

# Sandia National Laboratories Extracting an Empirical Intermetallic Hydride Design Principle from Limited Data via Interpretable Machine Learning

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## Introduction

An open question in the metal hydride community is whether there are simple, physics-based design rules that dictate the thermodynamic properties of these materials across the variety of structures and chemistry they can exhibit. While black box machine learning (ML)-based algorithms can predict these properties with some success, they do not directly provide the basis on which these predictions are made, therefore complicating the a priori design of novel materials exhibiting a desired property value. In this work we demonstrate how feature importance, as identified by a gradient boosting tree regressor, uncovers the strong dependence of the metal hydride equilibrium  $H_2$  pressure on a volume-based descriptor that can be computed from just the elemental composition of the intermetallic alloy. Elucidation of this simple structure–property relationship is valid across a range of compositions, metal substitutions, and structural classes exhibited by intermetallic hydrides. This permits rational targeting of novel intermetallics for high-pressure hydrogen storage (low-stability hydrides) by their descriptor values, and we predict a known intermetallic to form a low-stability hydride (as confirmed by density functional theory calculations) that has not yet been experimentally investigated [1].

## Data cleaning

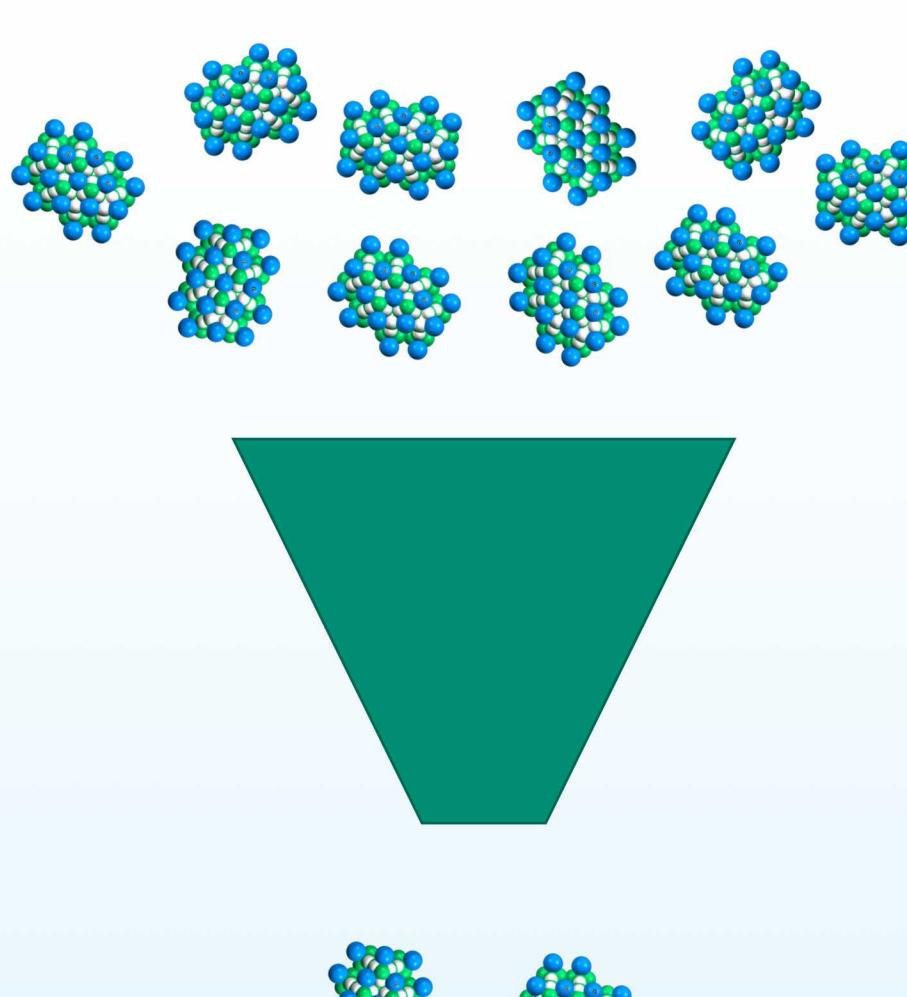
**HydPARK** is Sandia's historical dataset on metal hydride properties:

Class	Composition	H wt %	$\Delta H$ (kJ/mol $H_2$ )	$T$ (K)	$P_{eq}$ (atm)
A <sub>2</sub> B	Ce <sub>0.5</sub> Th <sub>1.5</sub> Al <sub>1</sub>	0.4	133	650	0.0003
AB <sub>5</sub>	La <sub>0.75</sub> Ce <sub>0.25</sub> Ti <sub>0.1</sub> Cu <sub>0.9</sub> Ni <sub>4</sub>	1.4	38.4	22	1.1

**Target property:** Compute equilibrium pressure at room temperature,

$$\ln P_{eq}^0 = -\Delta H/RT^0 + \Delta S/R$$

to gauge a material's thermodynamic utility in a given storage application



Initial: ~ 2500 HydPARK compositions

1. Remove duplicate compositions
2. Remove entries with missing data, i.e.  $\ln P_{eq}^0$  can't be computed

Final: ~ 400 "ML ready" compositions

## ML Model Development

1. **Magpie** presents a useful way to featurize inorganic materials in terms of elemental properties when exact crystal structures are not known [2]

$$\mathbf{x}_{LaNi5} = [\bar{v}_{pa}^{Magpie}, \bar{T}_{melt}, \dots] \in \mathbb{R}^{145}$$

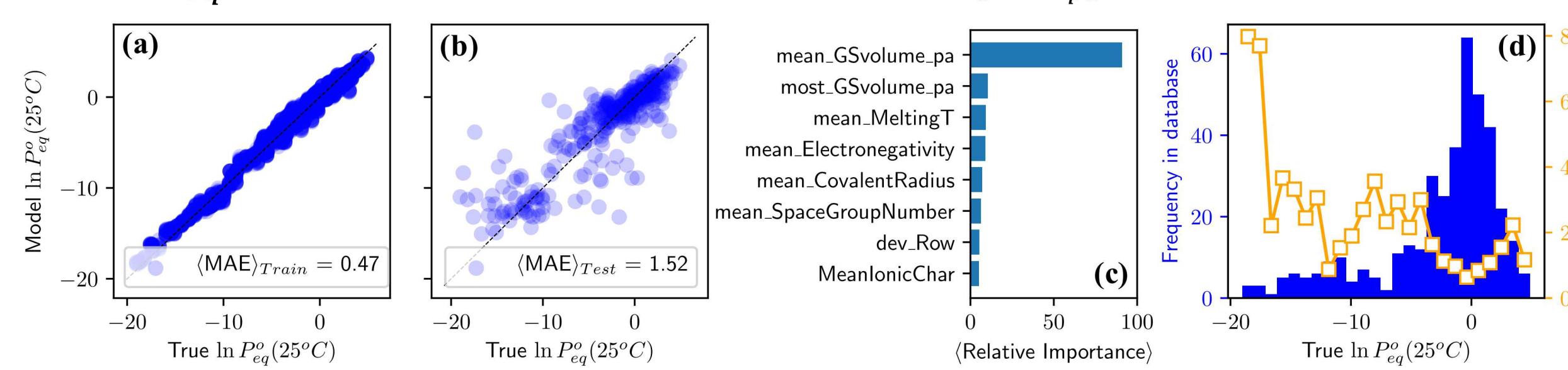
$$\bar{v}_{pa}^{Magpie} = \sum f_i v_i, \quad f_i \equiv \text{composition fraction of element } i \\ v_i \equiv \text{ground state volume per atom of solid element } i$$

2. **Materials Project (MP)** provides electronic structure data if crystal structure known (only ~70 HydPARK compositions found in MP)

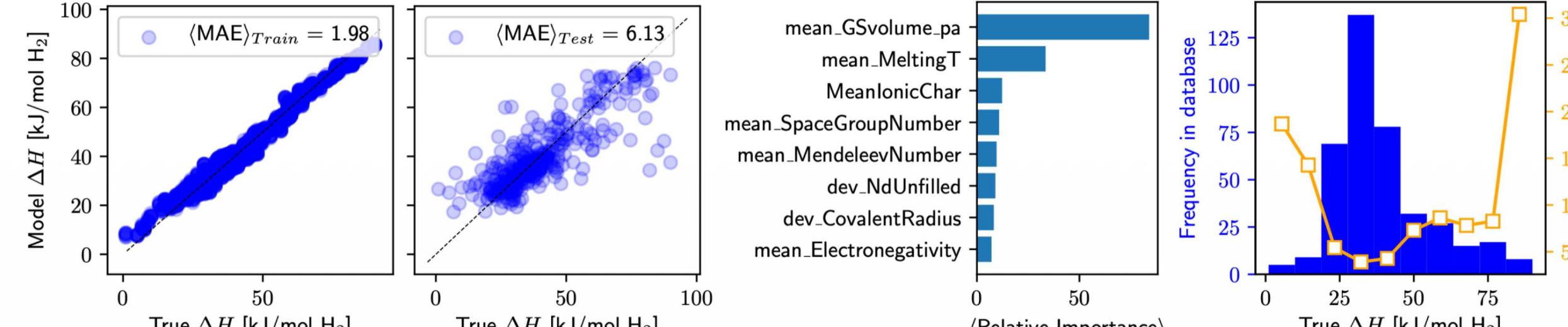
$$v_{pa}^{MP} = V_{cell}/n_{atoms} \quad V_{cell} \equiv \text{DFT optimized cell volume}$$

3. **Gradient Boosting Regressors** are "interpretable" : they reveal the relative importance of each feature in the model's prediction [3]

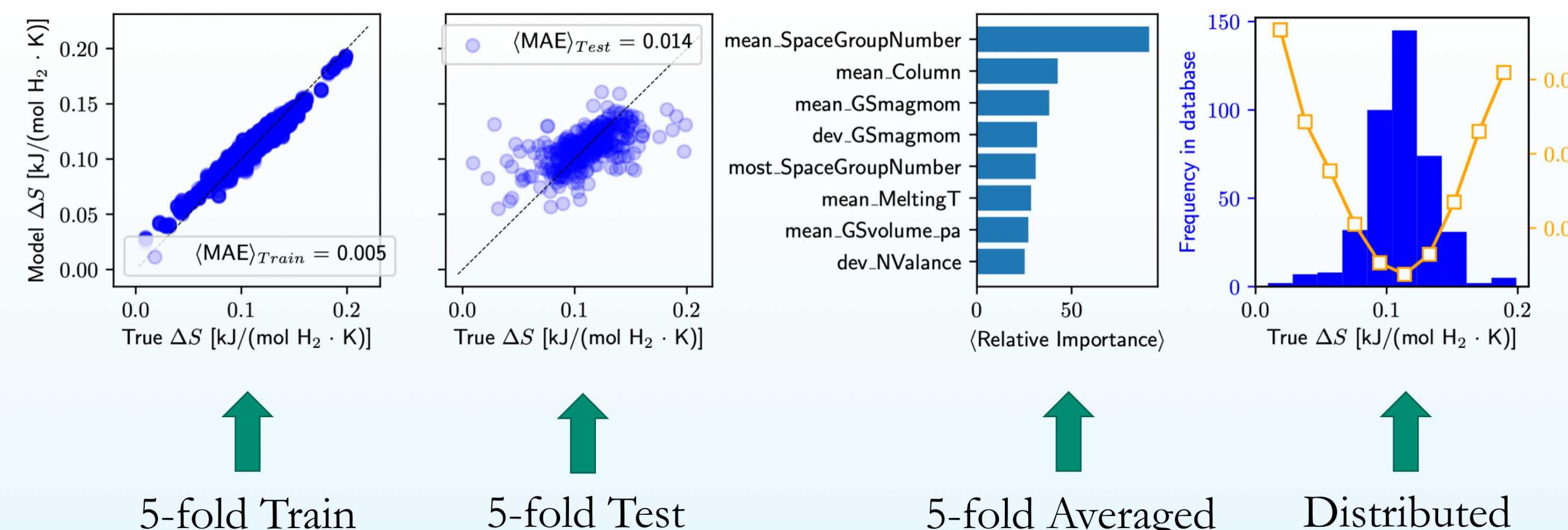
$\ln P_{eq}^0$  model:



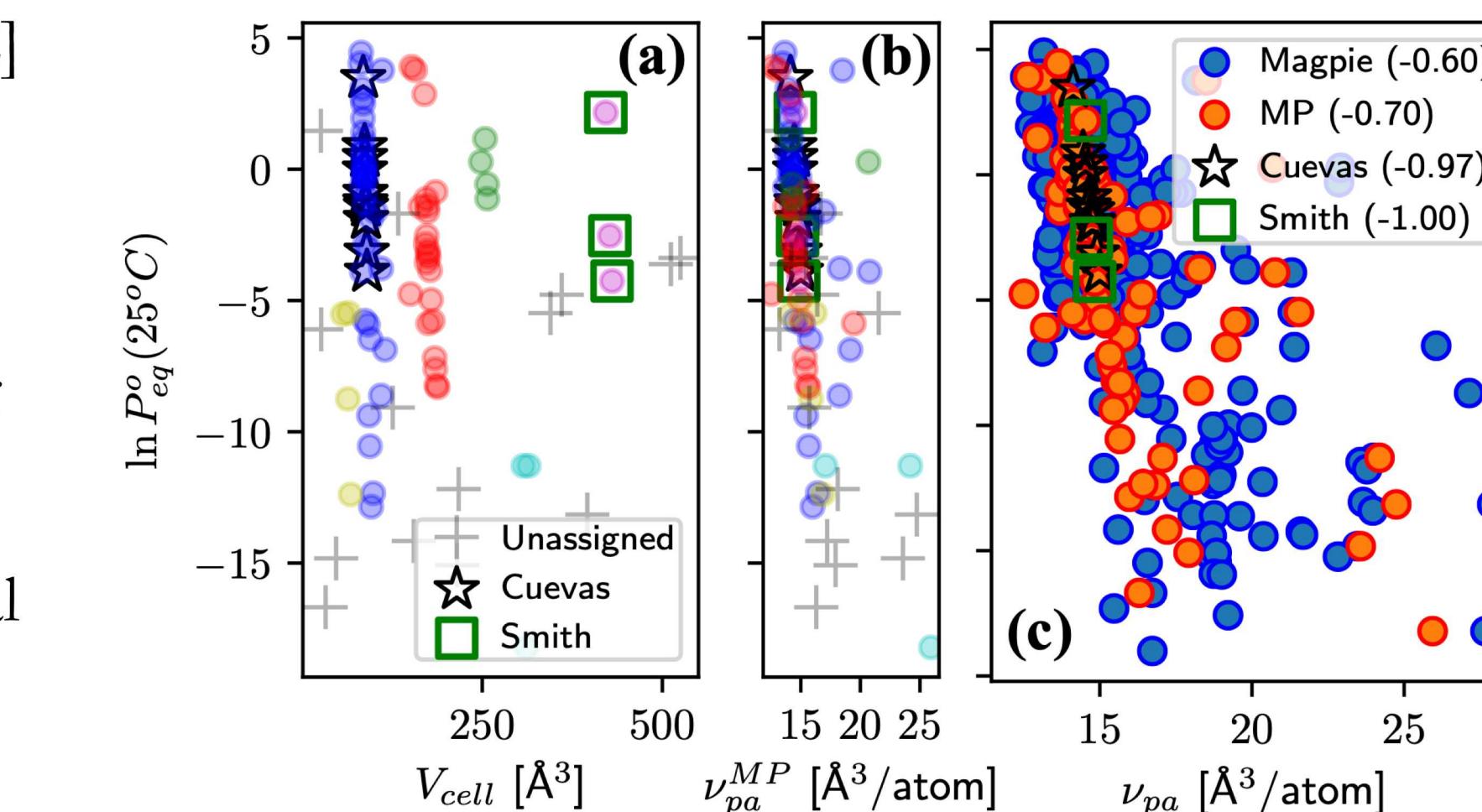
$\Delta H$  model:



$\Delta S$  model:



## Exploiting Explainable Insights



1. Reveals log-linear relationship with  $v_{pa}$
2. Unifies previous experimental results with a single structure–property relationship
3. Provides an empirical design rule to target low, moderate, or high stability hydrides

## Novel Hydride with Targeted Thermodynamics

Utilize DFT to (1) gain insight into the  $v_{pa}$  structure–property relationship and (2) validate the hypothesis that a known intermetallic (UNi<sub>5</sub> whose hydriding properties have not yet been tested) would form an ultra low-stability (high-pressure) hydride:

For ANi<sub>5</sub>  $\rightarrow$  ANi<sub>5</sub>H<sub>7</sub> (A=U, Ce, La)

$E_f$   $\equiv$  formation energy of ANi<sub>5</sub>H<sub>7</sub>

$\Delta E_{def}$   $\equiv$  deformation energy to accommodate H absorption

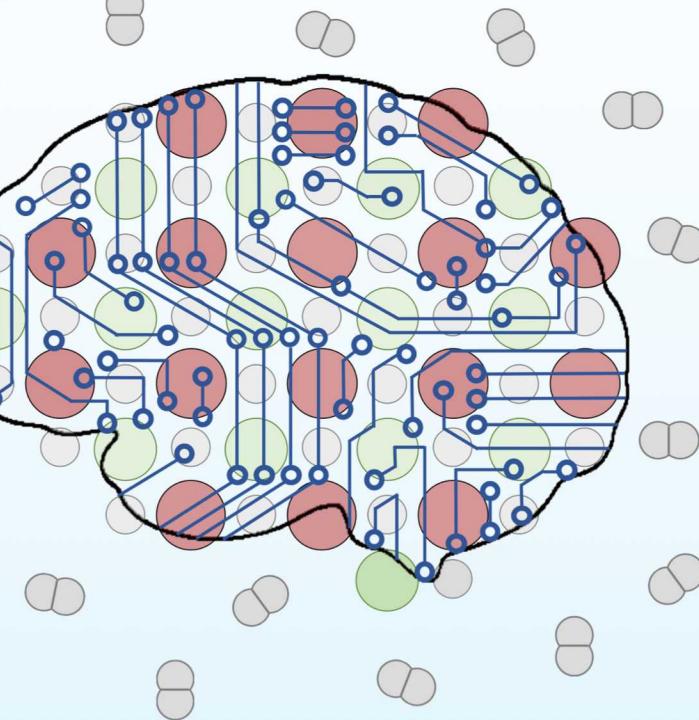
$\Delta E_H$   $\equiv$  binding energy of H

$V/V_0$   $\equiv$  volume expansion upon H absorption

	$v_{pa}$	$\Delta H$	$E_f$	$\Delta E_{def}$	$\Delta E_H$	$V/V_0$
UNi <sub>5</sub>	13.17	-0.60	-285	65.2	-65.8	1.278
CeNi <sub>5</sub>	13.76	-20.5	-353	49.3	-69.8	1.266
LaNi <sub>5</sub>	14.38	-36.1	-224	44.3	-80.5	1.256

## Conclusions

1. ML models and experimental data provide a powerful tool to explore phenomena too expensive for computational approaches
2. Equilibrium pressure in intermetallic hydrides can be predicted just from the alloy composition, despite noisy/incomplete data
3. Explainable insights from the ML model permit the rational design of novel materials with targeted thermodynamic properties



[1] Witman, M. et al. *J. Phys. Chem. Lett.* 2020, 11, 1, 40-47

[2] Ward, L. et al. *npj Comput. Mater.* 2016, 2, 16028

[3] Hastie, T. et al. *The Elements of Statistical Learning*. 2009



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