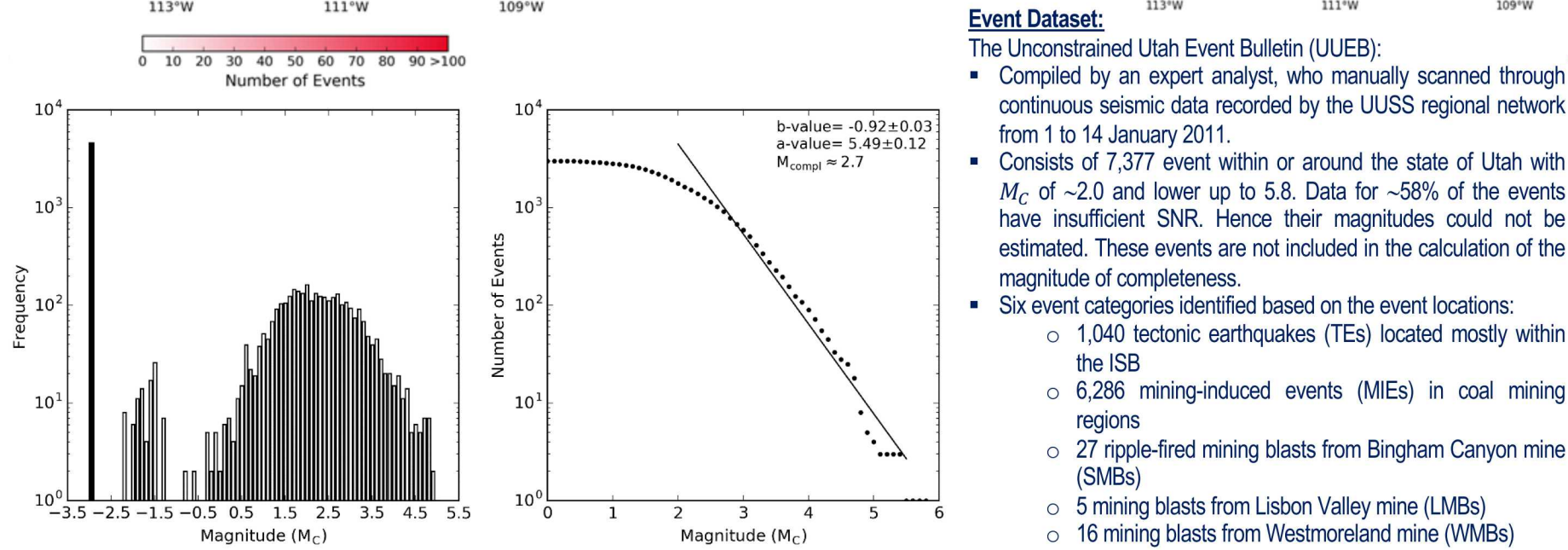
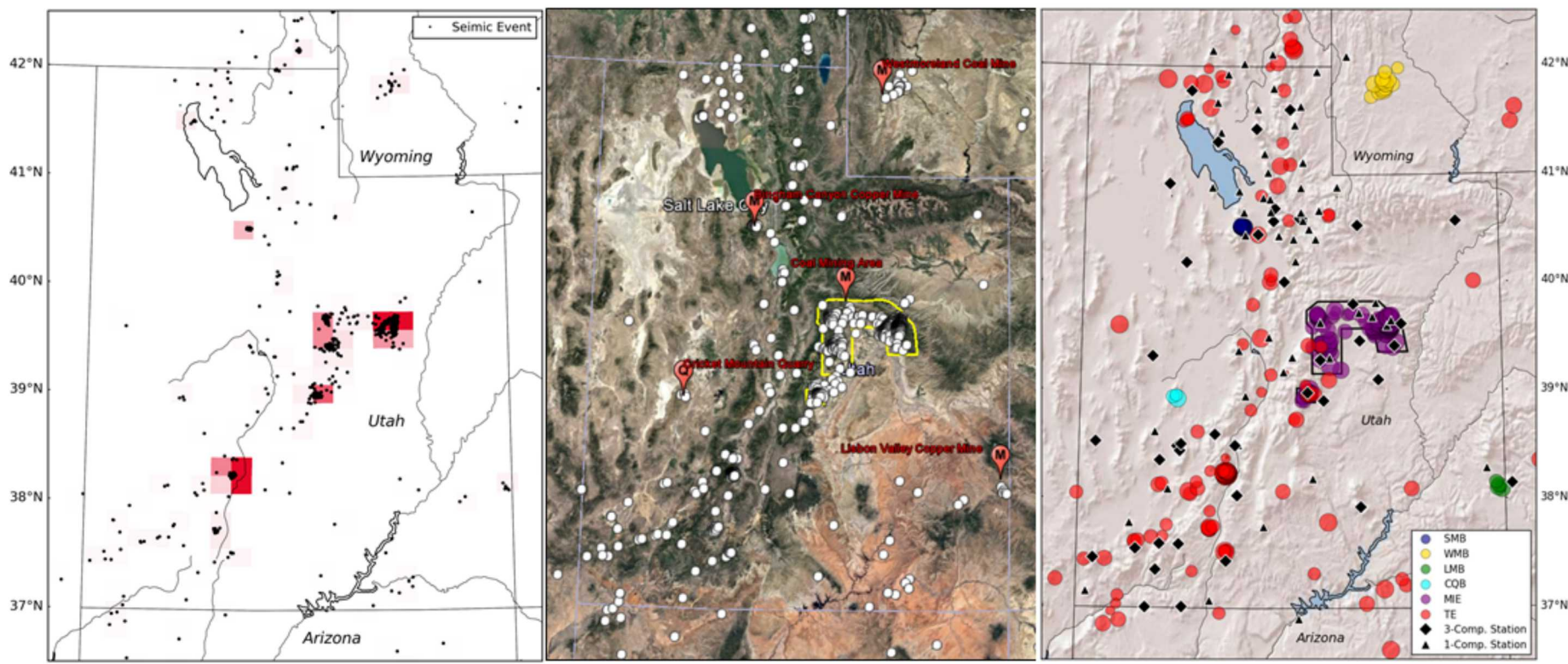




## OVERVIEW

The capability to discriminate low-magnitude earthquakes from low-yield anthropogenic sources, both detectable only at local distances, is of increasing interest to the event monitoring community. We used a dataset of seismic events in Utah recorded during a 14-day period (1–14 January 2011) by the University of Utah Seismic Stations (UUSS) network to perform a comparative study of event classification at local-scale using amplitude ratio (AR) methods and a machine learning (ML) approach. We compare the AR and ML methodologies using a broad set of criteria and conclude that a major advantage to machine learning methods is their robustness to low signal-to-noise ratio (SNR) data, allowing them to classify significantly smaller events.

## DATA

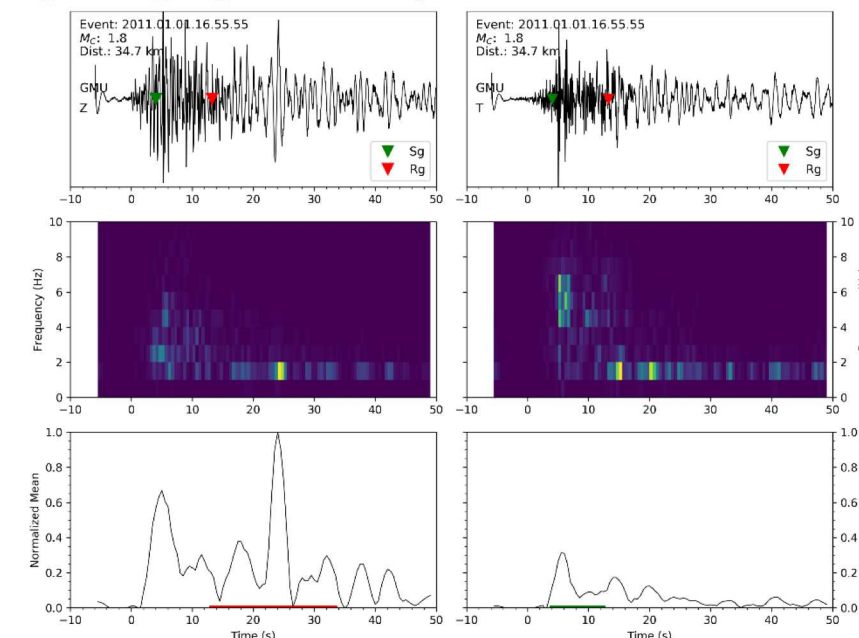


### Event Dataset:

- The Unconstrained Utah Event Bulletin (UUEB):
- Compiled by an expert analyst, who manually scanned through continuous seismic data recorded by the UUSS regional network from 1 to 14 January 2011.
  - Consists of 7,377 event within or around the state of Utah with  $M_c$  of  $\sim 2.0$  and lower up to 5.8. Data for  $\sim 58\%$  of the events have insufficient SNR. Hence their magnitudes could not be estimated. These events are not included in the calculation of the magnitude of completeness.
  - Six event categories identified based on the event locations:
    - 1,040 tectonic earthquakes (TEs) located mostly within the ISB
    - 6,286 mining-induced events (MIEs) in coal mining regions
    - 27 ripple-fired mining blasts from Bingham Canyon mine (SMBs)
    - 5 mining blasts from Lisbon Valley mine (LMBs)
    - 16 mining blasts from Westmoreland mine (WMBs)
    - 3 quarry blasts from the Cricket Mountain quarry (CQBs)

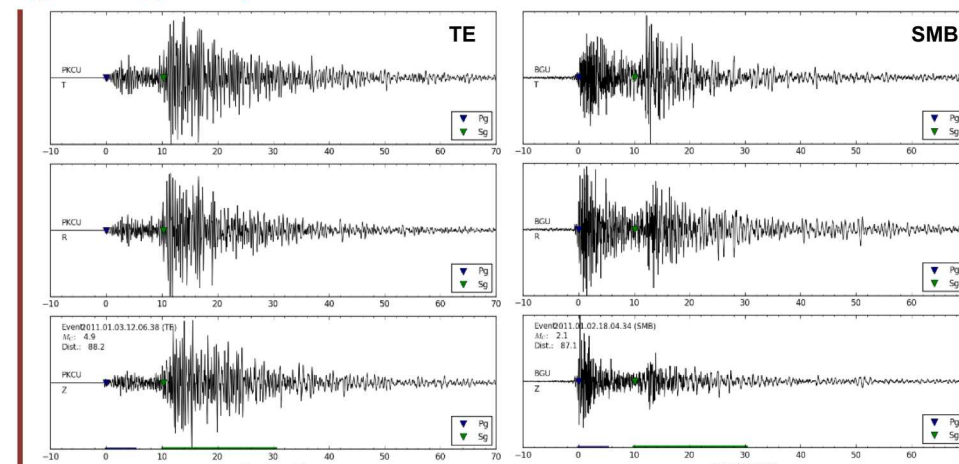
## METHODS

### Rg-to-Sg Spectral Amplitude Ratios



From the Z-component spectrogram, a mean time series is generated for the frequency range of 0.5–2 Hz. A similar time series is generated from the T-component spectrogram for the frequency range of 0.5–8 Hz. The time series are then smoothed. The maximum amplitude in the Rg window ( $\max\{Rg_{[0.5-2Hz]}\}$ ) of the Z time series is estimated. The same is done in the Sg window of the T time series to obtain ( $\max\{Sg_{[0.5-8Hz]}\}$ ). These amplitudes are then corrected for the propagation effects. The reported Rg-to-Sg ratios consists of the corrected  $\max\{Rg_{[0.5-2Hz]}\}$  divided by the corrected  $\max\{Sg_{[0.5-8Hz]}\}$ .

### Pg-to-Sg Amplitude Ratios



For each frequency in the range of 1–15 Hz in 1-Hz increment:  $A_{Pg} = (P_Z^2 + P_R^2)^{1/2}$ , where  $P_Z$  and  $P_R$  are rms of the amplitudes in the Pg window on the Z and R components, respectively;  $A_{Sg} = (S_Z^2 + S_R^2 + S_T^2)^{1/2}$ , whereby  $S_Z$ ,  $S_R$ , and  $S_T$  are the rms of the amplitudes in the Sg window on the Z, R and T components, respectively.  $A_{Pg}$  and  $A_{Sg}$  are then corrected for the propagation effects. The reported Pg-to-Sg ratios are obtained by dividing the corrected  $A_{Pg}$  by the corrected  $A_{Sg}$ .

To allow sufficient separation and avoid interferences between the phases, only data recorded at distances from 25 to 150 km were used for both Rg-to-Sg and Pg-to-Sg ratios.

## Multivariate Quadratic Discriminant Analysis

### Assumptions:

- $f_j(r)$  with  $j = 1, 2, \dots, N$  is the probability density associated with the  $j$ -th population, whereby  $r = (r_1, r_2, r_3, r_4, r_5)^T$  is the vector of amplitude ratios. The variables  $r_1$  to  $r_4$  are Pg-to-Sg ratios at 4 discrete frequencies, while  $r_5$  represents the Rg-to-Sg ratio. The characteristics of  $f_j(r)$  is inferred from the learning set.
- Amplitude ratios of the training sets are normally distributed within each population
- Events in the training sets are correctly classified.
- The  $N$  populations have equal prior probability of occurrence ( $\pi = 1/N$ ).
- The  $N$  populations have equal misclassification costs

The quadratic discriminant function,  $D_j(r)$ , is define as:

$$D_j(r) = -\frac{1}{2}(r - \mu_j)^T S_j^{-1} (r - \mu_j) - \frac{1}{2} \ln |S_j| + \ln \left( \frac{1}{N} \right),$$

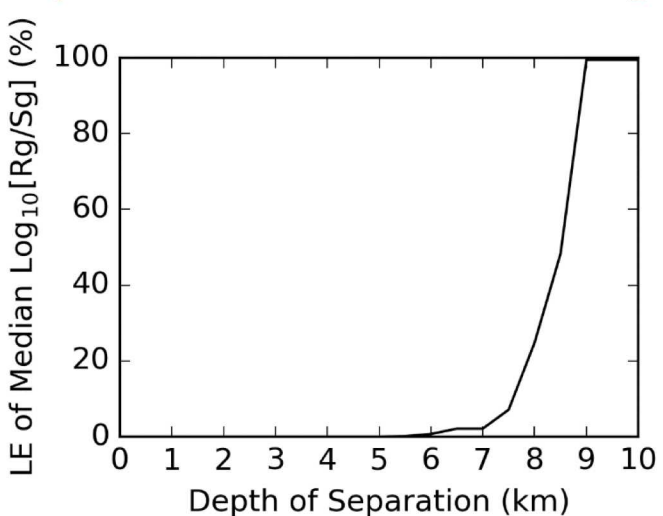
where  $\mu_j$  and  $S_j$  are the ratio vector mean and ratio covariance matrix of the learning set for the  $j$ -th population, respectively.

An event of interest with the ratio vector  $x$  is allocated to the  $i$ -th population if  $D_i(x)$  is the largest of the score values  $D_1(x), D_2(x), \dots, D_N(x)$ .

For  $N = 2$  (two populations  $p$  and  $q$ ), the event of interest is classified as  $p$ -type if the score difference  $d_{pq} = D_p(x) - D_q(x) > 0$ , and as  $q$  type if  $d_{pq} < 0$ .

## RESULTS

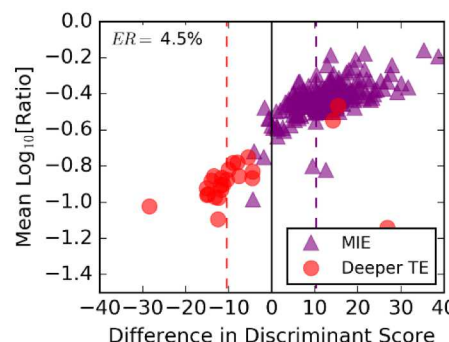
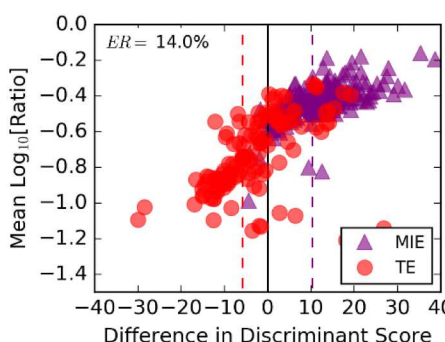
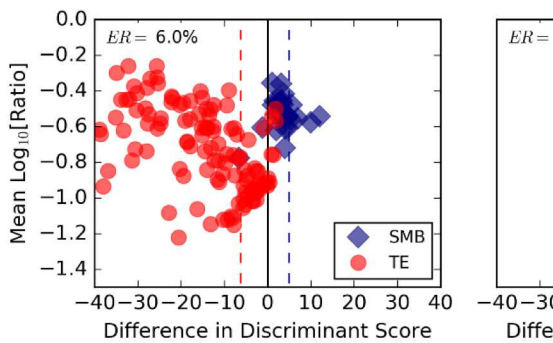
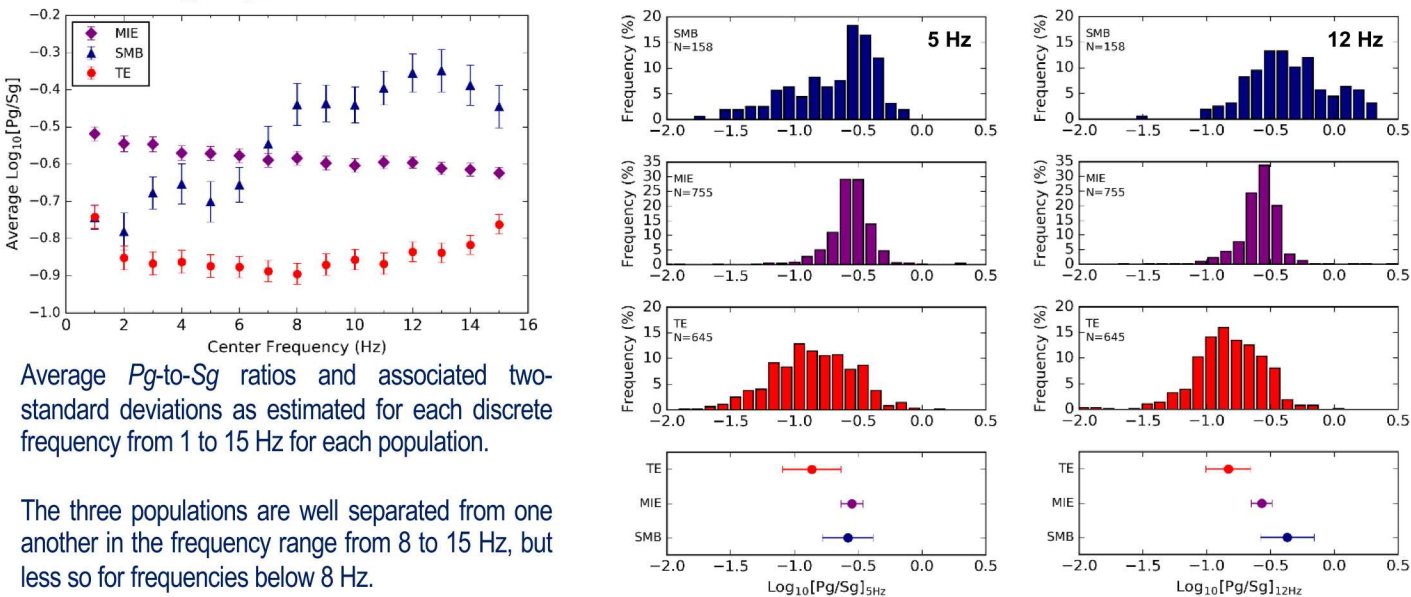
### Depth Discrimination Based on Rg-to-Sg Ratios



Likelihood of equality (LE, inferred from Mood's median tests) of the median Rg-to-Sg ratios as function of the depth of separation between shallow and deeper TEs.

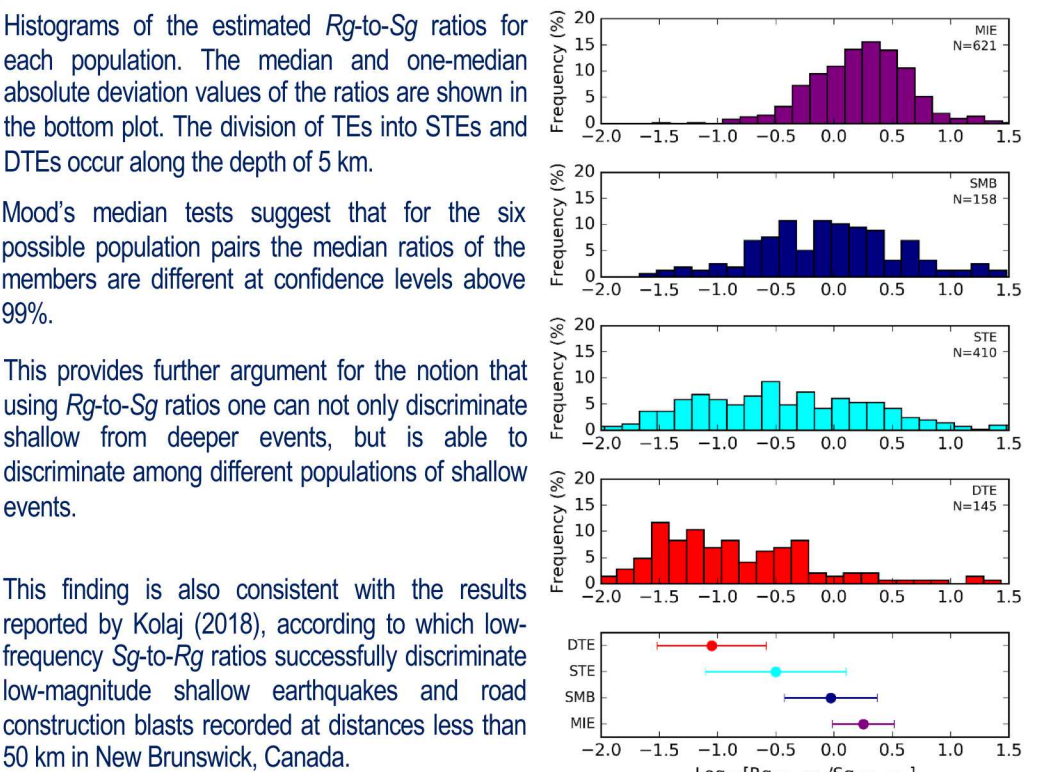
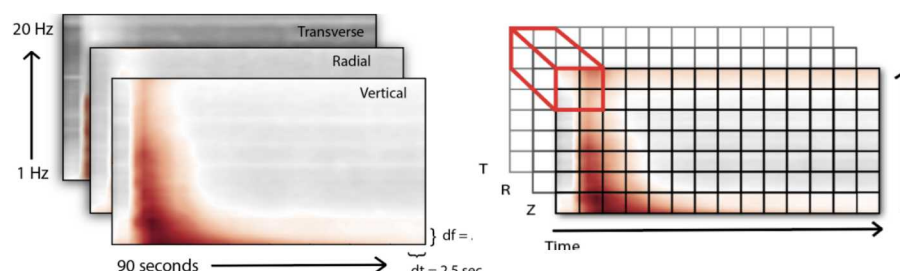
For the depths of separation of 6 km or less, the LE values are below 2%, implying that for any of those depths of separation shallow and deeper TEs are statistically different

### Two-Category, Pairwise Discrimination



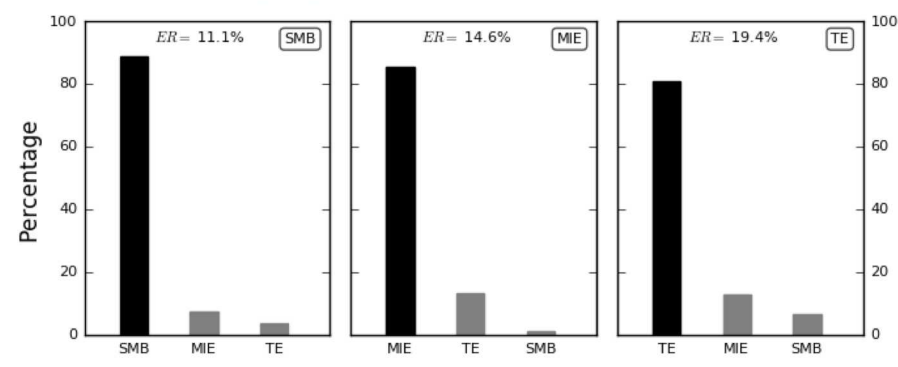
## Spectrogram-Based Machine Learning Method

- Input are 90-sec long spectrograms (starting 10 sec before first  $P$  arrivals) from 3-component (when available) or single local to near-regional stations
- Models were built using 5 years (2012–2016) of labeled UUSS events, except for the MIEs for which we used the current dataset
- We used the (VGG11) convolutional neural network (CNN) architecture, that involves between 64 and 512 filters for each layer and includes batch normalization and max pooling with ReLU non-linearity
- Our hyperparameter optimization relied on extensive testing from previous studies that relied on the UUSS dataset
- We used 10 fold cross validation and early stopping
- Our models trained between 20 and 80 epochs



This finding is also consistent with the results reported by Kolaj (2018), according to which low-frequency Sg-to-Rg ratios successfully discriminate low-magnitude shallow earthquakes and road construction blasts recorded at distances less than 50 km in New Brunswick, Canada.

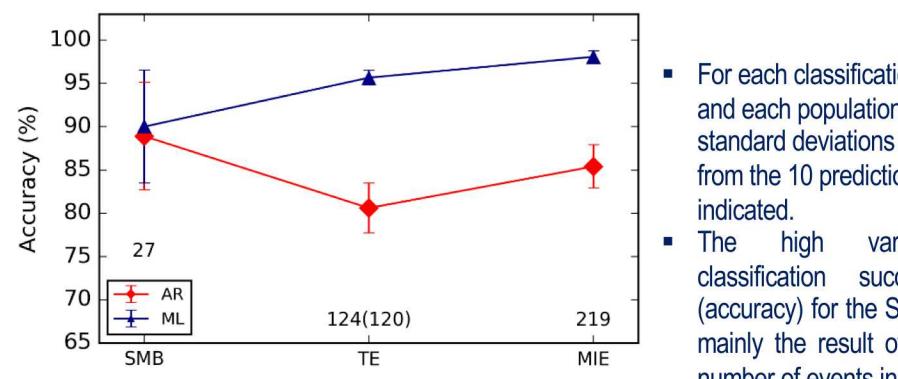
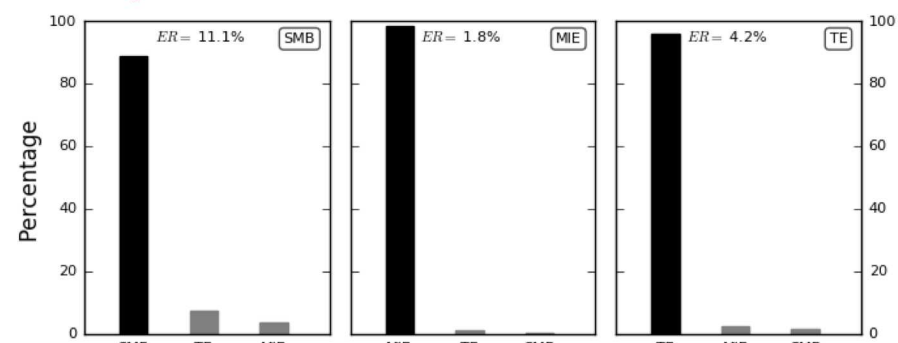
## Three-Category Classification Using the AR Method



Predicted Class	Actual Class		
	SMB	MIE	TE
SMB	24	3	8
MIE	2	187	16
TE	1	29	100

Confusion matrix: The diagonal elements indicate the number of events classified correctly (true positives).

## Comparison of the AR with the ML Method



- For the SMB population the performance of the AR method is comparable with that of the ML approach within the margin of errors.
- For the TE and MIE groups, however, the latter method outperforms the former by an average of about 14% in terms of success rate.

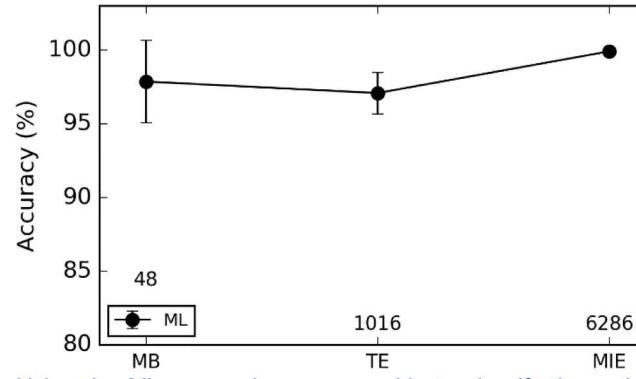
- All three populations are considered simultaneously in the QDF approach.
- The optimum frequency set for Pg-to-Sg ratios is 1, 2, 7, and 8 Hz.
  - On average about 85% of the events are classified correctly.
  - The population of SMBs is associated with the lowest error rate (ER = 11.1%) followed by the MIEs (14.6%). The TE group exhibits the highest error rate of any population (19.4%).
  - The majority of the misclassified TEs are assigned to the MIE group. Similarly, most of the misclassified MIEs are assigned to the TE population. This is consistent with the outcome of the two-category classification discussed above, which suggests that the two populations have some properties in common, which make it difficult to discriminate between them.

3-category classification using the ML approach.

Predicted Class	Actual Class		
	SMB	MIE	TE*
SMB	24	1	2
MIE	1	215	3
TE	2	3	115

Confusion matrix for the ML method. The reported values represent averages from 10 prediction runs.

\* Note that in this case only 120 TEs were investigated, compared with 124 TEs for the AR approach.



Using the ML approach, we were able to classify the entire UUEB dataset, including the abundant, extremely low-magnitude events. In this case, the SMBs, WMBs, LMBs, and CQBs were grouped together to form a class called "mining blast" (MB). We achieved success rates of  $\sim 97$ –99%.

## CONCLUSIONS

	AR Method	ML Method
Advantages	<ul style="list-style-type: none"><li>Require only limited number of learning events for each category</li><li>Fast computation</li><li>Physical basis well understood (i.e., energy partitioning between specific phases)</li></ul>	<ul style="list-style-type: none"><li>Achieve high accuracy (<math>\geq 90\%</math>)</li><li>Can classify extremely low-magnitude events</li><li>Fast to apply the model once it has been built</li></ul>
Limitations	<ul style="list-style-type: none"><li>Achieve moderate accuracy (<math>\sim 80</math>–<math>90\%</math>)</li><li>Require high-quality data</li></ul>	<ul style="list-style-type: none"><li>Require large dataset (100s–1000s) of labeled training events for each category</li><li>Computationally intensive to build the model</li><li>Lack of insight into the physical basis</li></ul>

- Using the same set of events that were well-recorded at local distances by the UUSS network, a traditional method of event classification in which amplitude ratios are exploited in the QDFs is compared with a spectrogram-based machine learning approach.
- With the AR method, we achieve classification success rates of about 80–90%.
- The ML approach uses convolutional neural network models to classify the populations, and achieves success rates of 90% and higher.
- The ML method is more robust to low SNR data, allowing it to classify extremely low-magnitude events.
- The complex algorithms involved in the ML method are able to expose and exploit characteristics that are specific to each event population to the level that the traditional AR approach cannot, allowing ML to achieve higher accuracies and classify significantly smaller events.
- The lack of insight into the physical basis for ML classifications has traditionally been a major reason why people have been reluctant to use ML methods. SNL intends to work on this problem.

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