

3D MHD Simulations of Wire Array Z-pinches

UCSD seminar

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Acknowledgements / Outline

Acknowledgements:

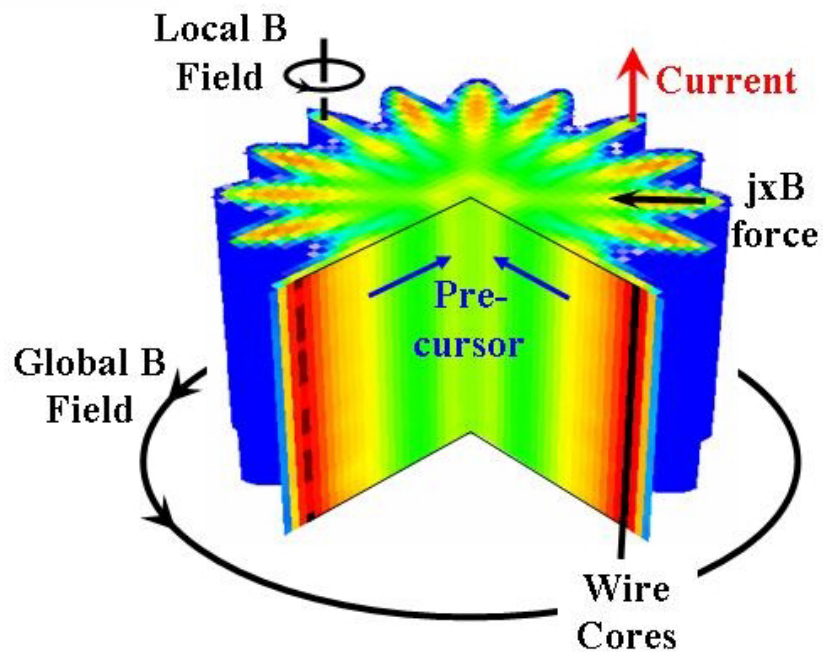
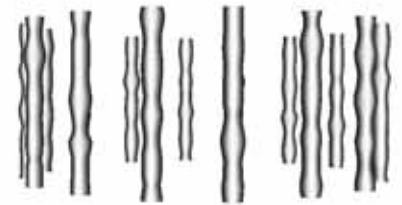
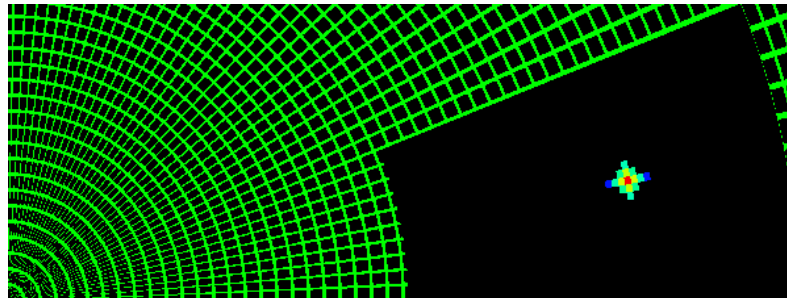
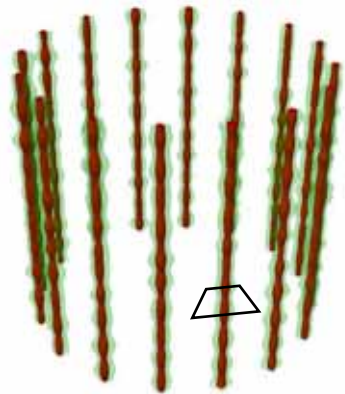
Jerry Chittenden, Mike Cuneo, Ray Lemke, Tim Pointon, Eduardo Waisman, Mike Jones

Outline

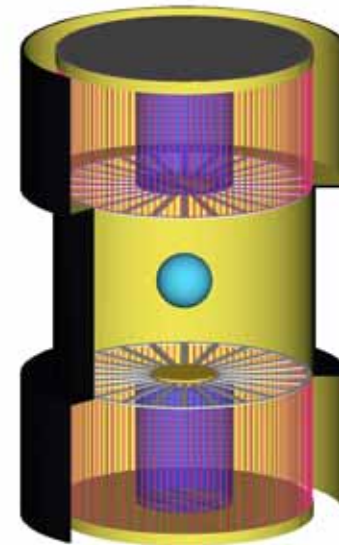
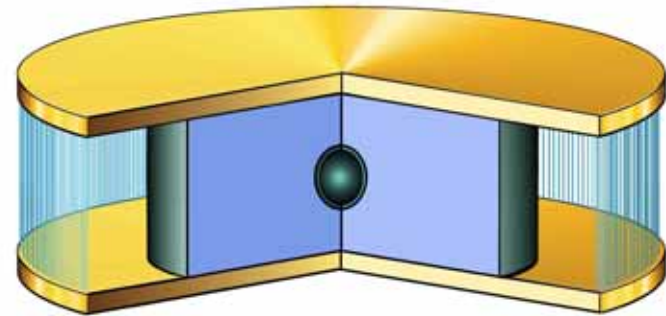
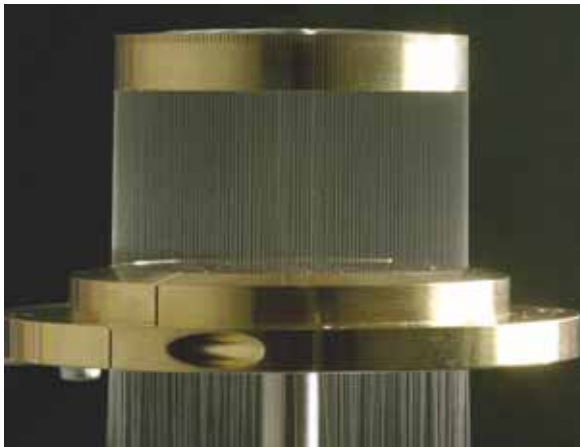
- **Introduce MHD code gorgon**
- **Transmission Line Circuit model**
- **Phenomenological convolute model**
- **Modeling of Mass Scan**
- **Modeling ZR shot 1787**
- **Return to Mass Scan**
- **Comparison with Radiography**
- **Modeling nested arrays**

Sandia is a multiprogram laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the United States Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

Wire Array Z-pinch on MAGPIE (~1MA)



Wire Array Z-pinch on Z





Modelling the Z-pinch

GORGON – 3D Resistive MHD

Fixed square grid finite volume hydrodynamics

Single fluid – separate electron and ion temperatures

Explicit electro-magnetic field solution (wave equation in vacuum / diffusion equation in plasma)

Thomas-Fermi Ionization

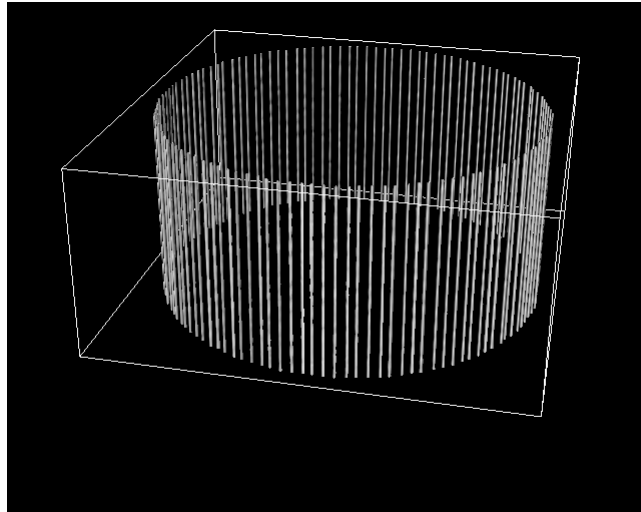
Van Leer Advection

Constrained Transport for Magnetic Field Advection

Single group radiation diffusion (not used for these calculations)

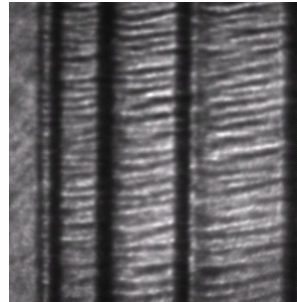


Simulation Setup

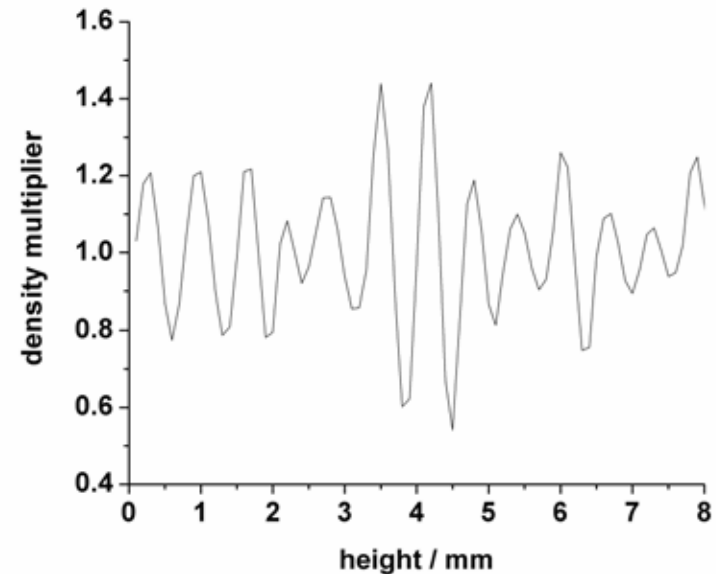


3D Full Circumference Calculation

- 120 wires substituted for 300 in simulation
 - Computational box 10 x 24 x 24 mm
 - Cell resolution – 110 micron square cells
 - 2 – 4 day runtime on 16 nodes



Initial wires given a mass perturbation in the axial direction to mimic ablation structure



Example density perturbation file

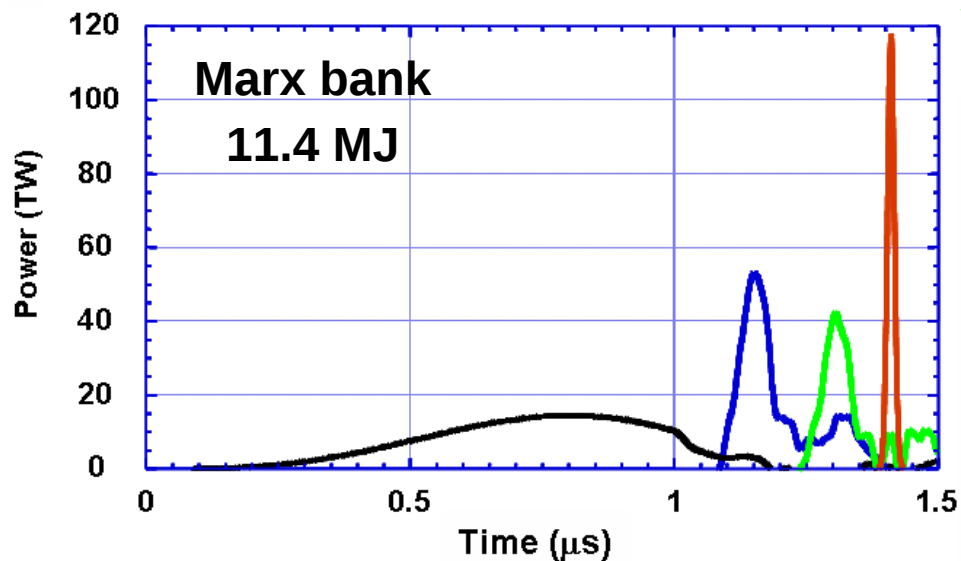
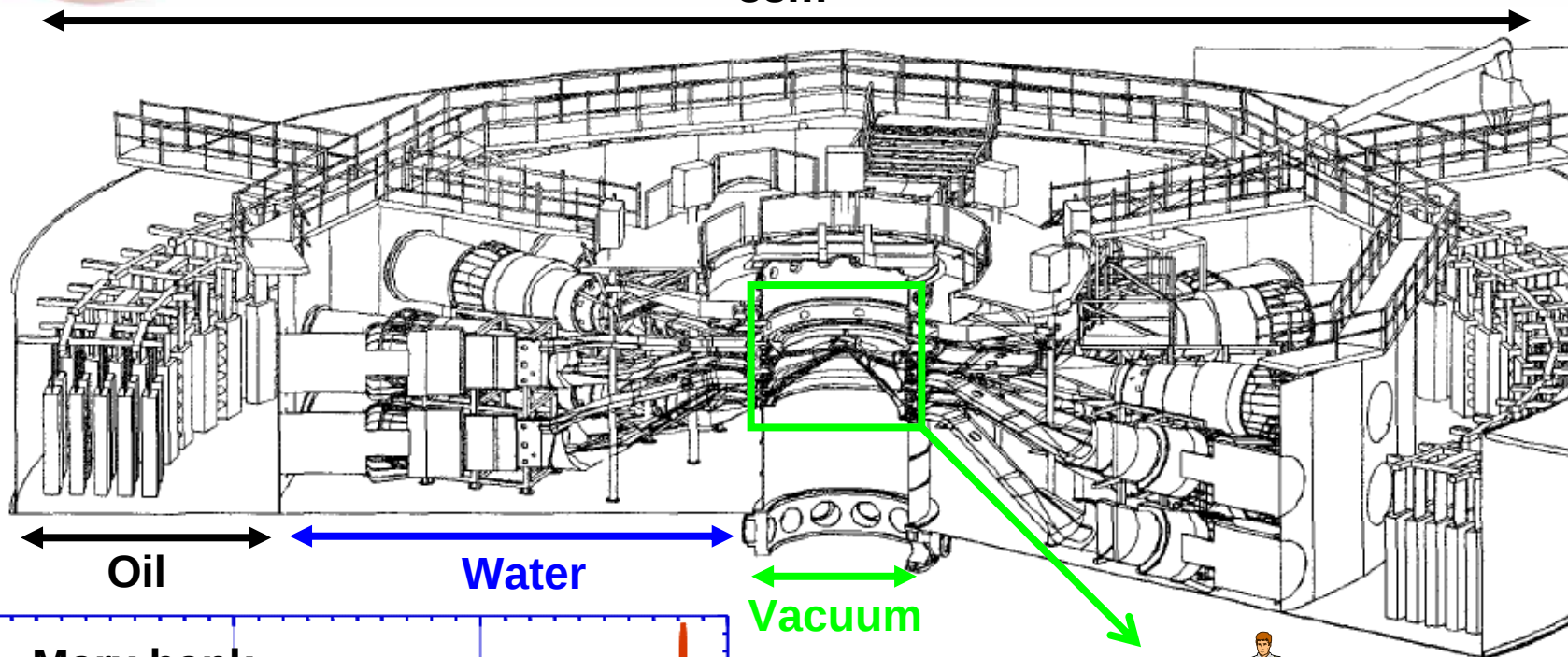
+/- 5 % mass perturbation used

Numerical sensitivities exist, e.g. resolution / vacuum cut-off / artificial viscosity, but MHD model is now fixed – no parameters are changed or tweaked. Only the initial array mass is varied in accordance with what was fired

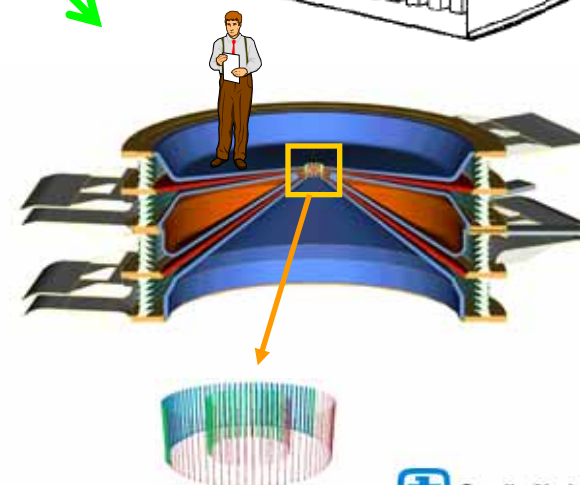


The Z Generator

33m



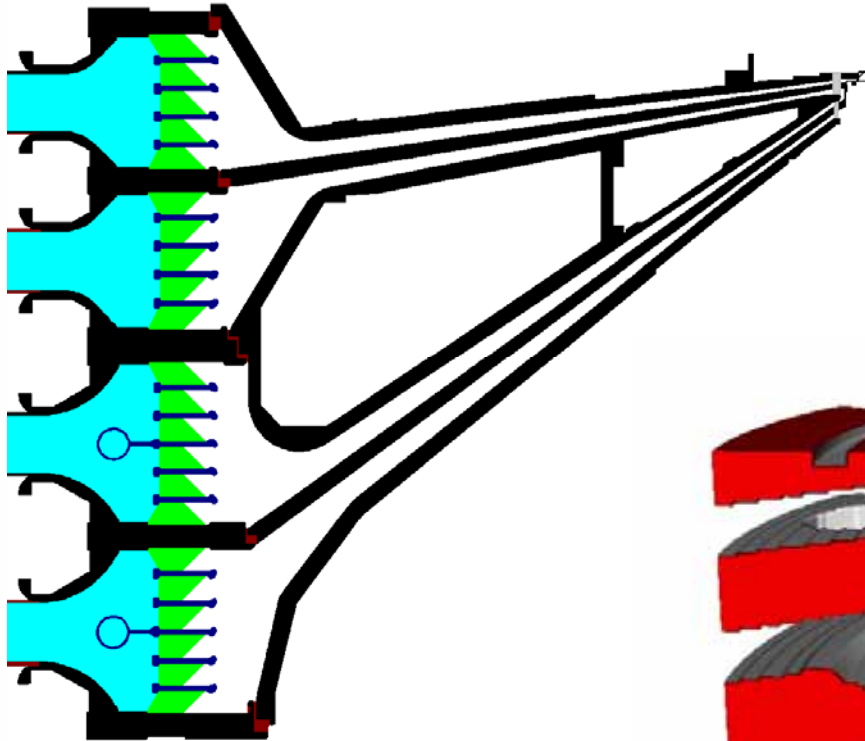
X-rays
>1.5 MJ
>250 TW
 $\eta \sim 15\%$
(electrical to x-ray)



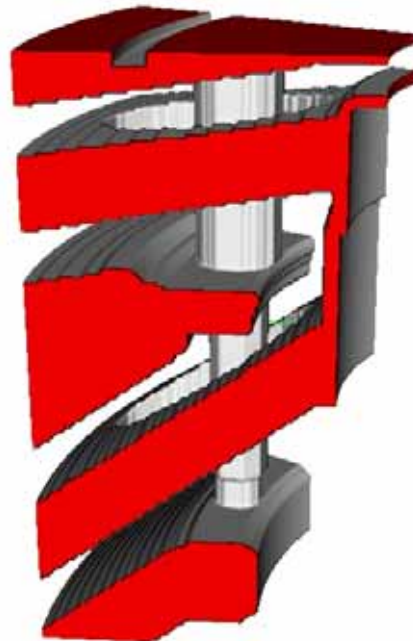
Hardware to include in the model



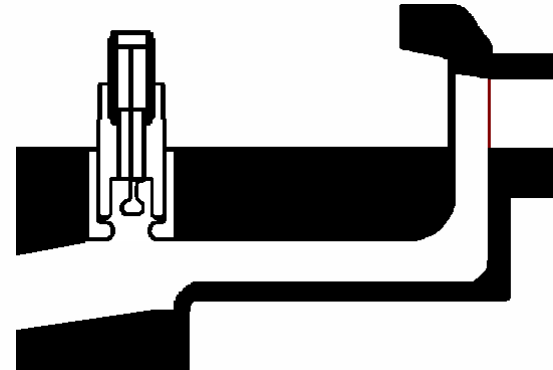
4 level MITL



Double post
hole
convolute



Feed to load

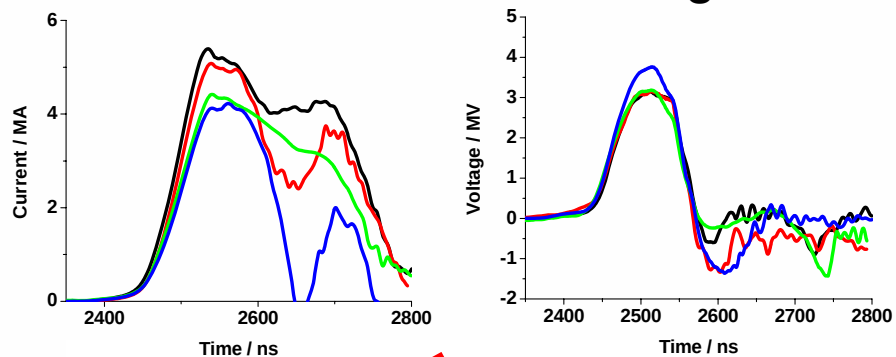


Wire Array Z-
pinch

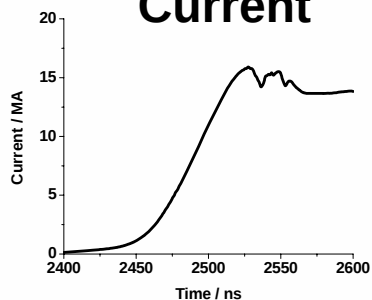


Measurements to Use and Compare Against

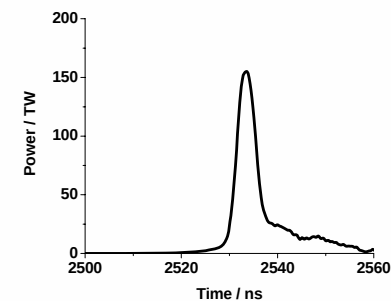
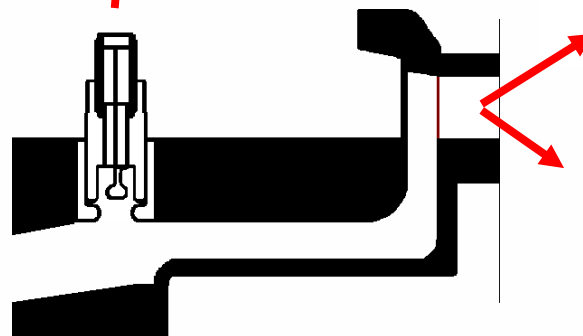
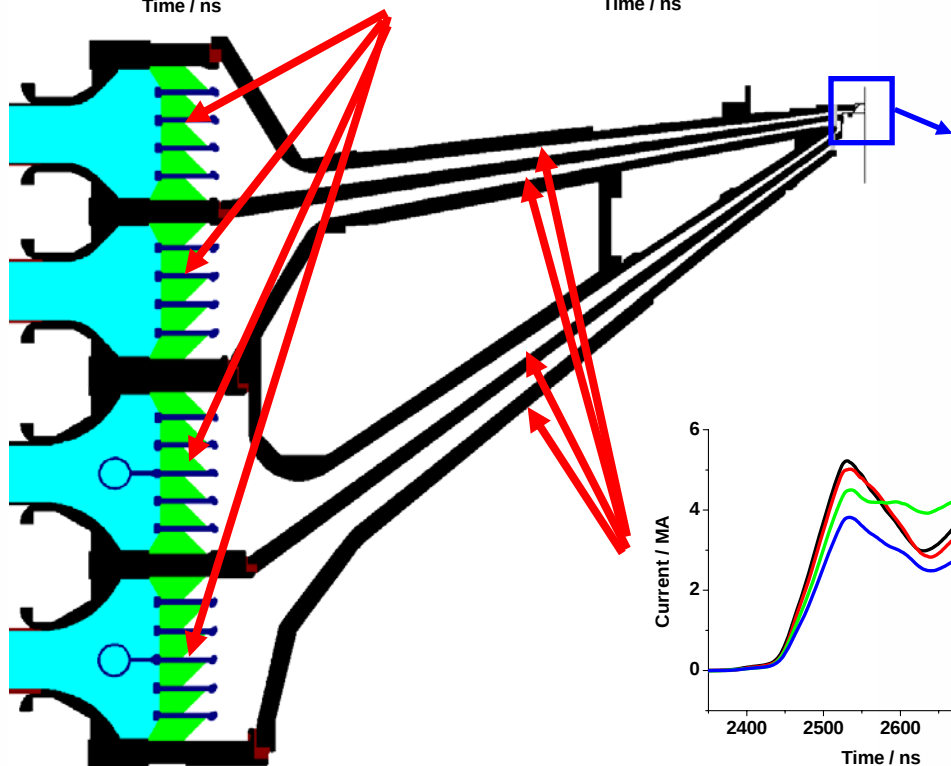
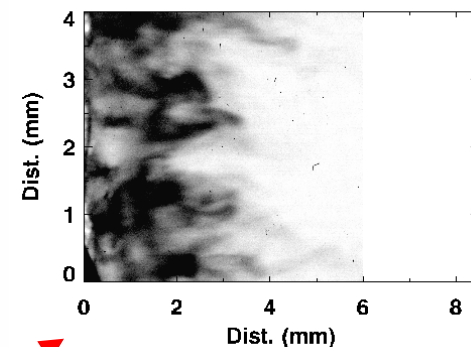
Stack Current / Voltage



Load Current

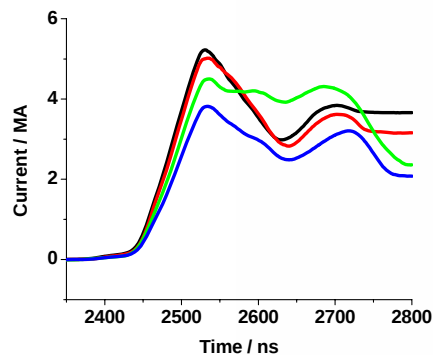


Radiography



X-ray

MITL Currents

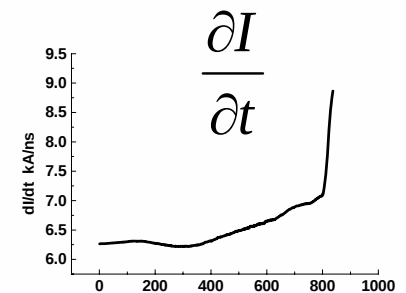
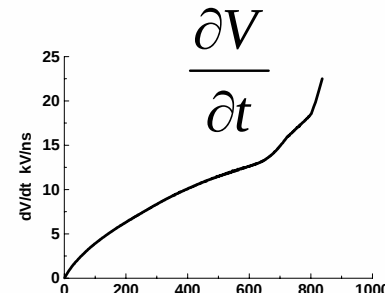
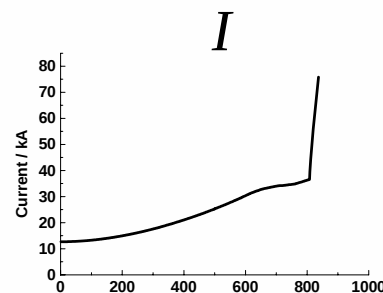
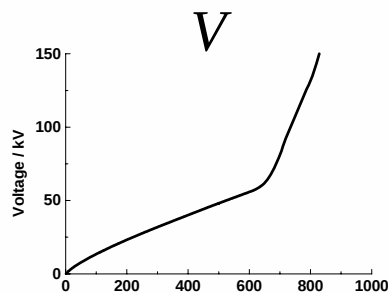
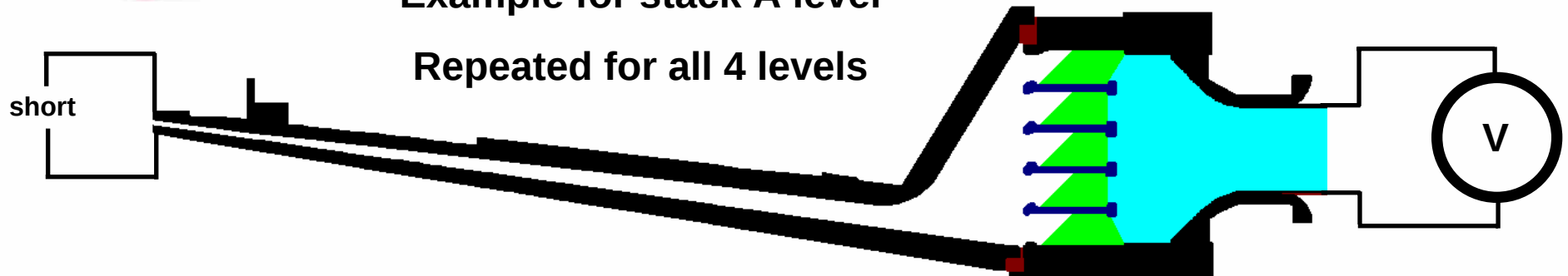


Electrode Configuration reduced to lumped element transmission line through EM simulation



Example for stack A level

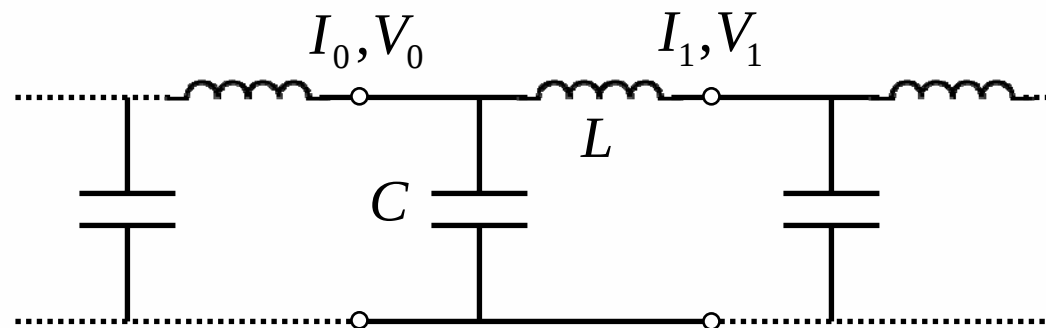
Repeated for all 4 levels



Telegraphers Equation

$$I_1 = I_0 - C\Delta r \frac{\partial V_0}{\partial t}$$

$$V_1 = V_0 - L\Delta r \frac{\partial I_1}{\partial t}$$

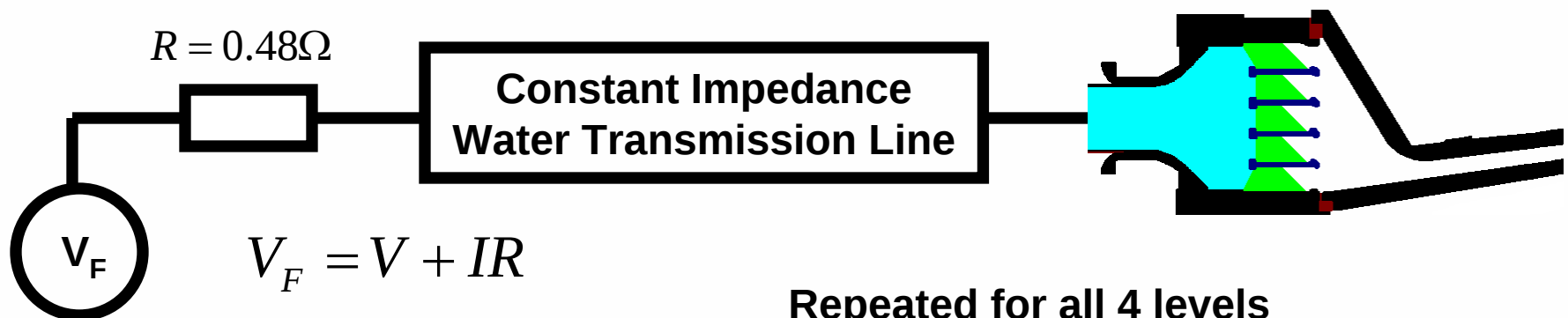
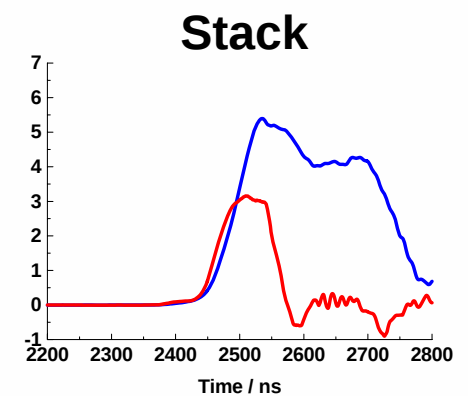
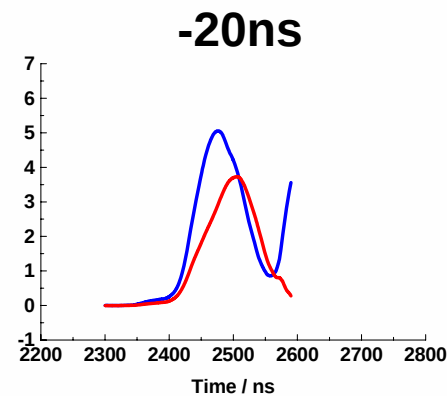
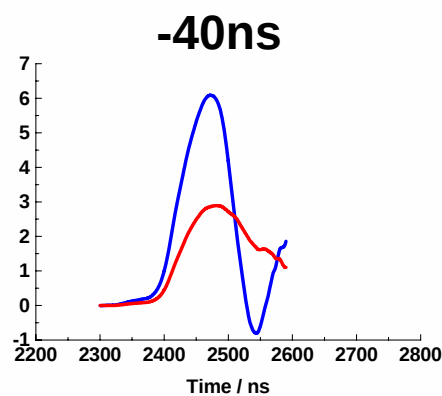
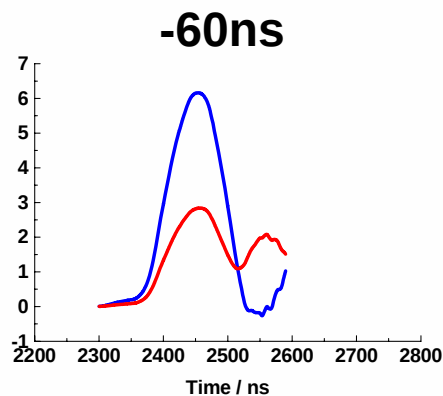


Lumped element transmission line

Voltage Source translated from stack measurements



— Current / MA — Voltage / MV



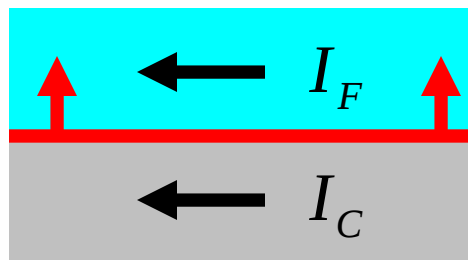
Electron Flow in Transmission Lines



To Load
←

Anode

I_A →



Cathode

$$I_A = I_C + I_F$$

**Cathode
Plasma**

- Cathode plasma forms for $E > 250\text{kV/cm}$
- Emits electrons which are magnetically confined forming electron flow layer
- Electrons in electron flow layer $E \times B$ drift towards load region

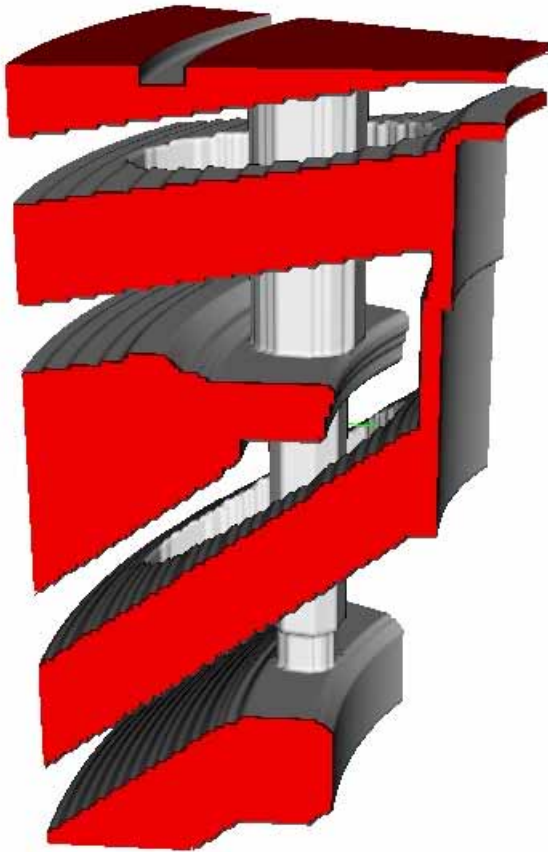
$$V = Z_0 \sqrt{I_A^2 - I_C^2} - \frac{mc^2}{2e} \frac{(I_A^2 - I_C^2)}{I_C^2} \quad \text{Mendel's Pressure Balance}$$

Corrected for cathode plasma expansion

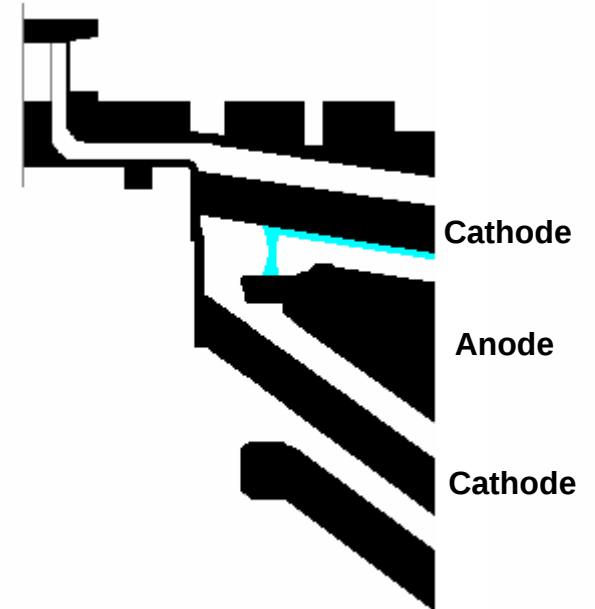
(Stygar 1997 IEEE Proceedings 11th international pulsed power conference pg. 591)

$$V = Z_0 \left(1 - \frac{vt}{g} \right) \sqrt{I_A^2 - I_C^2} - \frac{mc^2}{2e} \frac{(I_A^2 - I_C^2)}{I_C^2}$$

Electron flow current lost through magnetic nulls

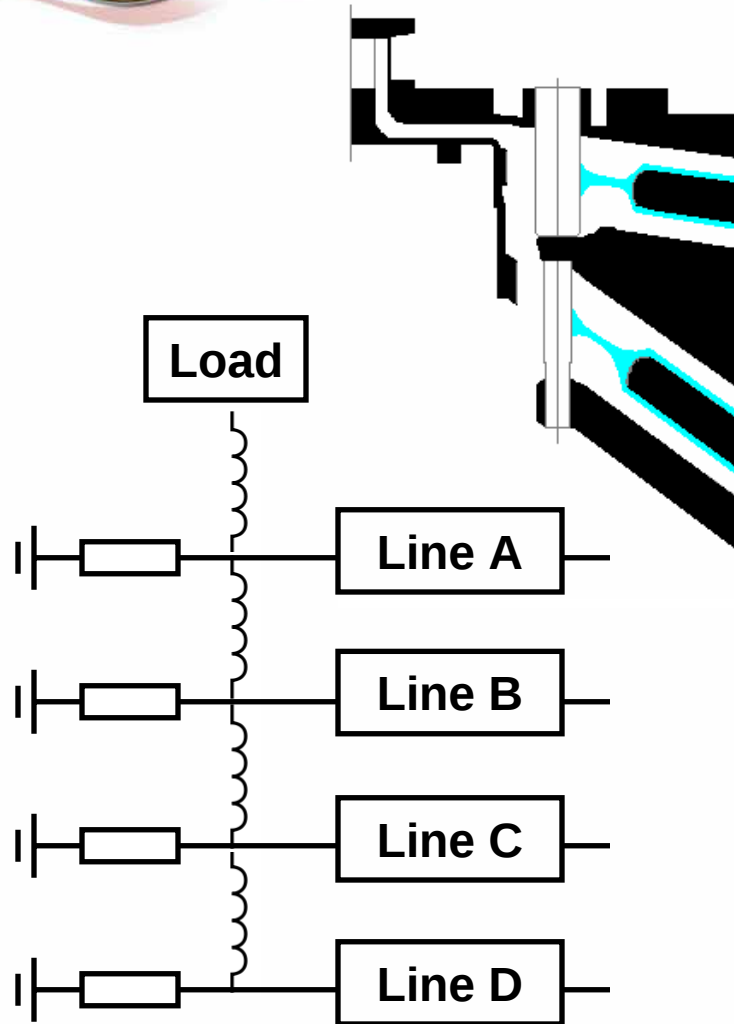


Current added
through double post
hole convolute



Magnetic insulation breaks down at
magnetic nulls, so electron flow current is
lost to the anode

Flow loss characterized by 4 loss resistances for the end of each line



$$Z_f = \frac{V}{\sqrt{I_A^2 - I_C^2}} \quad Z_v = Z_0 \left(1 - \frac{vt}{g} \right)$$

$$V = Z_v \sqrt{I_A^2 - I_C^2} - \frac{mc^2}{2e} \frac{(I_A^2 - I_C^2)}{I_C^2}$$

$$Z_f = \frac{Z_v}{2} + \frac{Z_v}{2} \left(1 - \frac{2mc^2 V}{e Z_v^2 I_C^2} \right)$$

P. Ottinger, Phys Plas 13, 063189

If all electron flow current lost then downstream current is just the cathode current and upstream is the total current

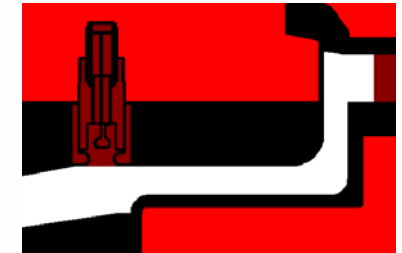
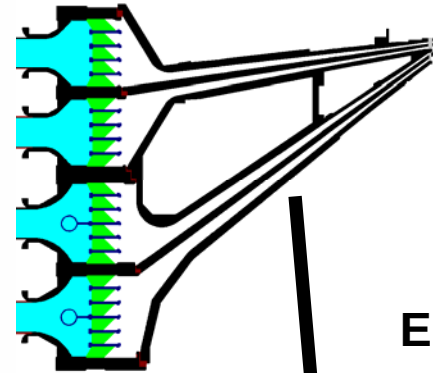
$$R = \frac{Z_f}{\alpha} \sqrt{\frac{I_{up} + I_{down}}{I_{up} - I_{down}}}$$

Simplified convolute model is fast to run with MHD

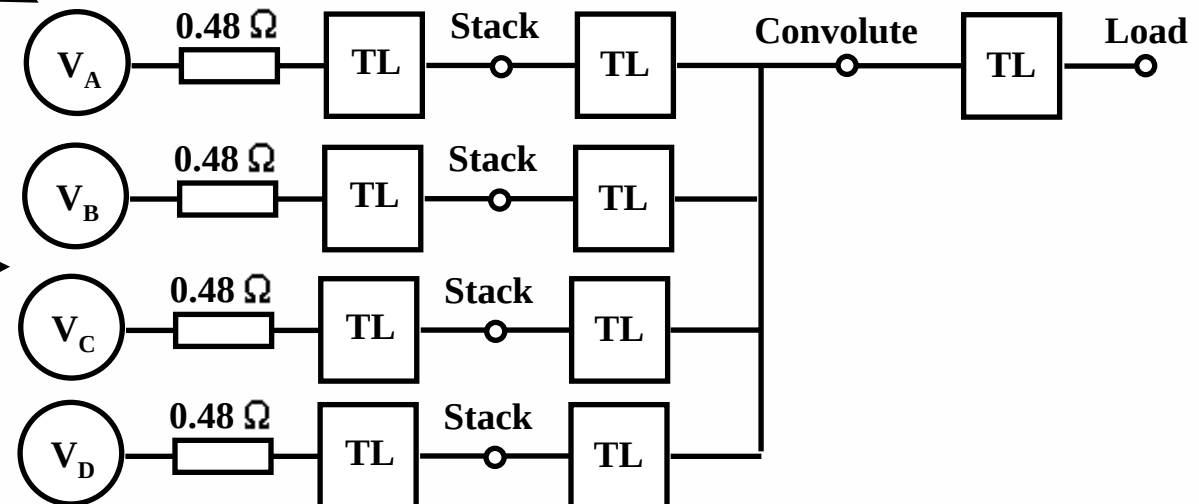
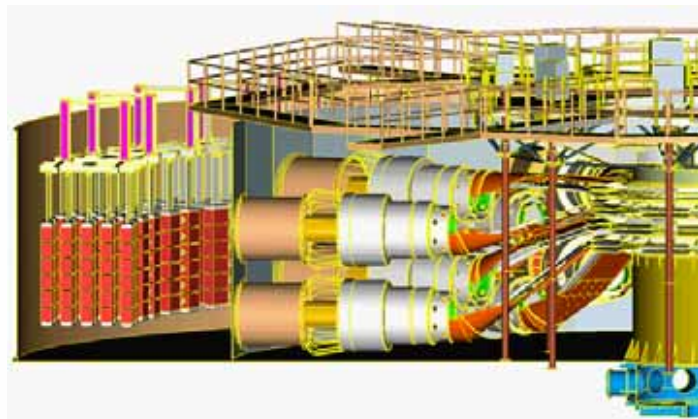
Simple circuit replaced by 4 line equivalent

Reconstructed
from stack
measurements

Constant
impedance water
line



EM calc.



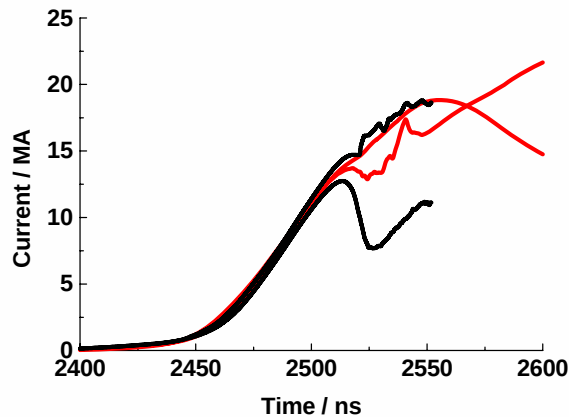
Circuit parameters calculated from hardware and measurements – main unknown is the cathode plasma expansion velocity

Mass scan assuming cathode plasma expansion rate of 7 cm / micro s

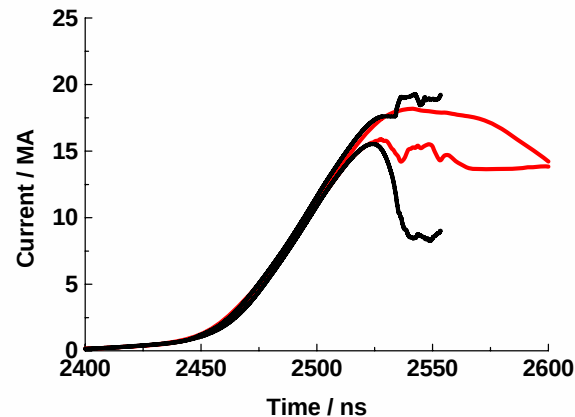


— Experiment — Simulation

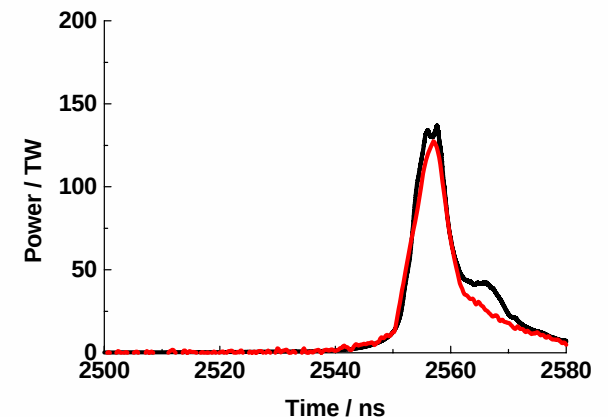
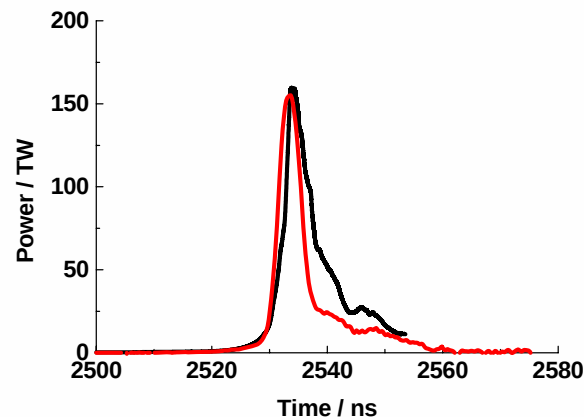
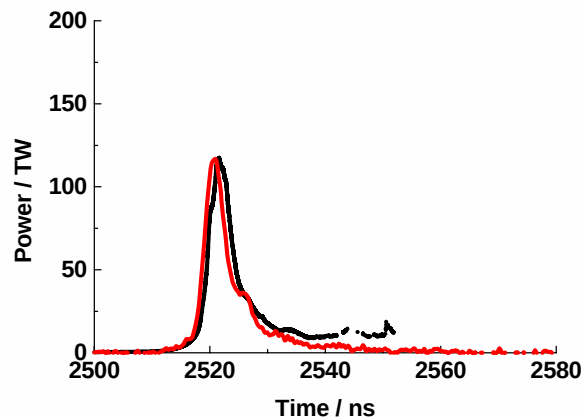
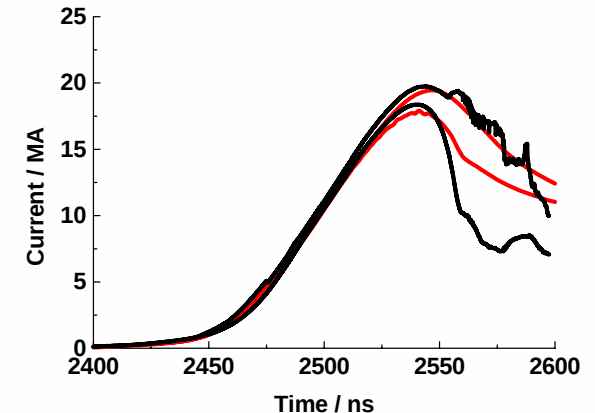
Z shot 1233



Z shot 1735



Z shot 1469

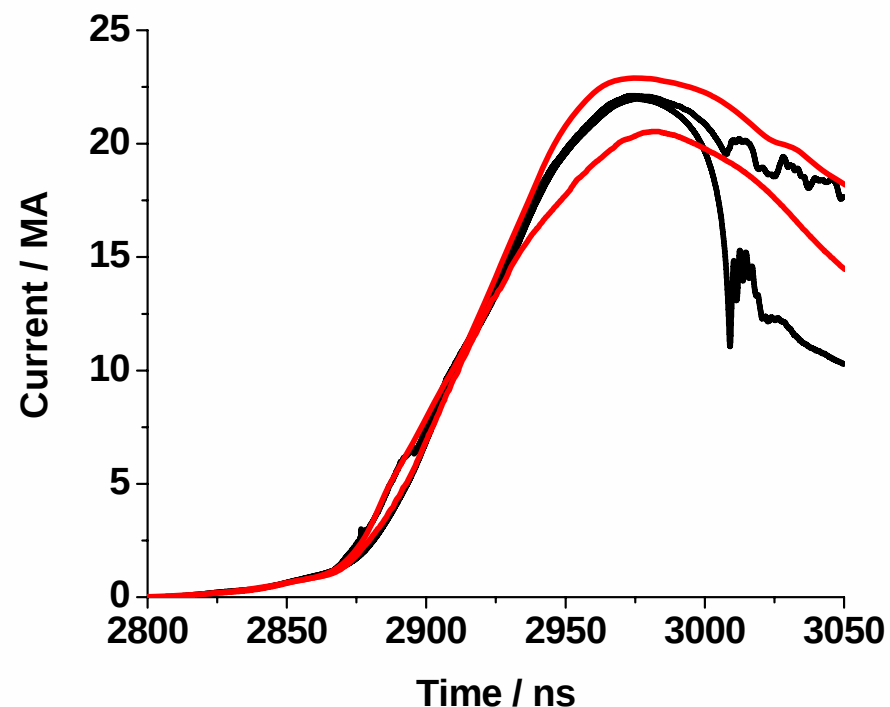
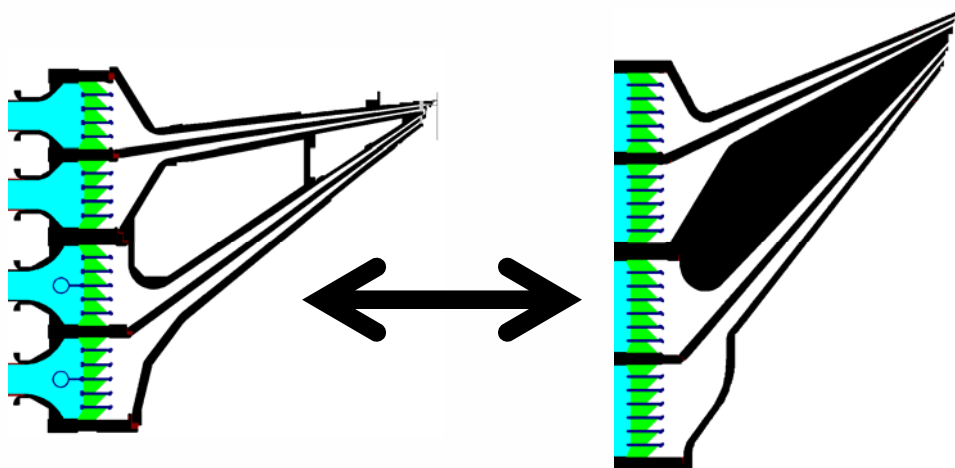


Good agreement but cathode plasma expansion velocity a bit high. Should perhaps be nearer 2.5 – 3 cm / micro s



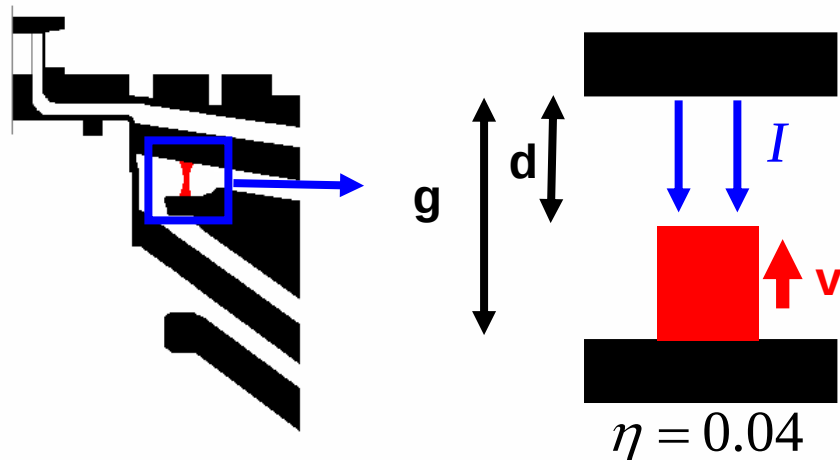
Electron flow insufficient to explain ZR shot 1787 (19.5mg single array) ZR data M. Jones

Swap out hardware in the
code for ZR and
recalculate voltage
source from stack
measurements taken
back through a constant
impedance water line





Invoke resistive short closing at 20 cm / micro s to recover correct circuit behavior and x-ray pulse



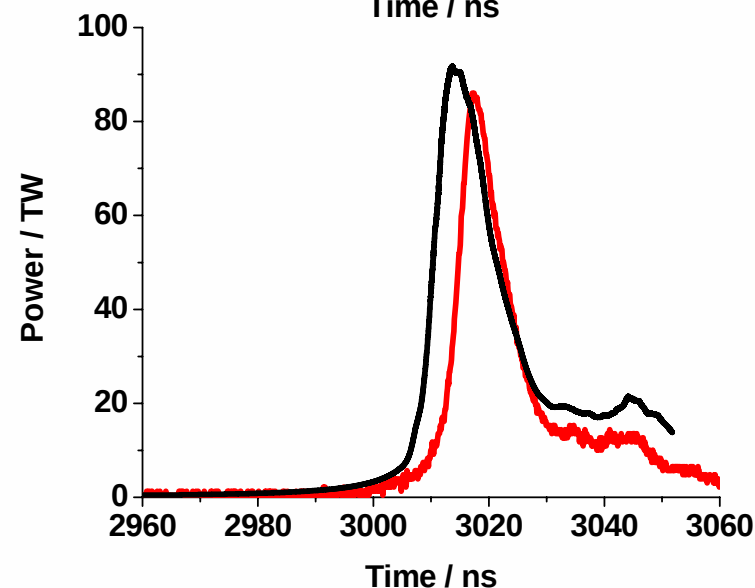
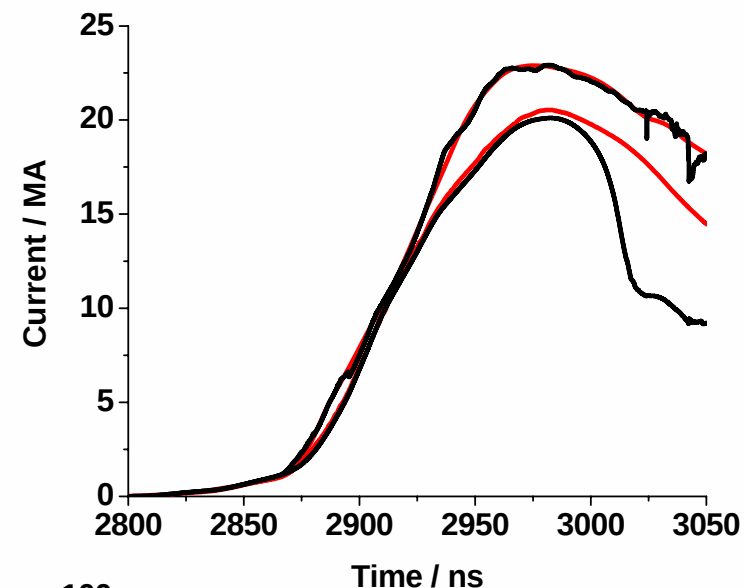
$$I = \frac{AkV^{1.5}}{d^2}$$

$$R = \frac{d^2}{Ak\sqrt{V}} + \frac{\eta(g-d)}{A}$$

If electron flow current deposited into anode heats surface sufficiently a plasma forms.

Electron flow calculations by T.Pointon indicate this null has the largest area and is most rapidly heated.

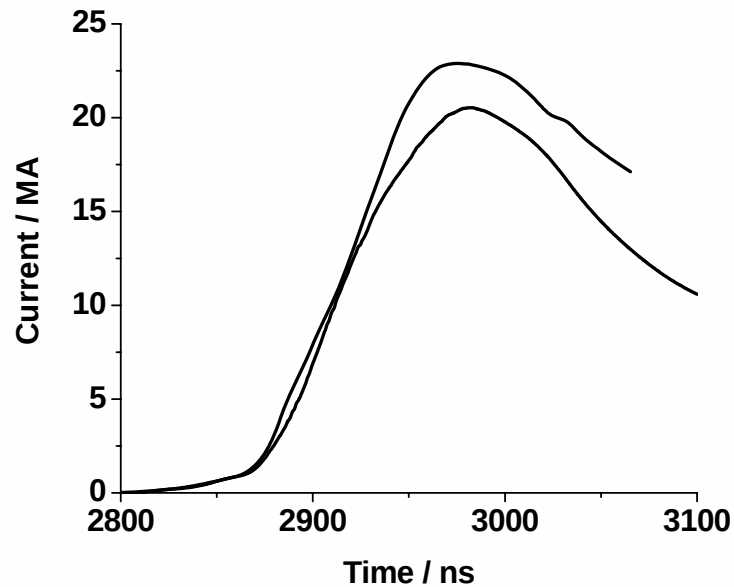
Circuit element just describes a plasma closing a gap – would be equivalent to cathode plasma expansion described by D.Rose last weeks seminar



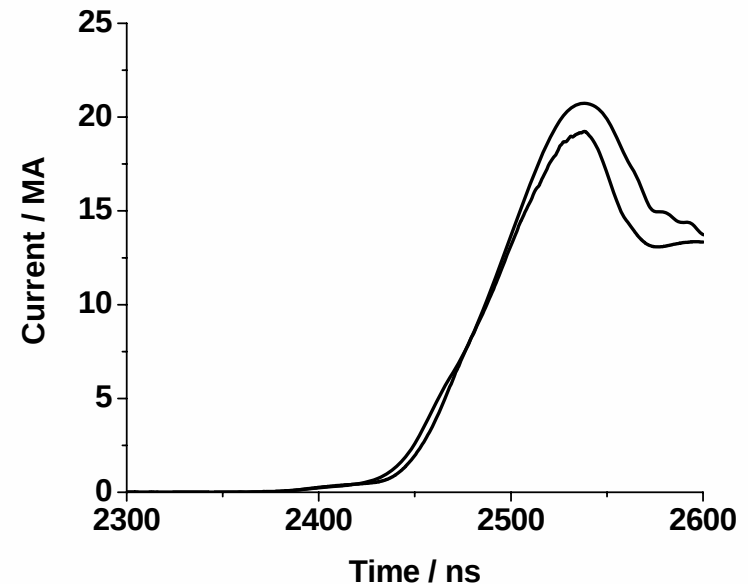


Behavior of currents qualitatively the same for ZR and Z

Z shot 1787 (19.5 mg ZR)



Z shot 1097 (6 mg Z)



Re-tune ZR shorting model for Z

ZR

Expansion velocity 20cm/ μ s

Effective area 15cm²

Z

Expansion velocity 17cm/ μ s

Effective area 5cm²

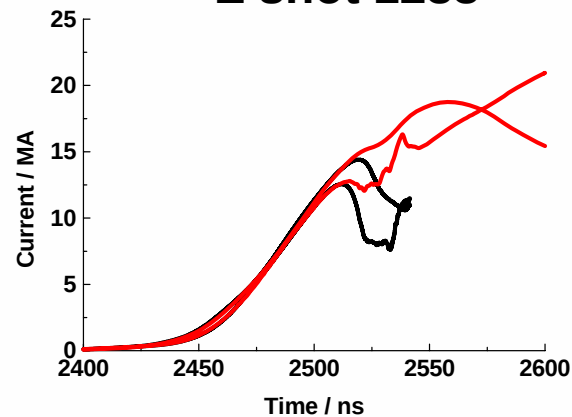
Can put cathode
plasma
expansion
velocity back to
2.5 cm/ μ s



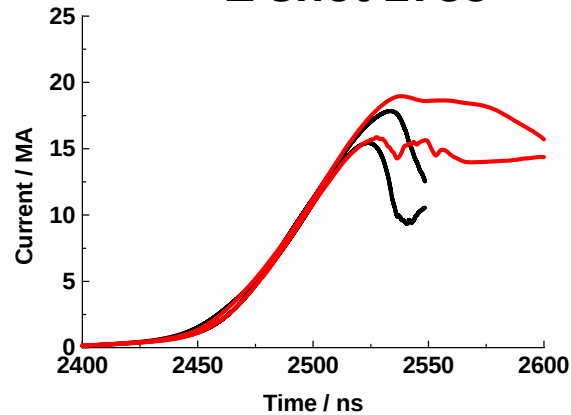
Retain good agreement for mass scan

— Experiment — Simulation

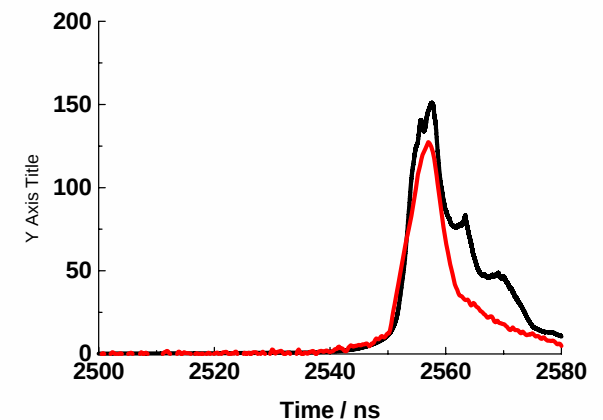
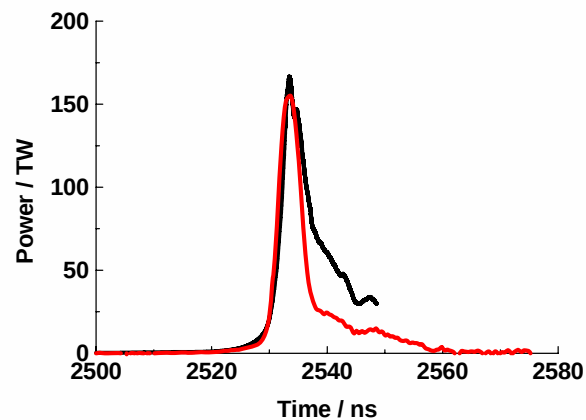
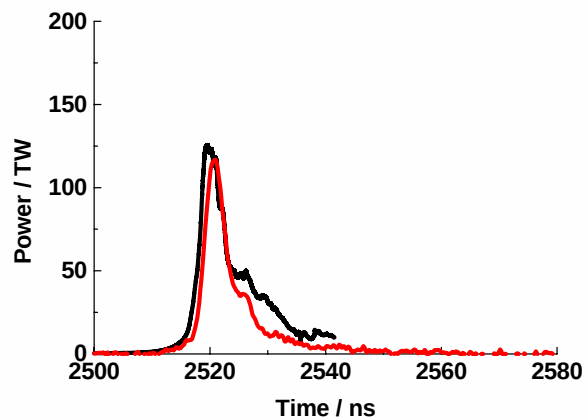
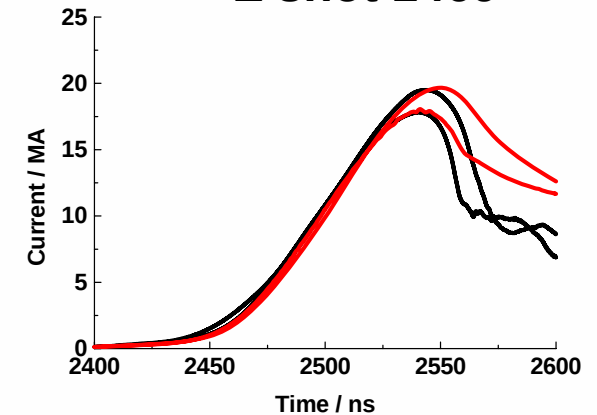
Z shot 1233



Z shot 1735



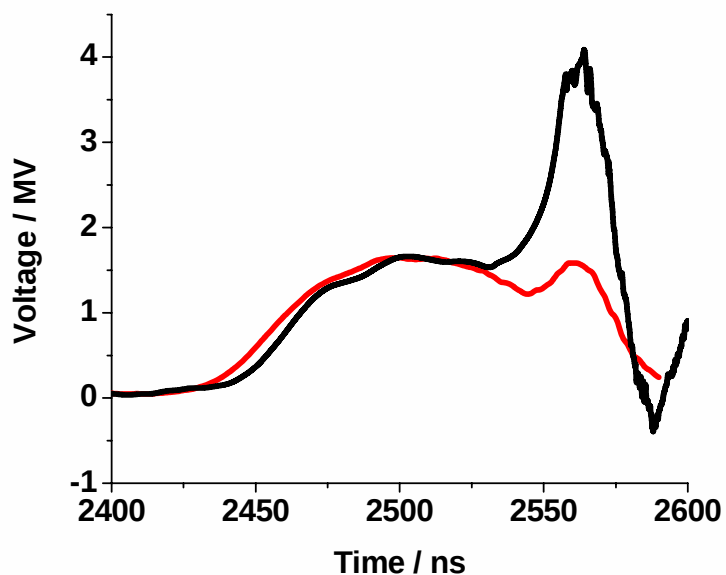
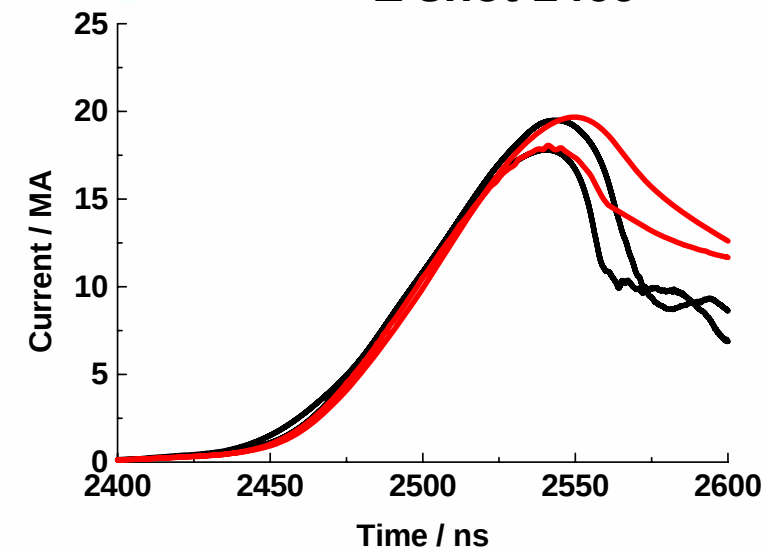
Z shot 1469





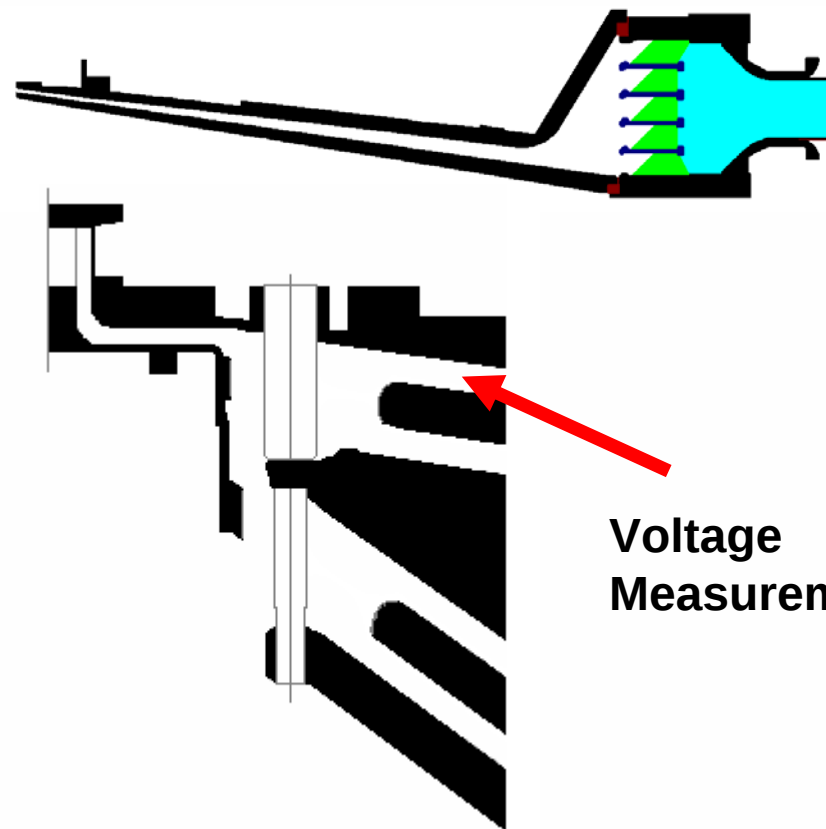
Can Compare to Convolute Voltage Measurement

Z shot 1469



— Experiment — Simulation

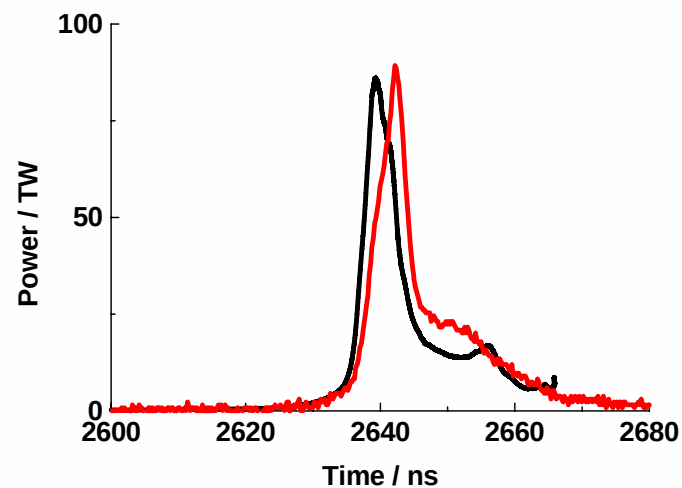
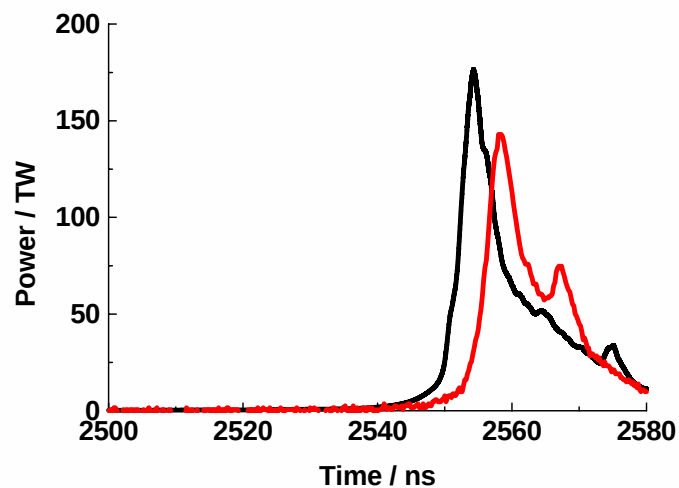
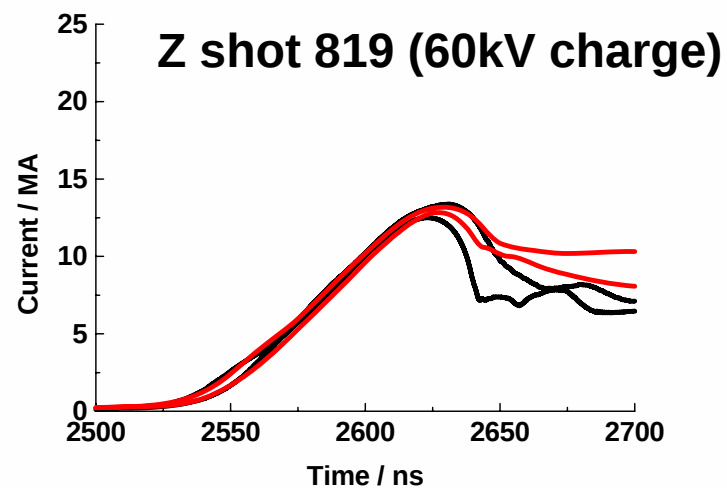
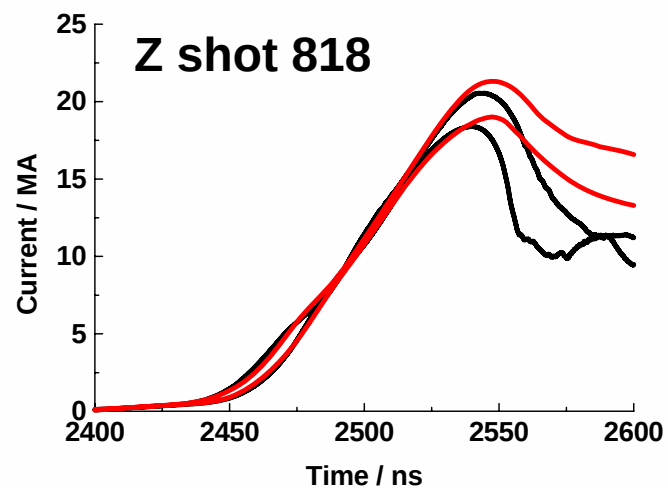
Translate stack measurements forward on A level to get convolute voltage



Reasonable agreement for Stygar current scan



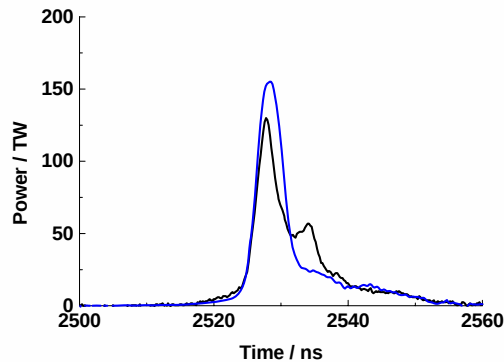
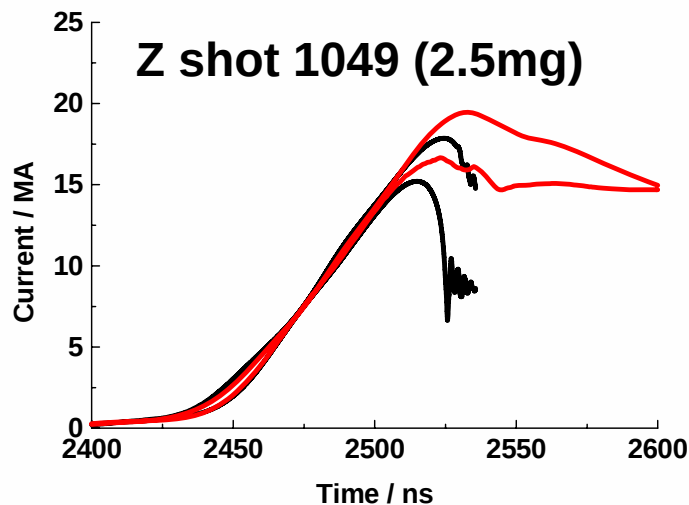
— Experiment — Simulation



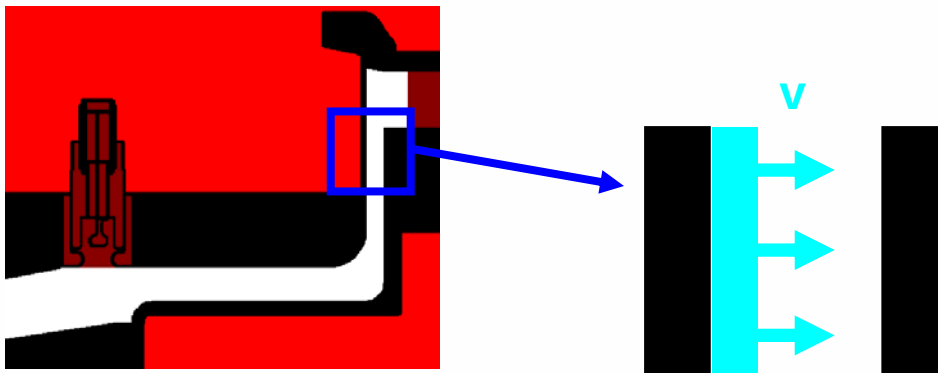
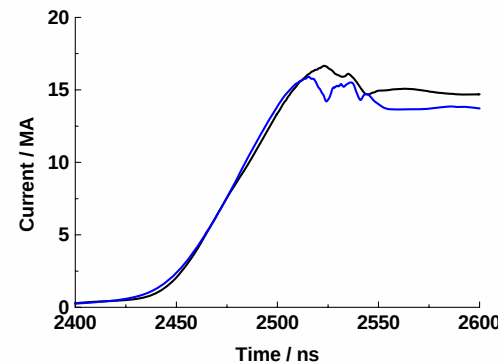
Simulated currents low for smaller AK gap of high L mass scan



— Experiment — Simulation



Z shot 1049
Z shot 1735

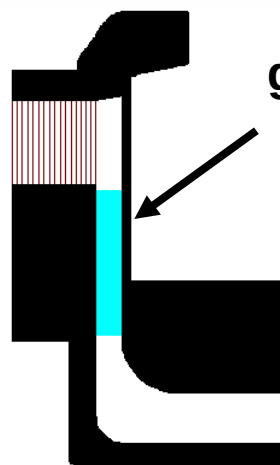
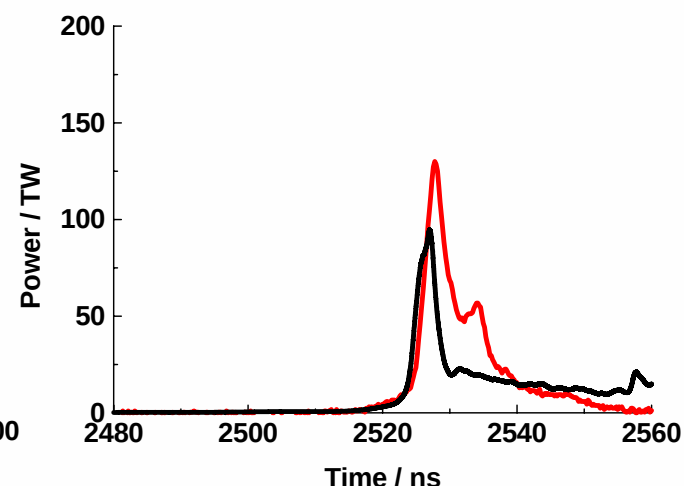
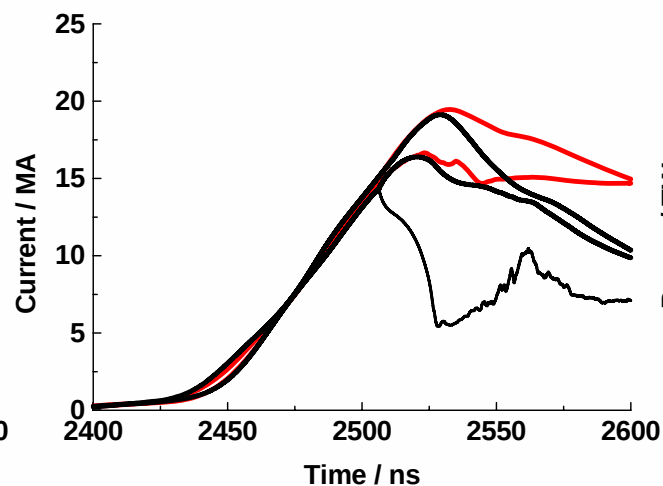
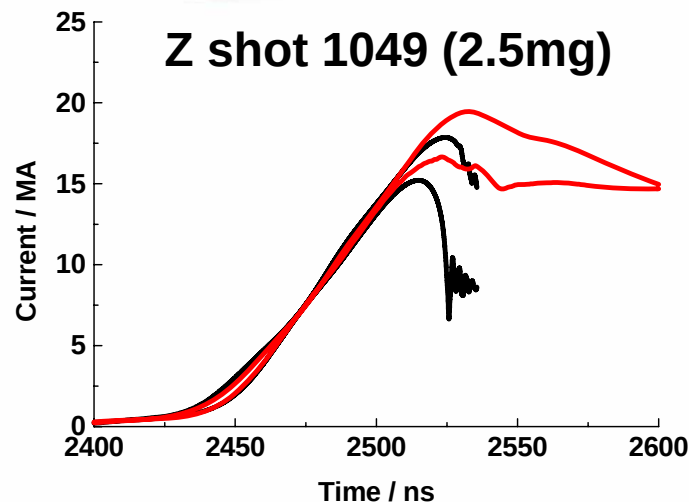


If we assume cathode plasma starts at 250 kV/cm and expands at 2.5cm/ μ s, then it is able to close 3mm AK gap before peak current for 2.5mg array implosion.



Resistive short in the feed gap recovers correct circuit behavior

— Experiment — Simulation



At point where AK gap closes we put a resistive plasma short into the feed

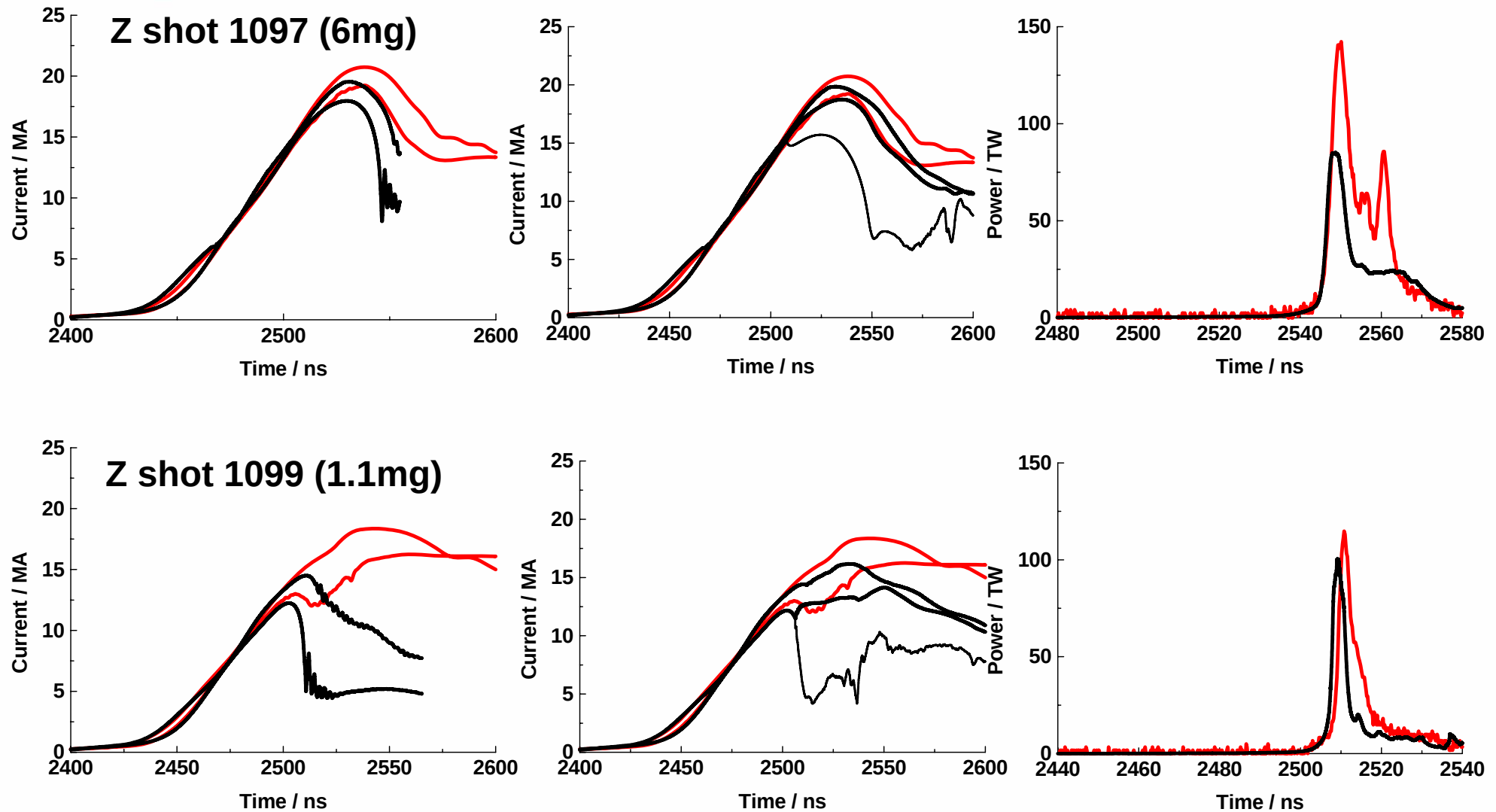
Can imagine mechanisms to raise resistivity after the gap shorts

Current limited by ion acoustic turbulence ?

$j \times B$ self clears feed by accelerating plasma ?

With more considered approach to shorting mechanism can probably recover agreement with x-ray pulse

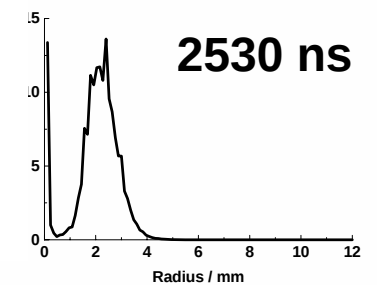
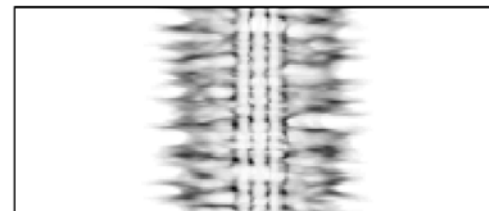
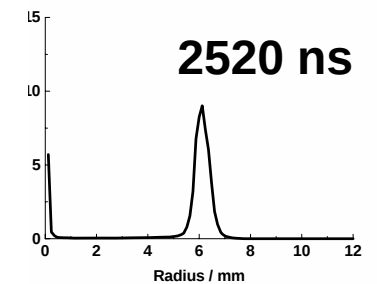
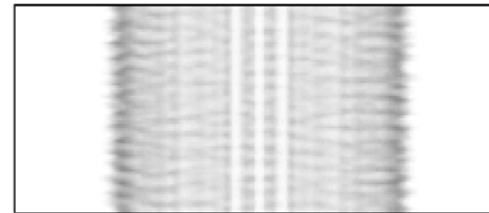
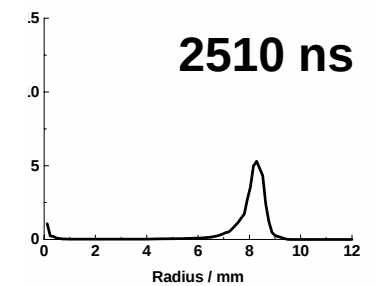
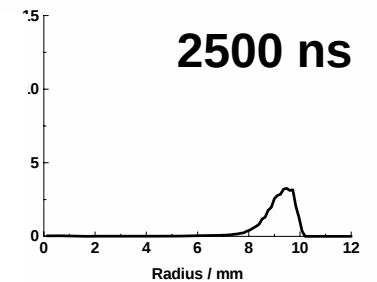
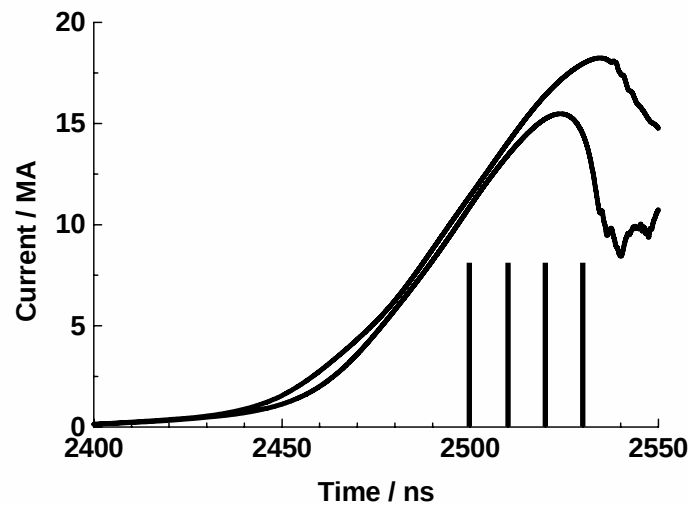
1.1 mg load is unaffected by the short in the feed





Density distribution for 2.5mg array implosion. Code results

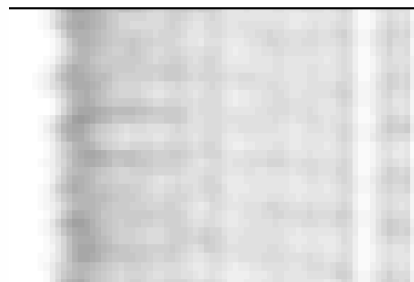
Load & MITL Currents



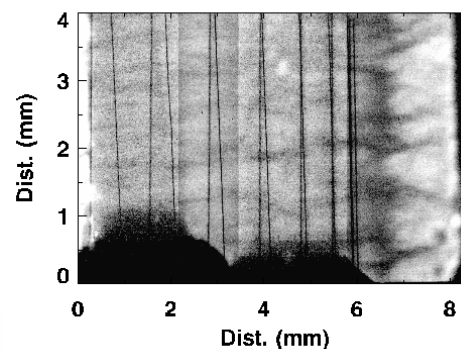
Good match to radiography measurement



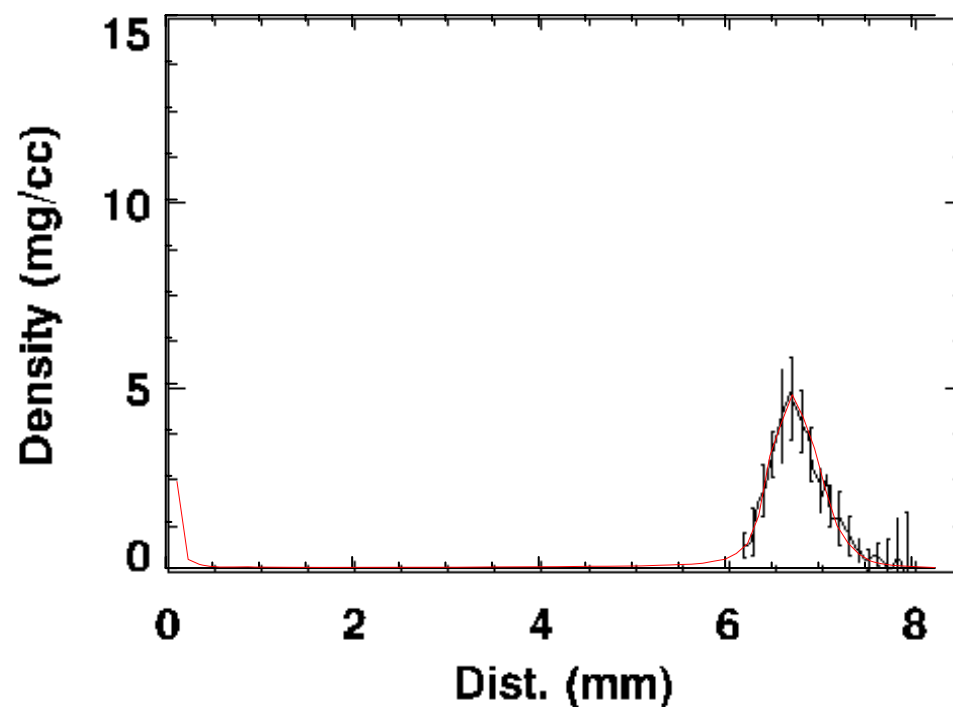
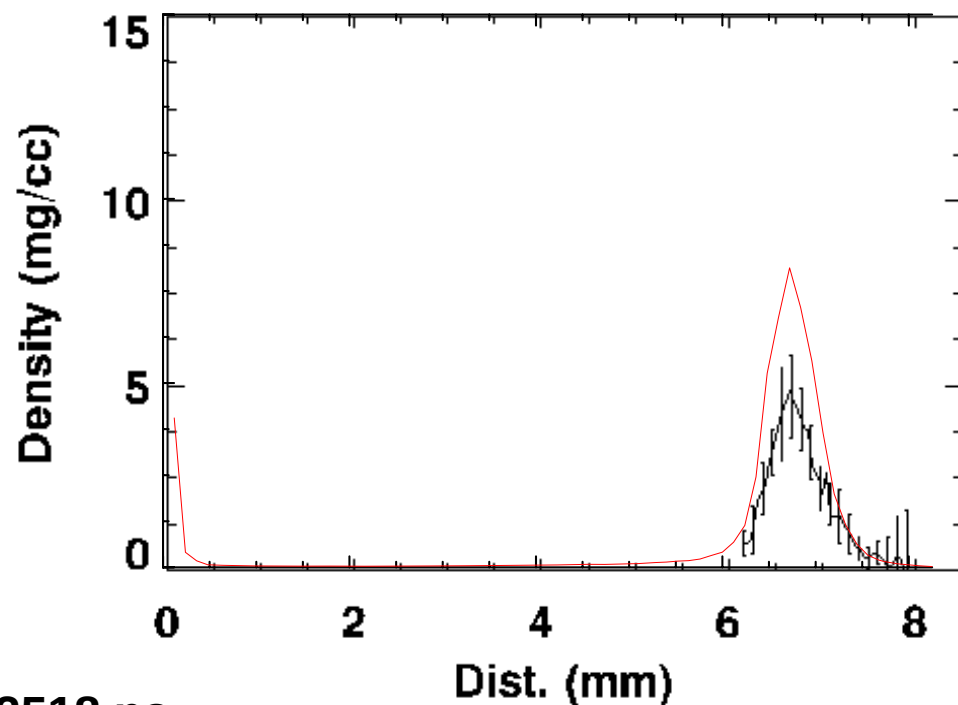
Simulation



Experiment



Simulation normalized to radiograph integrated mass of 1.4 mg



2518 ns

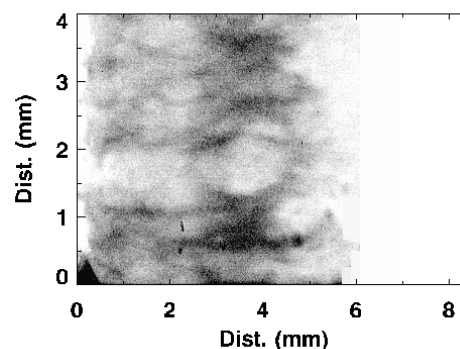
Not so good a match



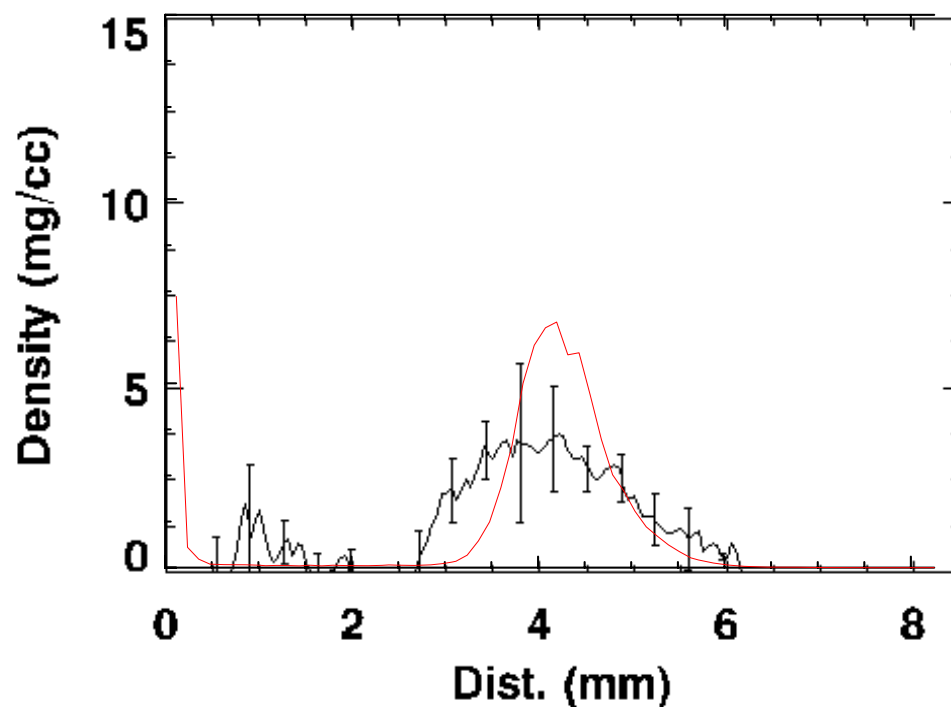
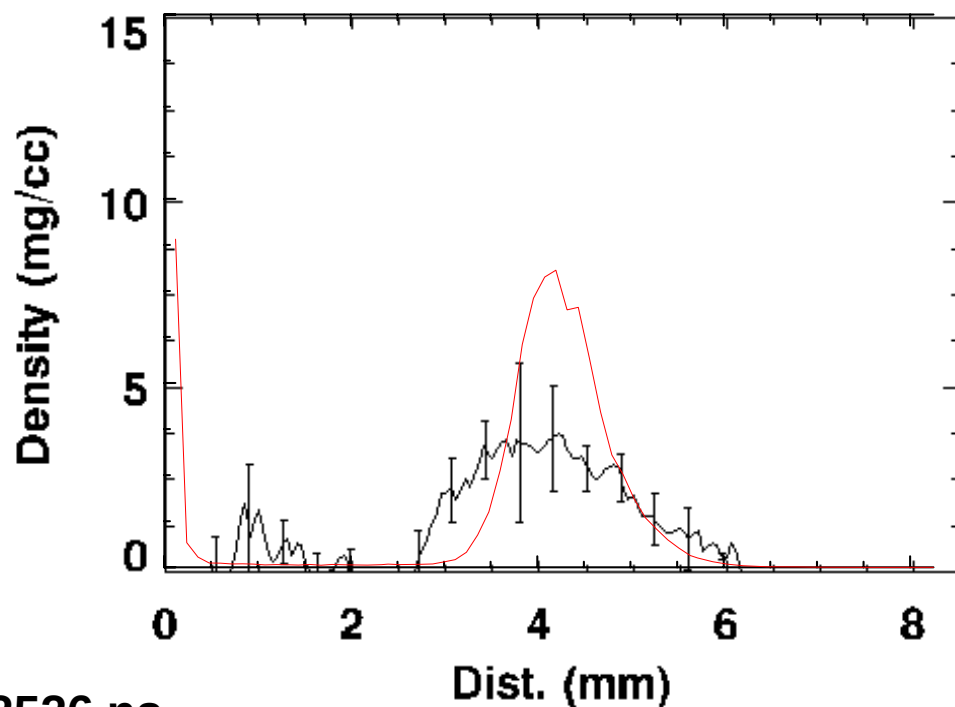
Simulation



Experiment



Simulation normalized to radiograph integrated mass of 2.0 mg



2526 ns

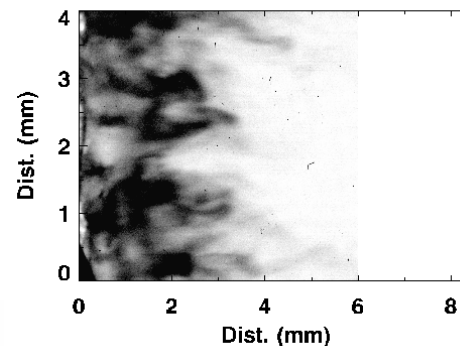


Good match to radiography measurement

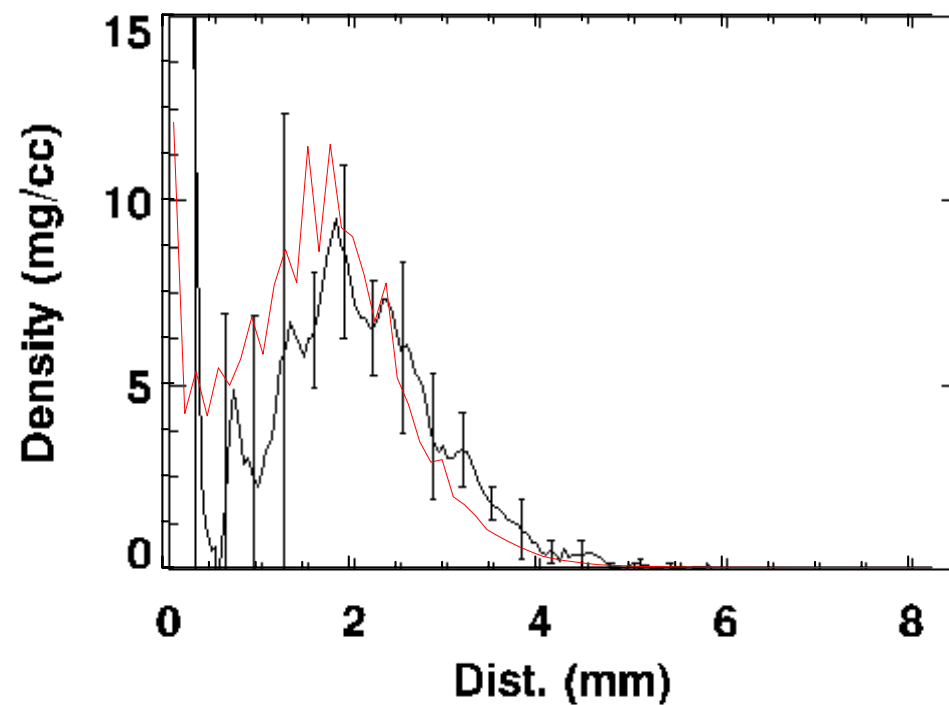
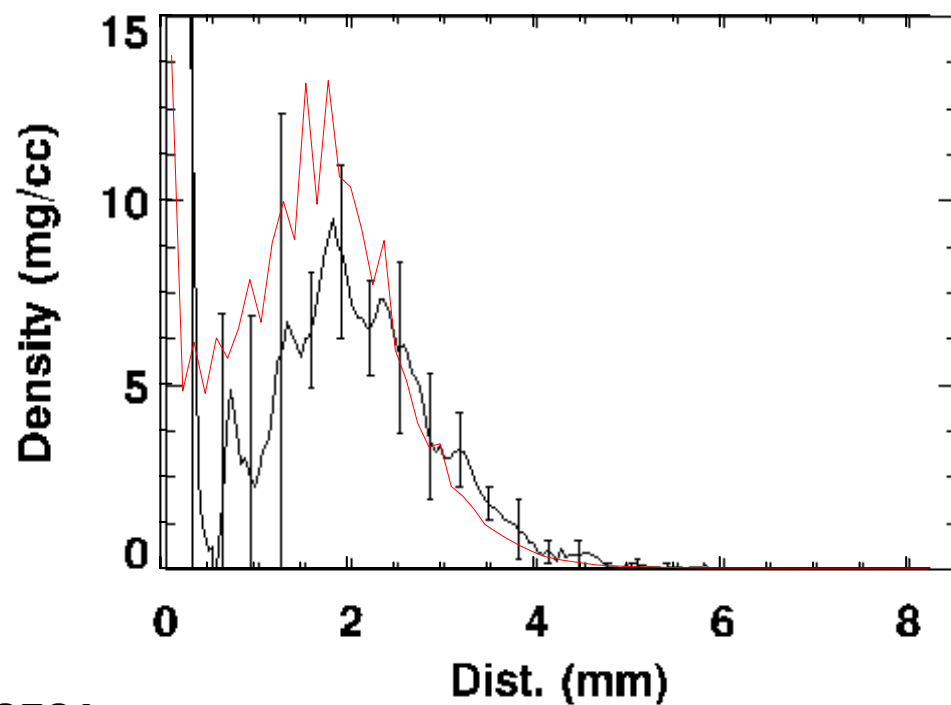
Simulation



Experiment



Simulation normalized to radiograph integrated mass of 2.1 mg

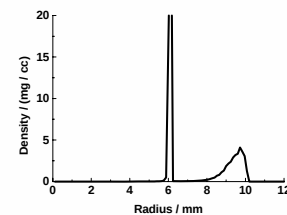
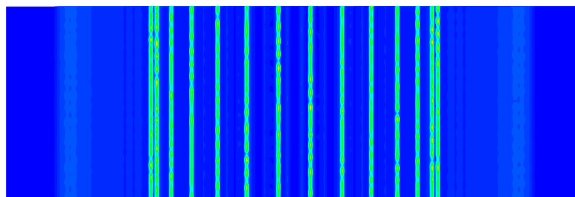


2531 ns

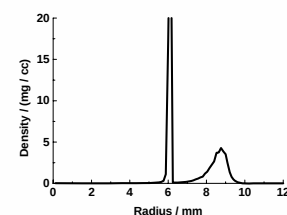
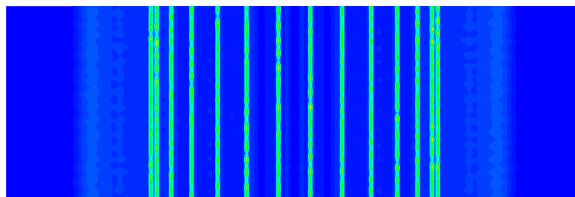


2.42 on 2.5 mg nested array

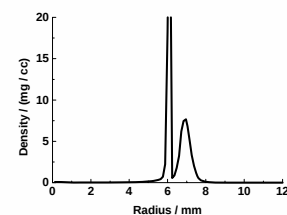
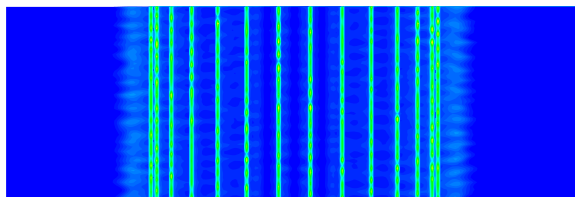
2500 ns



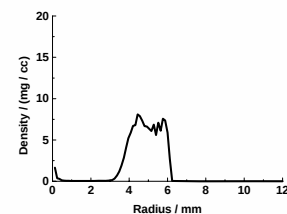
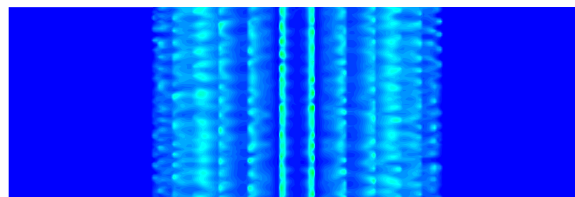
2510 ns



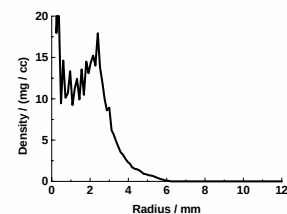
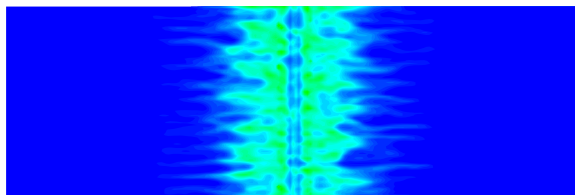
2520 ns



2530 ns



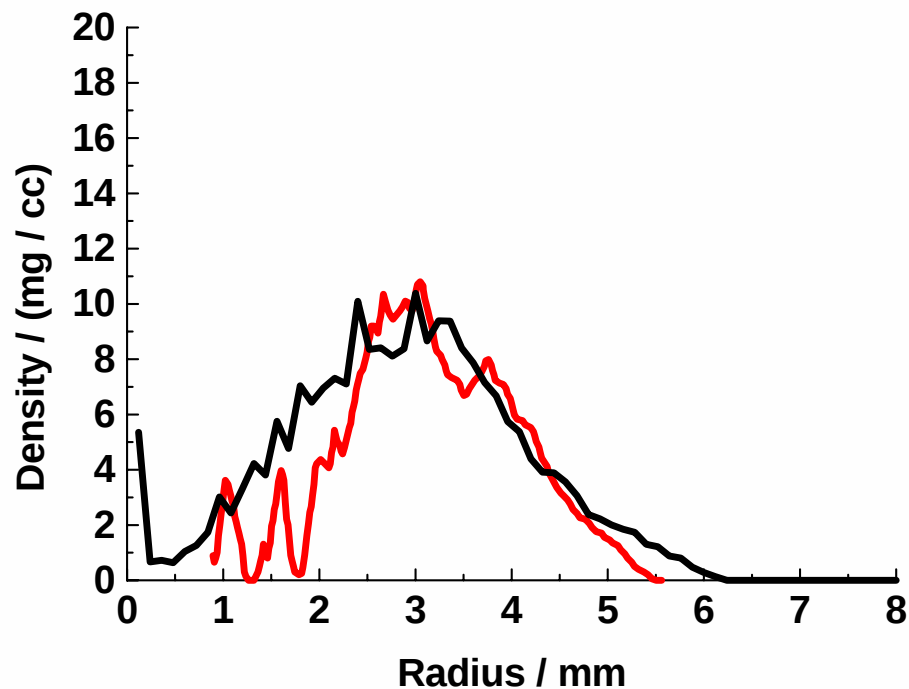
2540 ns



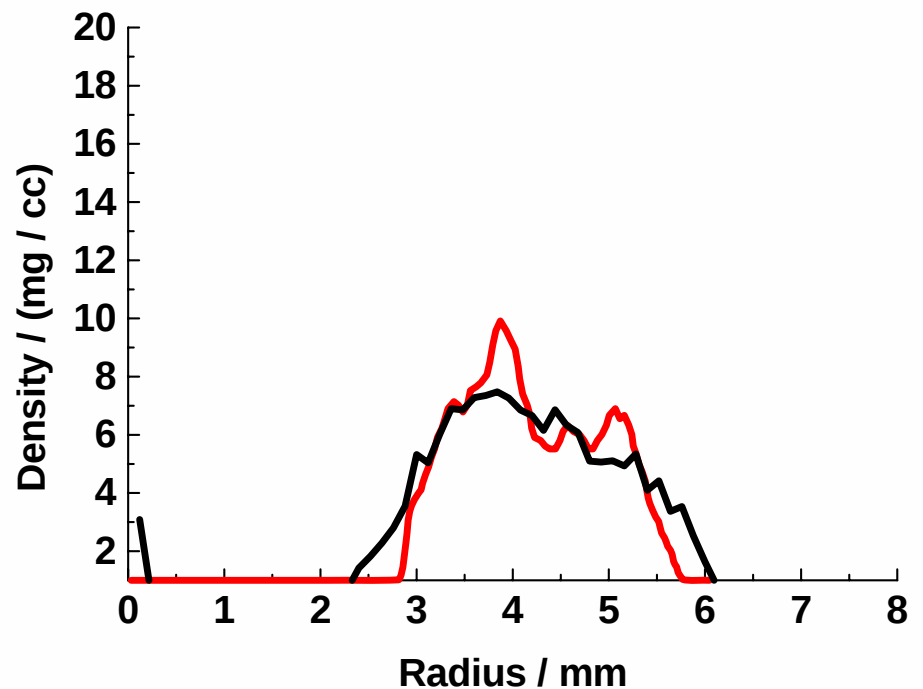


Good match to radiography measurement

— Experiment — Simulation



2537 ns

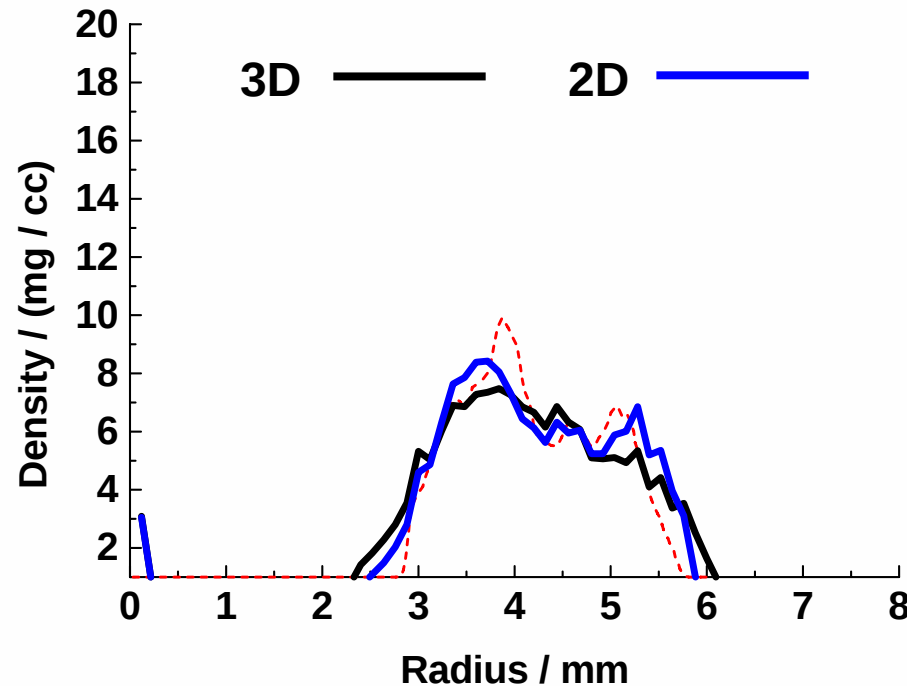


2533 ns

Mass distribution not a function of 3D perturbations, but later time evolution is

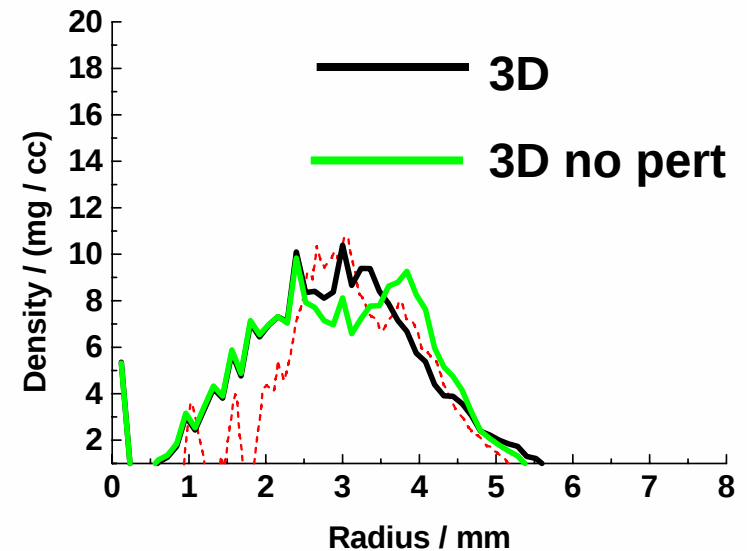
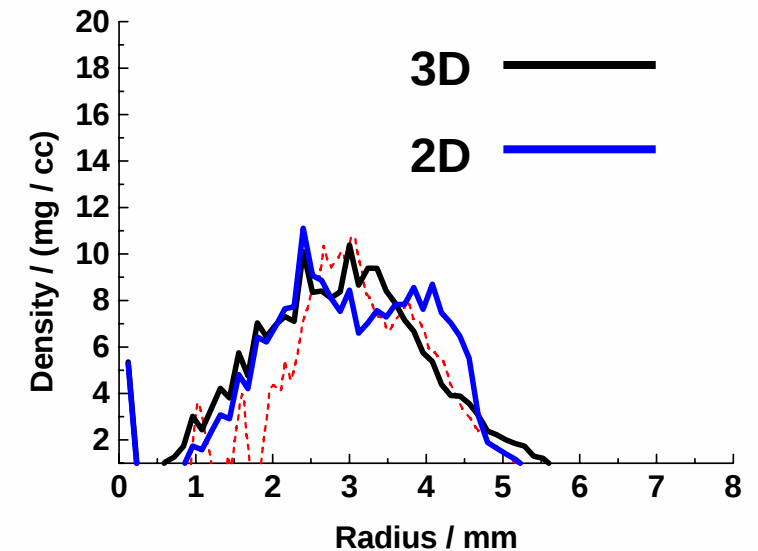


2533 ns



Large mass perturbation required on inner array to reproduce mass distribution

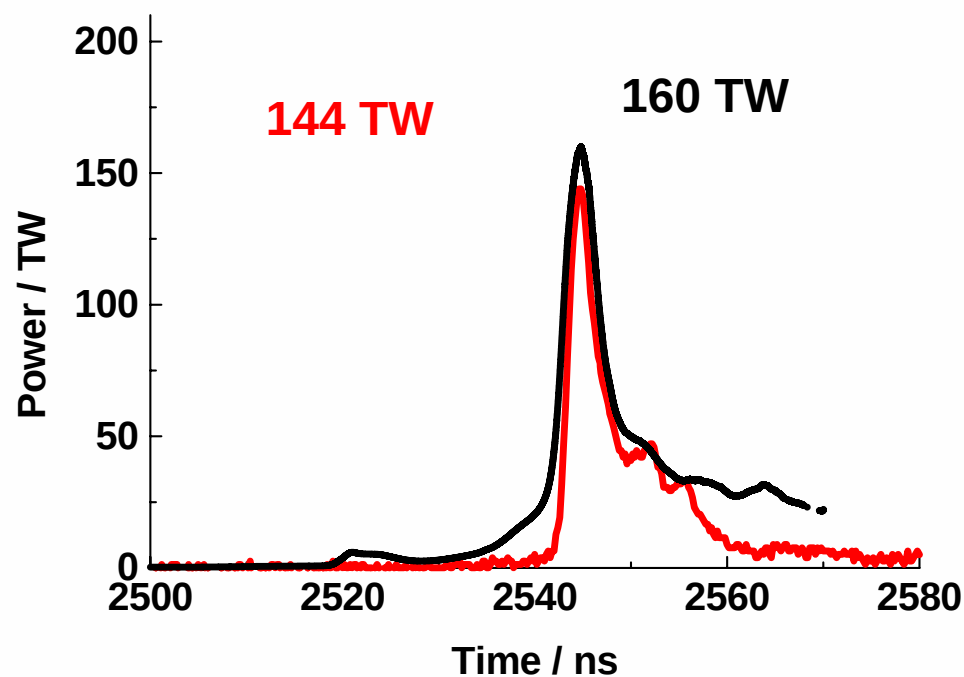
2537 ns



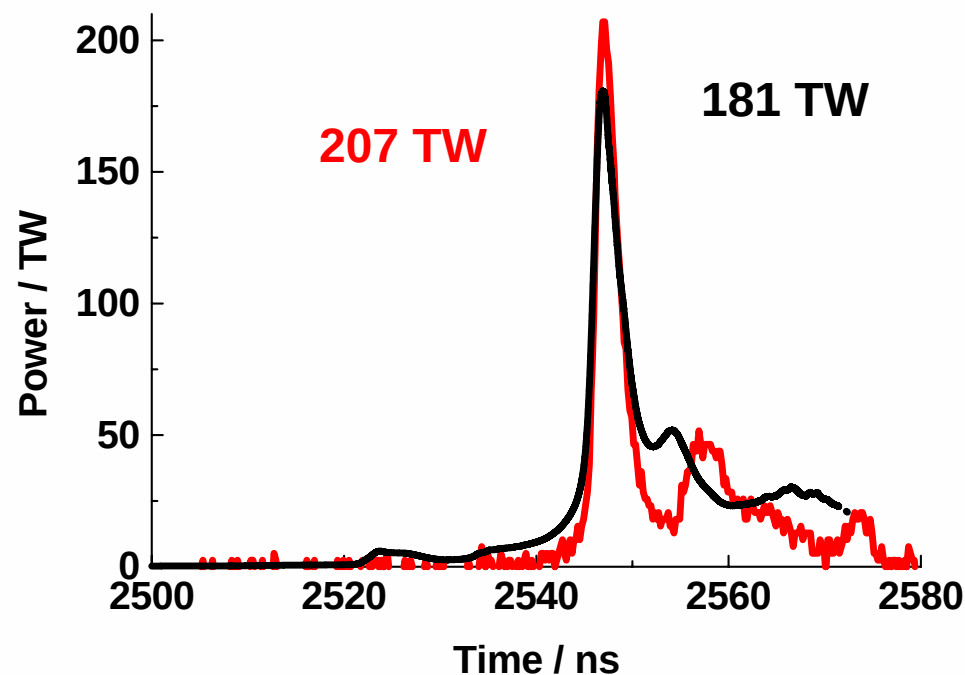
Good match to measure x-ray power with and without foam



No foam



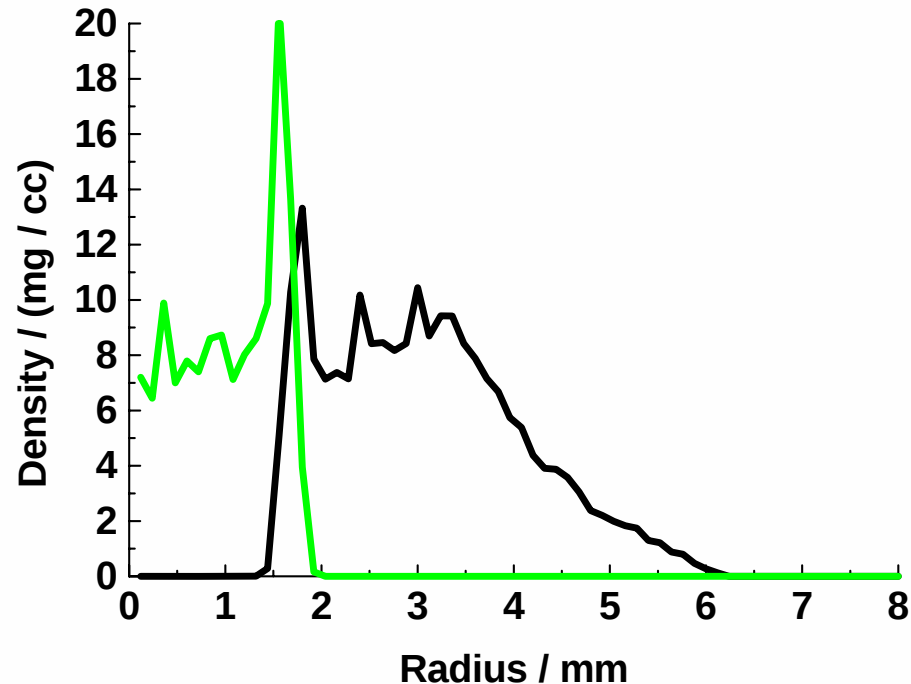
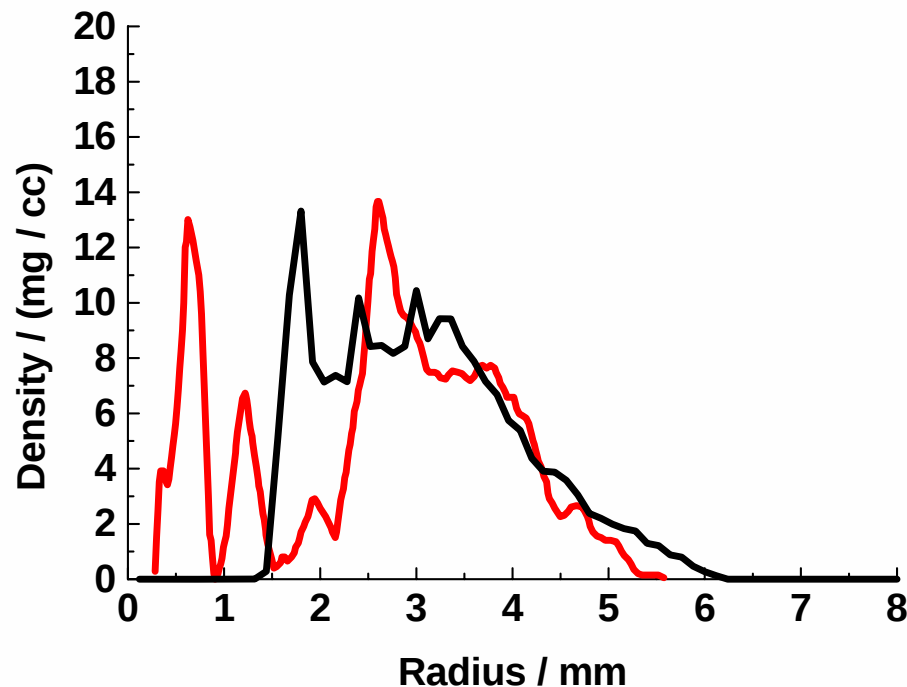
Foam



Experiment – foam raises power ~ 40 %

Simulation - foam raises power ~ 13 %

Foam acts to sharpen mass distribution. Not modeling radiation may be a problem



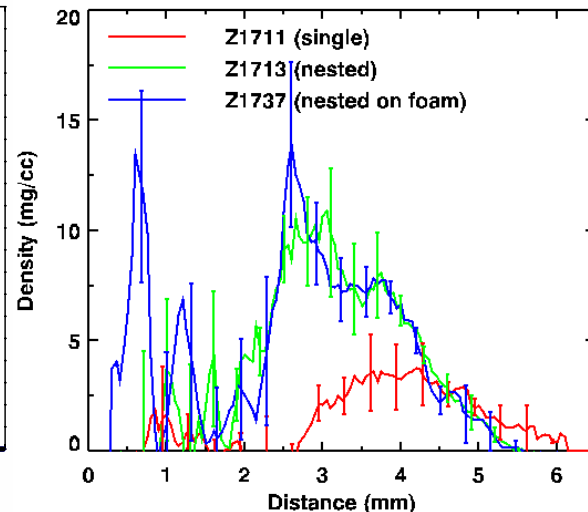
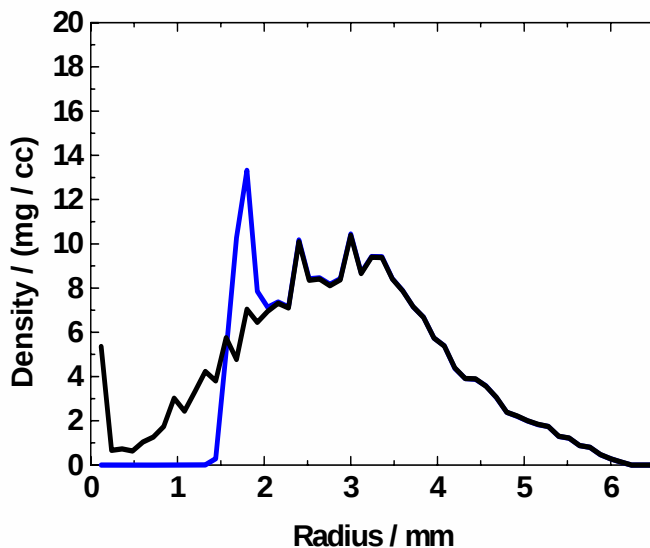
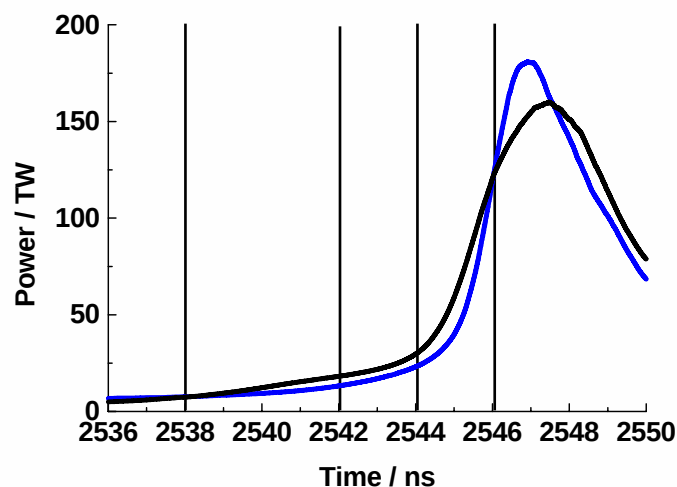
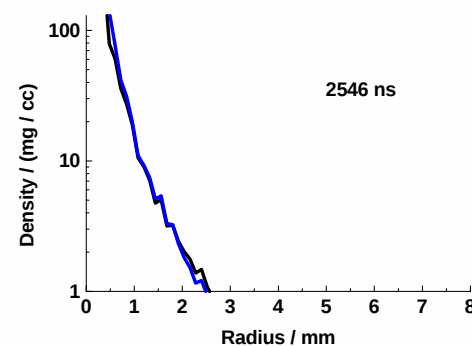
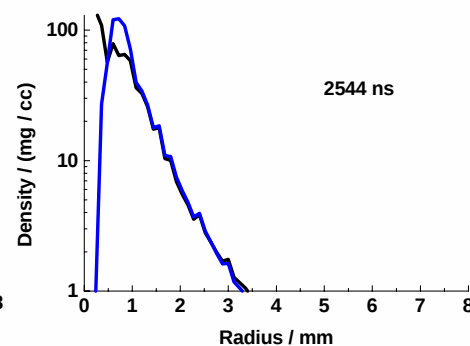
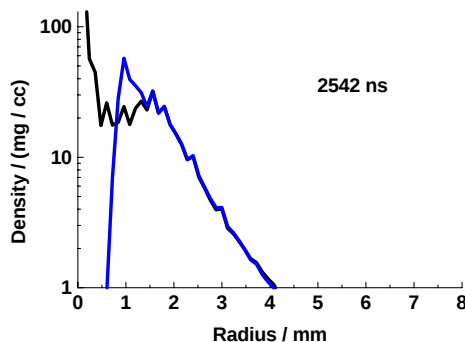
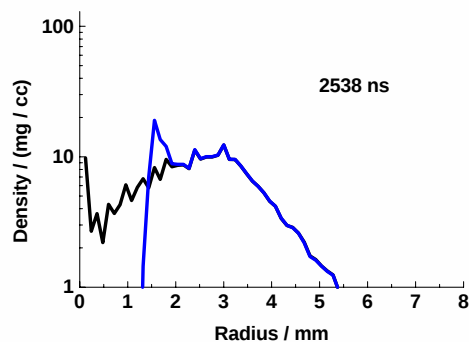
Mass profile has correct shape, but impact with foam appears to be at smaller radius than observed. Do we need to account for foam expansion ?

2537 ns



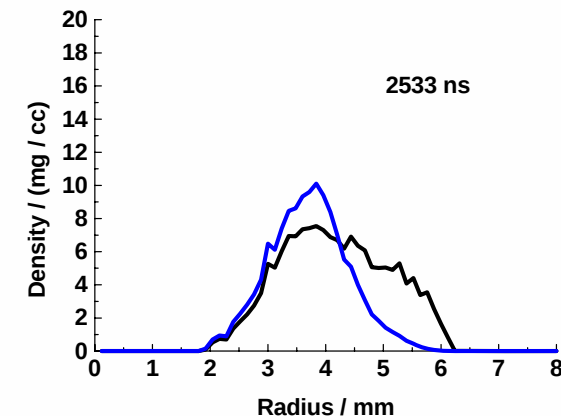
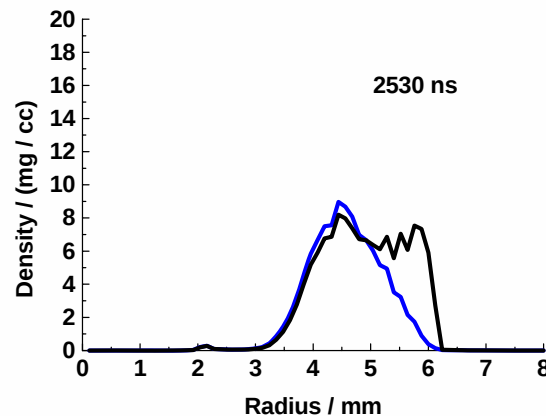
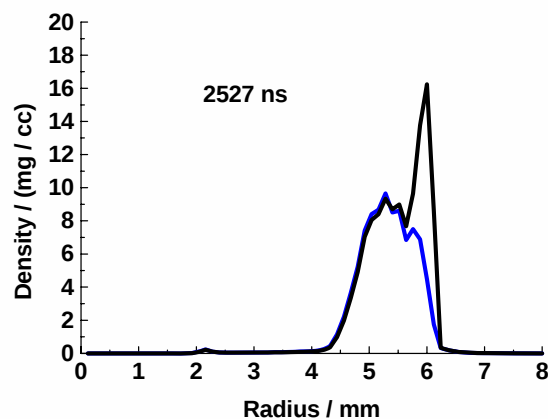
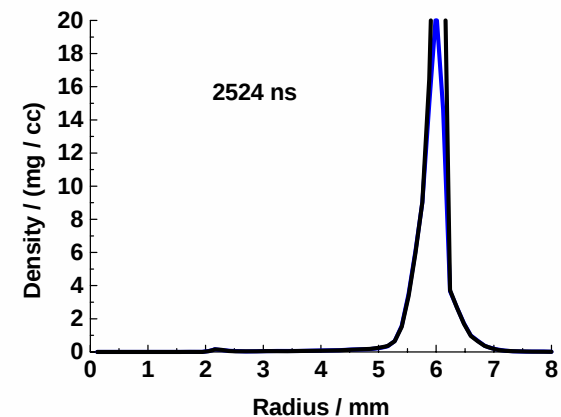
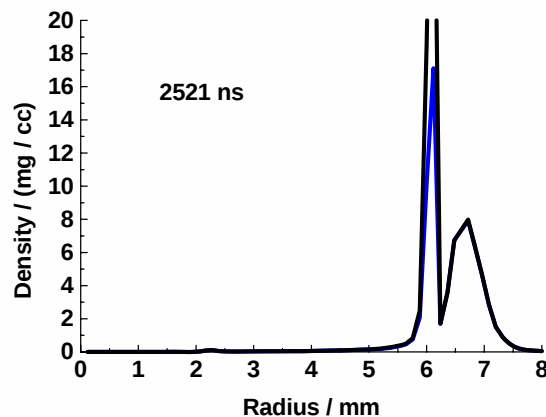
Narrower mass distribution results in sharper x-ray power rise and higher peak power

Comparison of simulated mass distribution with and without foam – mass profile steepens

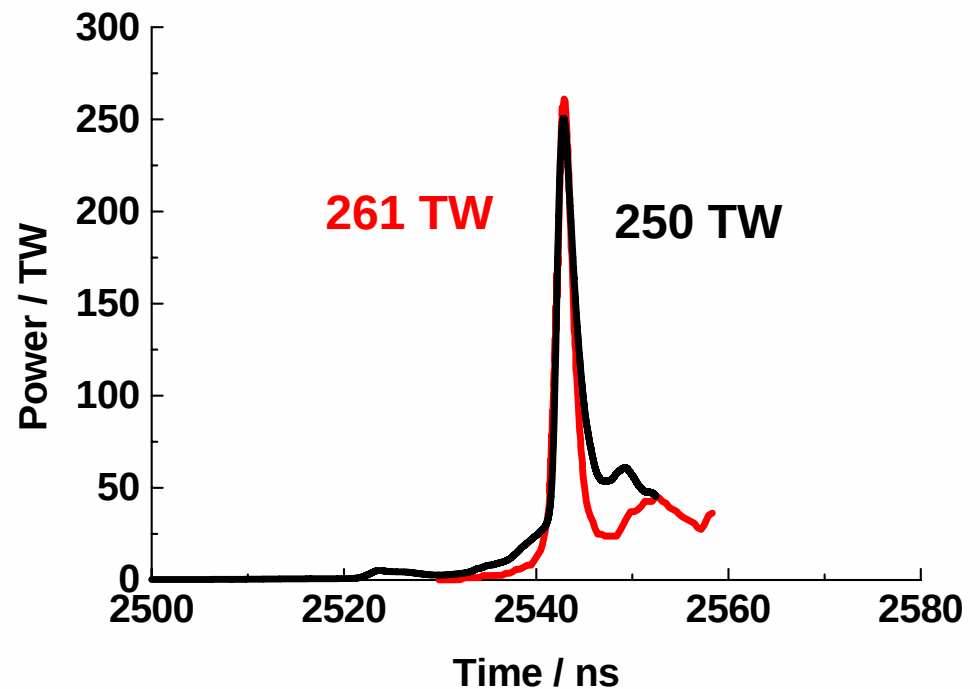
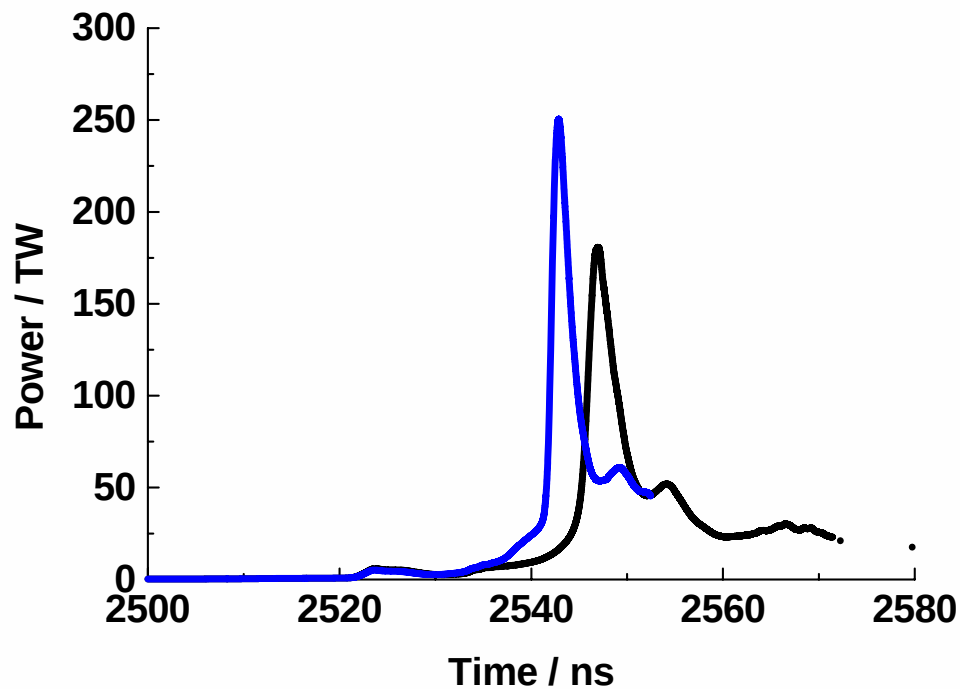


Lighter inner array creates narrower mass distribution at nested interaction point

Comparison of foam runs for different inner masses – mass profile steepens at nested interaction point



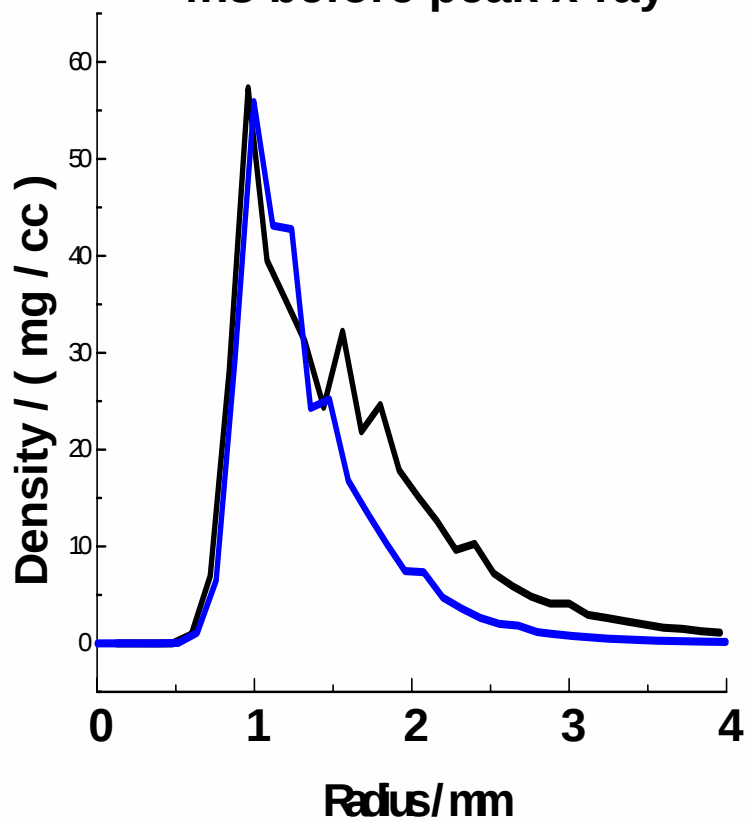
Better improvement can be obtained with lighter inner array mass (1.3 mg inner array)



Narrower mass distribution results in higher peak power

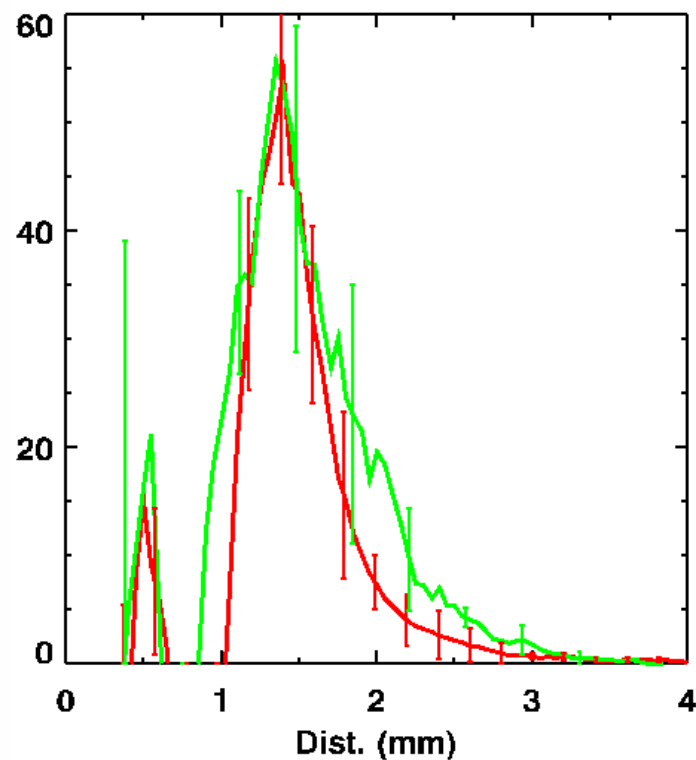


Density distribution from code ~
4ns before peak x-ray



- 2.5 inner
- 1.3 inner (translated 0.5mm)

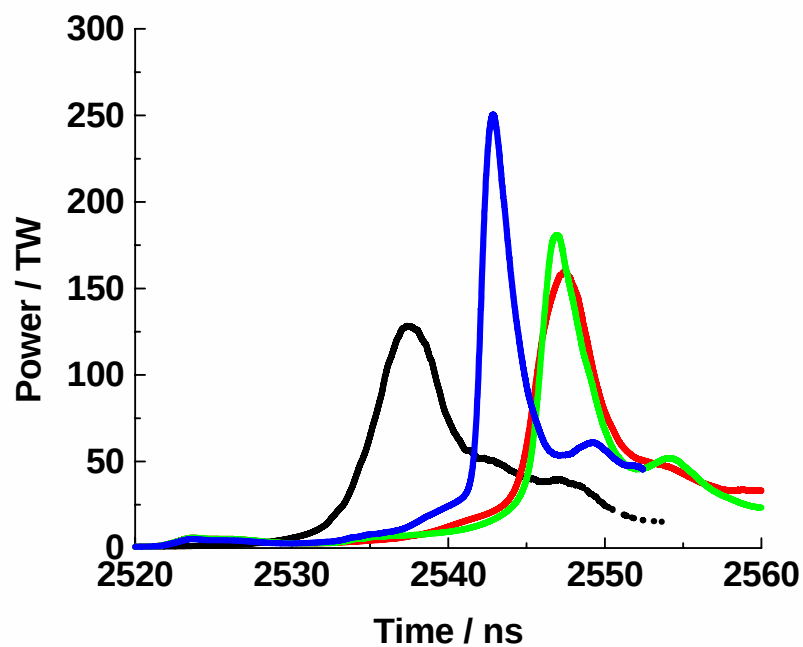
Experimental Density
distributions



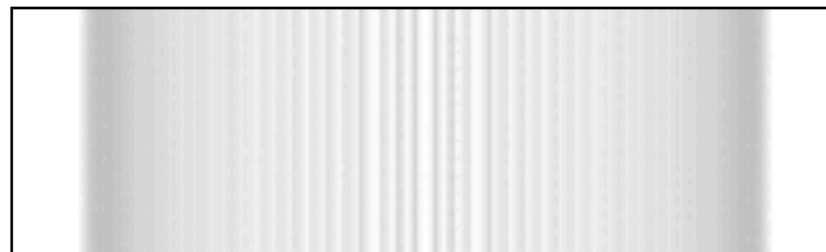
Experimental
Radiography



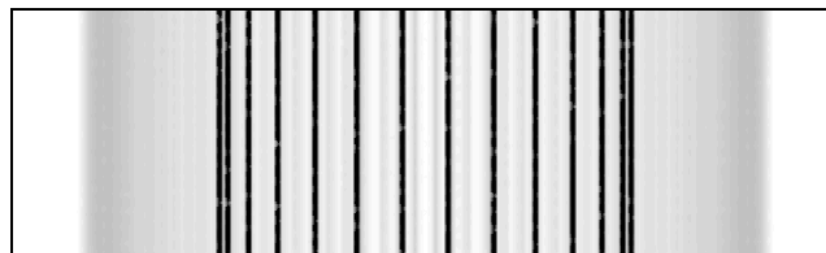
Simulation Results



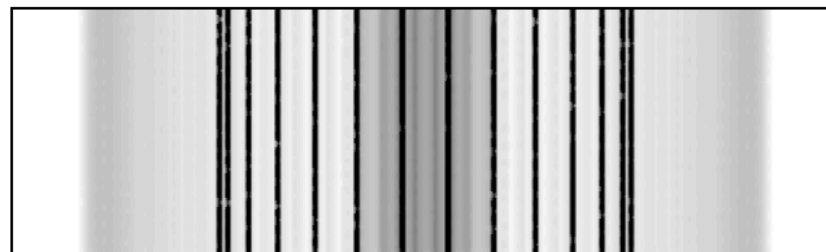
2.5mg



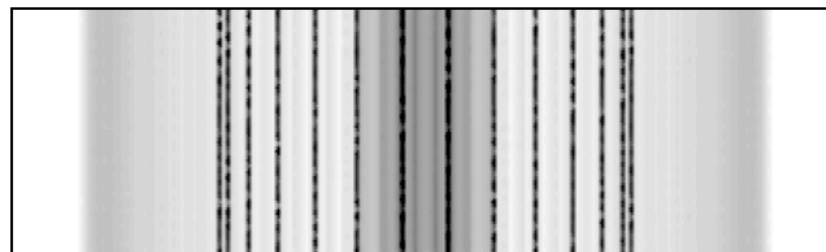
2.5mg
on
2.5mg



2.5mg
on
2.5mg
on foam



2.5mg
on
1.3mg
on foam





Summary

- Using the same model we are able to consistently get good agreement between simulation and experiment for single arrays and nested arrays on Z
- Simulations starting to give good quantitative agreement. We are able to reasonably and simultaneously match circuit behavior, x-ray pulse and mass distributions. With more benchmarking against ZR could be used as a useful design tool.
- More complete circuit model is now being used, but it contains free parameters that need to be better justified or calculated from first principles
- Possible gap closure issues for small AK gaps that need to be kept in mind, although more testing / data mining needed to be certain.