



Structure and Interactions in Nanoparticle/Polymer Blends

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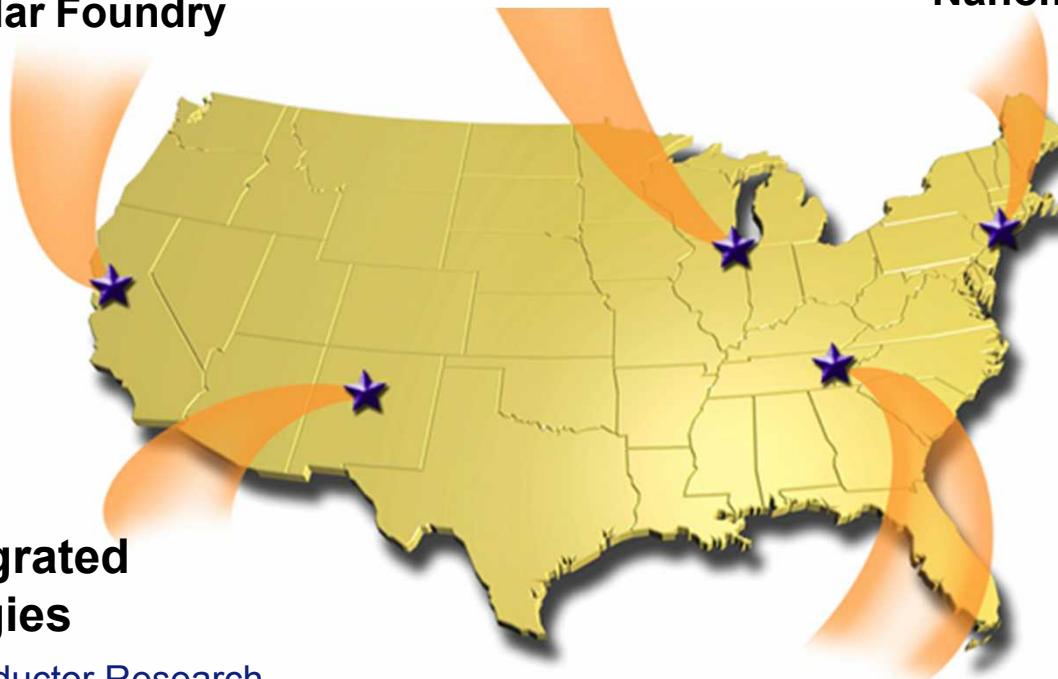
Compound Semiconductor Research
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Microelectronics Development Laboratory

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Los Alamos Neutron Science Center

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cint.lanl.gov
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Outline

- **overview**
- **density functional theory (DFT)**
- **coated nanorods in melts**
- **nanoparticles in polymer films**



Some Experimental Questions

- how best to disperse a nanoparticle in a polymer?
 - what materials?
 - use surfactant or polymer brush? what chain lengths?
 - what molecular weight vs. nanoparticle size?
- interfacial properties of nanocomposites
 - where do the particles go?
 - segregation, e.g. in block copolymer domains?
 - what happens at a substrate?



Challenges in Modeling

nanoparticle sizes:

7Å (buckeyball)

2 - 10 nm (cross-linked polymers, dendrimers)

2 - 50 nm (metals, oxides, ...)

polymer sizes

e.g. PS at entanglement length 18kDa

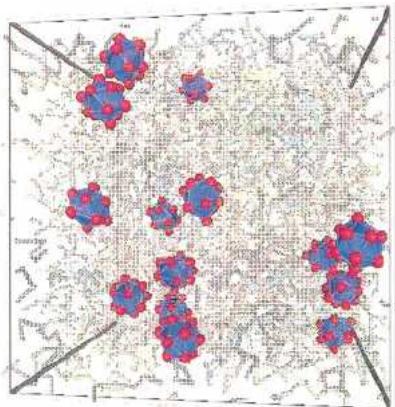
$R_g \approx 3.6 \text{ nm}$

→ can't treat nanoparticles as flat surfaces

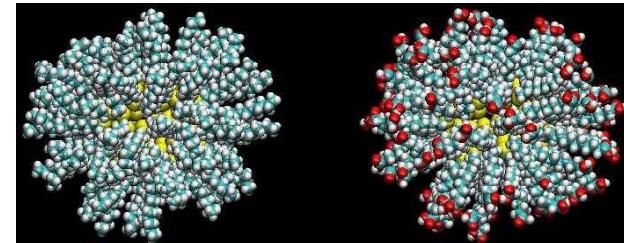


Simulations

- **length scales large for atomistics**
- **coarse-grained models**
 - **dilute limit**
 - **polymer dynamics near 1 nanoparticle**
 - **calculate PMF between two particles**
 - **small particles, $D = 2$ or $3x$ monomer size**



Starr et al., Macromolecules, 2003



alkanethiols on Au nanoclusters

Grest, Stevens, 2007

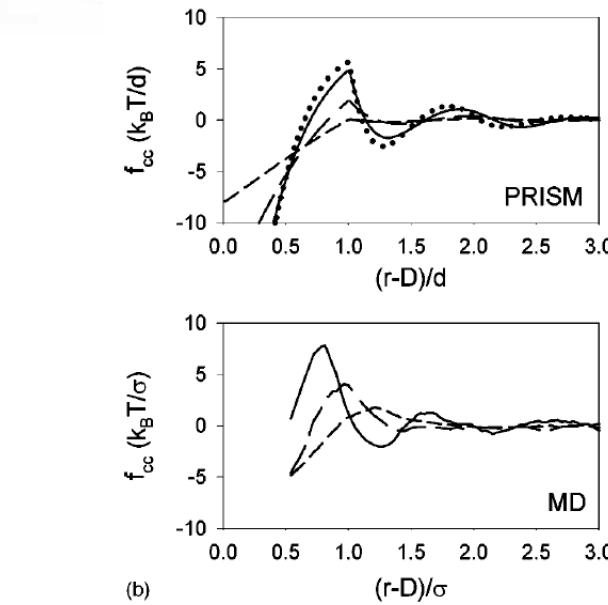
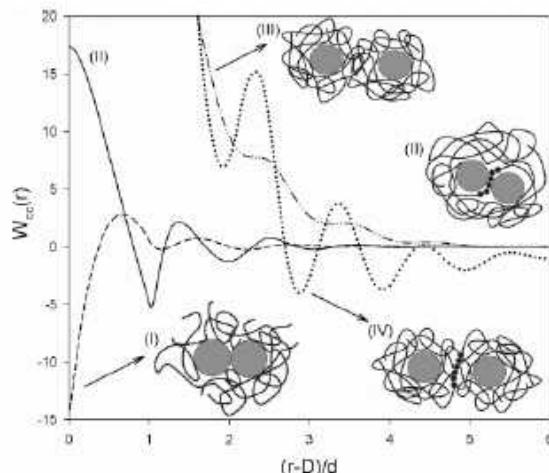
Bulk: Liquid State Theory

PRISM theory

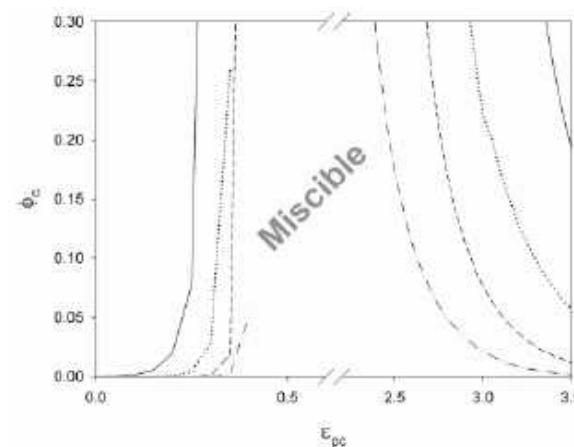
athermal: phase separation
due to depletion attraction

Hooper and Schweizer, *J. Chem. Phys.* 124, 6986 (2004)

with nanoparticle-polymer attractions



(b)

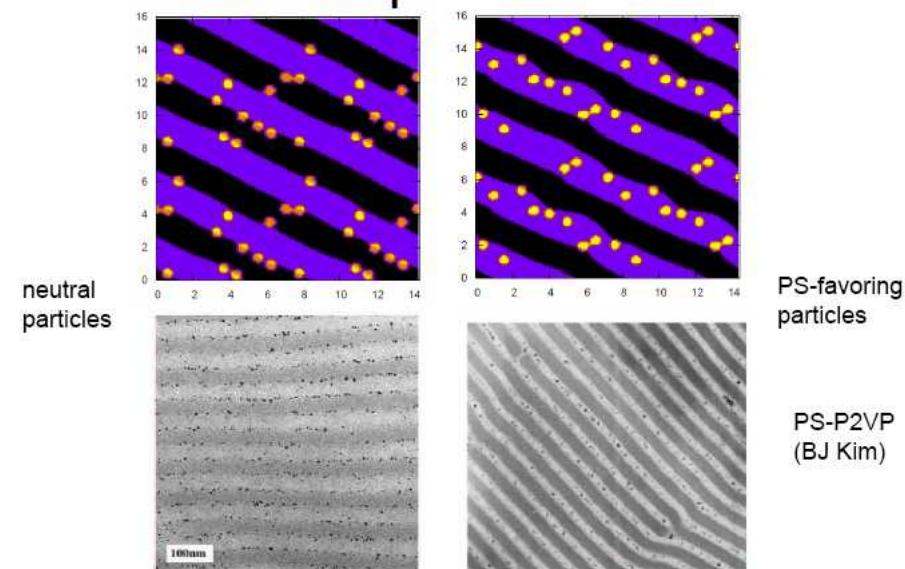
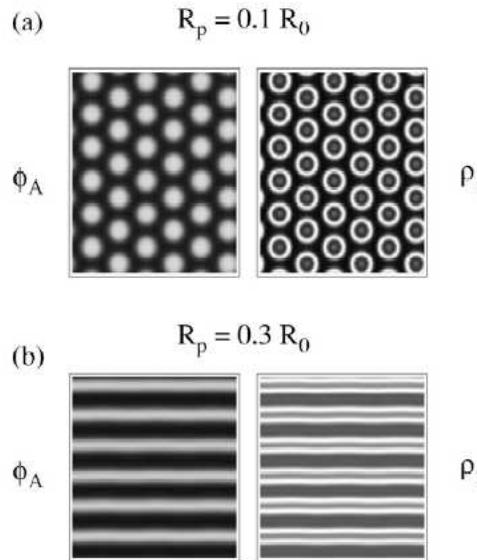


Hooper and Schweizer, *Macromolecules* 39, 5133 (2006)



Hybrid SCF Theories

- self-consistent field theory for polymers
 - especially diblocks
- particles
 - density functional theory (e.g. hard spheres)
 - treat as surfaces



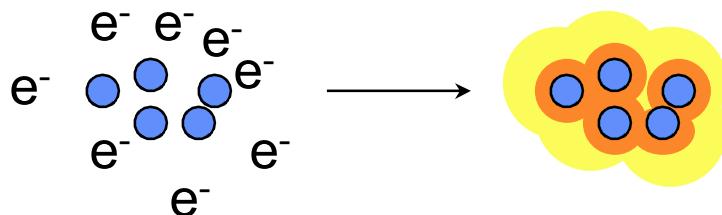
Balazs, Curr. Opin. Solid St. & Mat. Sci., 2003

Düchs, Fredrickson, Sides, 2007

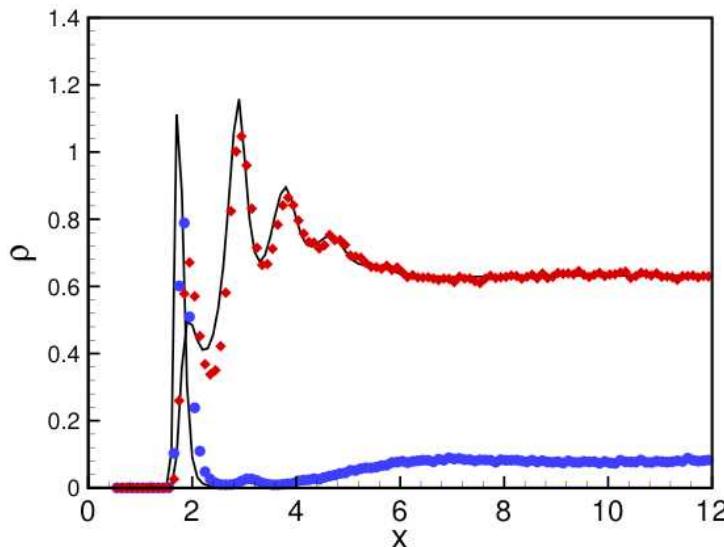
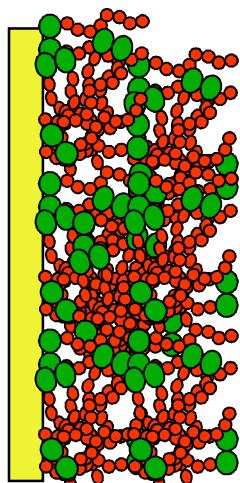
Density Functional Theory (DFT)

$$\Omega[\rho(r)] : V(r) \rightarrow \rho(r)$$

External field Density profile



Electronic Structure
(Closed system with N-electrons)



Fluid Structure
(Often open system with fixed chemical potential)



Structure of a Fluids-DFT

ansatz for Helmholtz free energy:

$$\begin{aligned} F[\rho(\mathbf{r})] &= F^{id} + F^{HS} + F^{att} + \dots \\ &= \int \rho(\mathbf{r}) [\ln(\rho(\mathbf{r}) - 1)] d\mathbf{r} + \int \Phi(\{n_\gamma\}) d\mathbf{r} \\ &\quad + \sum_i \sum_j \int d\mathbf{r} \int d\mathbf{r}' \rho_i(\mathbf{r}) \rho_j(\mathbf{r}') u_{ij}^{att}(|\mathbf{r} - \mathbf{r}'|) + \dots \end{aligned}$$

form in grand canonical (open) ensemble

$$\Omega[\rho(\mathbf{r})] = F[\rho(\mathbf{r})] + \int \rho(\mathbf{r}) [V^{ext}(\mathbf{r}) - \mu] d\mathbf{r}$$

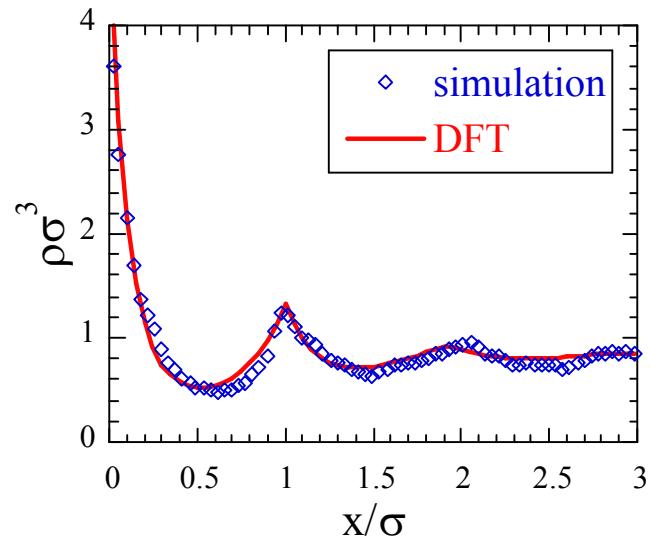
minimize free energy

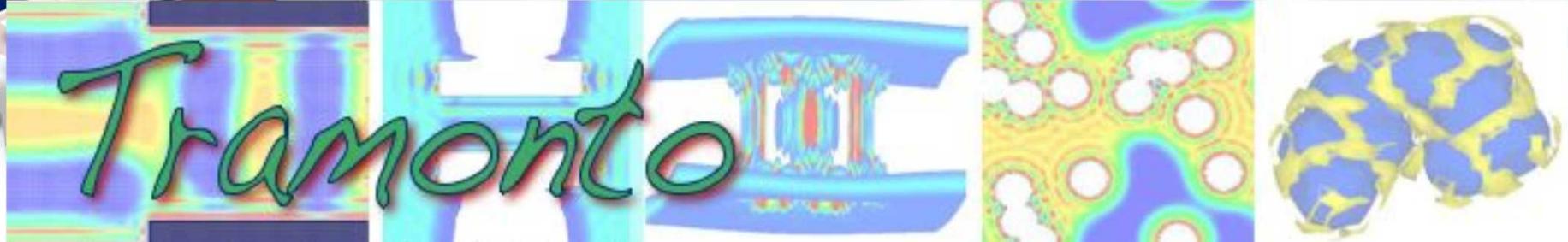
$$\frac{\delta \Omega}{\delta \rho(\mathbf{r})} = 0 \longrightarrow \text{equations to solve for } \rho(\mathbf{r})$$



Advantages/Capabilities of DFT

- treat different length scales
 - packing of individual “atoms” or sites
 - nano to mesoscopic length scales
- different kinds of fluids
 - hard spheres
 - attractive, Coulombic interactions
 - polymers
- compare directly to simulation results
- phase-space studies





Laura Frink, PI

<http://software.sandia.gov/tramonto/index.html>

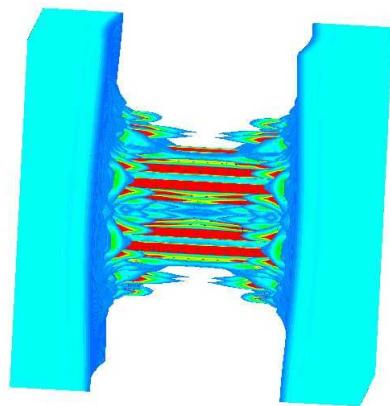
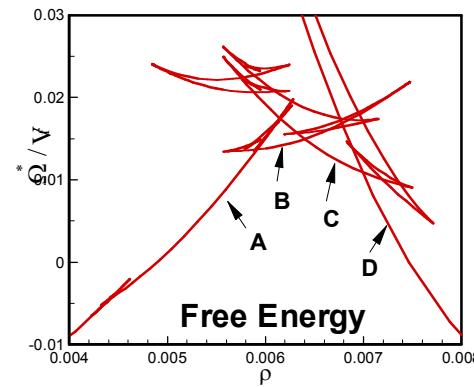
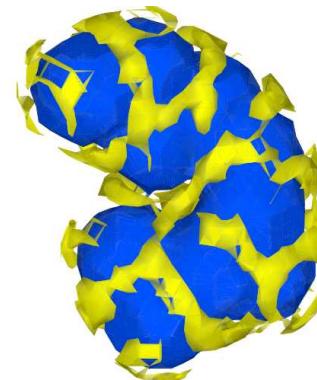
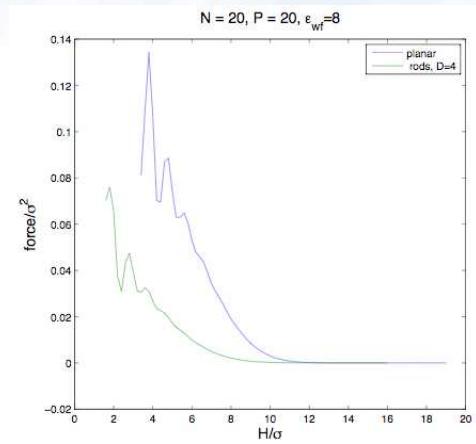
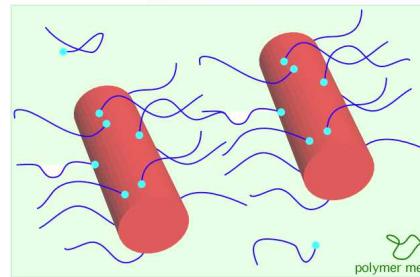
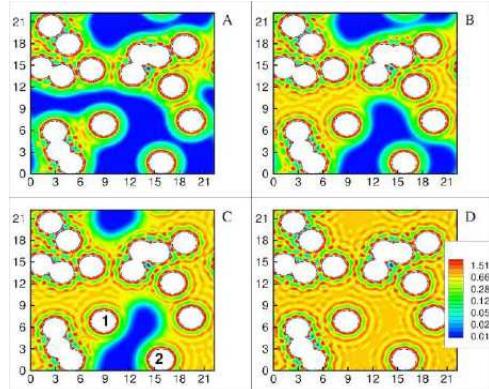
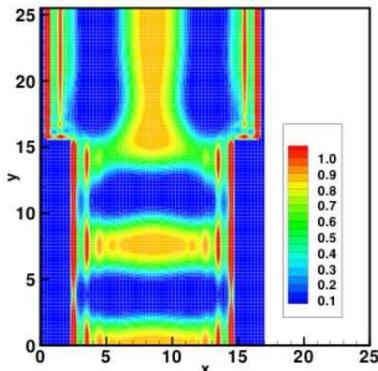
DFTs = nonlinear integral equations

- solve in 3D, Cartesian grid
- Newton-Raphson solver
- parallel
- sophisticated linear solver algorithms
- arc-length continuation algorithms

The Trilinos Project

What can F-DFT do?

- forces between particles
- phase behavior
- solvation free energies
 - implicit solvent
- complex geometries
- complex chain architectures
- compare to simulation (MD)



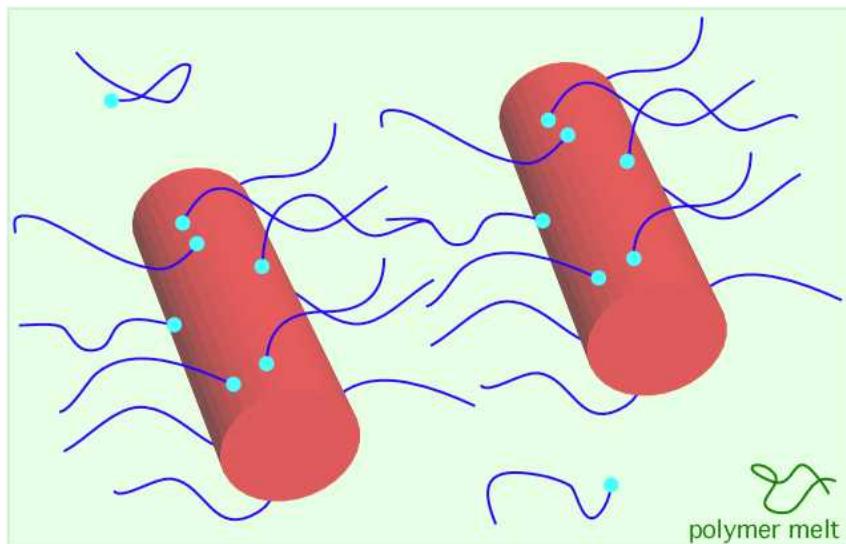


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The Problem:

dispersion of nanosized objects in a polymer melt
same rules as for polymer-stabilized colloids?

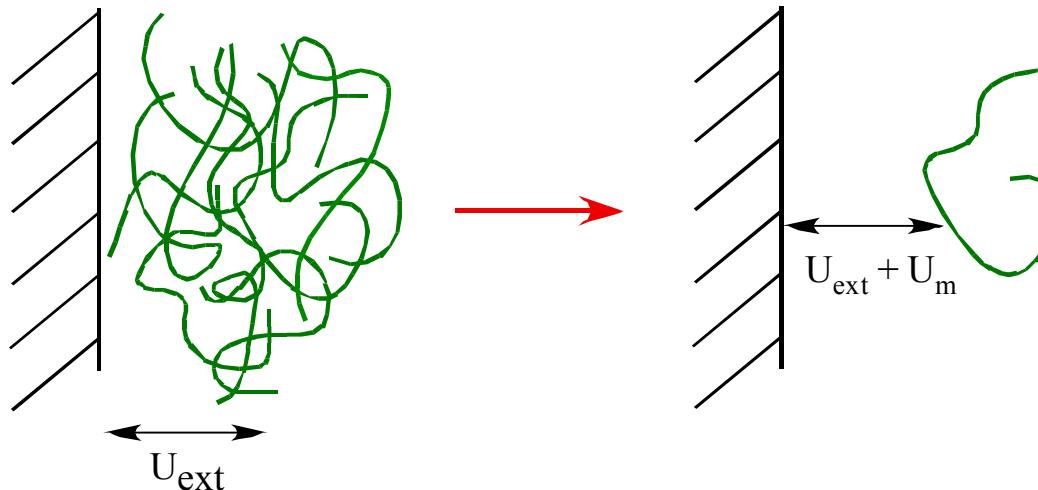


- adsorbed chains length N
 - sticky ends, energy ε_e
- matrix chains length P
- athermal ($\chi = 0$)
- nanorods with diameter D

is the force always repulsive?
will the chains desorb?

CMS-DFT

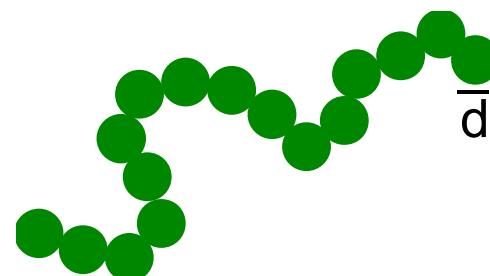
Chandler, McCoy, Singer (1986);
McCoy et al. (1990s)



- Minimize free energy, $\Omega[T, V, \mu; \rho(r)]$
- Solve self-consistently for density profile and mean field:

$$\rho(r) = G[U_{eff}(r)]$$

$$U_{eff}(r) = U_{ext}(r) + U_M[\rho(r)]$$





Our approach: CMS-DFT

- chains are flexible
- 2nd order density expansion

Chandler, McCoy, Singer (1986);
McCoy et al. (1990s)

$$\rho_\alpha(r) = \frac{\rho_\alpha^b}{N_\alpha} \sum_{s=1}^{N_\alpha} \frac{G_s(r) G_s^i(r)}{e^{-\beta U_\alpha(r)}}$$

$$U_\alpha(r) = V_{ext}(r) - \sum_\gamma \int c_{\alpha\gamma}(r-r') [\rho_\gamma(r') - \rho_\gamma^b] dr'$$

$$G_s(r) = e^{-\beta U_{\alpha,s}} \int w(r-r') G_{s-1}(r') dr'$$

$$G_s^i(r) = e^{-\beta U_{\alpha,s}} \int w(r-r') G_{s+1}^i(r') dr'$$

$$G_1 = G_N^i = e^{-\beta U(r)}$$

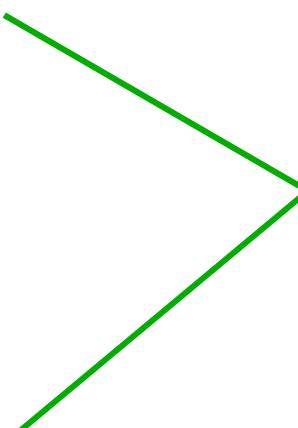
$$w(r) = \frac{1}{4\pi\sigma^2} \delta(|r| - \sigma)$$

Chain density distribution

Unknown field
 $c(r) = c_{rep}(r) - u_{att}(r)$

PRISM RPM
Theory Approx

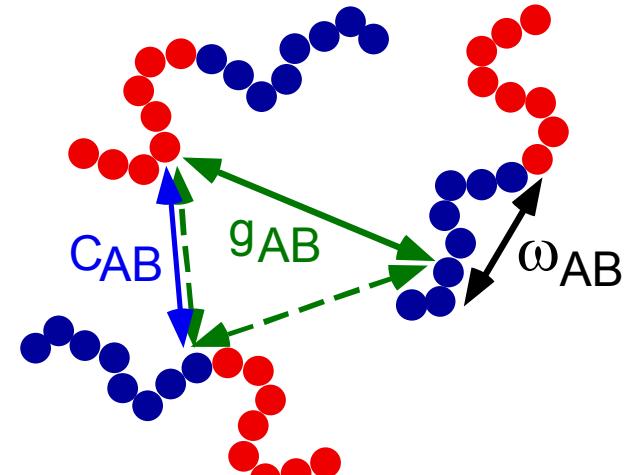
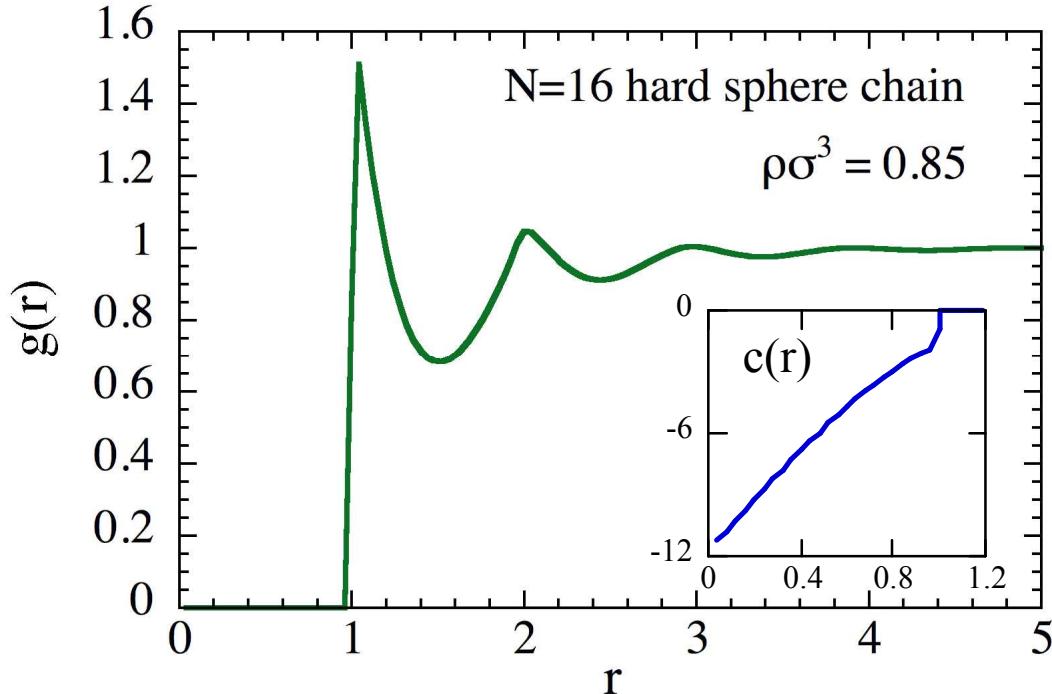
Chain Architecture
(gaussian chains)



Input to CMS-DFT: PRISM Theory

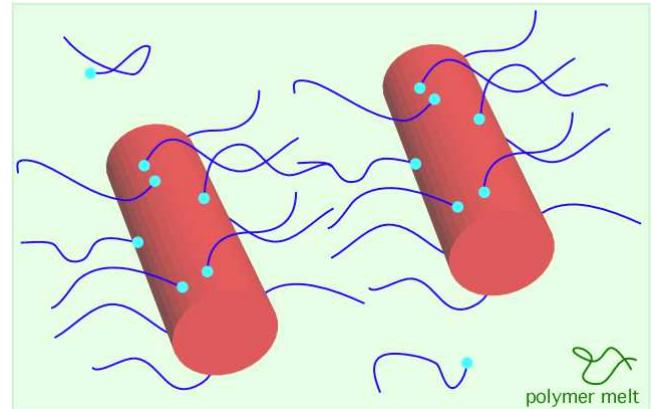
Curro and Schweizer

- Liquid state theory for homogeneous polymer fluids
 - intramolecular correlations ω_{AB}
 - intermolecular correlations $g_{AB}(r)$, $c_{AB}(r)$
- Excellent for repulsive interactions



Calculation Details

- parallel cylinders
- athermal (repulsive interactions)
- adsorbed chains
 - $N = 20$
 - $\rho_b d^3 = 0.04$
- matrix chains
 - $P = 10, 20, 40$
 - $\rho_b d^3 = 0.76$

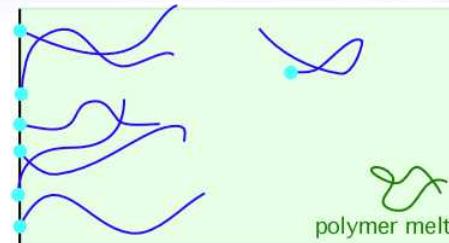
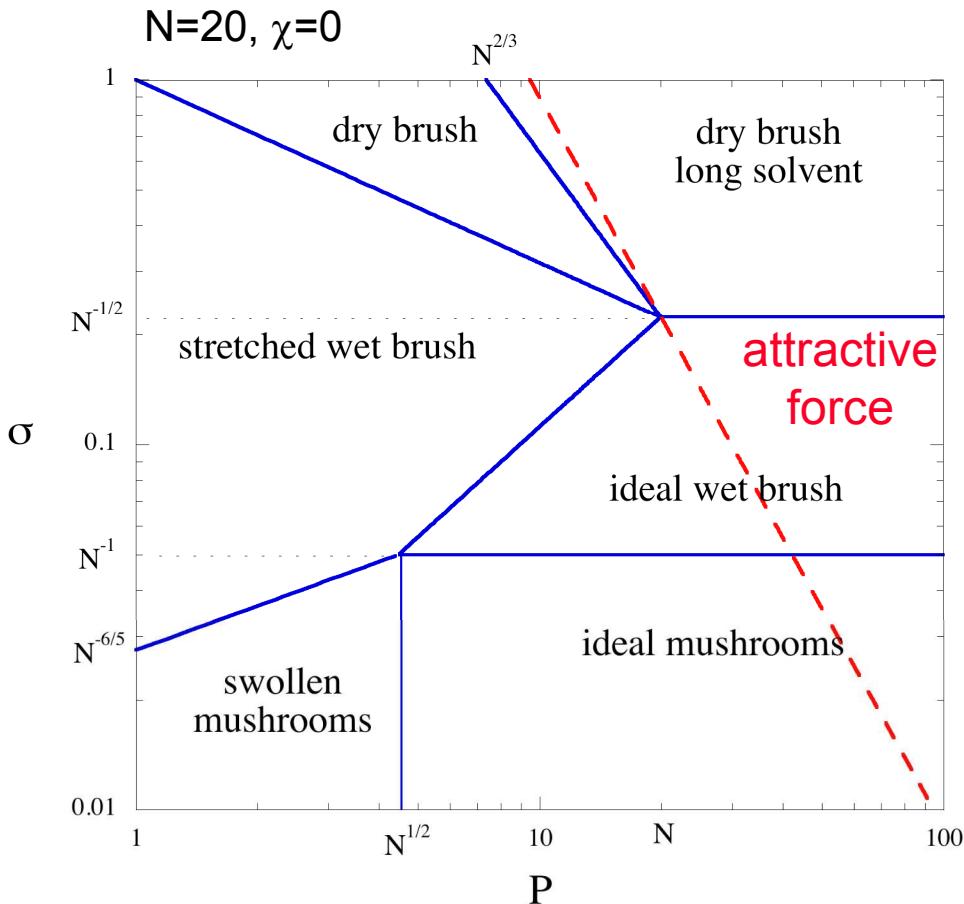


surface interactions:

- repulsive for matrix chains, sites 2-20 on adsorbing chains
- attractive to one end of adsorbing chains, depth ε_e

Diagram of State for Flat Surfaces

grafted chains on flat surfaces
behavior depends on:
 N, P, σ

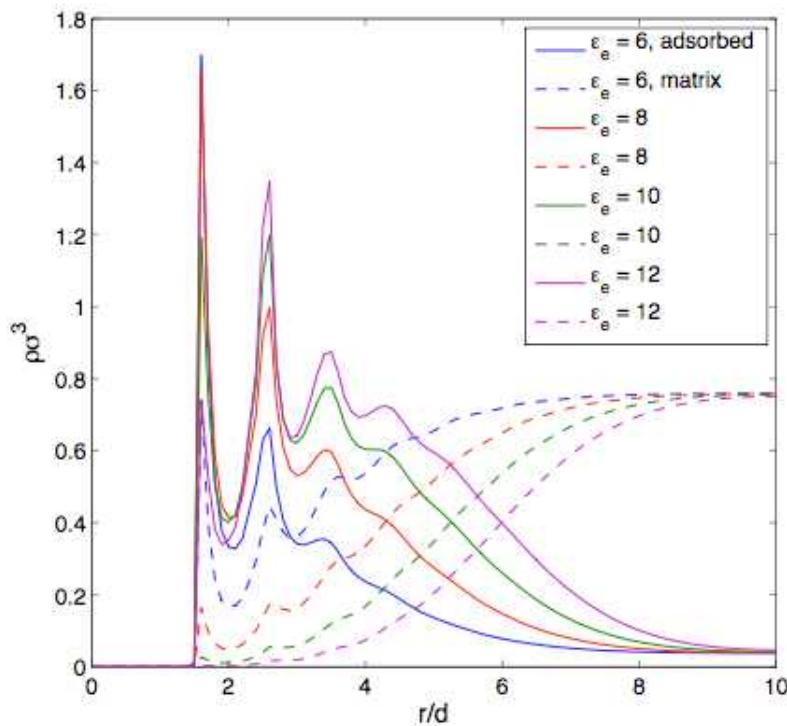




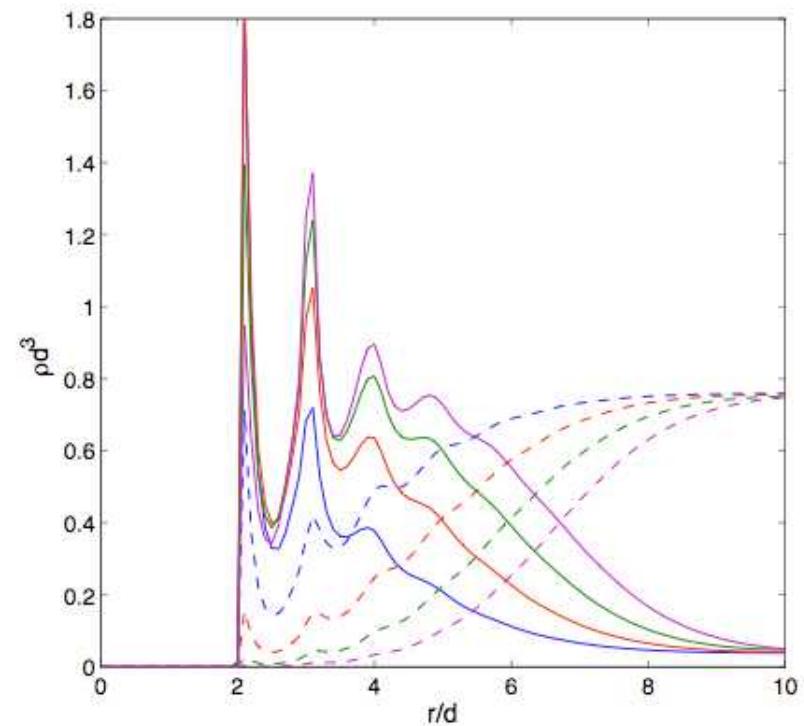
Nanorods: Brush Profiles

$N = 20, P = 20$

$D = 3d$



$D = 4d$

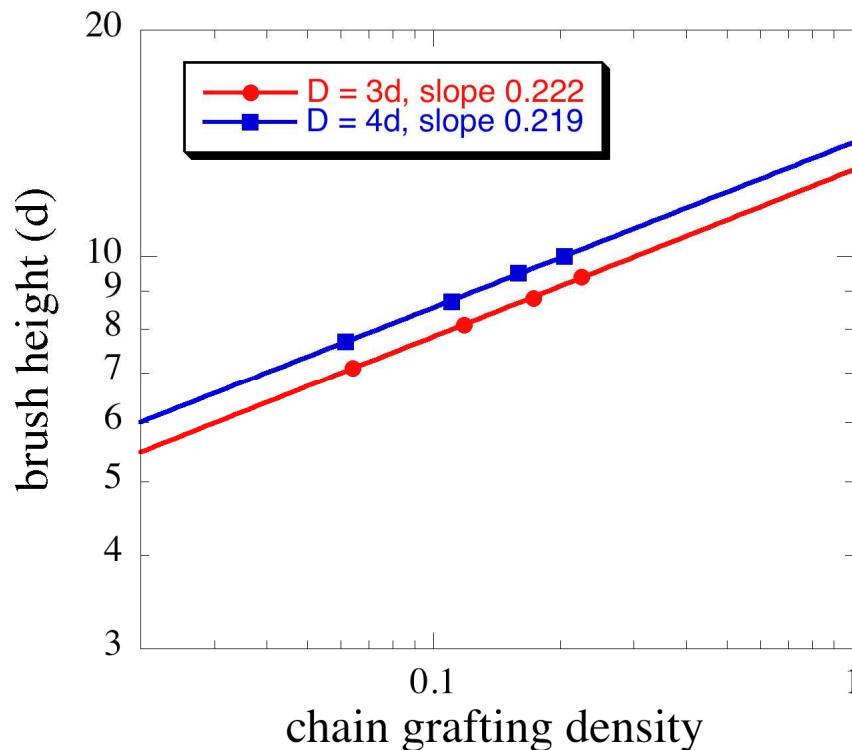


Brush Scaling

Flory argument: $F \sim \frac{h^2}{V} + \frac{wnV^2}{v} \sim \frac{h^2}{V} + \frac{w\sigma V^2}{h^2}$ $n = 2\pi RL\sigma, v = \pi h^2 L$

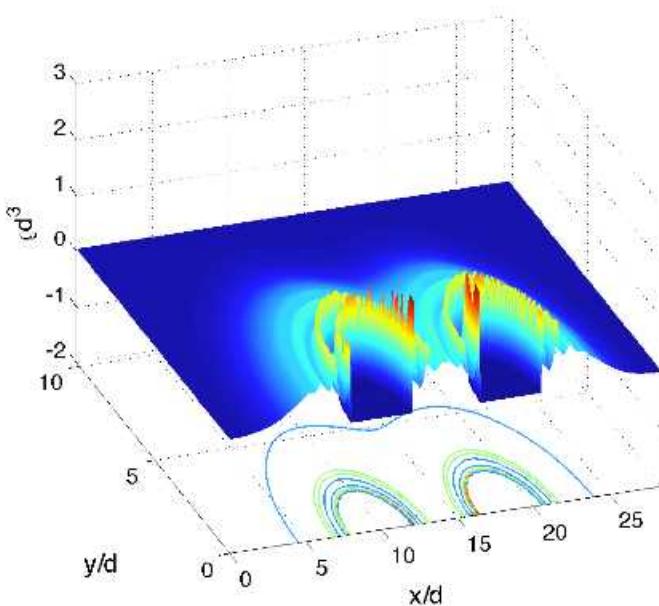
$$h \sim (Rw\sigma N^3)^{1/4}$$

Ball et al., Macromolecules, 1991

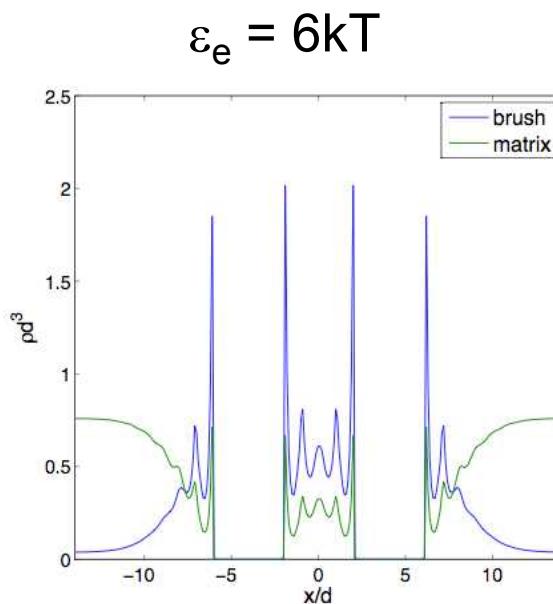
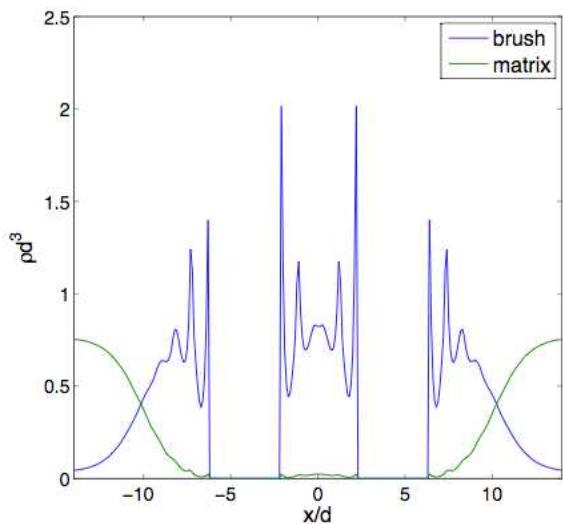


Two Nanorods

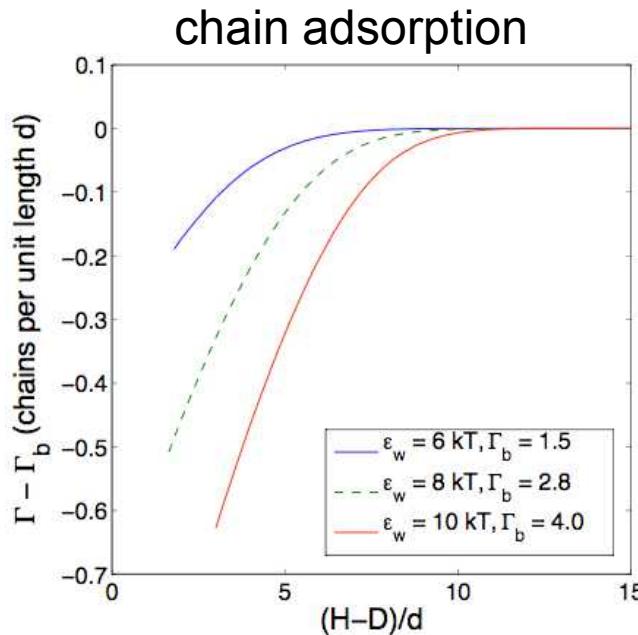
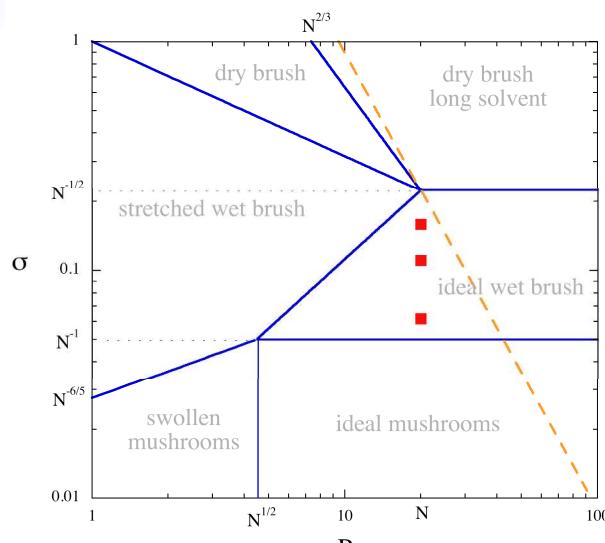
$N = 20, P = 20, D = 4d$



$\epsilon_e = 10kT$



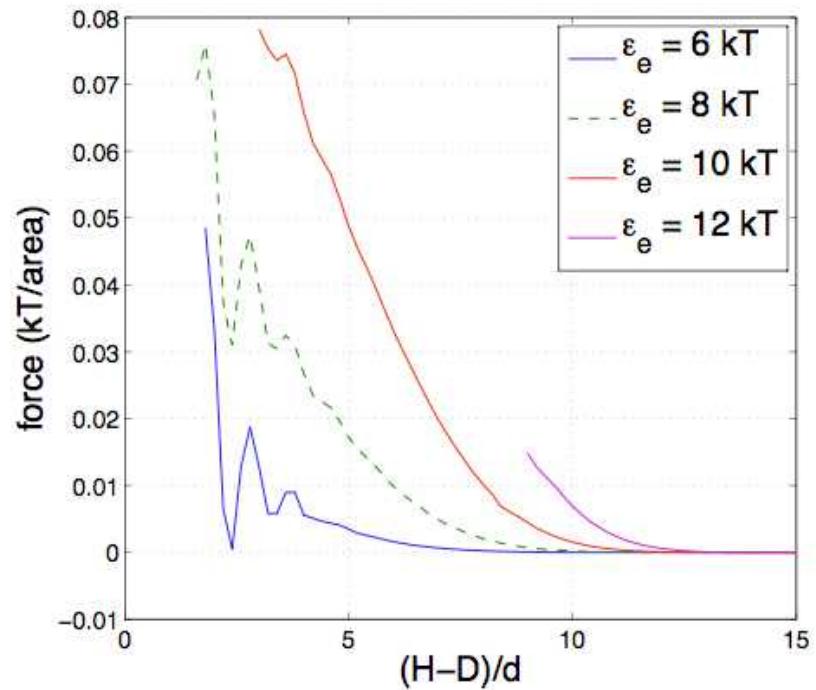
Force between rods



$$N = 20, P = 20, D = 4d$$

$$F = \frac{1}{A} \frac{\partial \Omega}{\partial H} = \frac{1}{\pi D} \frac{\partial(\Omega/L)}{\partial H}$$

force





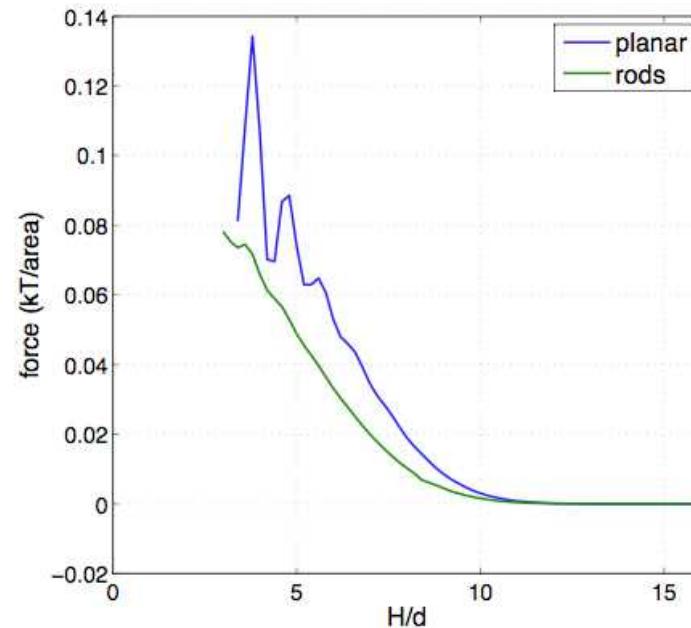
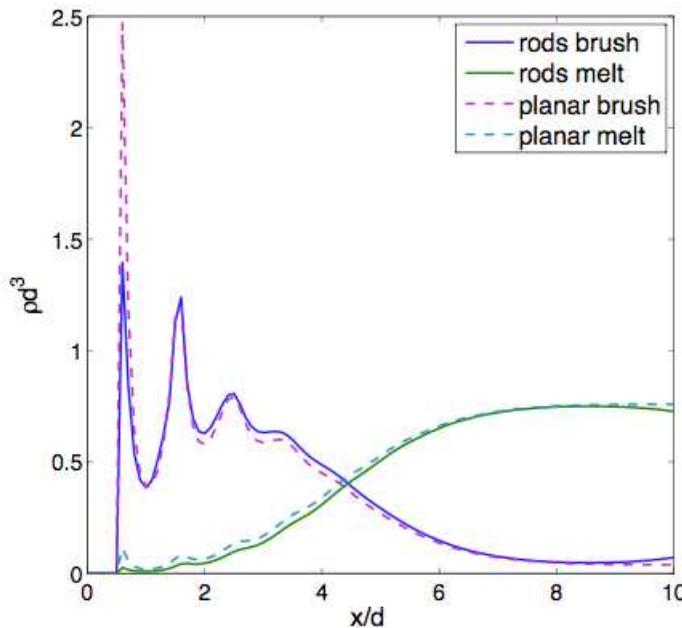
Less force due to curvature

$$N = 20, P = 20, D = 4d$$

planar brush: $\varepsilon_e = 8 kT$

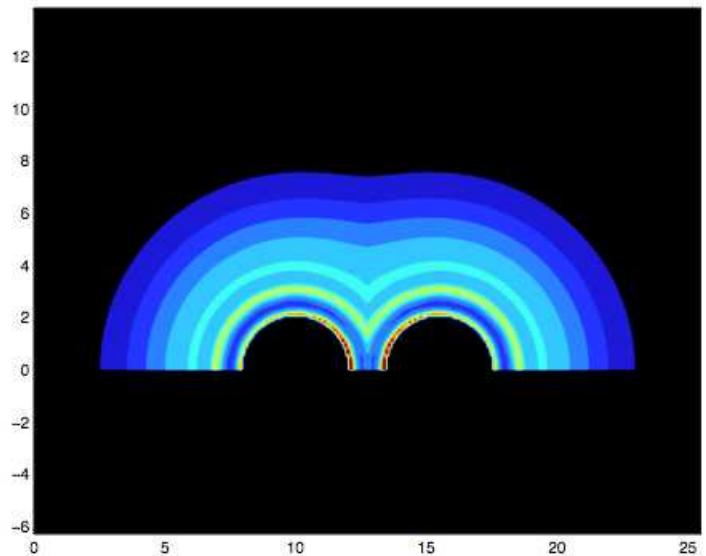
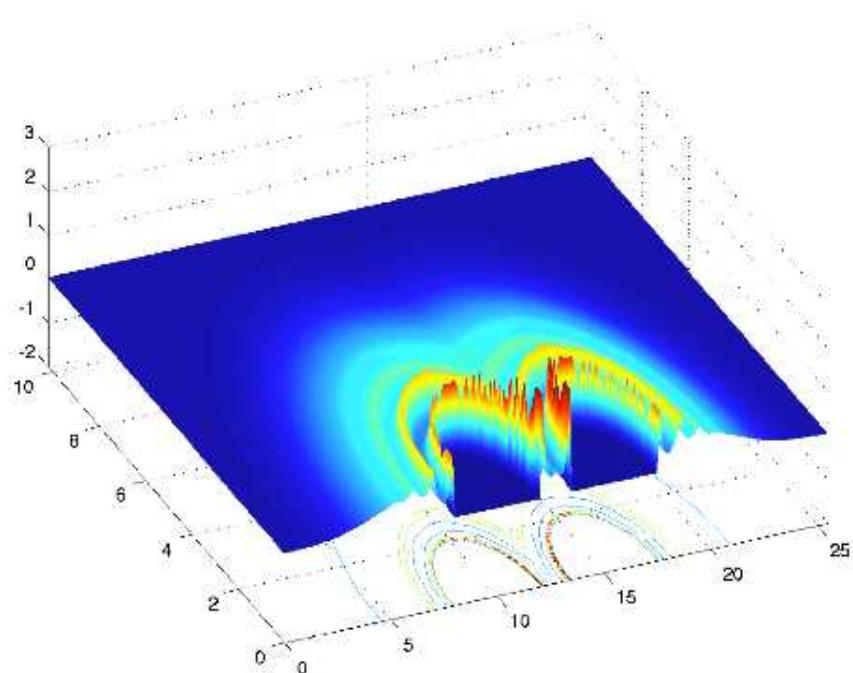
cylindrical brush: $\varepsilon_e = 10 kT$

similar brush heights, profiles
force less in curved system



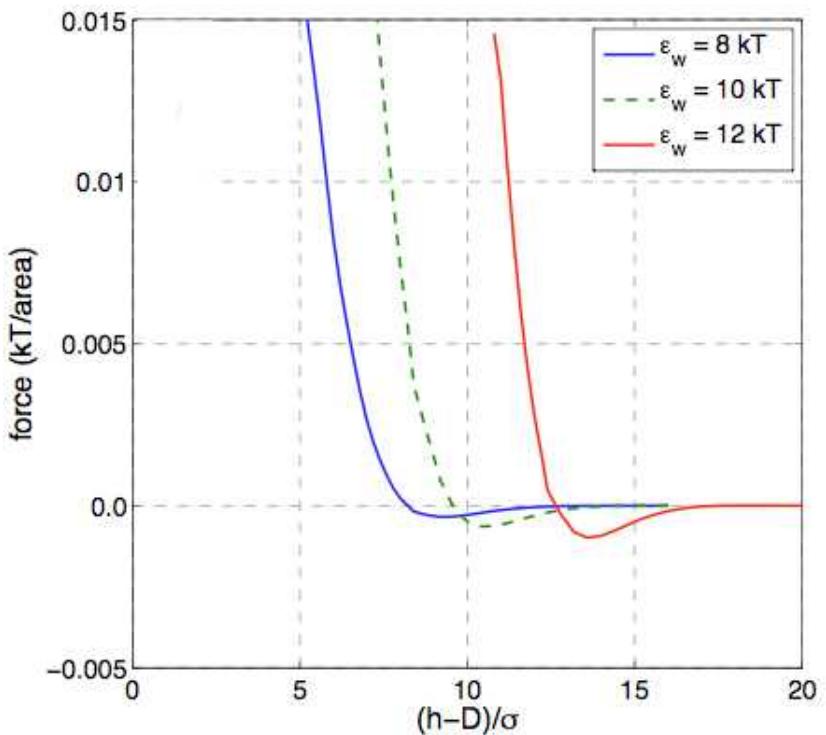
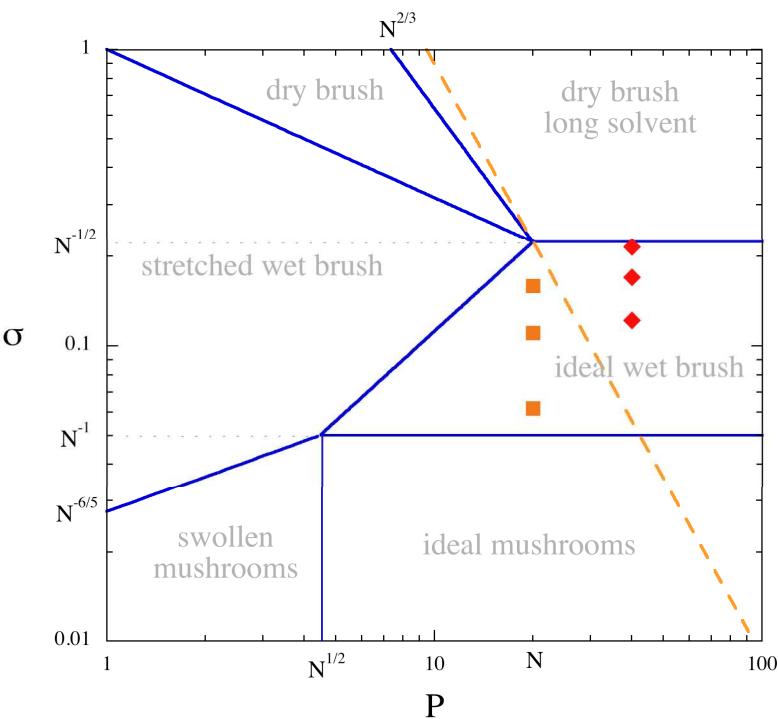


Chains go around rods



Polymer-Mediated Attractions

$$N = 20, P = 40, D = 4d$$



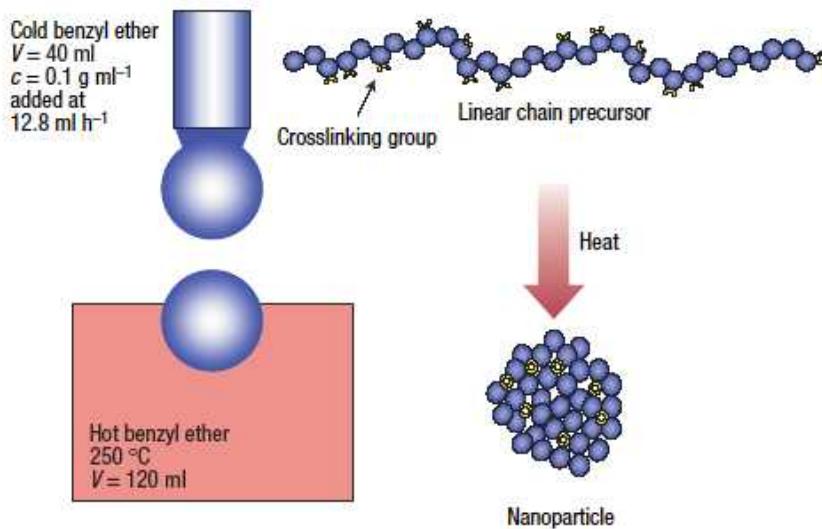


Outline

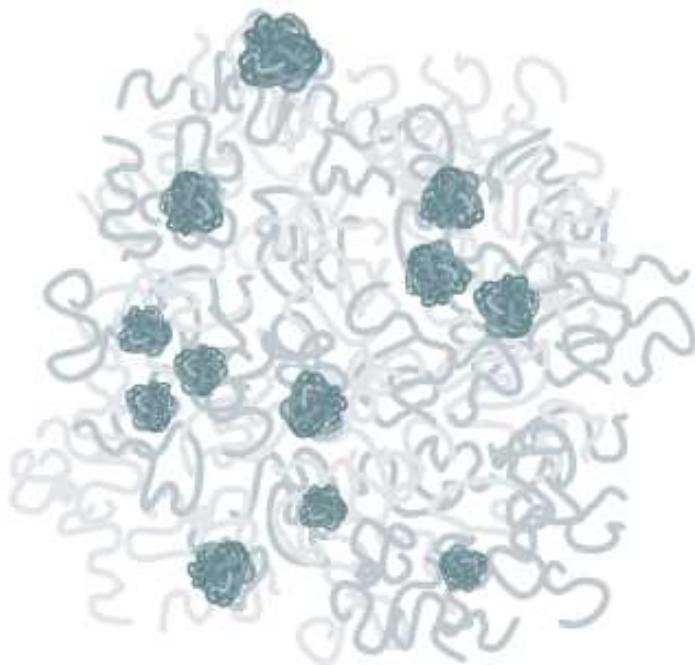
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- nanoparticles in polymer films

A Model Athermal System: PS NPs in PS

hard-sphere like nanoparticles



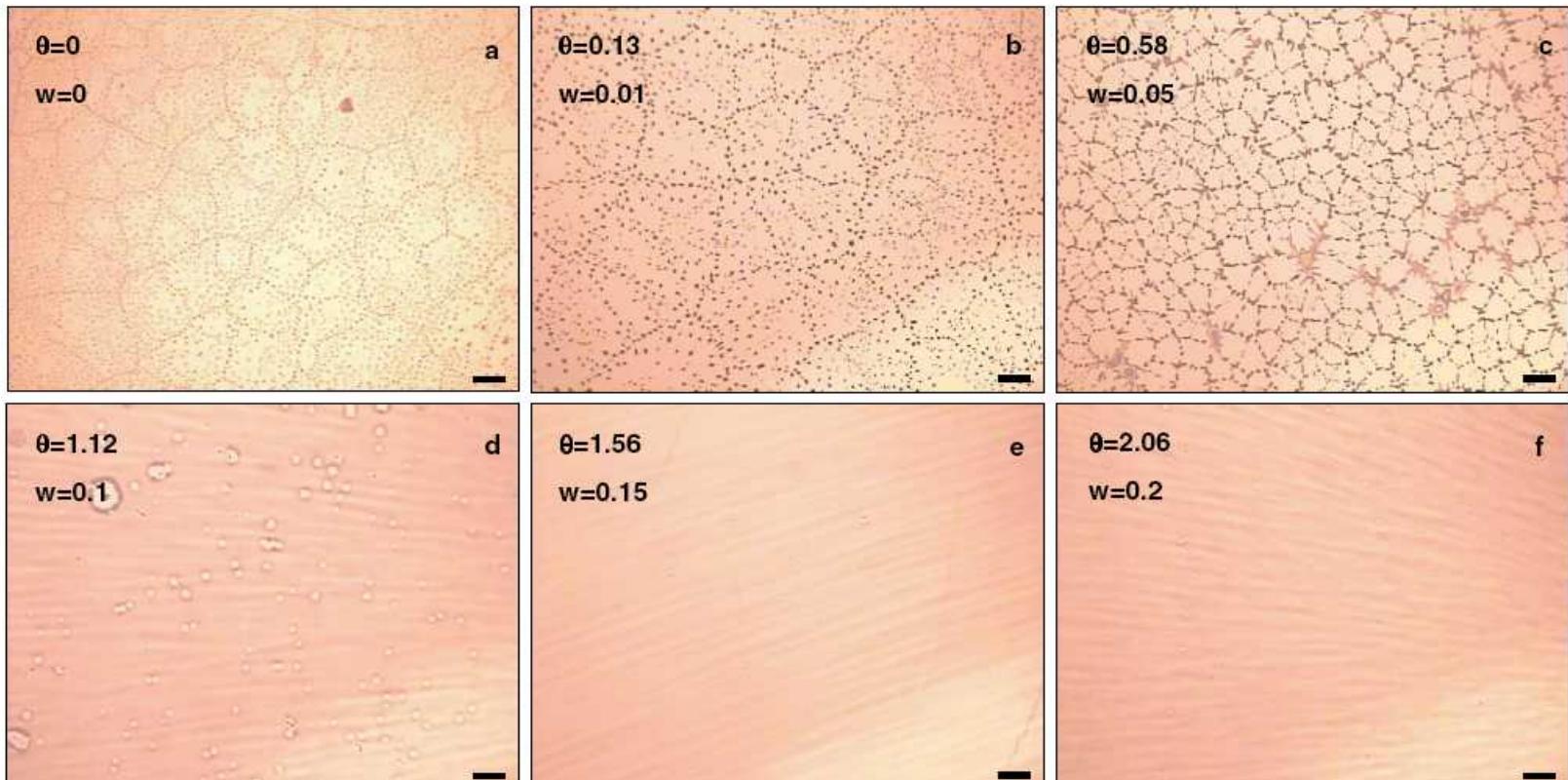
mix in melt PS



NPs stay dispersed!
(for $R_{NP} < R_g$)

Polymer/NP Thin Films

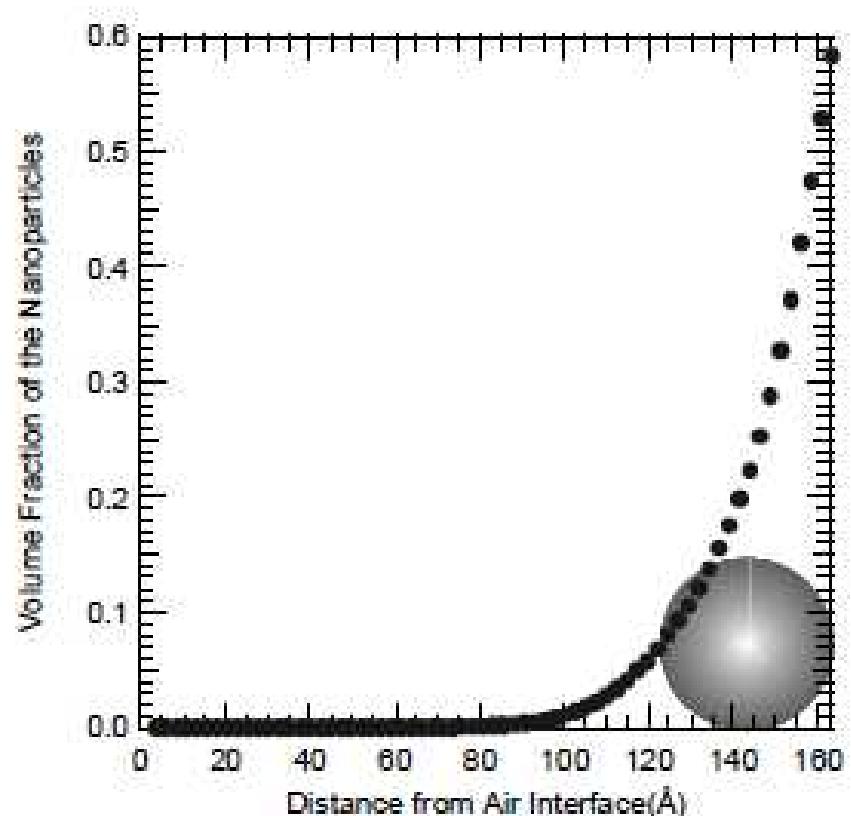
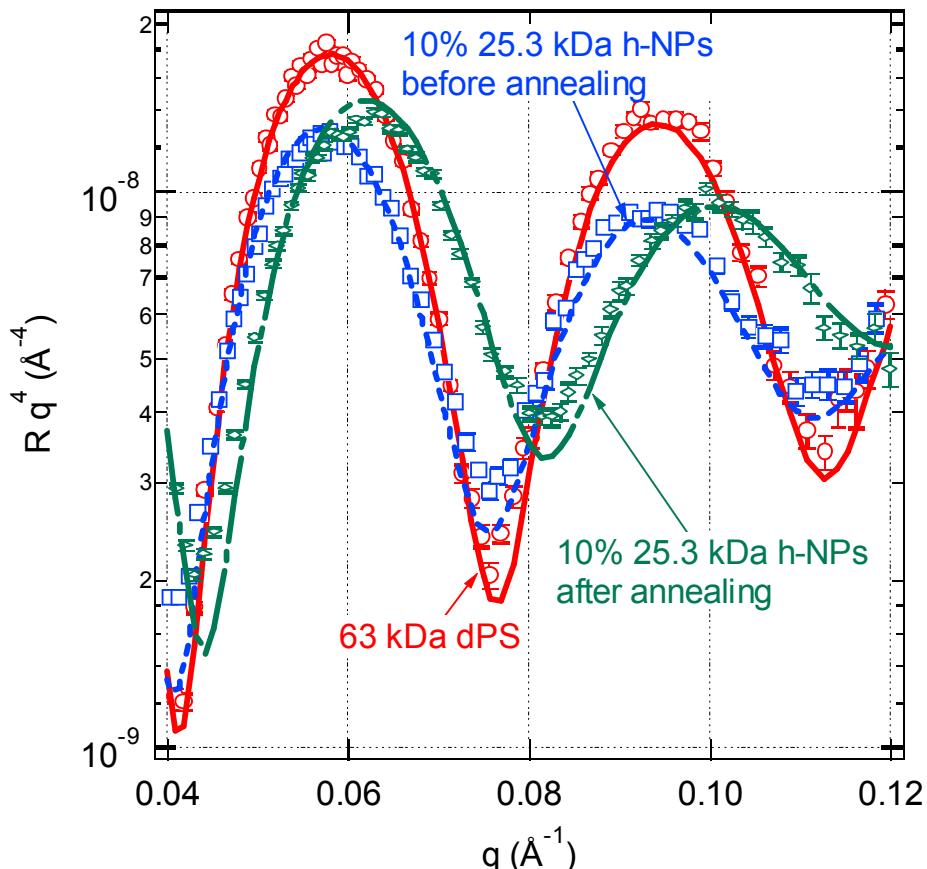
PS nanoparticles blended with PS on silicon
40 nm thick film
NPs prevent dewetting!



Krishnan et al, Langmuir, 2005

Where are the nanoparticles?

neutron reflectivity

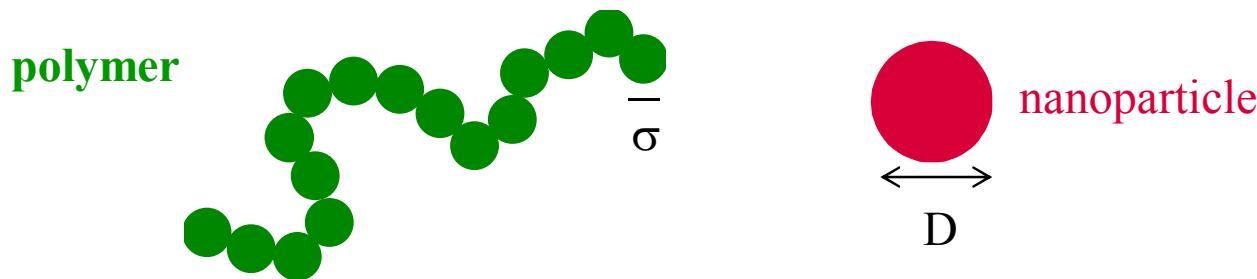


- nanoparticles segregate to surface
- lower surface energy/more surface roughness



Coarse-Grained Model

athermal system: repulsive LJ spheres



Kuhn length for PS: 1.485 nm

$$D = 2.0\sigma = 2.97 \text{ nm}$$

$$D = 2.5\sigma = 3.71 \text{ nm}$$



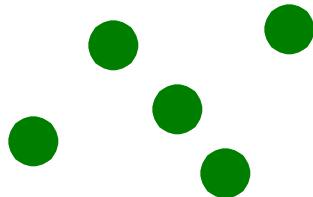
What's an appropriate DFT?

treat particles, polymers in same framework
accuracy for mixtures of diff. size sites

“WTC”-DFT

based on associating fluids
(Wertheim's TPT1 theory for bulk)

reference fluid: monomers



bonding sites



monomers bond:



as bonding energy $\rightarrow \infty$ get polymers



Elements in WTC functional

$$\Omega[\rho_\alpha(\mathbf{r})] = F[\rho_\alpha(\mathbf{r})] + \sum_\alpha \int d\mathbf{r} \rho_\alpha(\mathbf{r}) [V_\alpha(\mathbf{r}) - \mu_\alpha]$$

$$F = F^{id} + F^{hs} + F^{ch}$$

ideal gas part: $F^{id}[\rho_\alpha(\mathbf{r})] = kT \sum_\alpha \int d\mathbf{r} \rho_\alpha(\mathbf{r}) [\ln \rho_\alpha(\mathbf{r}) - 1]$

hard sphere functional: $F^{hs}[\rho_\alpha(\mathbf{r})] = kT \int d\mathbf{r} \Phi[n_\gamma(\mathbf{r})]$

chain bonding contribution:

$$F^{ch}[\rho_\alpha(\vec{r})] = kT \int d\vec{r}' \sum_{\alpha=1}^m \rho_\alpha^{\text{seg}}(\vec{r}') \sum_{\alpha'}^{\{\alpha'\}} \left(-\frac{1}{2} \ln \int d\vec{r}'' \frac{\delta(|\vec{r}' - \vec{r}''| - \sigma^{\alpha\alpha'})}{4\pi(\sigma^{\alpha\alpha'})^2} y^{\alpha\alpha'}(\vec{r}', \vec{r}'') \rho_{\alpha'}^{\text{seg}}(\vec{r}'') + \frac{1}{2} \right)$$



Calculational Details

surface potential:

$$V_\alpha(z) = \frac{2}{15} \left(\left(\frac{\sigma}{z - \delta_\alpha} \right)^9 - \left(\frac{\sigma}{z - \delta_\alpha} \right)^3 \right), \quad z < z_{cut}$$

monomers $\delta_p = 0$

nanoparticles $\delta_{np} = (\sigma_{np} - 1)/2$

- start at low particle concentrations
- keep total packing fraction fixed:

$$\rho_p \sigma^3 + \rho_{np} \sigma_{np}^3 = 0.79$$

- follow solution as particle concentration increases

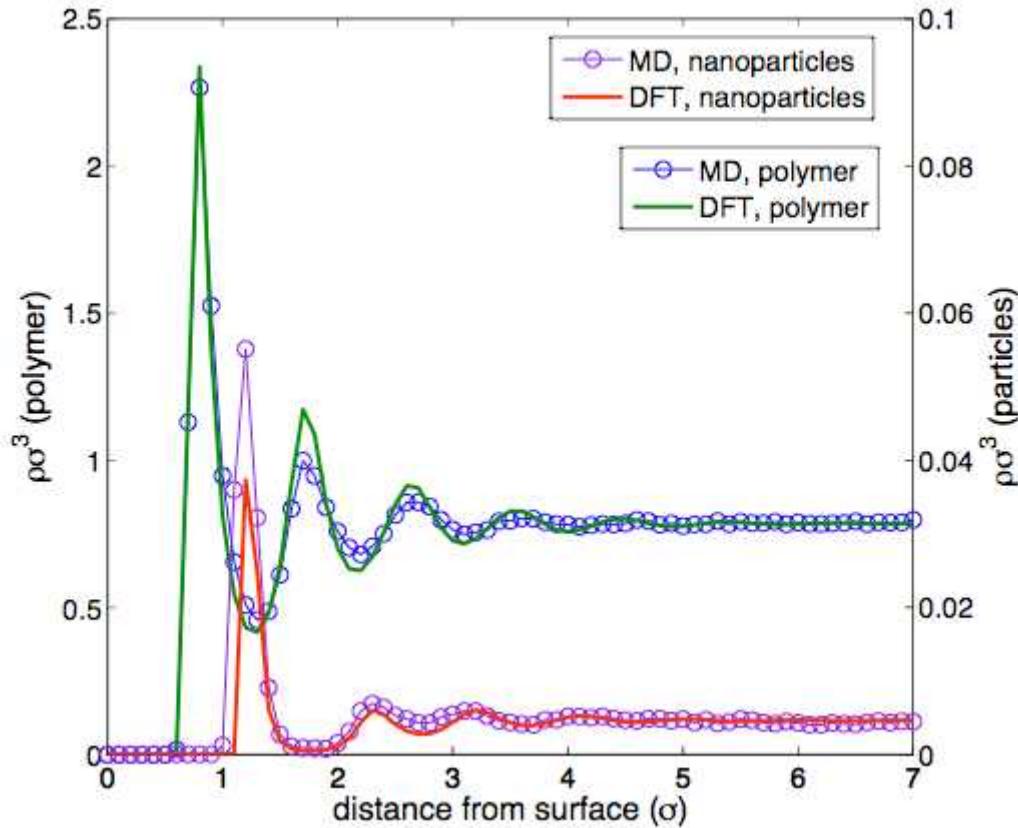


Nanoparticle/Polymer Thin Films

with E. S. McGarry and M. E. Mackay (MSU)

F-DFT matches simulation

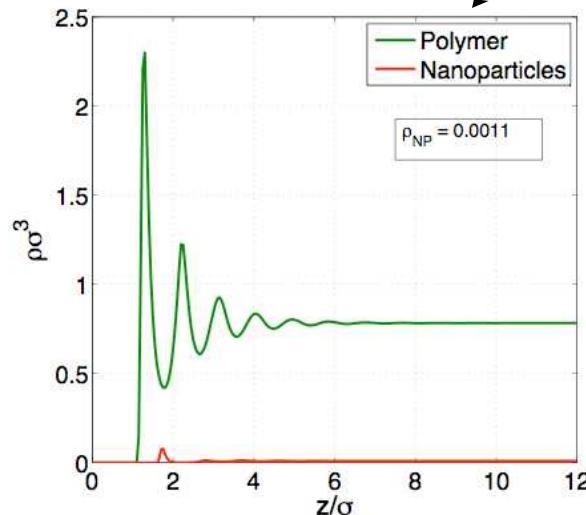
$$N = 20, D = 2\sigma$$



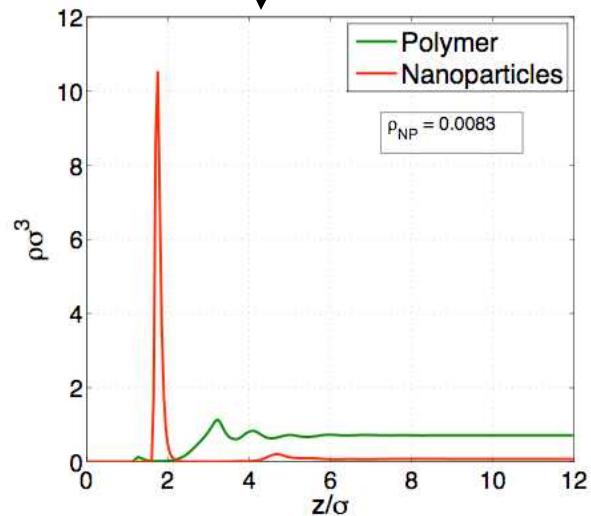
Layering Transitions

$N = 20, D=2\sigma$

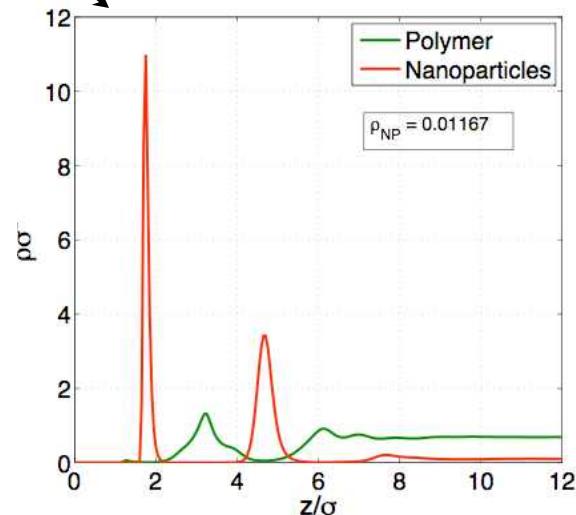
no layers



1 layer

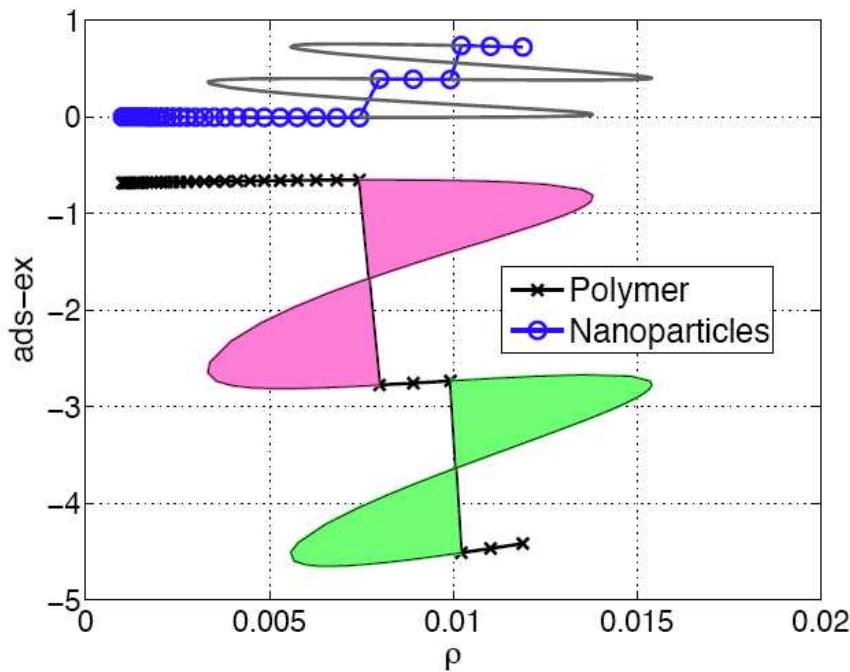


2 layers

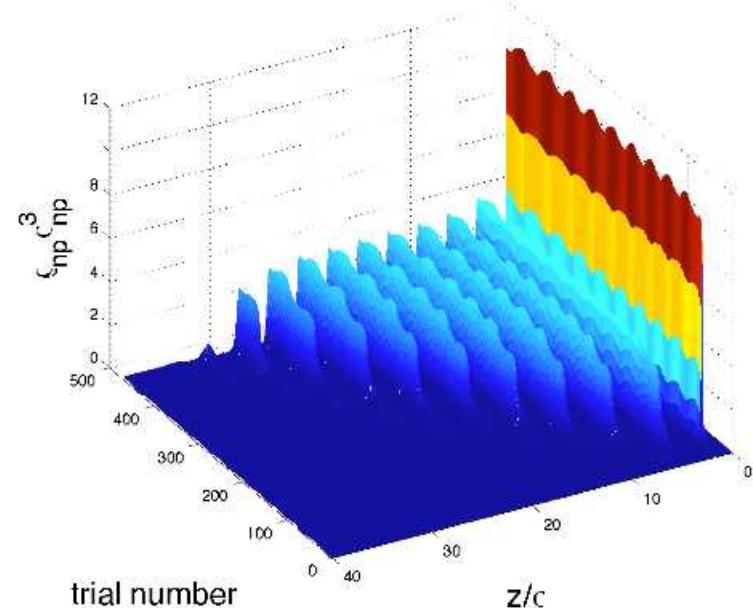


Layering

Excess adsorptions



Particle Densities





This is a polymer effect!

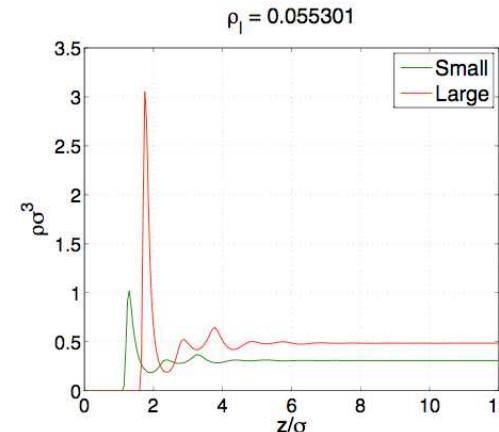
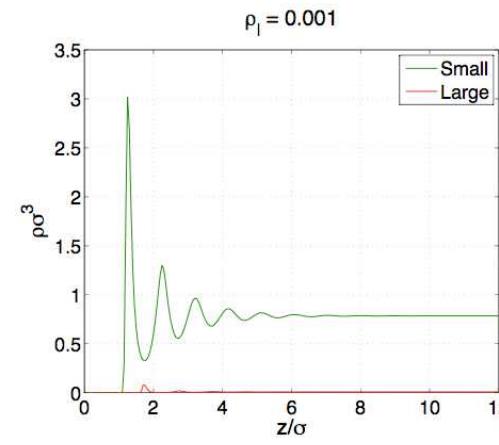
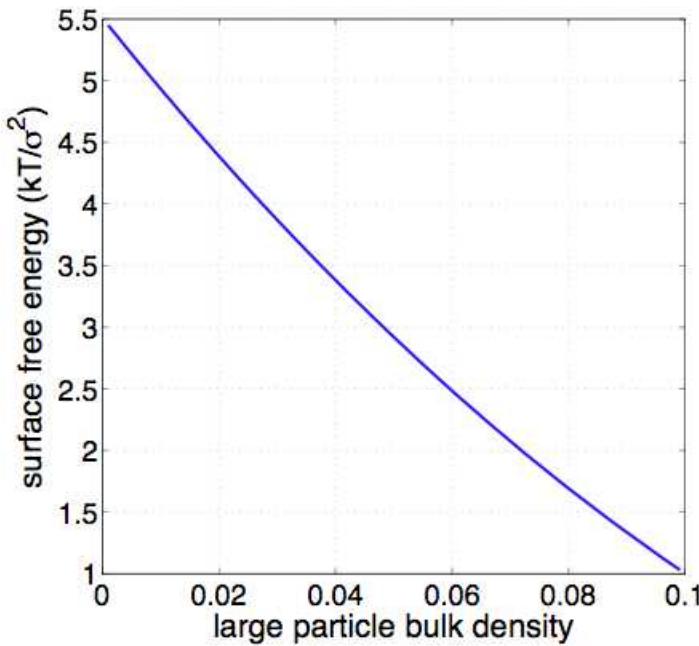
binary hard sphere mixture



$$D_s = 1\sigma$$

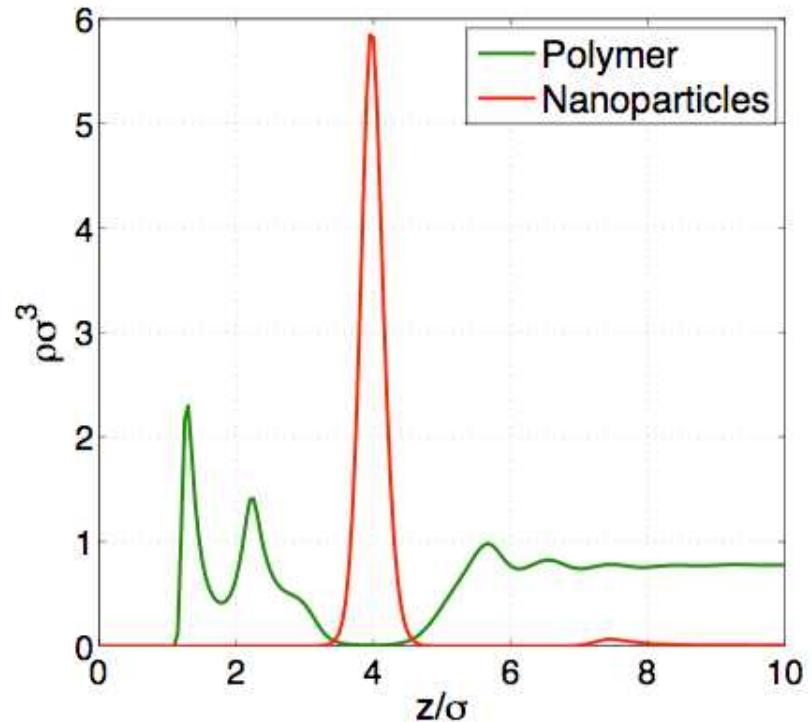
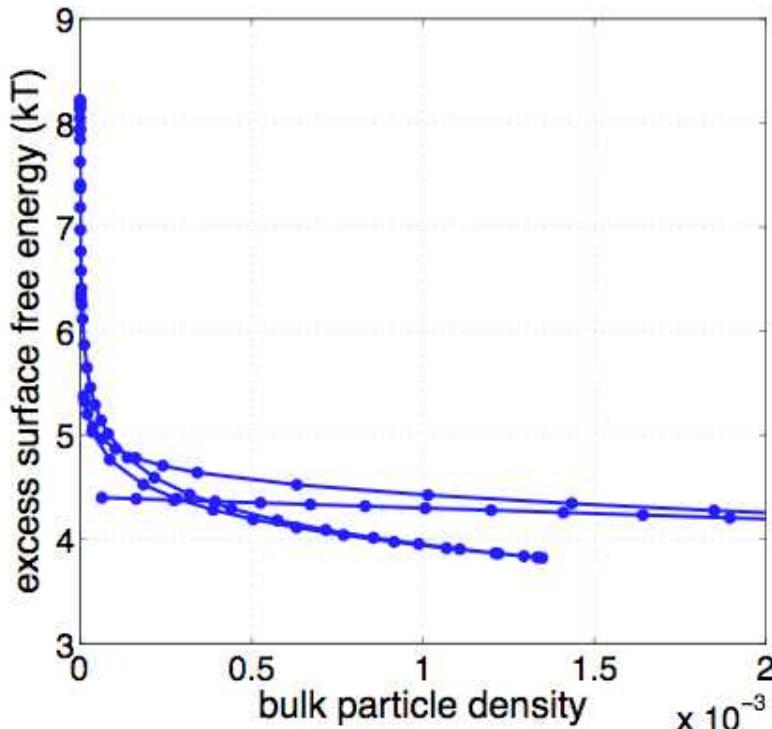
$$D_b = 2\sigma$$

no phase transition:



Larger Particles

$$N = 20, D = 2.5\sigma$$



- ongoing study
- effects of attractions?



Summary

- nanorods
 - brush profiles similar to scaling
 - attractions for $P > N$
 - repulsions for $P = N$ despite some desorption
- nanoparticle/polymer films
 - DFT appears accurate compared to MD
 - first-order layering transitions
 - polymer effect



Thanks

Collaborators

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CINT



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