

12 December 2018

# Dynamic Loading Response of $\text{CaF}_2$ under Shock and Shockless Compression

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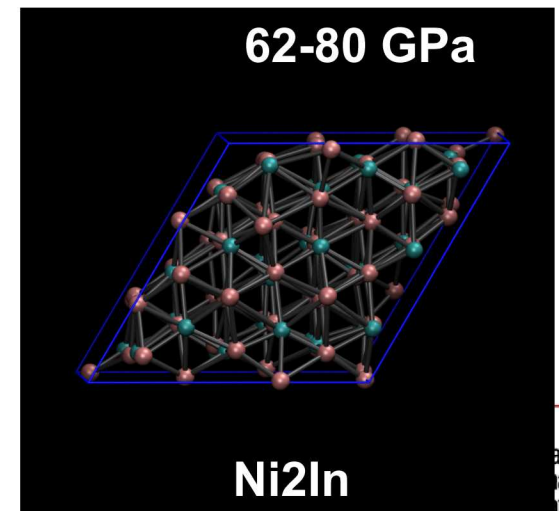
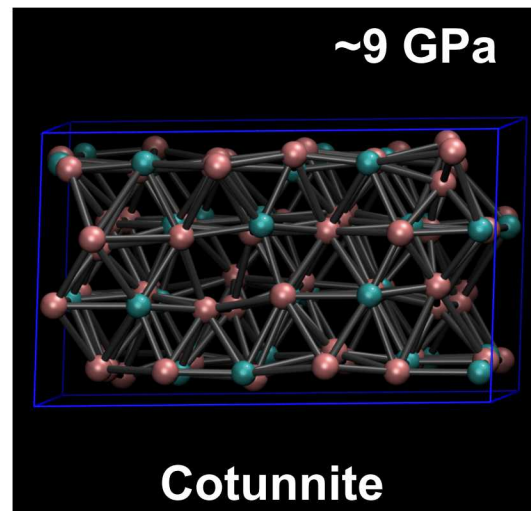
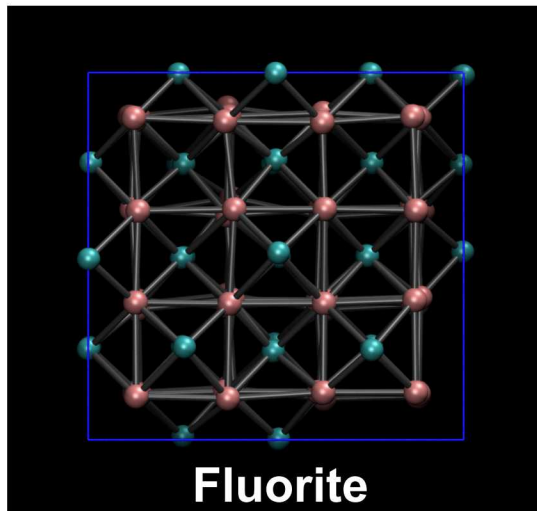
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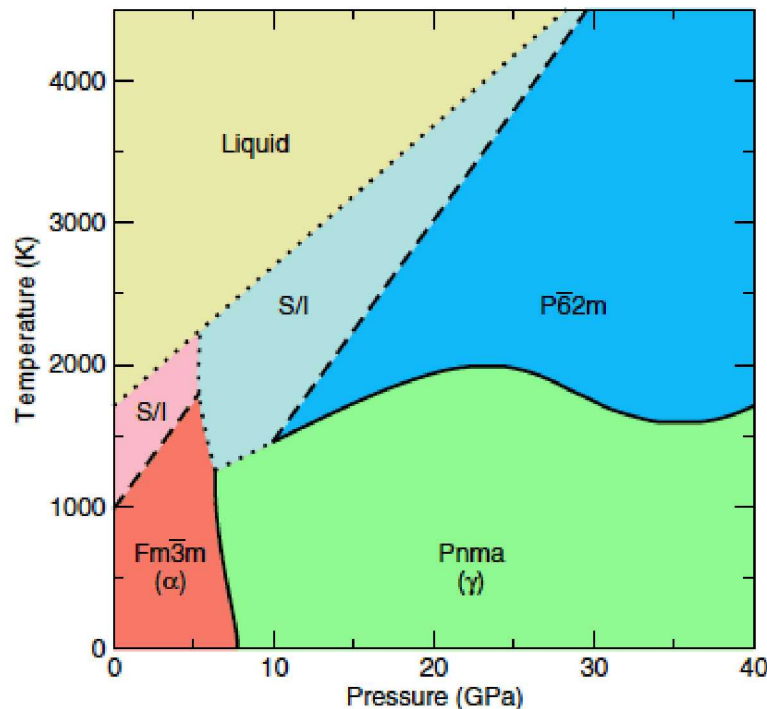
# Calcium Fluoride

- The fluorite structure and associated pressure-induced transitions are common to many compounds
- At ambient conditions, Calcium Fluoride ( $\text{CaF}_2$ ) crystallizes into the fluorite structure
- Static compression at ambient temperatures shows two solid-solid phase transitions: fluorite  $\rightarrow$  cotunnite  $\rightarrow$   $\text{Ni}_2\text{In}$
- $\text{CaF}_2$  has an orientation dependent elastic behavior
- $\text{CaF}_2$  samples are cheap, well-characterized, and easy to acquire in multiple orientations

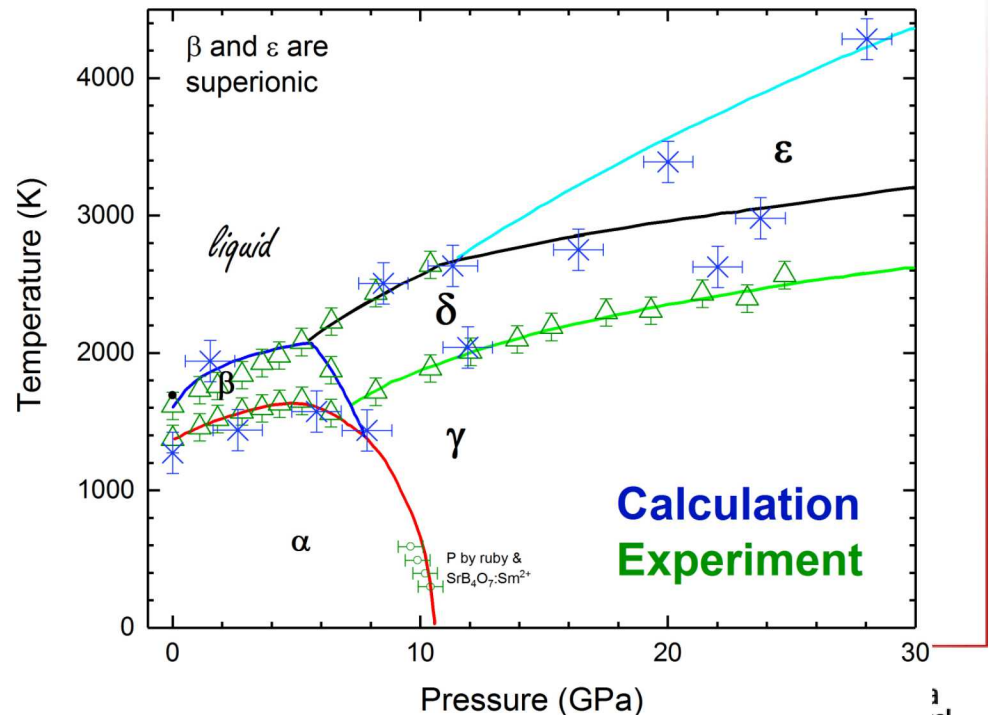


# CaF<sub>2</sub> Phase Diagram

- Extended phase diagram is undetermined determined
- Phase diagrams determined using QMD combined with limited static compression work below 30 GPa and elevated temperatures
- Both suggest two super ionic phases and a high P-T phase
- The high P-T phase does not correspond to the Ni<sub>2</sub>In phase
- Location and range of the Ni<sub>2</sub>In phase is unknown



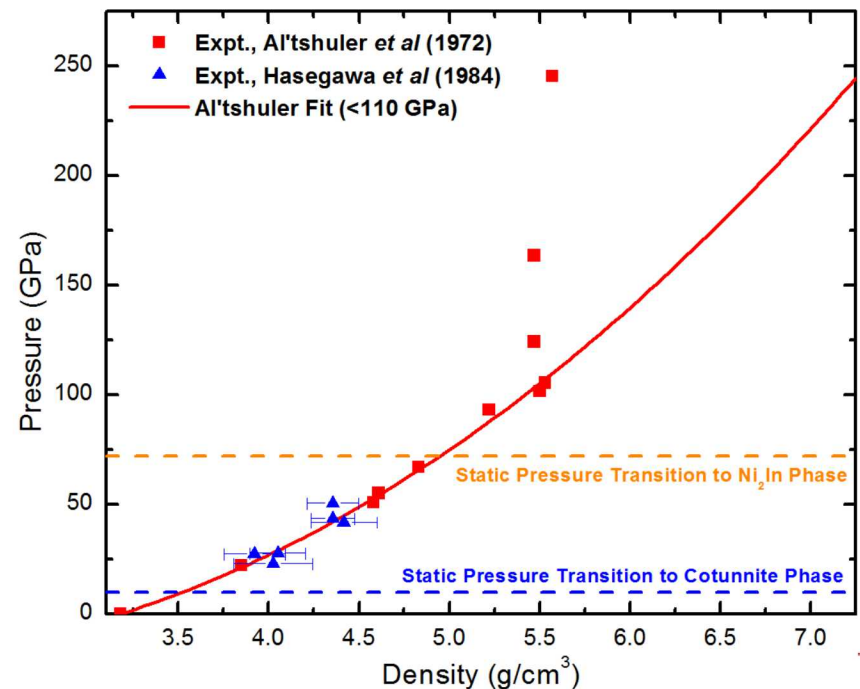
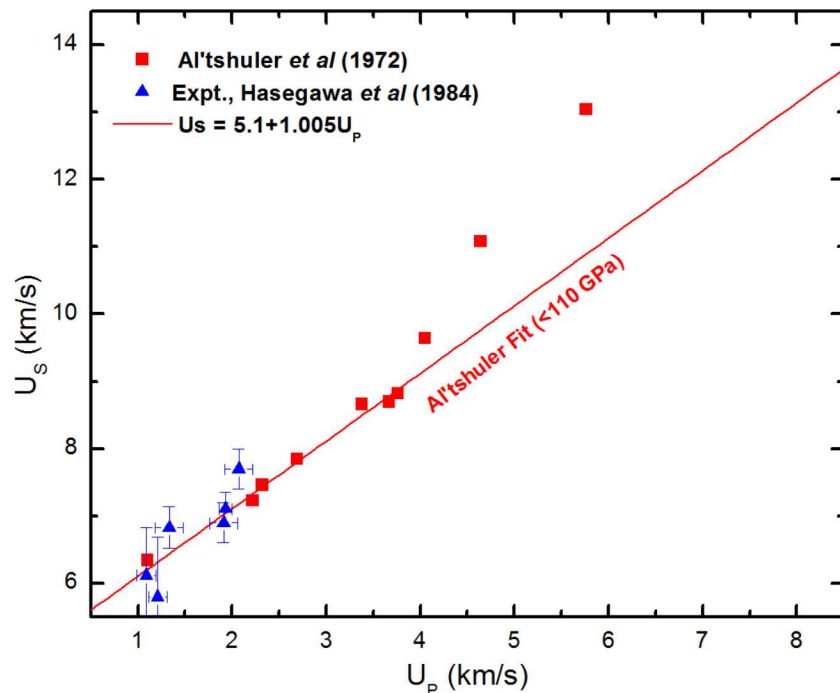
J. R. Nelson *et al*, PRB **95**, 054118 (2017)



C. Cazorla and D Errandonea, PRL **113**, 235902, (2014)

# Prior Shock Compression Work

- Observation of fluorite  $\rightarrow$  cotunnite phase along Hugoniot in wave profile<sup>1</sup> and x-ray diffraction<sup>2</sup> experiments ( $\sim 12$  GPa)
- Al'tshuler *et al* measured the Hugoniot to 250 GPa (no uncertainties listed)
- Monotonic increase to 100 GPa, but becomes highly incompressible above 100 GPa
- They attributed the incompressibility to F-F repulsion



1. T. Sekine and T. Kobayashi, **Phys. Chem. Minerals** **38**, 305 (2011)
2. P. Kalita *et al*, **Phys. Rev. Lett.** **119**, 255701 (2017)

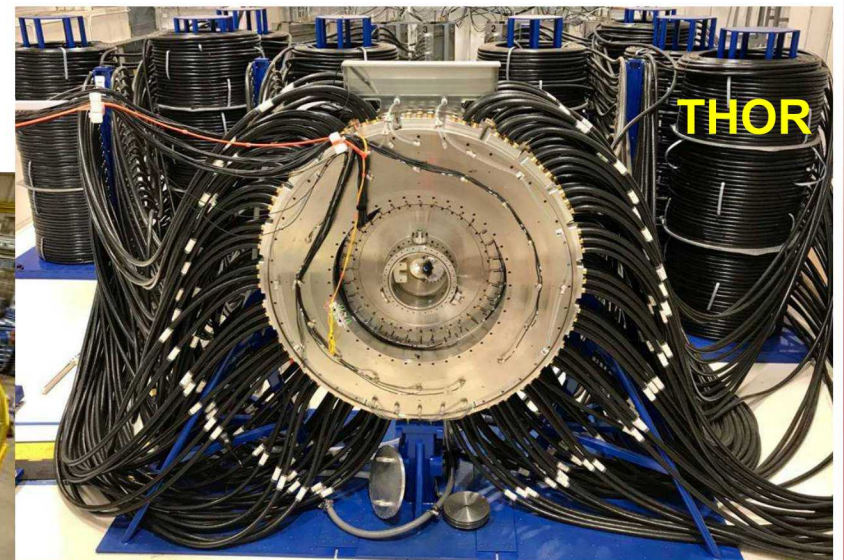
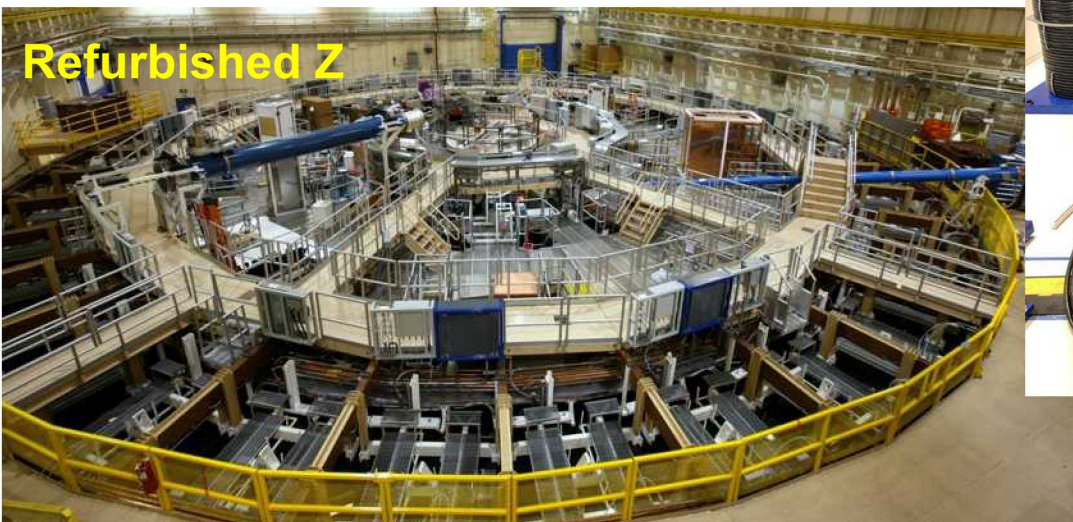
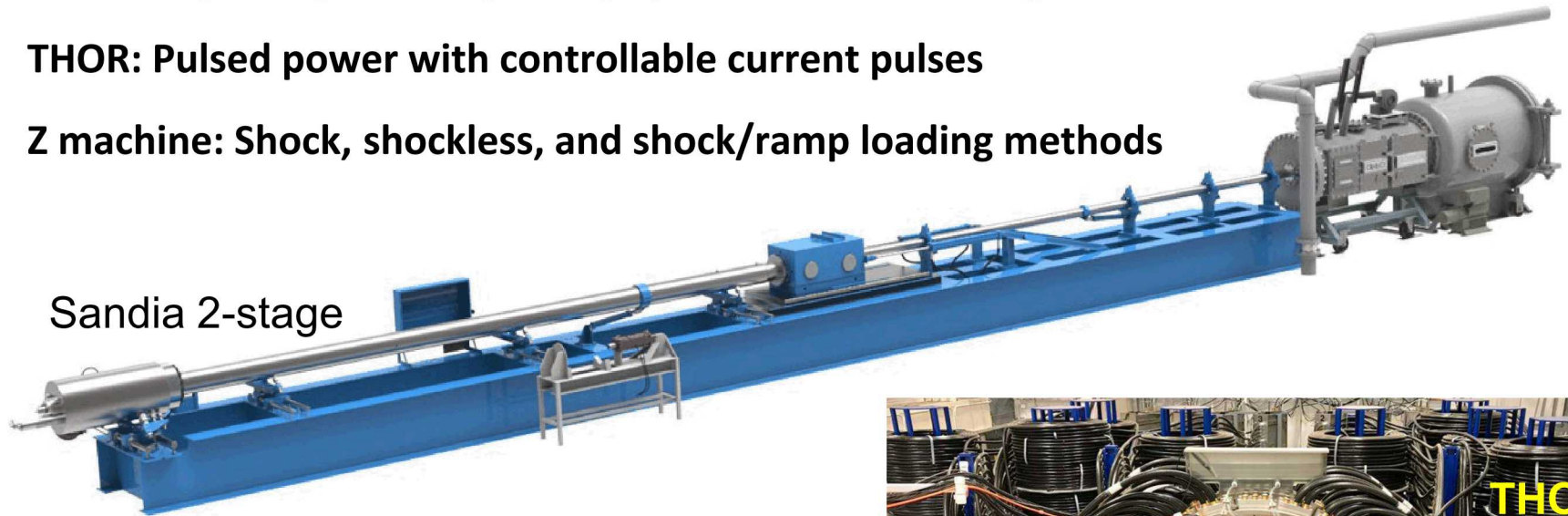


# Collaboration Objectives

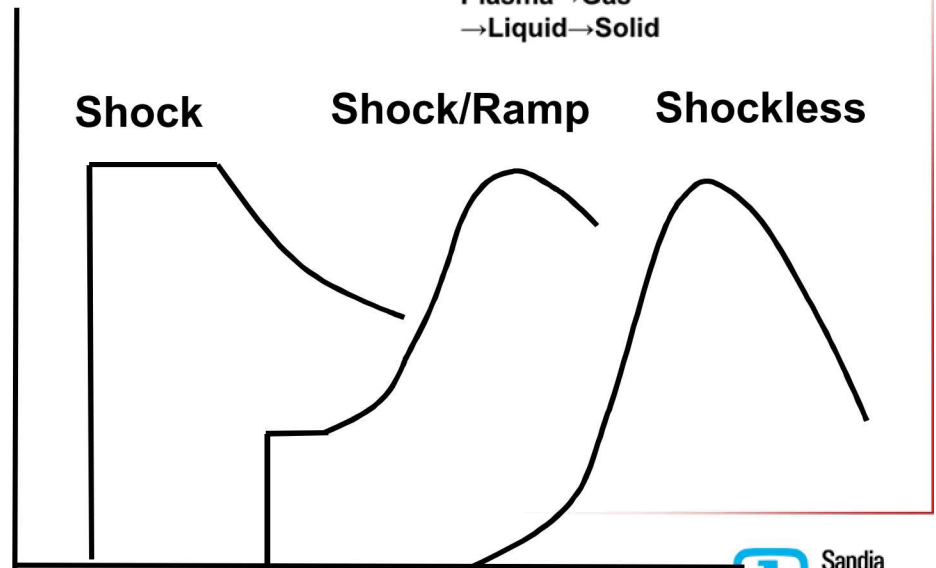
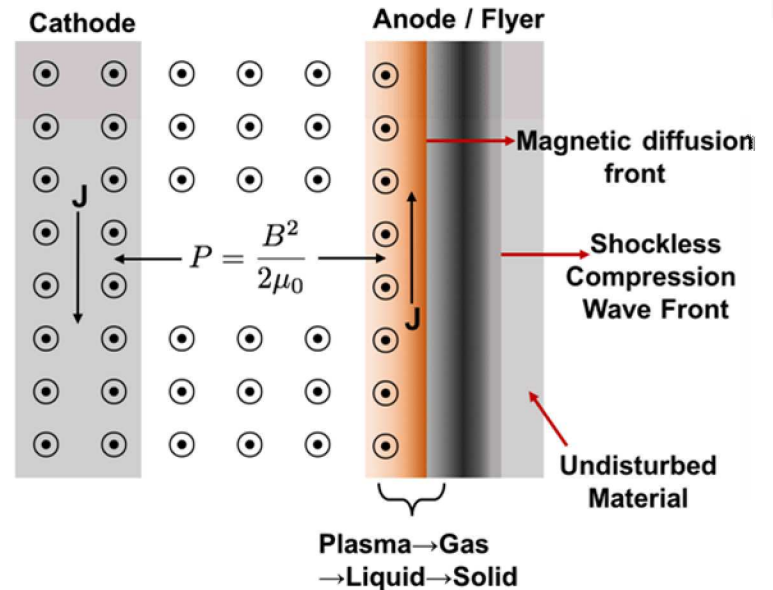
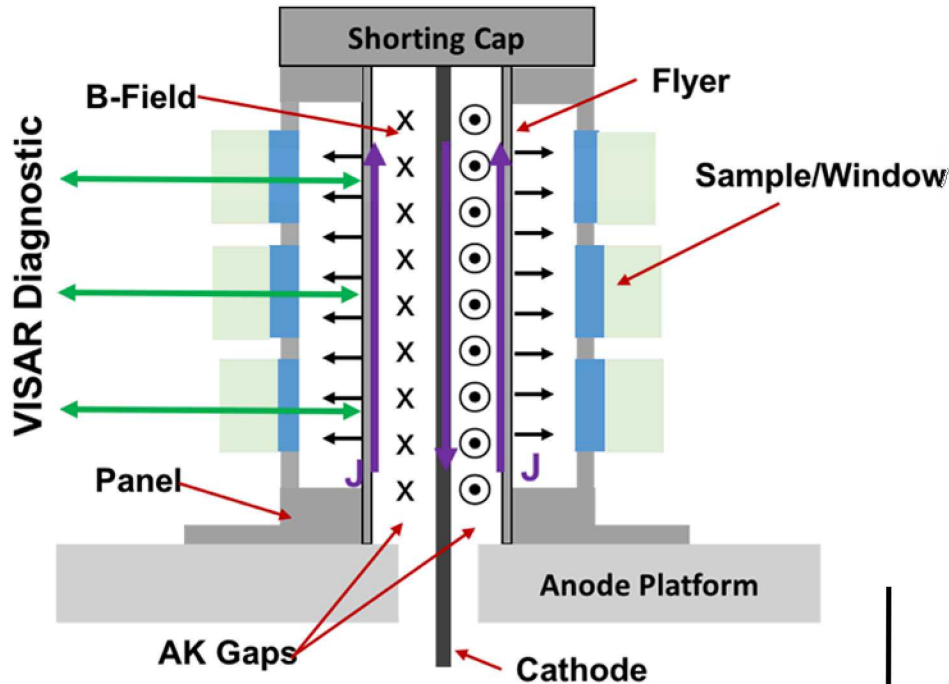
- **Develop a data-driven, multiphase equation of state**
  - Understand phase diagram over a broad range of pressure and temperature
  - Understand the kinetics of the phase transitions
  - Using shock, shock-ramp, shockless, static compression methods
  - Using density functional theory methods
- **Develop or validate a constitutive model**
  - Examine the dynamics of the constitutive response
  - Orientation, temperature, loading rate dependencies
  - Using shock and shockless compression methods

# Sandia's Experimental Platforms

- Guns: Single stage air, single stage powder, and two-stage launchers
- THOR: Pulsed power with controllable current pulses
- Z machine: Shock, shockless, and shock/ramp loading methods



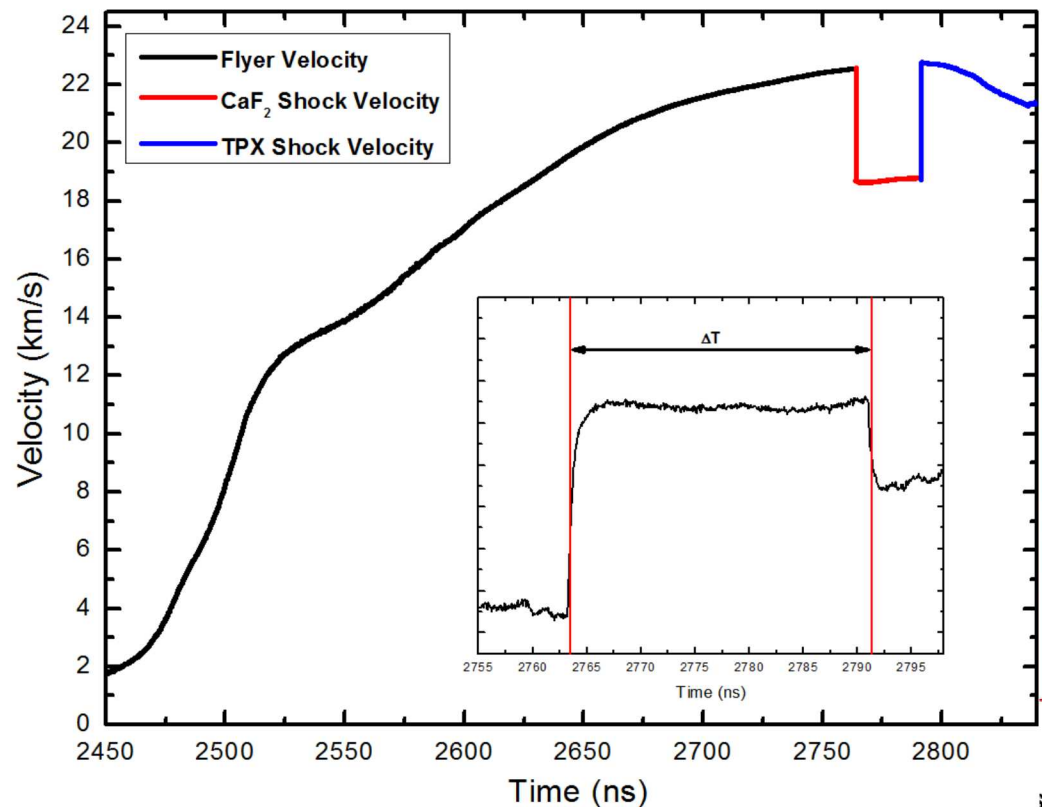
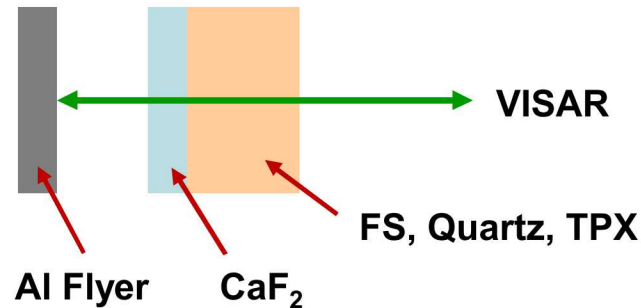
# Z Machine



- Shock compression with flyers
  - Up to 45 km/s
- Shockless Compression
  - Quasi-isentropic loading
- Samples are 100s of  $\mu\text{m}$  to a few mm

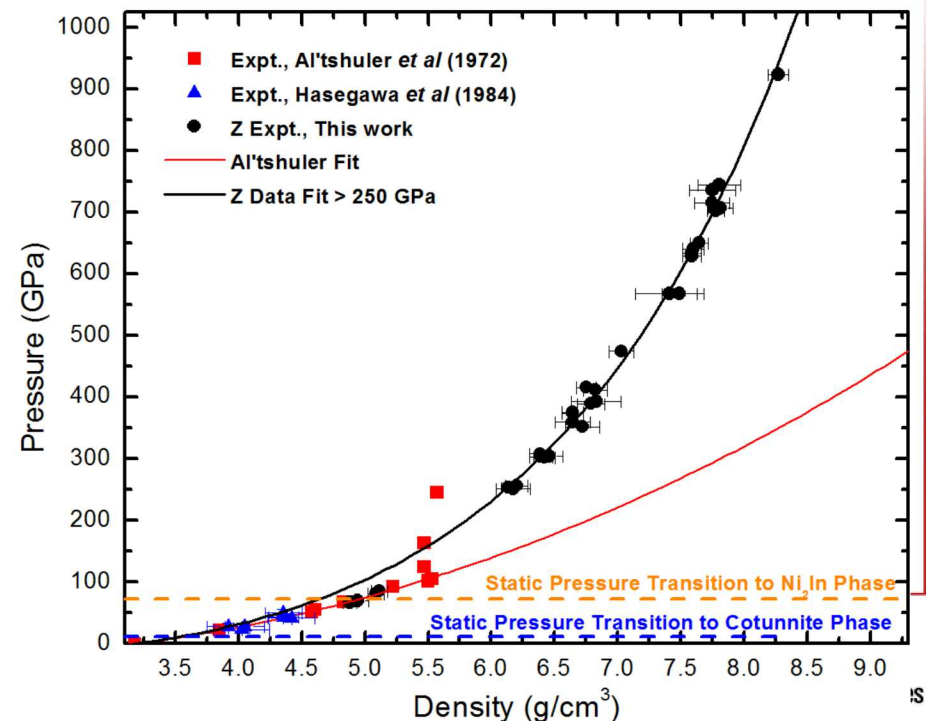
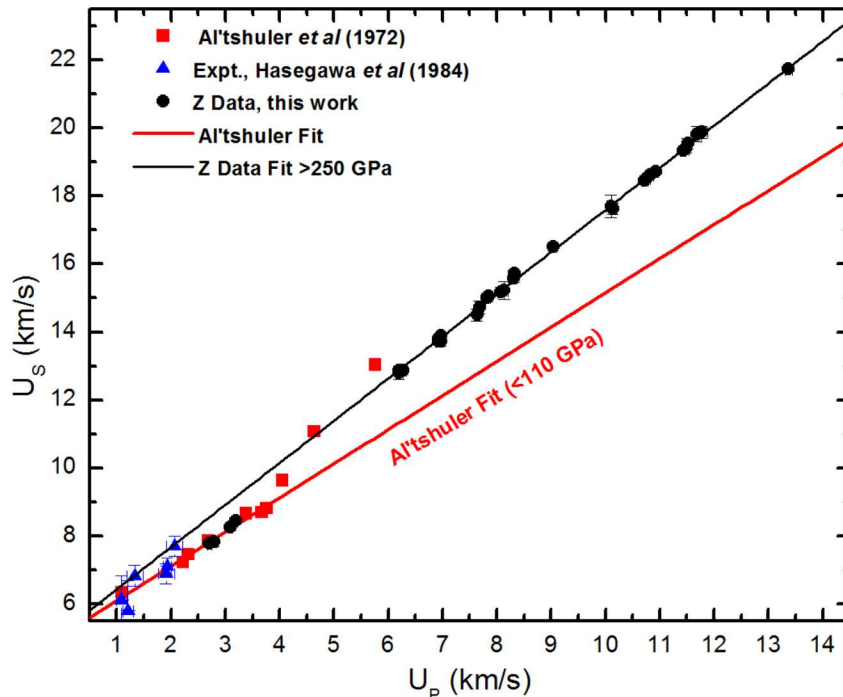
# Z Experiments Along the Hugoniot

- Single crystal  $\text{CaF}_2$  [111]
- Initial density =  $3.18 \text{ g/cm}^3$
- $\text{CaF}_2$  backed by various windows for release measurements
- Z machine shocklessly accelerate Aluminum flyers
- Generating steady shocks in  $\text{CaF}_2$
- At impact velocities  $< 18 \text{ km/s}$  the shock front is not reflective
- VISAR measures impact velocity, shock velocities and transit times



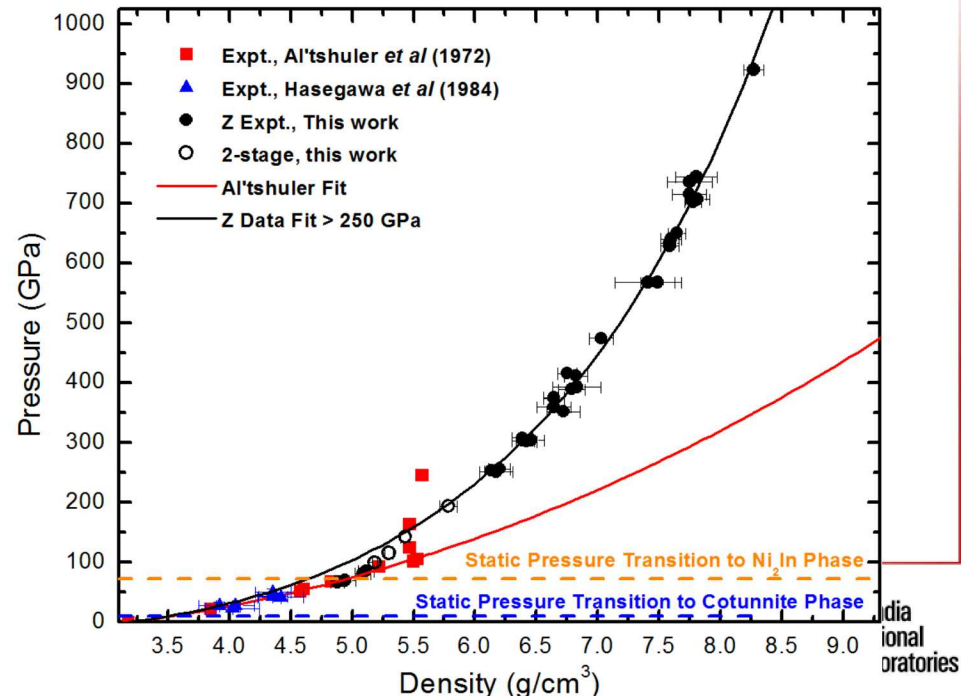
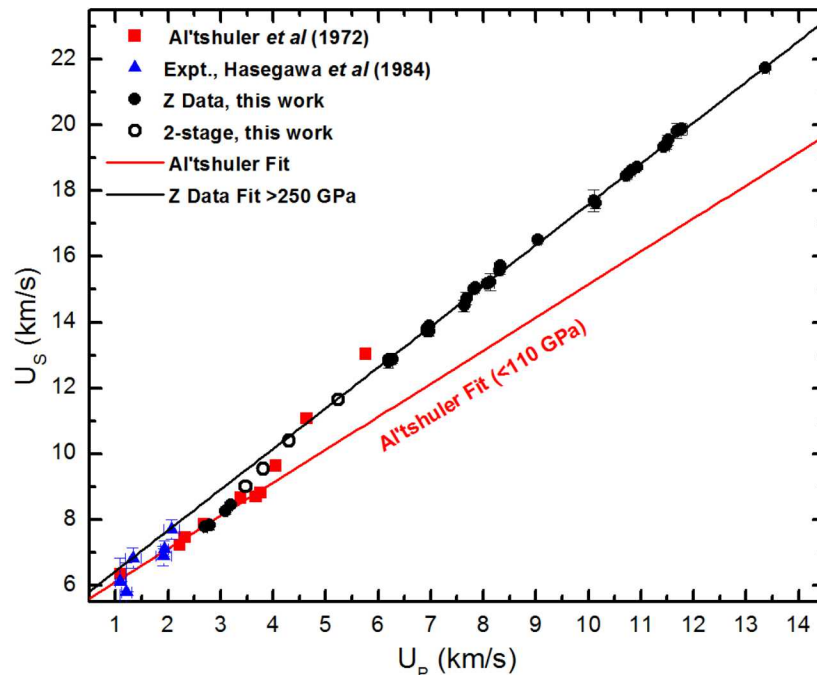
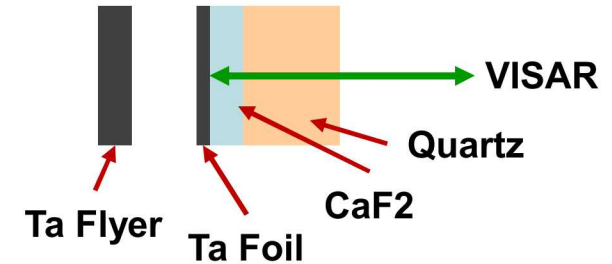
# Z Experimental Results

- Measured the Hugoniot from 250 GPa to 950 GPa
- One shot at 65 – 85 GPa – consistent with Al'tshuler data below 100 GPa
- Hugoniot determined using *Monte Carlo* impedance matching
- Data show a monotonically increasing trend above 250 GPa
- Data deviate from the <110 GPa Al'tshuler fit
- Data are not consistent with the observed incompressible behavior



# Two-Stage Experimental Results

- Two-stage experiments using Ta impactors and [111] CaF<sub>2</sub>
- Impact velocities from 4.7 km/s to 7 km/s
- Transit time measurement with *Monte Carlo* impedance matching to Ta
- Higher pressure data (~200 GPa) consistent with the Z data
- Data between 100 GPa and 150 GPa show a slope change suggesting a phase transition



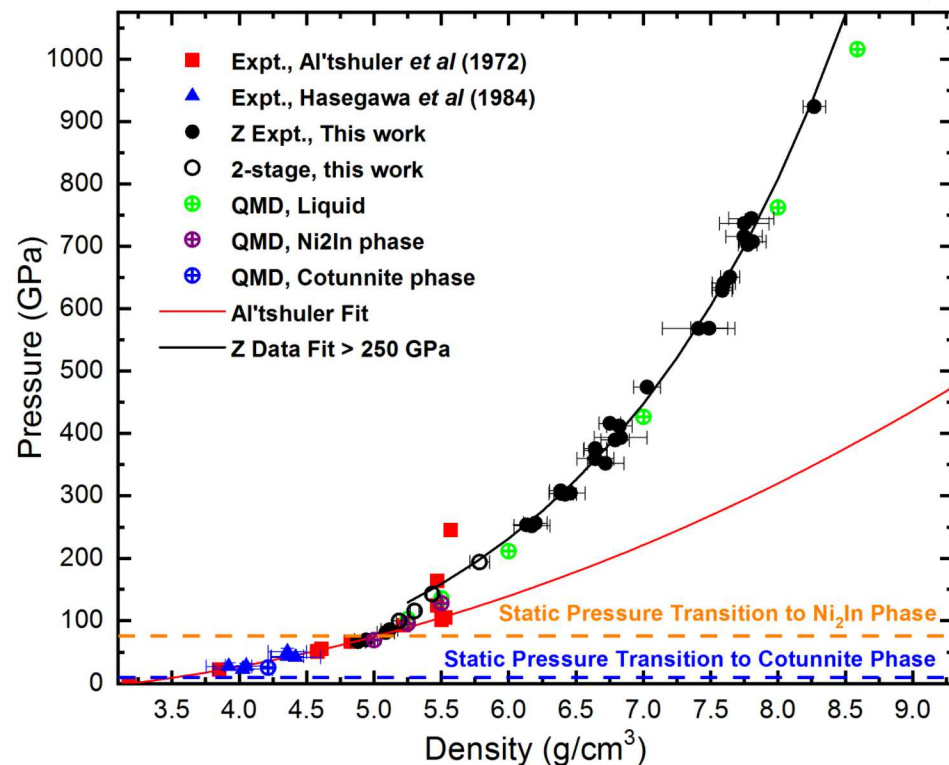
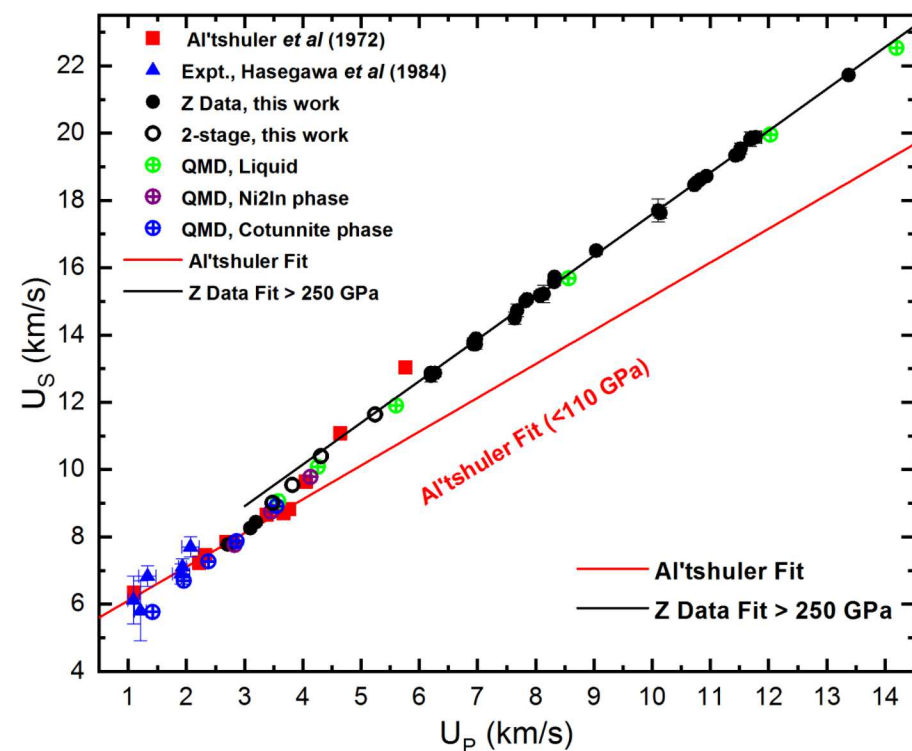
# Density Functional Theory Simulations

- **Use DFT-MD to assess the  $\text{CaF}_2$  Hugoniot at high pressures and temperatures**
- DFT-MD simulations performed using VASP 5.4.1\*
- Electronic states occupied according to Mermin's finite-temperature formulation
- Calculate energy and pressure for a given density and finite temperature
- Satisfy the Hugoniot Condition:  $2(E - E_{ref}) - (P + P_{ref})(v_{ref} - v) = 0$
- **Atoms/Simulation: Fluorite, Cotunnite, and Liquid = 96;  $\text{Ni}_2\text{In}$  = 108**
- **PBEsol exchange correlation functional**
- **Energy cutoff is 900eV**
- **Checked for convergence: number of atoms, energy cutoff, etc**
- **VASP PAW potentials: Ca\_sv\_GW\_31Mar2010 (10e-), F\_GW\_19Mar2012 (7e-)**

\* G. Kresse and J. Hafner, Phys. Rev. B **47**, 558 (1993) and Phys. Rev. B **49**, 14251 (1994).

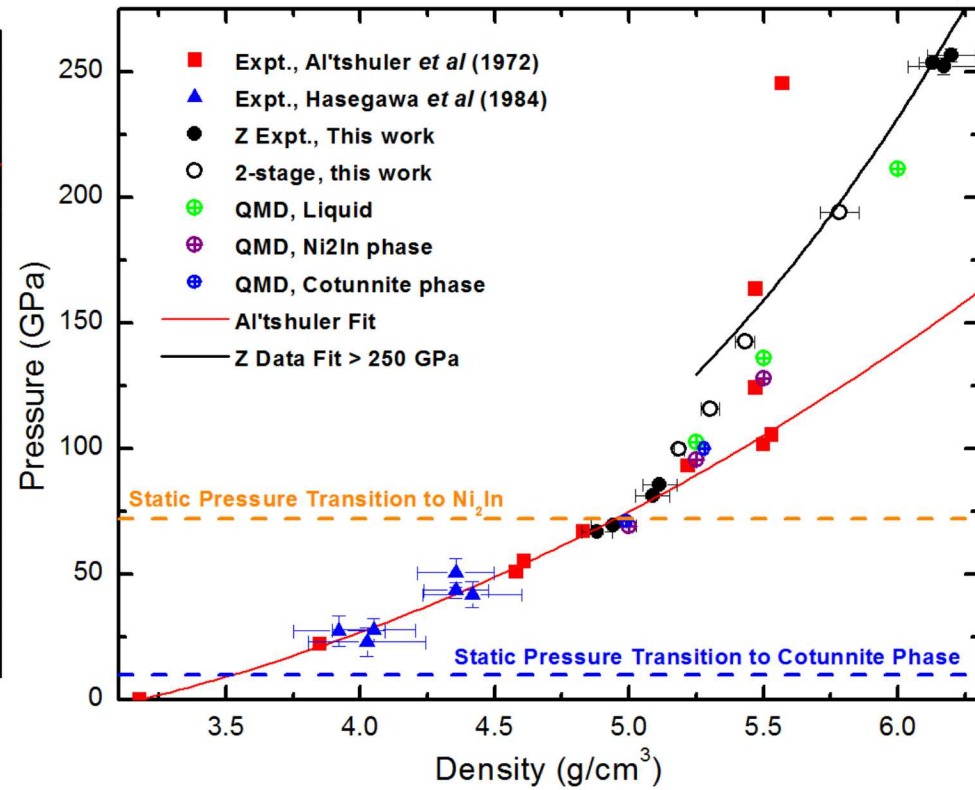
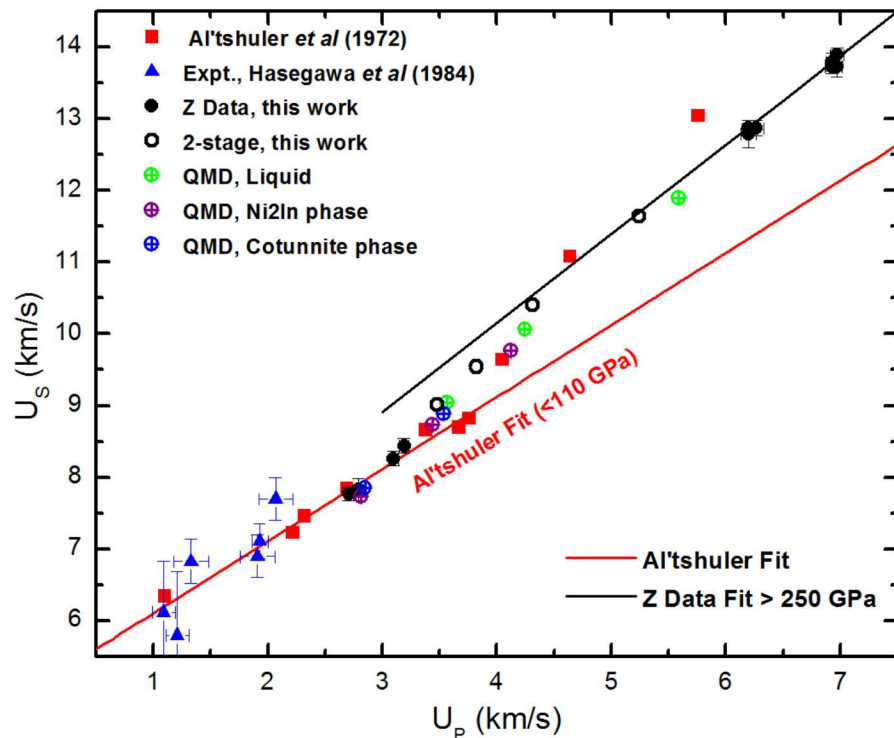
# DFT Results and Comparison

- DFT Liquid Hugoniot is consistent with the Z data above 200 GPa
- DFT simulations do not show Al'tshuler incompressibility
- Simulations on the liquid are consistent with the slope change between 100 GPa and 150 GPa
- Simulations on  $\text{Ni}_2\text{In}$  phase are also consistent
- Cotunnite simulations melt at a density of  $5.5 \text{ g/cm}^3$



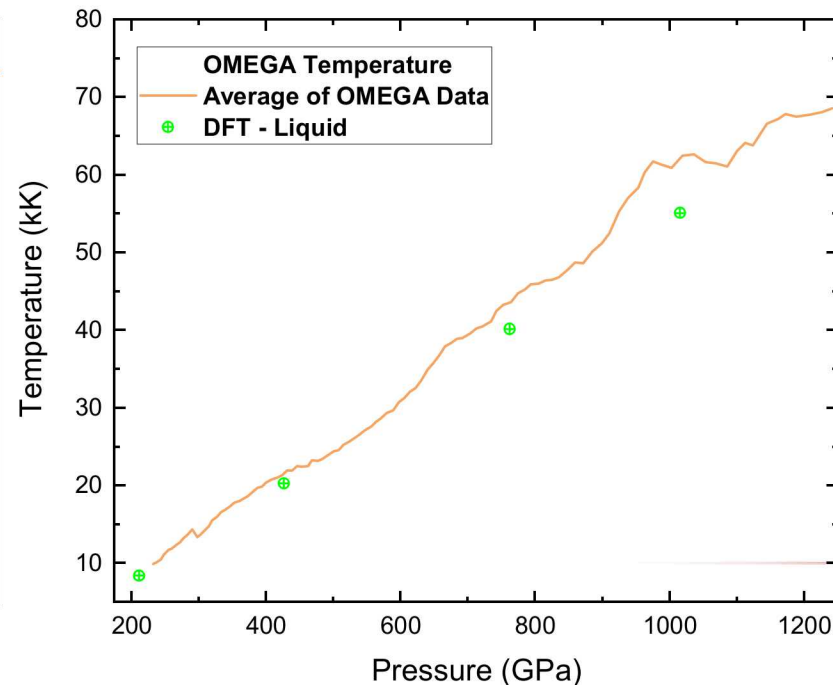
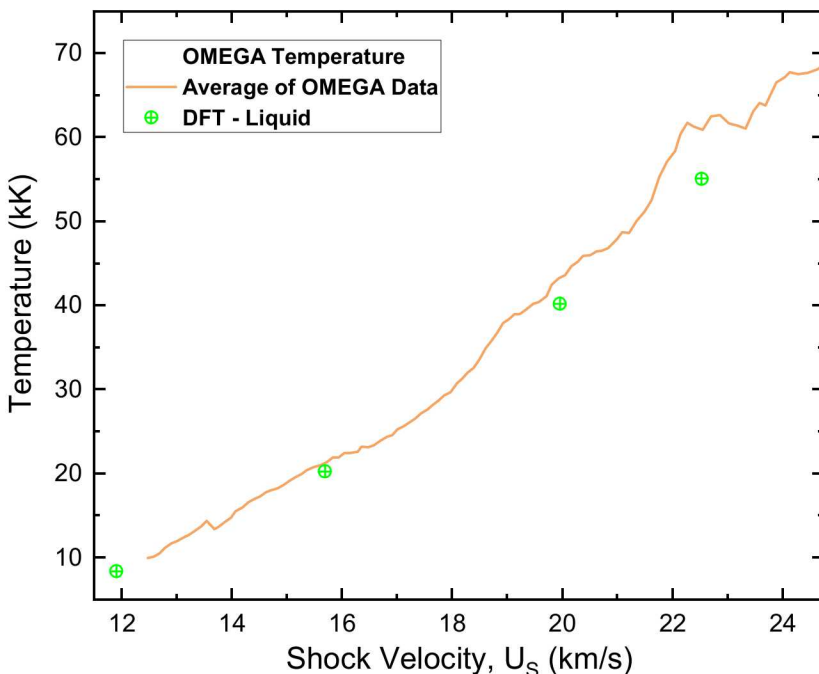
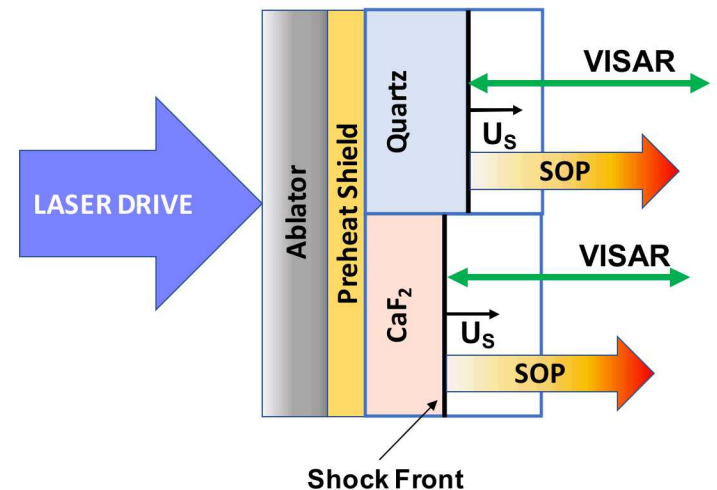
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- Cotunnite simulations melt at a density of  $5.5 \text{ g/cm}^3$
- $\text{CaF}_2$  is likely melting, but further work is needed



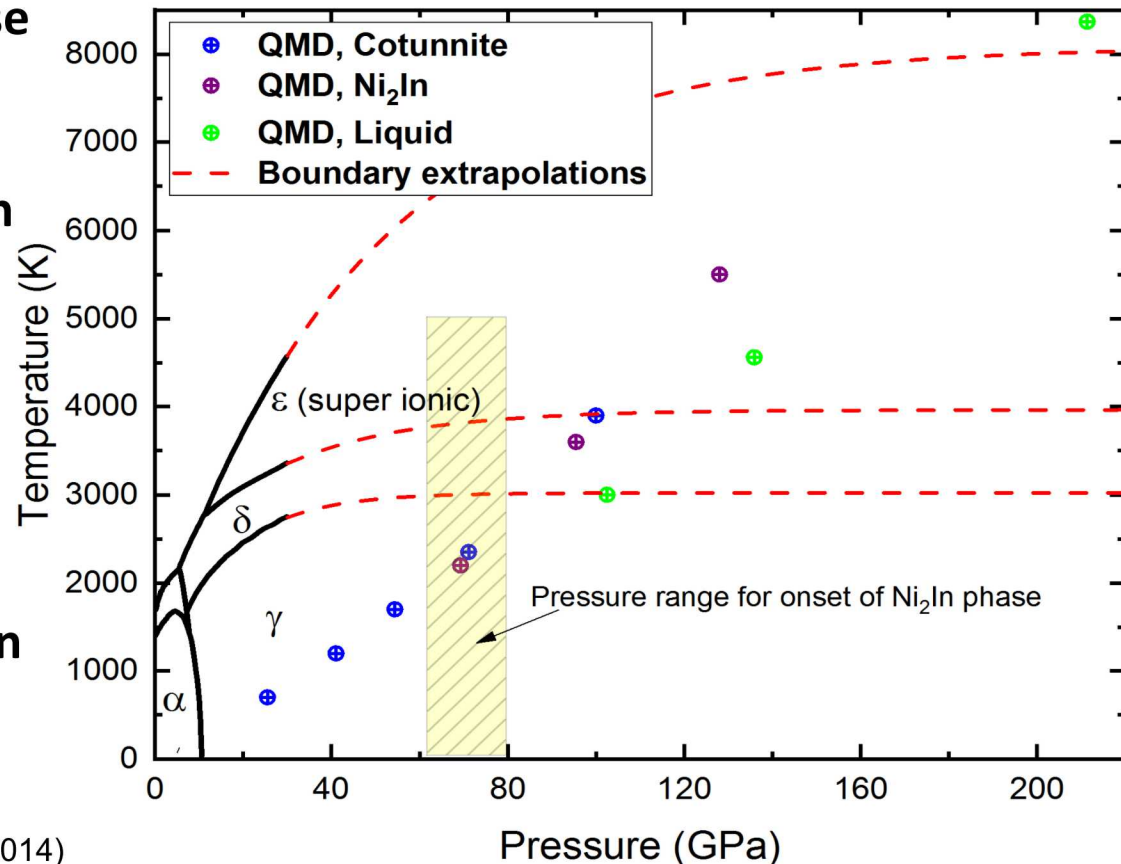
# Hugoniot Temperatures

- Z has temperature measurement capability
- Hugoniot temperature easily measured using decaying shocks at OMEGA facility
- The QMD provides temperature automatically
- QMD and OMEGA temperatures are in good agreement



# Calcium Fluoride Phase Diagram

- The extended phase diagram is unknown
- Both Carzola and Nelson predict a high pressure, high temperature phase  $\delta$
- Both Carzola and Nelson predict a super-ionic phase
- Dorfman's results show a high pressure phase starting around 62 GPa
- Comparison of QMD and phase boundary extrapolations suggest the melt boundary is lower than Carzola and Nelson predict
  - Extrapolations are not unique
- Range of the  $\delta$  phase is undetermined
- Location and range of the  $\text{Ni}_2\text{In}$  phase are undetermined

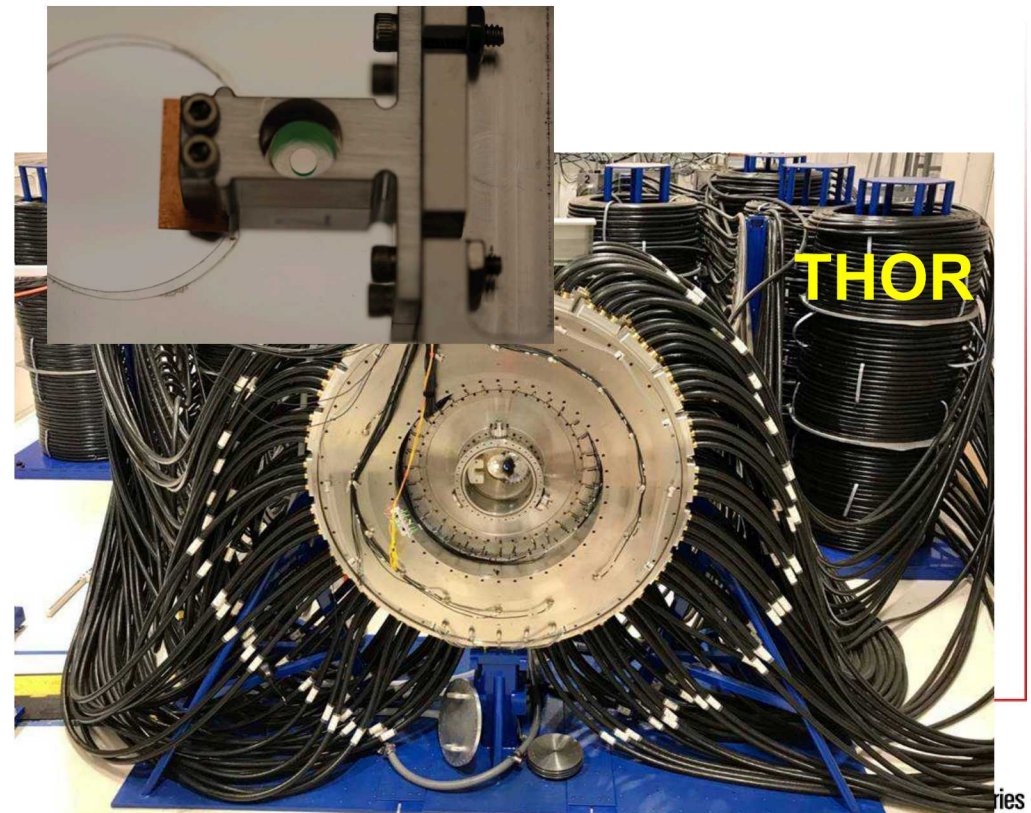
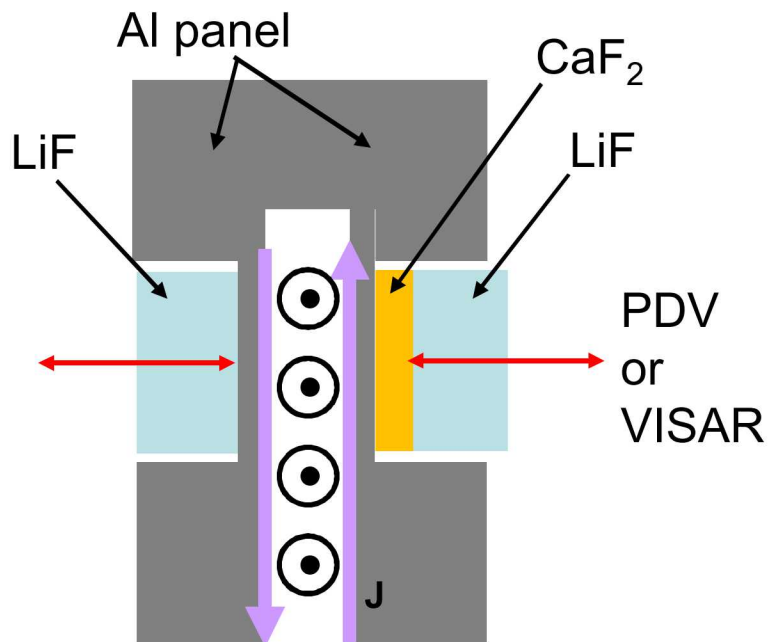


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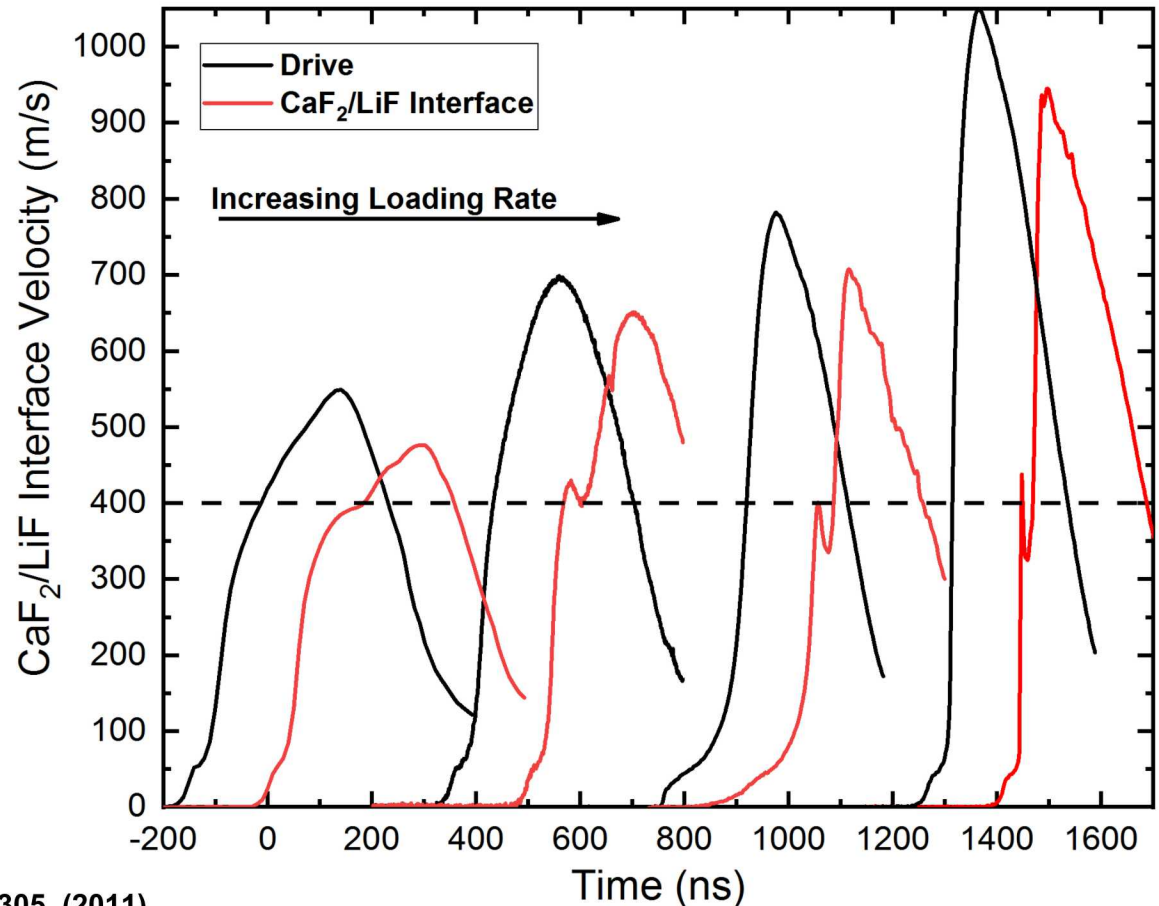
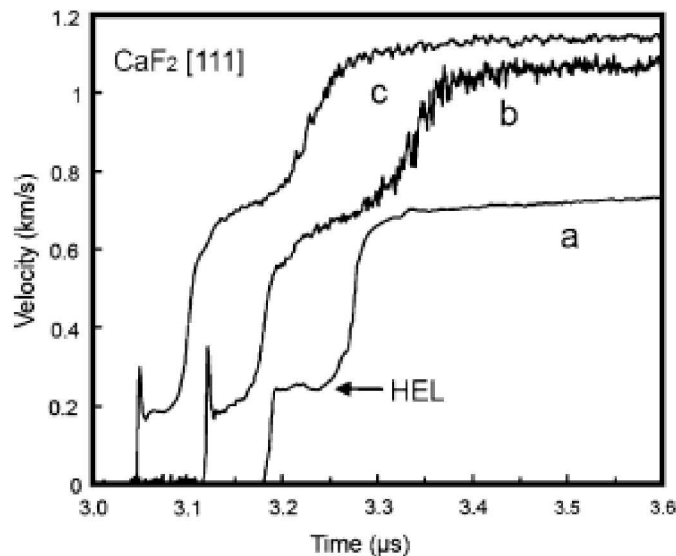
# Shockless Compression Experiments

- Preliminary experiments and analysis
- Used THOR to drive increasing loading rates into  $\text{CaF}_2$  [111] to examine elastic precursor behavior
- Comparison of [100] and [111] compressed above fluorite – cotunnite phase transition



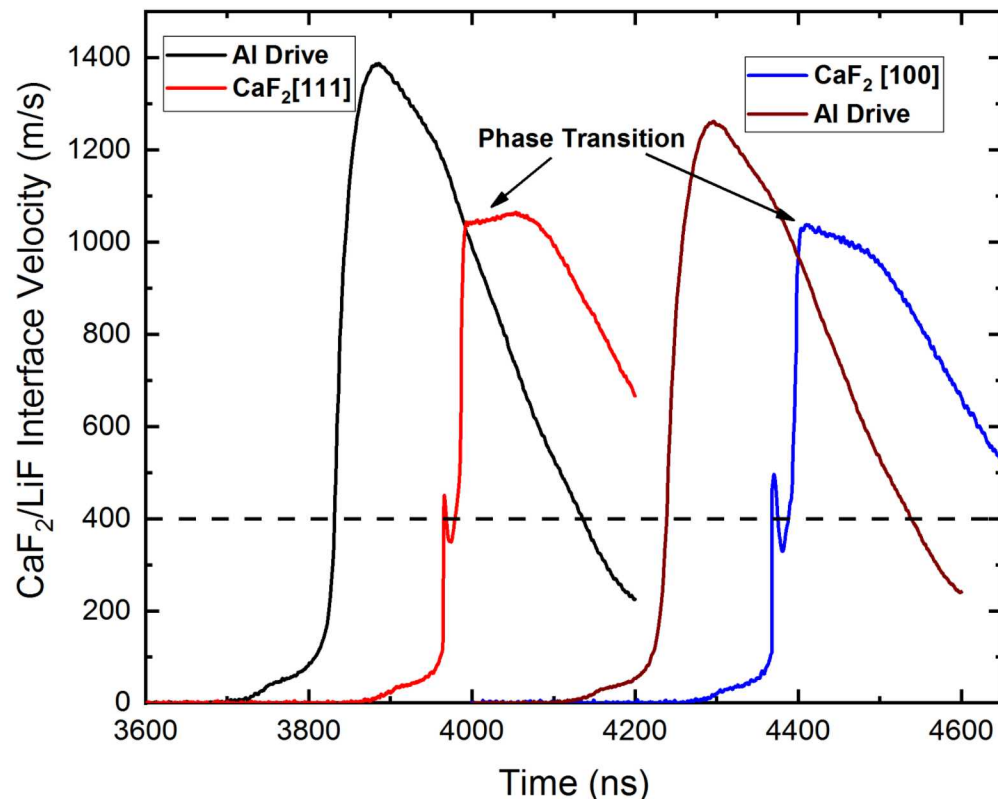
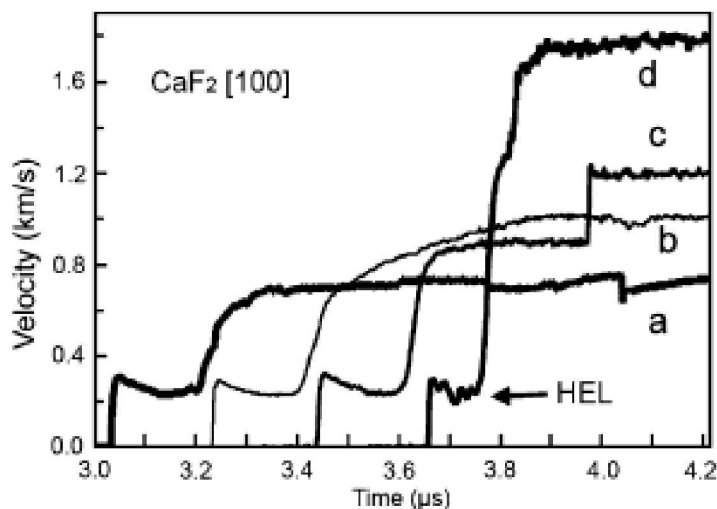
# Shockless Compression Experiments

- Preliminary experiments and analysis
- Used THOR to drive increasing loading rates into  $\text{CaF}_2$  [111]
- As loading rate increases, elastic precursor qualitatively looks like earlier shock work
- Lowering the loading rate changes the elastic peak
- Lowering rate also lowers the peak stress state



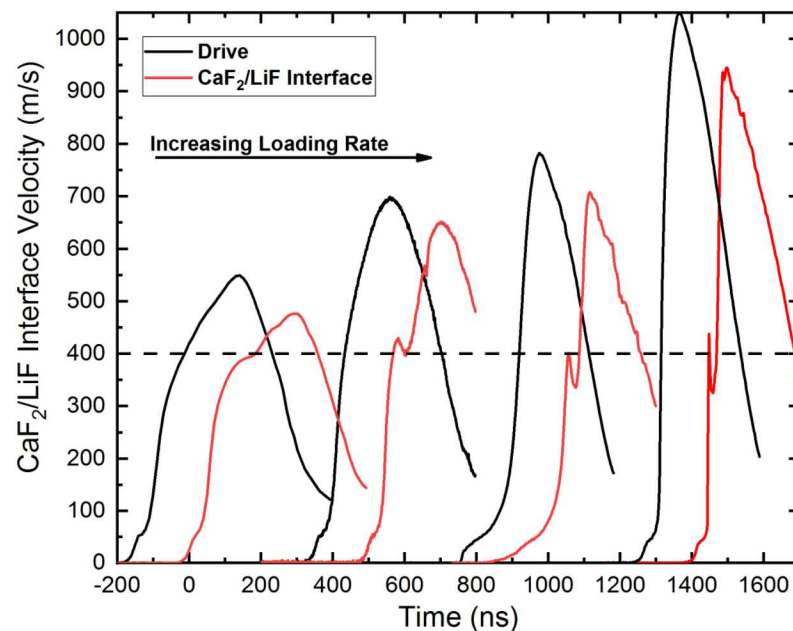
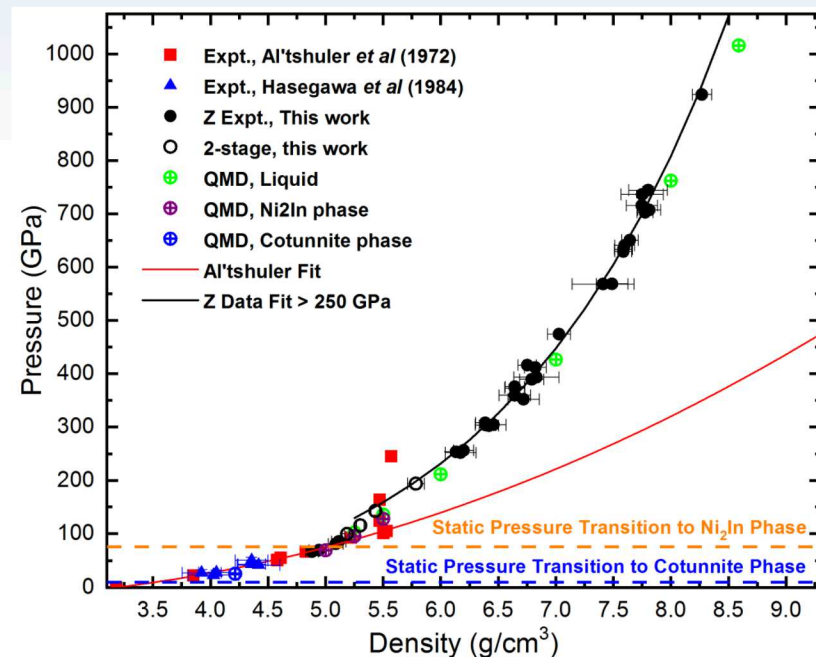
# Shockless Compression Experiments

- Preliminary experiments and analysis
- Used THOR to drive  $\text{CaF}_2$  above the fluorite-cotunnite transition
- High loading rate: both [111] and [100] show a sharp elastic precursor
  - Contrasts with Sekine's results on [100]
- Phase transition shows at velocities near 1000 m/s
- Under static compression the transition reduces volume by ~6%



# Summary

- Shock compressed  $\text{CaF}_2$  from 65 GPa to 950 GPa
- Above 200 GPa,  $\text{CaF}_2$  is likely melted
- DFT simulations in liquid state are consistent with the Z data > 200 GPa
- Between 100 and 150 GPa, the QMD results using solid  $\text{CaF}_2$  and liquid are consistent with the data
- Further DFT work is needed – comparison of Gibbs energies
- Phase boundaries are undetermined
- Loading rate affects the behavior of the elastic precursor



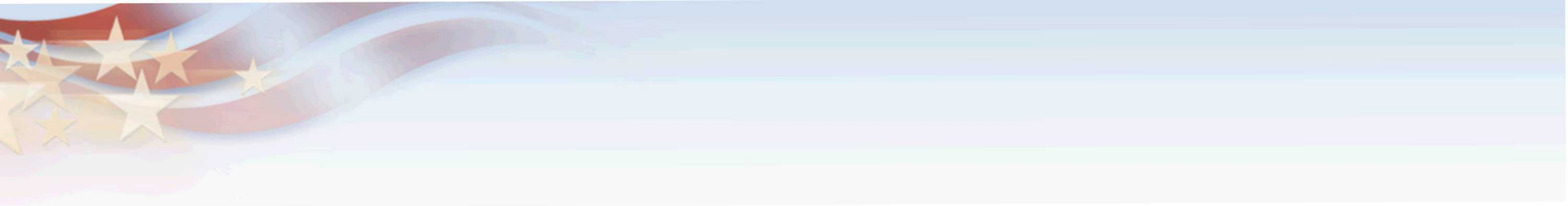
# Collaboration Objectives and Questions

## Phase Transitions and Phase Diagram

- **Develop a data-driven, multiphase equation of state for  $\text{CaF}_2$**
- Understand phase diagram over a broad range of pressure and temperature
- Understand the kinetics of the phase transitions
  - The Hugoniot below 100 GPa is complicated by multiple wave structures – can we understand these?
  - Along the Hugoniot, does melt start from the cotunnite phase or do other solid phases exist?
  - What does the extended phase diagram look like?
  - Shock, Shock-Ramp, and DAC experiments and DFT-QMD calculations

## Elastic – Plastic Behavior

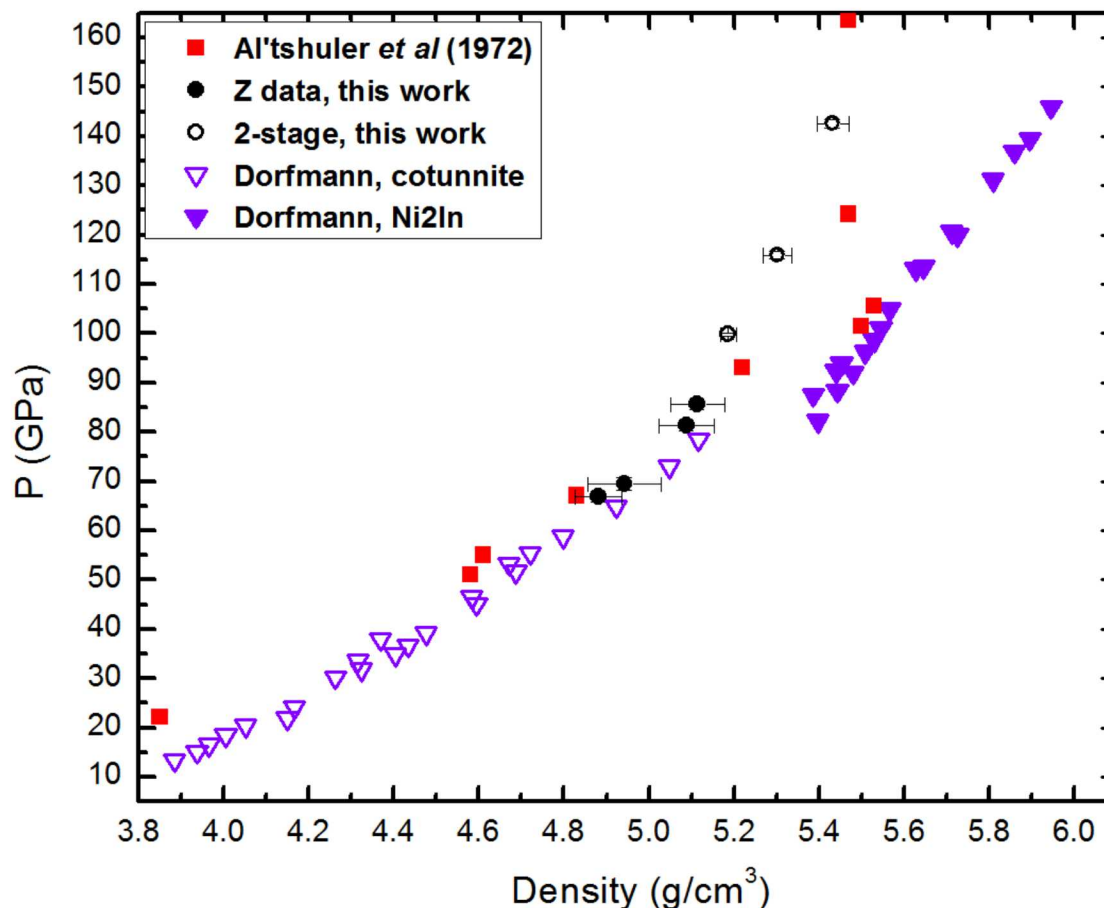
- **Examine the dynamics of the constitutive response and develop or validate a constitutive model**
  - How does loading rate and peak stress affect elastic precursor behavior?
  - Temperature and orientation effects on the elastic precursor?
  - Shock and shockless compression experiments



# Extra Slides

# Melting Transition

- $\text{CaF}_2$  is likely melting
- $\text{CaF}_2$  becomes less compressible between 100 – 150 GPa range
- Dorfman's data show the  $\text{Ni}_2\text{In}$  transition has a volume reduction



\* S. Dorfman et al, Phys. Rev. B **81**, 174121 (2010)  
Dorfmann, private communication

# Fluorite phase Hugoniot calculations

