



Low Frequency Turbulence in a High Beta Plasma

V. I. Sotnikov

University of Nevada at Reno, NV 89557

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In collaboration with

V. V. Ivanov, R. Presura, E. Yasin, J. Kindel

University of Nevada at Reno, NV 89557, USA

J.N. Leboeuf

JNL Scientific, Casa Grande, AZ 85222, USA

O.G. Onishenko

Institute of Physics of Earth, 123995 Moscow, Russia

B.V. Oliver, T. A. Mehlhorn

Sandia National Laboratories, Albuquerque, NM 87123, USA

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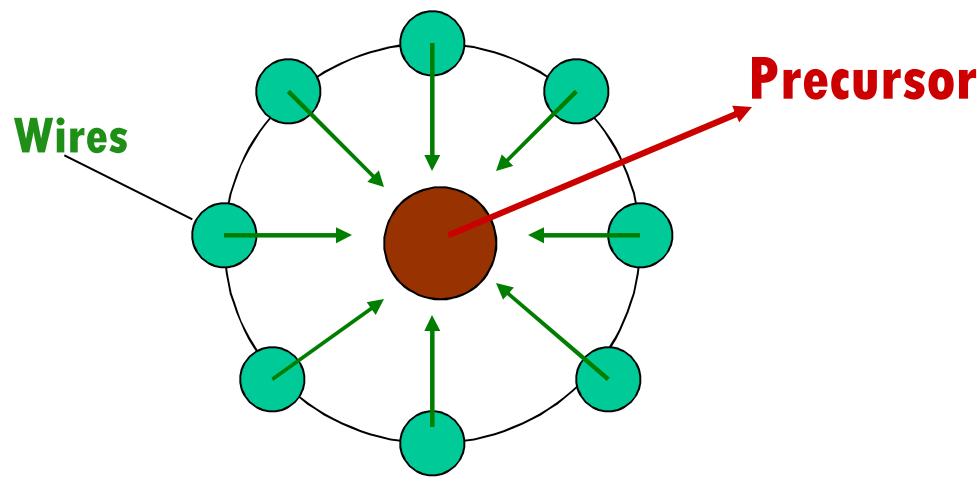
Sandia is a multiprogram laboratory operated by Sandia Corporation, A Lockheed Martin Company, for the United States Department of Energy's National Nuclear Security Administration under contract

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Wire array imploding experiments at NTF



Current in the wire array ~ 1 MA

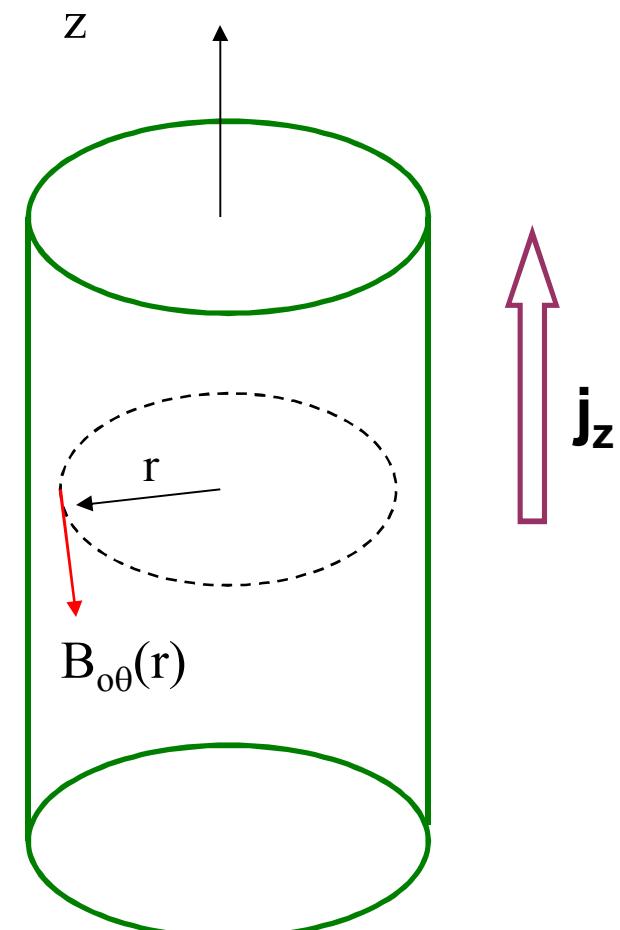


Plasma parameters in a precursor plasma

$$n_{0e} = 2.0 \times 10^{19} \text{ cm}^{-3}, n_{0i} = 2.0 \times 10^{18} \text{ cm}^{-3},$$

$$T_i \sim T_e = 50 \text{ eV}, B_0 = 0.3 \text{ MG}$$

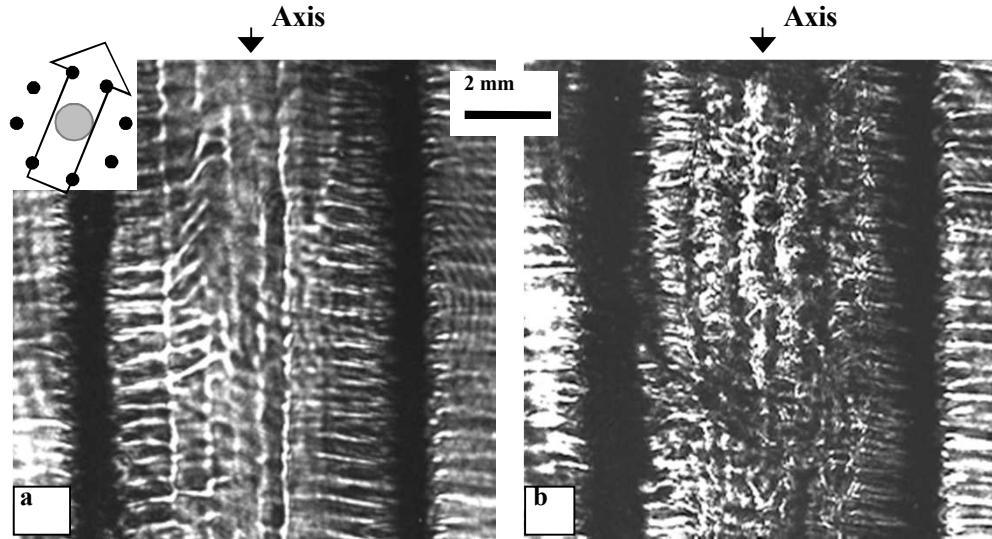
$$\beta = 0.55 \quad \Omega_{cA} = 1.1 \times 10^{10} \text{ s}^{-1} \quad \omega_{pAL} = 1.4 \times 10^{13} \text{ s}^{-1}$$



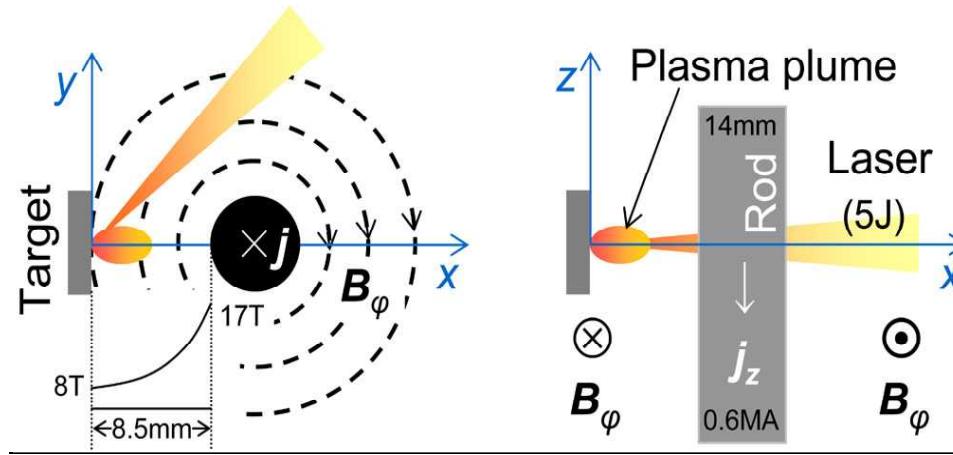
Instability of flute modes in a Z-pinch plasma of a precursor can explain experimentally observed properties of excited perturbations



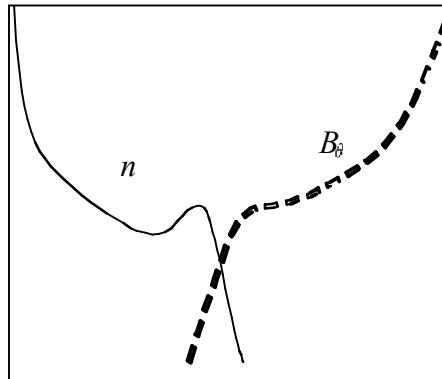
- **Characteristic wavelengths of excited waves $\sim 0.1 - 1$ mm**
- **Typical rise time of excited waves ~ 20 ns**
- **Development of large scale cells on nonlinear stage**
- **Wave spectrum cascading towards short scales**



Laboratory Astrophysics Experiments



Experimental set-up

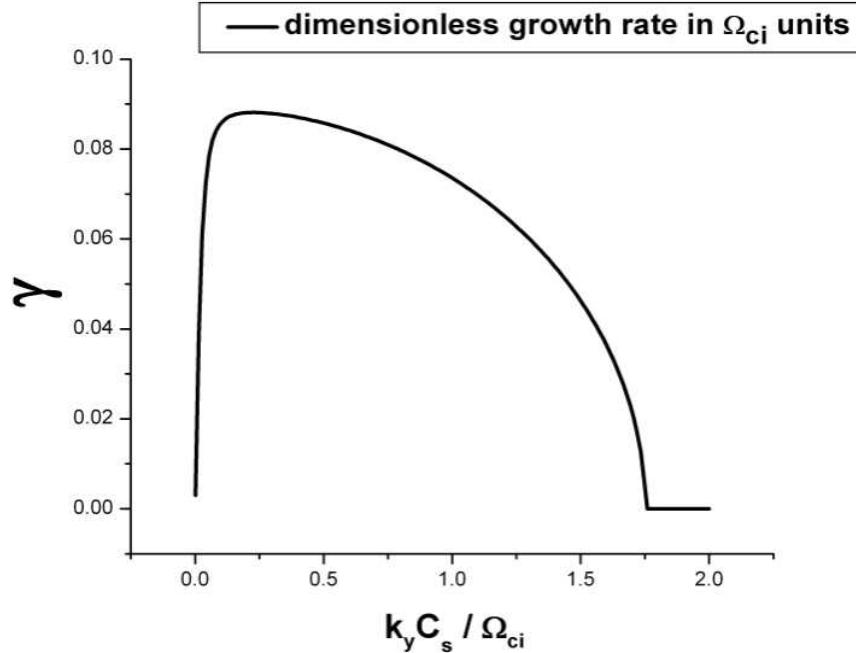


Experimental density profile and adjusted magnetic field radial profile

Presura et al., *Astrophys. Space Sci.*, 2006

Sotnikov et al., *Astrophys. Space Sci.*, 2006

Growth rate and frequency of flute modes



Experimentally observed plasma parameters

$$n_{0e} = 2.0 \times 10^{19} \text{ cm}^{-3}, n_{0i} = 2.0 \times 10^{18} \text{ cm}^{-3}, T_i \sim T_e = 50 \text{ eV}, B_0 = 0.3 \text{ MG}$$

$$\frac{\omega_{pAl}}{c} = 4 \times 10^2 \text{ cm}^{-1} \quad \frac{kc}{\omega_{pAl}} \square 0.3 \quad \lambda \square 0.5 \text{ mm} \quad R \square 1 \div 3 \text{ mm} \quad g \square \frac{2V_A^2}{R}$$

$$\gamma \square 3 \times 10^7 \text{ s}^{-1}$$

$$\beta = 0.55 \quad \Omega_{cAl} = 1.1 \times 10^{10} \text{ s}^{-1} \quad \omega_{pAL} = 1.4 \times 10^{13} \text{ s}^{-1}$$

Flute instability



small density perturbation $\delta n \sim \cos(\omega_k t - k_z z)$

perturbation of “gravitational” force $\delta F_r \sim g \delta n$

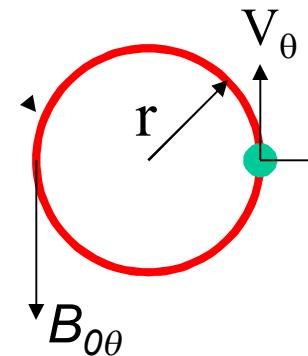
ions drift in axial z -direction

separation of charge

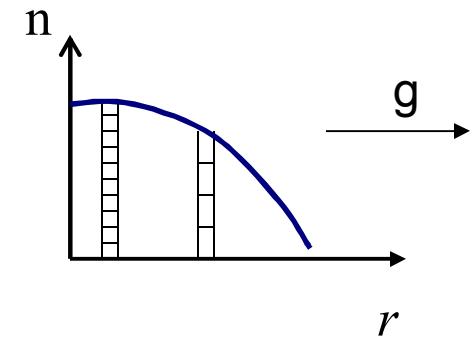
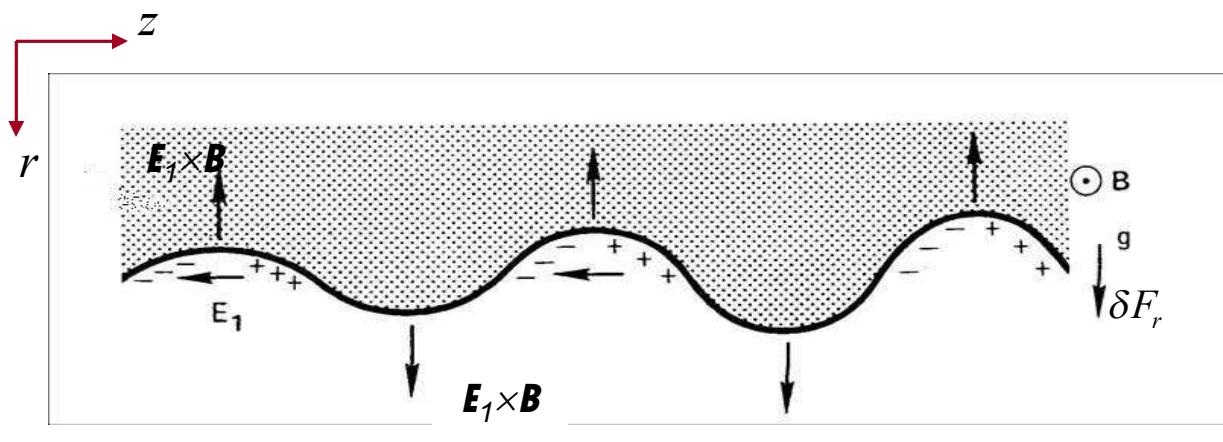
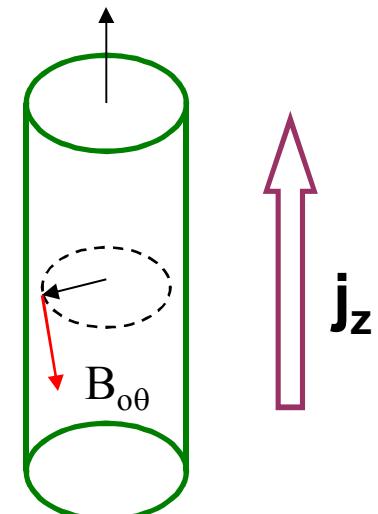
electric field

drift motion in r -direction brings particles from denser plasma core

instability



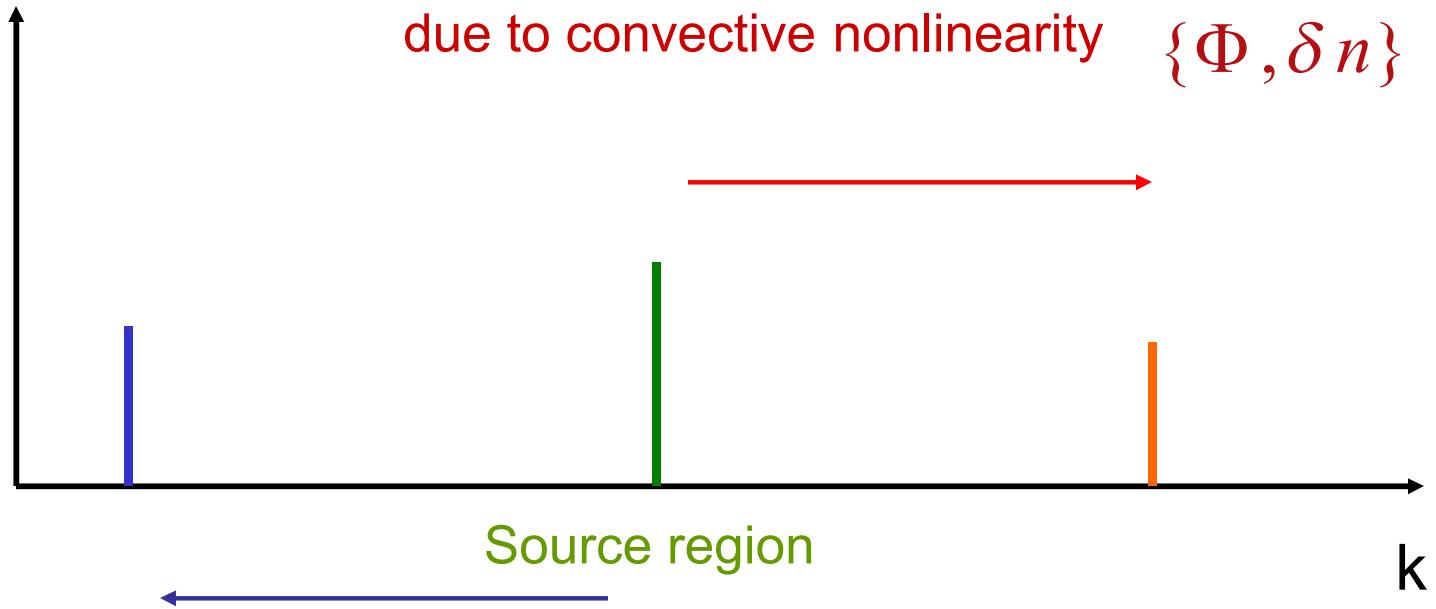
$$g = \frac{V_\theta^2}{r} \approx \frac{V_T^2}{r}$$



Nonlinear wave cascades



Wave energy cascade to small wavelengths
due to convective nonlinearity $\{\Phi, \delta n\}$



Wave energy cascade to large wavelengths and excitation
of large scale structures due to polarization drift nonlinearity
and diamagnetic component of polarization drift nonlinearity $\{\Delta_\perp \Phi, \Phi\}$
 $\text{div}\{\vec{\nabla}_\perp \Phi, \delta n\}$

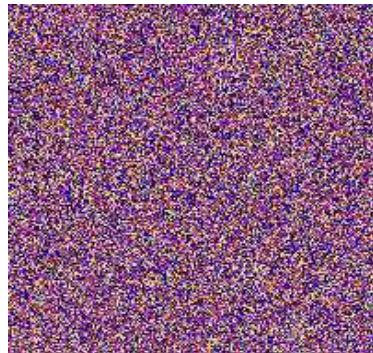
Kodama and Pavlenko, PRL 1988; Sandberg et al., PoP 2005.

Sotnikov et al., IEEE TPS, 2005; Sotnikov et al., CiCP 2008, to be published

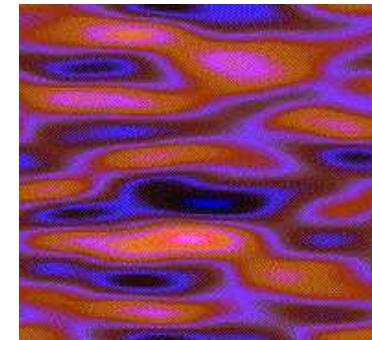
Numerical results



Density in linear stage

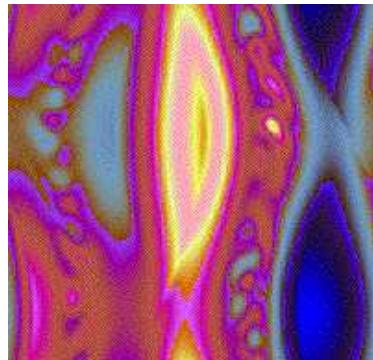


$$\Omega_i t = 0$$

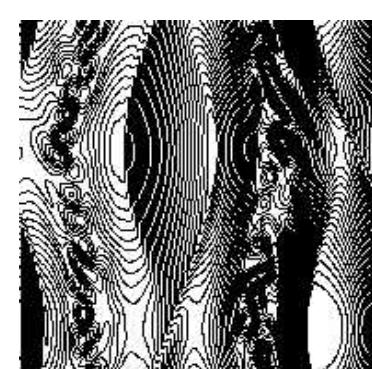


$$\Omega_i t = 1400$$

Density in nonlinear stage and formation of dipolar vortices



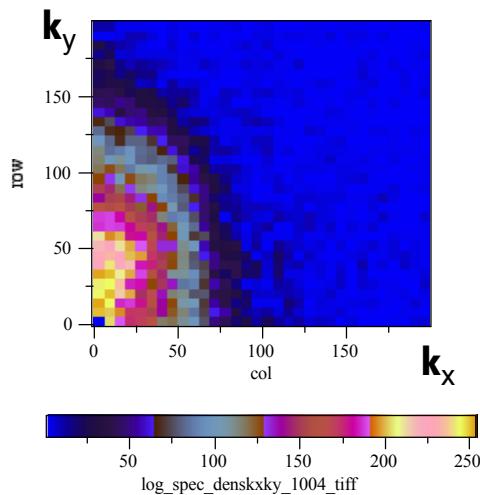
$$\Omega_i t = 4600$$



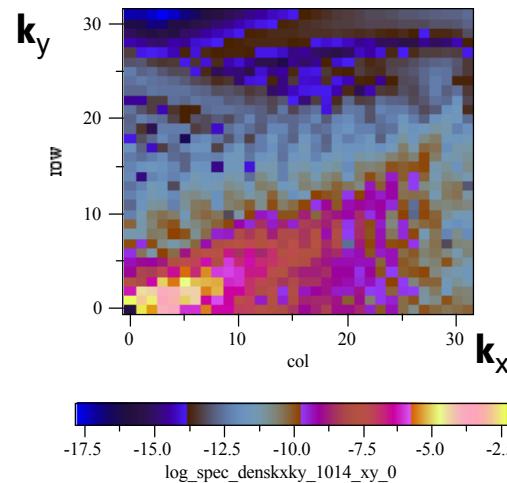
Formation of zonal flow on the nonlinear stage



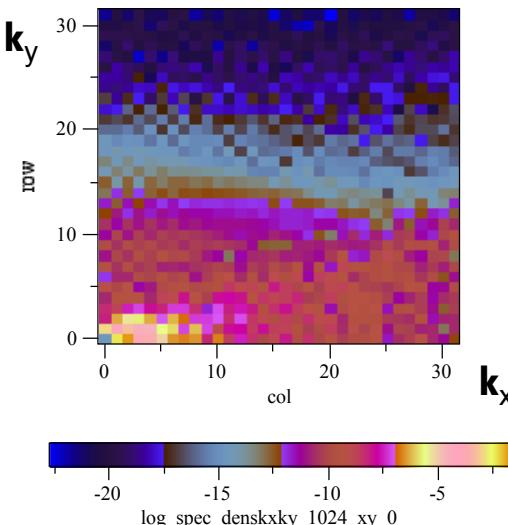
**2D density spectrum
at the linear stage**



**2D density spectrum at the early
nonlinear stage**



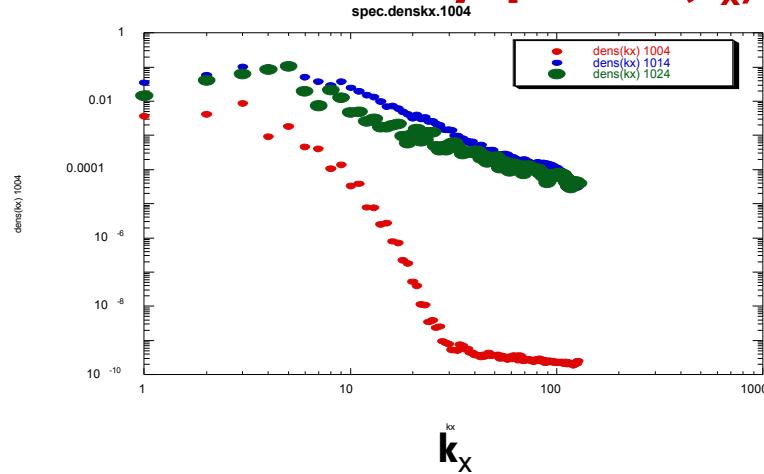
2D density spectrum at the late nonlinear stage



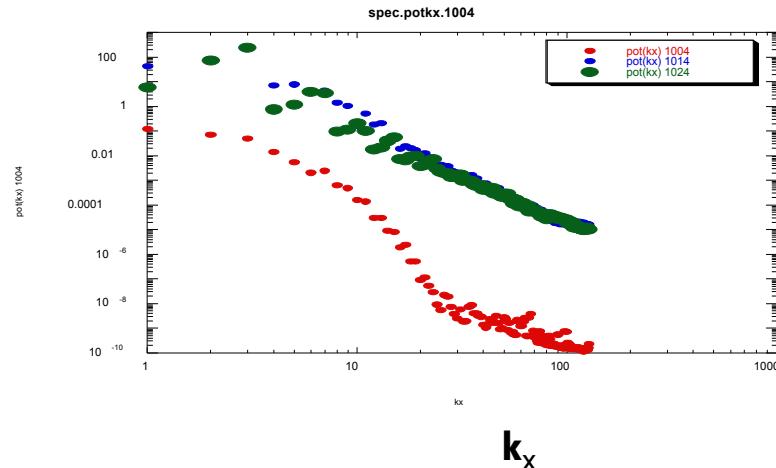
Spectral cascade to short scales



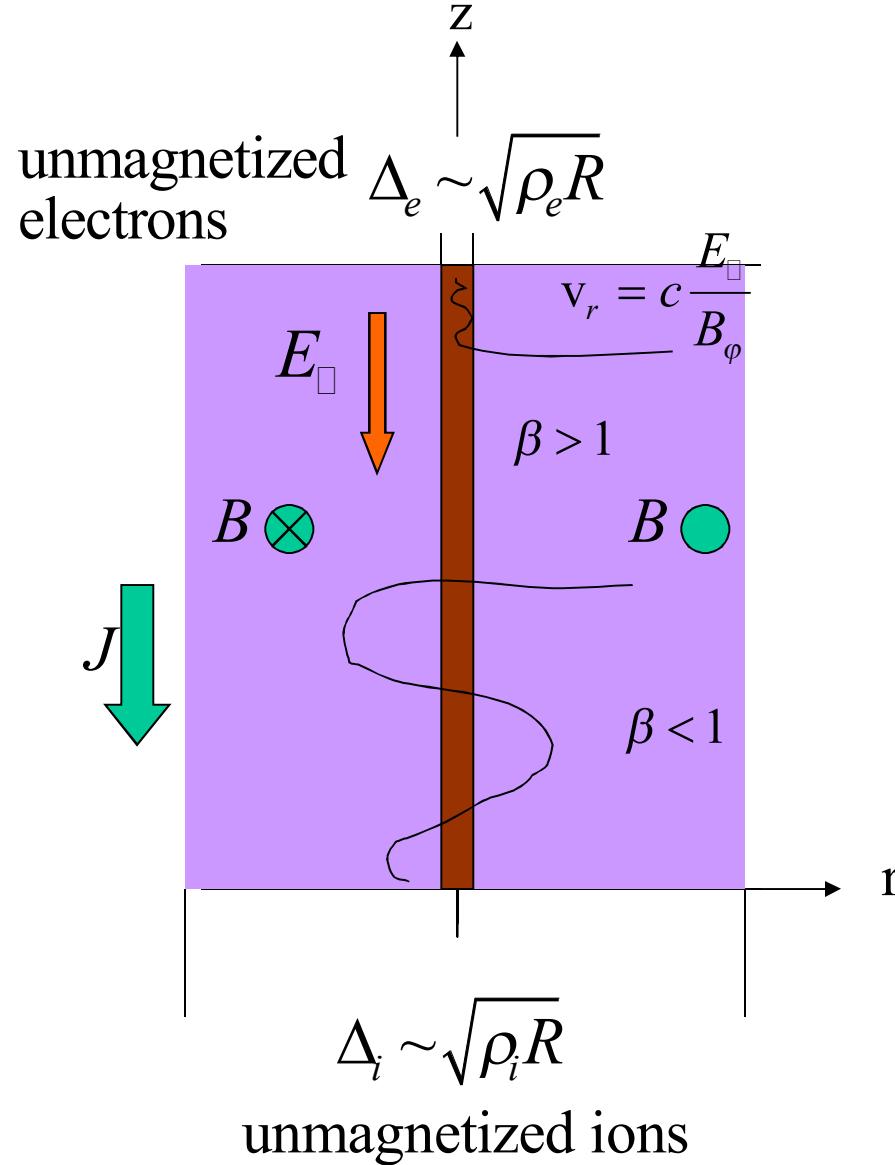
Evolution of the density spectrum (k_x) in time



Evolution of the potential spectrum (k_x) in time



New ion instability of the Buneman type and associated anomalous resistivity in Z-pinch discharge configuration



Conclusions



- Wave activity experimentally observed in the central region of imploding wire array, where significant part of the current is concentrated, can be connected with excitation of flute-type compressible electromagnetic oscillations in high beta plasma.
- Flute-type instability can be observed in laboratory astrophysics experiments on interaction of laser ablated plasma flow with strong magnetic field.
- Linear dispersion equation for electromagnetic flute-like mode instability has growing solution even in a finite beta plasma. Typical growth time and spatial scales of excited waves are in agreement with experimental data.
- Fluid model of flute turbulence can describe nonlinear dynamics of large scale density and magnetic field structures as well as wave energy cascading towards the short scales observed in experiment.