

# Salado Flow Modeling in WPP Performance Assessment

## KHNP Training Program Module 6: Assembly of a Safety Case

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**Martin B. Nemer  
Sandia National Laboratories  
Carlsbad Programs Group**

**SAND 2007-XXXP**



# Outline

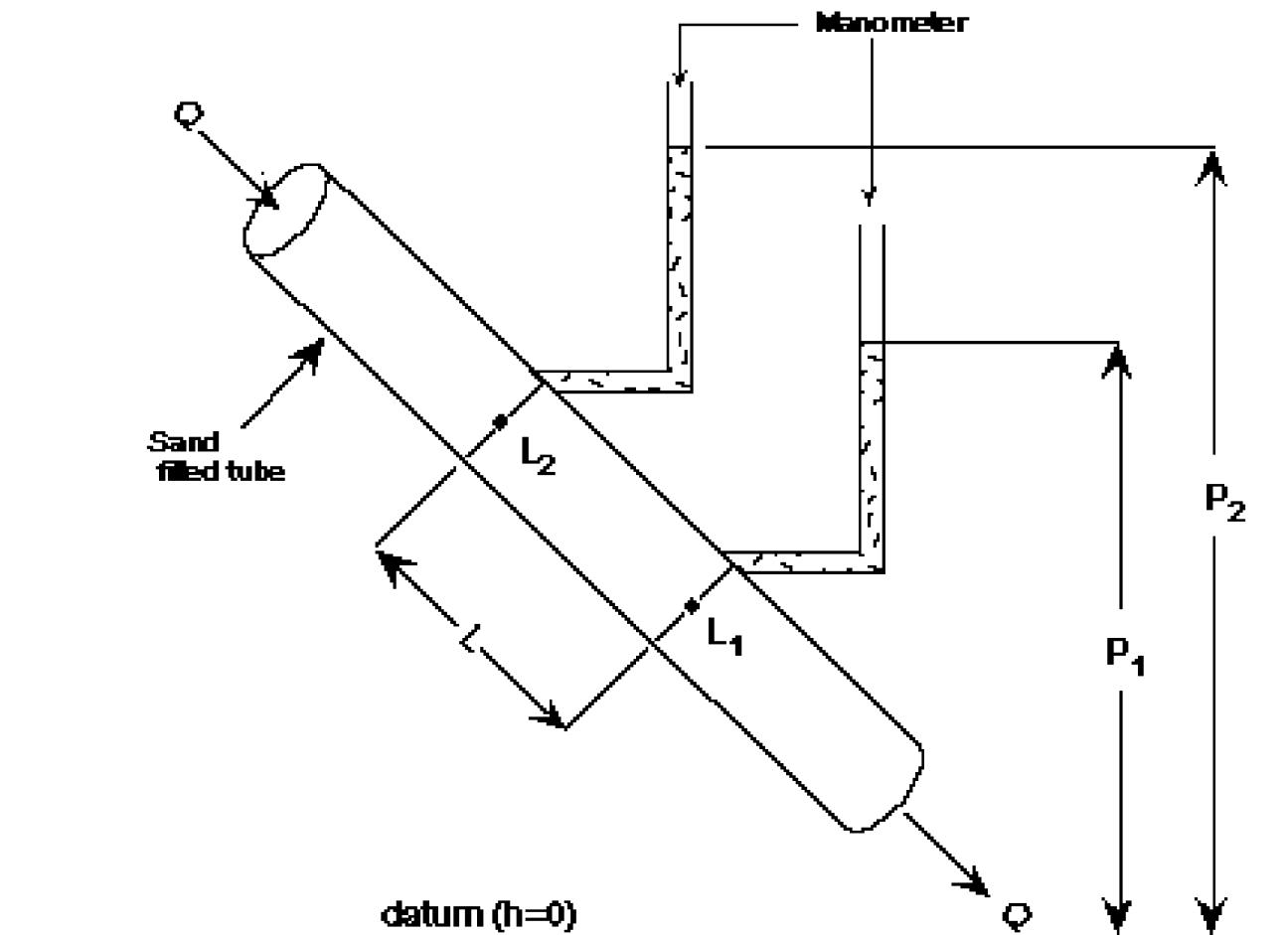
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- I. Introduction to Two-Phase Porous Media Flow**
- II. Description of Conceptual Model**
- III. Numerical Implementation**
- IV. PABC Results**



# Introduction to Two-Phase Porous Media Flow

# Darcy's Experiment



TRI-6042-0876-0



## Darcy's Law

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$$q = \frac{-k\rho}{\mu} (\nabla P + \rho g \nabla h)$$

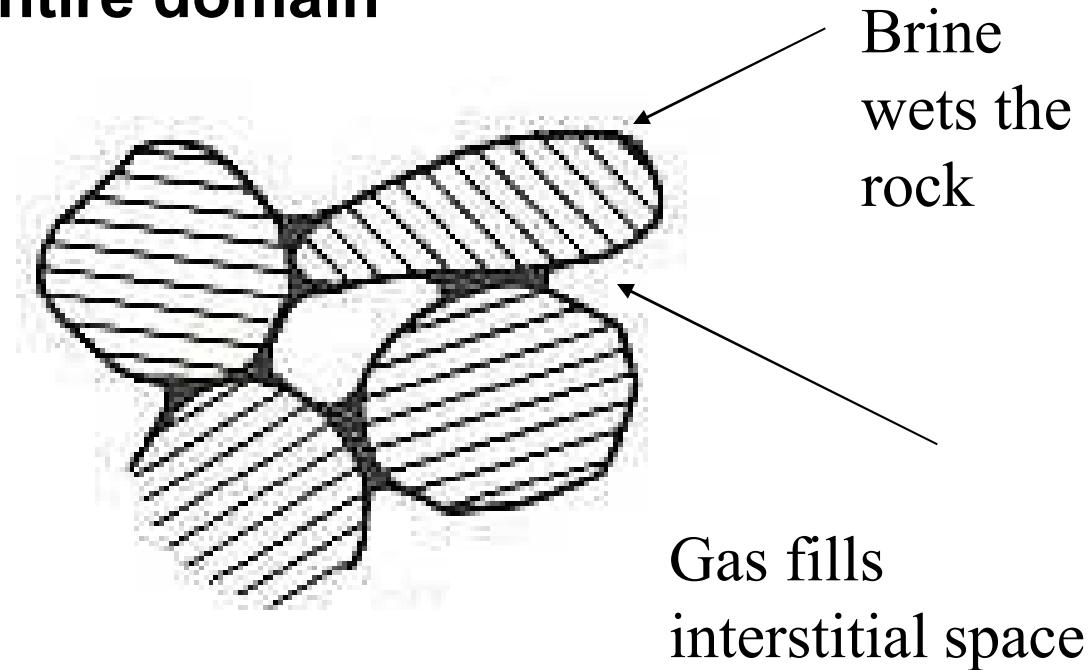
- $q$  = **mass flow rate per unit of crossectional area**
- $k$  = **permeability**
- $A$  = **cross-sectional area**
- $\mu$  = **viscosity**
- $P$  = **pressure**
- $\rho$  = **density**
- $g$  = **gravitational acceleration**
- $h$  = **height above reference point**



# Two Phase Porous Media Flow

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- **Assumption: two immiscible continuous phases occupy the entire domain**





## Two Phase Porous Media Flow

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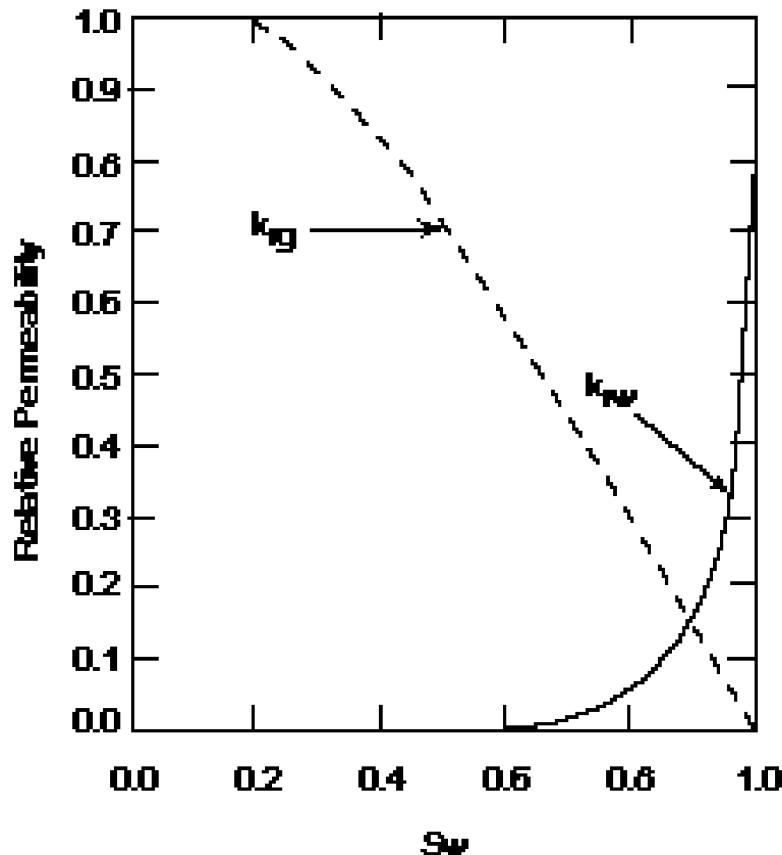
$$q_{brine} = -\frac{kk_b\rho_b}{\mu_b}(\nabla P_b + \rho_b g \nabla h).$$

$$q_{gas} = -\frac{kk_g\rho_g}{\mu_g}(\nabla P_g + \rho_g g \nabla h).$$

- $k_{brine}$  = **relative brine permeability**
- $k_{gas}$  = **relative gas permeability**

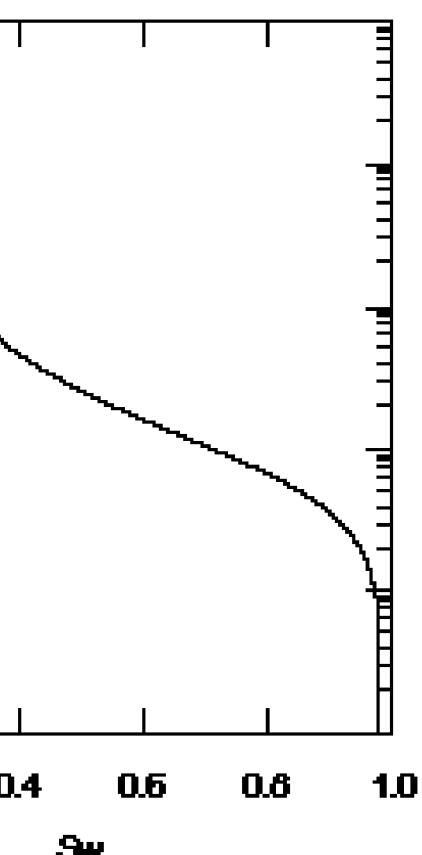


# Capillary Pressure and Relative Permeabilities: van Genuchten-Parker Model



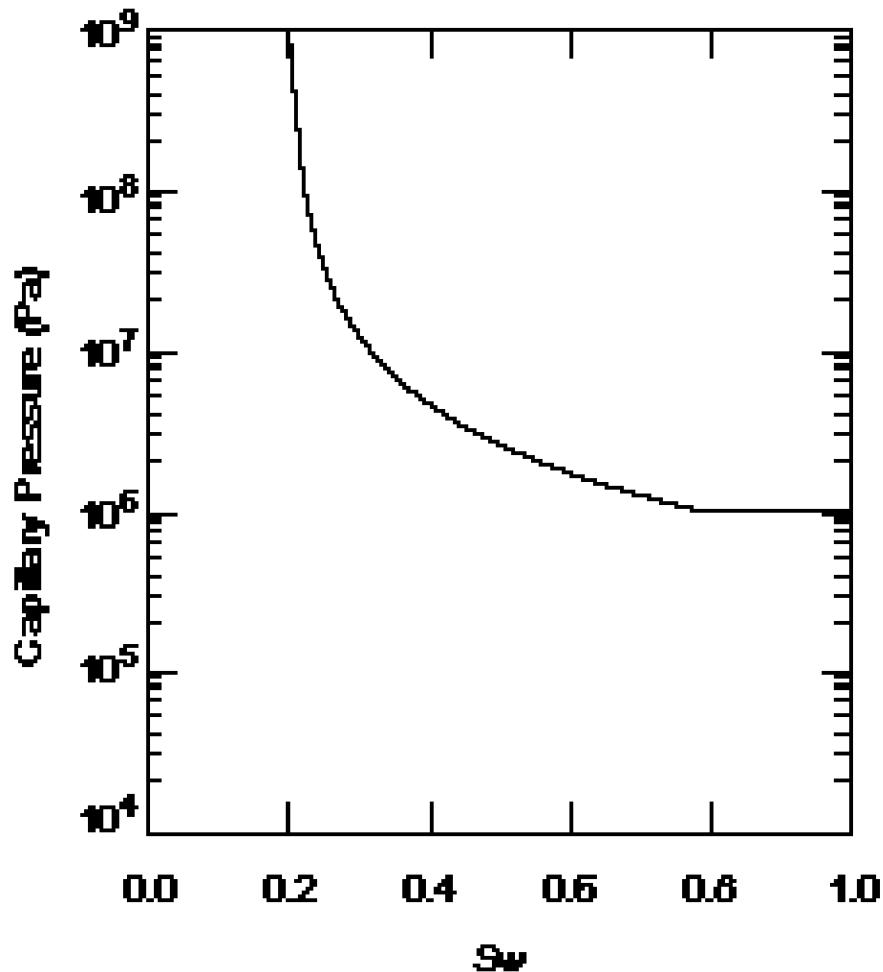
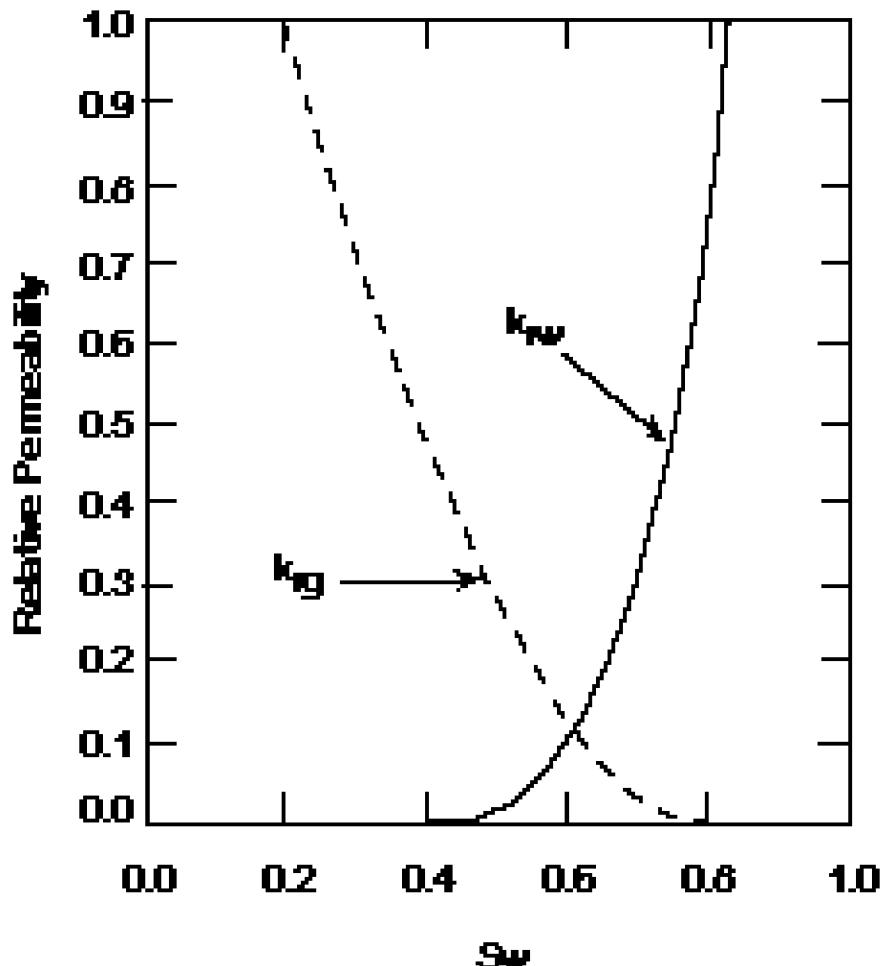
$S_w$  = brine saturation

TRI-6042-0870-0(a)



TRI-6042-0870-1(b)

# Brooks-Corey Model





# Conservation of mass

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$$\nabla \bullet q_{brine} + q_{sb} = \frac{\partial (\phi \rho_b S_b)}{\partial t}$$
$$\nabla \bullet q_{gas} + q_{sg} = \frac{\partial (\phi \rho_g S_g)}{\partial t}$$

- $q_{sb}$  = **source (or sink) of brine**
- $q_{sg}$  = **source (or sink) of gas**
- $\phi$  = **porosity**
- $S_b$  = **brine saturation**
- $S_g$  = **gas saturation = 1 - S<sub>b</sub>**



# Description of Conceptual Model

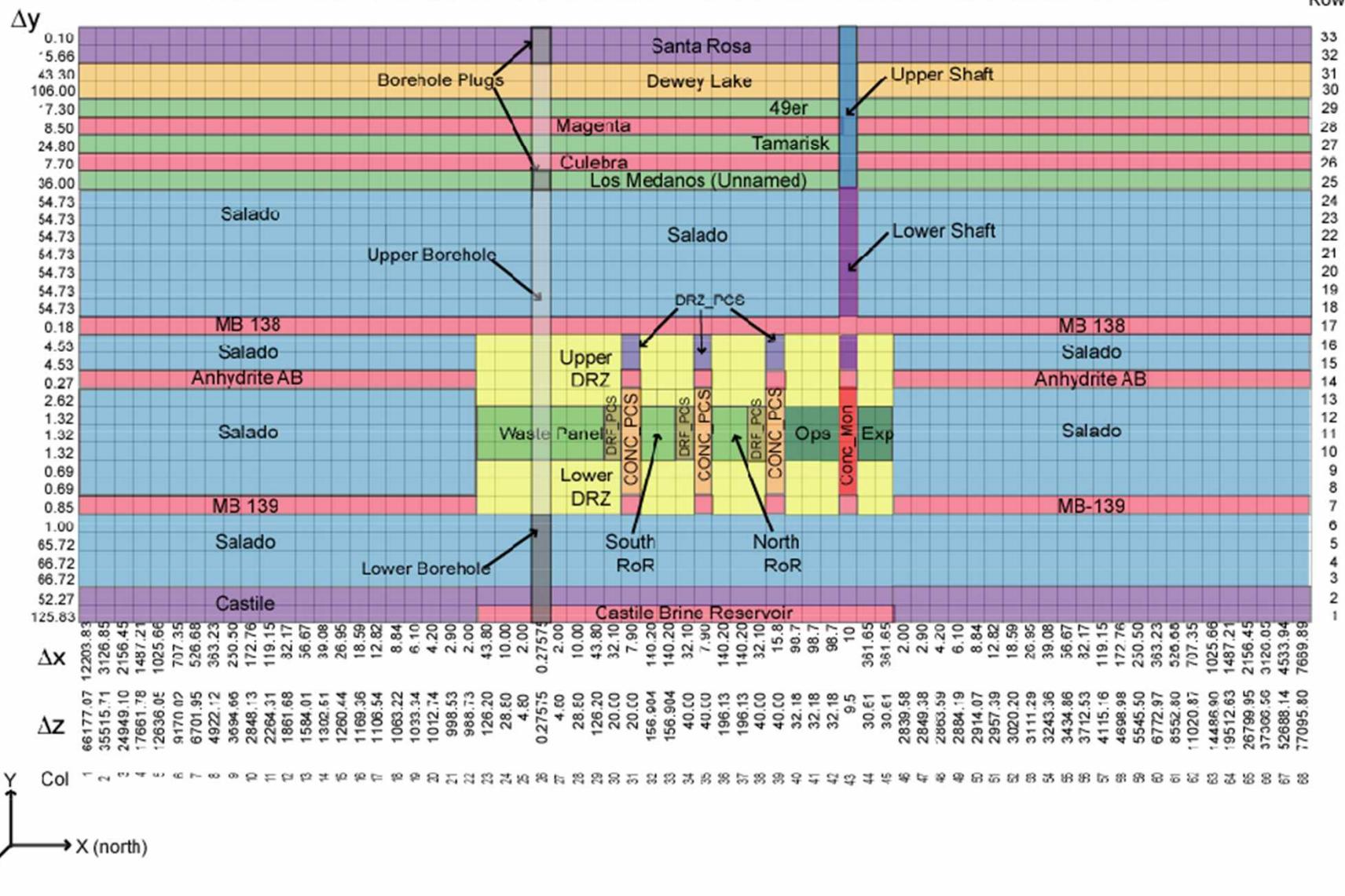


## BRAGFLO code

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- **Brine And Gas Flow (BRAGFLO)**
  - Developed by oil and gas industry pre 1980
  - Brought to Sandia with Palmer Vaughn for WIPP project
  - Simple well documented finite-element code
  - Capable of 2-D or 3-D modeling, although 3-D has never been extensively used

CRA-2004 and CRA-2004 PABC BRAGFLO Grid





# Key Geometric Assumptions

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- **Two Dimensional Grid with flaring adequately predicts flow**
- **Single (down-dip) panel models what would happen in any given panel**
- **Single borehole into a waste panel can be used to adequately model multiple intrusions**
- **Remainder of repository can be modeled as a two large areas**



# Conceptual Model

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- **Geology is defined by the: Santa Rosa, Dewey Lake, Rustler, Salado, Castile**
- **Culebra is the only unit of the Rustler that is allowed flow**
- **Anhydrite marker beds in the Salado above and below the repository: MB138, AB, MB139**
- **Disturbed Rock Zone (DRZ) remains permeable for 10,000 years**
- **Waste filled areas remain permeable for 10,000 years**



# Modeled Permeabilities

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Unit	Permeability (m <sup>2</sup> )
Santa Rosa	$10^{-10}$
Dewey Lake	$10^{-16}$
Culebra	$10^{-13}$
Anhydrite Marker Beds	$10^{-19}$
DRZ	$10^{-17}$
Intact Halite	$10^{-23}$
Waste Area	$10^{-13}$
Borehole (sand)	$10^{-14}$
Castile	$10^{-12}$



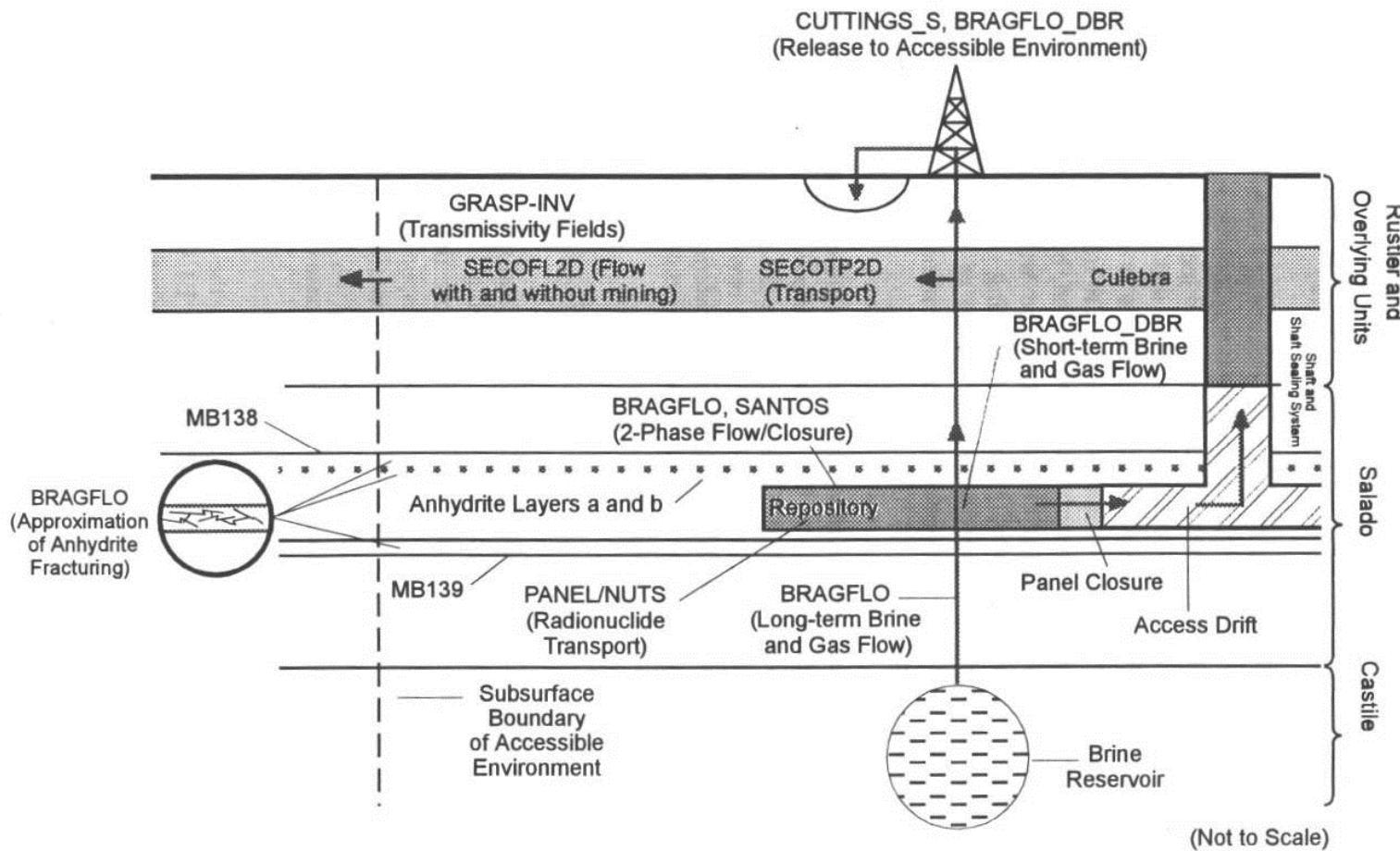
## Shaft Seals

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- Portion of the Shaft that resides in the Salado is assumed to undergo significant permeability decrease after 200 years due to salt healing
- SHFTL\_T1  $k = 10^{-18}$
- SHFTL\_T2 (200 years after closure)  $k = 10^{-20}$

**“Analysis Report for Development of a Simplified Shaft Seal Model for the WIPP Performance Assessment,” James (2003), ERMS 525203**

# Intrusion Scenarios



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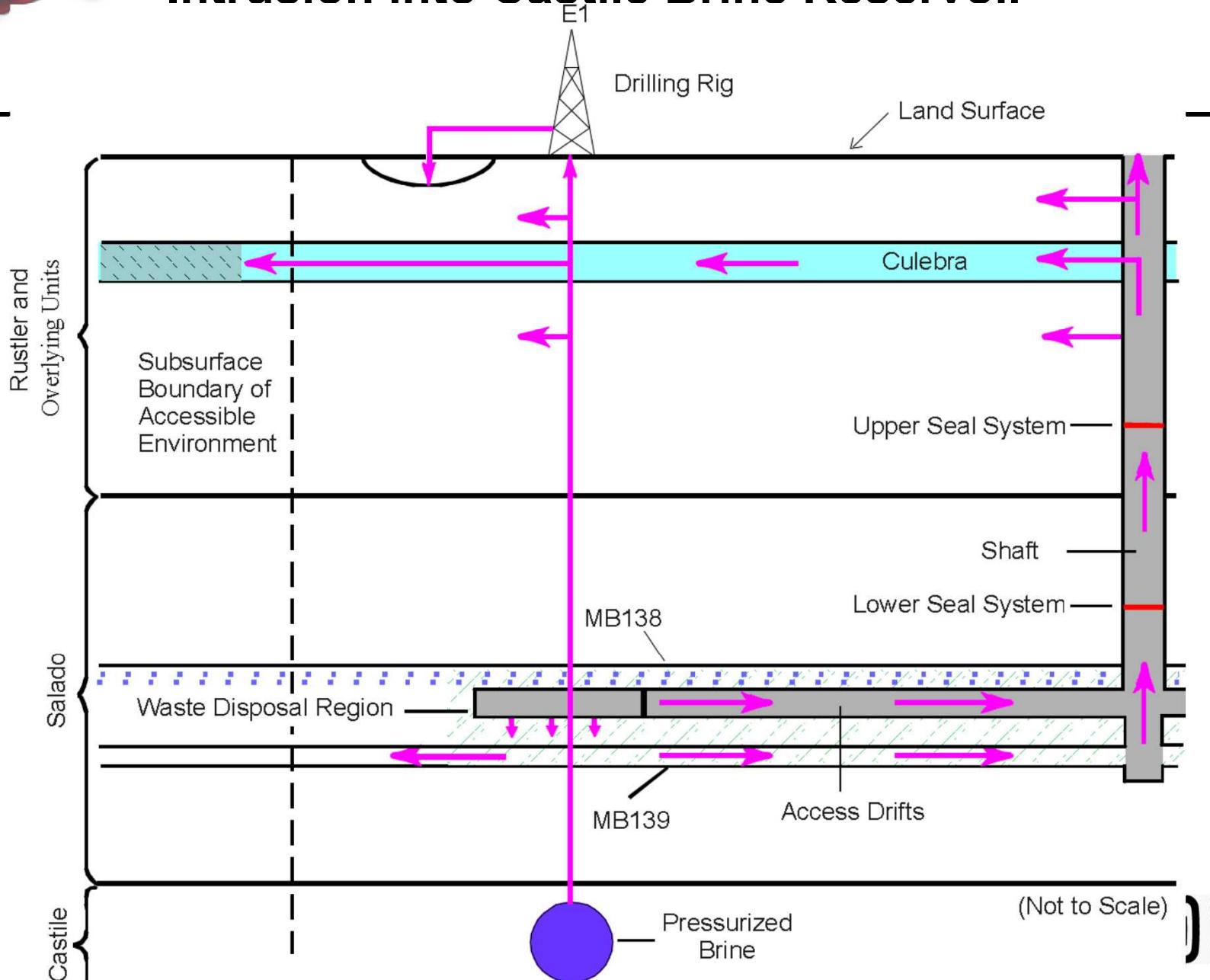
# Intrusion Scenarios

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- **Undisturbed Scenario**
  - No drilling events into the repository
- **Disturbed Scenario**
  - Predict consequences if someone were to drill through the repository looking for oil or gas
    - Hit a Castile brine reservoir (E1 intrusion)
    - Never hit brine capable of reaching the repository (E2 intrusion)

# Disturbed Scenario Sequence: E1

## Intrusion into Castile Brine Reservoir

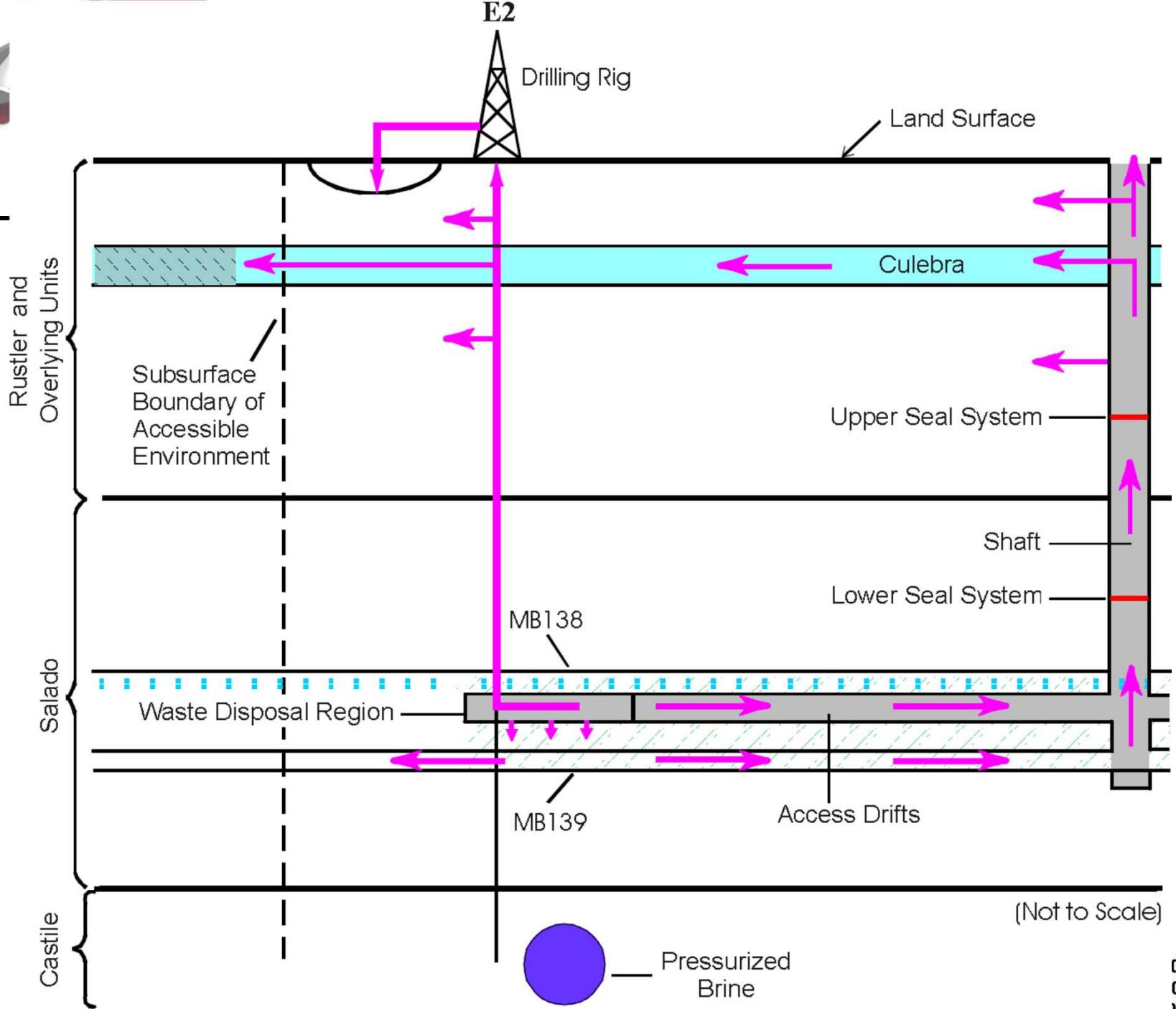


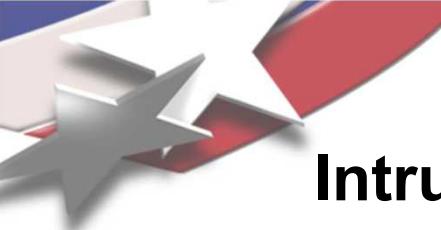


# Disturbed Scenario Sequence: E1 Intrusion into Castile Brine Reservoir

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- Borehole intrusion (E1) through the Waste Panel into a hypothetical pressurized brine reservoir in the underlying Castile Formation. Concrete borehole plugs are immediately emplaced in the borehole at the Culebra and at the surface.
- **200 years later:** Borehole plugs fail and the borehole (top to bottom) is assumed to have properties equivalent to sand (material: BH\_SAND).
- **1,000 years later:** the permeability of the borehole between the repository and the Castile Formation decreases due to creep closure of the salt (material: BH\_CREEP).



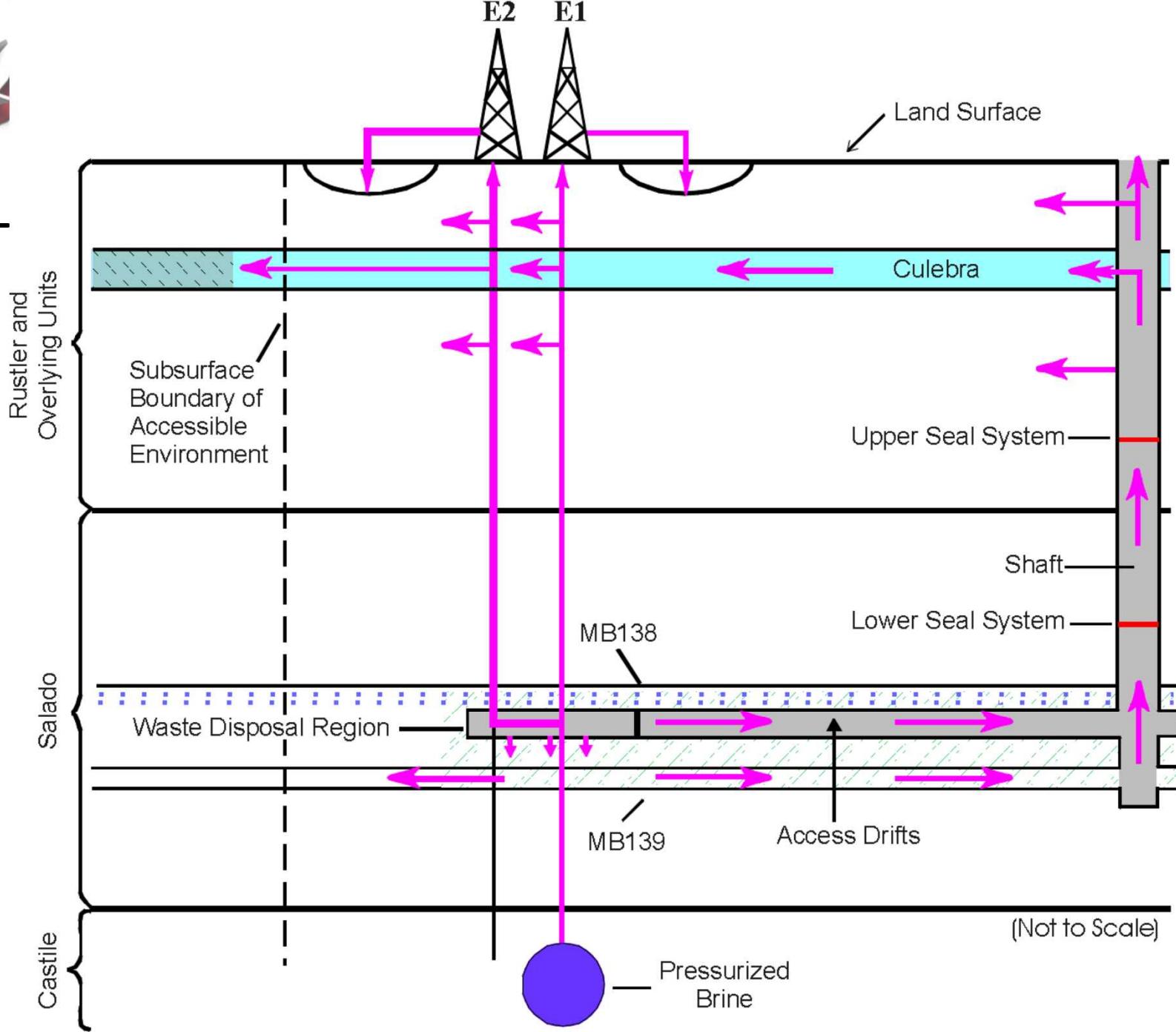


# Disturbed Scenario Sequence: E2

## Intrusion without penetrating Castile Brine Reservoir

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- **Borehole intrusion (E2) through a Waste Panel terminating at the base of the DRZ in the modeling grid (no connection to the underlying Castile Formation).** Two plugs are present in the upper part of the borehole.
- **200 years later:** Borehole plugs fail and the borehole (top to bottom) is assumed to have properties equivalent to sand (material: BH\_SAND).





# Disturbed Scenario Sequence: E2E1

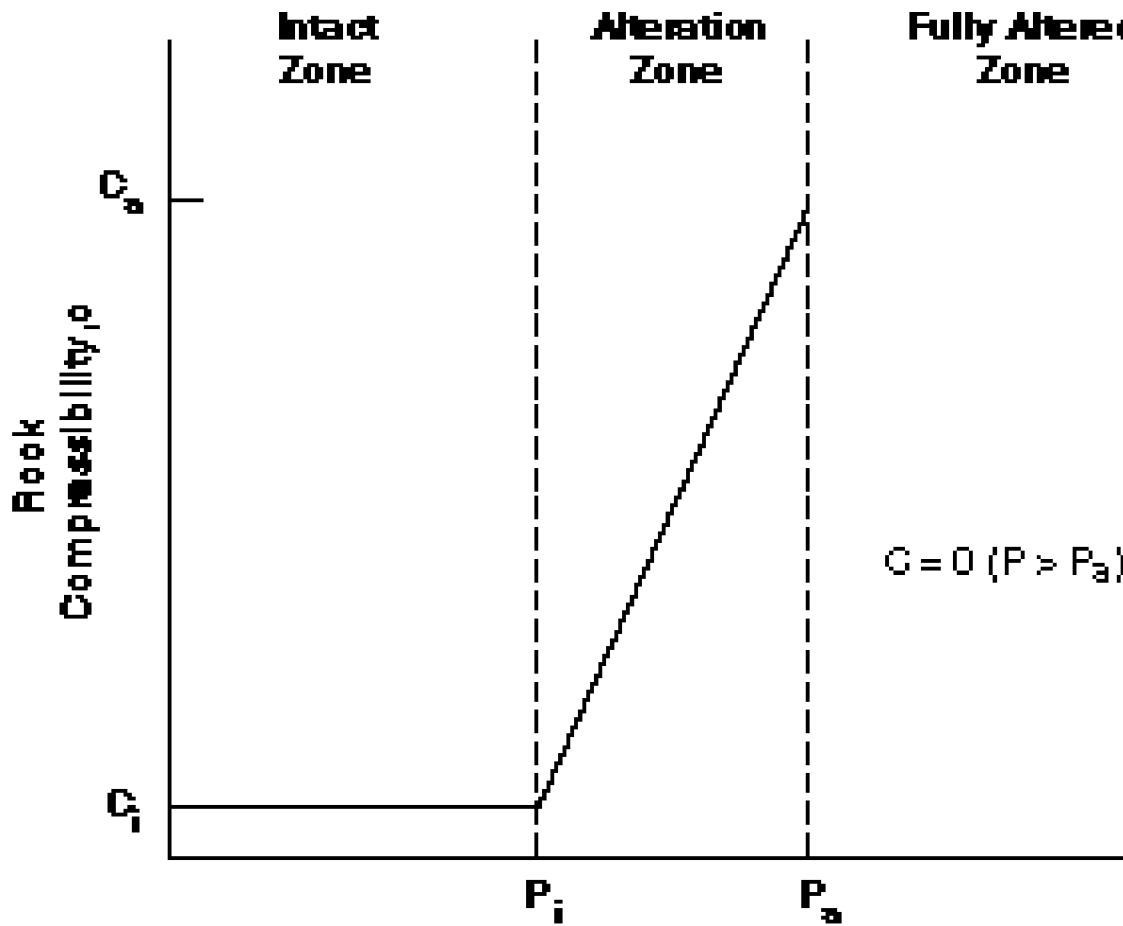
## Two Intrusions

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- Borehole intrusion (E2) through a Waste Panel terminating at the base of the DRZ in the modeling grid (no connection to the underlying Castile Formation) Borehole filled with sand.
- **1,000 years later:** borehole intrusion (E1) through a Waste Panel into a hypothetical pressurized brine reservoir in the underlying Castile Formation
- **1,200 years later:** Borehole plugs fail and the borehole (top to bottom) is assumed to have properties equivalent to sand (material: BH\_SAND).
- **2,200 years later:** the permeability of the borehole between the repository and the Castile Formation decreases due to creep closure of the salt (material: BH\_CREEP).

# Fracturing

- Rock is modeled as fractured if pressures are > lithostatic + fracture initiation pressure

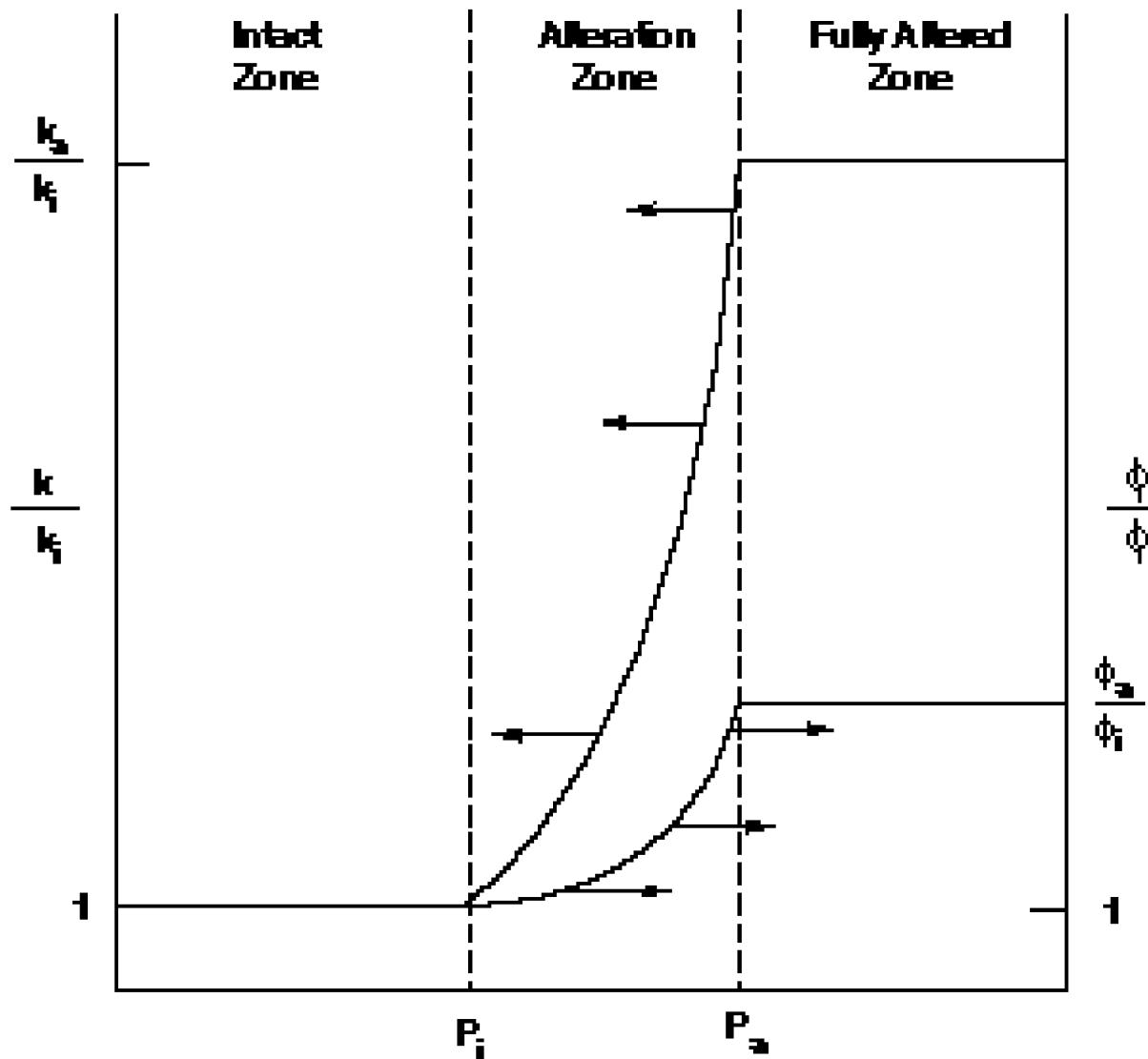


Pore Pressure

Module 6: The Safety Case

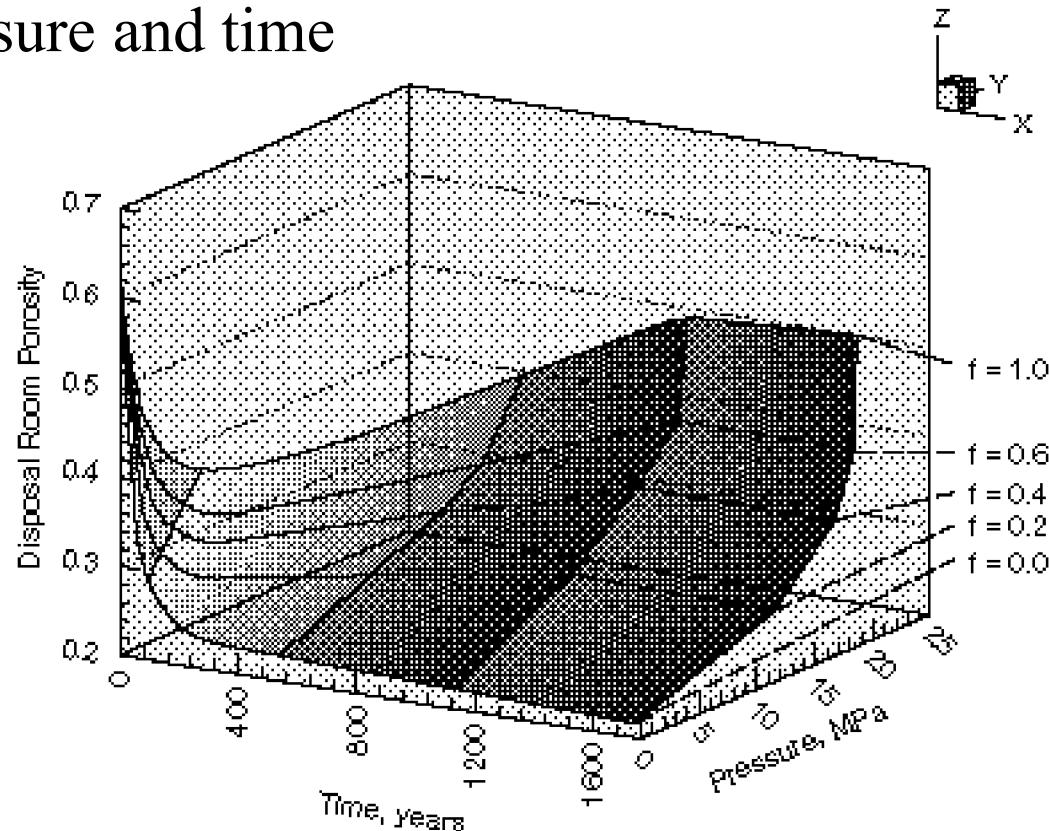
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# Fractured Rock Permeability



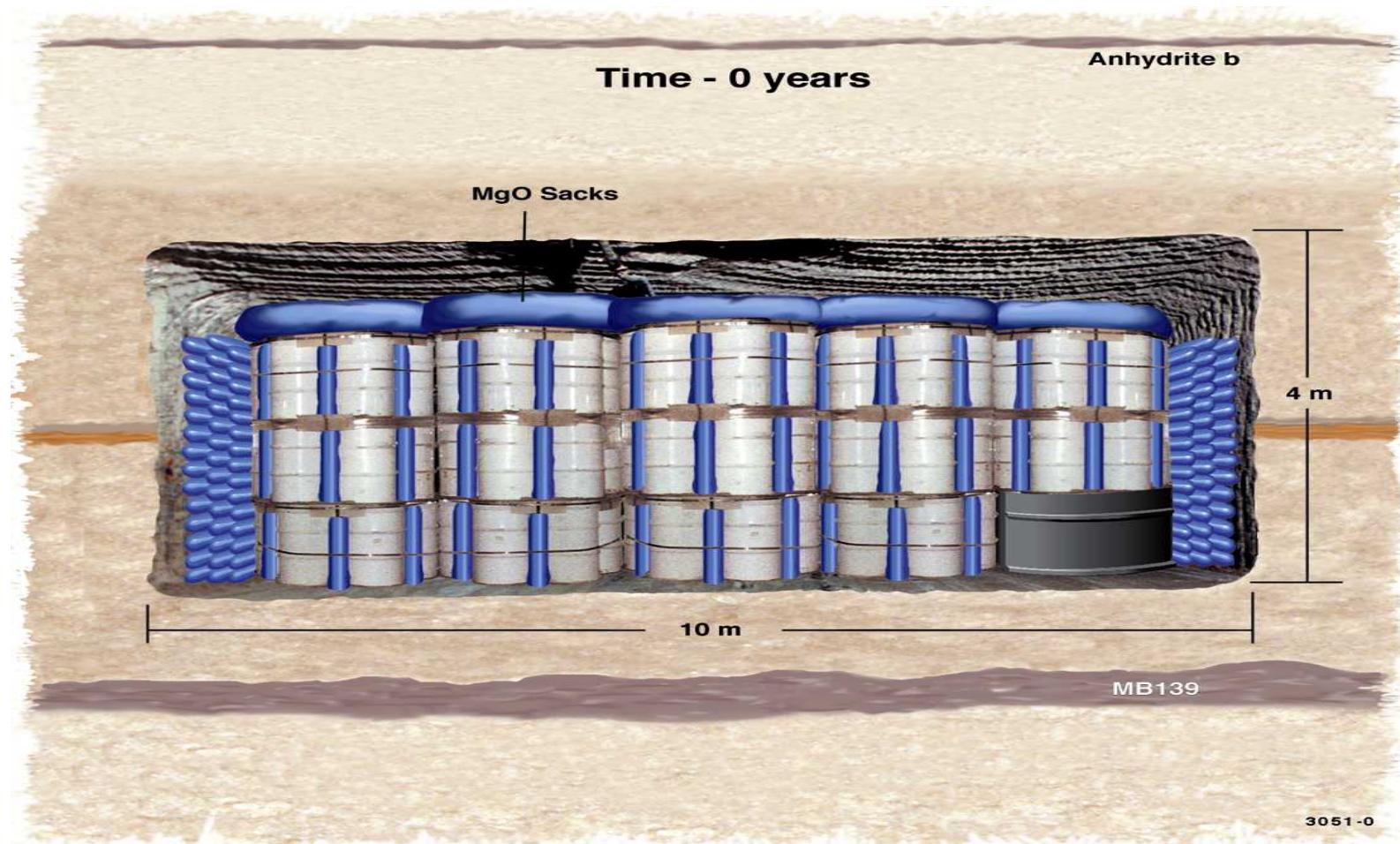
# Room closure Due to Salt Creep

- SANTOS calculates Waste Area porosity as a function of pressure and time



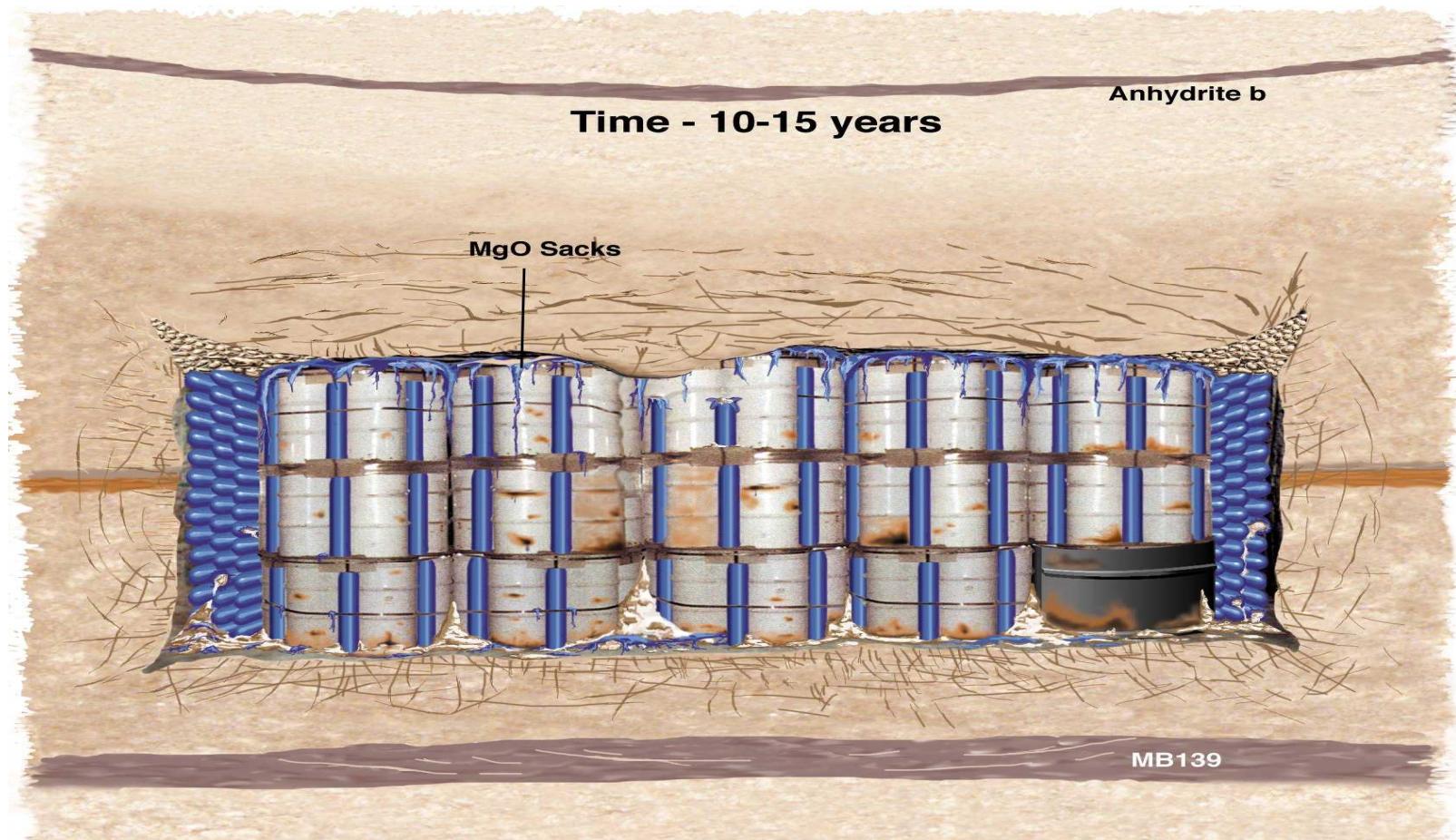
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# Room closure Due to Salt Creep: $t = 0$ y





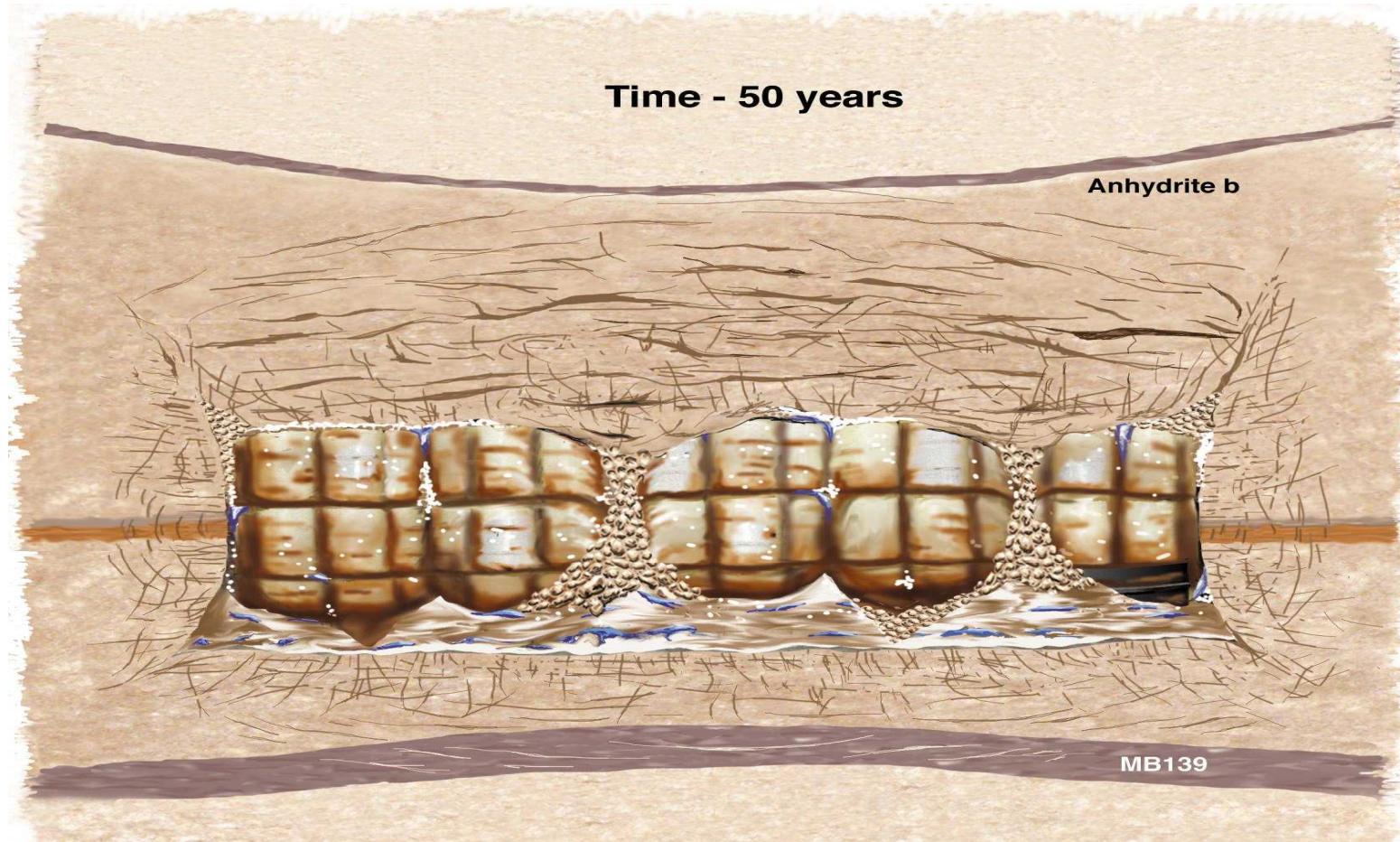
# Room closure Due to Salt Creep: $t = 15$ y



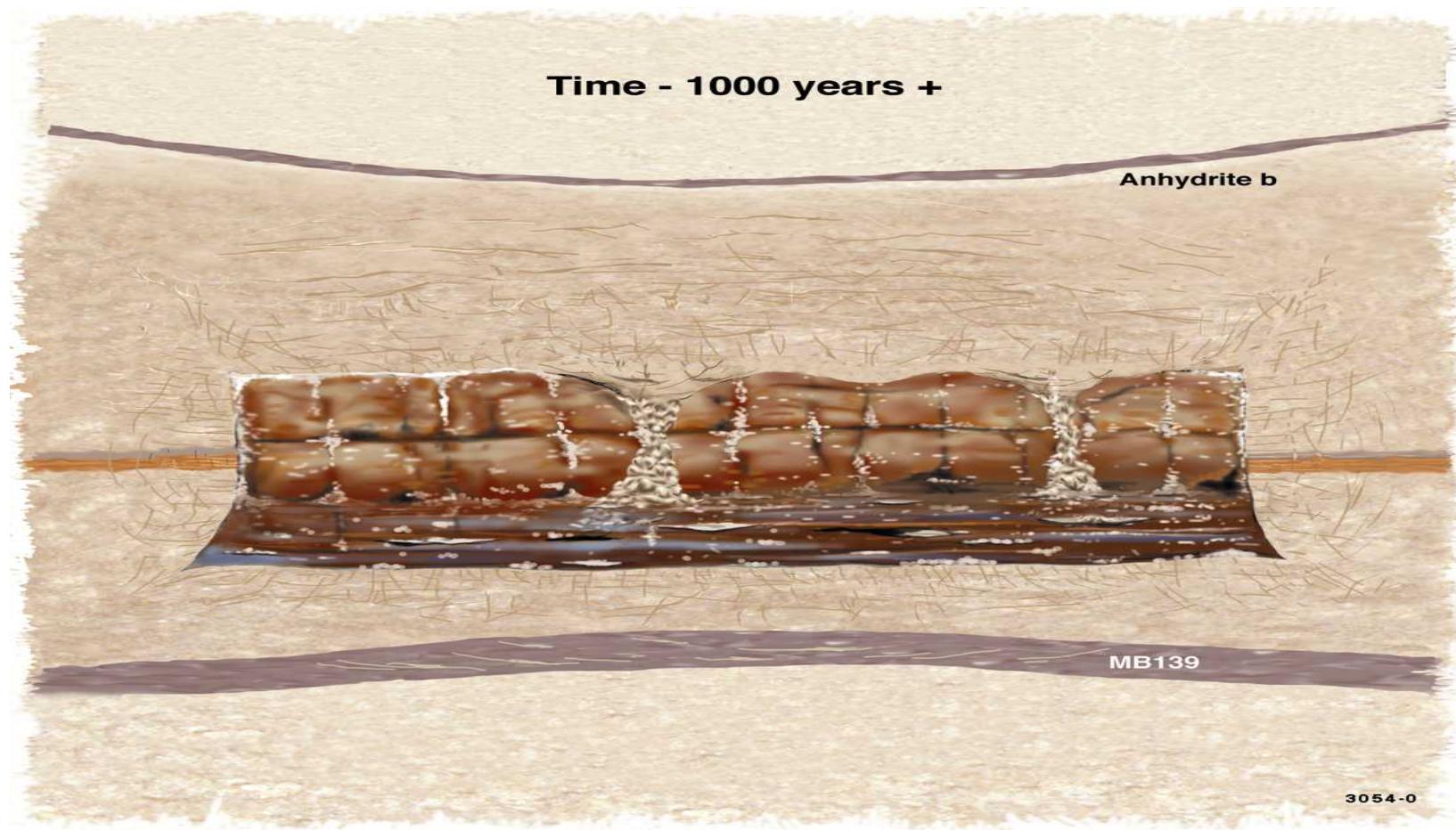


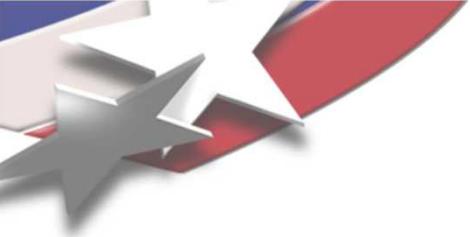
# Room closure Due to Salt Creep: $t = 50$ y

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# Room closure Due to Salt Creep: $t = 1000 + y$





# Gas Generation

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## Corrosion of Fe- and Al-base metals

- Will produce  $H_2$ , consume  $H_2O$

## Possible microbial consumption of cellulosic, plastic, and rubber (CPR) materials

- Could produce  $CH_4$ ,  $CO_2$ ,  $H_2S$ ,  $N_2$

## Alpha radiolysis of $H_2O$ in brine, and of CPR materials

- Will produce  $H_2$ ,  $O_2$ , other gases; and consume  $H_2O$

## Corrosion $\simeq$ microbial activity $>>$ radiolysis



# Gas Generation (cont.)

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## Effects of gas generation on Salado Flow

- Brine inflow and outflow
- Room closure
  - Porosity and permeability of materials in the repository, DRZ, and marker beds
  - Resistance of waste to erosion and spalling in the event of human intrusion
- Gas drives spallings releases



# Anoxic Corrosion

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**Relative importance of different types of corrosion:**

- Anoxic corrosion >> oxic corrosion

**Experimentally observed anoxic corrosion reactions**

- $\text{Fe} + (\text{x} + 2)\text{H}_2\text{O} \rightleftharpoons \text{Fe(OH)}_2 \cdot \text{xH}_2\text{O} + \text{H}_2$
- $\text{Fe} + \text{H}_2\text{O} + \text{CO}_2 \rightleftharpoons \text{FeCO}_3 + \text{H}_2$
- $\text{Fe} + \text{H}_2\text{S} \rightleftharpoons \text{FeS} + \text{H}_2$

**Other possible anoxic corrosion reactions**

- $3\text{Fe} + 4\text{H}_2\text{O} \rightleftharpoons \text{Fe}_3\text{O}_4 + 4\text{H}_2$
- $\text{Fe} + 2\text{H}_2\text{S} \rightleftharpoons \text{FeS}_2 + 2\text{H}_2$



# Microbial Activity

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**Significant microbial activity possible, but by no means certain**

**Implementation in the CCA PA, the PAVT, and the CRA-2004 PA**

- Microbial consumption of all cellulosic materials possible:
  - Probability = 0.25 (included in ~25% of the PA vectors)
- Microbial consumption of all CPR materials possible:
  - Probability = 0.25 (included in ~25% of the vectors)
- No microbial activity:
  - Probability = 0.50 (included in the other~50% of the vectors)

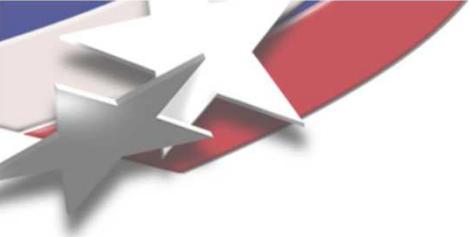


# Microbial Activity

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## Implementation in the CRA-2004 PABC

- For the PABC, the EPA stipulated that microbial activity can occur in **ALL** vectors
- However, the EPA allowed the use of lower microbial gas-generation rates based on long-term results from the laboratory study of microbial gas generation at BNL
- Furthermore, the EPA established an arbitrary factor, which can vary from 0 to 1, used to multiply the sampled value of the microbial gas generation rate
- Microbial consumption of all cellulosic materials possible:
  - Probability – 0.75 (included in ~ 75% of the PA vectors)
- Microbial consumption of all CPR materials possible:
  - Probability ~ 02.5 (included in the other ~25% of the vectors)



# Microbial Activity (cont.)

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## Potentially significant microbial respiratory pathways

- Denitrification
  - $C_6H_{10}O_5 + 4.8H^+ + 4.8NO_3^- \rightarrow 7.4H_2O + 6CO_2 + 2.4N_2$
- $SO_4^{2-}$  reduction
  - $C_6H_{10}O_5 + 6H^+ + 3SO_4^{2-} \rightarrow 5H_2O + 6CO_2 + 3H_2S$
- Fermentation and methanogenesis
  - $C_6H_{10}O_5 + H_2O \rightarrow 3CH_4 + 3CO_2$

## Implementation in PA

- Sequential use of electron acceptors
- However, the EPA has disallowed the use of methanogenesis
- Given the current inventory, denitrification will consume 4% and  $SO_4^{2-}$  reduction will consume 96% of the CPR materials in the repository if all CPR materials are consumed



# Role of MgO

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**Functions as an engineered barrier by consuming CO<sub>2</sub> from possible microbial activity, thereby decreasing actinide solubilities**

- Will react with CO<sub>2</sub> and H<sub>2</sub>O in brine and water vapor to form hydrous and, eventually, anhydrous Mg carbonates
- Will consume essentially all CO<sub>2</sub> and remove CO<sub>3</sub><sup>2-</sup> from brine
- Will buffer pH at ~9

**Consumption of significant quantities of H<sub>2</sub>O could also affect long-term performance**

**The DOE is emplacing sufficient MgO to consume all CO<sub>2</sub> that could be produced by microbial consumption of all cellulosic, plastic, and rubber (CPR) materials**



## Role of MgO (cont.)

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**DOE asserted in the 1996 Compliance Certification Application (CCA) that borehole plugs, MgO, panel closures, and shaft seals would help satisfy the EPA's assurance requirement for multiple natural and engineered barriers**

- Barriers defined as “any material or structure that prevents or substantially delays movement of water or radionuclides toward the accessible environment.” Barriers can be “... a geologic structure, a canister, a waste form, or a material placed over and around waste provided that material or structure substantially delays movement of water or radionuclides”

**MgO recognized as the only engineered barrier in the WIPP disposal system in the EPA's 1998 certification of the WIPP**



## Role of MgO (cont.)

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### Hydration of periclase to form brucite:

- $\text{MgO} + \text{H}_2\text{O} = \text{Mg}(\text{OH})_2$

### Carbonation of brucite to form hydromagnesite or magnesite

- $5\text{Mg}(\text{OH})_2 + 4\text{CO}_2 \rightleftharpoons \text{Mg}_5(\text{CO}_3)_4(\text{OH})_2 \cdot 4\text{H}_2\text{O}$ 
  - Reaction assumed to control  $f_{\text{CO}_2}$  for the actinide-solubility calculations
- $\text{Mg}(\text{OH})_2 + \text{CO}_2 \rightleftharpoons \text{MgCO}_3 + \text{H}_2\text{O}$ 
  - Likely long-term carbonation reaction

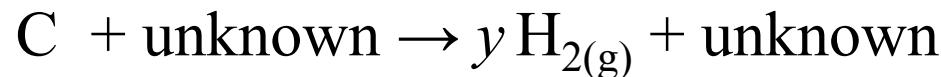
### Reaction that will buffer pH:

- $\text{Mg}(\text{OH})_2 \rightleftharpoons \text{Mg}^{2+} + 2\text{OH}^-$



# Gas Generation in BRAGFLO

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$$\frac{dM_{CPR}}{dt} = k_{CPR,I} S_B + k_{CPR,H} (1 - S_B)$$

- $k_{CPR,I}$  = Inundated CPR consumption rate
- $k_{CPR,H}$  = Humid CPR consumption rate
- $S_B$  = Brine saturation



## Gas Generation in BRAGFLO contd.

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$$\frac{dM_{Fe}}{dt} = k_{Fe,I} S_B$$

$k_{Fe,I}$  = Inundated CPR consumption rate  
 $S_B$  = Brine saturation



# Gas Generation: Wicking

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- Waste is assumed to wick water by capillarity

$$S_{eff} = S_b + S_{wick} \left( 1 - e^{\alpha S_b} \right)$$

- Gas-generating reactions use a humid and inundated rate. However with wicking, most reactions use only the inundated rate

- $S_{eff}$  = wicked saturated in the waste
- $S_{wick}$  = Sampled parameter [0 – 1]
- $\alpha$  = smoothing parameter [= -1000]

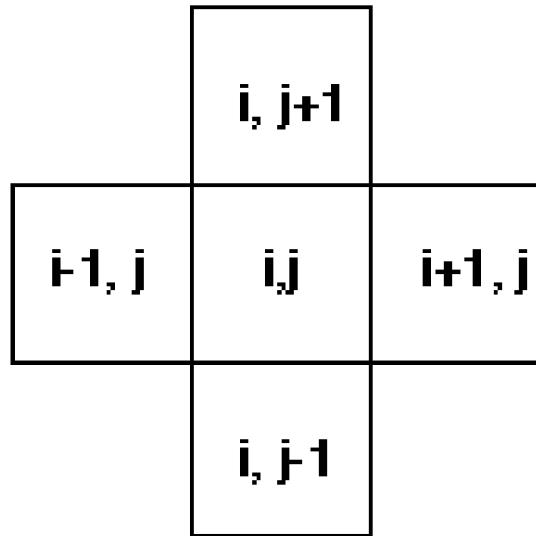


# Numerical Implementation



# Finite Difference code

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- Blocks
- Nodes
- Block interfaces

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$$f_1(x_1, x_2) = f_1(x_1^k, x_2^k) + \frac{\partial f_1}{\partial x_1} (x_1^k, x_2^k) (x_1 - x_1^k) + \frac{\partial f_1}{\partial x_2} (x_1^k, x_2^k) (x_2 - x_2^k)$$



# Upstream Weighting

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$S_g > S_{gr}$	$S_g \leq S_{gr}$
$P_{g,i}$	$P_{g,i+1}$

$x_i$                     interface                     $x_{i+1}$

$$k_{\text{interface}} = \begin{cases} k_{i+1}, & P_i < P_{i+1} \\ k_i, & \text{otherwise.} \end{cases}$$



## Implicit Time Stepping

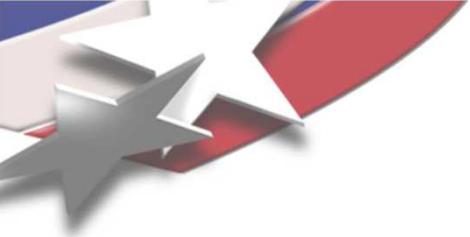
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$$\frac{\partial \hat{x}}{\partial t} = g(\hat{x})$$

$$\frac{\Delta \hat{x}}{\Delta t} = g(\hat{x}_{t+\Delta t}) \approx g(\hat{x}_t) + \frac{\partial g}{\partial \hat{x}} \Delta x$$

BRAGFLO calculates the Jacobian numerically

$$J(\hat{x}) = \frac{\partial g}{\partial \hat{x}}$$



## Netwon's Method

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$$F = \left\{ \nabla \bullet q_{brine} + q_{sb} = \frac{\partial(\phi \rho_b S_b)}{\partial t}, \nabla \bullet q_{gas} + q_{sg} = \frac{\partial(\phi \rho_g S_g)}{\partial t} \right\}$$

$$F(\hat{x}^k) = 0$$

$$\hat{x} = \{P_b, S_g\}$$

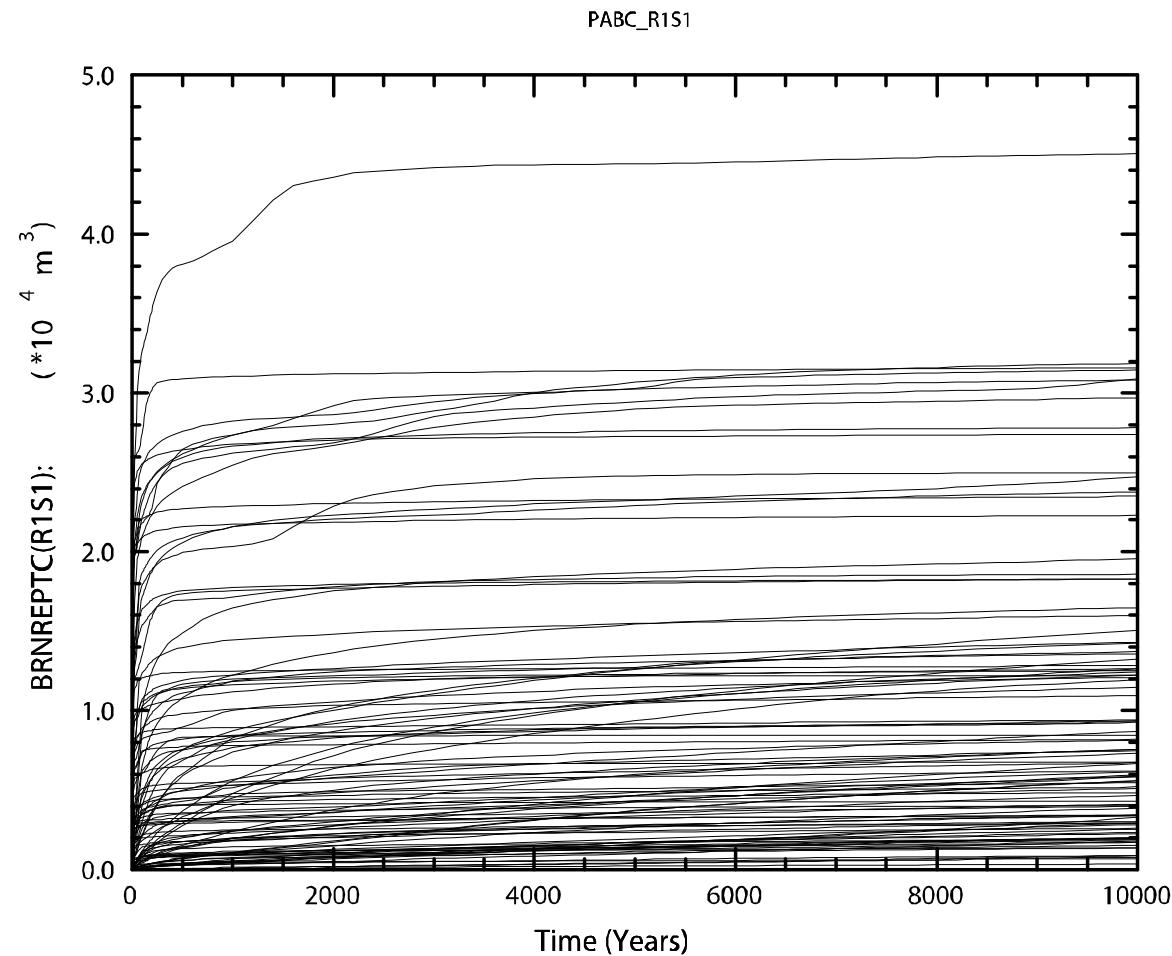
$$\hat{\mathbf{x}}^{k+1} = \hat{\mathbf{x}}^k + \delta \hat{\mathbf{x}}.$$

$$\delta \hat{\mathbf{x}} = -\mathbf{J}^{-1}(\hat{\mathbf{x}}^k) \mathbf{F}(\hat{\mathbf{x}}^k)$$



# PABC Results

# Undisturbed: Brine flow into Repository



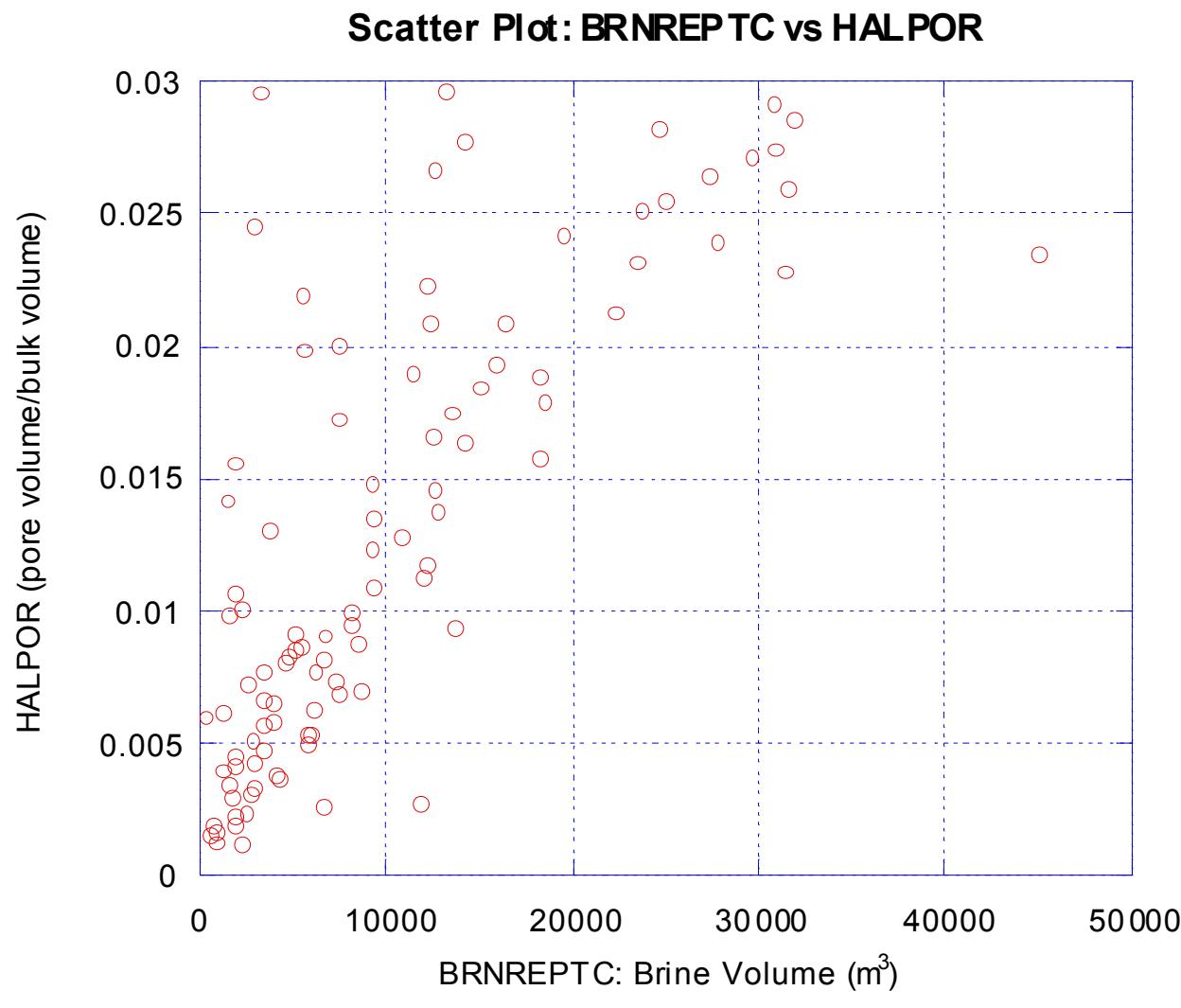
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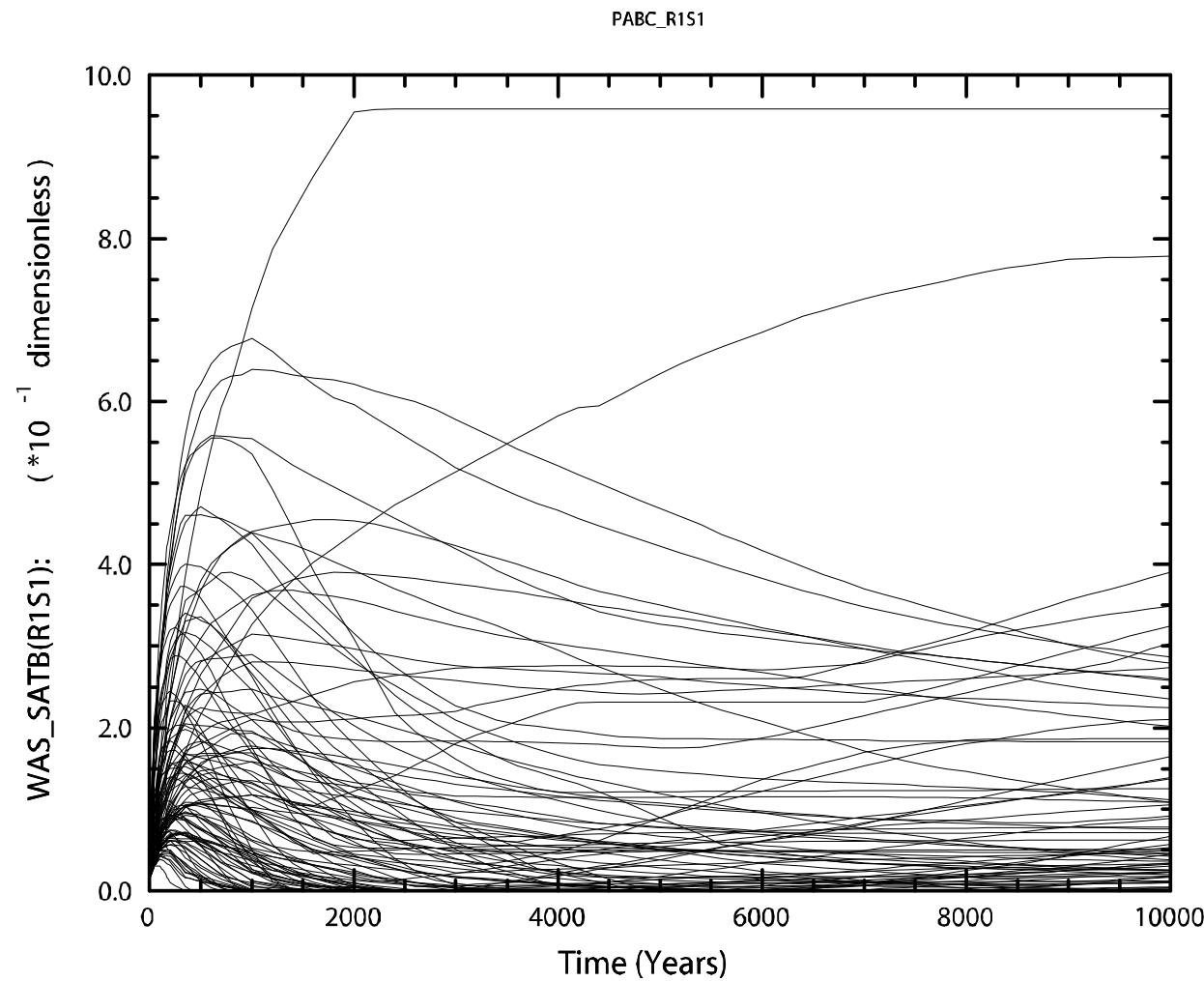
a) PABC

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# Undisturbed: Brine is coming from the DRZ



# Undisturbed: Brine Saturation



SPLAT\_PABC\_R1S1\_WAS\_SATB.CMD;1

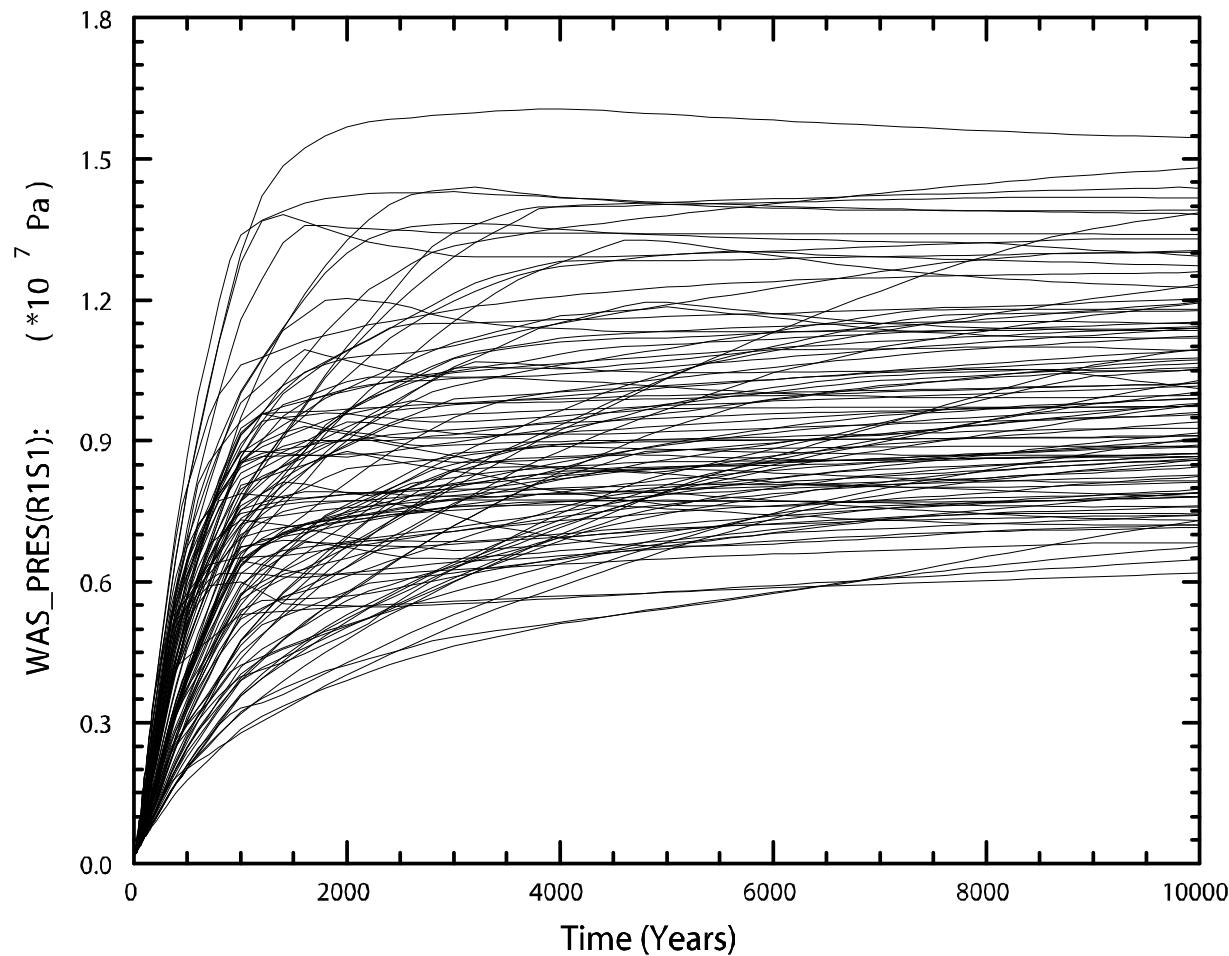
SPLAT\_PA96\_2 1.02 06/06/05 10:13:09

a) PABC

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# Undisturbed: Pressure

PABC\_R1S1



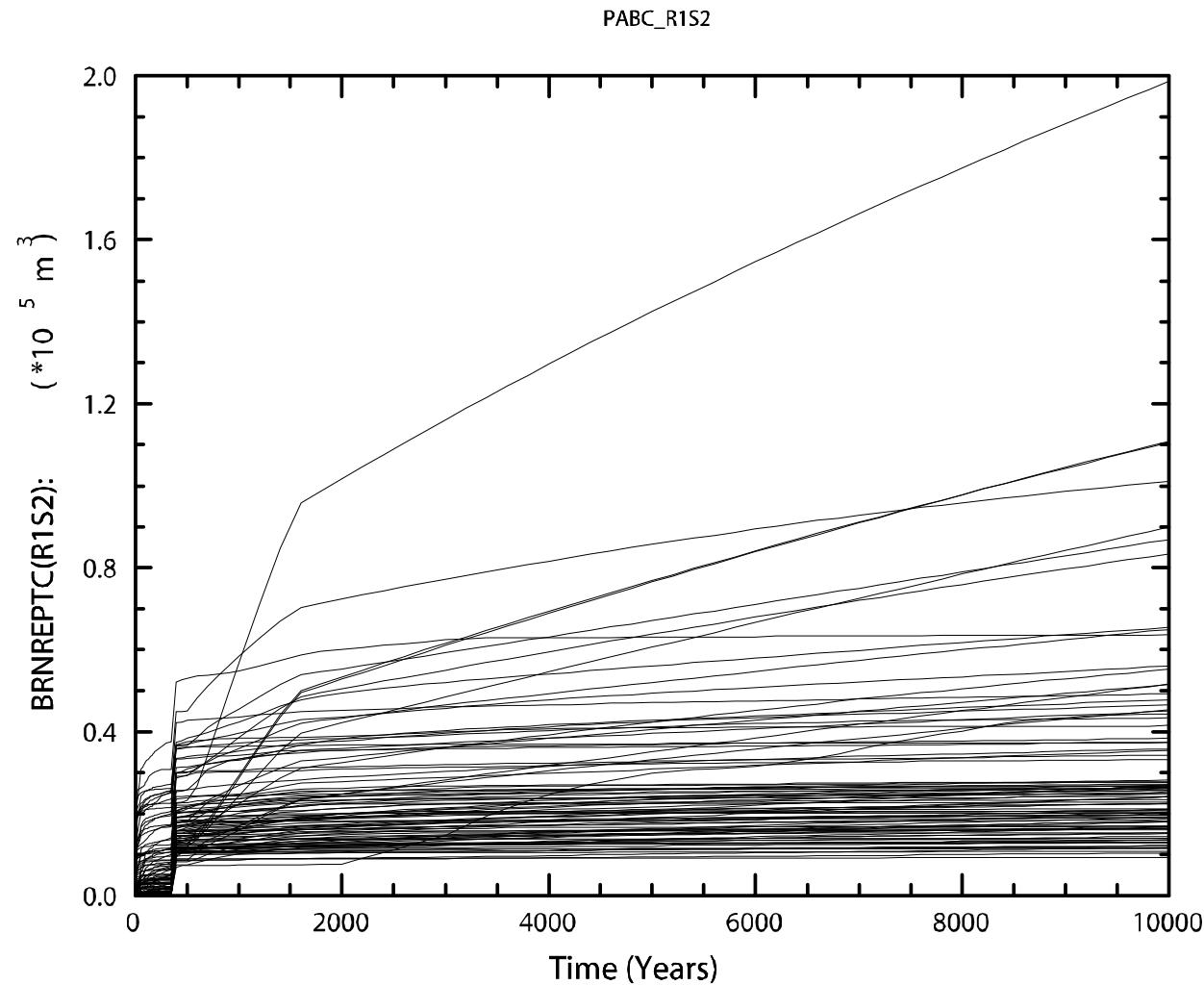
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SPLAT\_PA96\_2 1.02 06/06/05 10:12:25

a) PABC

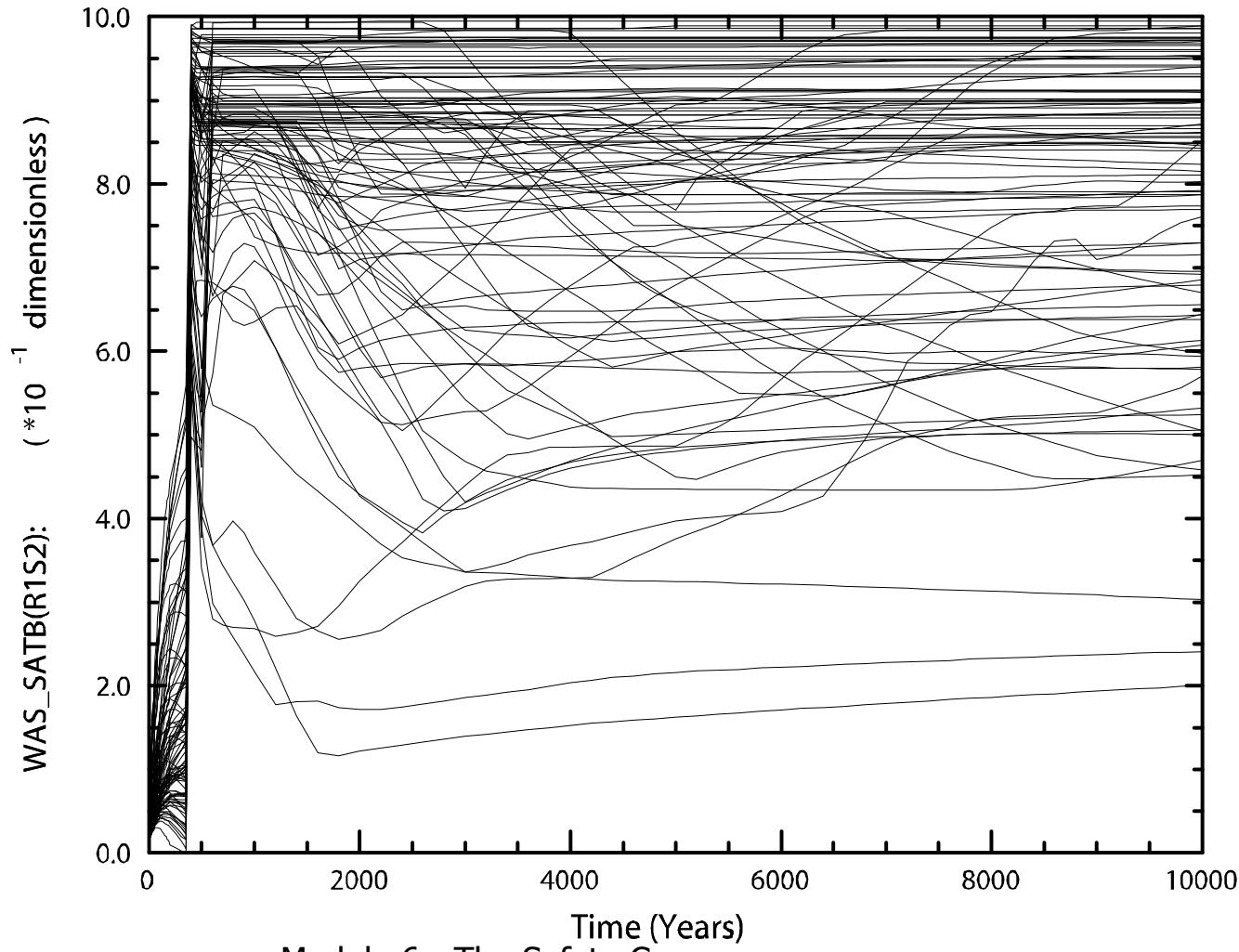
Module 6: The Safety Case

# Disturbed E1: Brine Inflow into Repository



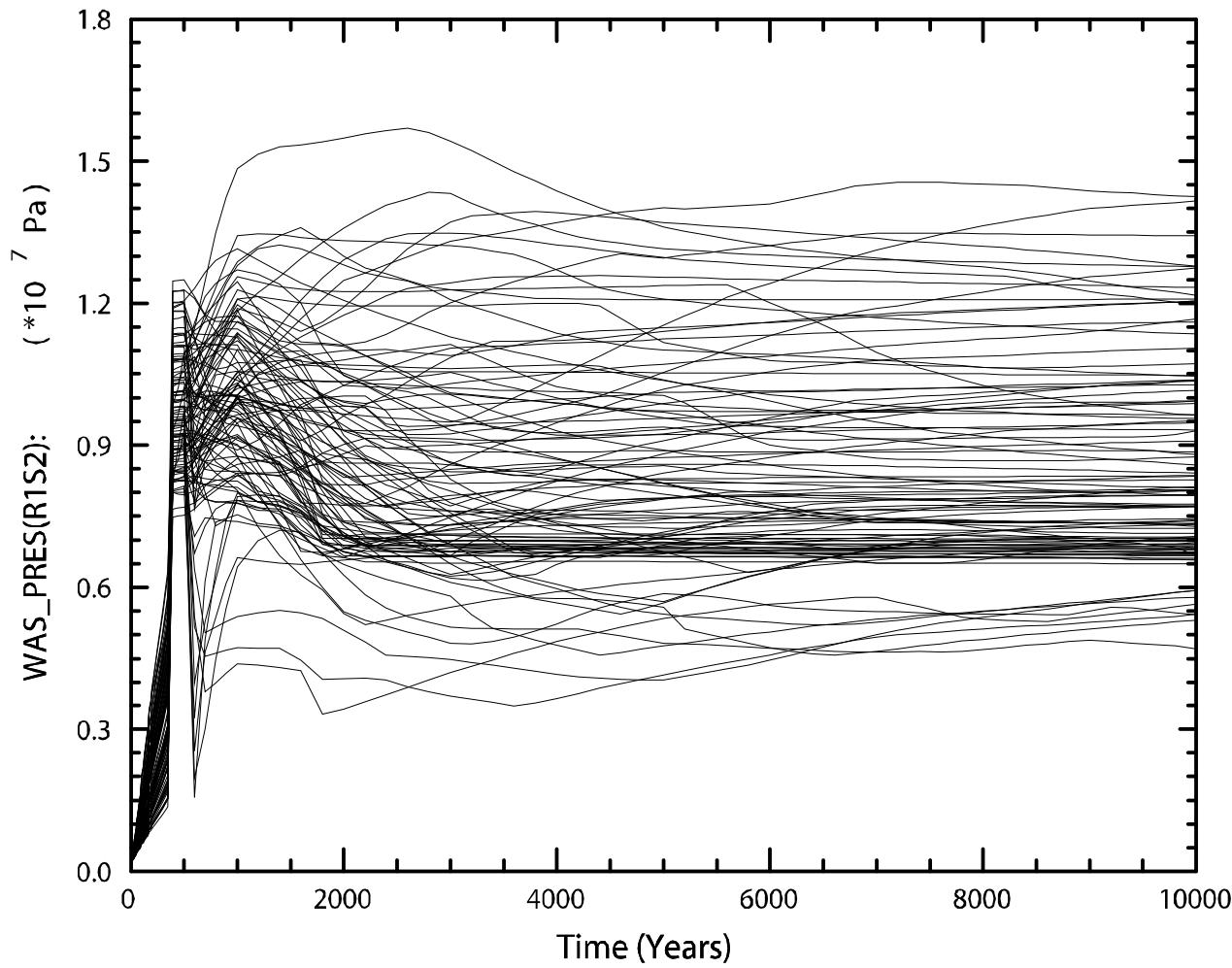
# Disturbed E1: Brine Saturation

PABC\_R1S2



# Disturbed E1: Pressure

PABC\_RTS2



SPLAT\_PABC\_RTS2\_WAS\_PRESS.CMD;1

SPLAT\_PA96\_2 1.02 06/06/05 11:30:34

a) PABC

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