

# Sandia National Laboratories Extracting an Empirical Intermetallic Hydride Design Principle from Limited Data via Interpretable Machine Learning



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## Introduction

An open question in the metal hydride community is whether there are simple, physics-based design rules that dictate the thermodynamic properties of these materials across the variety of structures and chemistry they can exhibit. While black box machine learning (ML)-based algorithms can predict these properties with some success, they do not directly provide the basis on which these predictions are made, therefore complicating the a priori design of novel materials exhibiting a desired property value. In this work we demonstrate how feature importance, as identified by a gradient boosting tree regressor, uncovers the strong dependence of the metal hydride equilibrium H<sub>2</sub> pressure on a volume-based descriptor that can be computed from just the elemental composition of the intermetallic alloy. Elucidation of this simple structure-property relationship is valid across a range of compositions, metal substitutions, and structural classes exhibited by intermetallic hydrides. This permits rational targeting of novel intermetallics for high-pressure hydrogen storage (low-stability hydrides) by their descriptor values, and we predict a known intermetallic to form a low-stability hydride (as confirmed by density functional theory calculations) that has not yet been experimentally investigated [1].

## Data cleaning

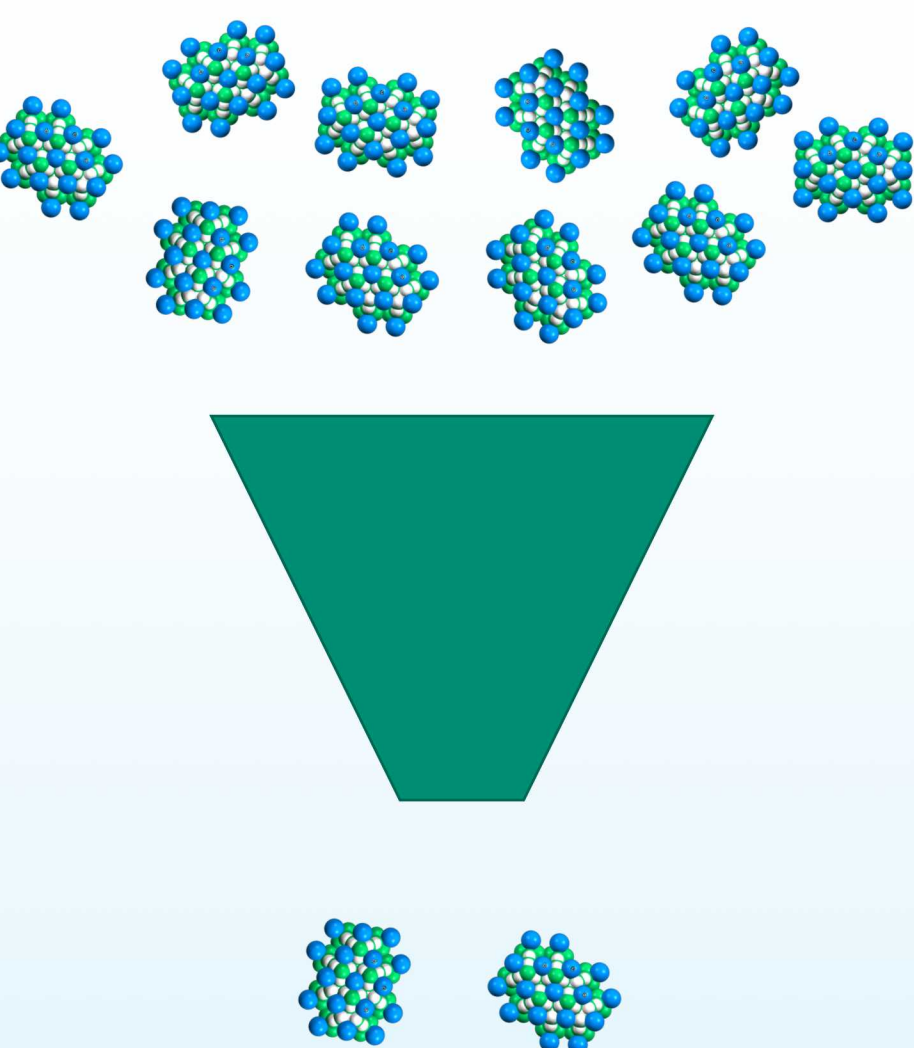
**HydPARK** is Sandia's historical dataset on metal hydride properties:

Class	Composition	H wt %	$\Delta H$ (kJ/mol H <sub>2</sub> )	$T$ (K)	$P_{eq}$ (atm)
A <sub>2</sub> B	Ce <sub>0.5</sub> Th <sub>1.5</sub> Al <sub>1</sub>	0.4	133	650	0.0003
AB <sub>5</sub>	La <sub>0.75</sub> Ce <sub>0.25</sub> Ti <sub>0.1</sub> Cu <sub>0.9</sub> Ni <sub>4</sub>	1.4	38.4	22	1.1

**Target property:** Compute equilibrium pressure at room temperature,

$$\ln P_{eq}^o = -\Delta H/RT^o + \Delta S/R$$

to gauge a material's thermodynamic utility in a given storage application



**Initial:** ~ 2500 HydPARK compositions

1. Remove duplicate compositions
2. Remove entries with missing data, i.e.  $\ln P_{eq}^o$  can't be computed

**Final:** ~ 400 "ML ready" compositions

## ML Model Development

**1. Magpie** presents a useful way to featurize inorganic materials in terms of elemental properties when exact crystal structures are not known [2]

$$\mathbf{x}_{\text{LaNi}_5} = [\bar{v}_{pa}^{\text{Magpie}}, \bar{T}_{\text{melt}}, \dots] \in \mathbb{R}^{145}$$

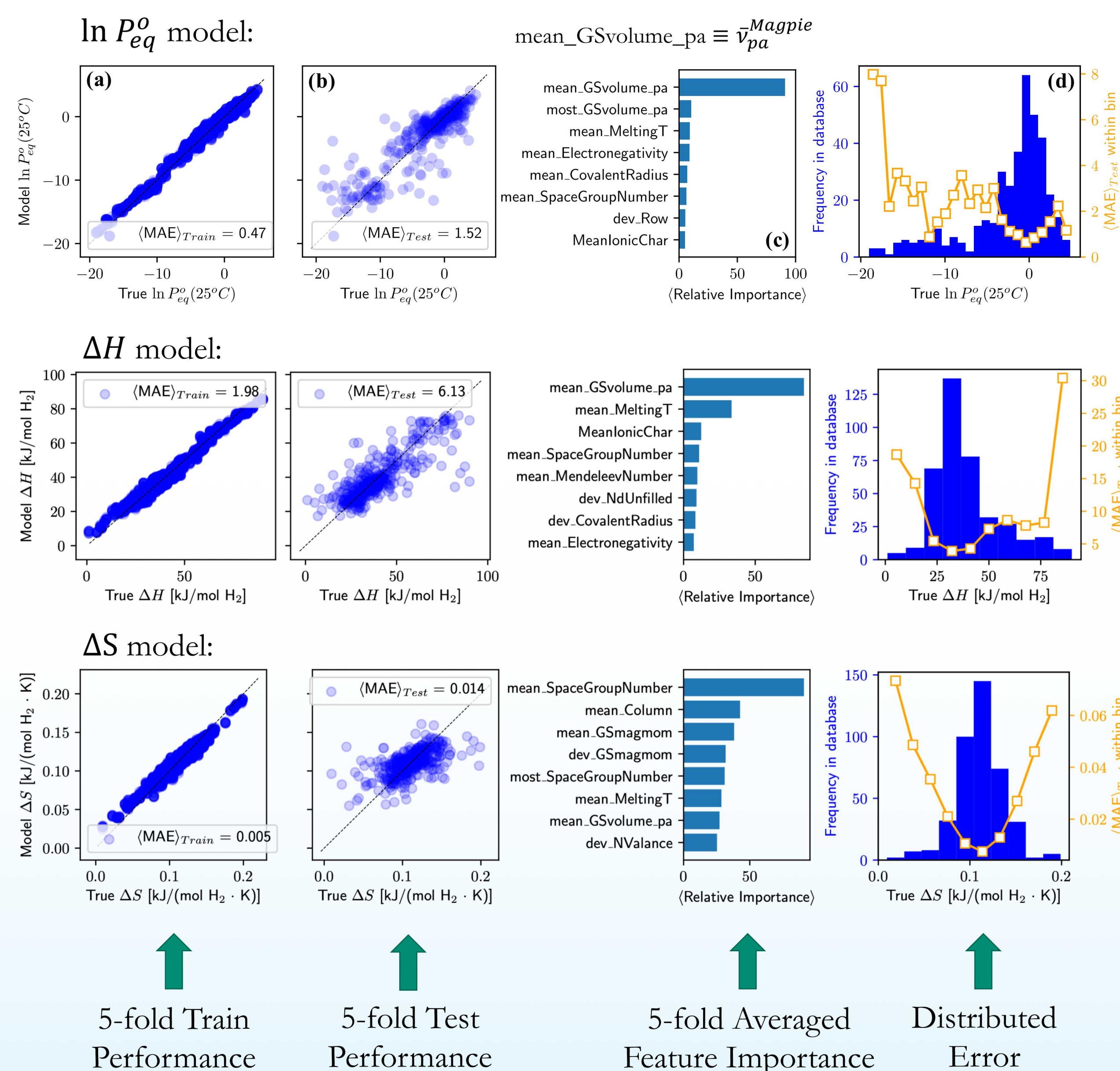
$$\bar{v}_{pa}^{\text{Magpie}} = \sum f_i v_i, \quad f_i \equiv \text{composition fraction of element } i$$

$$v_i \equiv \text{ground state volume per atom of solid element } i$$

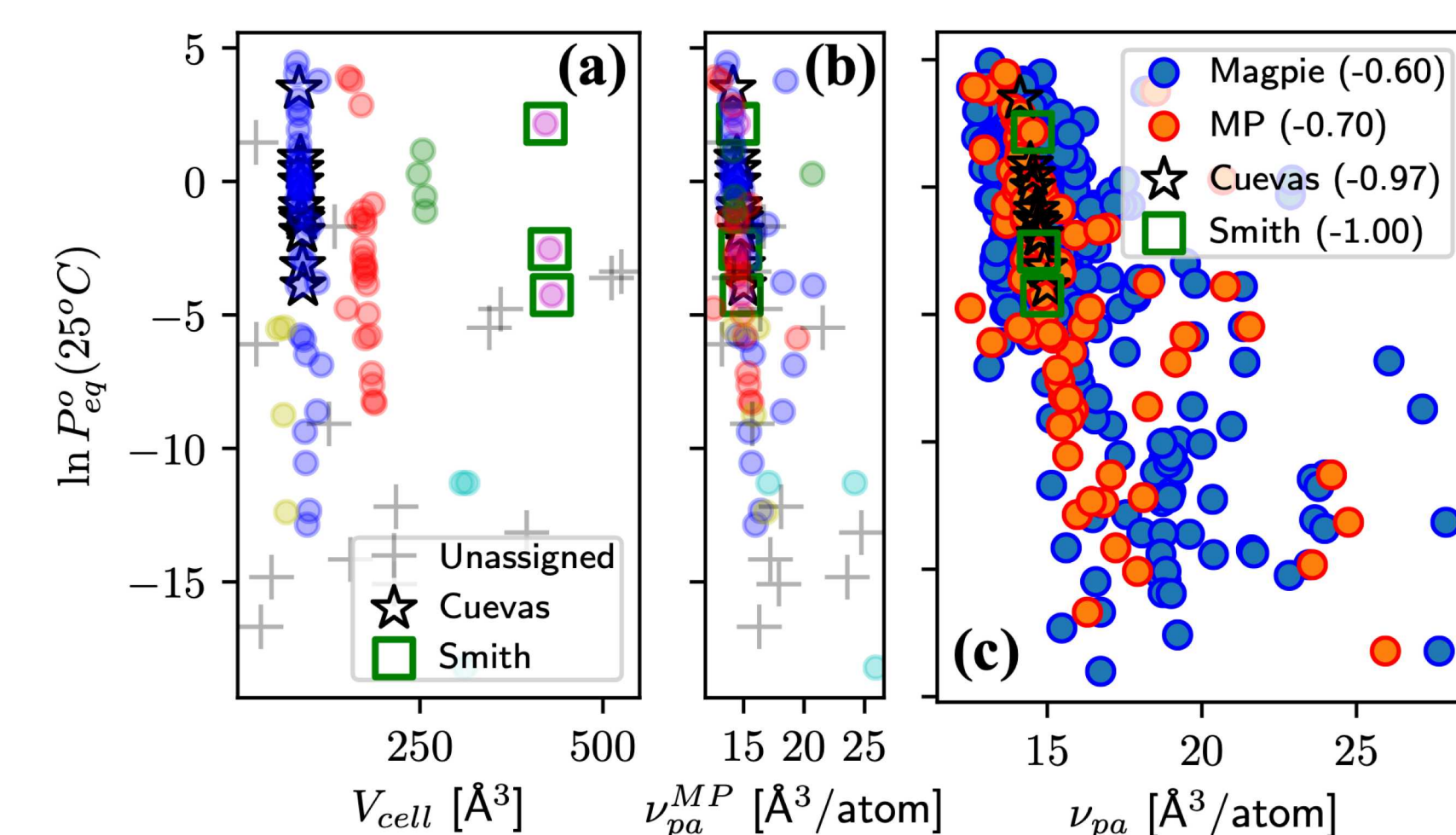
**2. Materials Project (MP)** provides electronic structure data if crystal structure known (only ~70 HydPARK compositions found in MP)

$$v_{pa}^{\text{MP}} = V_{\text{cell}}/n_{\text{atoms}} \quad V_{\text{cell}} \equiv \text{DFT optimized cell volume}$$

**3. Gradient Boosting Regressors** are "interpretable": they reveal the relative importance of each feature in the model's prediction [3]



## Exploiting Explainable Insights



1. Reveals log-linear relationship with  $v_{pa}$
2. Unifies previous experimental results with a single structure-property relationship
3. Provides an empirical design rule to target low, moderate, or high stability hydrides

## Novel Hydride with Targeted Thermodynamics

Utilize DFT to (1) gain insight into the  $v_{pa}$  structure-property relationship and (2) validate the hypothesis that a known intermetallic (UNi<sub>5</sub> whose hydriding properties have not yet been tested) would form an ultra low-stability (high-pressure) hydride:

$$\text{For ANi}_5 \rightarrow \text{ANi}_5\text{H}_7 \quad (\text{A}=\text{U, Ce, La})$$

$$E_f \equiv \text{formation energy of ANi}_5\text{H}_7$$

$$\Delta E_{\text{def}} \equiv \text{deformation energy to accommodate H absorption}$$

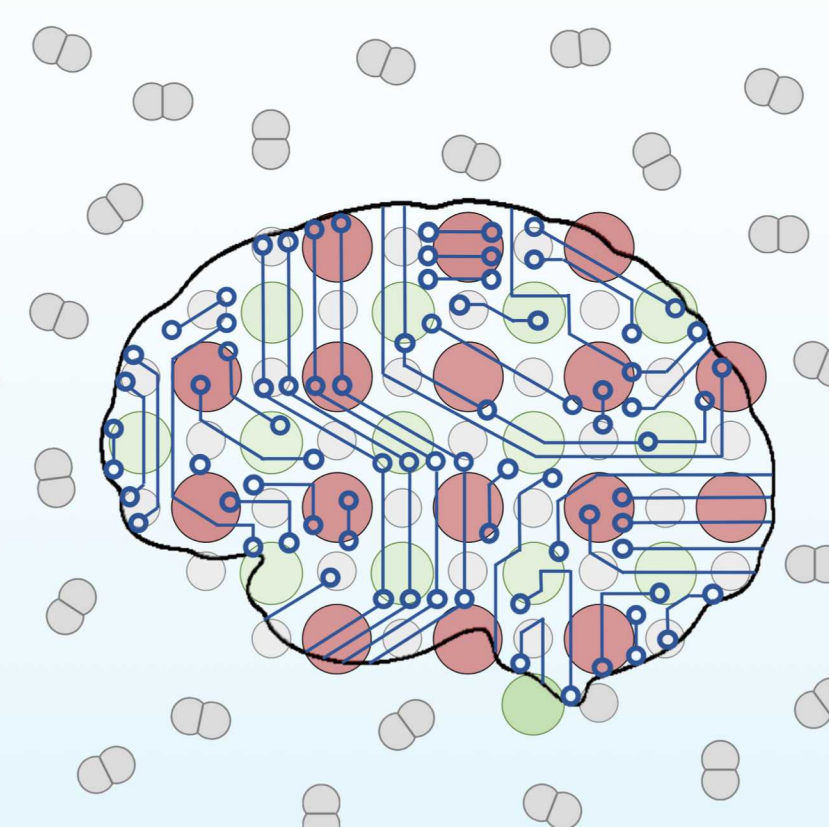
$$\Delta E_H \equiv \text{binding energy of H}$$

$$V/V_0 \equiv \text{volume expansion upon H absorption}$$

	$v_{pa}$	$\Delta H$	$E_f$	$\Delta E_{\text{def}}$	$\Delta E_H$	$V/V_0$
UNi <sub>5</sub>	13.17	-0.60	-285	65.2	-65.8	1.278
CeNi <sub>5</sub>	13.76	-20.5	-353	49.3	-69.8	1.266
LaNi <sub>5</sub>	14.38	-36.1	-224	44.3	-80.5	1.256

## Conclusions

1. ML models and experimental data provide a powerful tool to explore phenomena too expensive for computational approaches
2. Equilibrium pressure in intermetallic hydrides can be predicted just from the alloy composition, despite noisy/incomplete data
3. Explainable insights from the ML model permit the rational design of novel materials with targeted thermodynamic properties



[1] Witman, M. et al. *J. Phys. Chem. Lett.* **2020**, 11, 1, 40-47

[2] Ward, L. et al. *npj Comput. Mater.* **2016**, 2, 16028

[3] Hastie, T. et al. *The Elements of Statistical Learning*. **2009**