



Sandia
National
Laboratories



SAND2020-1723PE

Shock Waves

Steven N. Todd PhD

sntodd@sandia.gov

Sandia National Laboratories

Energetic Systems Research 05437

(505) 844-5274



Sandia
National
Laboratories



Outline

- What is a shock wave?
- How does a shock wave form?
- Wave types
- Shock Waves – Compression & Release
- Shock Wave Reflections

The course will mainly focus on solids

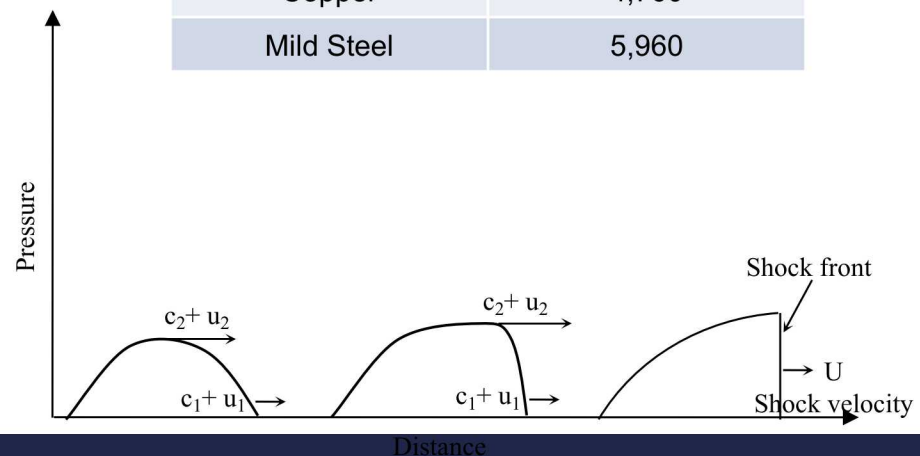


What is a Shock Wave?

- Most materials will transmit sound at a speed that increases with increasing pressure and/or density above a minimum pressure amplitude
- Above the minimum pressure amplitude, the disturbance or compression wave will steepen until it propagates as a jump or discontinuous disturbance which is considered a shock wave

$$c = \sqrt{\frac{dP}{d\rho}}$$

Material	Speed (m/s)
Air (0 °C)	331
Air (20 °C)	343
Water, sea	1,531
Aluminum	6,420
Copper	4,760
Mild Steel	5,960





Sandia
National
Laboratories

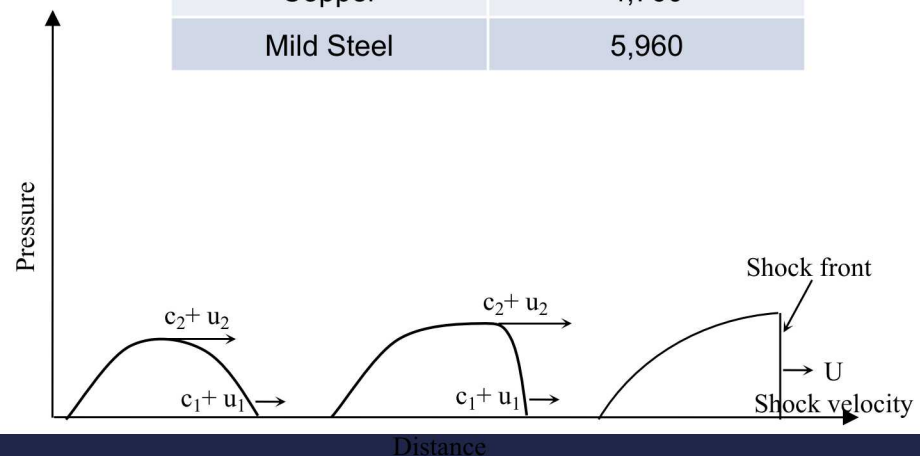


What is a Shock Wave?

- The speed of this compression wave is $c + u$ (c is the sound speed and u is the velocity of the material at a point of interest)
- The speed of the shock wave after formation is U

$$c = \sqrt{\frac{dP}{d\rho}}$$

Material	Speed (m/s)
Air (0 °C)	331
Air (20 °C)	343
Water, sea	1,531
Aluminum	6,420
Copper	4,760
Mild Steel	5,960



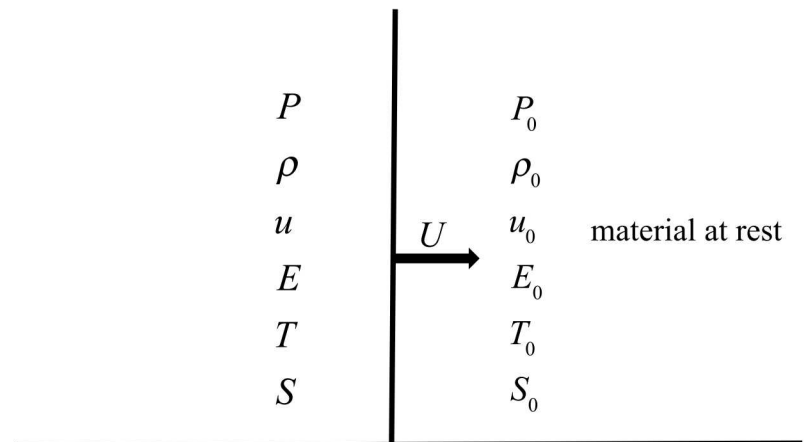


Sandia
National
Laboratories



What is a Shock wave?

- The shock wave produces a jump in pressure (P), density (ρ), particle velocity (u), energy (E), temperature (T), and entropy (S)



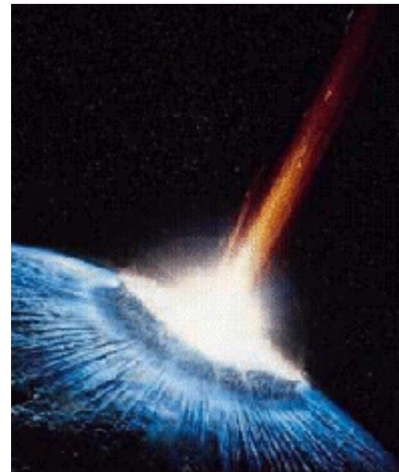


Sandia
National
Laboratories



Examples of How a Shock Wave can Form

- Lighting bolt
- Meteor impact
- Pulsed power
- Accidental or deliberate impacts
- Accidental or deliberate explosions
- Supersonic flow (air flow around jet airplanes)
- Etc.





Sandia
National
Laboratories



Types of Shock Waves

- Compressive
 - Steady
 - Attenuating
- Release
 - Edge
 - Rarefaction
- Collision
 - Compressive
 - Rarefaction
 - Spall



Sandia
National
Laboratories



Compressive Waves

- Occur when pressure is suddenly applied to a material boundary (surface)

→ initial flyer velocity material at res $P_0, \rho_0, u_0, E_0, T_0, S_0$ jump in P, ρ, u, E, T, S



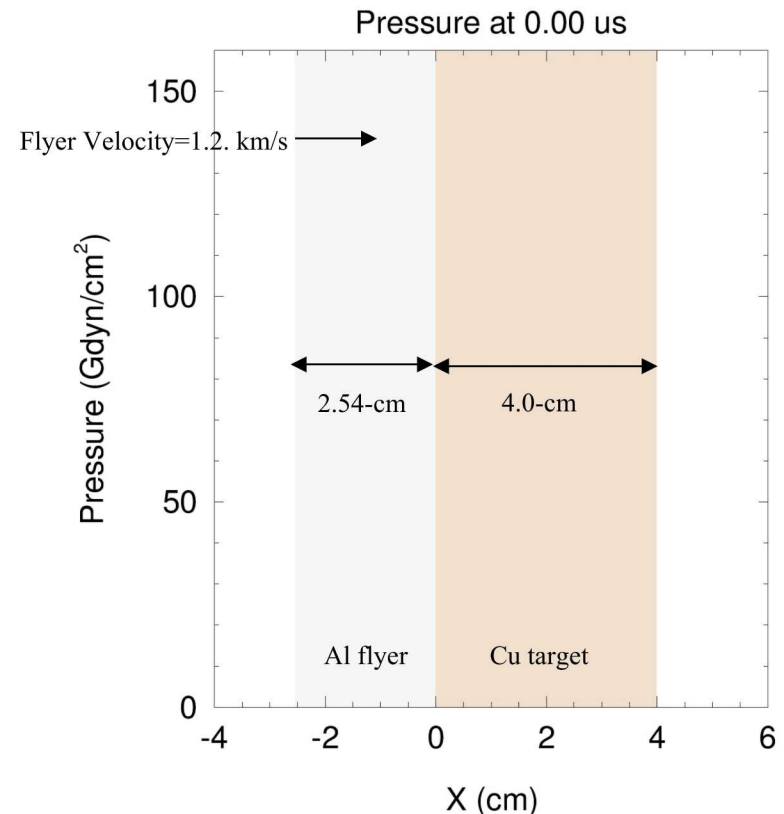


Sandia
National
Laboratories



Compressive Wave

- Aluminum flyer impacting a Copper target
 - 2.54-cm (1-in) Al flyer (1.2 km/s)
 - 4.0-cm (1.575-in) Cu target
 - Upon impact, shock wave propagates into Al flyer and Cu target at the same P and u_p





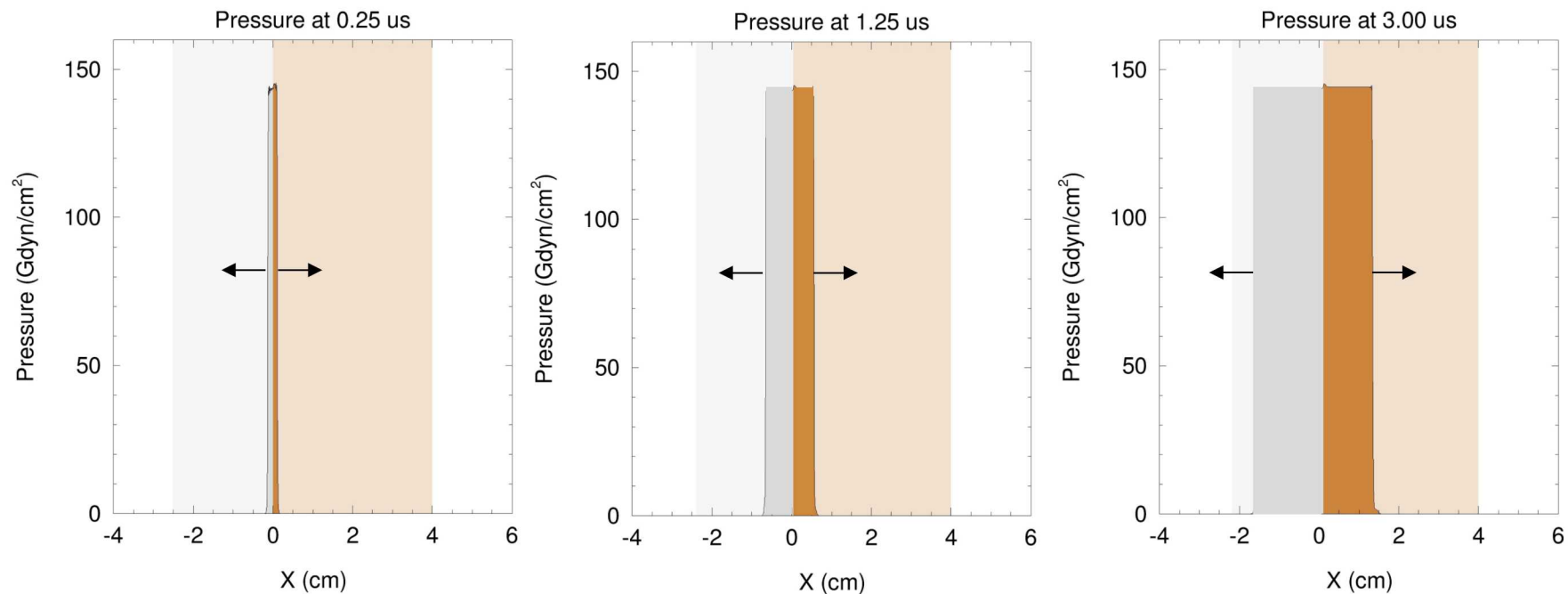
Sandia
National
Laboratories



Impact Compresses The Material

- Aluminum flyer impacting a Copper target

Shock (compression) Wave Propagation

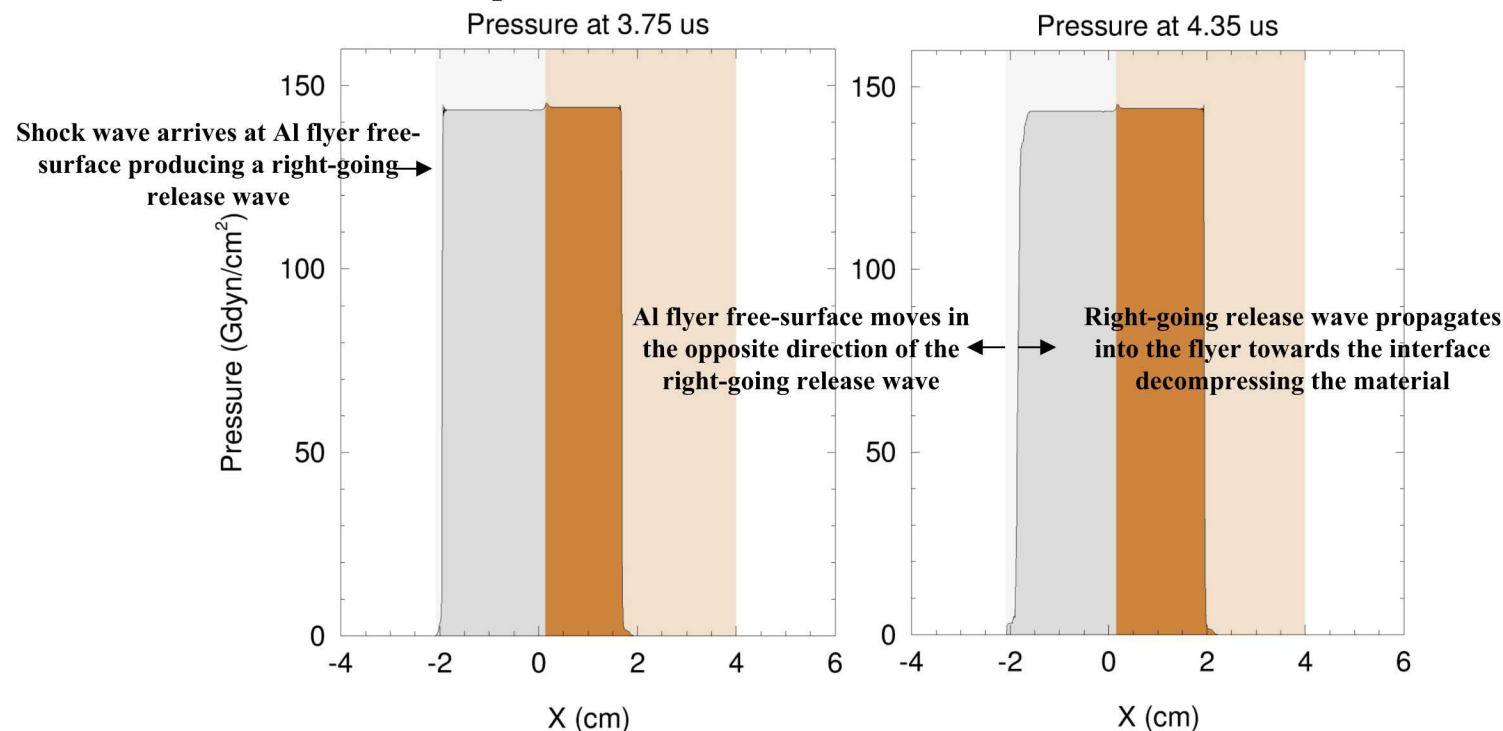




Sandia
National
Laboratories



Decompression of The Material



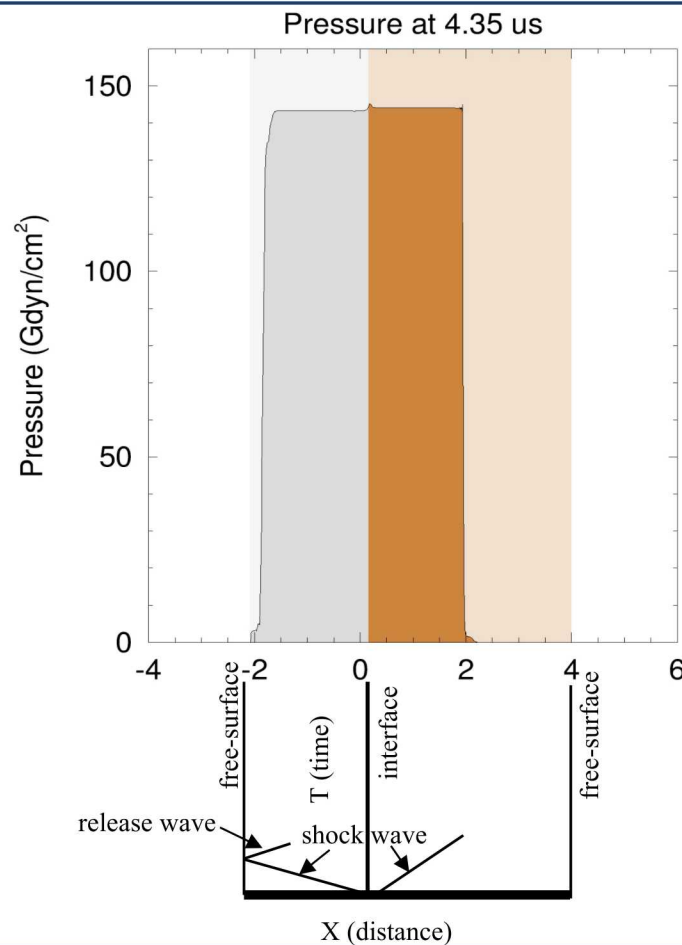
- When the shock wave reaches a free-surface, the free-surface starts to move in a direction away from the interface
- This creates a release, relief, or rarefaction (to rarify) wave that starts to decompress the material



Sandia
National
Laboratories



X – T diagram

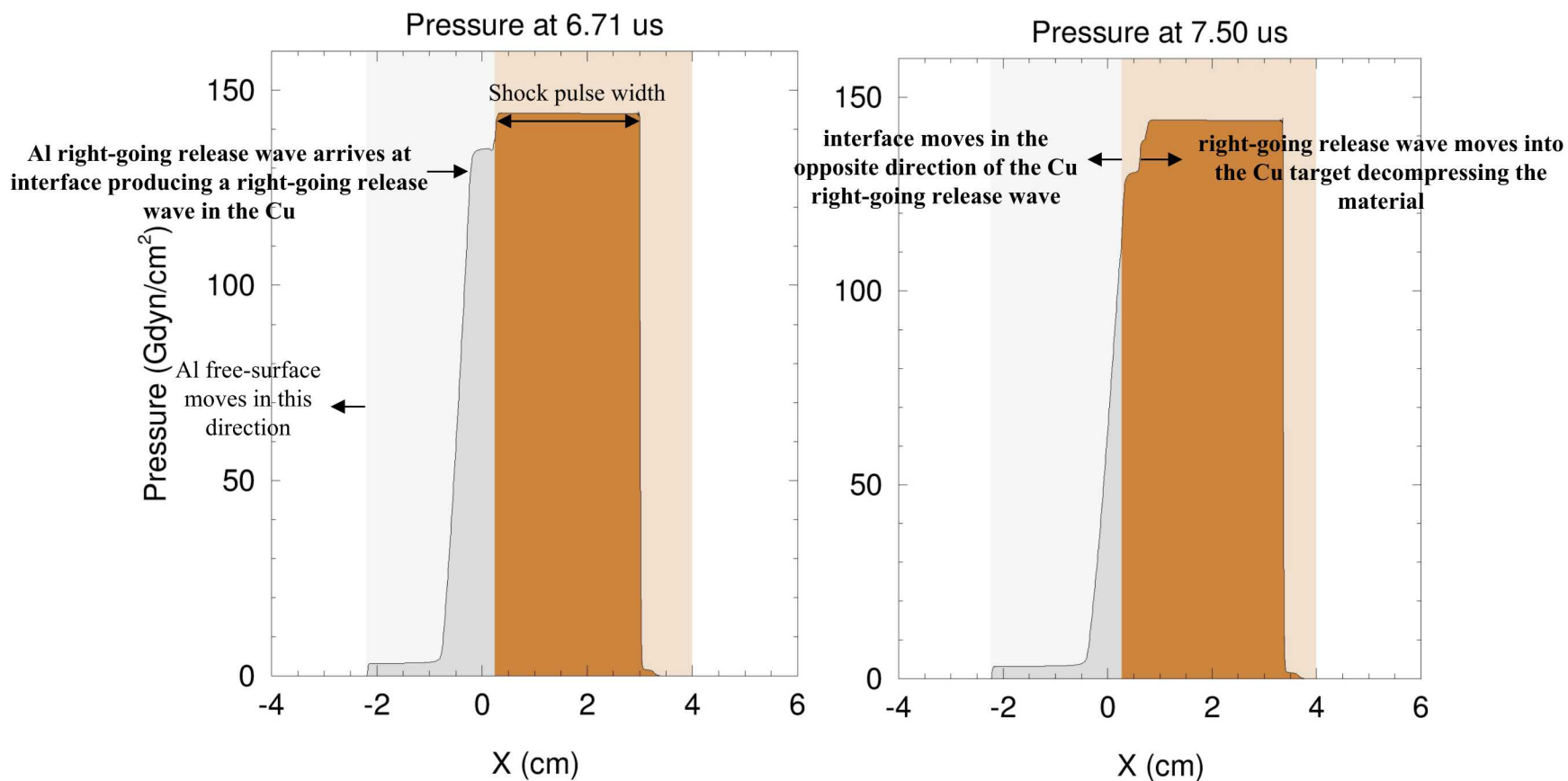




Sandia
National
Laboratories



Decompression of the Material



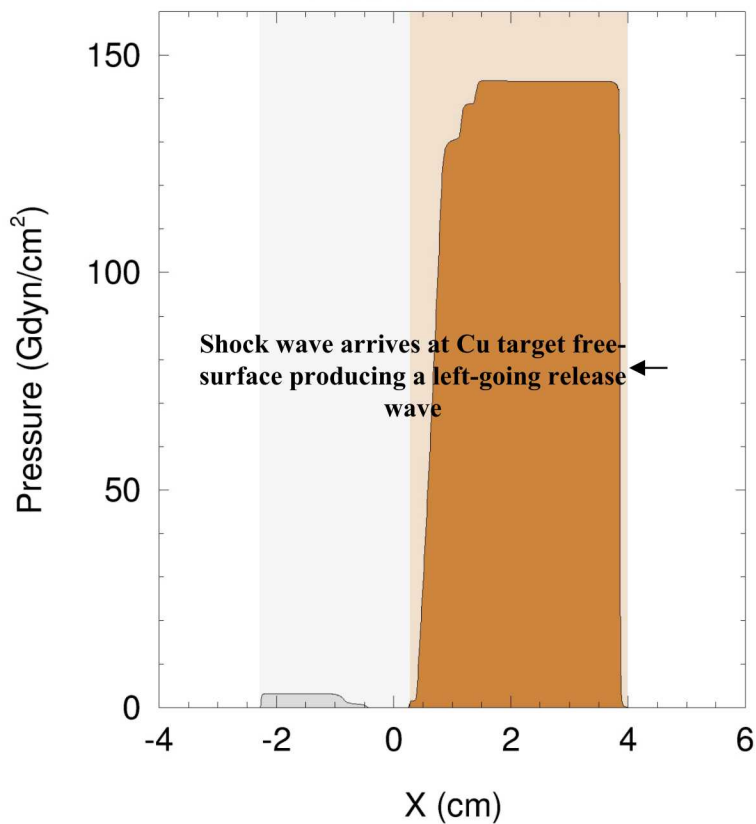


Sandia
National
Laboratories

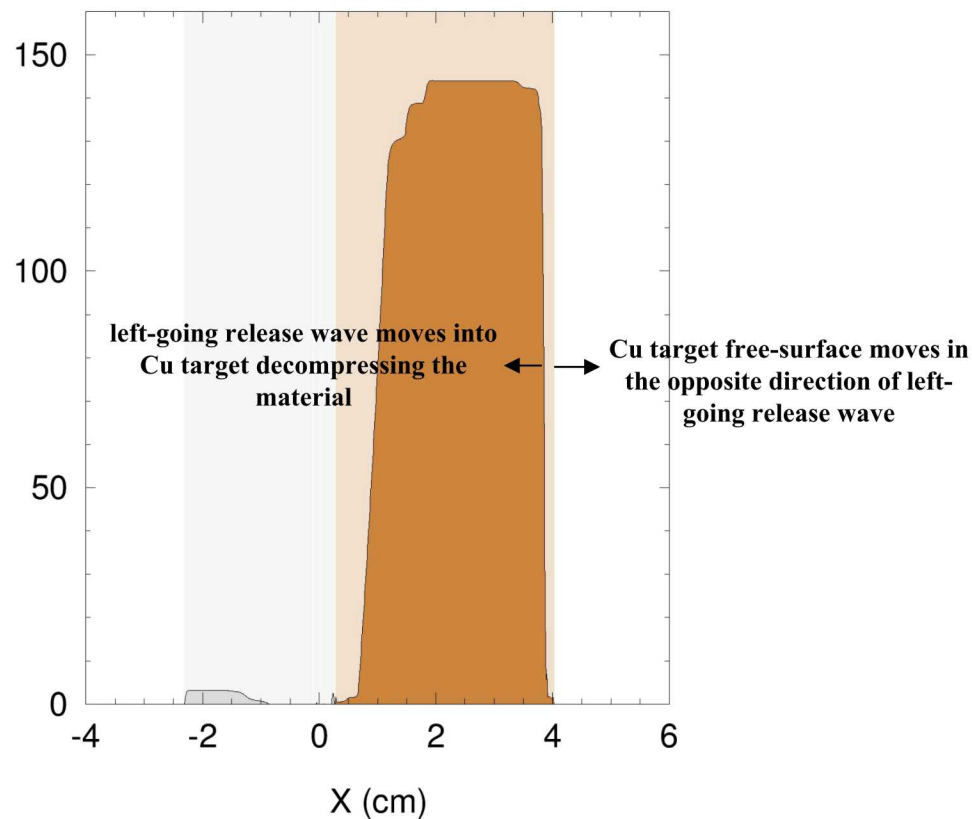


Decompression of the Material

Pressure at 8.60 μ s



Pressure at 9.31 μ s



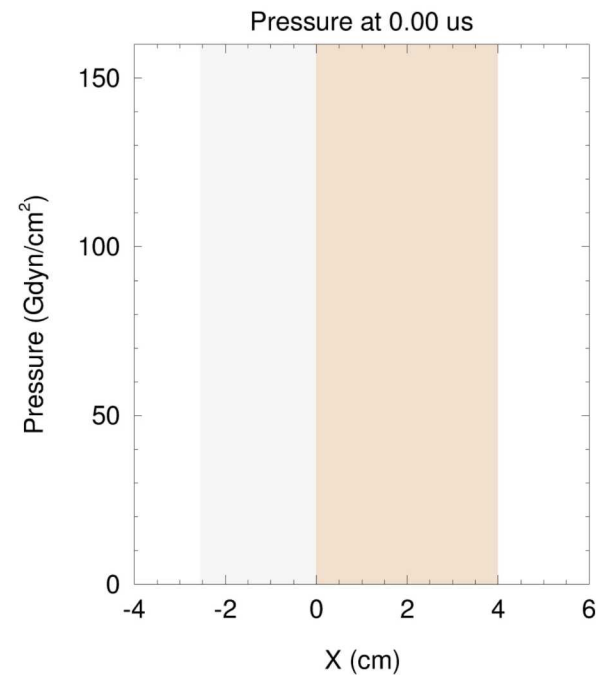
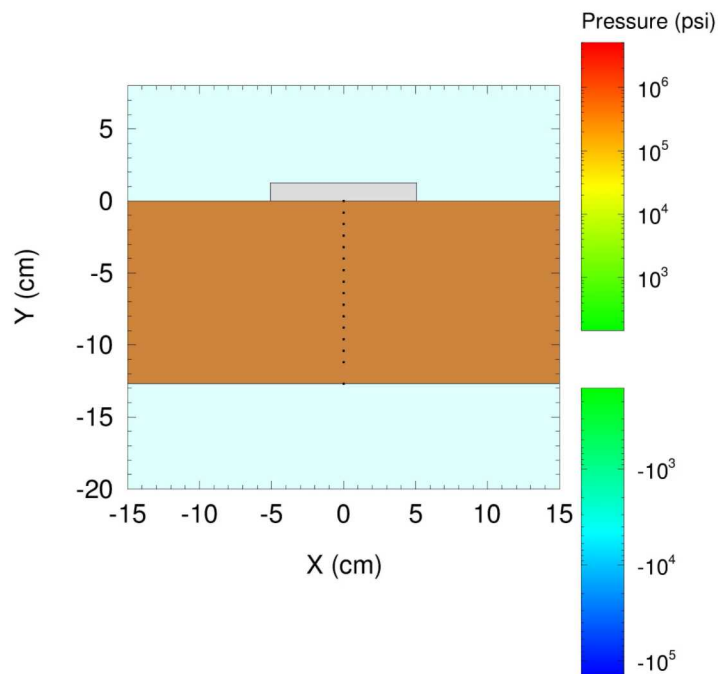


Sandia
National
Laboratories



Al Flyer Impacting Cu Target

Pressure at 0.00 us
Al Flyer impacting Cu Plate



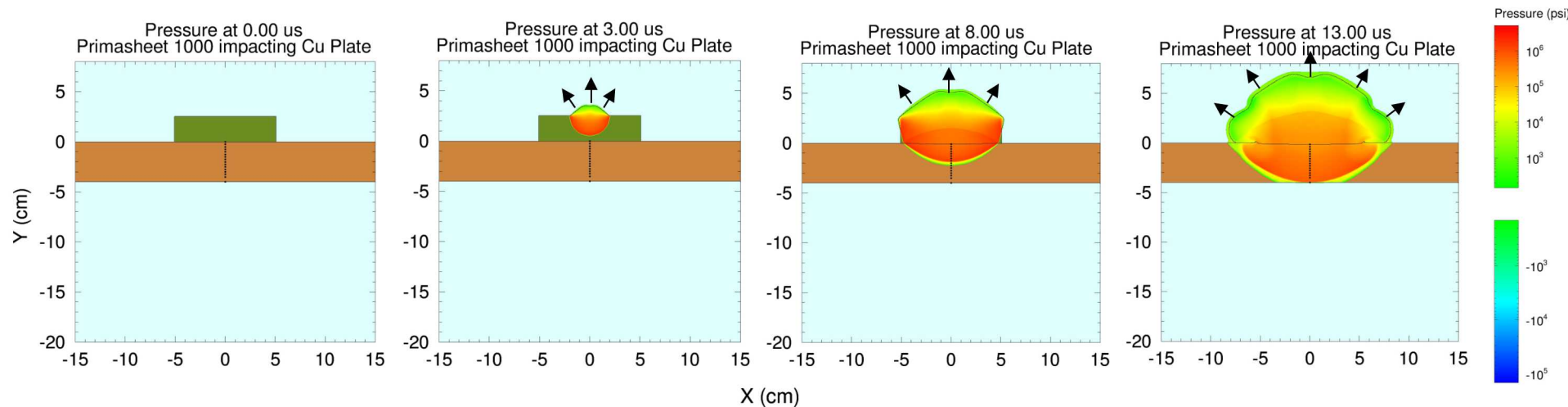


Sandia
National
Laboratories



Creating Shock Waves With Explosives

- Pressure in material is generated from high pressure detonation products
- Pressure decreases as detonation products expand
- The Release/relief/rarefaction wave is dependent on how rapidly the detonation products expand



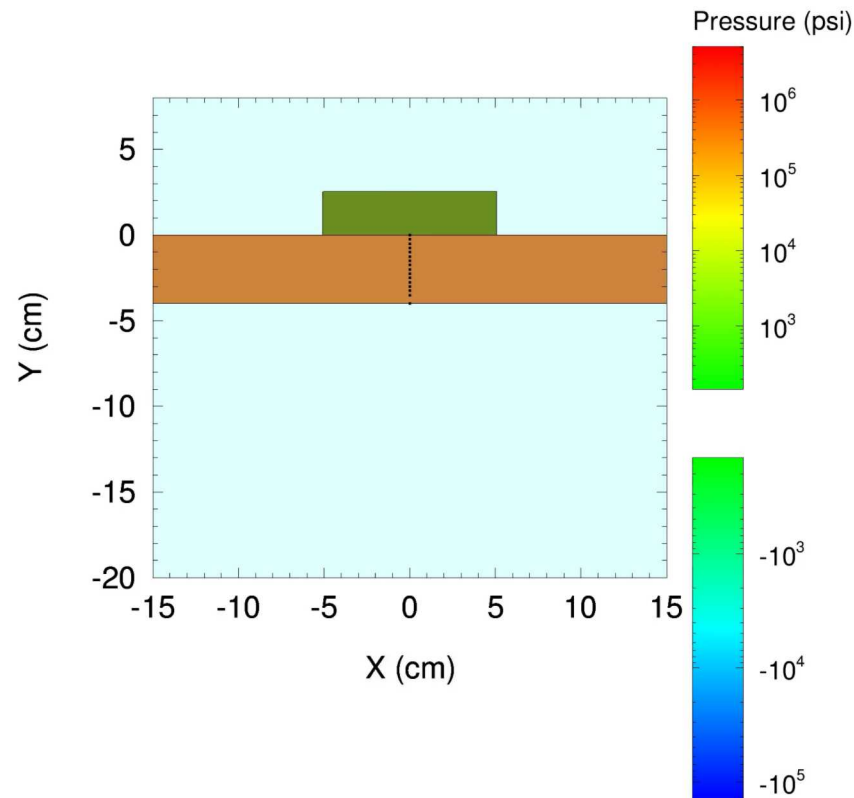


Sandia
National
Laboratories



Creating Shock Waves With Explosives

Pressure at 0.00 μ s
Primasheet 1000 impacting Cu Plate





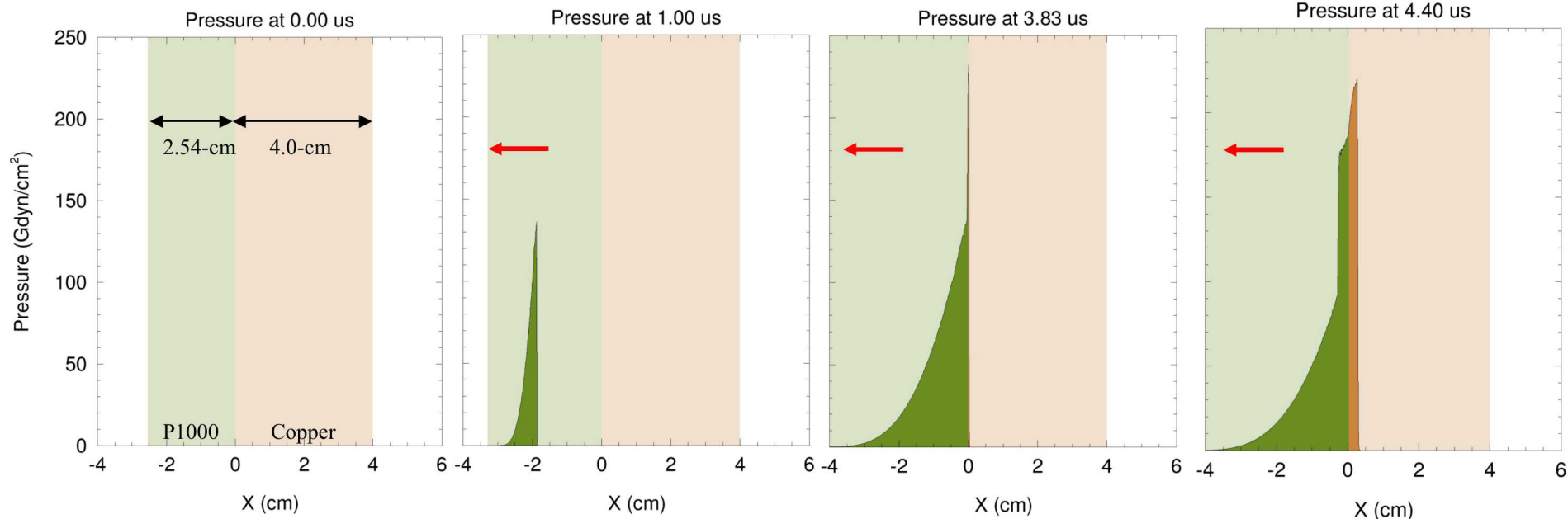
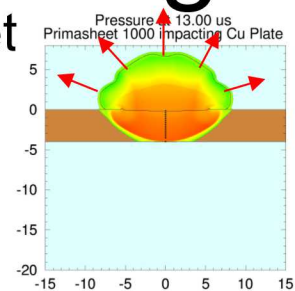
Sandia
National
Laboratories



Characteristics of Explosive Loading

- Primasheet 1000 (P1000) explosively loading Copper target
 - 2.54-cm (1-in) thick P1000
 - 4.0-cm (1.575-in) Cu target

← Detonation products are rapidly expanding radially outward

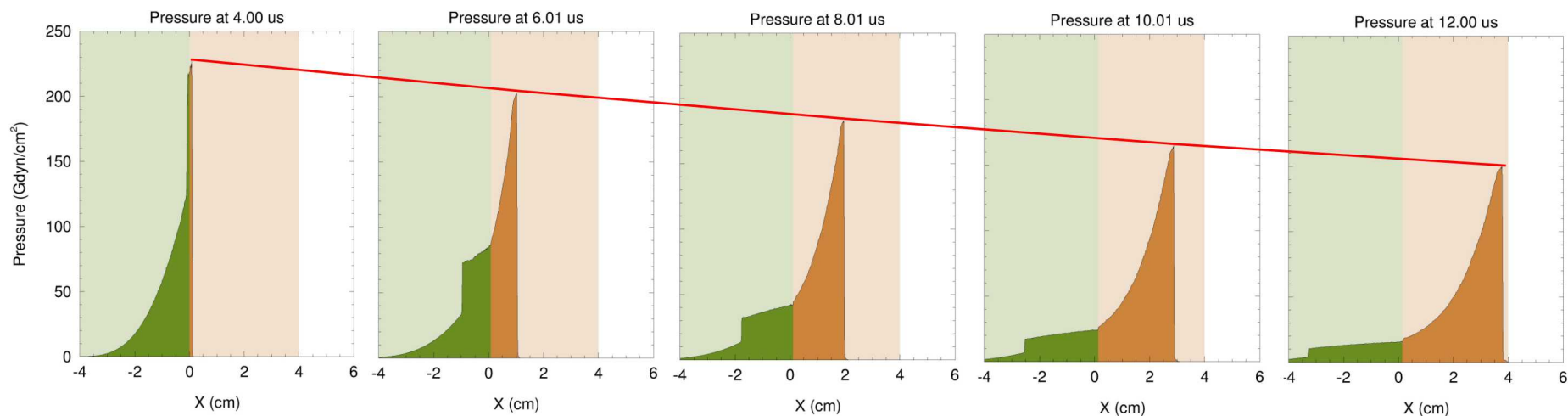




Sandia
National
Laboratories



Shock Wave Attenuation



Detonation products are
expanding rapidly

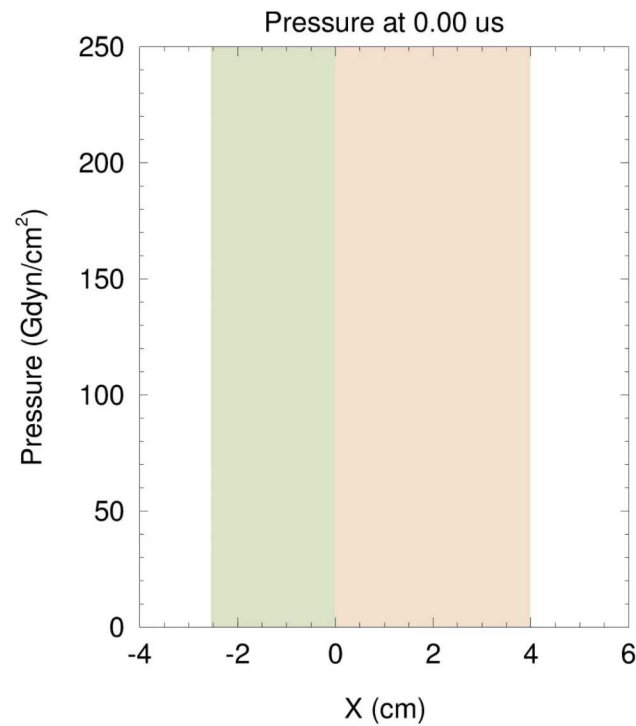
The relief (rarefaction) wave from the explosive/steel interface collides with the relief (rarefaction) wave from the free surface generating a tensile loading that's amplitude produces a spall plane



Sandia
National
Laboratories



Characteristics of Explosive Loading





Sandia
National
Laboratories



Shock Wave Impedance Matching

- Benefits of understanding shock wave impedance matching
 - Determining the peak stress of a material subjected to an impact or explosive load
 - Determine the influence of the peak stress of a shock wave as it propagates through multiple layers (composite systems) of materials in contact with each other
 - Aid in developing tools, applications, and/or techniques that enhance or mitigate a shock wave



Sandia
National
Laboratories



Shock Wave Impedance Matching

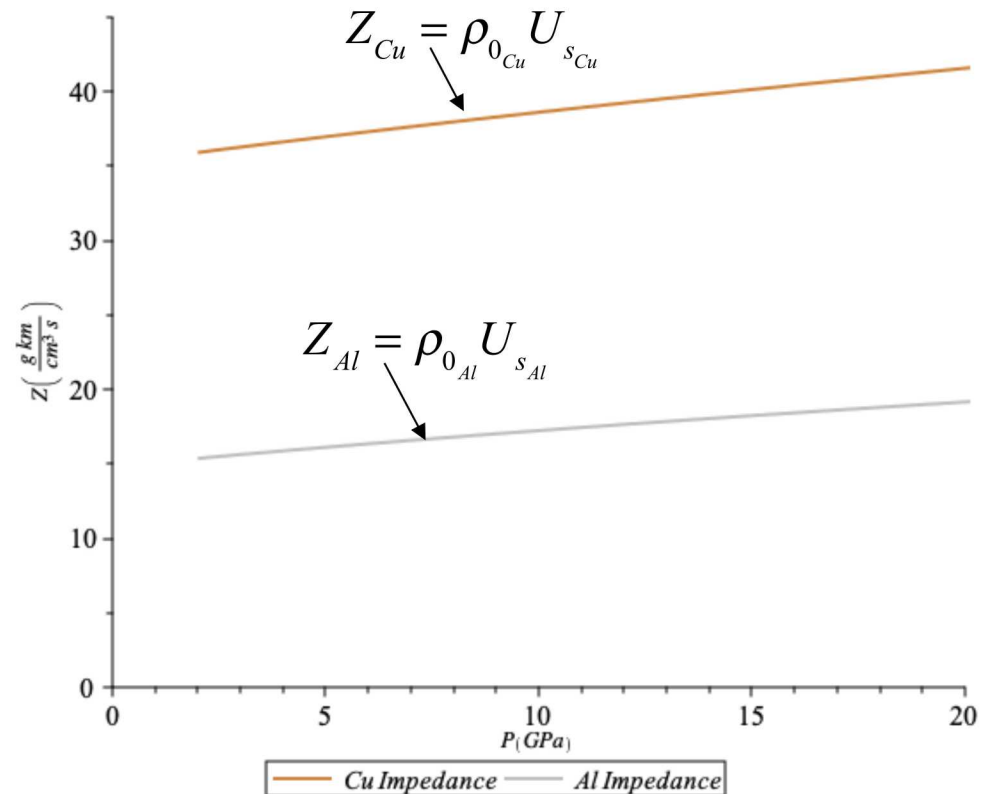
- Impedance matching of interest
 - Impact of two materials
 - Interaction of a shock wave at a boundary
 - Interaction of two shock waves
 - Interaction of two release waves



Shock Wave Impedance Matching

- What is shock wave impedance?
 - A measure of a material to resist compression
 - A measure of a material's ability to generate pressure under a given loading conditions

$$P = \rho_0 U_s u_p = Z u_p, \quad Z = \rho_0 U_s$$



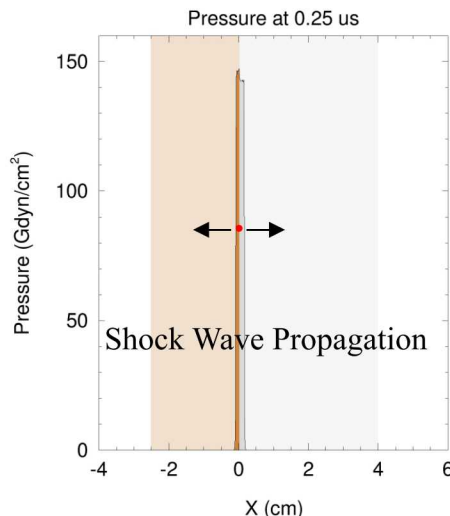
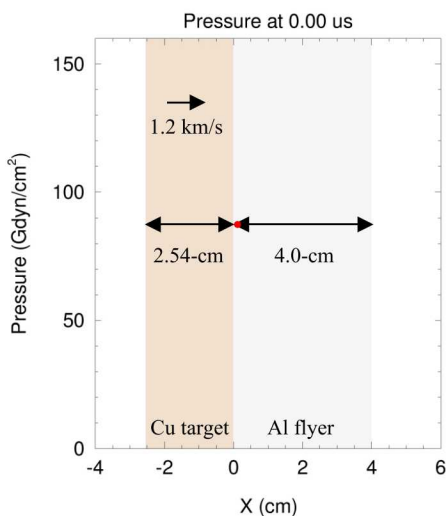


Sandia
National
Laboratories

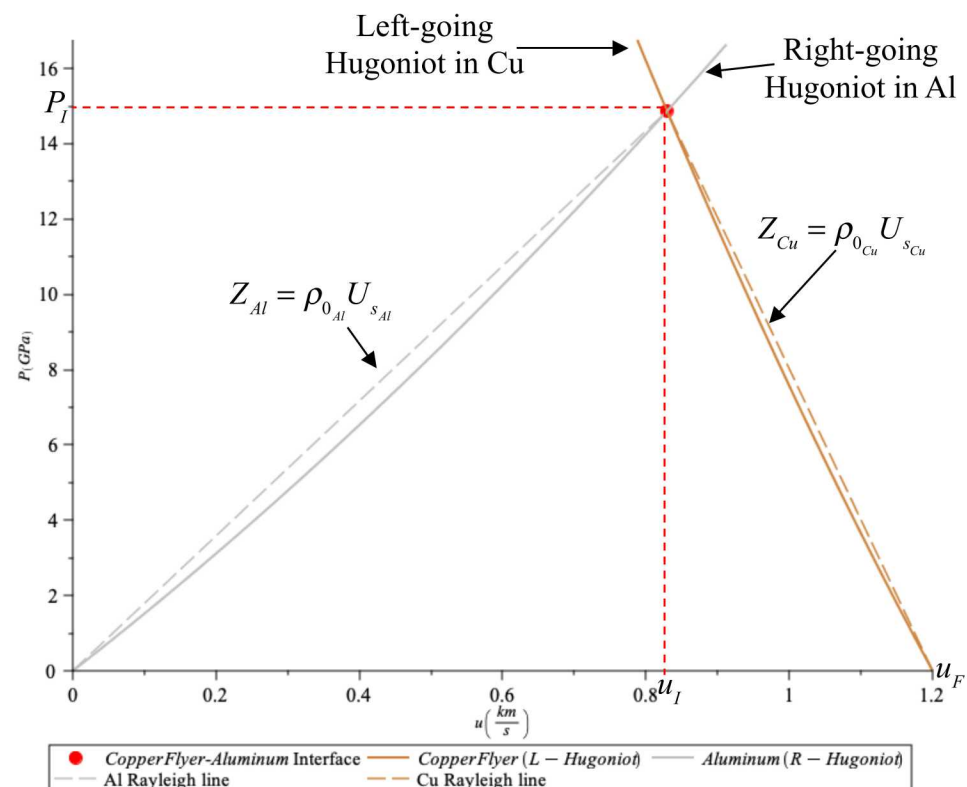


Shock Impedance Matching: Impact

The shock impedance Z_{Al} and Z_{Cu} represent the slope of the Rayleigh line for the $P - u_p$



$$Z_{Cu} > Z_{Al}$$

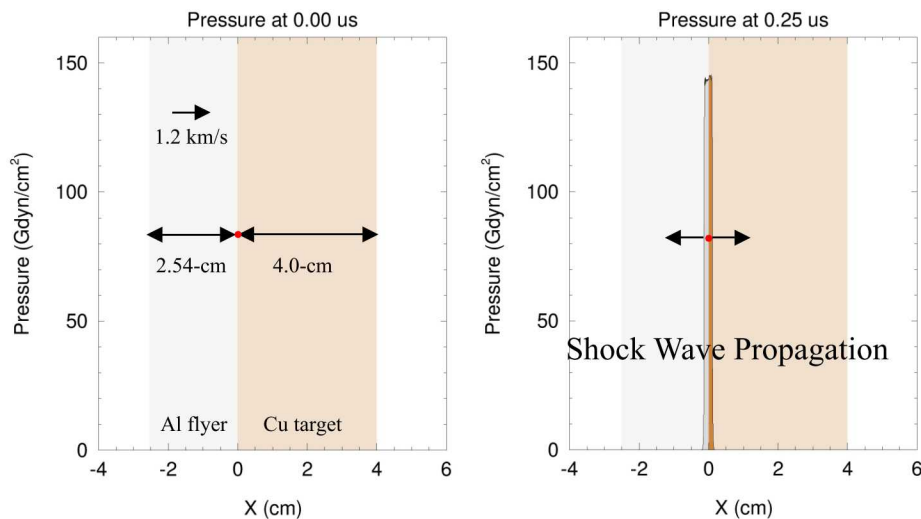




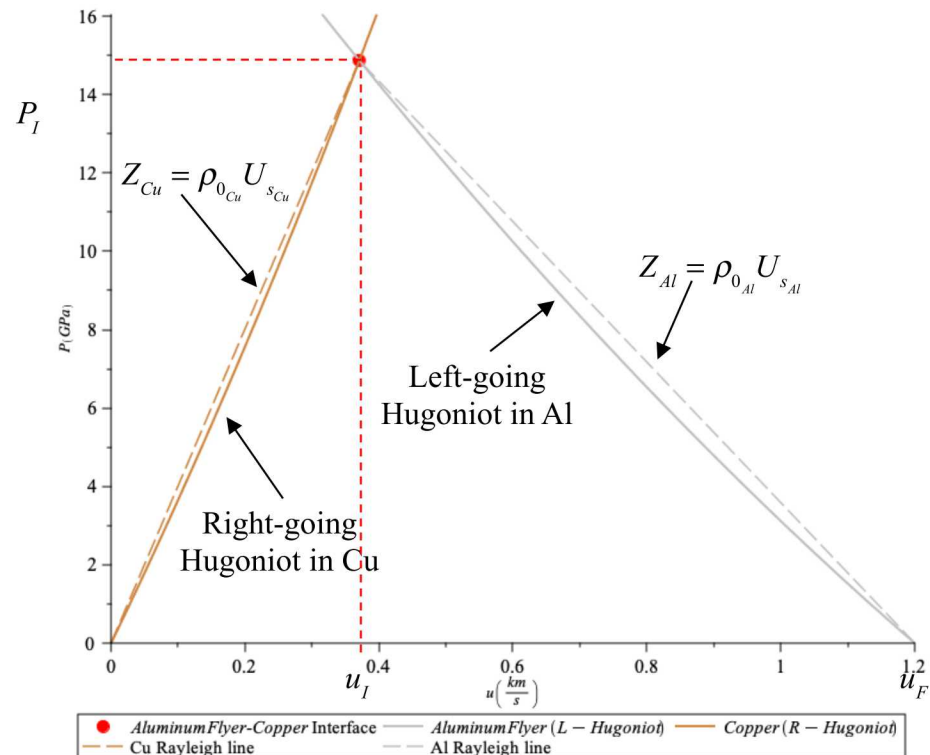
Sandia
National
Laboratories



Shock Impedance Matching: Impact



$$Z_{Al} < Z_{Cu}$$



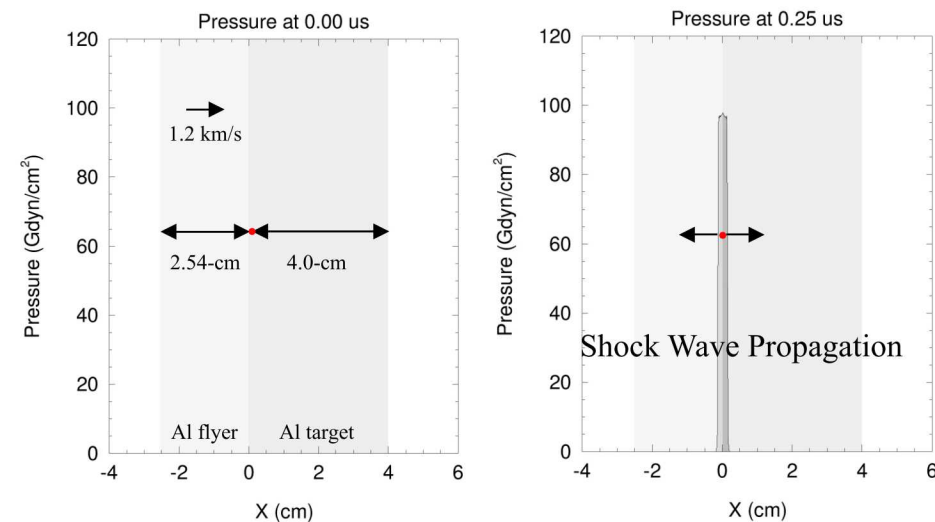


Sandia
National
Laboratories

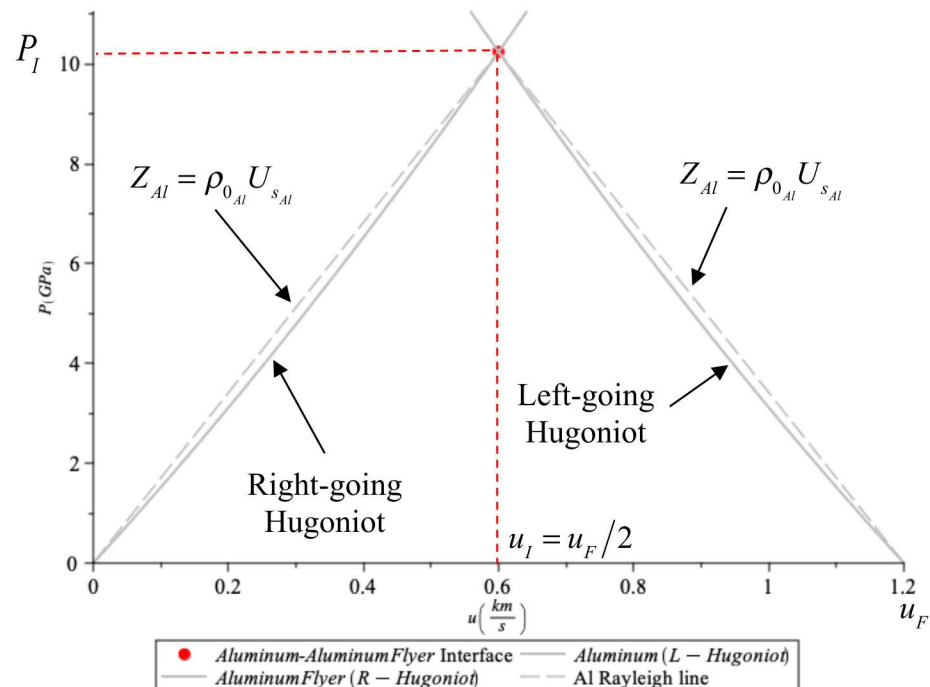


Shock Impedance Matching: Impact

Symmetric impact



$$Z_{Al} = Z_{Al}$$

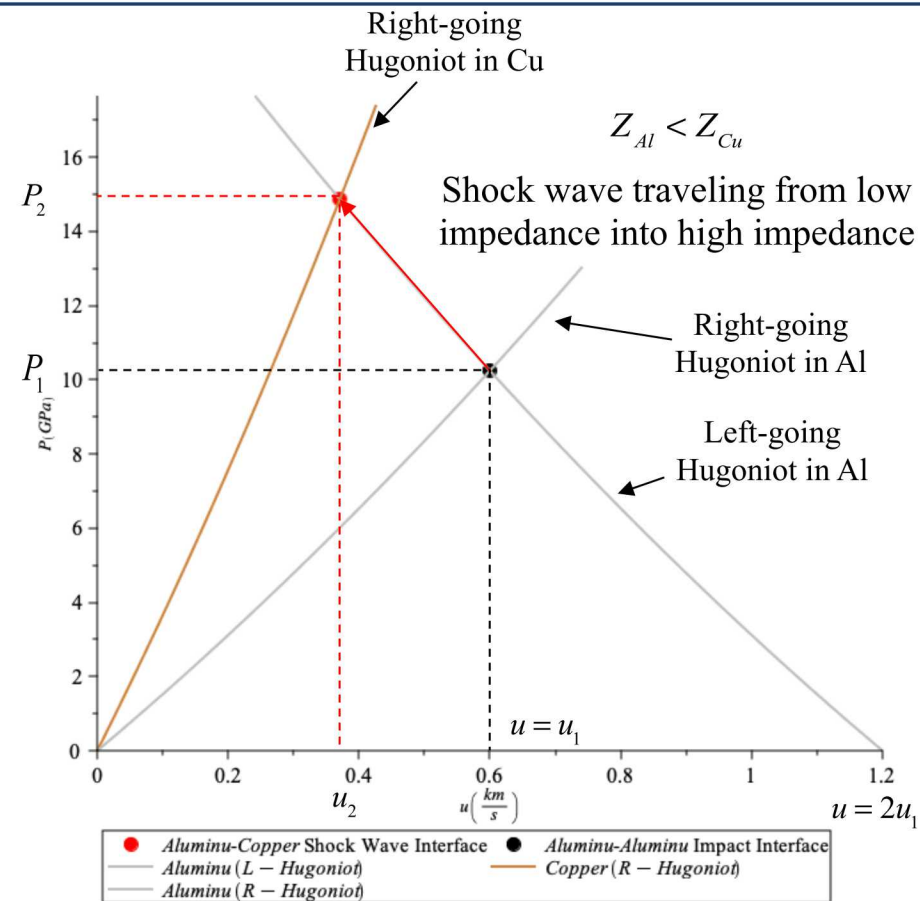
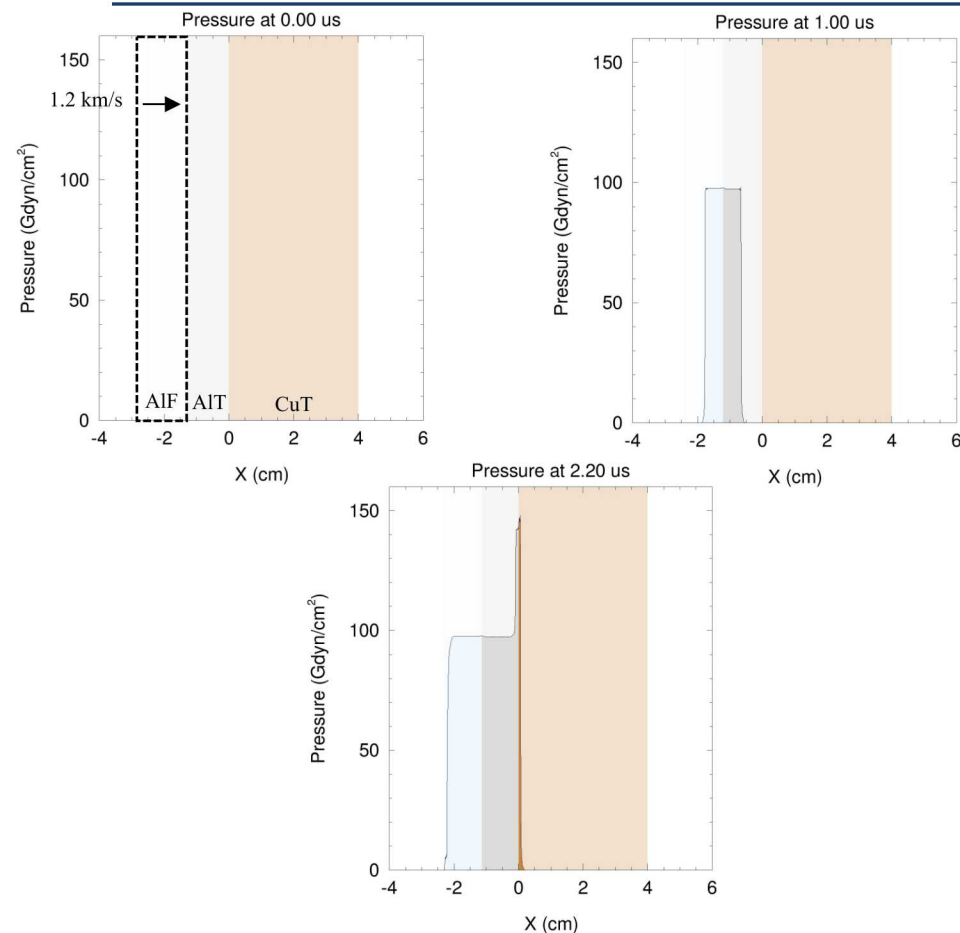




Sandia
National
Laboratories



Shock Waves at an Interface



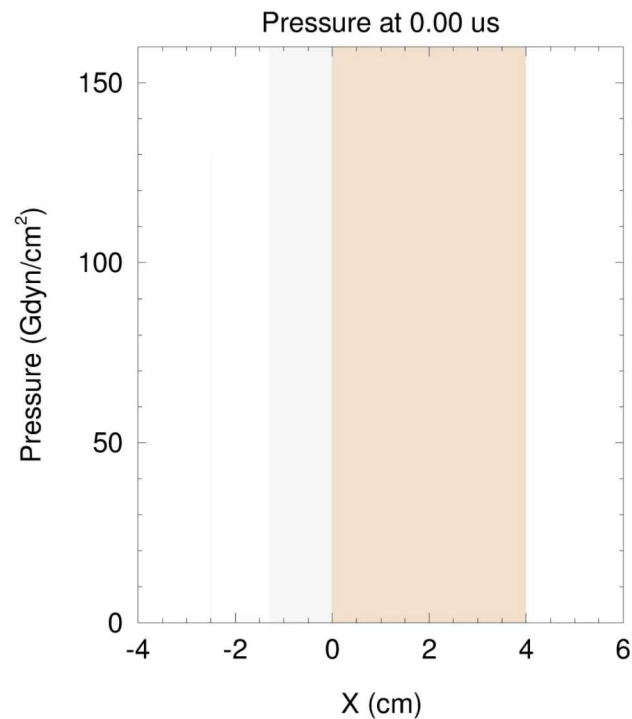
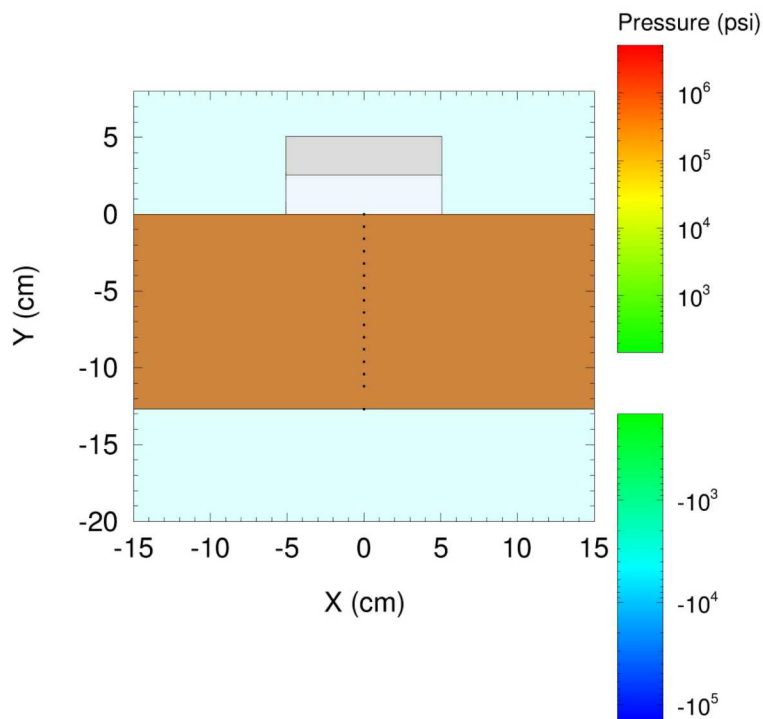


Sandia
National
Laboratories



Shock Waves at an Interface

Pressure at 0.00 us
Al Flyer impacting Al Disc Shock into Cu Plate

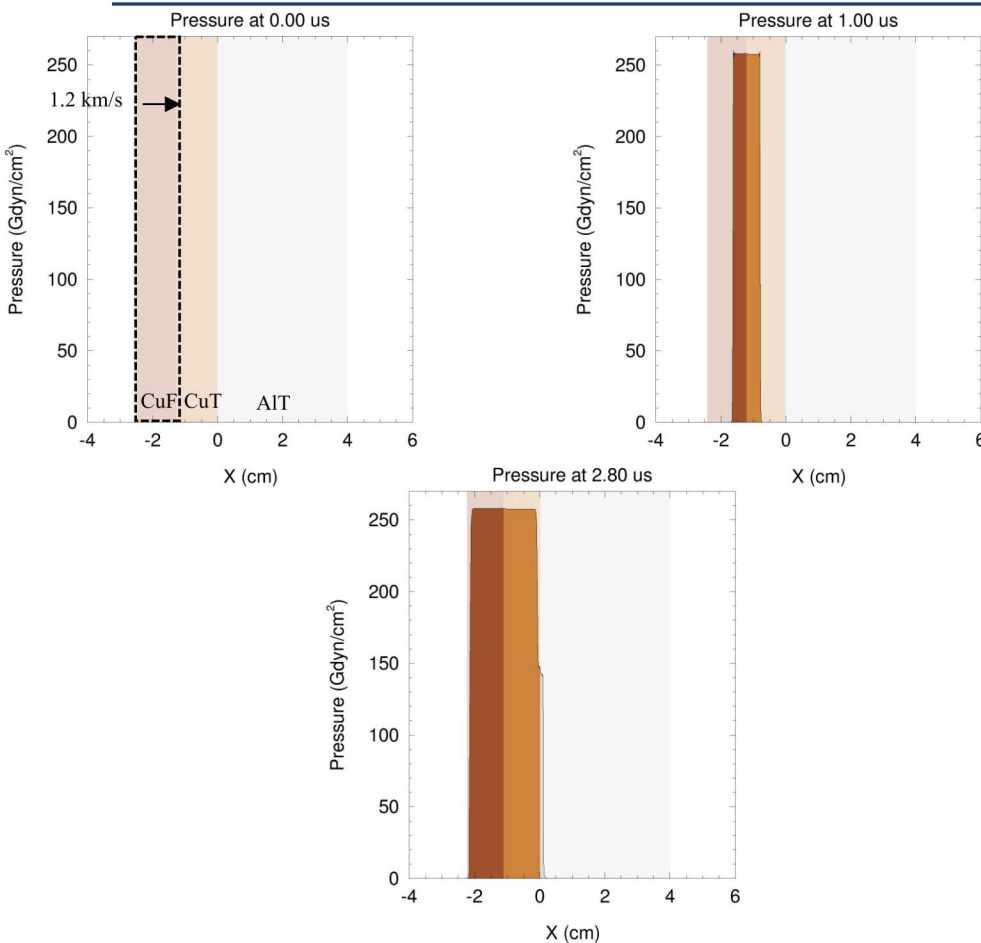




Sandia
National
Laboratories

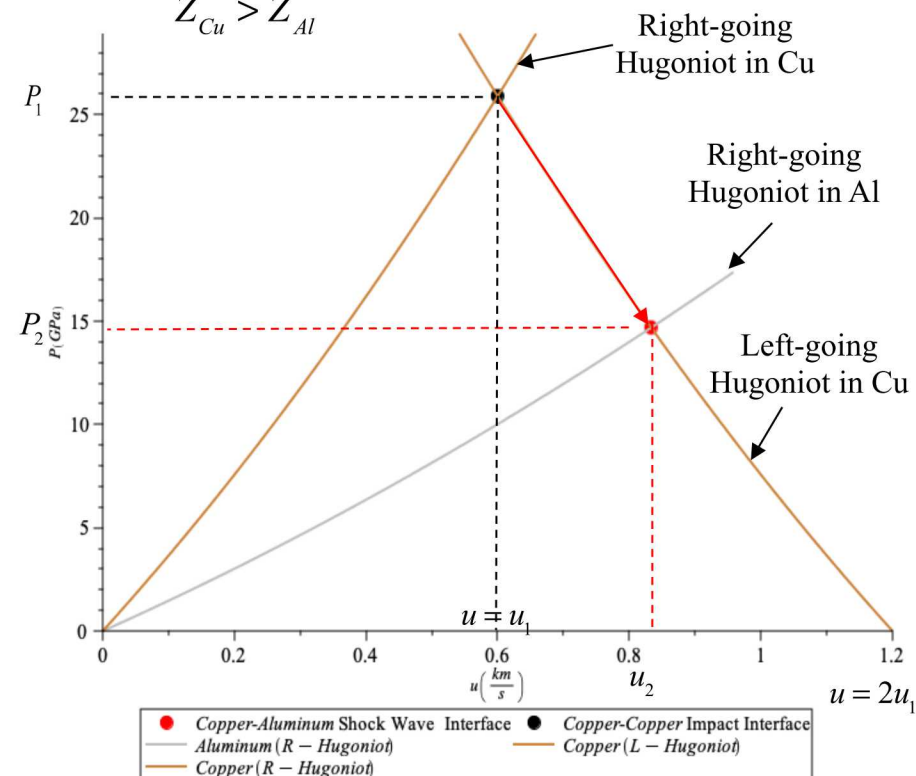


Shock Waves at an Interface



Shock wave traveling from high impedance into low impedance

$$Z_{Cu} > Z_{Al}$$



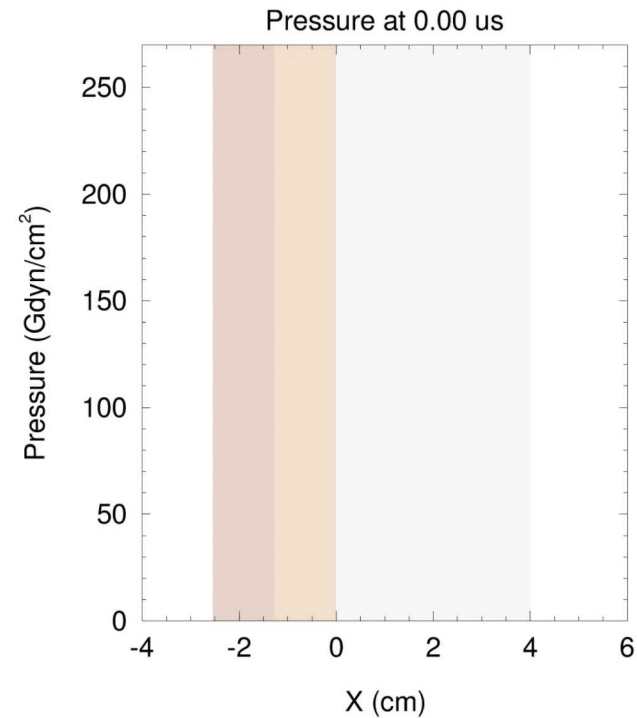
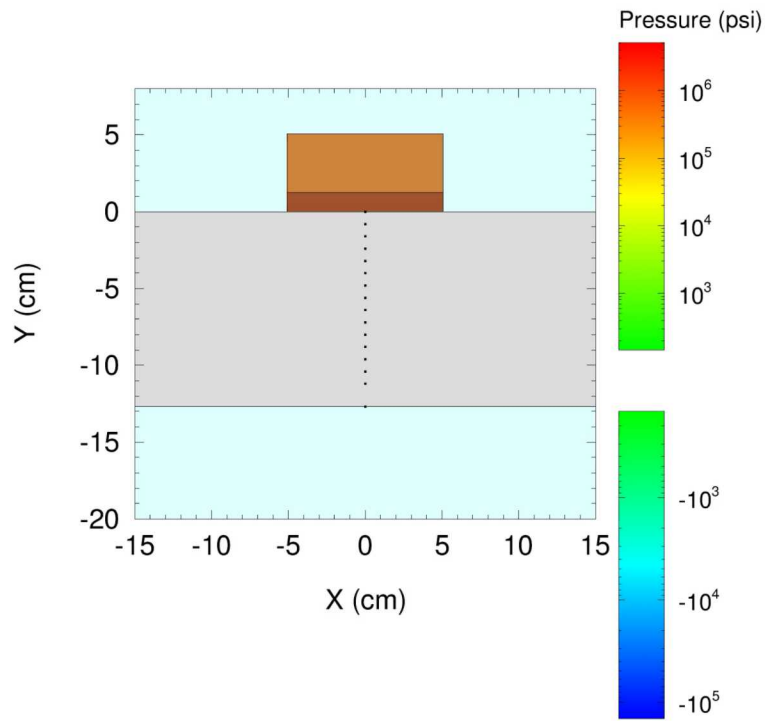


Sandia
National
Laboratories



Shock Waves at an Interface

Pressure at 0.00 us
Cu Flyer impacting Cu Disc Shock into Al Plate

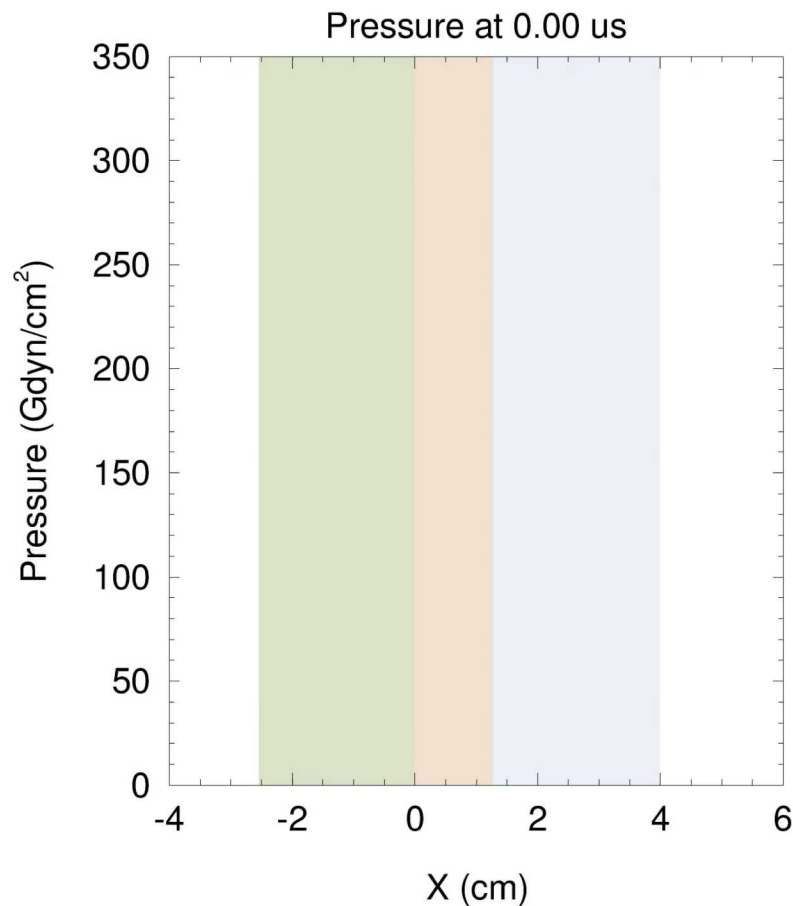




Sandia
National
Laboratories

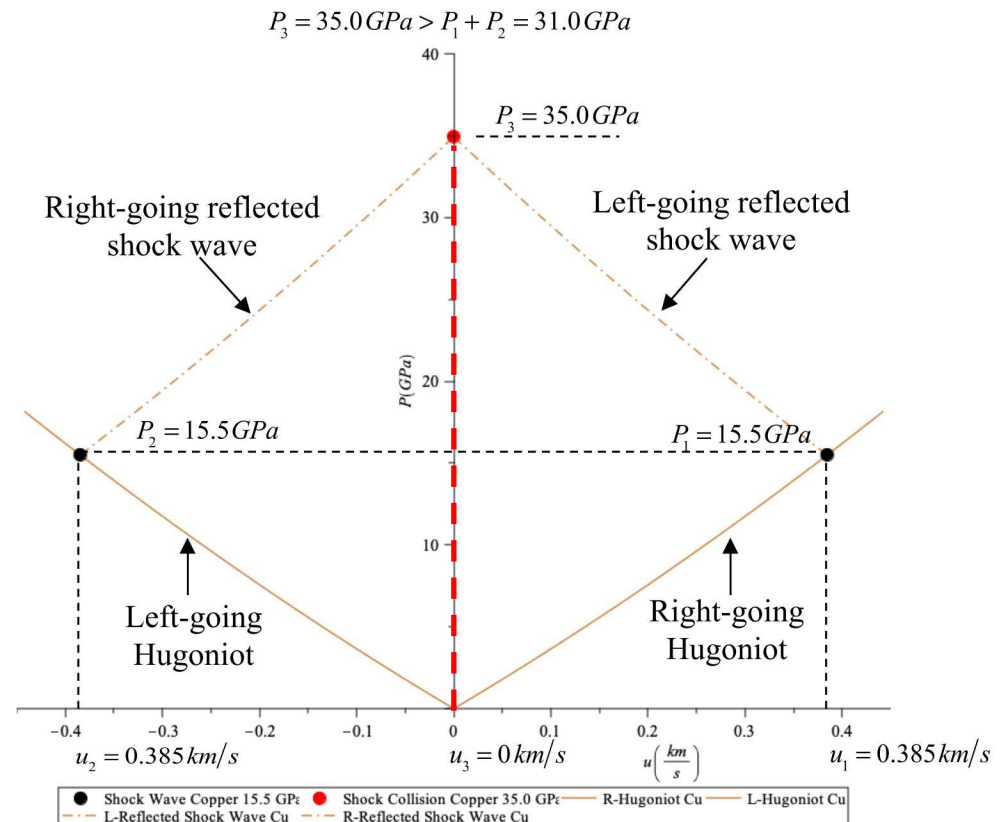
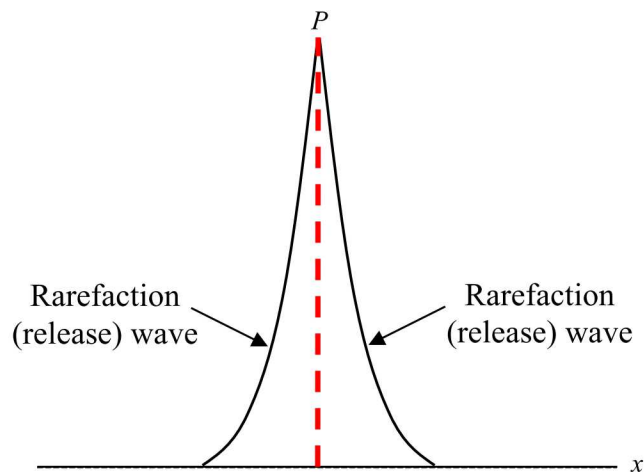
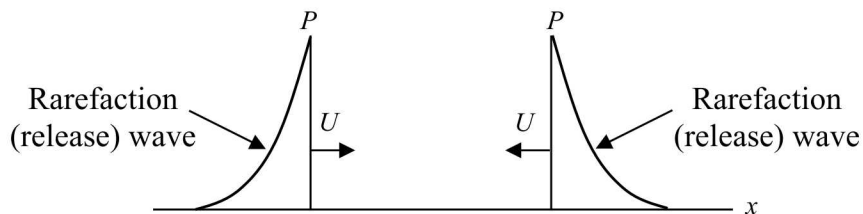


Shock Waves at an Interface





Collision of Shock Waves

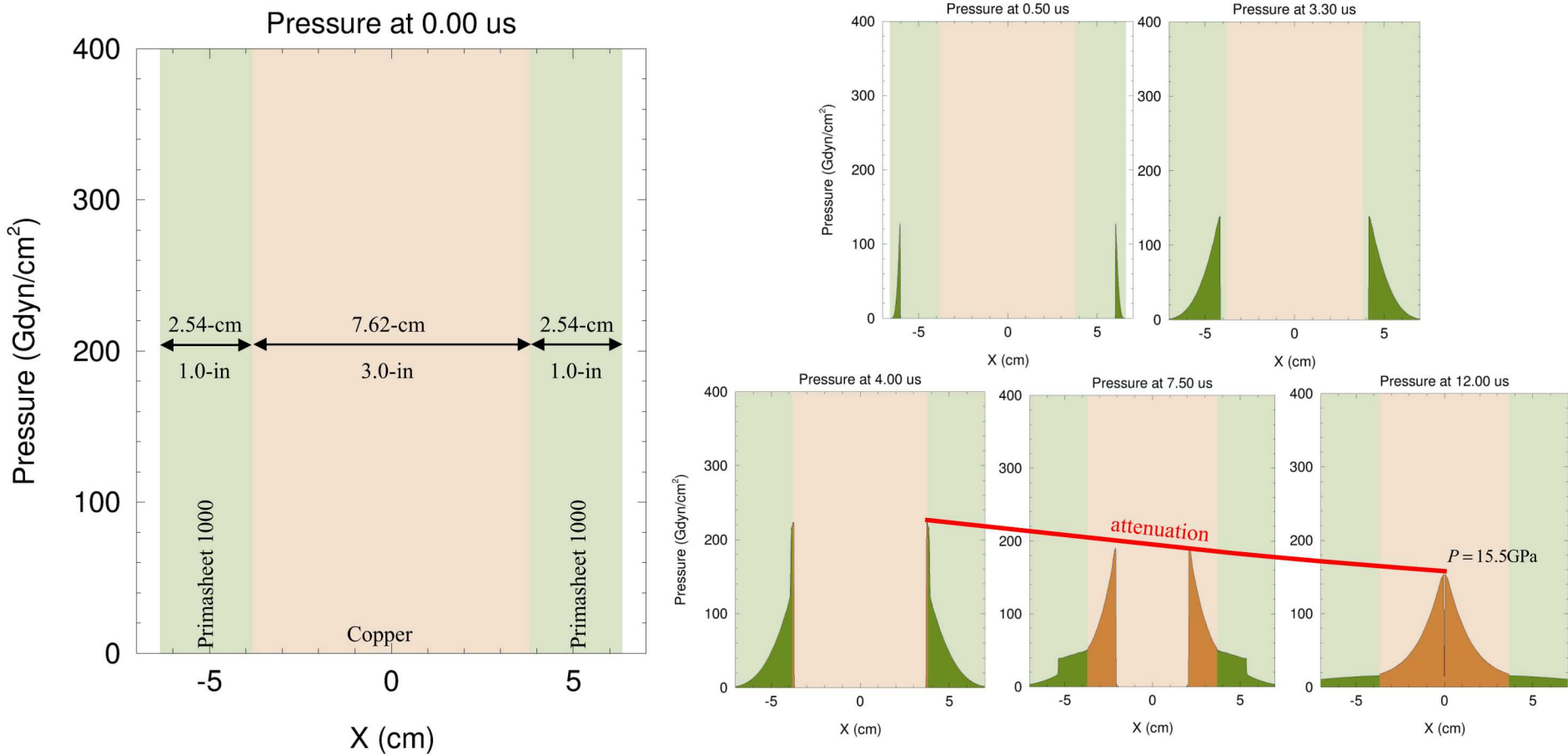




Sandia
National
Laboratories



Collision of Shock Waves

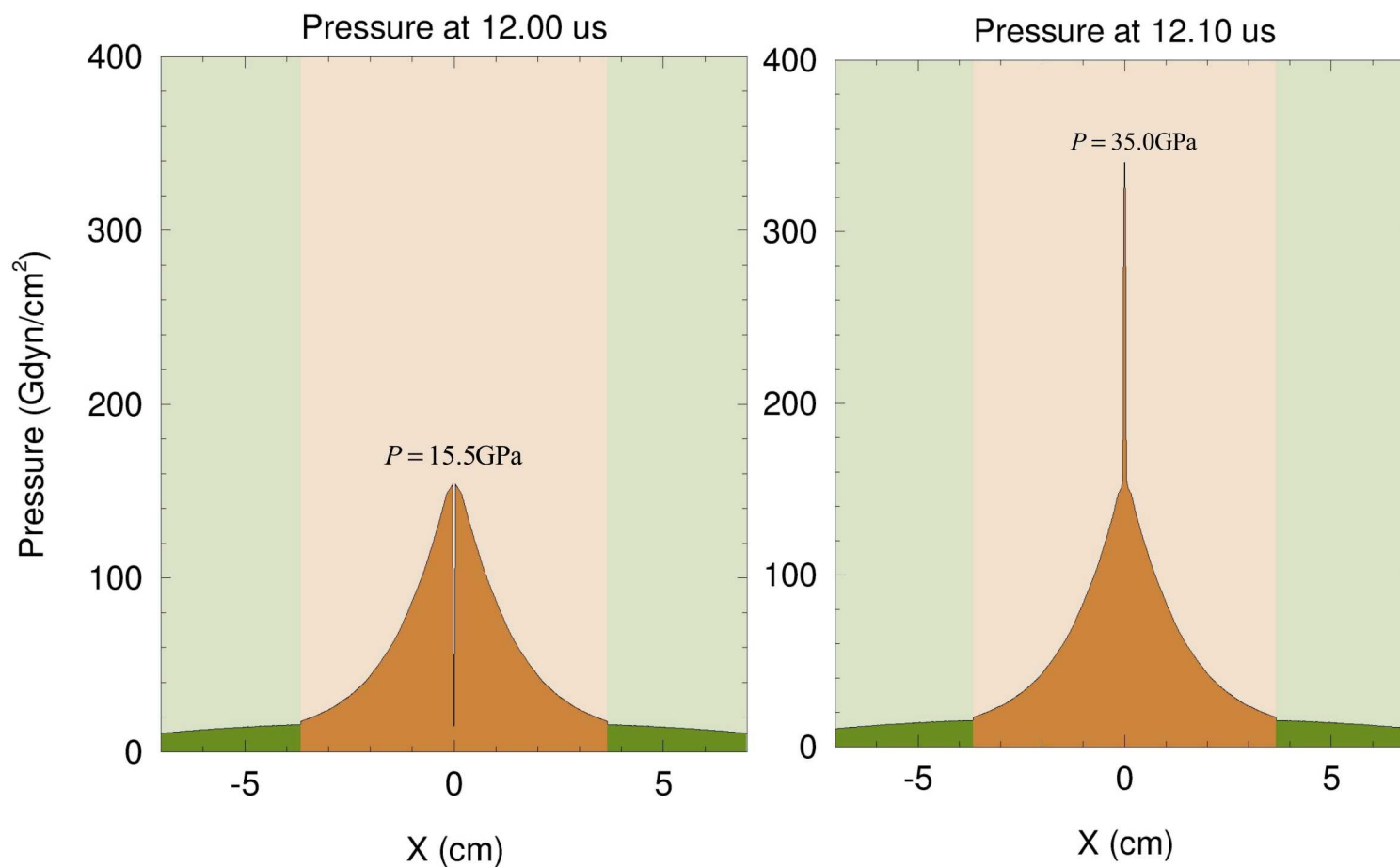




Sandia
National
Laboratories



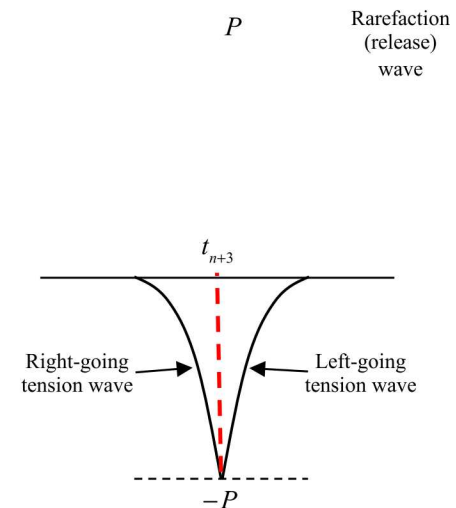
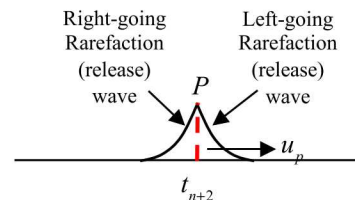
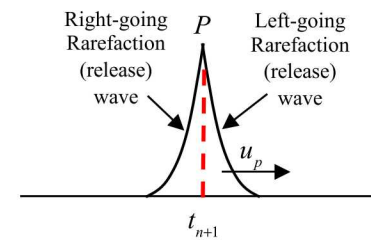
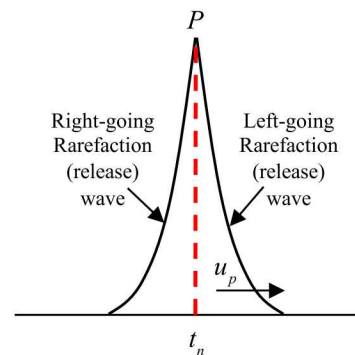
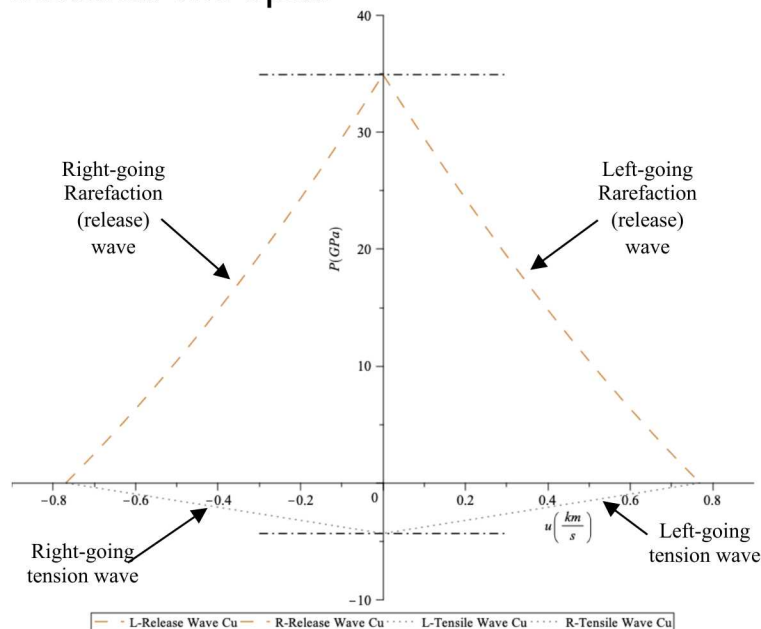
Collision of Shock Waves





Collision of Rarefaction Waves

- Material mass velocity, u_p , is decelerating and starting to have velocity in the opposite direction. It is decompressing
- If the tensile pressure is large enough the material will spall

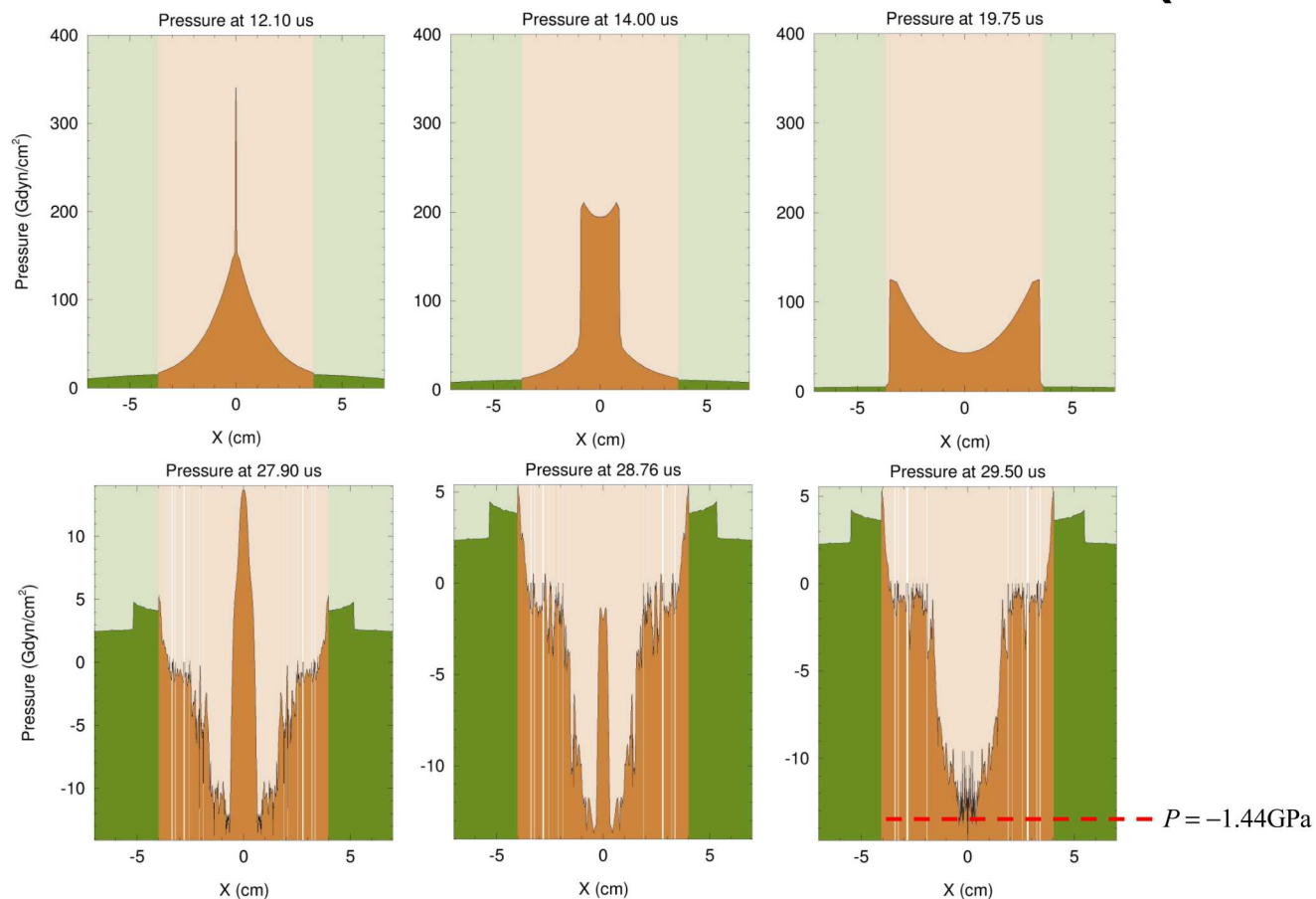




Sandia
National
Laboratories



Collision of Rarefaction Wave (cont)

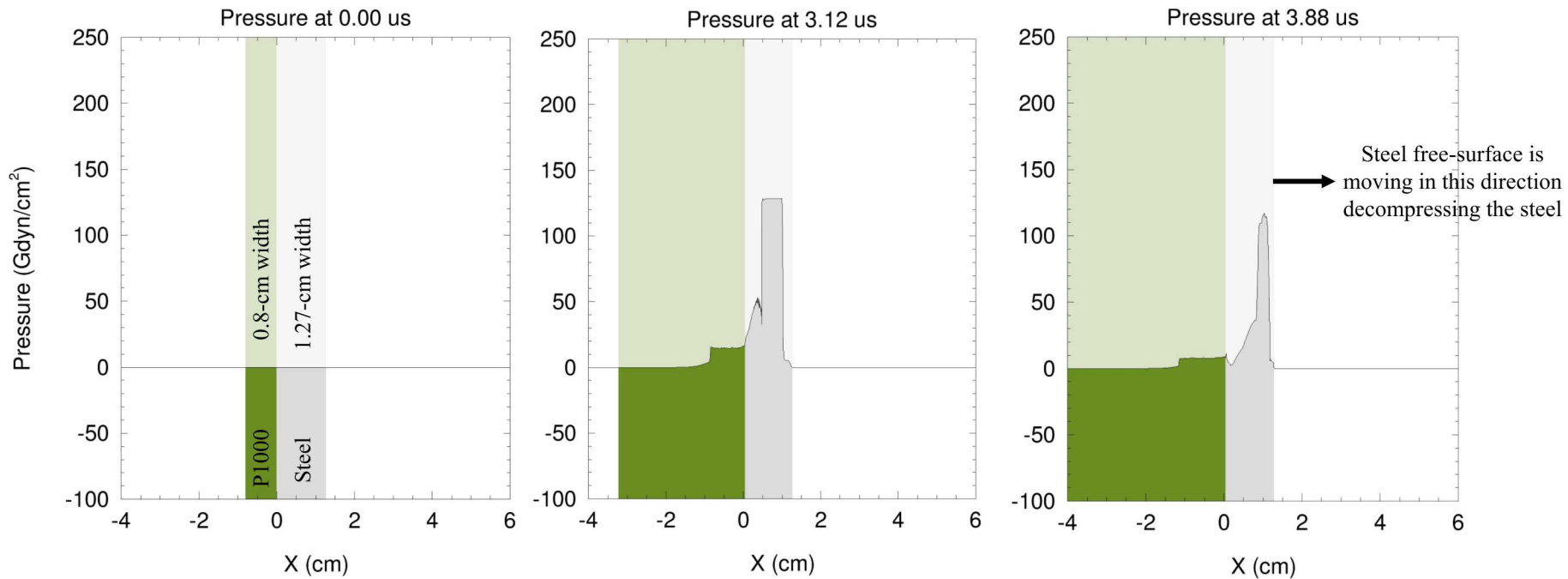




Sandia
National
Laboratories



Spall Planes (cont)

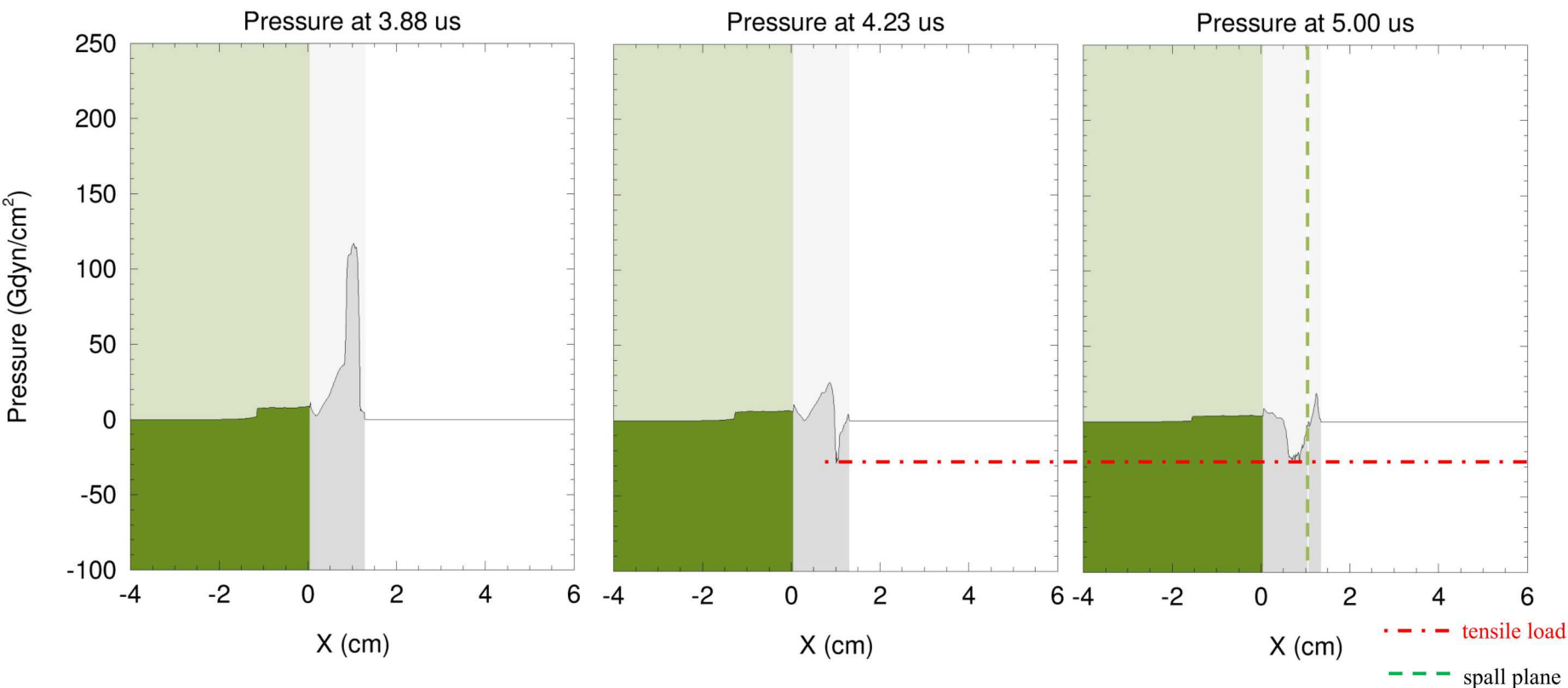




Sandia
National
Laboratories



Spall Planes (cont)



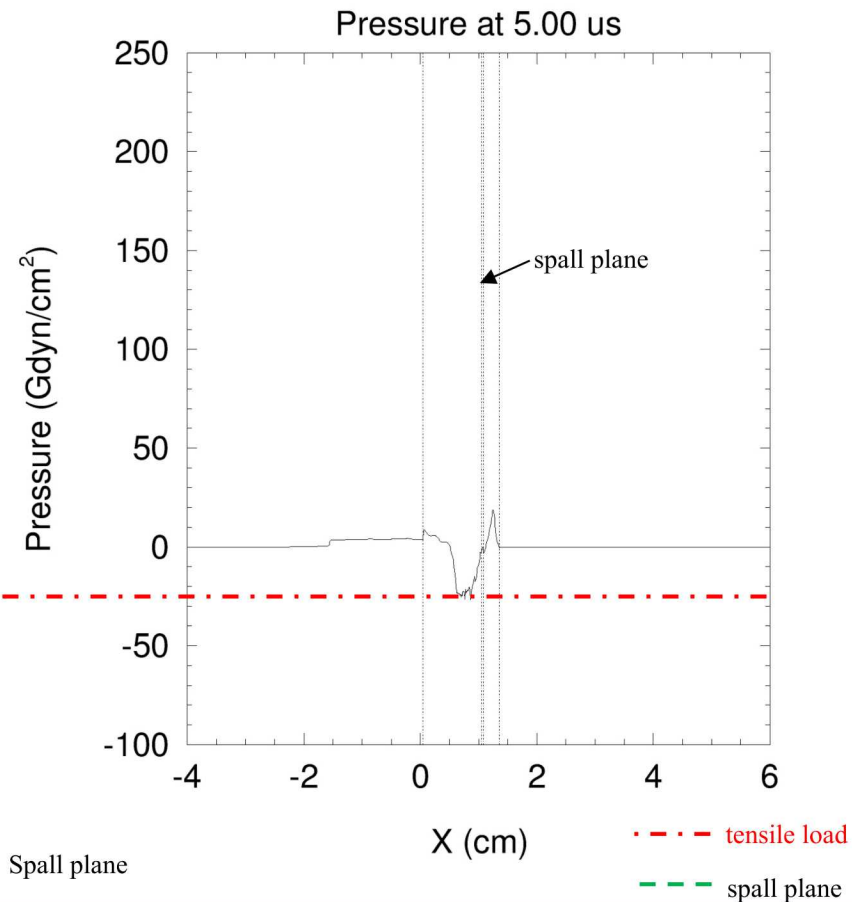
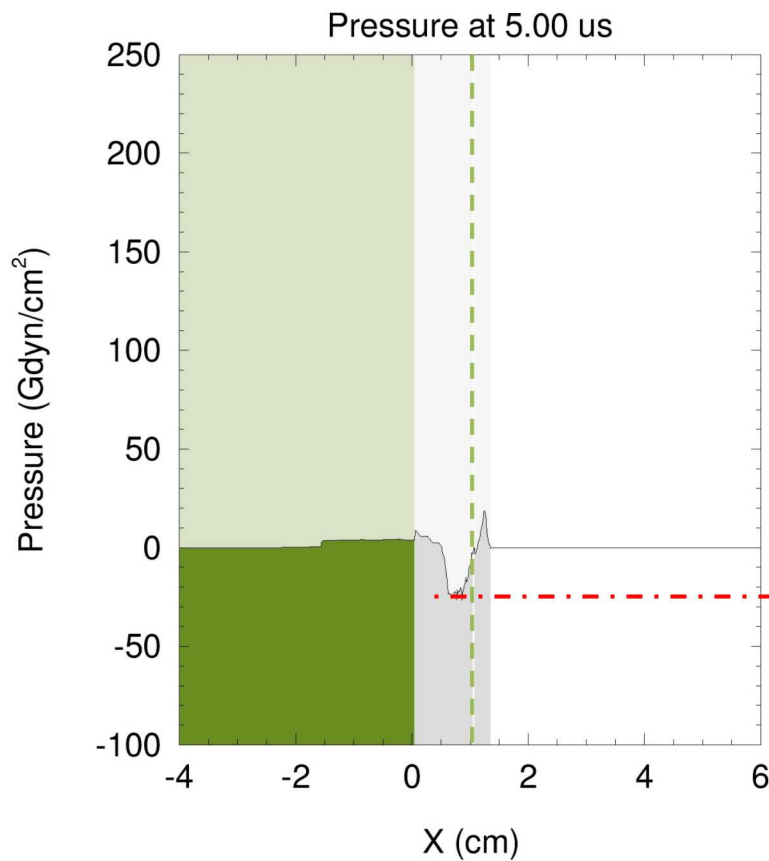
The relief (rarefaction) wave from the explosive/steel interface collides with the relief (rarefaction) wave from the free surface generating a tensile loading that's amplitude is large enough to produce a spall plane



Sandia
National
Laboratories



Spall Planes (cont)





Sandia
National
Laboratories



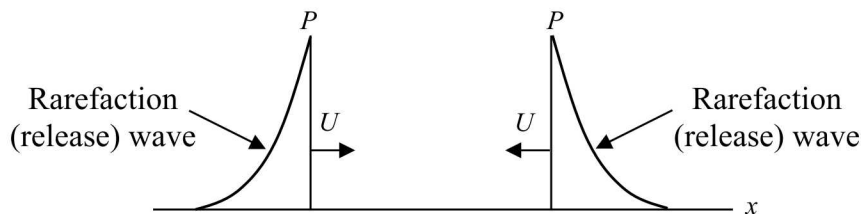
Questions?



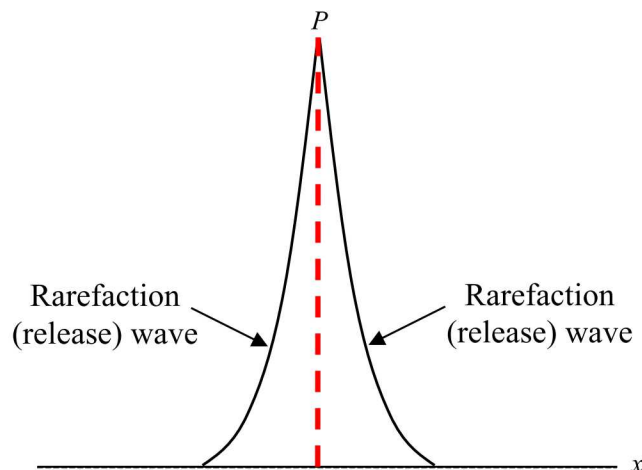
Sandia
National
Laboratories



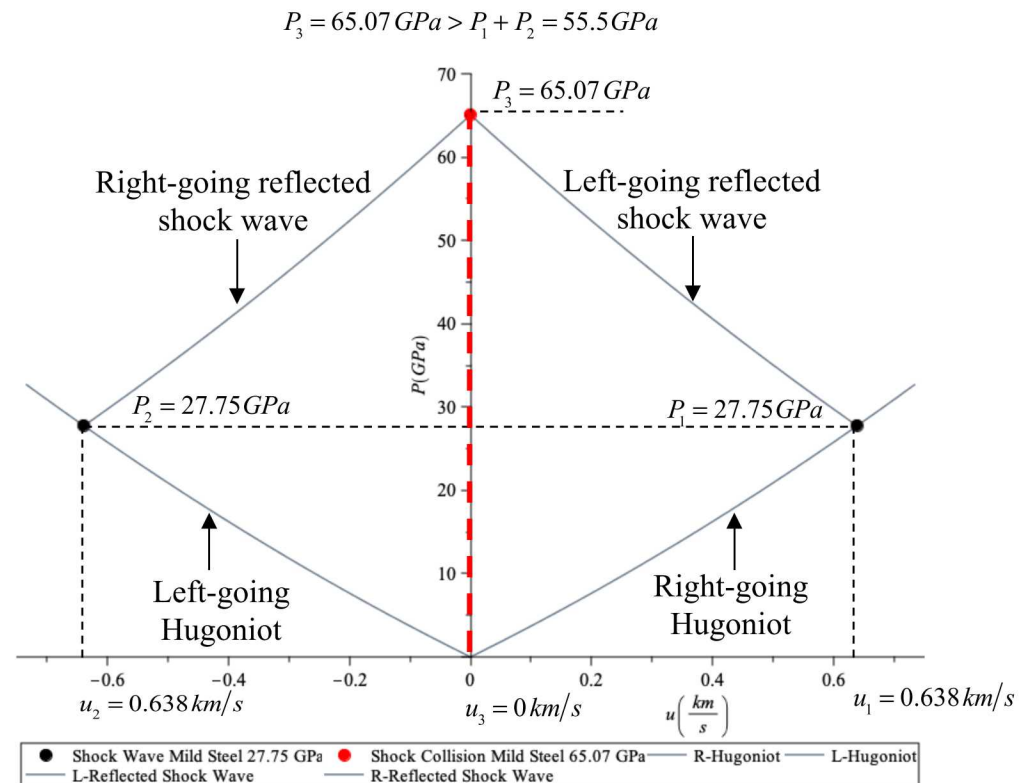
Collision of Shock Waves



two shock waves (same pressure amplitude)
propagating toward each other in mild steel



two shock waves (same pressure amplitude)
collide in mild steel

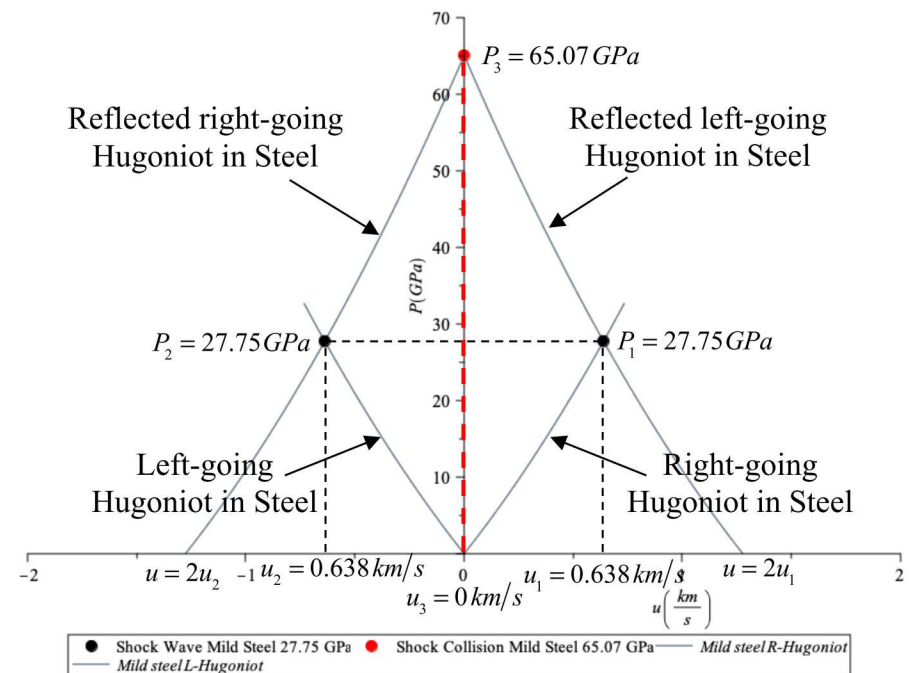
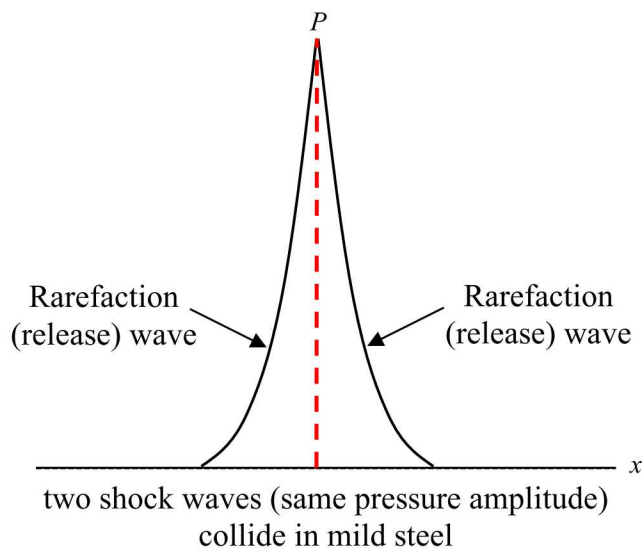
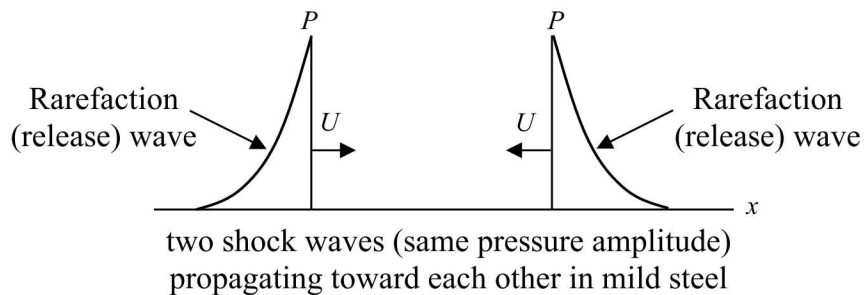




Sandia
National
Laboratories



Collision of Shock Waves



$$P_3 = 65.07 \text{ GPa} > P_1 + P_2 = 55.5 \text{ GPa}$$