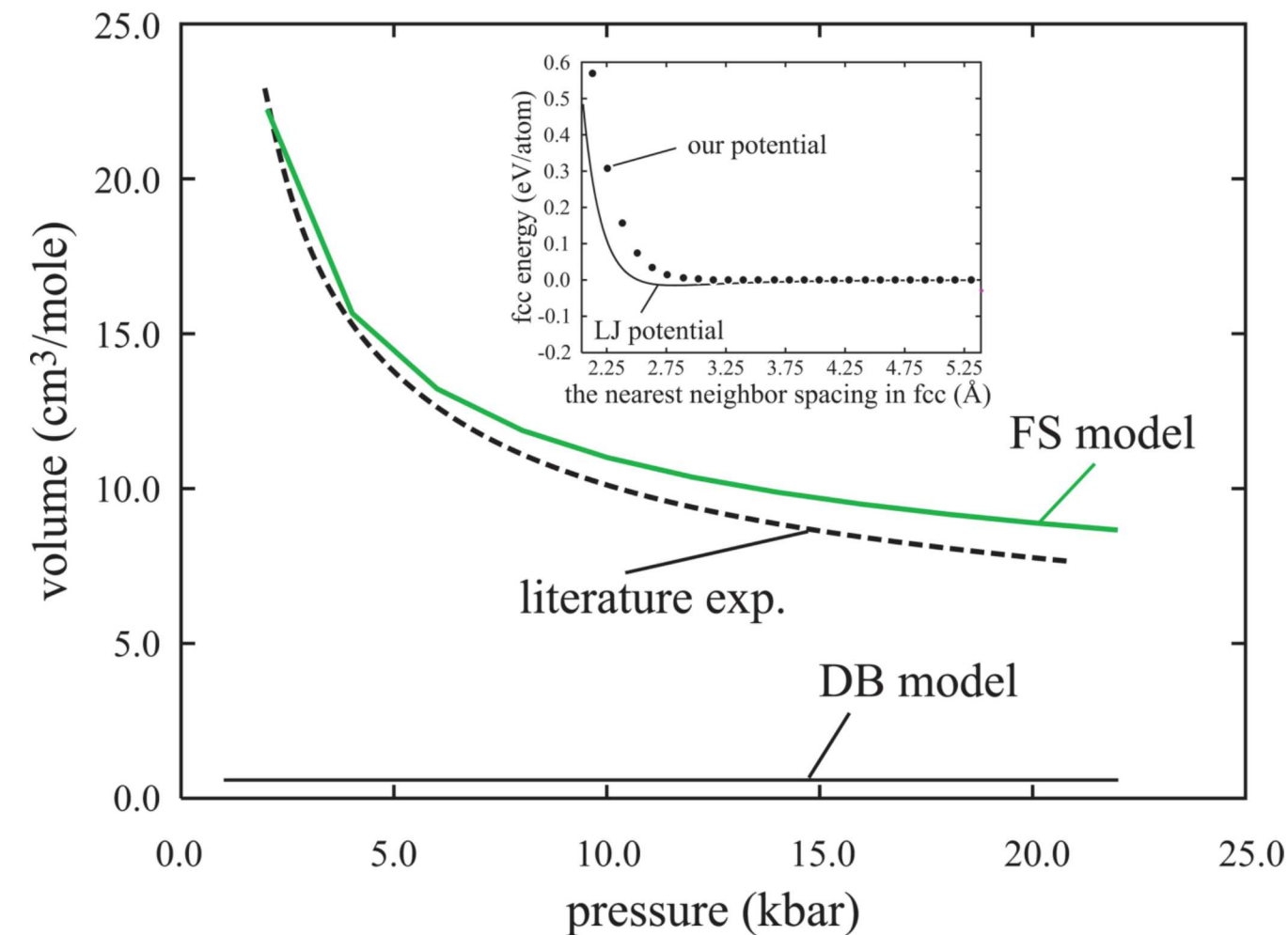
- He always repels electrons towards Pd
- The electron transfer processes are complex

Validation of Some Critical Properties

methods	Q_{He}	$\Omega_{0,\text{H}}$ e	$\Omega_{\text{He,He}}$	$\Omega_{\text{H,He}}$	E_{He}	$r_{\text{He-He}}$	$E_{\text{He-He}}$	$\Delta\Omega_{\text{Pd} \rightarrow \text{Pd}}$ He	$\Delta E_{\text{Pd} \rightarrow \text{PdH}}$ e
DB	0.19	10.1	10.0	9.7	3.63	1.75	-0.87	9.2	2.92
FS	0.14	8.7	18.8	8.4	4.04	1.72	-1.49	13.6	2.95
PBE	0.11	9.7	10.3	9.5	3.64	1.7	-0.87	6.7	2.99
LDA	0.07	7.3	8.0	10.1	3.63	1.7	-0.85	7.4	2.96



Validation of He Equation of State

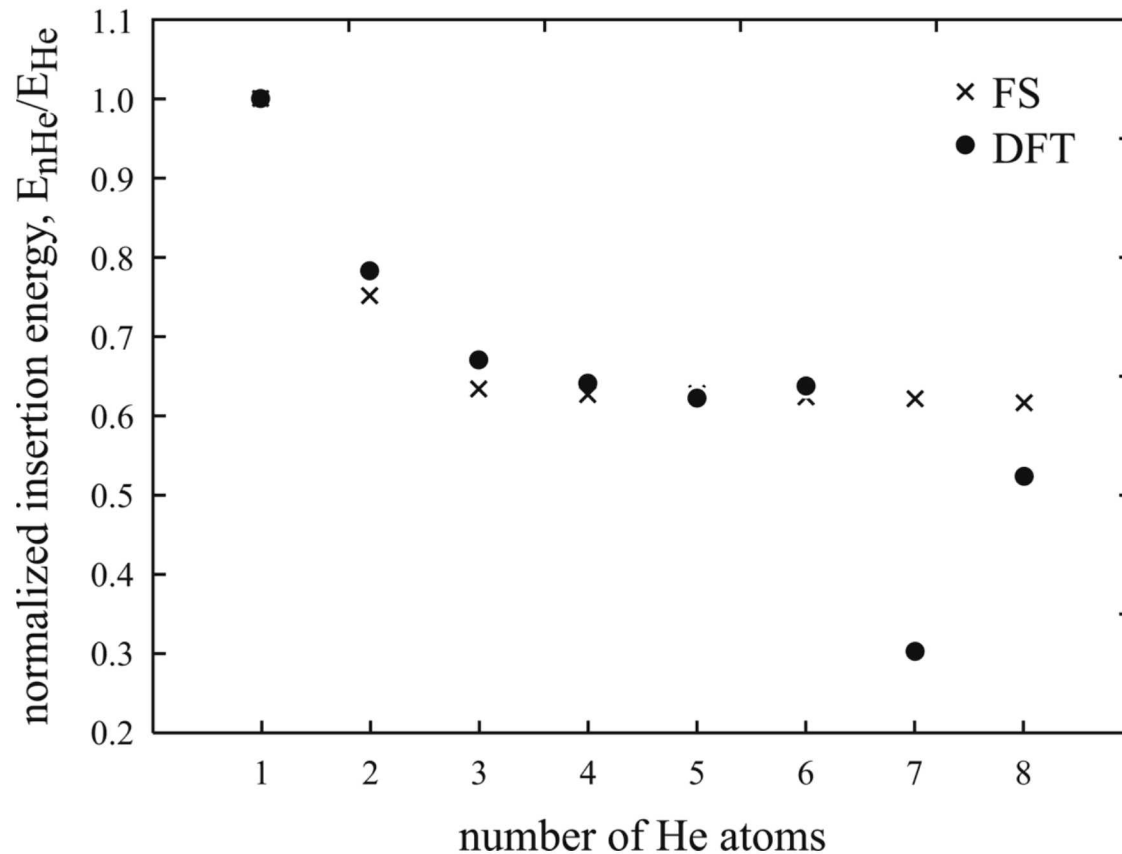


- **Our He-He interactions are purely repulsive and can capture well the He equation of state**
- **Our pure He potential is not that different from literature LJ potential****

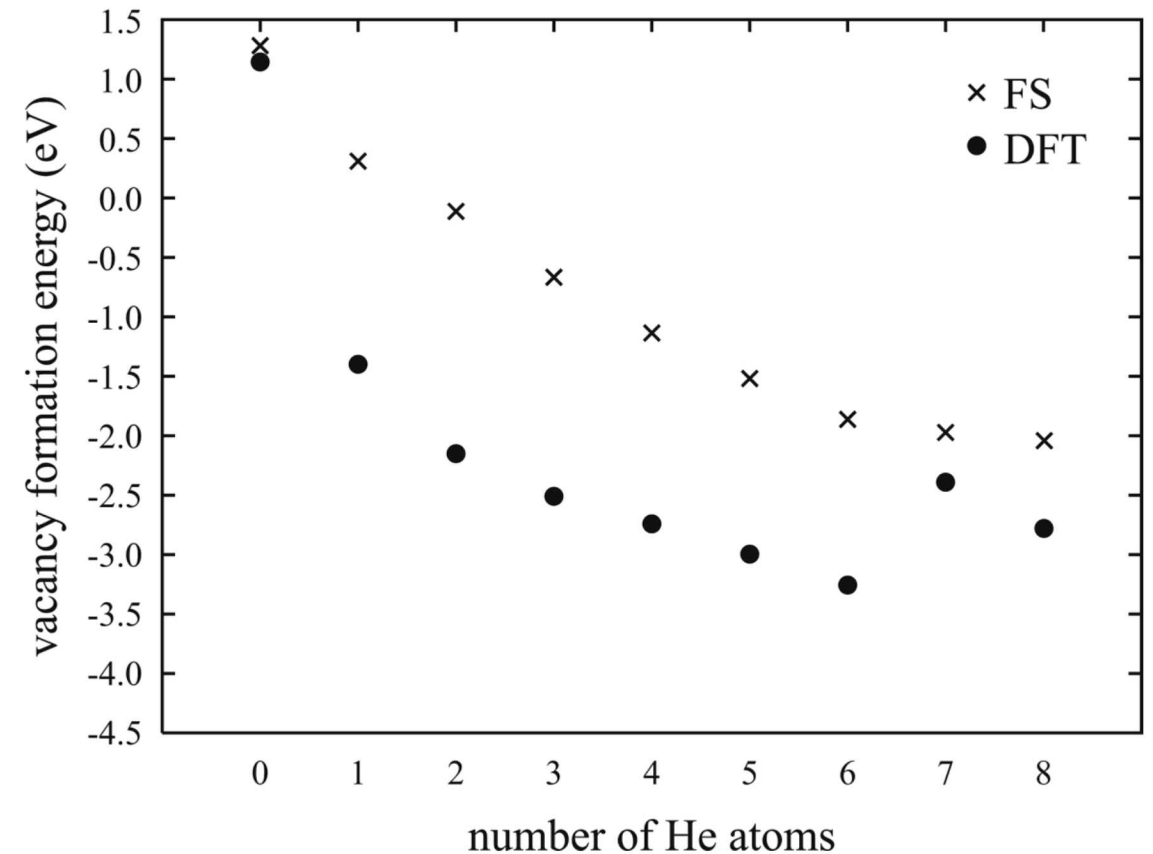
*literature equation of state: Phys. Rev. B, 21, 5137 (1980), **LJ: J. Chem. Phys. 144, 194705 (2016)

Validation of He Insertion and Pd Vacancy Energies

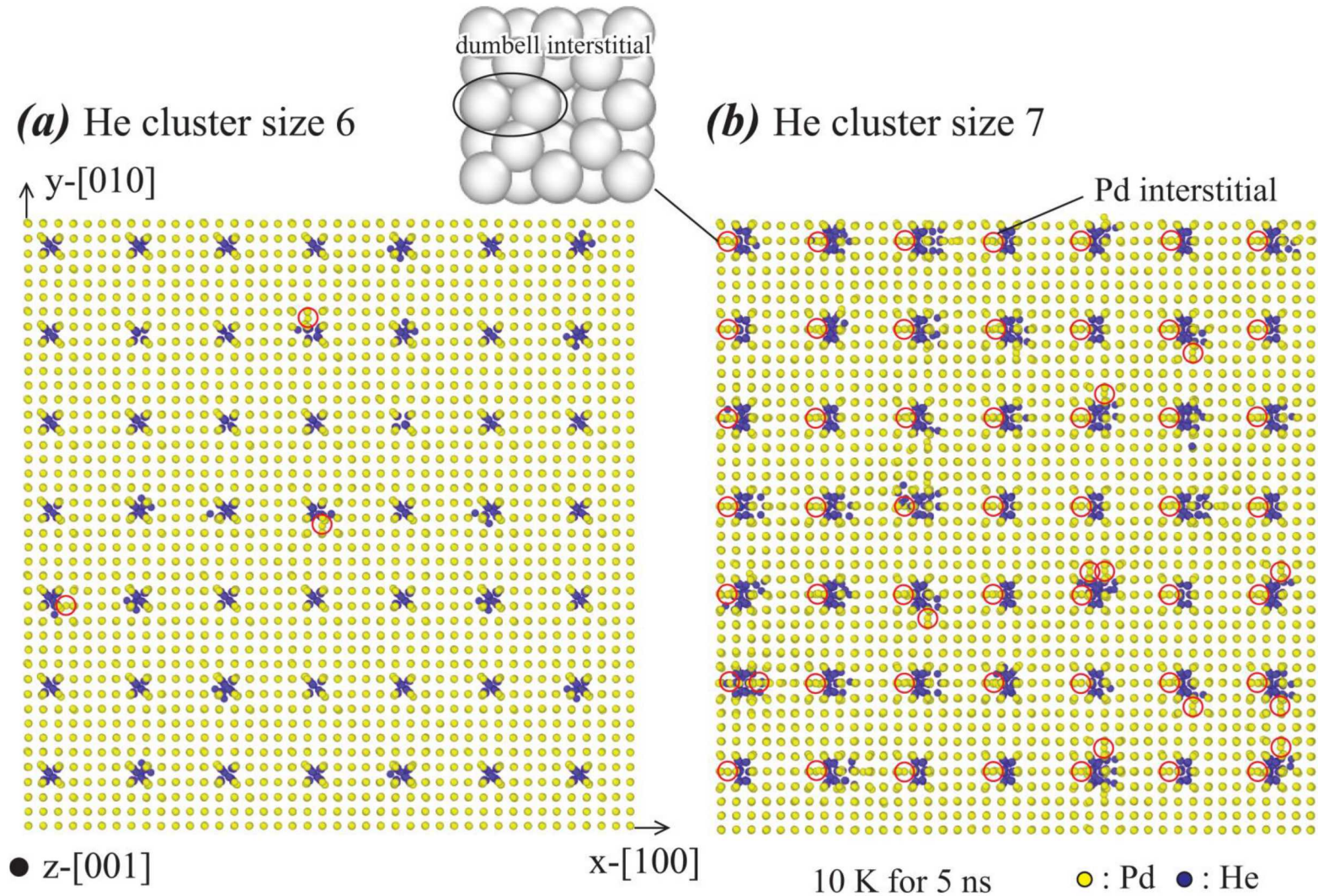
(a) normalized He insertion energy (at He # 1)



(b) Pd vacancy formation energy

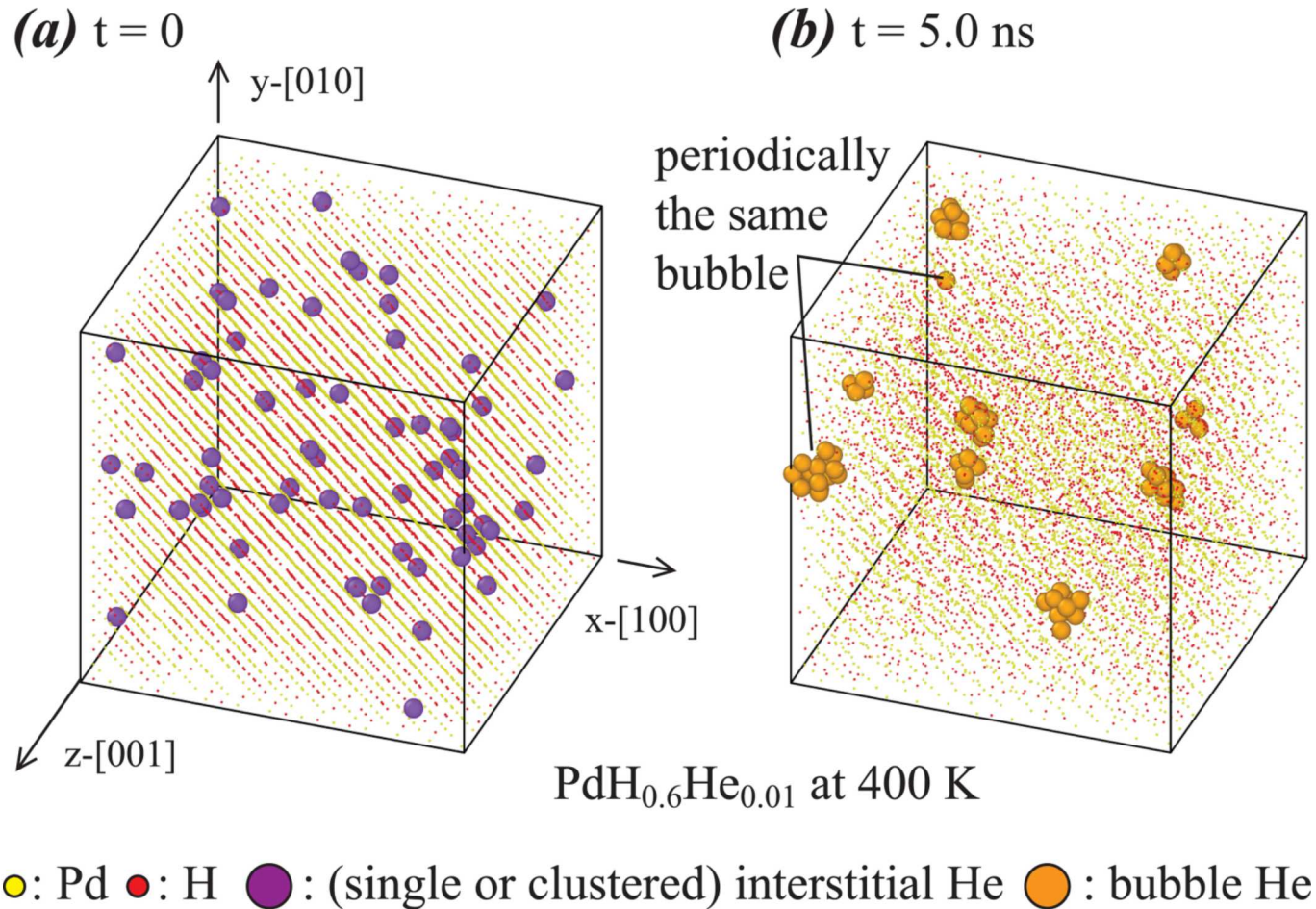


Validation of Critical He Size



- At He size 6, few Pd interstitials are seen
- At He size 7, all He clusters induce Pd interstitials, in good agreement with DFT results

Stringent MD Tests



- Initially, He atoms are randomly populated at octahedral sites in a $\text{PdH}_{0.6}$ lattice
- After MD simulations at 400 K for 5 ns, He bubbles are formed
- Enables simulations of bubble formation without assumptions

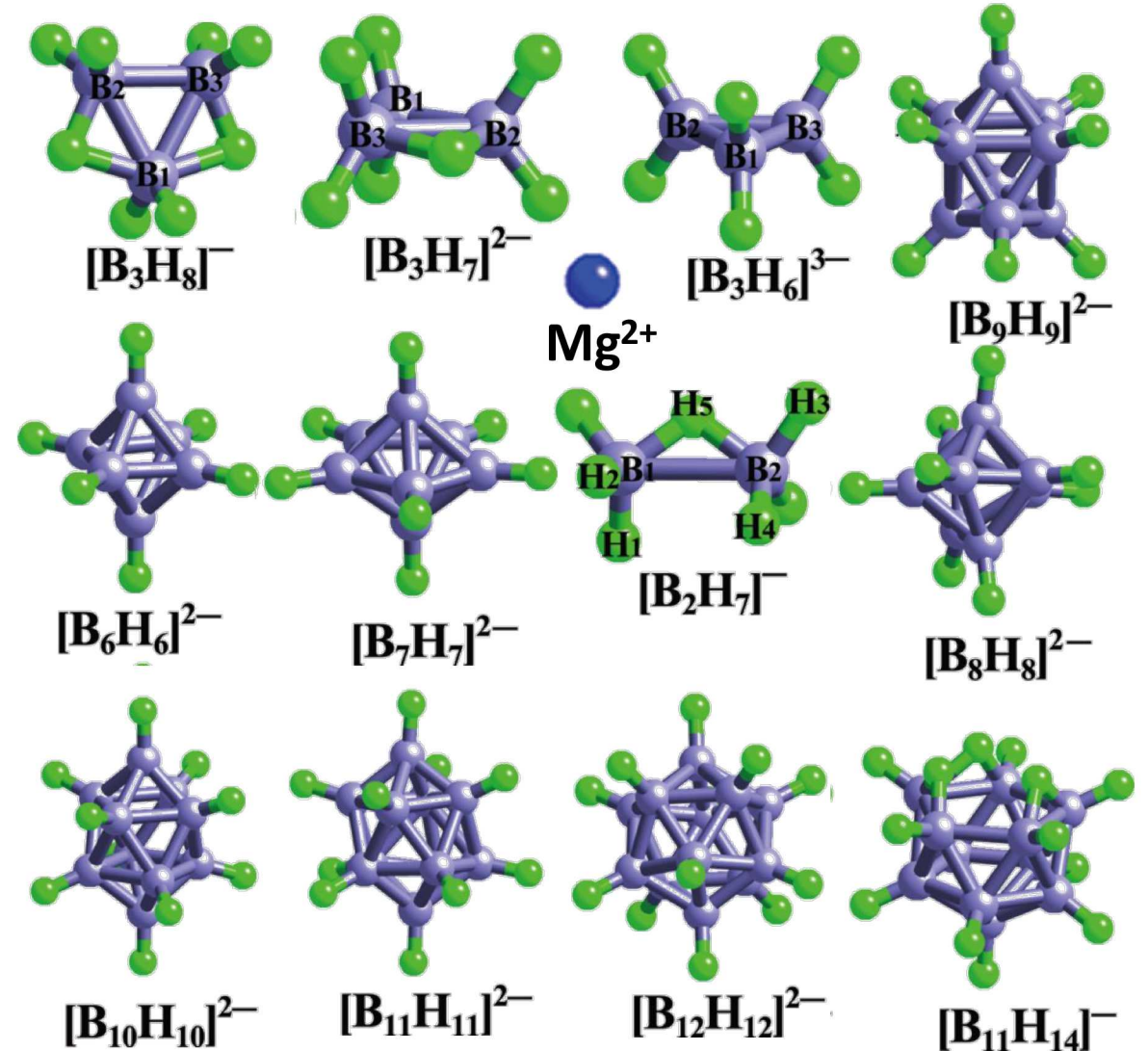
Mg-B-H Potential - Motivation

- **Hydrogen is an efficient and clean energy carrier**
- **Solid state hydrogen storage materials draw interests due to an ideal combination of volumetric and gravimetric densities**
- **HyMARC (Hydrogen Materials Advanced Research Consortium) aims to develop an understanding on how to improve (de)hydrogenation kinetics**
- **Magnesium boron hydrides are one type of materials being explored within HyMARC**

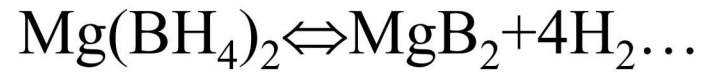
Perspective

- ❑ LLNL is developing a phase field model for (de)hydrogenation kinetics of MgB_xH_y
- ❑ The phase field model requires thermodynamic and kinetic properties as inputs
- ❑ Many molecules may occur, and many exhibit amorphous structures \Rightarrow challenging for DFT studies
- ❑ We will use MD to fill the gaps

Example Molecules



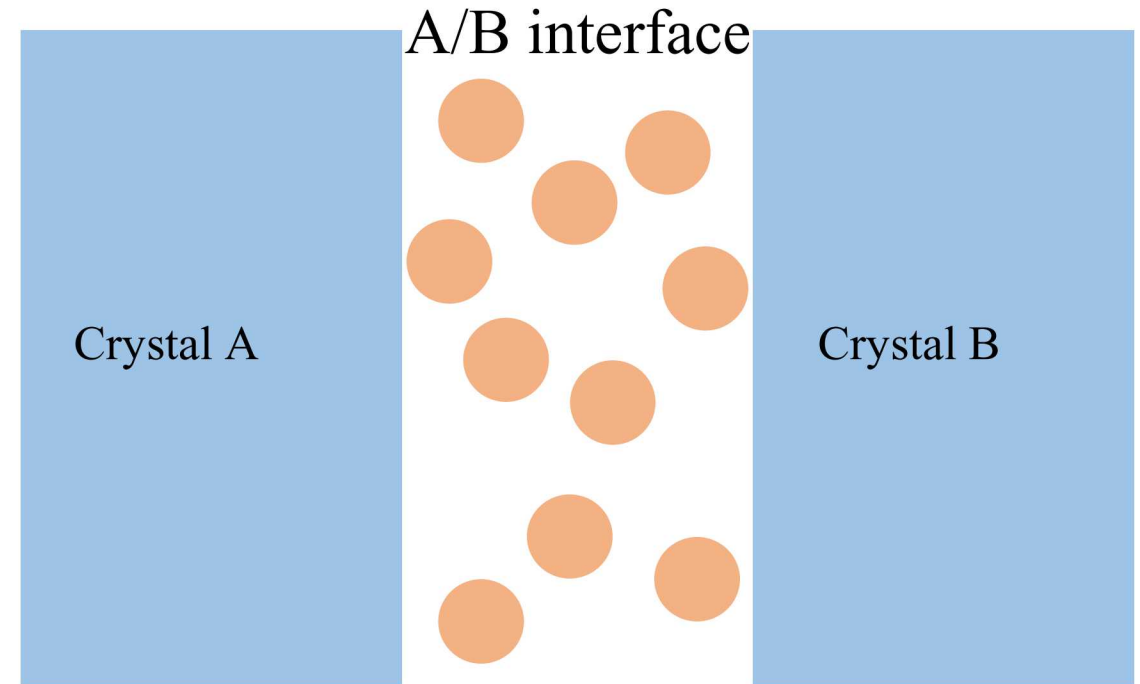
MgB_xH_y: Two Goals



...

- Many molecules were observed in NMR, XES, XAS, but not XRD \Rightarrow amorphous
- DFT is not sufficient for amorphous complex hydrides

Goal 1: Use MD to evaluate stabilities of different intermediates



- Interfaces between crystalline solids are often exhibit amorphous “soup” containing different molecular species

Goal 2: Use MD to calculate interfacial energies

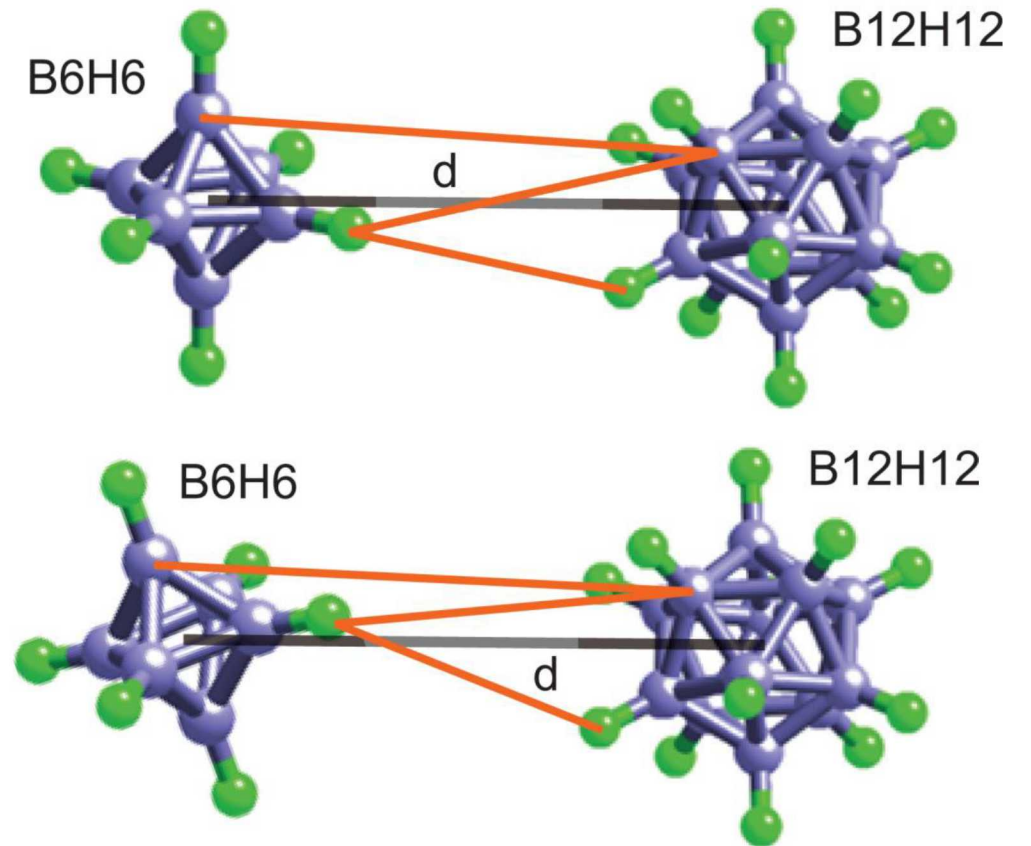
Molecular Dynamics Challenges

- ❑ Traditional MD can only simulate atoms, but we have molecules
- ❑ We will develop an innovative “molecular” dynamics method
 - An intra-molecule force field to stabilize molecules
 - An inter-molecule force field to capture energetics
 - MD must track which atom is in which molecule
- ❑ As a first trial, we parameterize force fields DFT energies between two isolated molecules
- ❑ Five molecules (Mg , H_2 , MgH_2 , BH_4 , $\text{B}_{12}\text{H}_{12}$) are considered

MgB_xH_y: Methods

- ❑ Energy comes from interactions between atoms from different (similar and dissimilar) molecules
- ❑ Perform DFT calculations of energies of all pairs of molecules at various distances and angles
- ❑ Fit pair potentials to DFT energies
- ❑ Implement the approach in LAMMPS

Interactions between different pairs of species are distinguished by rotation

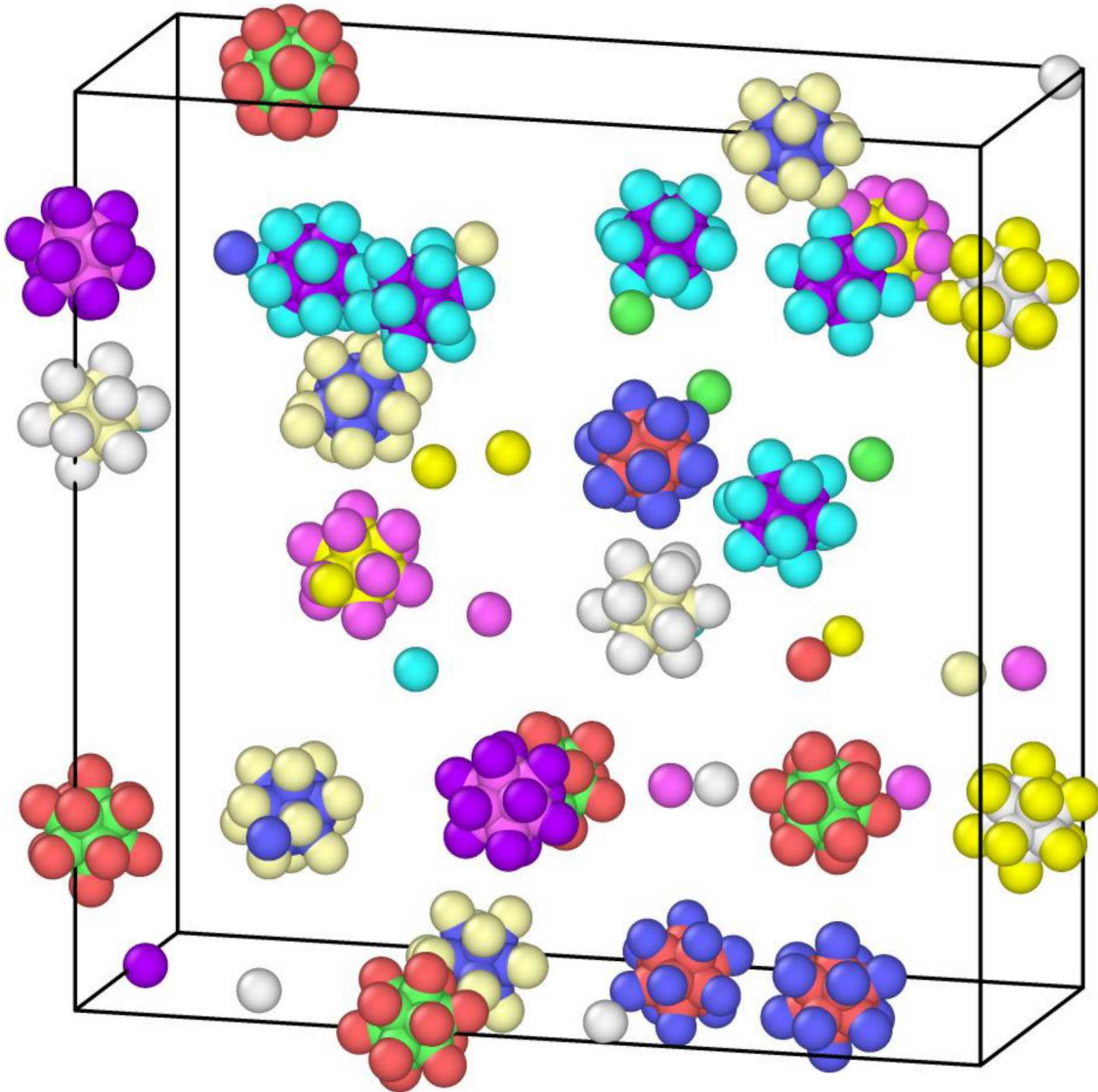


36 Inter-Molecule Interactions

□ For a $\text{Mg} + \text{H}_2 + \text{BH}_4 + \text{MgH}_2 + \text{B}_{12}\text{H}_{12}$ model, there are 36 inter-molecule interactions:

$\text{Mg-Mg}(\text{Mg-Mg})$, $\text{Mg-H}_2(\text{Mg-H})$, $\text{Mg-BH}_4(\text{Mg-B}, \text{Mg-H})$, $\text{Mg-MgH}_2(\text{Mg-Mg}, \text{Mg-H})$, $\text{Mg-B}_{12}\text{H}_{12}(\text{Mg-B}, \text{Mg-H})$, $\text{H}_2\text{-H}_2(\text{H-H})$, $\text{H}_2\text{-BH}_4(\text{H-B}, \text{H-H})$, $\text{H}_2\text{-MgH}_2(\text{H-Mg}, \text{H-H})$, $\text{H}_2\text{-B}_{12}\text{H}_{12}(\text{H-B}, \text{H-H})$, $\text{BH}_4\text{-BH}_4(\text{B-B}, \text{B-H}, \text{H-H})$, $\text{BH}_4\text{-MgH}_2(\text{B-Mg}, \text{B-H}, \text{H-Mg}, \text{H-H})$, $\text{BH}_4\text{-B}_{12}\text{H}_{12}(\text{B-B}, \text{B-H}, \text{H-B}, \text{H-H})$, $\text{MgH}_2\text{-MgH}_2(\text{Mg-Mg}, \text{Mg-H}, \text{H-H})$, $\text{MgH}_2\text{-B}_{12}\text{H}_{12}(\text{Mg-B}, \text{Mg-H}, \text{H-B}, \text{H-H})$, $\text{B}_{12}\text{H}_{12}\text{-B}_{12}\text{H}_{12}(\text{B-B}, \text{B-H}, \text{H-H})$

MD Implementation

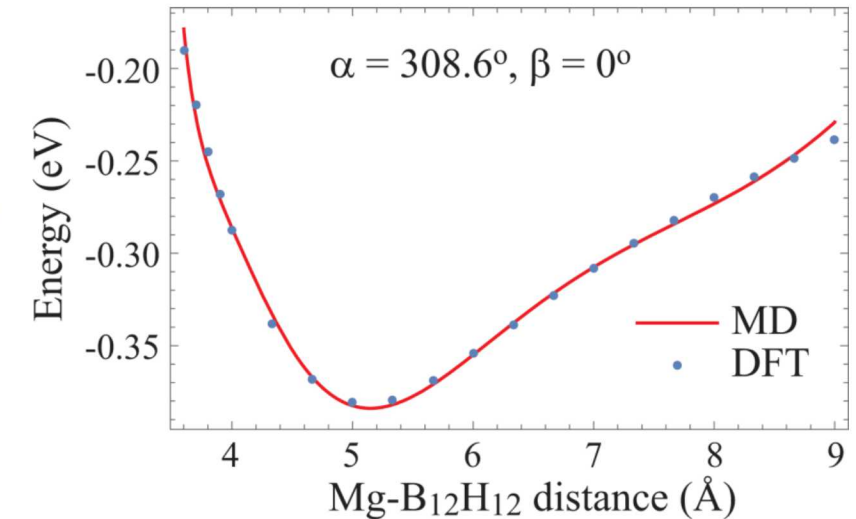
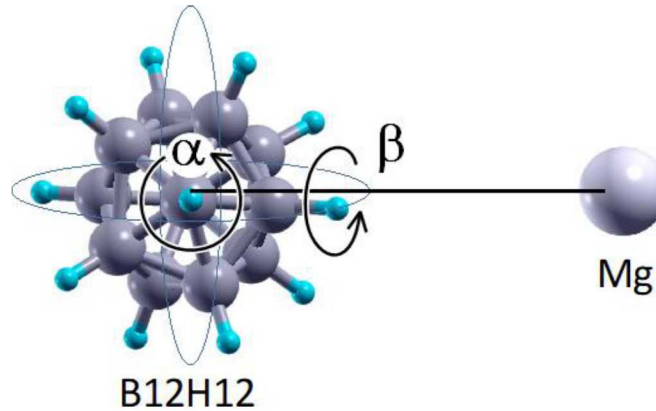
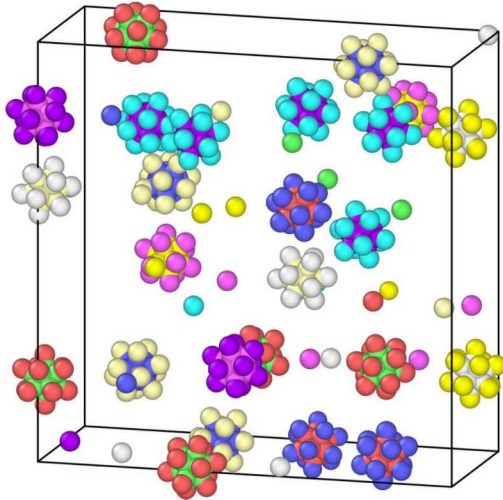


- ☐ Atom-based MD does not know molecules
- ☐ Assign different atom types for different molecules
- ☐ Create mapping tables between atom types and pair interactions

Progress

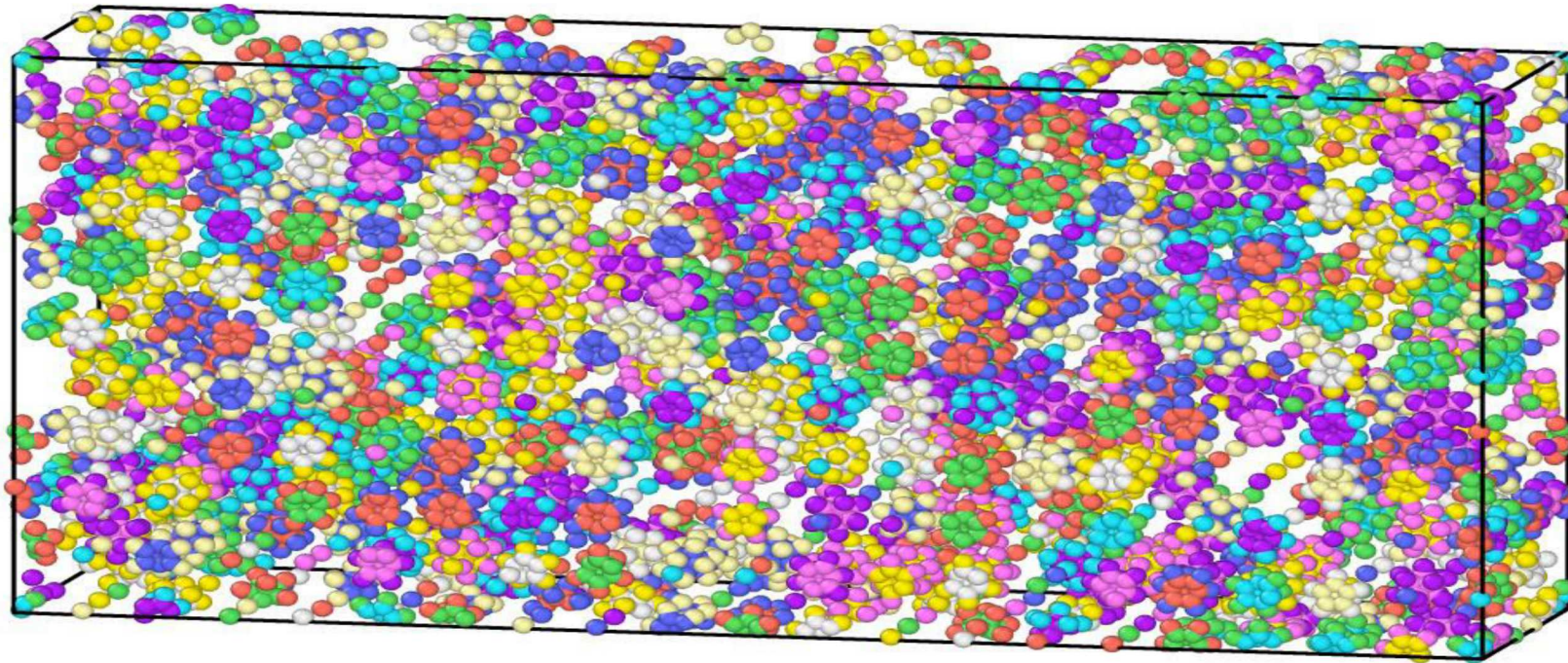
“Molecular” Dynamics Case

Example Mg-B₁₂H₁₂ Interaction



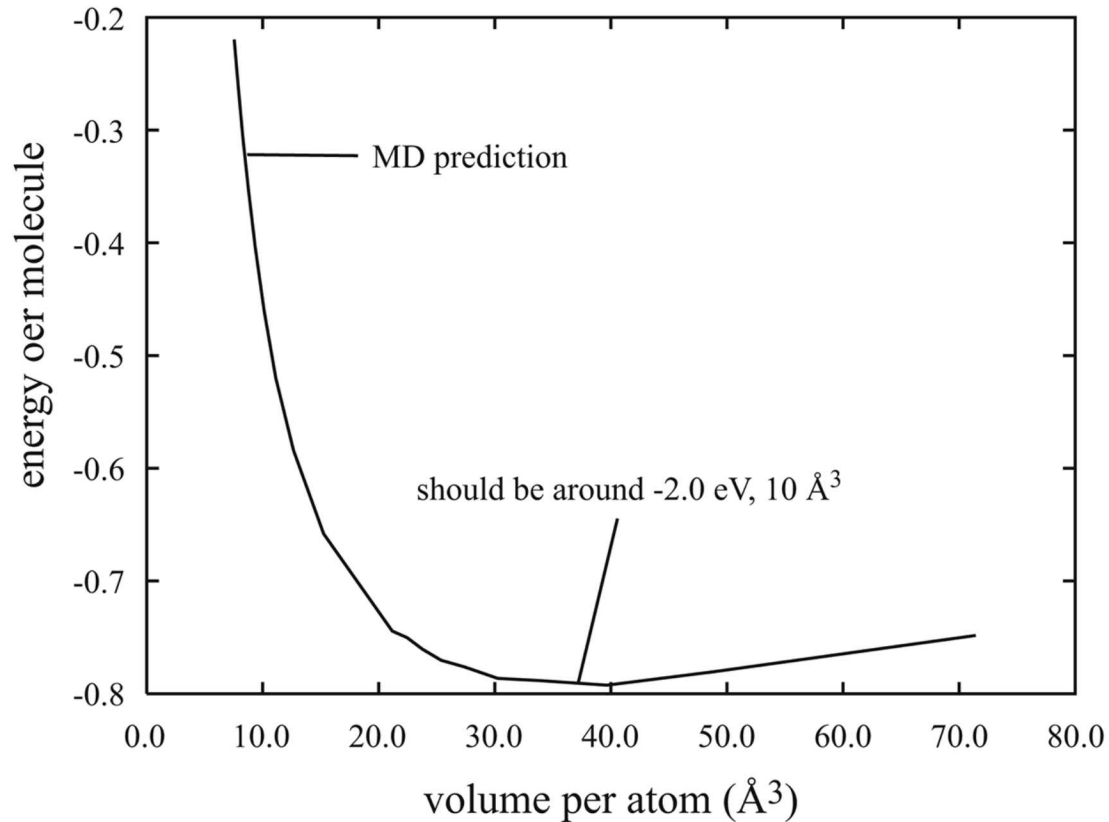
- ❑ Fitted all 36 molecular interactions needed for Mg, H₂, MgH₂, BH₄, B₁₂H₁₂
- ❑ Implemented the “molecular” dynamics method in LAMMPS
- ❑ Demonstrated successful “molecular” dynamics simulations
- ❑ Performed simulations for MgB₁₂H₁₂ and Mg(BH₄)₂

MgB_xH_y : “Molecular” Dynamics Simulation

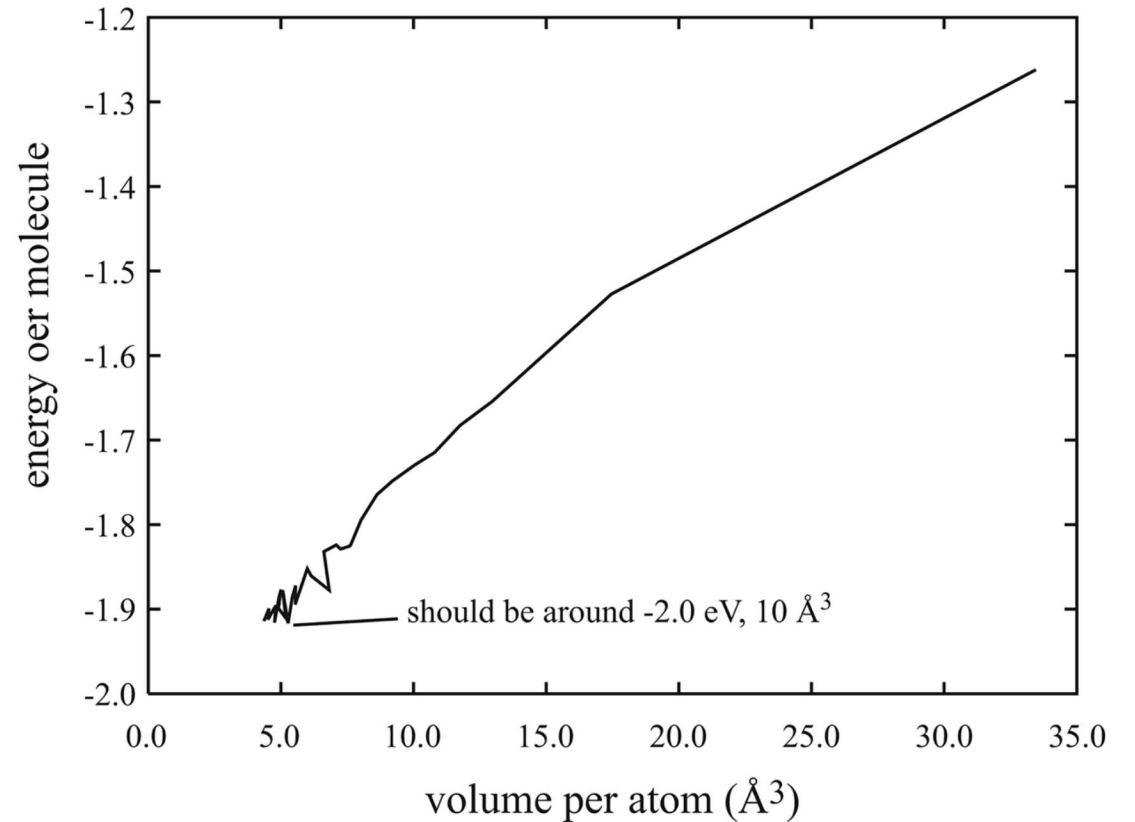


Issues

(a) amorphous $\text{MgB}_{12}\text{H}_{12}$



(b) amorphous $\text{Mg}(\text{BH}_4)_2$

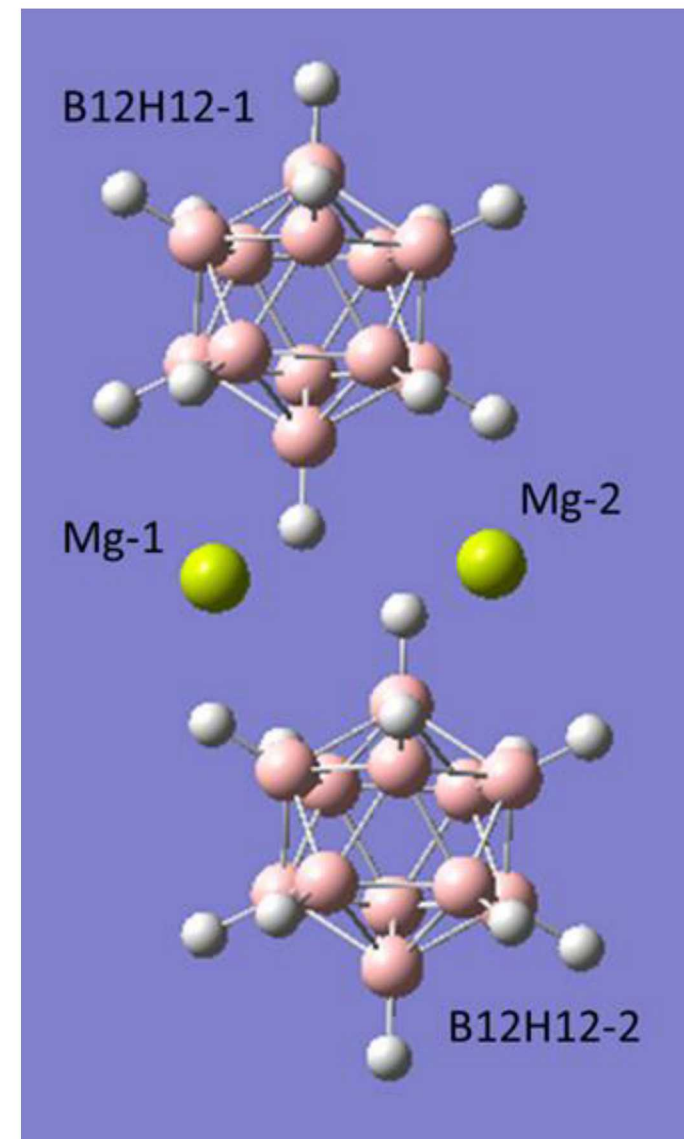


- ❑ MD matches DFT on isolated molecule-molecule cases, but not on condensed phases
- ❑ Solution: directly fit condensed phases

Origins of the Issues

DFT Energies do not sum up due to charge transfer

	ETOT (Hartree)	Interaction Energy (eV)
Mg (Charge = 2)	-199.2273	
B12H12-1 (Charge = -2)	-305.7702	
B12H12-2 (Charge = -2)	-305.7702	
Mg--Mg (Charge = 4)	-397.9869	12.7284
B12H12 -- B12H12 (Charge = -4)	-611.2426	8.1035
B12H12-1 -- Mg-1 (Charge = 0)	-505.7188	-19.6276
B12H12-1 -- Mg-2 (Charge = 0)	-505.7569	-20.6621
B12H12-2 -- Mg-1 (Charge = 0)	-505.7569	-20.6630
B12H12-2 -- Mg-2 (Charge = 0)	-505.7188	-19.6273
MgB12H12 (Charge = 0)	-505.7188	
MgB12H12 (Charge = 0)	-505.7188	
Mg2(B12H12)2 (Charge = 0)	-1011.6945	-6.9881



Highlights

- ❑ MD tools for PdH_x are mature, and have been applied to study various hydrogen storage problems including the diffusion example presented
- ❑ We have been working on a “molecular” dynamics tool to study complex hydrides such as MgB_xH_y