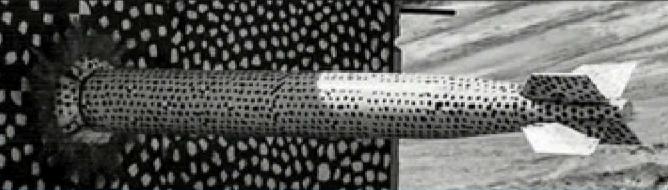


# Optimization-based Design for Manufacturing: Using Plato to Incorporate Manufacturability Objectives into the Design Process



## CONTRIBUTORS

Miguel Aguijo, Brett Clark, Bradley Jared, Kyle Johnson,  
Joshua Robbins

## PRESENTED BY

Brett Clark



# Motivation

Additive manufacturing process outcomes, e.g., residual stress and part distortion, vary with part design and support structure.

**Objective:** Create software for generating designs and support structure that are optimized for performance *and* manufacturability.

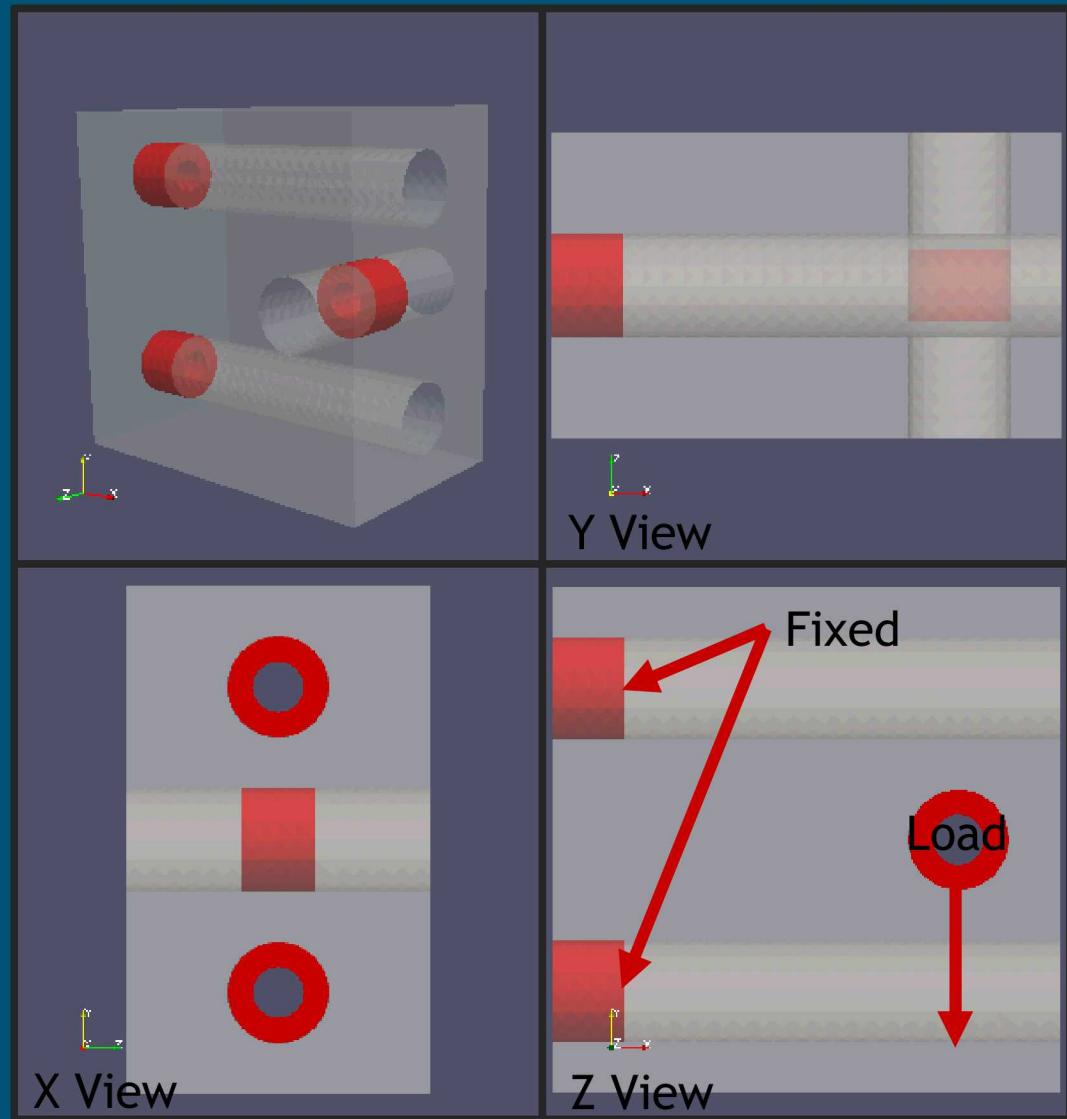
**Approach:** Incorporate fast process simulations into the optimization loop to introduce manufacturability objectives.

- Plato Engine - parallelism
- Plato Analyze - fast PDE enforcement



Design courtesy of Clinton Holtey using Plato. Displacement predictions by Kyle Johnson. Red = 0.1 mm.

# Topology Optimization with “Process Objectives”



*Objectives:*

Mechanical stiffness

+

Manufacturability

*PDE Constraints:*

Mechanical equilibrium w/ Load

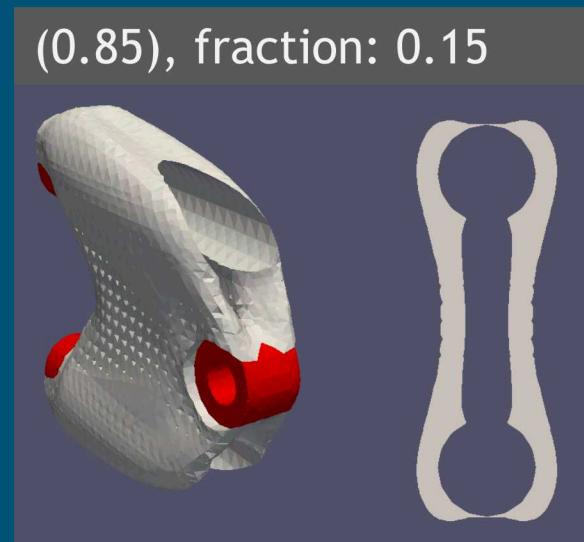
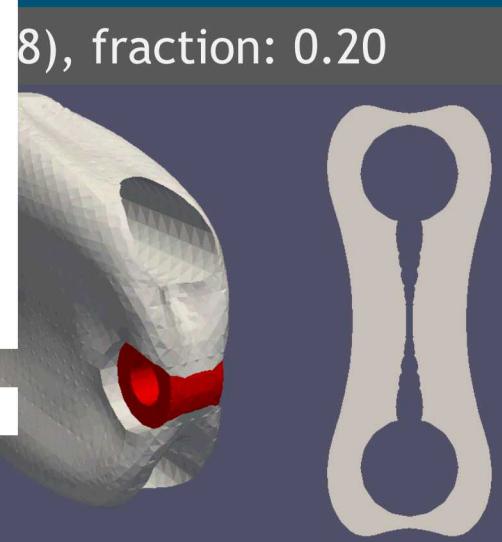
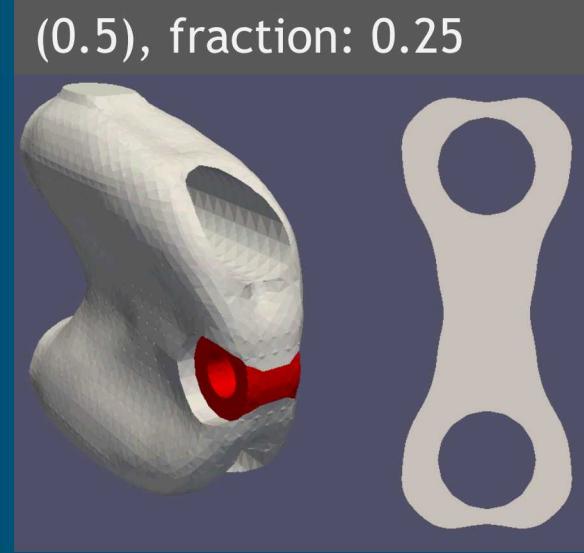
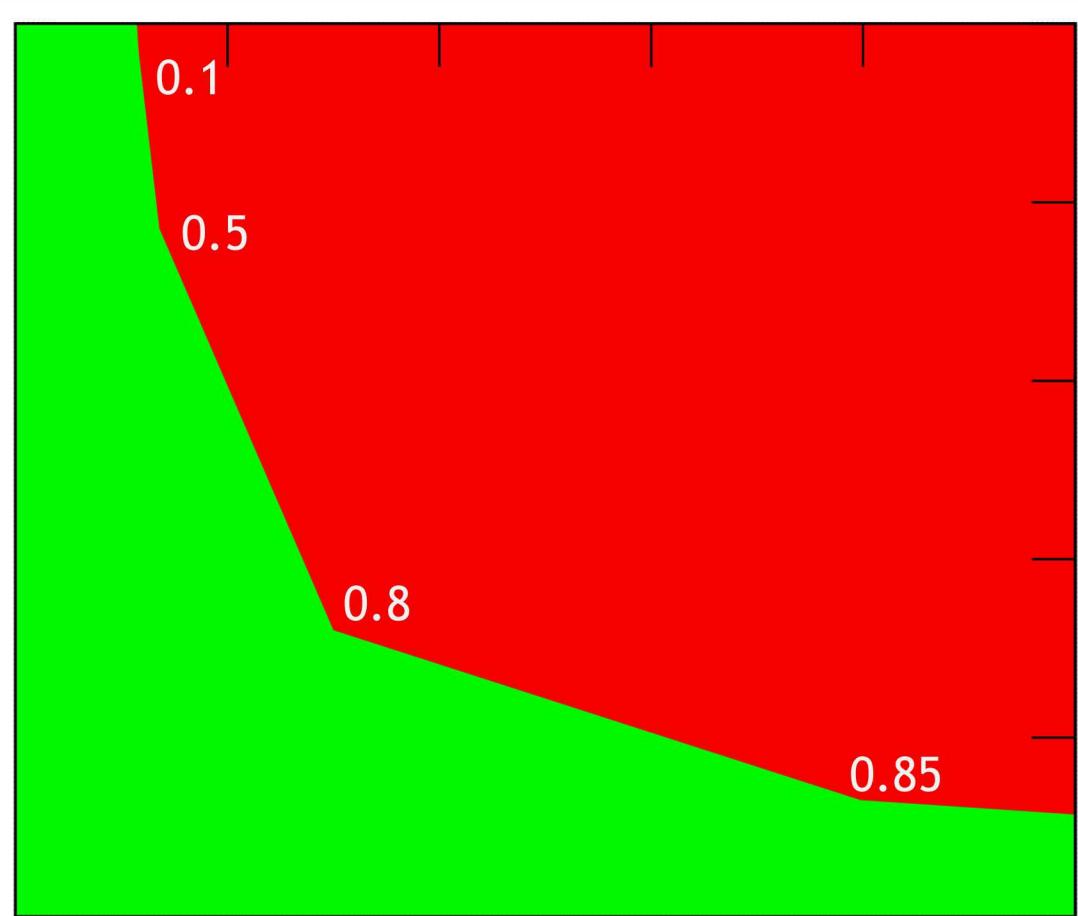
+

Mechanical equilibrium w/ IS

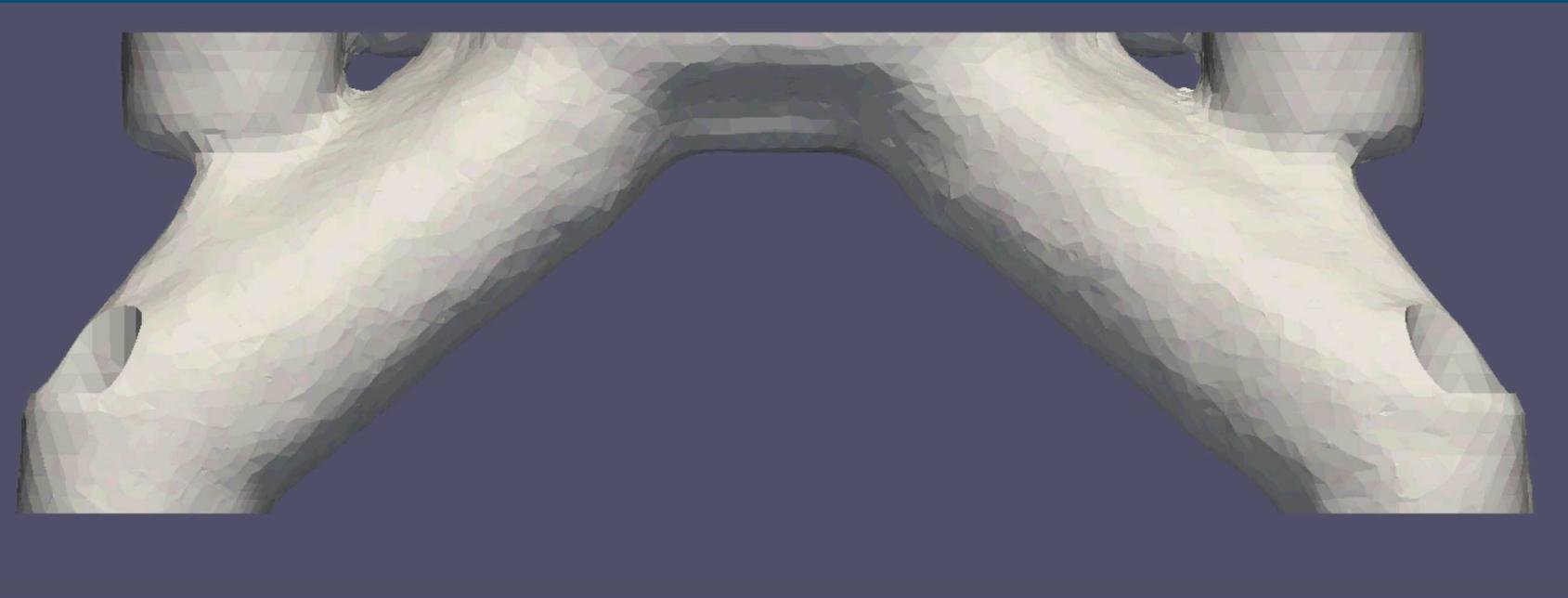
*Inequality Constraint:*

Design volume

## Topology Optimization with “Manufacturability Objectives”



# Approach: Fast Process Simulation



## Simulation Process

- For each “super layer”
  - Deposition
  - Time dependent thermomechanical equilibration
- Remove from baseplate
- Compute mechanical equilibrium and process outcomes (metrics)

## Balance Equations

$$\rho C_p \dot{T} - \nabla \cdot q - \dot{q}_v = 0$$

$$\nabla \cdot \sigma + b = 0$$

## Material Response

$$\sigma = C \varepsilon^e$$

$$q = k \nabla T$$

$$\varepsilon^e = \nabla_s u - \alpha(T - T_{ref}) - \varepsilon^p(c)$$

## Solution Variables

$$u \equiv u(x, t) \in R^{n_d}$$

$$T \equiv T(x, t) \in R$$

$$c \equiv c(x, t) \in R^{n_s}$$

### Advantages:

- Improved accuracy relative to Inherent Strain Method. Important for residual stresses.
- Quantities of interest are available at intermediate stages. Control distortion *during the print*.
- Support structure is produced with the design, so it can inform constraints and objectives.

### Disadvantages:

- Higher computational cost relative to Inherent Strain Method.

### Progress:

- (100%) Time dependent heat equation
- (100%) Stabilized thermomechanics
- (100%) J2 Plasticity
- (90%) Path-dependent adjoint
- (50%) Differentiable support structure

Initial capability to be available mid FY20

# Plato Analyze

## Code Design:

- Uses hardware abstraction so compiles readily on GPU and CPU
- Uses Automatic Differentiation and Adjoint Variable Method so gradients are automagic
- Physics, objectives, and constraints are templated, so new additions are straightforward

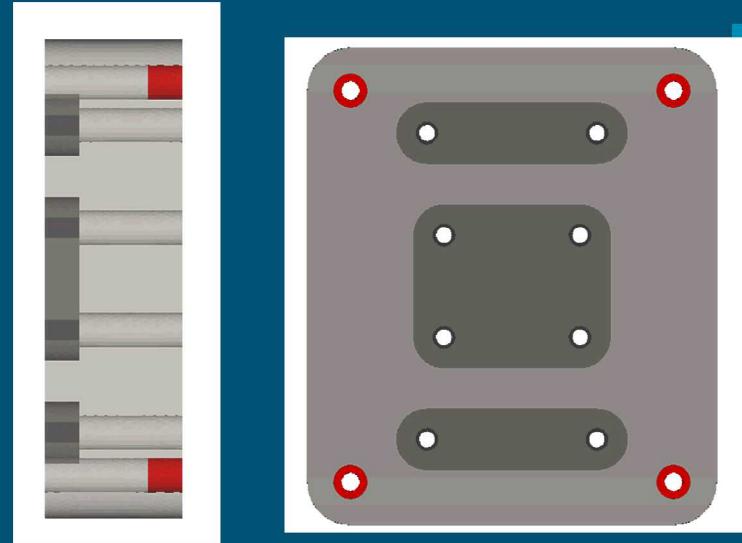
## Physics:

- Thermal / electrostatics
- Elastostatics
- Coupled thermomechanics, electromechanics
- Time dependent heat equation, thermomechanics
- Nearly incompressible mechanics, thermomechanics
- Coming soon: elastoplasticity, thermoelastoplasticity

Available at [github.com/platoengine/platoanalyze](https://github.com/platoengine/platoanalyze)

Plato training session in early 2020.

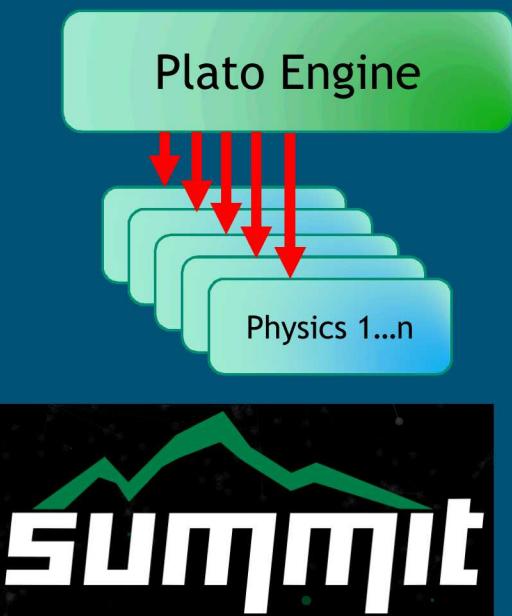
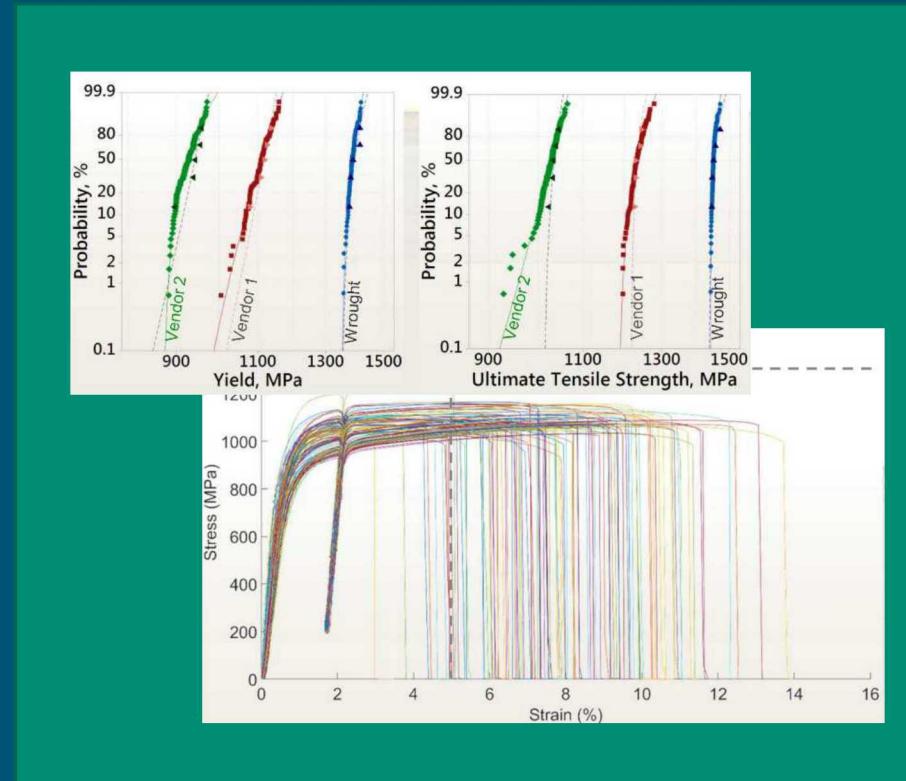
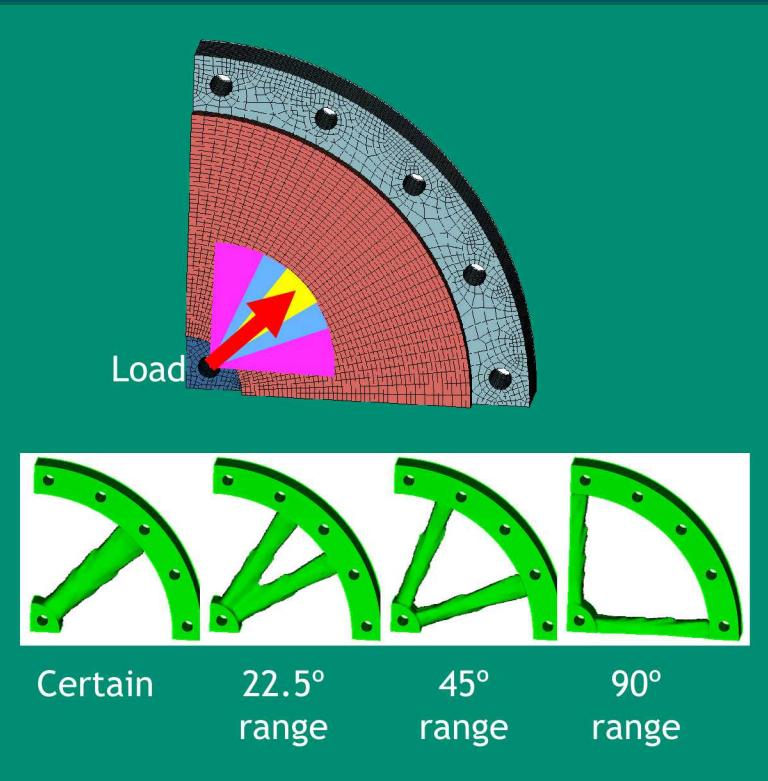
Contact [Plato3D-help@sandia.gov](mailto:Plato3D-help@sandia.gov) for more info.



Load Uncertainty

+ Material Uncertainty

Huge  
= Computational  
Cost



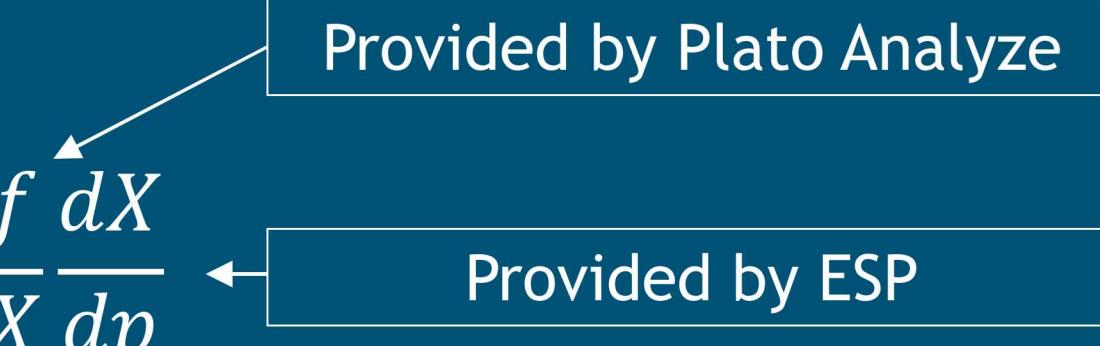


For shape optimization, we need derivatives with respect to the parameters,  $p$ :

$$\frac{df}{dp} = \frac{df}{dX} \frac{dX}{dp}$$

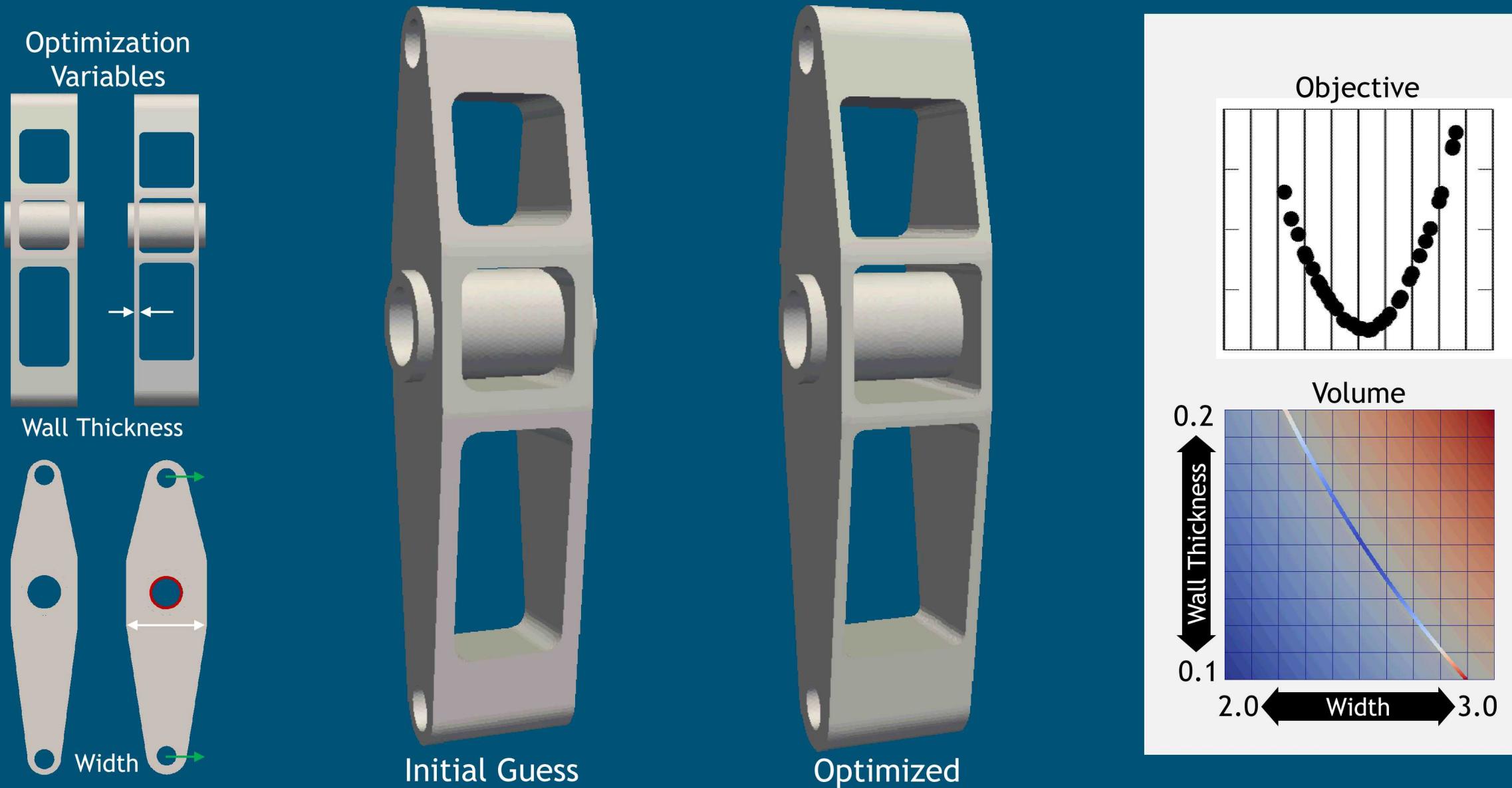
Provided by Plato Analyze

Provided by ESP



Derivatives with respect to design parameters require parameterized models

# Compliance Minimization with Volume Constraint



File Tool StepThru Help

Up to date Undo  
H L R B T +

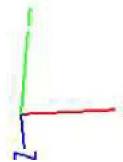
Design Parameters

TotalHeightA 1.7  
BottomWidthA 0.4  
TopWidthA 0.5  
WaistWidthA 0.3  
SkirtHeightA 0.3  
HeadHeightA 0.3  
WaistHeightA 0.1  
PitWidthA 0.4  
BarrelHeightA 0.6  
TaperHeightA 0.2  
TaperWidthA 0.4  
ThicknessA 0.2  
HeadFilletA 0.0  
CutoutOffsetA 0.7  
CutoutWidthA 0.3  
CutoutHeightA 0.6  
CutoutDepthA 0.1  
CutoutFilletA 0.0  
CutoutBackFilletA 0.0  
TopBoltYOffsetA 1.4  
TopBoltXOffsetA 0.1  
TopBoltHeadRadiusA 0.0  
TopBoltHeadCutoutDepthA 0.0  
TopBoltShaftRadiusA 0.0  
TopBoltDepthA 0.2  
StubWidthA 0.3  
StubDepthA 0.1  
StubHeightA 0.0  
StubFilletA 0.0  
BridgeThickness 0.0  
BridgeHeight 0.2

Local Variables

Branches

Display Viz  
solid\_body Viz  
Axes Viz  
DisplayType  
DisplayFilter



```
Adding: select $body 88
select $face 71 13 1
attribute capsGroup $terminal_2
====> Re-build is needed <====

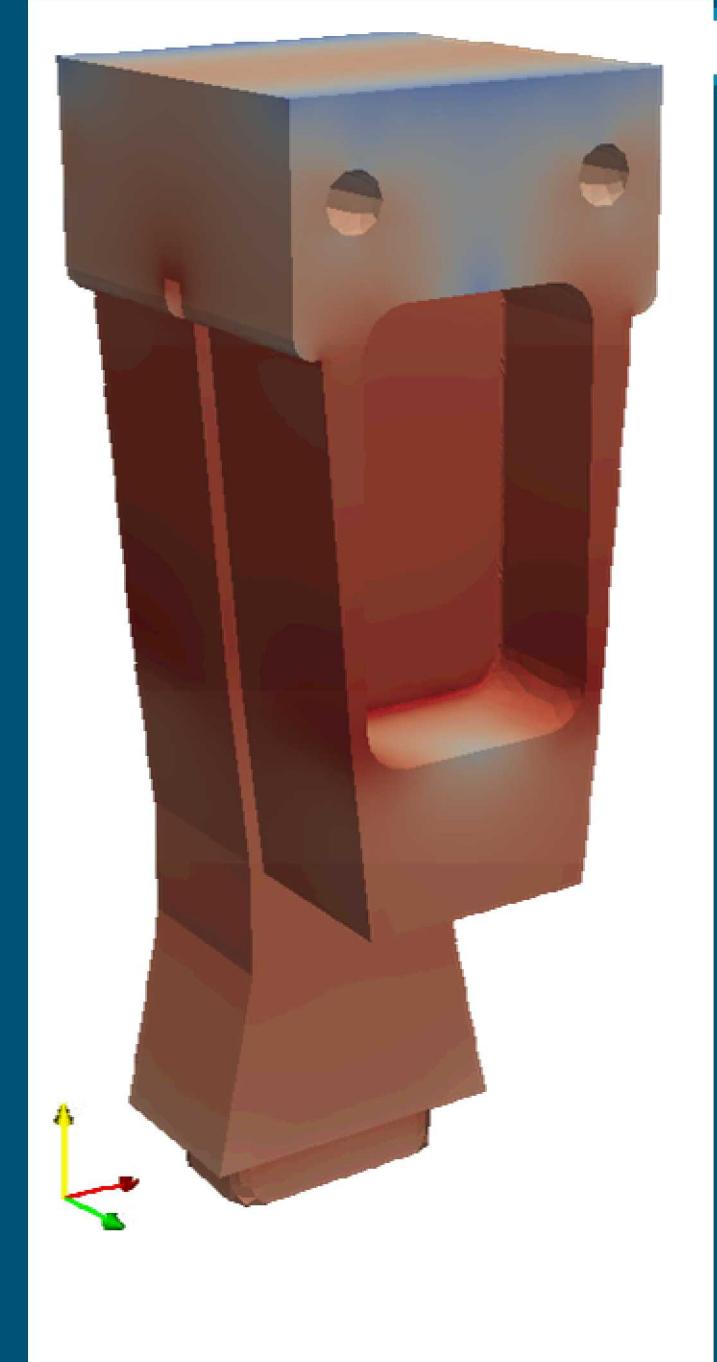
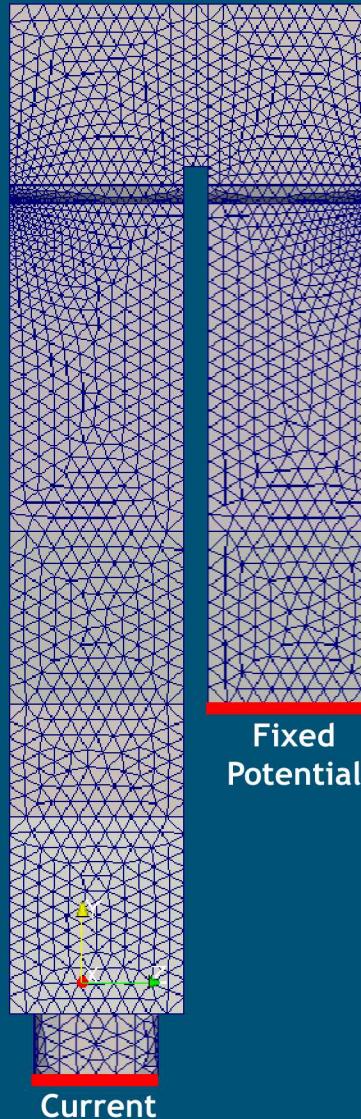
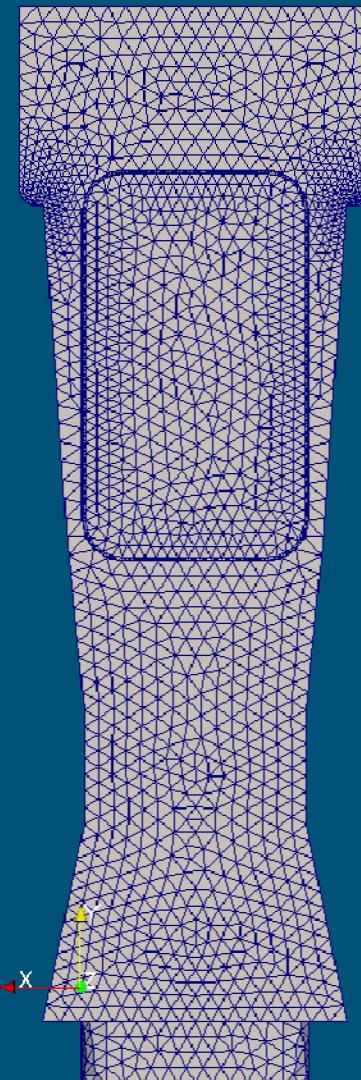
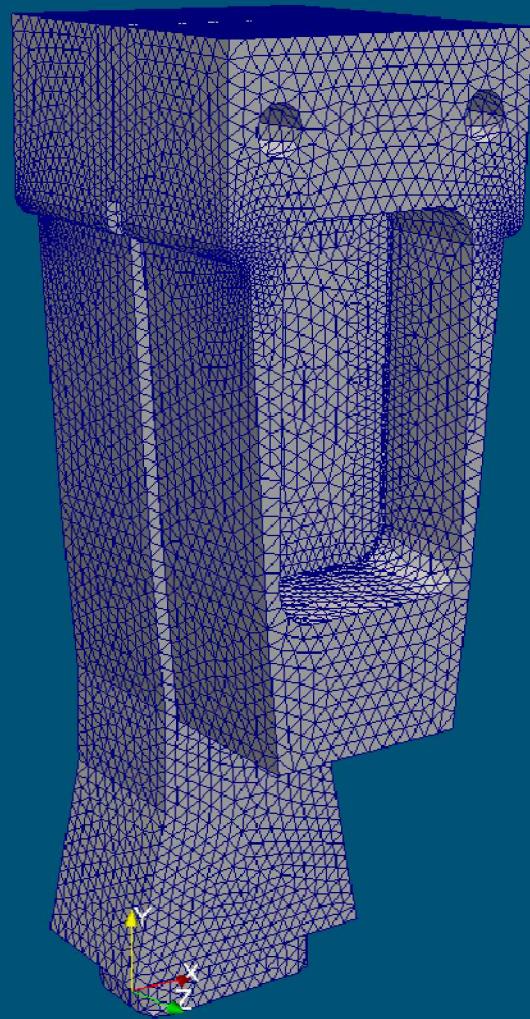
Entire build complete, which generated 1 Body(s)

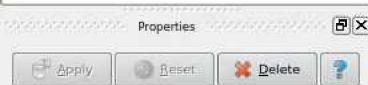
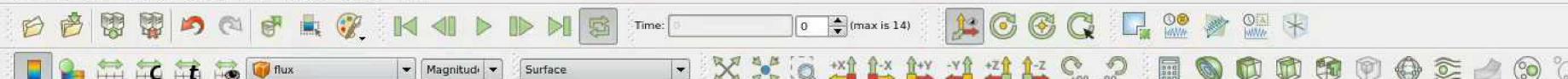
Saving model to 'load.csm'

Parameter 'TotalHeightA[1,1]' has been changed to 1.7 =====> Re-build is needed <====

Entire build complete, which generated 1 Body(s)
```

## Electrostatic Load Case



**File Edit View Sources Filters Tools Catalyst Macros Help****Properties (steps.pvd)**

File Name: /Load/forward/pnorm/out\_vtk/steps.pvd

**Display (Unstructured)**

Representation: Surface

**Coloring**

Coloring: flux

Magnitude

Edit

Color

Color

Scalar Coloring

Map Scalars

Interpolate Scalars Before Mapping

**Styling**

Opacity: 1

Point Size: 2

Line Width: 1

**Lighting**

Interpolation: Gouraud

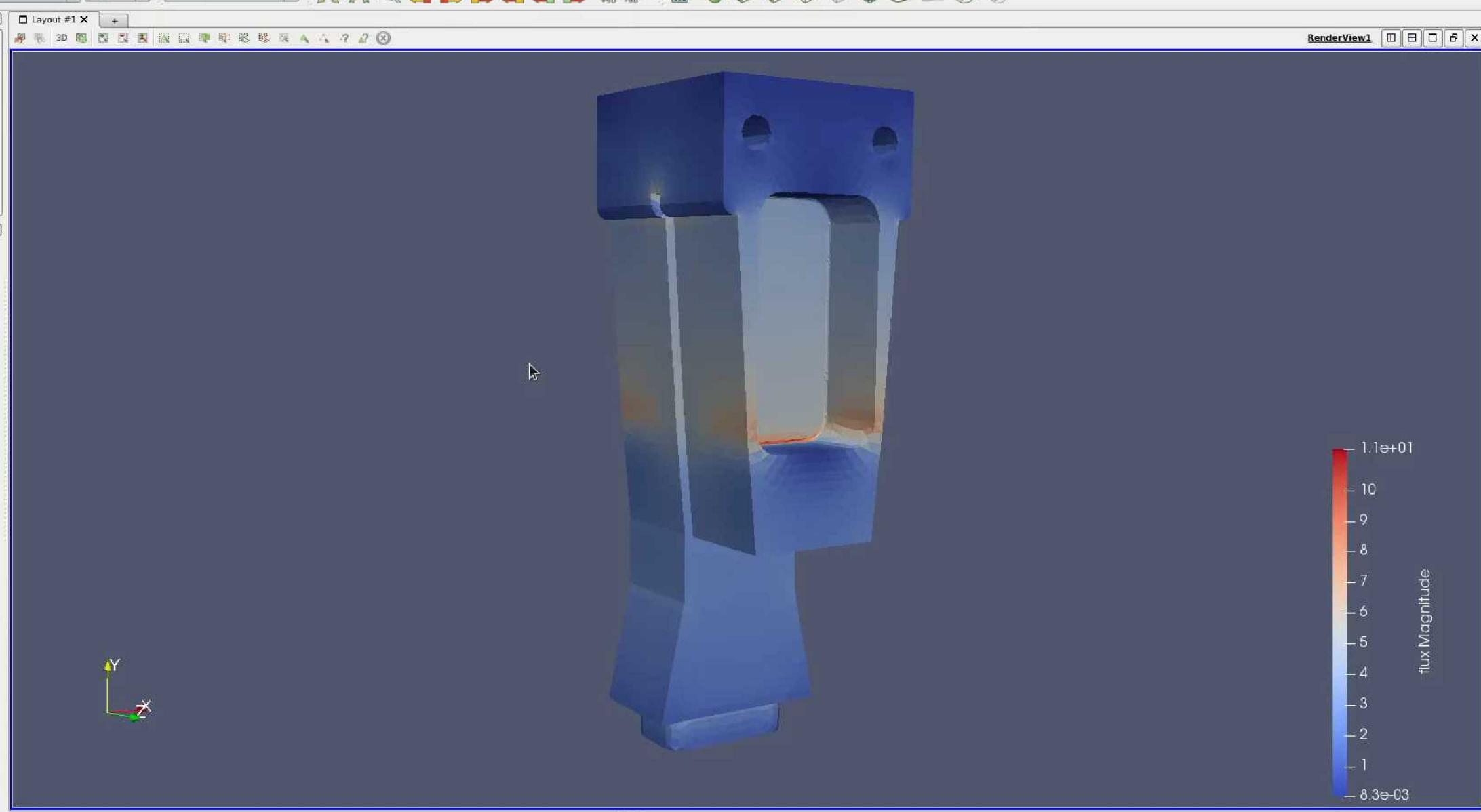
Specular: 0

Specular Color

Specular Power: 100

Ambient: 0

Diffuse: 1



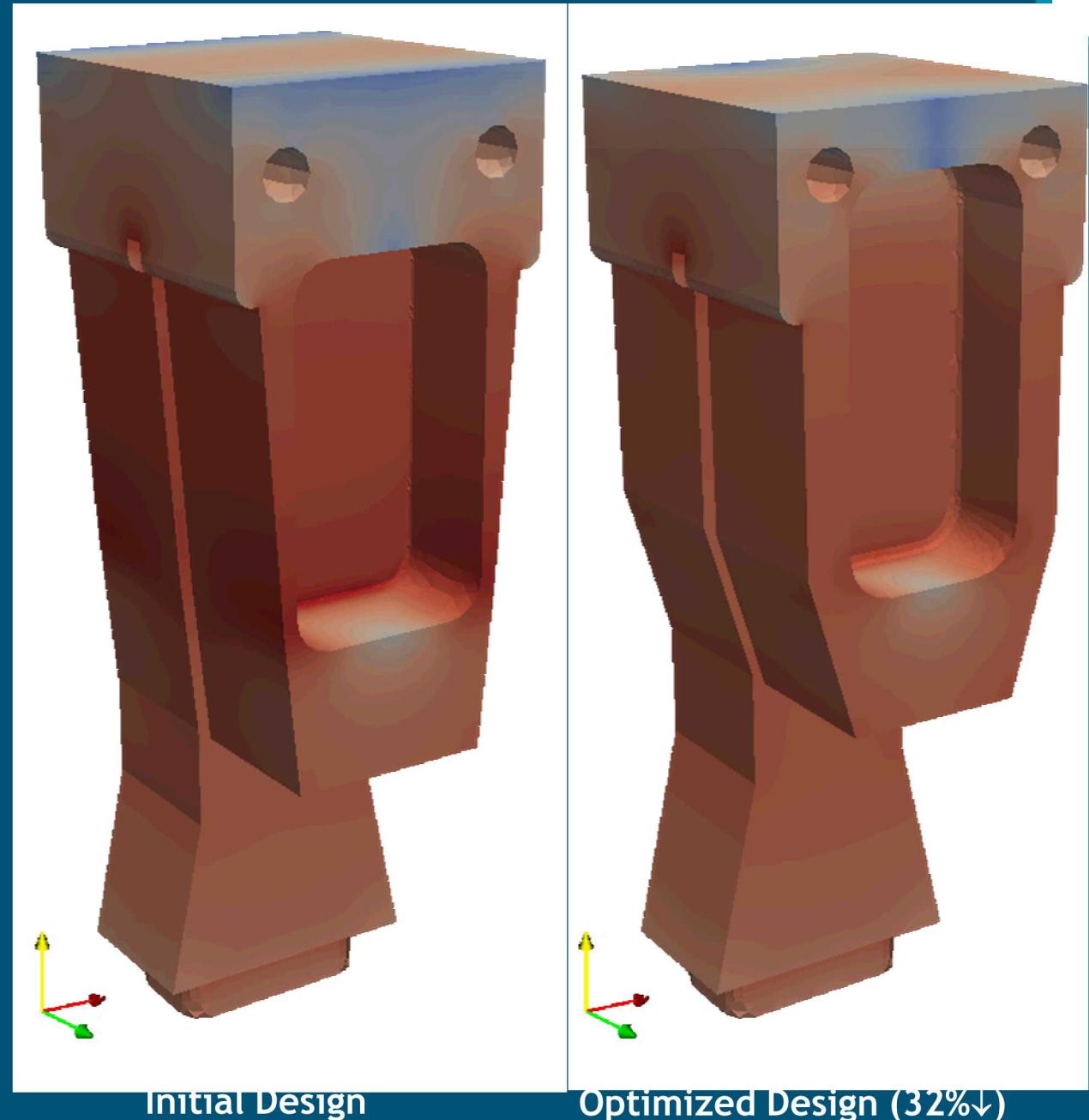
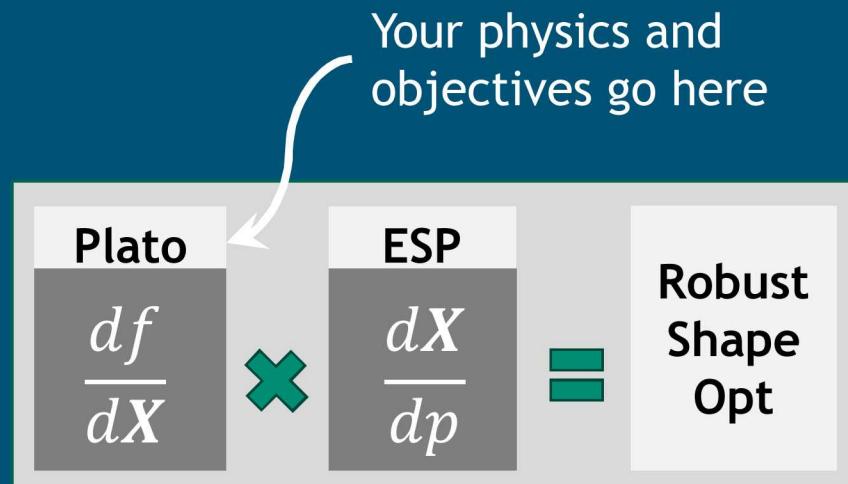
# Shape Optimization with Plato/ESP

## Progress:

- ESP functionality implemented in Plato Engine
- Beta Plato/ESP capability available for early adopters.

## Next Steps:

- Testing and hardening of Plato/ESP
- Shape optimization + topology optimization

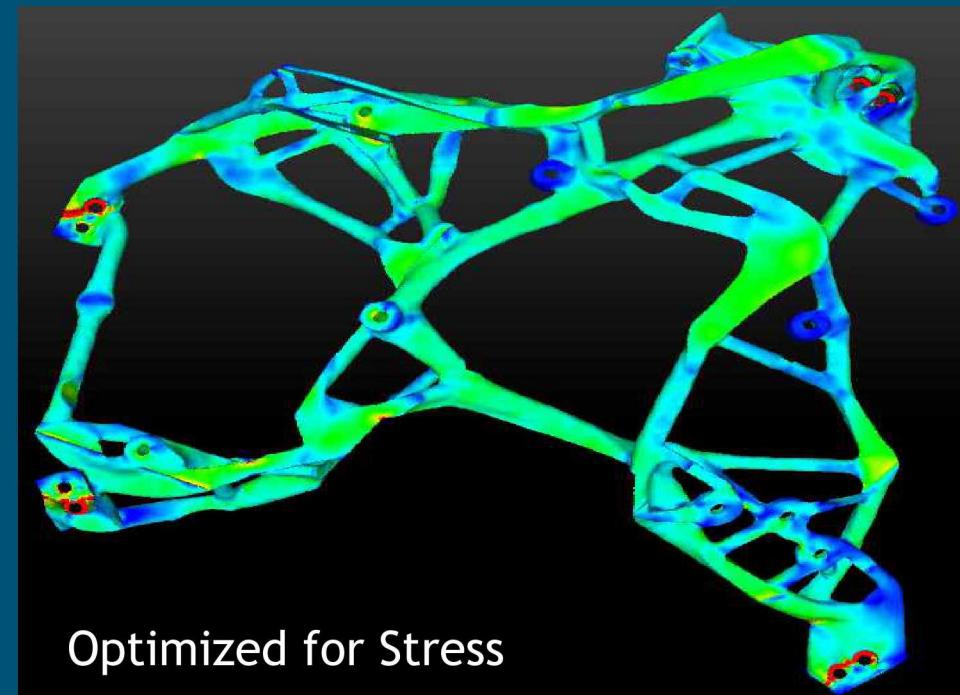
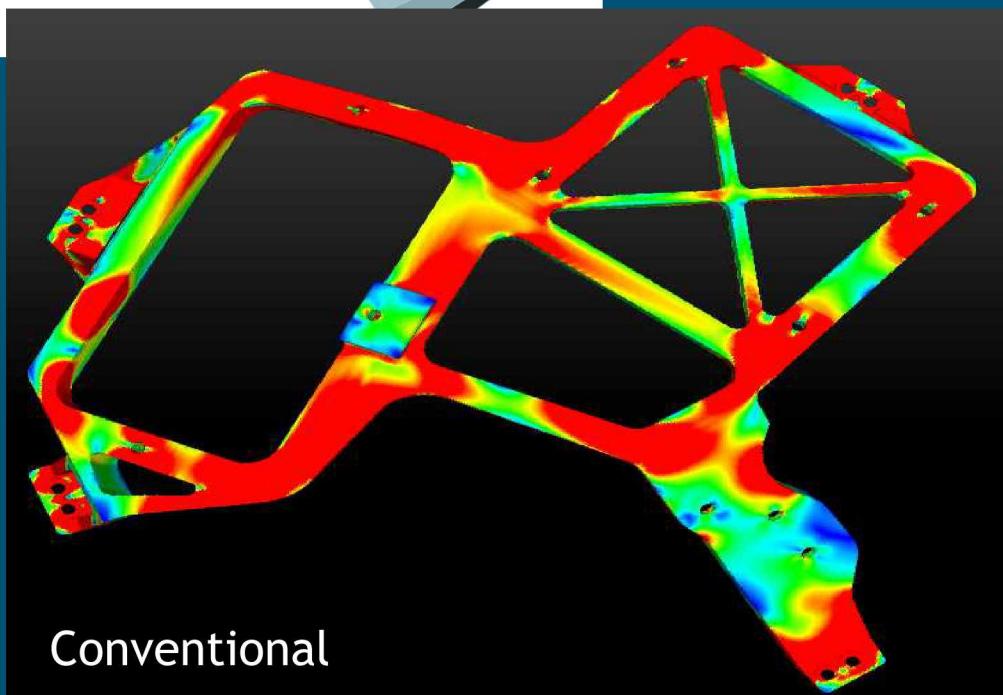


## Local Constraints



New PLATO capability for locally constraining quantities of interest (like stress) during optimization

(stress plot showing stress hot spots as red)



# Summary



**Approach:** compose objectives that reflect details of the print process so designs can be computed that i) exhibit superior printability, and ii) meet essential performance requirements.

## Progress:

- Stabilized two-field formulation
- Implemented forward and adjoint problems
- Comparison with finite difference shows good agreement
- Initial performance is encouraging
- Local state residual implemented and thoroughly unit tested

## Current effort:

- Integrate stabilized two-field residual and local state residual for non-linear transient thermomechanics
- Experiments: hole drilling w/ digital image correlation
- Implement layer hatching for super-layer deposition
- Differentiable support structure