

# RECENT INTERATOMIC POTENTIAL DEVELOPMENT ACTIVITIES AT SANDIA

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# Two Topics

- Pd-H-He potential
- Mg-B-H potential



# Pd-H-He Potential - Motivation

- Pd is a solid-state tritium storage material
- Tritium decays to He, forming He bubbles
- Bubbles causes PCT shift, swelling, He release, all leading to failures
- MD can study bubble nucleation / growth



# Criteria for Acceptable Pd-H-He Potential

- Octahedral interstitial sites in fcc
- Low He diffusion barrier (~0.1 eV)
- Large He swelling (~10 Å<sup>3</sup>)
- Short He-He spacing in Pd (~1.7 Å)
- Non-bonding in pure He (equation of state)
- Strong He-He attraction in Pd (~-0.85 eV)
- Correct volume and energy for PdHe rock-salt
- Correct Pd vacancy and He insertion energies as a function of He number
- Stringent MD tests



# Two Paradoxes

- Increasing swelling is against a low diffusion energy barrier
- Increasing He-He attraction in Pd is against He-He repulsion in pure He



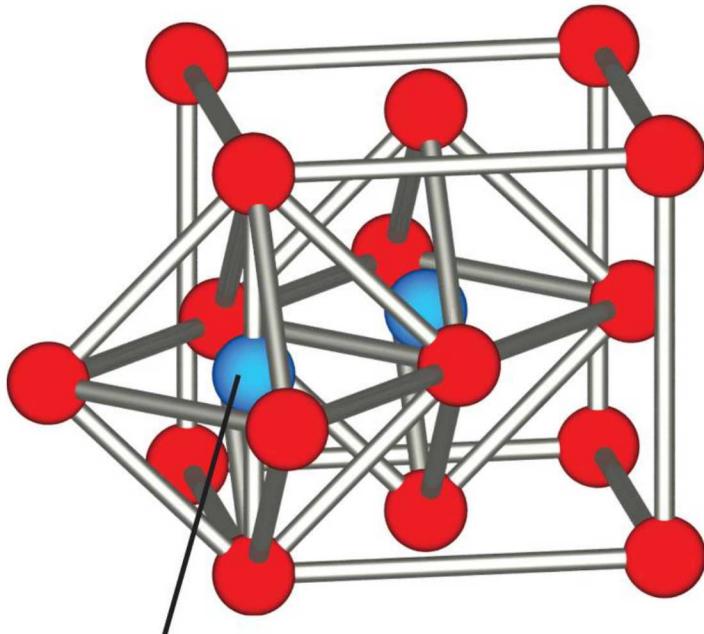
# Past MD Simulations of He Bubbles

- Two papers are published after 2016
- Nuc. Sci. Tech. 27, 106 (2016) prescribes incorrect tetrahedral H sites and manually creates He bubbles
- J. Chem. Phys. 144, 194705 (2016) prescribes a He diffusion energy barrier of  $> 3.0$  eV
- He bubbles in W have been successfully studied, see, for example, Nucl. Fusion, 53, 073015 (2013), and J. Nucl. Mater., 432, 61 (2013)



# Difference between Pd and W

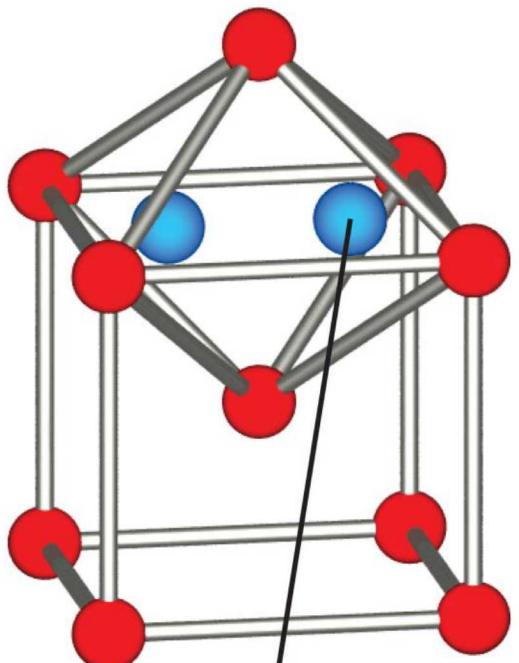
(a) He sites in fcc Pd



octahedral sites  
(with spacing = 2.75 Å)

DFT He-He spacing in Pd = 1.7 Å

(b) He sites in bcc W



tetrahedral sites  
(with spacing 1.58 Å)

- **He at octa sites in fcc Pd but tetra sites in bcc W**
- **Diffusion barrier is smaller in bcc than in fcc**
- **Octa spacing in Pd is way longer than He-He spacing**
- **Tetra spacing in W is short than He-He spacing**



# Solution

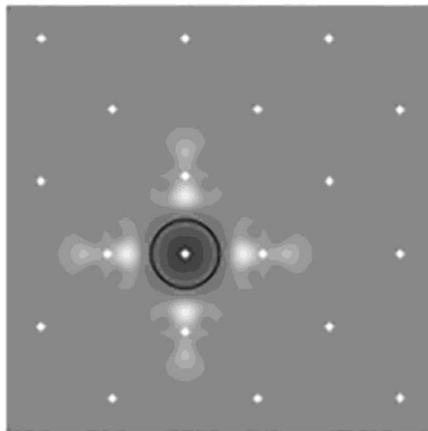
- Use the EAM potential by Finnis-Sinclair\*:  $\rho_i = \rho_j^i(r_{ij})$ , as opposed to the one by Daw-Baskes\*\*:  $\rho_i = \rho_j(r_{ij})$
- Electron density created by Pd at He sites is negative
- Electron density created by He at He sites is positive
- He embedding energy is minimum at zero electron density
- Use EAM's many-body effect to increase swelling

\*Phil. Mag. A 50, 45 (1984), \*\*Phys. Rev B. 29, 6443 (1984).

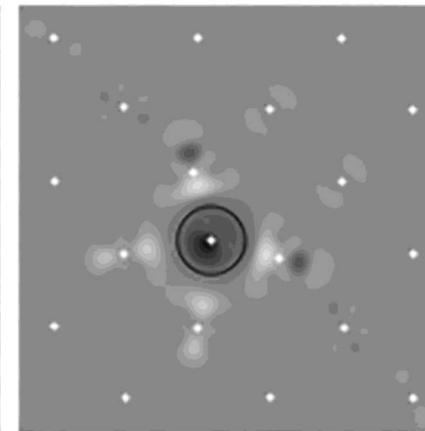


# DFT Justification

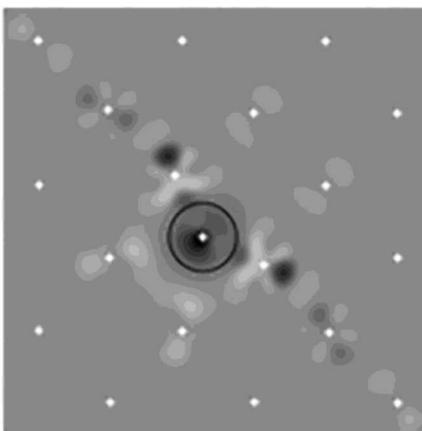
(a) octahedral site (b) step 1



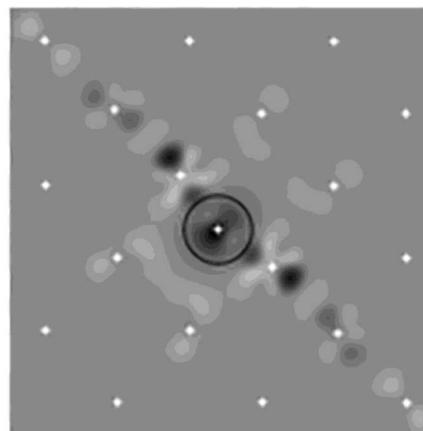
(c) step 2



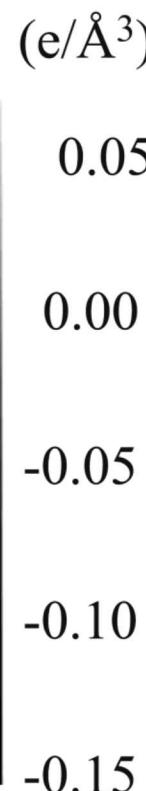
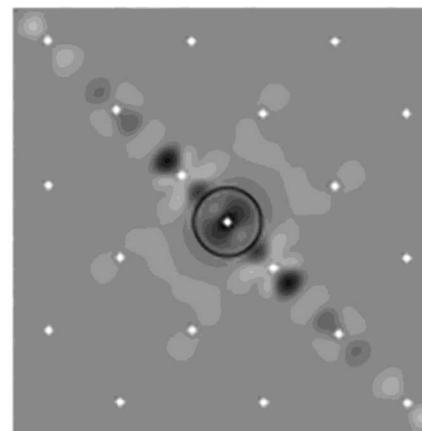
(d) step 3



(e) step 4



(f) saddle point



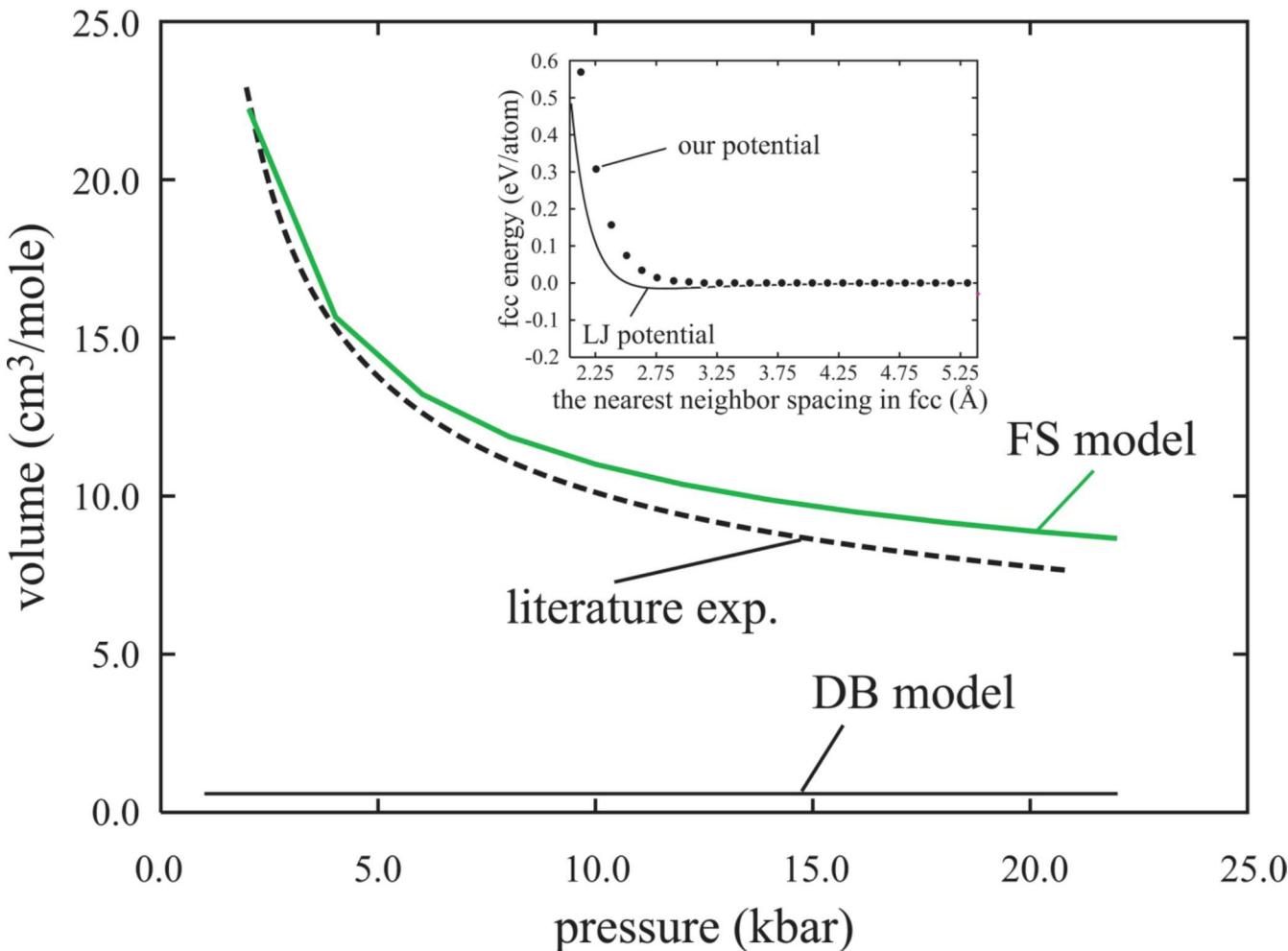
- **He always repels electrons towards Pd**
- **The electron transfer processes are complex**

# Validation of Some Critical Properties

methods	$Q_{He}$	$\Omega_{0,H}$ e	$\Omega_{He,He}$	$\Omega_{H,He}$	$E_{He}$	$r_{He-He}$	$E_{He-He}$	$\Delta\Omega_{Pd \rightarrow Pd}$ He	$\Delta E_{Pd \rightarrow PdH}$ e
DB	0.19	10.1	10.0	9.7	3.63	1.75	-0.87	9.2	2.92
FS	0.14	8.7	18.8	8.4	4.04	1.72	-1.49	13.6	2.95
PBE	0.11	9.7	10.3	9.5	3.64	1.7	-0.87	6.7	2.99
LDA	0.07	7.3	8.0	10.1	3.63	1.7	-0.85	7.4	2.96



# Validation of He Equation of State

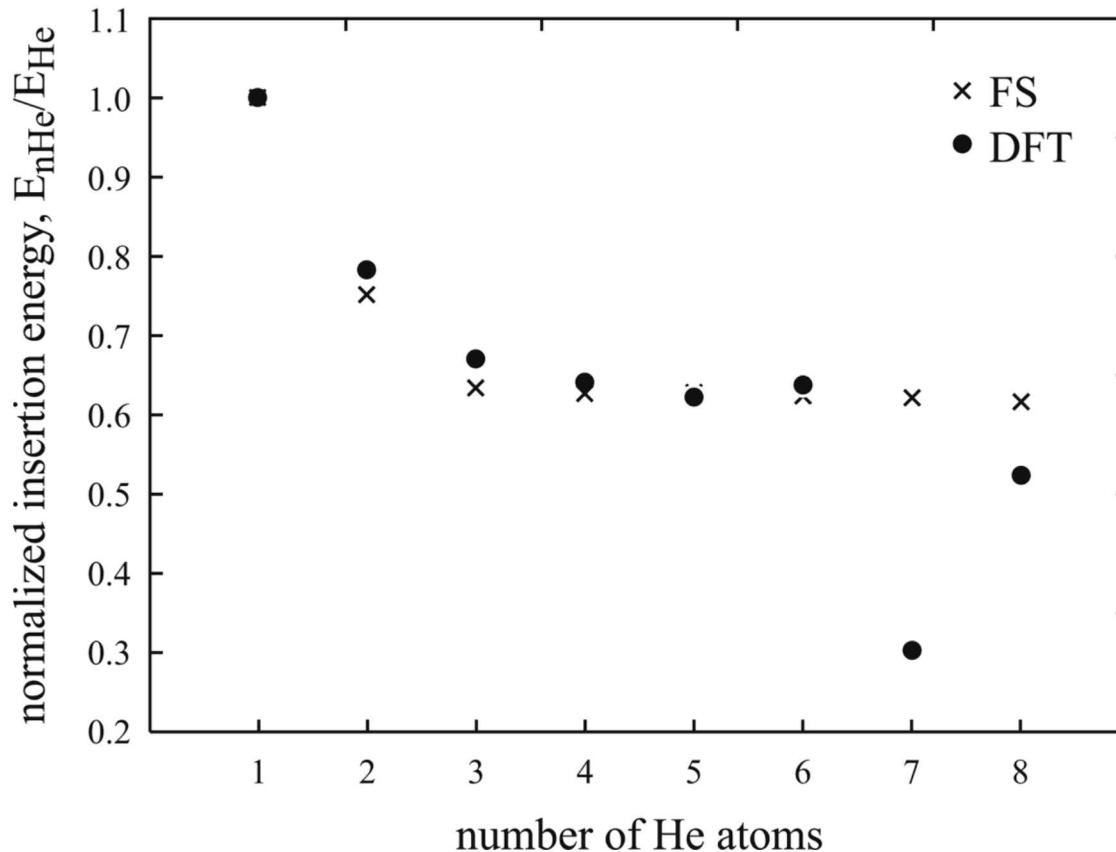


- Our He-He interactions are purely repulsive and can capture well the He equation of state
- Our pure He potential is not that different from literature LJ potential\*\*

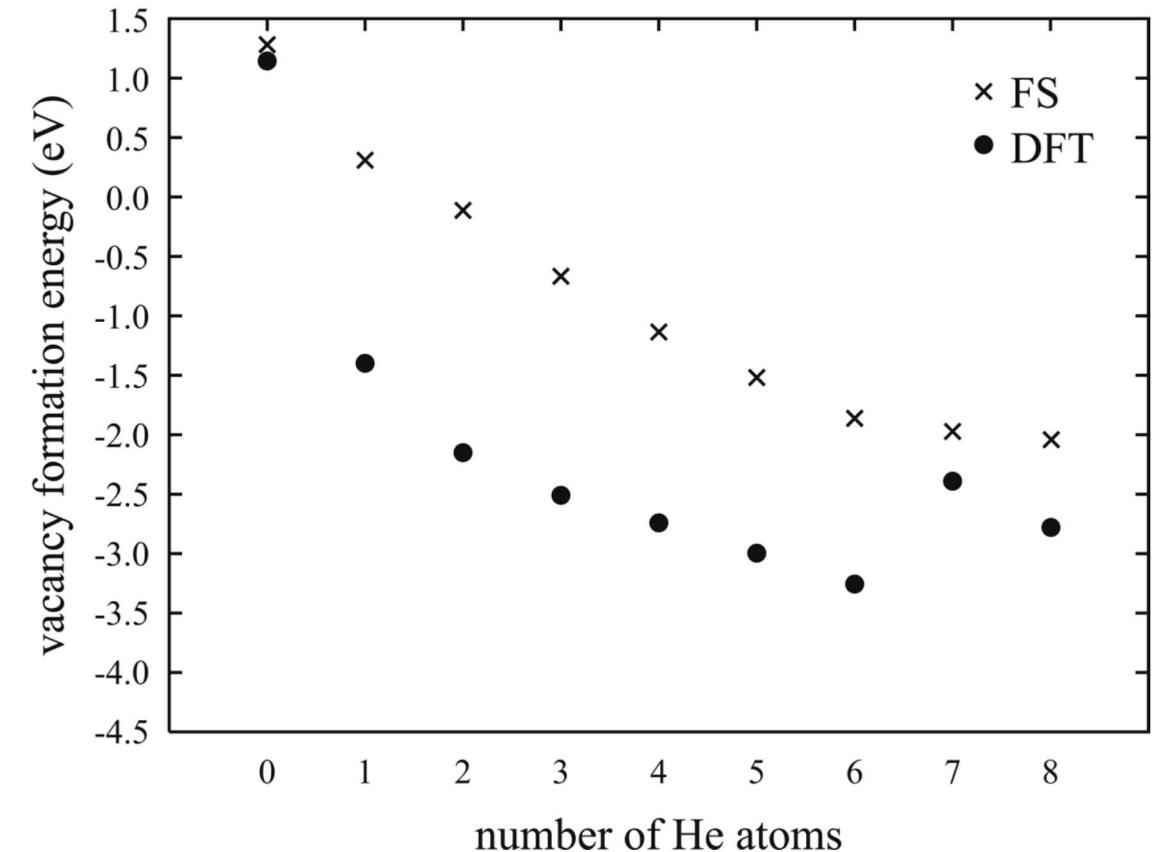
\*literature equation of state: Phys. Rev. B, 21, 5137 (1980), \*\*LJ: J. Chem. Phys. 144, 194705 (2016)

# Validation of He Insertion and Pd Vacancy Energies

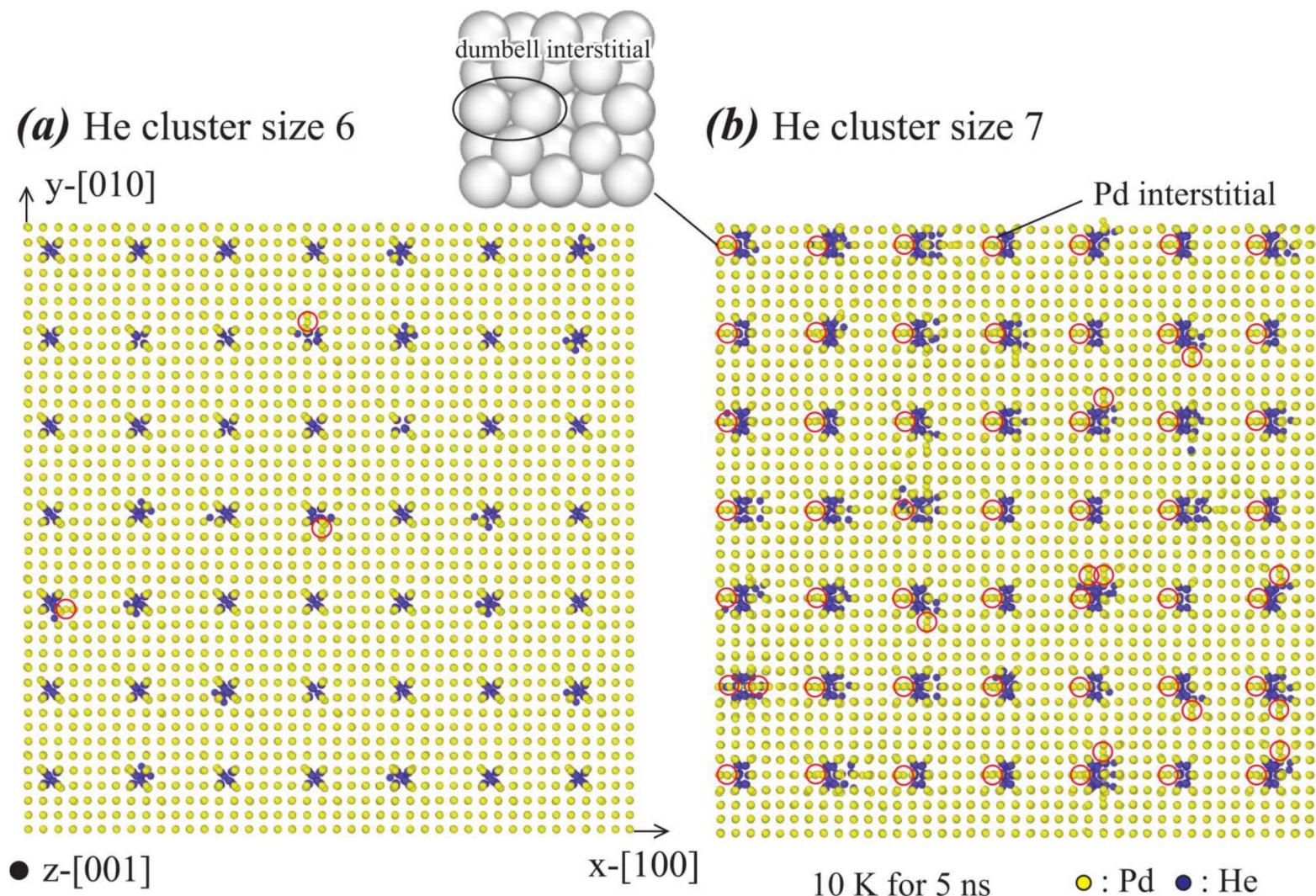
(a) normalized He insertion energy (at He # 1)



(b) Pd vacancy formation energy

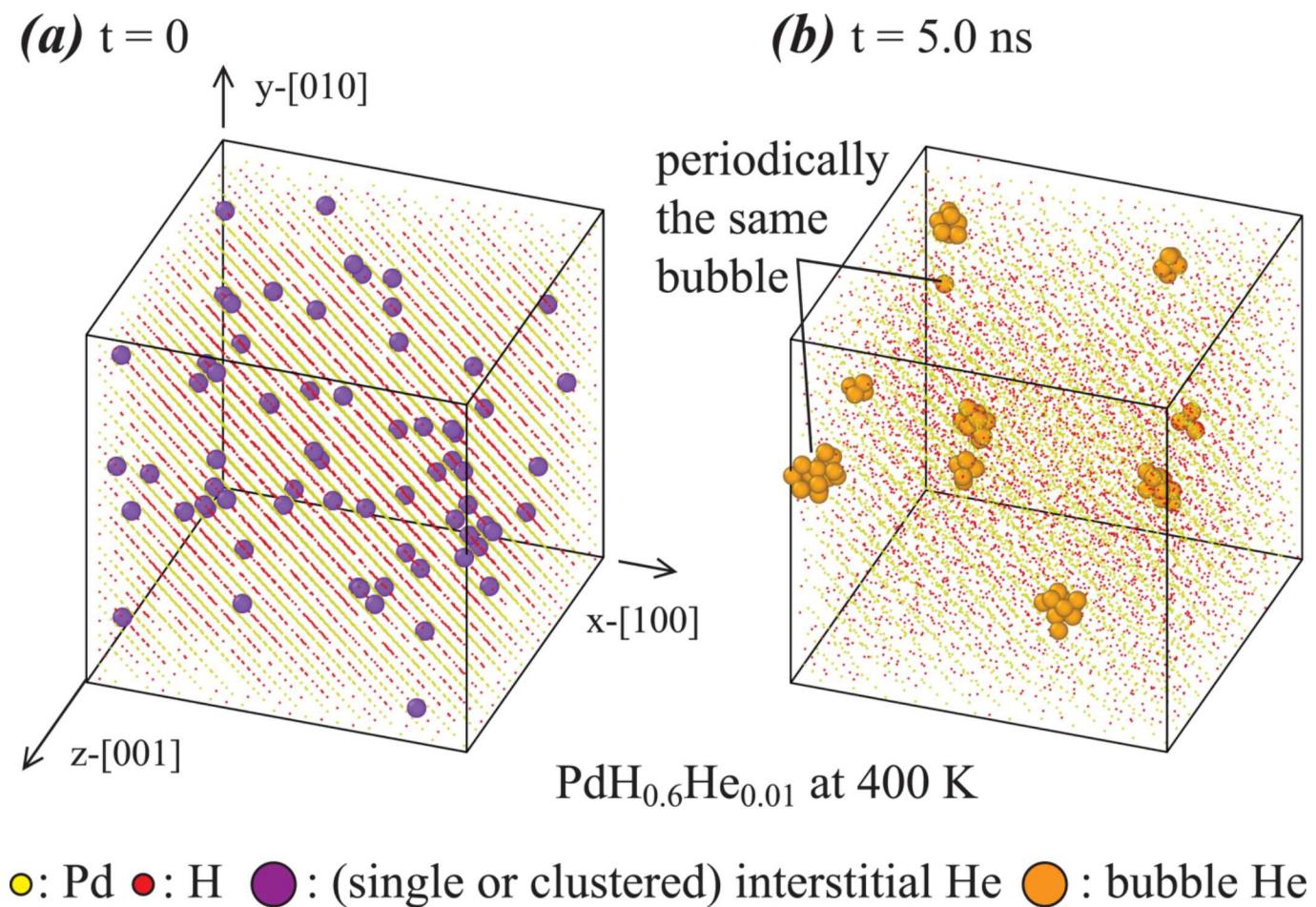


# Validation of Critical He Size



- At He size 6, few Pd interstitials are seen
- At He size 7, all He clusters induce Pd interstitials, in good agreement with DFT results

# Stringent MD Tests



- Initially, He atoms are randomly populated at octahedral sites in a  $\text{PdH}_{0.6}$  lattice
- After MD simulations at 400 K for 5 ns, He bubbles are formed
- Enables simulations of bubble formation without assumptions

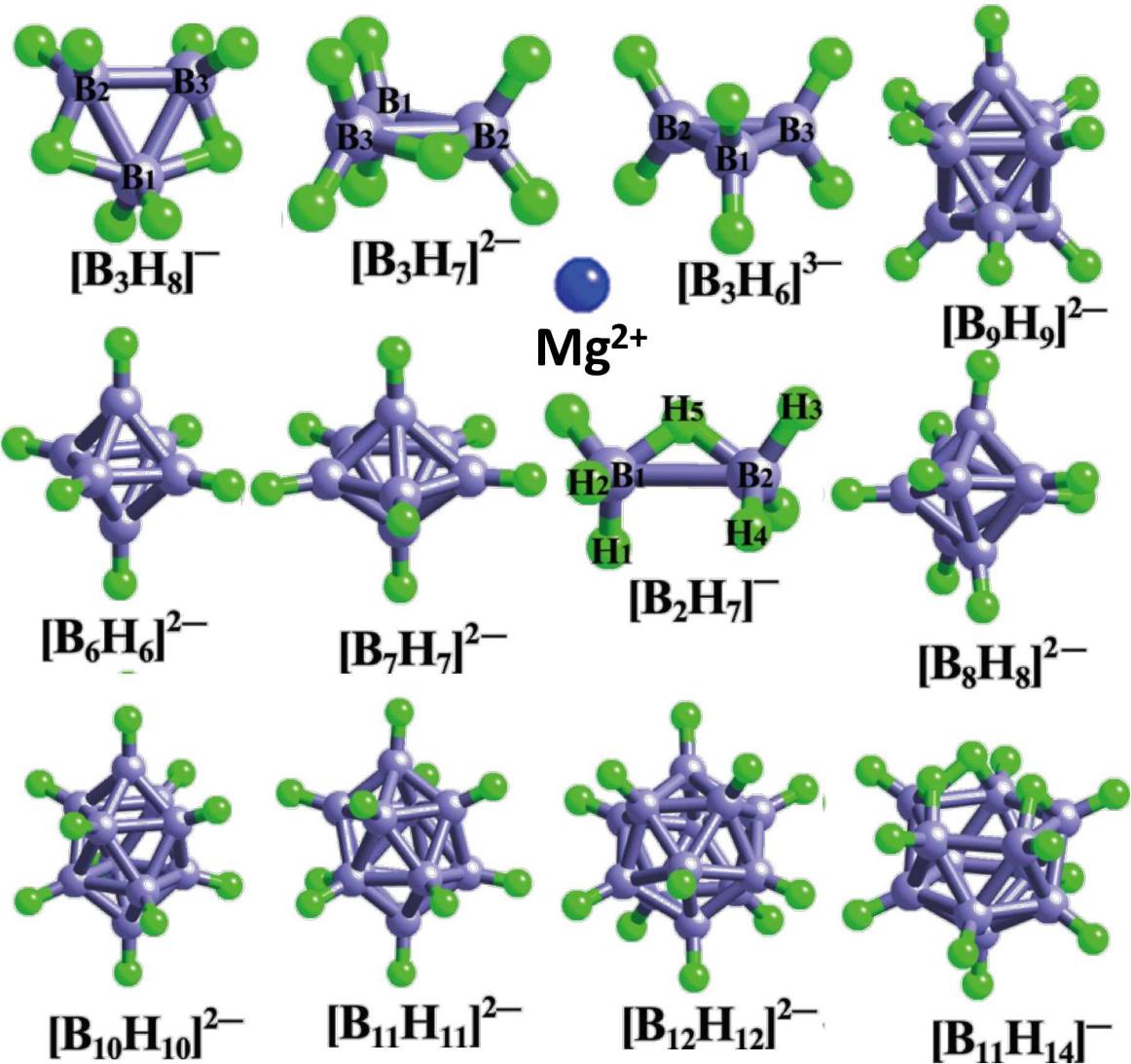
# Mg-B-H Potential - Motivation

- Hydrogen is an efficient and clean energy carrier
- Solid state hydrogen storage materials draw interests due to an ideal combination of volumetric and gravimetric densities
- HyMARC (Hydrogen Materials Advanced Research Consortium) aims to develop an understanding on how to improve (de)hydrogenation kinetics
- Magnesium boron hydrides are one type of materials being explored within HyMARC

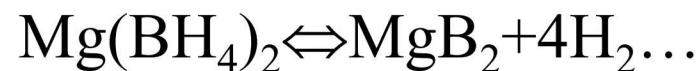
# Perspective

- LLNL is developing a phase field model for (de)hydrogenation kinetics of  $\text{MgB}_x\text{H}_y$
- The phase field model requires thermodynamic and kinetic properties as inputs
- Many molecules may occur, and many exhibit amorphous structures  
⇒ challenging for DFT studies
- We will use MD to fill the gaps

## Example Molecules



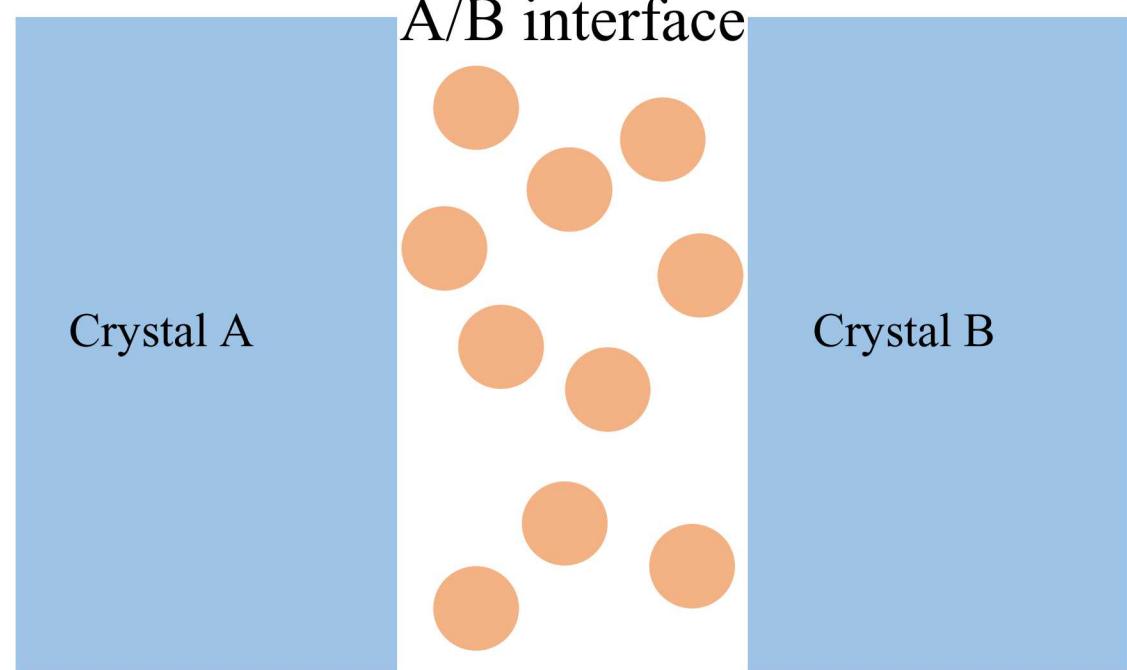
# $\text{MgB}_x\text{H}_y$ : Two Goals



...

- Many molecules were observed in NMR, XES, XAS, but not XRD  $\Rightarrow$  amorphous
- DFT is not sufficient for amorphous complex hydrides

Goal 1: Use MD to evaluate stabilities of different intermediates



- Interfaces between crystalline solids are often exhibit amorphous “soup” containing different molecular species

Goal 2: Use MD to calculate interfacial energies

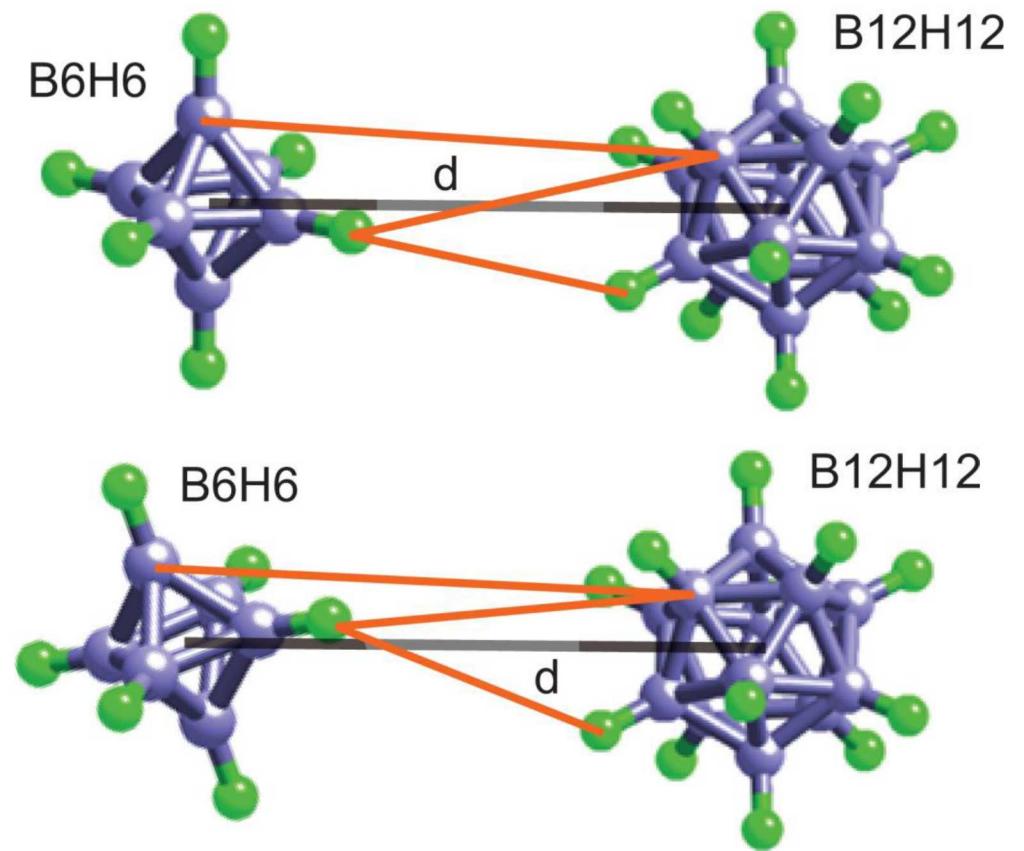
# Molecular Dynamics Challenges

- Traditional MD can only simulate atoms, but we have molecules
- We will develop an innovative “molecular” dynamics method
  - An intra-molecule force field to stabilize molecules
  - An inter-molecule force field to capture energetics
  - MD must track which atom is in which molecule
- As a first trial, we parameterize force fields DFT energies between two isolated molecules
- Five molecules ( $\text{Mg}$ ,  $\text{H}_2$ ,  $\text{MgH}_2$ ,  $\text{BH}_4$ ,  $\text{B}_{12}\text{H}_{12}$ ) are considered

# MgB<sub>x</sub>H<sub>y</sub>: Methods

- Energy comes from interactions between atoms from different (similar and dissimilar) molecules
- Perform DFT calculations of energies of all pairs of molecules at various distances and angles
- Fit pair potentials to DFT energies
- Implement the approach in LAMMPS

Interactions between different pairs of species are distinguished by rotation

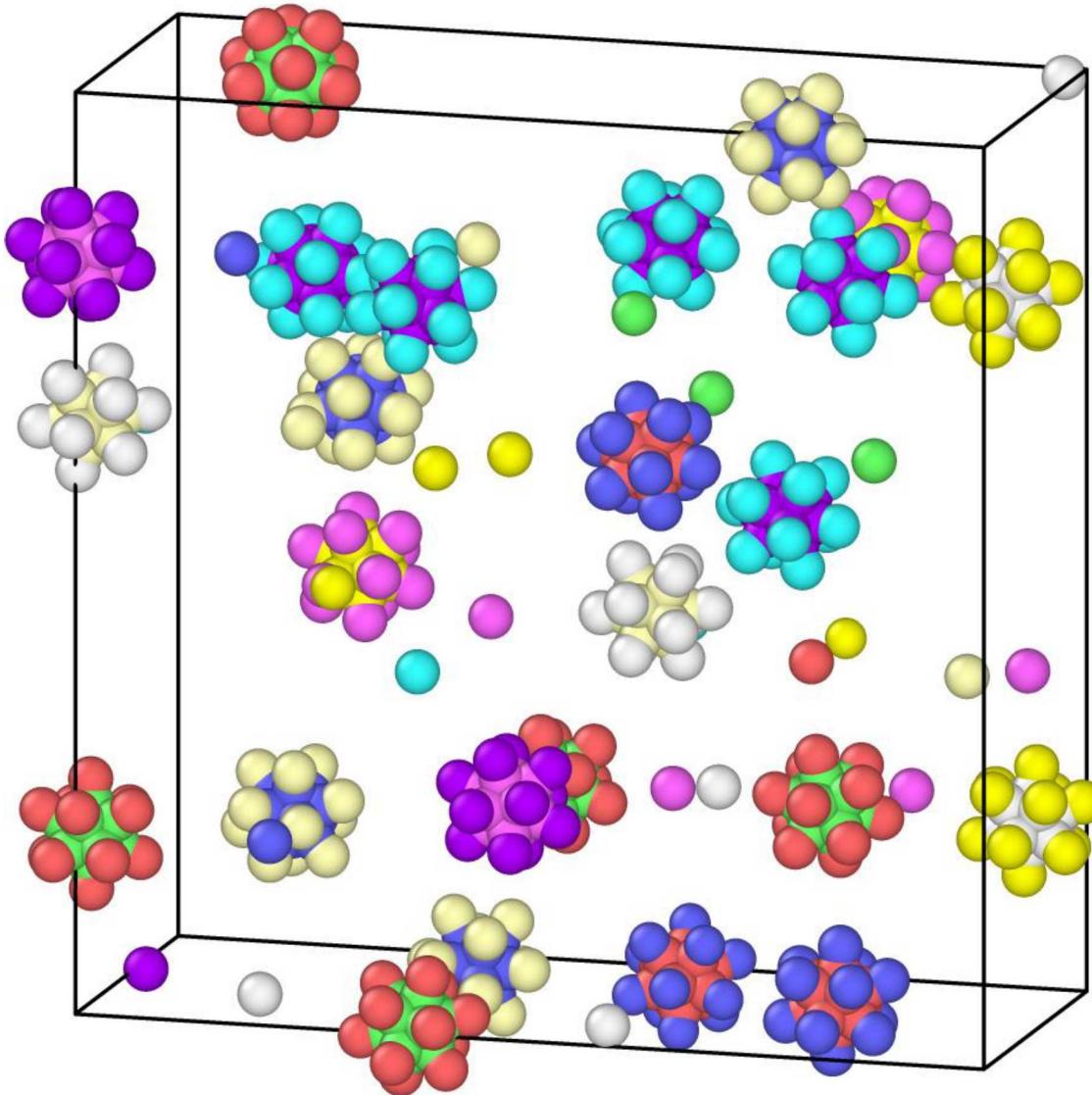


# 36 Inter-Molecule Interactions

□ For a  $\text{Mg} + \text{H}_2 + \text{BH}_4 + \text{MgH}_2 + \text{B}_{12}\text{H}_{12}$  model, there are 36 inter-molecule interactions:

$\text{Mg}-\text{Mg}(\text{Mg}-\text{Mg})$ ,  $\text{Mg}-\text{H}_2(\text{Mg}-\text{H})$ ,  $\text{Mg}-\text{BH}_4(\text{Mg}-\text{B}, \text{Mg}-\text{H})$ ,  $\text{Mg}-\text{MgH}_2(\text{Mg}-\text{Mg}, \text{Mg}-\text{H})$ ,  $\text{Mg}-\text{B}_{12}\text{H}_{12}(\text{Mg}-\text{B}, \text{Mg}-\text{H})$ ,  $\text{H}_2-\text{H}_2(\text{H}-\text{H})$ ,  $\text{H}_2-\text{BH}_4(\text{H}-\text{B}, \text{H}-\text{H})$ ,  $\text{H}_2-\text{MgH}_2(\text{H}-\text{Mg}, \text{H}-\text{H})$ ,  $\text{H}_2-\text{B}_{12}\text{H}_{12}(\text{H}-\text{B}, \text{H}-\text{H})$ ,  $\text{BH}_4-\text{BH}_4(\text{B}-\text{B}, \text{B}-\text{H}, \text{H}-\text{H})$ ,  $\text{BH}_4-\text{MgH}_2(\text{B}-\text{Mg}, \text{B}-\text{H}, \text{H}-\text{Mg}, \text{H}-\text{H})$ ,  $\text{BH}_4-\text{B}_{12}\text{H}_{12}(\text{B}-\text{B}, \text{B}-\text{H}, \text{H}-\text{B}, \text{H}-\text{H})$ ,  $\text{MgH}_2-\text{MgH}_2(\text{Mg}-\text{Mg}, \text{Mg}-\text{H}, \text{H}-\text{H})$ ,  $\text{MgH}_2-\text{B}_{12}\text{H}_{12}(\text{Mg}-\text{B}, \text{Mg}-\text{H}, \text{H}-\text{B}, \text{H}-\text{H})$ ,  $\text{B}_{12}\text{H}_{12}-\text{B}_{12}\text{H}_{12}(\text{B}-\text{B}, \text{B}-\text{H}, \text{H}-\text{H})$

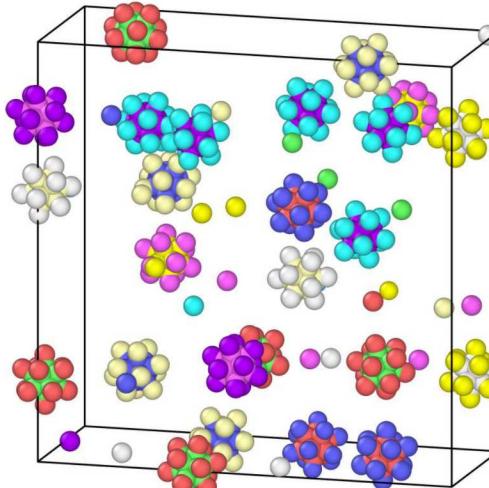
# MD Implementation



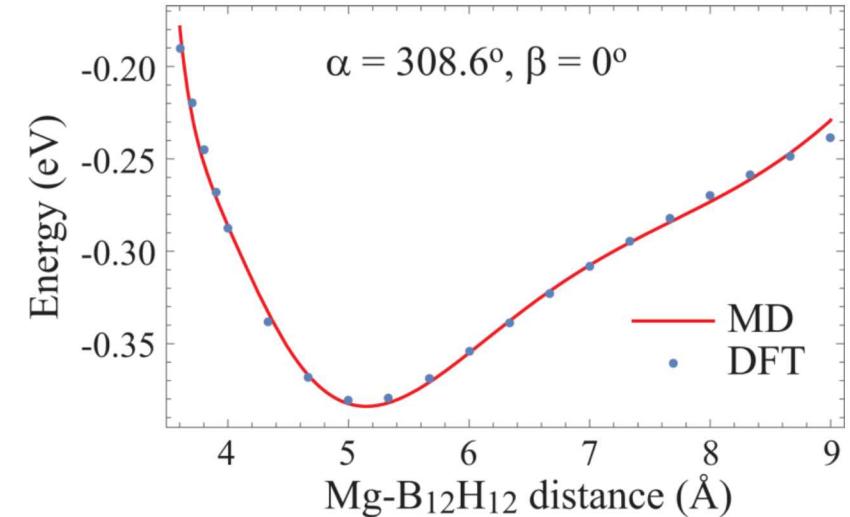
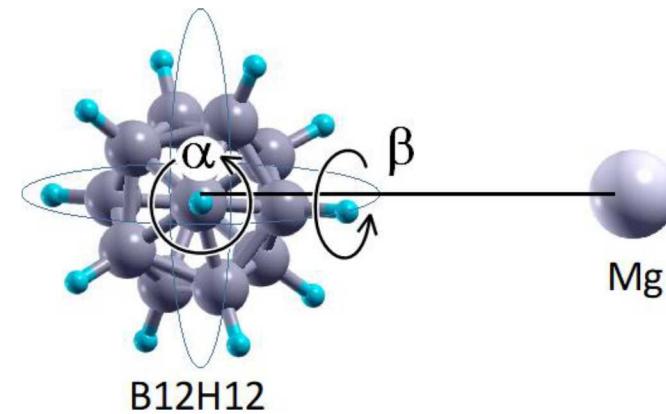
- Atom-based MD does not know molecules
- Assign different atom types for different molecules
- Create mapping tables between atom types and pair interactions

# Progress

## “Molecular” Dynamics Case

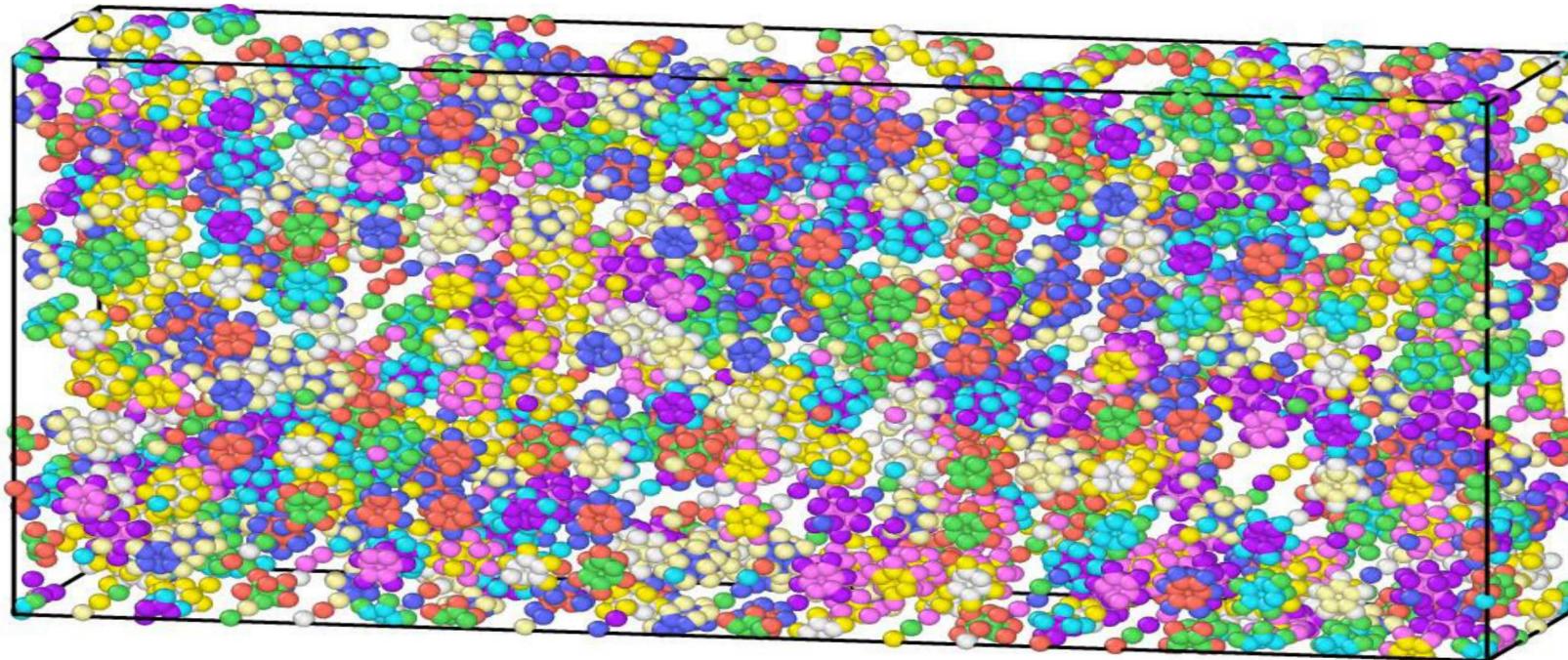


## Example Mg-B<sub>12</sub>H<sub>12</sub> Interaction



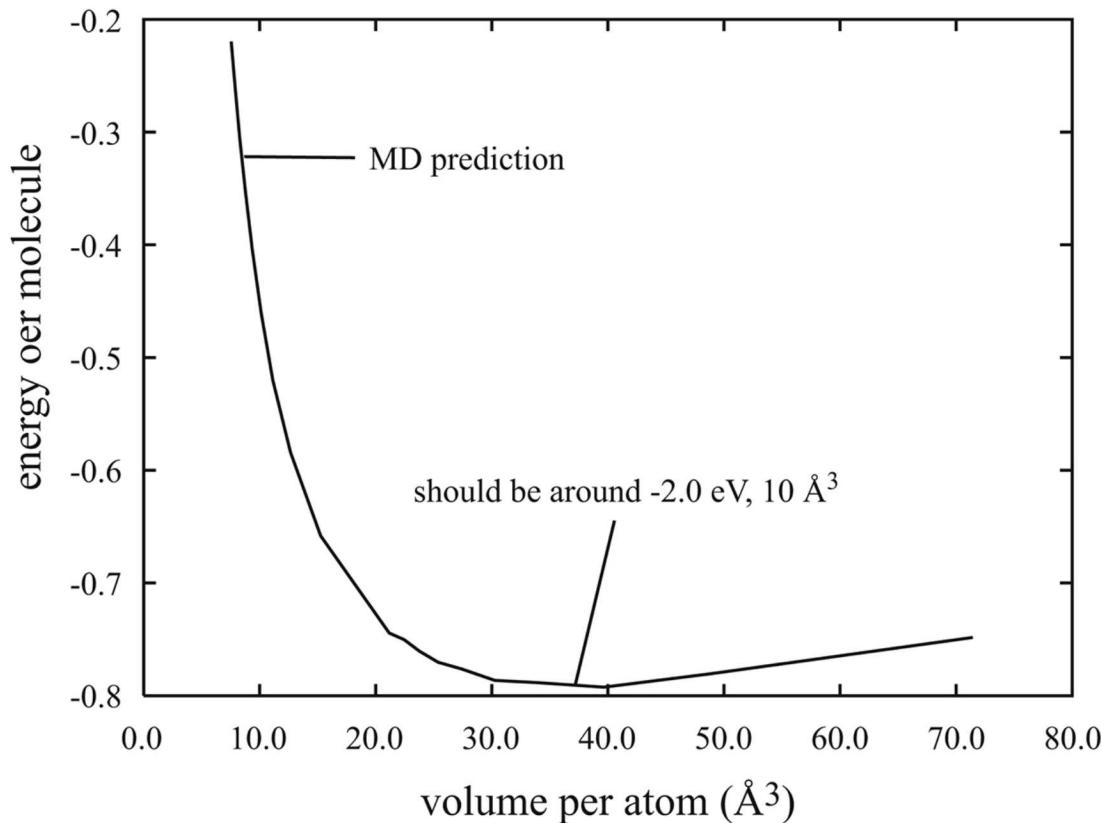
- Fitted all 36 molecular interactions needed for Mg, H<sub>2</sub>, MgH<sub>2</sub>, BH<sub>4</sub>, B<sub>12</sub>H<sub>12</sub>
- Implemented the “molecular” dynamics method in LAMMPS
- Demonstrated successful “molecular” dynamics simulations
- Performed simulations for MgB<sub>12</sub>H<sub>12</sub> and Mg(BH<sub>4</sub>)<sub>2</sub>

# $MgB_xH_y$ : “Molecular” Dynamics Simulation

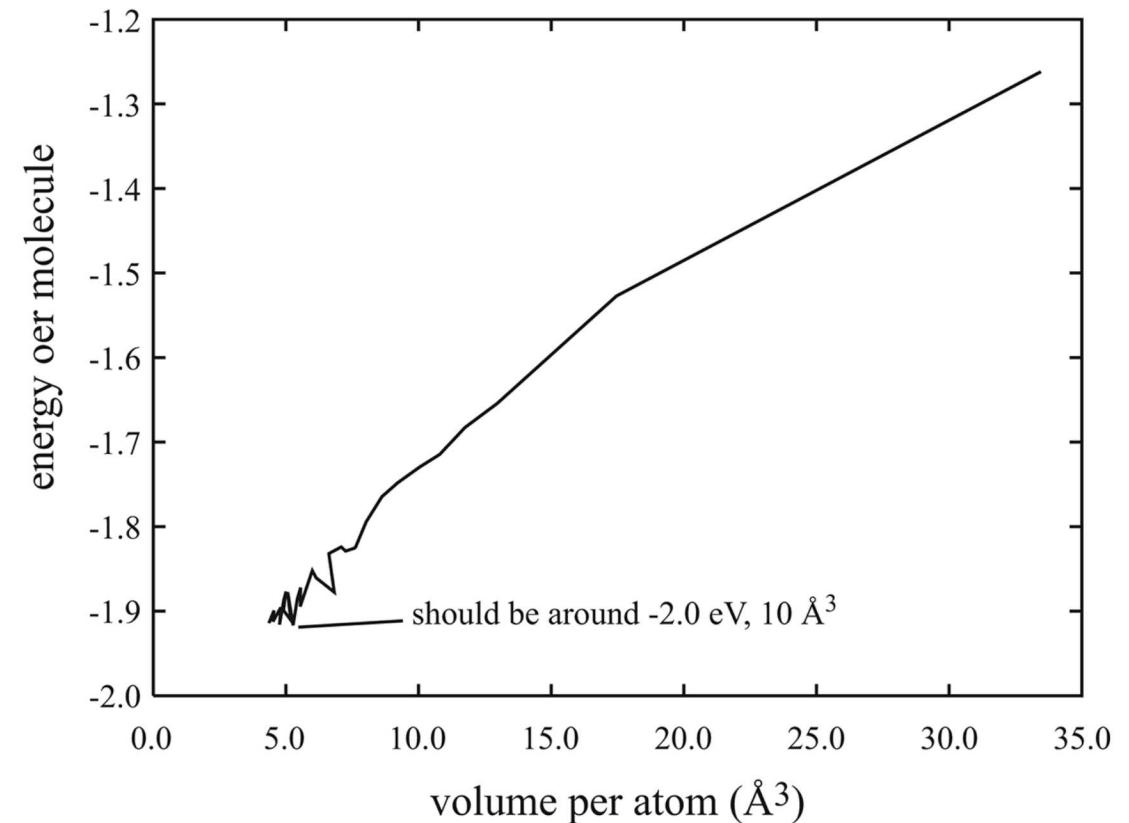


# Issues

(a) amorphous  $\text{MgB}_{12}\text{H}_{12}$



(b) amorphous  $\text{Mg}(\text{BH}_4)_2$

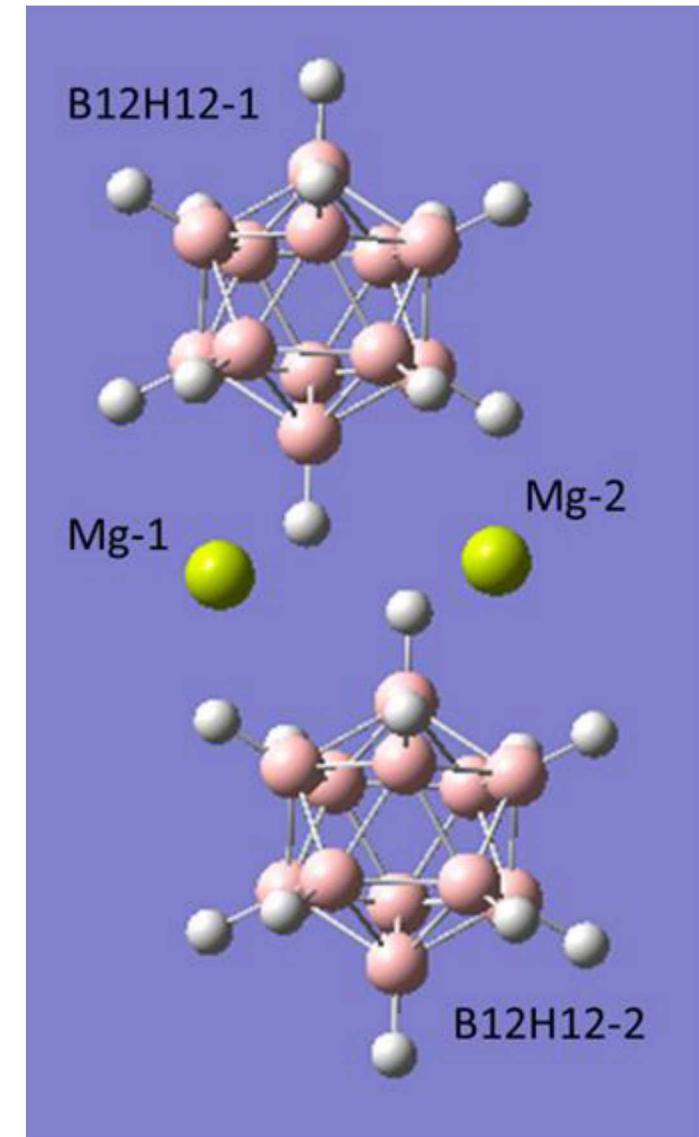


- MD matches DFT on isolated molecule-molecule cases, but not on condensed phases
- Solution: directly fit condensed phases

# Origins of the Issues

DFT Energies do not sum up due to charge transfer

	ETOT (Hartree)	Interaction Energy (eV)
Mg (Charge = 2)	-199.2273	
B12H12-1 (Charge = -2)	-305.7702	
B12H12-2 (Charge = -2)	-305.7702	
Mg--Mg (Charge = 4)	-397.9869	12.7284
B12H12 -- B12H12 (Charge = -4)	-611.2426	8.1035
B12H12-1 -- Mg-1 (Charge = 0)	-505.7188	-19.6276
B12H12-1 -- Mg-2 (Charge = 0)	-505.7569	-20.6621
B12H12-2 -- Mg-1 (Charge = 0)	-505.7569	-20.6630
B12H12-2 -- Mg-2 (Charge = 0)	-505.7188	-19.6273
MgB12H12 (Charge = 0)	-505.7188	
MgB12H12 (Charge = 0)	-505.7188	
Mg <sub>2</sub> (B12H12) <sub>2</sub> (Charge = 0)	-1011.6945	-6.9881



# Highlights

- MD tools for  $\text{PdH}_x$  are mature, and have been applied to study various hydrogen storage problems including the diffusion example presented
- We have been working on a “molecular” dynamics tool to study complex hydrides such as  $\text{MgB}_x\text{H}_y$