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# **Low Frequency Turbulence in a High Beta Plasma**

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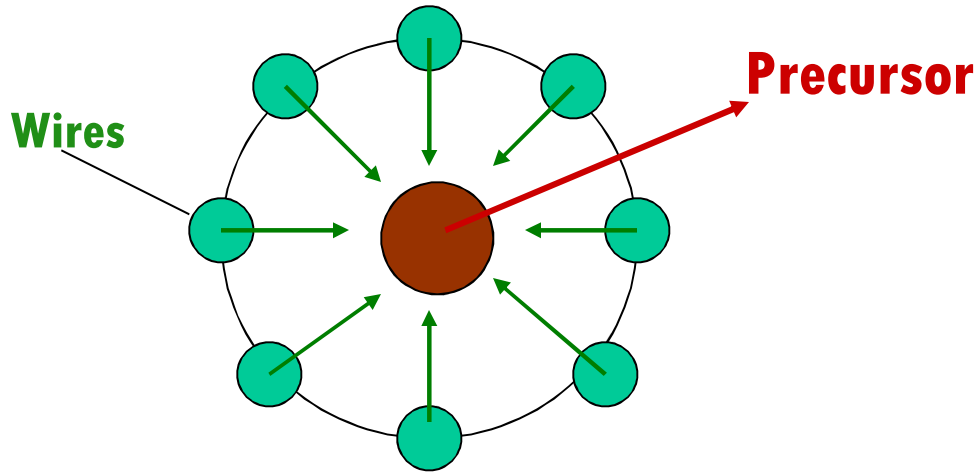
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# Wire array imploding experiments at NTF



Current in the wire array  $\sim 1$  MA

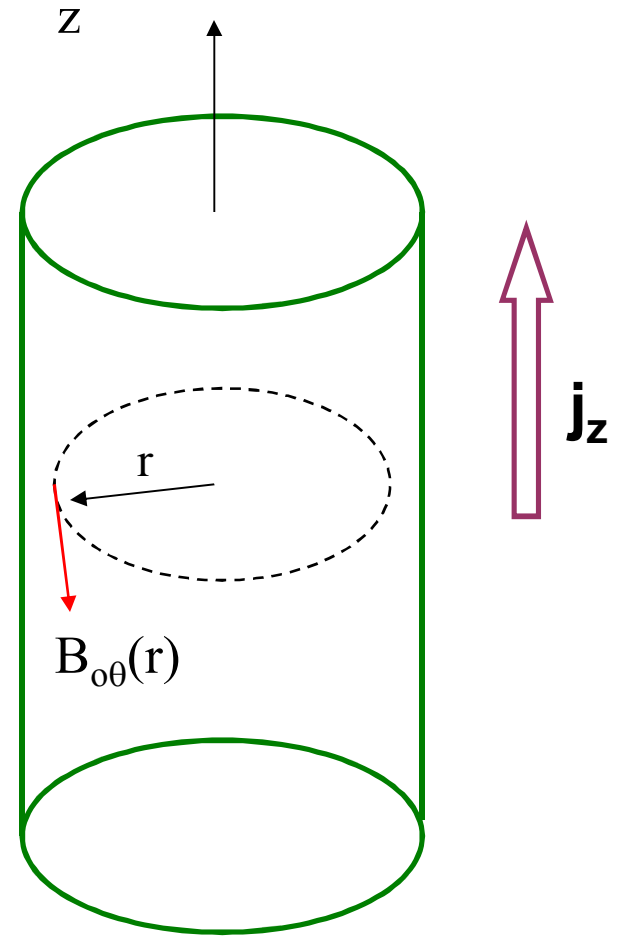


Plasma parameters in a precursor plasma

$$n_{0e} = 2.0 \times 10^{19} \text{ cm}^{-3}, n_{0i} = 2.0 \times 10^{18} \text{ cm}^{-3},$$

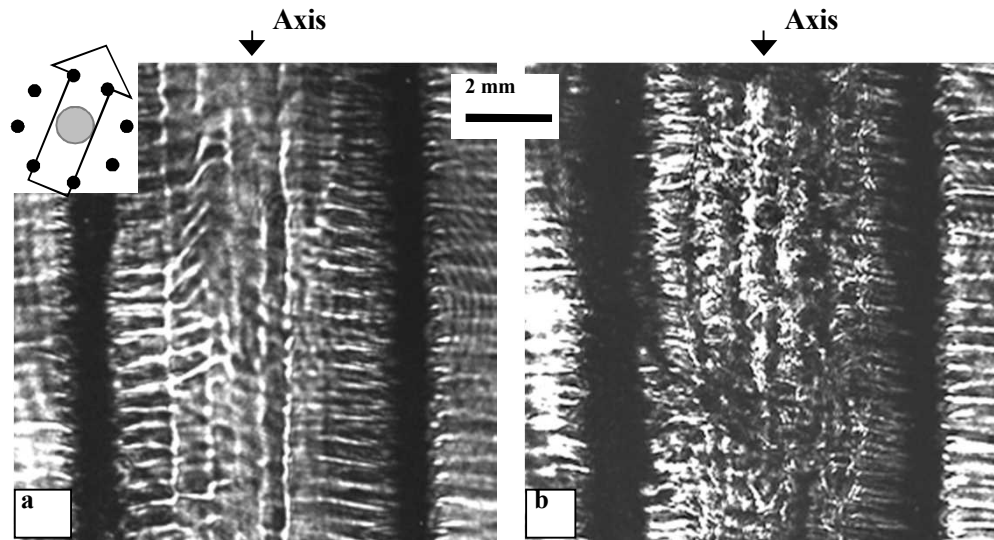
$$T_i \sim T_e = 50 \text{ eV}, B_0 = 0.3 \text{ MG}$$

$$\beta = 0.55 \quad \Omega_{eA} = 1.1 \times 10^{10} \text{ s}^{-1} \quad \omega_{pAL} = 1.4 \times 10^{13} \text{ s}^{-1}$$

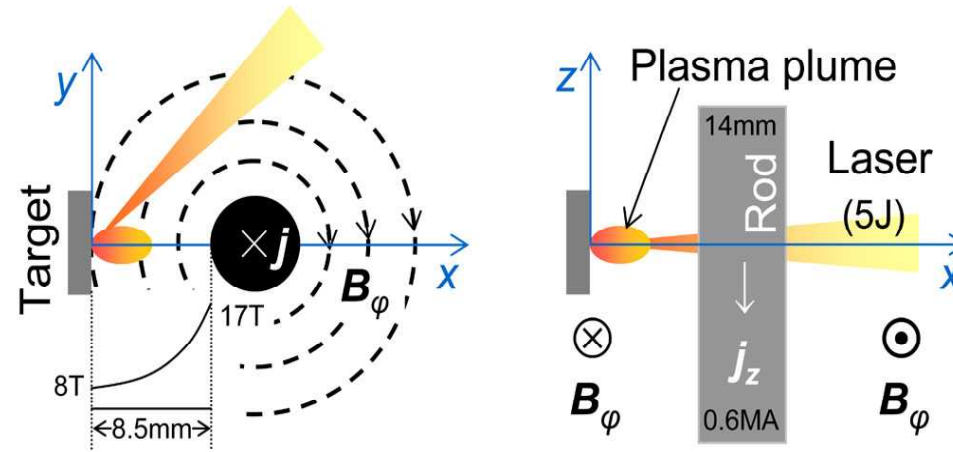


# Instability of flute modes in a Z-pinch plasma of a precursor can explain experimentally observed properties of excited perturbations

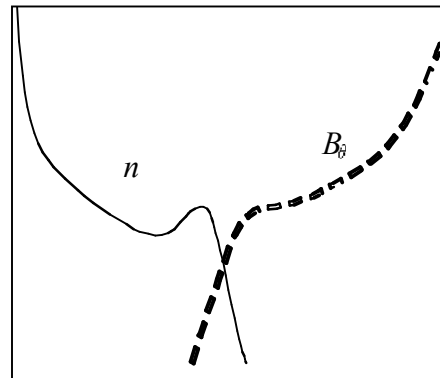
- Characteristic wavelengths of excited waves  $\sim 0.1 - 1$  mm
- Typical rise time of excited waves  $\sim 20$  ns
- Development of large scale cells on nonlinear stage
- Wave spectrum cascading towards short scales



# Laboratory Astrophysics Experiments



## Experimental set-up

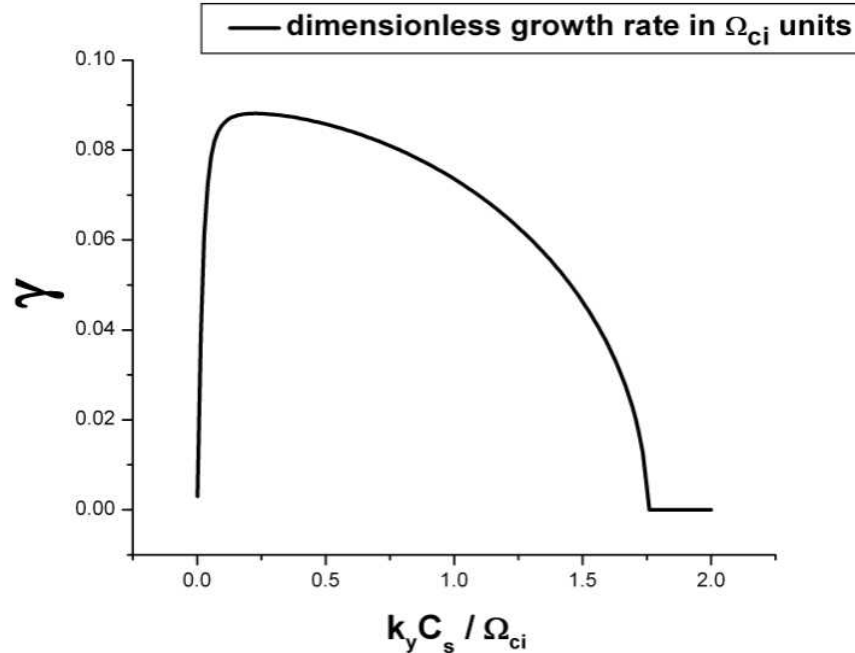


## Experimental density profile and adjusted magnetic field radial profile

Presura et al., *Astrophys. Space Sci.*, 2006

Sotnikov et al., *Astrophys. Space Sci.*, 2006

# Growth rate and frequency of flute modes



## Experimentally observed plasma parameters

$$n_{0e} = 2.0 \times 10^{19} \text{ cm}^{-3}, n_{0i} = 2.0 \times 10^{18} \text{ cm}^{-3}, T_i \sim T_e = 50 \text{ eV}, B_0 = 0.3 \text{ MG}$$

$$\frac{\omega_{pAl}}{c} = 4 \times 10^2 \text{ cm}^{-1} \quad \frac{kc}{\omega_{pAl}} \approx 0.3 \quad \lambda \approx 0.5 \text{ mm} \quad R \approx 1 \div 3 \text{ mm} \quad g \approx \frac{2V_A^2}{R}$$

$$\gamma \approx 3 \times 10^7 \text{ s}^{-1}$$

$$\beta = 0.55 \quad \Omega_{cAl} = 1.1 \times 10^{10} \text{ s}^{-1} \quad \omega_{pAL} = 1.4 \times 10^{13} \text{ s}^{-1}$$

# Flute instability



small density perturbation  $\delta n \sim \cos(\omega_k t - k_z z)$

perturbation of "gravitational" force  $\delta F_r \sim g \delta n$

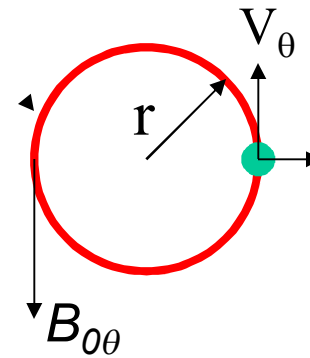
ions drift in axial z-direction

separation of charge

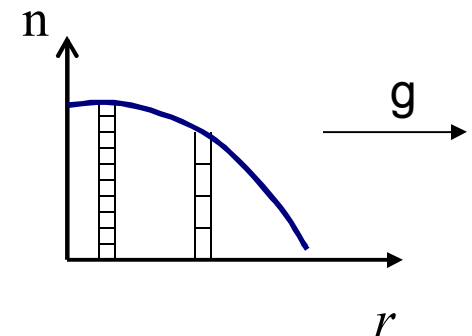
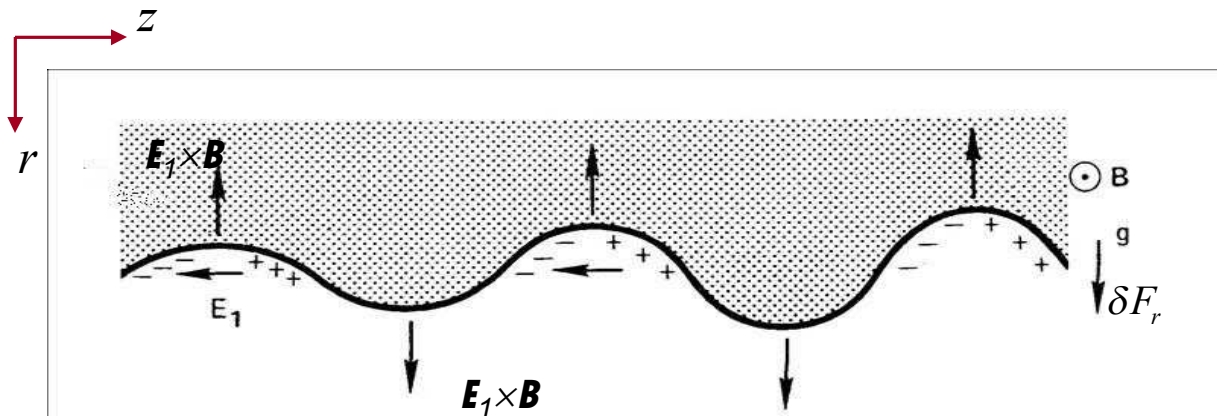
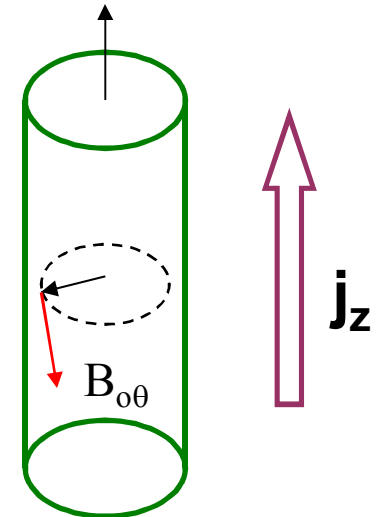
electric field

drift motion in  $r$ -direction brings particles from denser plasma core

instability



$$g = \frac{V_\theta^2}{r} \approx \frac{V_T^2}{r}$$

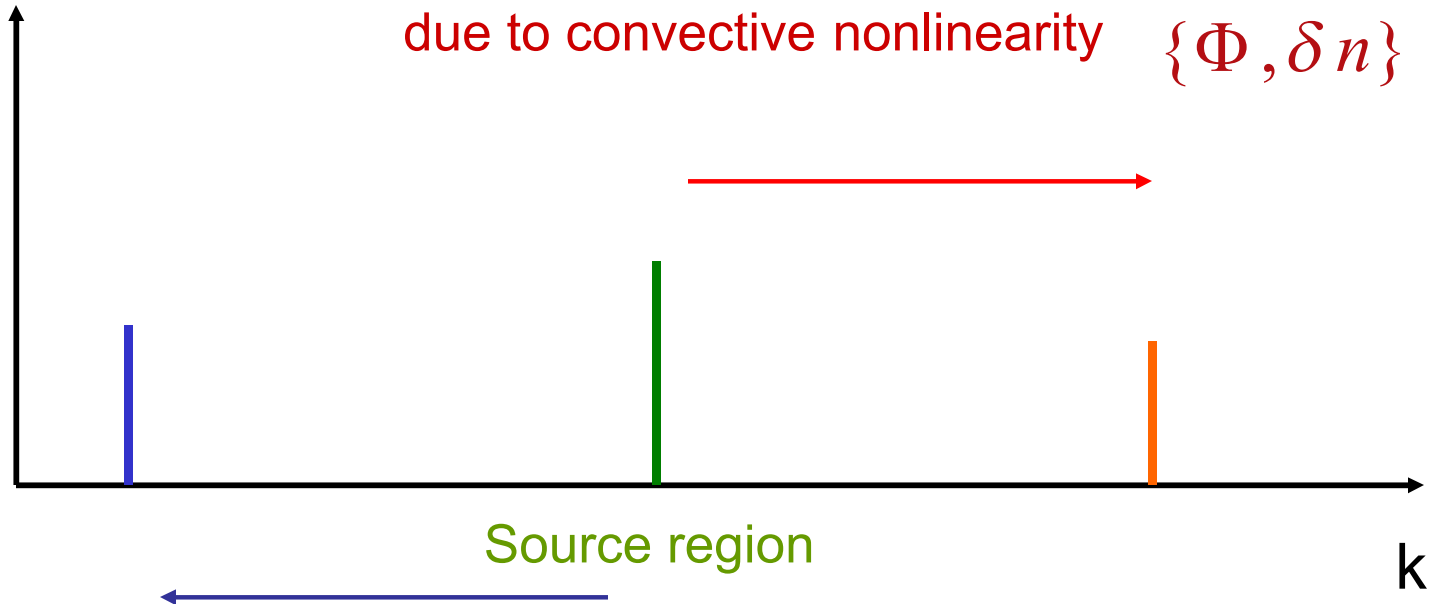




# Nonlinear wave cascades



Wave energy cascade to small wavelengths  
due to convective nonlinearity  $\{\Phi, \delta n\}$



Wave energy cascade to large wavelengths and excitation  
of large scale structures due to polarization drift nonlinearity  $\{\Delta_{\perp} \Phi, \Phi\}$   
and diamagnetic component of polarization drift nonlinearity  $div\{\vec{\nabla}_{\perp} \Phi, \delta n\}$

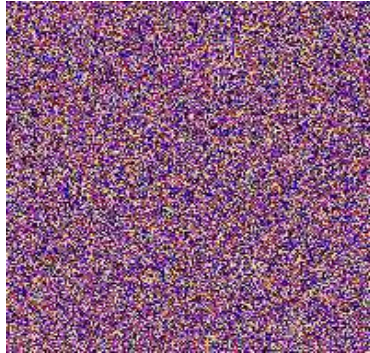
Kodama and Pavlenko, PRL 1988; Sandberg et al., PoP 2005.

**Sotnikov et al., IEEE TPS, 2005; Sotnikov et al., CiCP 2008, to be published**

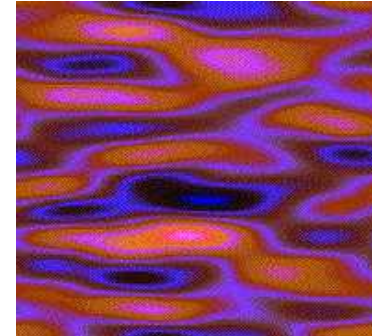
# Numerical results



## Density in linear stage

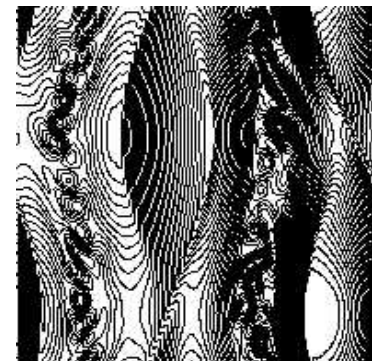
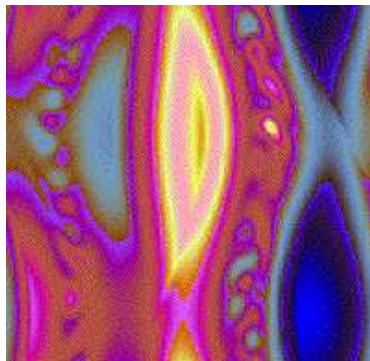


$$\Omega_i t = 0$$



$$\Omega_i t = 1400$$

## Density in nonlinear stage and formation of dipolar vortices

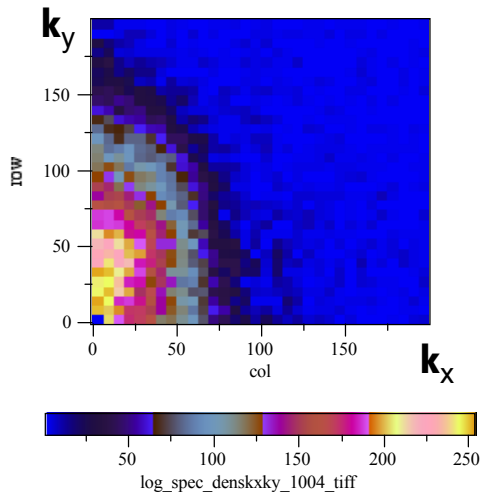


$$\Omega_i t = 4600$$

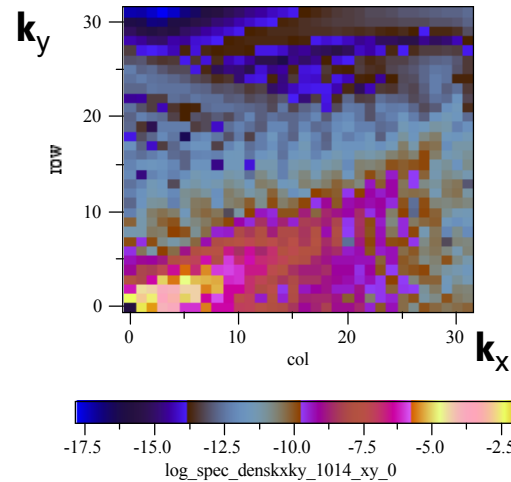
# Formation of zonal flow on the nonlinear stage



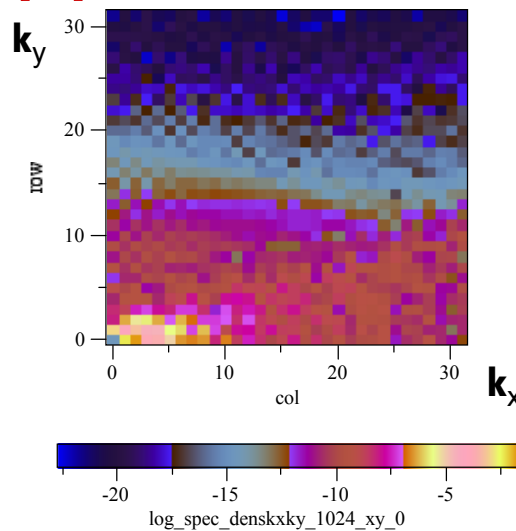
**2D density spectrum  
at the linear stage**



**2D density spectrum at the early  
nonlinear stage**



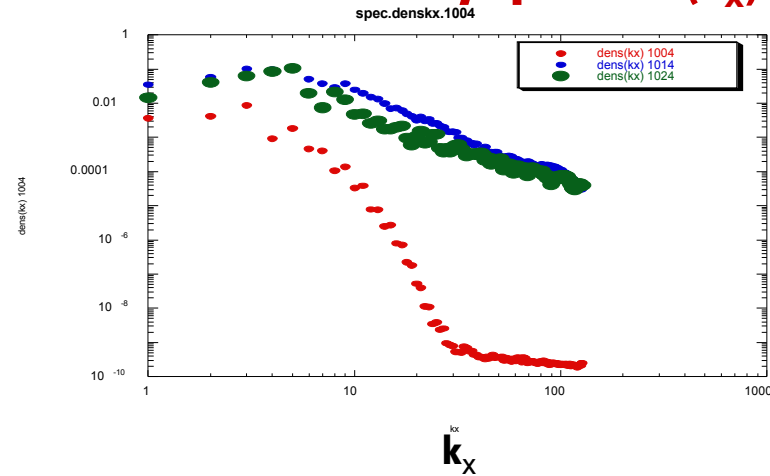
**2D density spectrum at the late nonlinear stage**



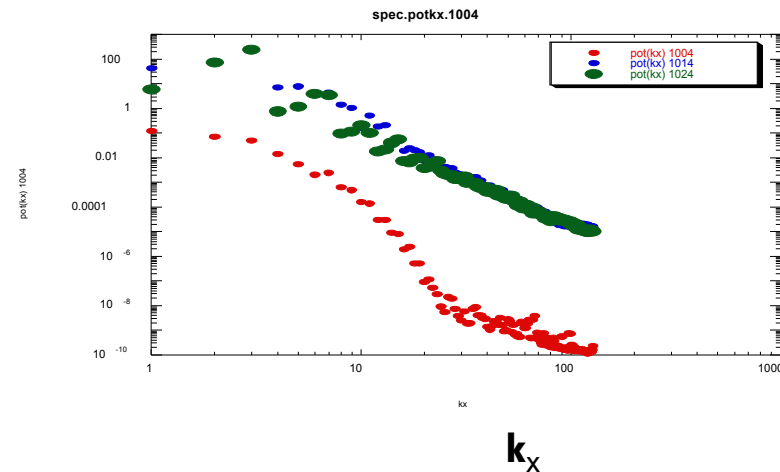
# Spectral cascade to short scales



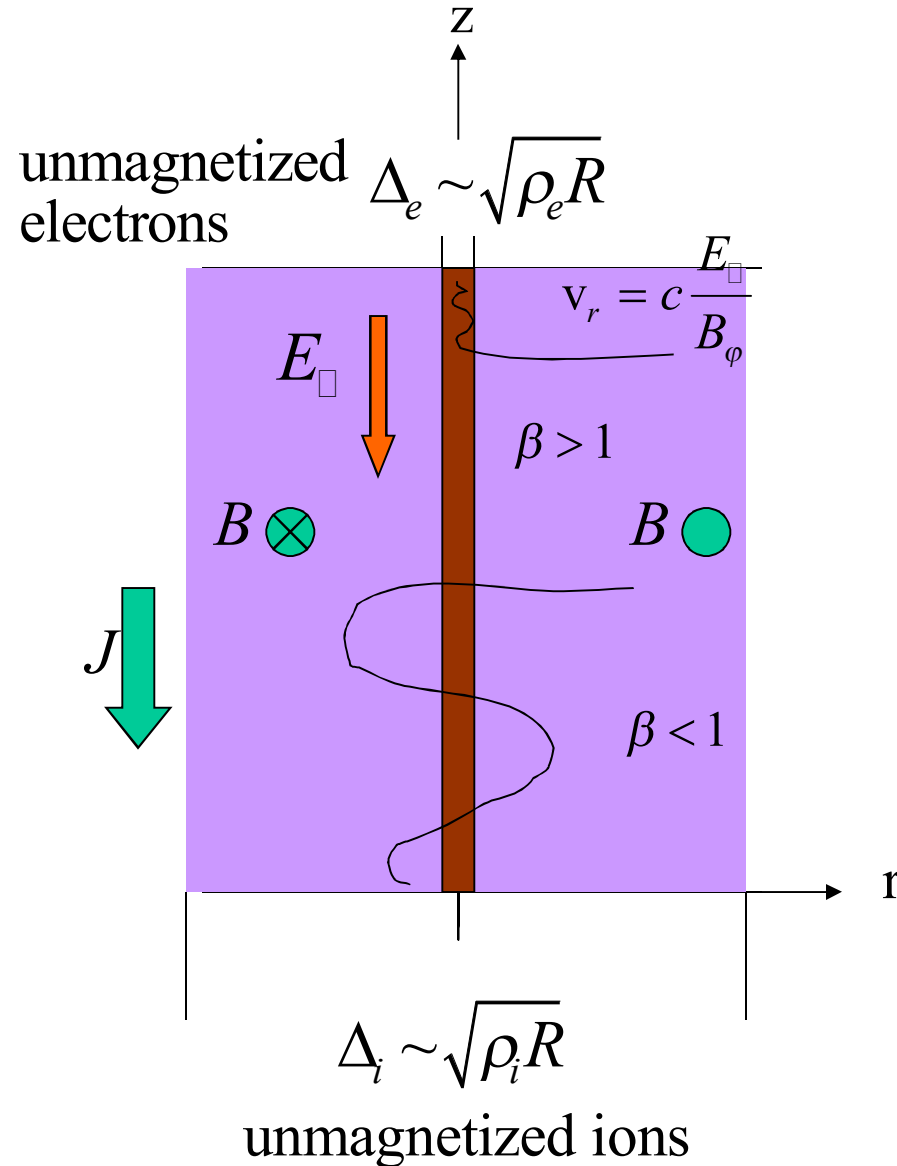
## Evolution of the density spectrum ( $k_x$ ) in time



## Evolution of the potential spectrum ( $k_x$ ) in time



# New ion instability of the Buneman type and associated anomalous resistivity in Z-pinch discharge configuration



## Conclusions



- Wave activity experimentally observed in the central region of imploding wire array, where significant part of the current is concentrated, can be connected with excitation of flute-type compressible electromagnetic oscillations in high beta plasma.
- Flute-type instability can be observed in laboratory astrophysics experiments on interaction of laser ablated plasma flow with strong magnetic field.
- Linear dispersion equation for electromagnetic flute-like mode instability has growing solution even in a finite beta plasma. Typical growth time and spatial scales of excited waves are in agreement with experimental data.
- Fluid model of flute turbulence can describe nonlinear dynamics of large scale density and magnetic field structures as well as wave energy cascading towards the short scales observed in experiment.